# INTERNATIONAL STANDARD

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# Fatigue test method for transmission precision roller chains

Méthode d'essai de fatigue pour chaînes de transmission de précision à rouleaux



#### ISO 15654:2004(E)

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## **Contents** Page

Forewo	ord	. iv
1	Scope	1
2	Normative references	1
3	Symbols	2
4	Principle	3
5 5.1 5.2	Apparatus Testing machine Test fixtures	3
6	Test specimens	4
7 7.1 7.2 7.3	Test procedure	4 6
8 8.1 8.2 8.3	Staircase test data analysis  Data  Plotting staircase data  Statistical calculations	8 8
9 9.1 9.2 9.3	Report of test results	9 9
Annex	A (informative) Survival test with abridged Probit analysis	11
Annex	B (informative) Combined test method	15
Annex	C (informative) Justification for adding one step to fatigue limit in staircase analysis	21
Annex	D (informative) Adding an additional "phantom" point at the end of staircase test	24
Annex	E (informative) Reporting fatigue test results	25
Annex	F (informative) Establishing chain application fatigue ratings	32
Annex	G (informative) Extrapolating fatigue strength from 3 × 10 <sup>6</sup> cycles to 10 <sup>7</sup> cycles	38
Annex	H (informative) Finite life testing and data analysis	42
Bibliog	ranhy	47

ISO 15654:2004(E)

#### **Foreword**

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 2.

The main task of technical committees is to prepare International Standards. Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75 % of the member bodies casting a vote.

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights.

ISO 15654 was prepared by Technical Committee ISO/TC 100, Chains and chain wheels for power transmission and conveyors.

## Fatigue test method for transmission precision roller chains

#### 1 Scope

This International Standard specifies an axial force fatigue test method for transmission roller chains, the tests being of the fluctuating tension type, carried out at room temperature in air, with the force applied along the longitudinal axis of the chain. It also specifies procedures for statistically analyzing the test results and gives formats and elements for presenting the results of fatigue tests and analyses.

#### 2 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 606, Short-pitch transmission precision roller and bush chains, attachments and associated chain sprockets

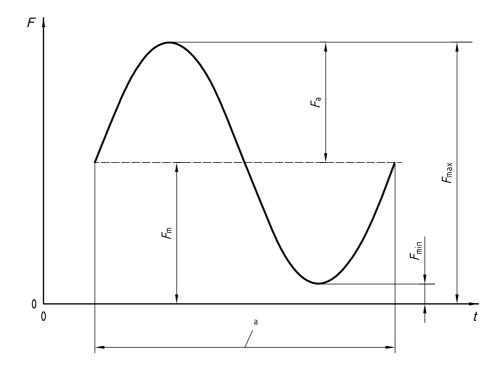
ISO 10190, Motor cycle chains — Characteristics and test methods

#### **Symbols** 3

See Table 1 and Figure 1.

Table 1 — Symbols

Symbol	Description	Unit
d	Step size — interval between adjacent force levels in a staircase test [see Equation (5)]	N
$F_{\sf max}$	Maximum force — maximum value of force in the cycle	Ν
$F_{min}$	Minimum force — minimum value of force in the cycle	N
$F_{m}$	Mean force — half the sum of the maximum and minimum forces in the force cycle [see Equation (1)]	N
$F_{a}$	Force amplitude — half the difference between the maximum force and minimum force [see Equation (2)]	N
$F_{b}$	Mean fatigue strength — test force, corrected to zero minimum force, at which there is a 50 % probability of failure at endurance [see Equation (6)]	N
$F_{\sf d}$	Fatigue limit — test force, corrected to zero minimum force, at which there is a calculated $0.135\%$ probability of failure at $10^7$ force cycles — approximates the force below which a chain may endure an indefinite number of force cycles [see Equation (8)]	
$F_{t}$	Test force — maximum force, corrected to zero minimum force, at which a test is run [see Equation (3)]	N
$F_{u}$	Minimum UTS — minimum tensile strength of chain as specified in ISO 606 or ISO 10190	N
N	Number of cycles, at a given alternating force, applied to a specimen chain at a particular time in the test	
$N_{e}$	Endurance — predetermined number of cycles at which a test will be discontinued without failure of the specimen chain	_
n	Number of test data points included in the analysis	_
p	Chain pitch	mm
S	Standard deviation of the staircase test data [see Equation (7)]	N



$$F_{\rm m} = \left(\frac{F_{\rm max} + F_{\rm min}}{2}\right) \tag{1}$$

$$F_{\mathbf{a}} = \left(\frac{F_{\mathsf{max}} - F_{\mathsf{min}}}{2}\right) \tag{2}$$

#### Key

F force

t time

a 1 cycle.

Figure 1 — Typical force cycle

#### 4 Principle

Tests are made on transmission chains to determine fatigue properties of chain plates such as those shown on a F-N diagram or to verify conformance to dynamic strength requirements in ISO 606 and ISO 10190.

#### 5 Apparatus

#### 5.1 Testing machine

The size of the testing machine shall be selected so that the maximum force on the test specimen is  $\geq$  10 % of the maximum capacity of the machine. Tests shall be conducted on a machine capable of applying a sinusoidal fluctuating force to the test specimen in axial tension.

The test frequency shall be chosen so as not to induce a damaging temperature increase in the test specimen.

The machine shall be calibrated periodically in order to maintain suitable accuracy and should be calibrated to within  $\pm\,2\,\%$  of its maximum capacity. A force-monitoring system could be mounted in series with the test specimen to ensure that the force cycle is maintained throughout the test.

#### ISO 15654:2004(E)

The testing machine shall also have

- a) a counter to record the number of force cycles,
- b) a device to stop the machine when the chain fails, and
- c) a device to prevent the machine from restarting after an emergency stop due to power failure, etc.

#### 5.2 Test fixtures

The test fixtures shall be capable of transmitting an axial force to the test piece without inducing a subsidiary force caused by the fixtures. Universal type fixtures shall be used for fatigue testing of transmission chains.

The universal fixtures shall be designed according to the chain dimensions specified in the separate standards. Examples of the structure of the fixtures are shown in Figure 2.

Universal fixtures shall permit free movement on both sides of the chain centreline in both the normal plane of articulation and in the transverse plane. The hole in the fixture shall be a size equal to the bush hole diameter of the chain under test.

NOTE The test specimens all illustrate five free pitches.

When testing chain on sheaves, the chain shall be restrained from moving around the sheaves to ensure that only specific pitches of the chain are tested.

#### 6 Test specimens

**6.1** At least five free pitches of chain shall be used as a fatigue test specimen, except for chain pitch over 50,8 mm where a minimum of three free pitches are acceptable.

Free pitches are those chain pitches that do not contact the fixtures.

**6.2** The test specimens shall be unused, undamaged chains on which all phases of manufacture have been completed. The final lubricant type is discretionary.

#### 7 Test procedure

#### 7.1 Test forces

#### 7.1.1 Minimum force

The minimum force for the test shall be at least 1 % but not more than 5 % of the minimum tensile strength given for the subject chain in ISO 606 or ISO 10190.

#### 7.1.2 Maximum force

The maximum force for the test shall be determined in accordance with 7.2 for a conformity test or in accordance with 7.3 for a staircase test.

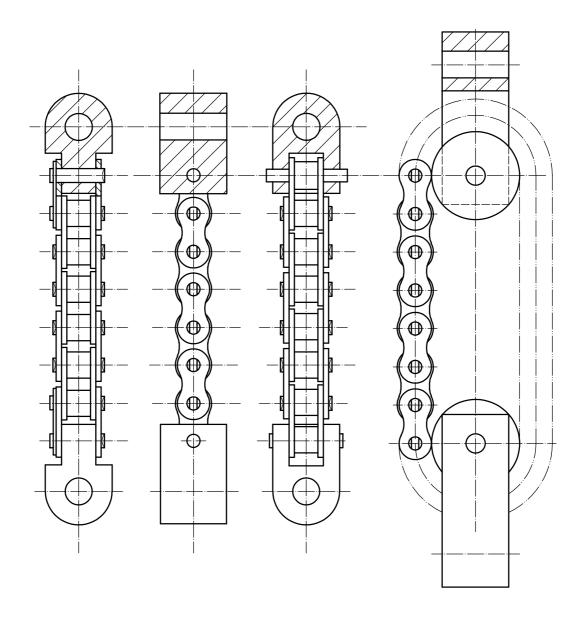
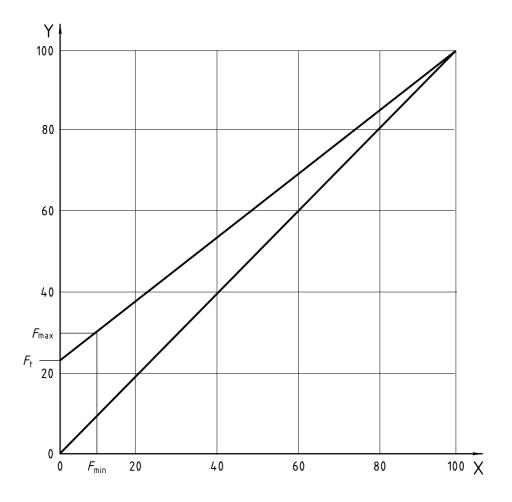


Figure 2 — Examples of test specimens mounted in universal fixtures

#### 7.1.3 Test force

For analyses of fatigue test data, maximum forces shall be corrected to zero minimum force. A test force is obtained by correcting the maximum force to zero minimum force by means of the Johnson–Goodman method [Equation (3)]. The Johnson–Goodman relationship is illustrated by Figure 3, where  $F_{\min}$  is  $0.05 \times F_{\mathrm{u}}$ , and  $F_{\max}$  is  $0.3 \times F_{\mathrm{u}}$ , and the resulting  $F_{\mathrm{t}}$  is  $0.263 \times F_{\mathrm{u}}$ .

$$F_{\mathsf{t}} = \frac{F_{\mathsf{u}}(F_{\mathsf{max}} - F_{\mathsf{min}})}{F_{\mathsf{u}} - F_{\mathsf{min}}} \tag{3}$$



#### Key

- minimum force, % of  $F_{\mu}$
- maximum force, % of  $F_{II}$

Figure 3 — Johnson-Goodman diagram

#### Force application

A longitudinal tensile force shall be applied, sinusoidally varying between the minimum test force determined according to 7.1.1 and the maximum test force determined according to 7.1.2. The test shall continue to endurance or until the specimen fails, whichever is sooner.

#### 7.2 **Conformity test**

#### 7.2.1 Purpose

The purpose of this test is to determine whether or not a chain meets the dynamic strength requirements given for it in ISO 606 or ISO 10190.

#### 7.2.2 Endurance

Endurance shall be  $3 \times 10^6$  cycles.

#### 7.2.3 Minimum test force

The minimum force for the test shall be set in accordance with 7.1.1.

#### 7.2.4 Maximum test force

The maximum test force shall be determined using Equation (4):

$$F_{\text{max}} = \frac{F_{\text{t}}F_{\text{u}} + \left[F_{\text{min}}\left(F_{\text{u}} - F_{\text{t}}\right)\right]}{F_{\text{u}}} \tag{4}$$

#### 7.2.5 Number of tests

Three specimens shall be tested.

#### 7.2.6 Acceptance

All specimens shall survive to endurance without failure.

#### 7.3 Staircase test

#### 7.3.1 Purpose

The purpose of this test is to determine the fatigue limit of the subject chain.

#### 7.3.2 Description

For the purposes of this International Standard, a staircase test is one in which specimens are tested sequentially at predetermined, equally spaced, force levels. The first specimen is tested at a force level slightly greater than the estimated mean fatigue strength of the chain. If the first specimen runs to endurance (runs-out), the next specimen is tested at the next higher predetermined force level. If the first specimen fails before endurance, the next specimen is tested at the next lower predetermined force level. Force levels for subsequent tests are determined in a like manner, and the testing continues until the required number of tests are completed.

#### 7.3.3 Endurance

Endurance shall be 10<sup>7</sup> cycles when testing for fatigue limit.

#### 7.3.4 Rules for conducting a staircase test

The test shall begin with a response reversal, then a run-out followed by a failure, or a failure followed by a run-out.

The test shall have at least ten data points to determine the mean with 95 % confidence and six data points to determine the mean with 90 % confidence. It shall have the minimum number of data points in accordance with Table 2 to detect a difference in the mean of approximately one-half step size.

Table 2 — Required sample sizes

Confidence	3-step staircase	4-step staircase	5-step staircase
90 %	6	11	16
95 %	10	15	20

The highest force level in a staircase shall contain only failures.

The lowest force level in a staircase shall contain only run-outs.

Intermediate force levels in a staircase shall contain both failures and run-outs.

#### 7.3.5 **Determining step size**

#### 7.3.5.1 Using survival test with Probit analysis

See Annex A. The step size shall be determined in accordance with A.5.

#### 7.3.5.2 Using combined test method (CTM)

See Annex B. The step size shall be determined in accordance with B.3.4.3 [see Equation (B.10)].

#### 7.3.5.3 Using empirical method

Extensive testing has shown that reliable results can be obtained when the step size, expressed in newtons (N), is set according to Equation (5):

$$d \approx 14 p^{1,5} \tag{5}$$

#### Staircase test data analysis

#### 8.1 Data

The data for a staircase test analysis shall be gathered in accordance with 7.3.

An additional test point at the end of a staircase test can be determined by the rules for conducting a staircase test (see 7.3). This additional test point, sometimes called a "phantom" point, shall be included in the analysis.

#### Plotting staircase data 8.2

It is customary to tabulate and plot the data as a staircase test progresses to ensure that the rules for constructing a staircase are followed. An example of such a data plot (3 levels and 95 % confidence level) is shown in Table 3.

Table 3 — Staircase data plot — Example

Test force	Invalid	d tests	Valid tests									
F <sub>t</sub> + 2d	х											
$F_{t} + d$		х						х		х		#
$F_{t}$			х		х		0		0		0	
$F_{t}-d$				0		0						

run-out

failure

phantom point

#### 8.3 Statistical calculations

#### 8.3.1 Mean fatigue strength: 0,50 probability of survival

The mean fatigue strength shall be calculated using Equation (6).

$$F_{\mathsf{b}} = \frac{\sum_{i=1}^{n} F_{\mathsf{t}i}}{n} \tag{6}$$

where n is the total number of valid tests in the staircase calculations.

#### 8.3.2 Standard deviations

The standard deviations of the staircase data shall be calculated using Equation (7).

$$S = \left[ \frac{\sum_{i=1}^{n} F_{ti}^{2}}{n} - F_{b}^{2} \right]^{0.5} \tag{7}$$

#### 8.3.3 Fatigue limit: 0,99865 probability of survival

The fatigue limit shall be calculated using Equation (8).

$$F_{\mathsf{d}} = F_{\mathsf{b}} - 3S + d \tag{8}$$

#### 9 Report of test results

#### 9.1 Test chain information

The originator shall provide to the user

- a) the brand name or other identifying name or mark of the test chain,
- b) the ISO number or manufacturer's number and the pitch of the test chain, and
- c) the length in free pitches of the test specimens.

#### 9.2 Test equipment and procedures

#### 9.2.1 Test equipment

The originator shall provide to the user

- a) the brand name and type of testing machine,
- b) the maximum rated capacity of the test machine,
- c) the number of machines used if more than one,
- d) the method of dynamic force verification and monitoring, and
- e) the method of calibration and the most recent date calibrated.

#### ISO 15654:2004(E)

#### 9.2.2 Test procedures

The originator shall provide to the user

- a) the type of test; conformity or staircase,
- b) the number of cycles to endurance, and
- c) any ambient conditions that could affect the test results.

#### 9.3 Test results for conformity and staircase tests

The originator shall provide a table of test results to the user, which shall include

- a) identification of the test specimen,
- b) the test sequence, the order in which the specimens were run,
- c) the maximum and minimum force for each test,
- d) the test force, corrected to zero minimum force, for each test,
- e) the force cycling frequency,
- f) the number of cycles at which each test was terminated,
- g) the reason each test was terminated and, if a failure, the component of the chain that failed,
- h) a brief summary of the post-test examination, if any, and
- i) the machine used for each test, if more than one machine was used.

For a staircase test, the originator shall also provide the user with

- the mean fatigue strength,  $F_b$ , and
- the minimum fatigue strength, or fatigue limit.

## Annex A (informative)

### Survival test with abridged Probit analysis

#### A.1 Principle

The purpose of this test is determine the mean fatigue limit and its standard deviation. A survival test with abridged Probit analysis may also be used to determine the step size for future staircase testing of the subject chain model.

#### A.2 Description

The survival test is a procedure in which groups of chain specimens are tested at different force levels such that the central force level contains approximately 50 % failures, the highest force level contains 90 % to 95 % failures, and the lowest force level contains 5 % to 10 % failures.

The Probit analysis is used to estimate the mean fatigue limit and standard deviation of the tested population. The step size is then set equal to between 67 % and 150 % of the standard deviation for future staircase testing of the subject chain model.

#### A.3 Test procedure

#### A.3.1 Test specimens

Prepare at least fifty, and preferably a hundred, test specimens in accordance with Clause 6, with all test specimens from the same production batch.

Provide additional test specimens for preliminary or invalid tests.

#### A.3.2 Endurance

Set endurance at 10<sup>7</sup> cycles.

#### A.3.3 Force levels

Use five force levels in the survival test; one giving approximately 50 % failures before endurance (very close to the mean), two force levels above that, and two below. There may be only four force levels if the mean falls approximately midway between two force levels.

Ensure that the interval between adjacent force levels is uniform.

The central force level may be selected by means of a brief (five or six tests) staircase test.

#### A.3.4 Testing

Allocate test specimens to each level according to Table A.1 or Table A.2 in order to make the precision at each force level comparable. At least five specimens at each level, and fifty specimens in total, are required for acceptable accuracy.

Table A.1 — Allocation of test specimens for five force levels

Expected run-out %	Relative group size
25 to 75	1,0
15 to 20 or 80 to 85	1,5
10 or 90	2,0
5 or 95	3,0
2 or 98	5,0

Table A.2 — Allocation of test specimens for four force levels

Expected run-out	Relative group size
20 to 80	1,0
5 to 10 or 90 to 95	2,5

Test each specimen until it fails or reaches endurance.

- Central force level: approximately 50 % failures.
- Highest force level: at least one run-out.
- Lowest force level: at least one failure.

#### A.4 Analysis procedure

#### A.4.1 General

A Probit analysis is a complex technique for calculating an optimum line through the survival data points using a least-squares analysis to weight each data point according to its distance from the optimum line. This abridged method calculates a regression line through a single survival point on each force level. The abridged method has proven to be quite adequate for the purposes of this International Standard.

#### A.4.2 Distributions

Visually check the distributions of survival (cycles to failure) and force by means of a probability plot and confirm that the distribution of cycles to failure at the central and each higher force level is log-normal and that of survival across the force levels is normal.

As the Probit analysis assumes normal distributions, if either distribution is obviously not normal (or log-normal), do not attempt the analysis.

#### A.4.3 Standard deviation

Estimate the standard deviation of the survival test data, *S*, which is also the slope of the regression line, using Equation (A.1).

$$S = \left| \frac{n_{L} \Sigma XY - \Sigma X \Sigma Y}{n_{L} \Sigma X^{2} - (\Sigma X)^{2}} \right|$$
(A.1)

where

- $n_1$  is the number of force levels in the test;
- X is survival, in standard normal transform units, Z;
- Y is the test force, in newtons (N).

#### A.4.4 Mean fatigue limit

Estimate the mean fatigue limit of the survival test data,  $Y_0$ , which is also the Y-intercept (of force with 50 % survival), using Equation (A.2).

$$Y_0 = \frac{\Sigma Y + S\Sigma X}{n_{\mathsf{L}}} \tag{A.2}$$

#### A.5 Step size

Set the step size for subsequent staircase testing at 67 % to 150 % of the standard deviation. The step size should be set nearly equal to 100 % of the standard deviation.

#### A.6 Example

A survival test was conducted with specimens of 16A chain tested at six force levels. All failures were obtained at the highest force level and all run-outs were obtained at the lowest force level. Survival data from the remaining four force levels are shown in Table A.3.

Force level **Failures Run-outs**  $n_{\mathsf{L}}$ kΝ 19,45 25 23 2 17,60 10 6 4 15,75 10 4 6 13,90 25 1 24

Table A.3 — Test results

A table usually is created for the survival test data and preliminary calculations. Table A.4 was created for this example.

Table A.4 — Survival test data and Probit analysis

$n_{L}$	X	Survival %	Z	Force, F kN	X	Y	X <sup>2</sup>	Y <sup>2</sup>	(XY)
25	1	96,00	1,751	13,90	1,751	13,90	3,0660	193,2	24,34
10	4	60,00	0,253	15,75	0,253	15,75	0,0640	248,1	3,98
10	6	40,00	-0,253	17,60	-0,253	17,60	0,0640	309,8	-4,45
25	23	8,00	-1,405	19,45	-1,405	19,45	1,9740	378,3	-27,33
				Total	0,346	66,70	5,168	1129,3	-3,46

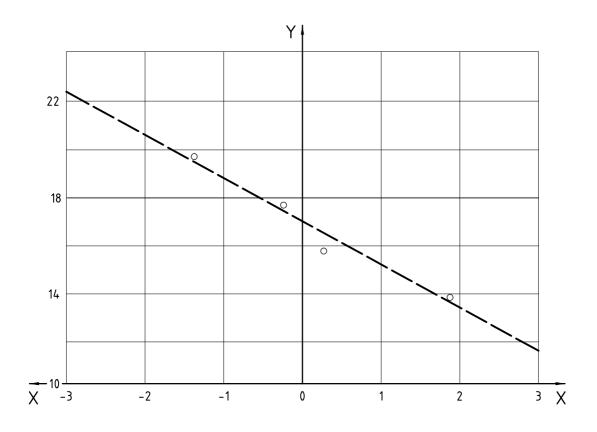
From this data, the calculated standard deviation was

$$S = \left| \frac{4(-3,46) - (0,346 \times 66,70)}{4 \times 5,168 - 0,346^2} \right| = 1,796 \text{ kN}$$

and the mean fatigue limit

$$Y_0 = \left| \frac{66,70 + (1,796 \times 0,346)}{4} \right| = 16,83 \text{ kN}$$

The results of this analysis are plotted in Figure A.1.



#### Key

X survival probability, standard normal transform units, Z

Y force, F, kN

Figure A.1 — Probit analysis

## Annex B (informative)

#### Combined test method

#### **B.1 Purpose**

The purpose of this test is to determine the slope of the F-N line and the fatigue limit of a particular chain in a single test series. The CTM also may be used to determine the step size for future staircase testing of the subject chain model.

#### **B.2 Description**

Numbers of test specimens in the CTM are determined by the different probabilities of survival, R, of the mean F-N line. The 14 F-N test method for determining R=90%, and the 24 F-N test method for determining R=95%, are described here. The 14 F-N test method is a procedure in which eight chain specimens are tested at four force levels in the finite life range, and five specimens plus one phantom data are tested in a staircase. The 24 F-N test method is a procedure in which fourteen chain specimens are tested at four force levels in the finite life range, and nine specimens plus one phantom data are tested in a staircase. The mean F-N line and the standard deviation of fatigue life are determined by statistical calculation. The standard deviation of force in a staircase is derived from the standard deviation of fatigue life in a finite life range, and is the step size for the staircase test.

#### **B.3 Test procedure**

#### **B.3.1 Test specimens**

Prepare at least 13 test specimens for the 14 F–N test method, or 23 test specimens for the 24 F–N test method, in accordance with Clause 6, with all test specimens from the same production batch. Provide additional test specimens for preliminary or invalid tests.

#### **B.3.2 Endurance**

For the staircase portion of the test, set endurance at  $10^7$  cycles. If endurance is set between  $3 \times 10^6$  and  $10^7$  cycles, extrapolate the results to  $10^7$  cycles by the method given in Annex G.

#### **B.3.3 Force levels**

For the finite life portion of the test, establish four test force levels ( $F_A$ ,  $F_B$ ,  $F_C$ , and  $F_D$ ) in accordance with B.3.4.1.

For the staircase portion of the test, an initial test force level,  $F_1$ , may be set at the force of two steps plus the force where the mean F-N line intersects  $10^6$  cycles, with additional test force levels in increments of the step size.

#### B.3.4 Testing

#### **B.3.4.1** Preliminary tests

Test one specimen at the lowest force level  $(F_D)$  in the finite life portion. If the measured fatigue life departs significantly from the  $5 \times 10^5$  cycles, test an additional specimen at an adjusted force level. When the resulting fatigue life is near  $5 \times 10^5$  cycles, use that force level as  $(F_D)$ . Then test one specimen at the highest force level (F<sub>A</sub>) in the finite life portion, with this highest force level set at no more than 60 % of the minimum tensile strength in ISO 606 or ISO 10190. Calculate the other test force values using Equations (B.1) to (B.3).

$$\Delta = \frac{F_{\mathsf{A}} - F_{\mathsf{D}}}{3} \tag{B.1}$$

$$F_{\mathsf{B}} = F_{\mathsf{A}} - \Delta \tag{B.2}$$

$$F_{\rm C} = F_{\rm A} - 2\Delta \tag{B.3}$$

#### B.3.4.2 Finite life tests

For the 14 F-N test method, complete the finite life portion of the test by testing a total of two specimens at each force levels. For the 24 F-N test method, complete the finite life portion of the test by testing a total of four specimens at force levels  $F_{\rm A}$  and  $F_{\rm B}$ , and three specimens at force levels  $F_{\rm C}$  and  $F_{\rm D}$ . Determine the equation for the F-N line using Equations (B.4) to (B.8). Calculate the standard deviation of logarithmic life using Equation (B.9). Derive the standard deviation of force using Equation (B.10).

#### **B.3.4.3** Staircase tests

The step size for the staircase test should be equal to the calculated standard deviation of force determined by Equation (B.10). Conduct a six-test staircase test (five valid test points plus one phantom point) for the 14 F-N test method, or a ten-test staircase test (nine valid test points plus one phantom point) for the 24 F-N test method, in accordance with 7.3.

#### B.4 Analysis procedure

#### **B.4.1 Finite life portion**

In the CTM, fatigue life is plotted on a logarithmic scale and force is plotted on a linear scale. The F-N line, standard deviation of logarithmic life, and standard deviation of force are determined from Equations (B.4) to (B.10).

The regression equations for the F–N line are

$$\lg N = \hat{\alpha} + \hat{\beta} F_{\dagger} \tag{B.4}$$

$$\hat{\alpha} = \overline{\lg N} - \hat{\beta} \overline{F}_{\mathsf{t}} \tag{B.5}$$

$$\hat{\beta} = \frac{\sum_{i=1}^{n_f} \left( F_{ti} - \overline{F}_{t} \right) \left( \lg N_i - \overline{\lg N} \right)}{\sum_{i=1}^{n_f} \left( F_{ti} - \overline{F}_{t} \right)^2}$$
(B.6)

$$\overline{\lg N} = \frac{1}{n_{\mathsf{f}}} \sum_{i=1}^{n_{\mathsf{f}}} \lg N_i \tag{B.7}$$

$$\overline{F}_{\mathsf{t}} = \frac{1}{n_{\mathsf{f}}} \sum_{i=1}^{n_{\mathsf{f}}} F_{\mathsf{t}i} \tag{B.8}$$

where the number of tests,  $n_{\rm f}$ , are 8 for the 14 F-N test method, and 14 for the 24 F-N test method.

The estimated standard deviation of logarithmic life is

$$\hat{\sigma}_{|gN} = \sqrt{\frac{1}{n_f - 2} \sum_{i=1}^{n_f} \left[ |gN_i - (\hat{\alpha} + \hat{\beta}F_{ti}) \right]^2}$$
(B.9)

#### **B.4.2 Staircase portion**

The estimated standard deviation of force is

$$\hat{\sigma}_{\mathsf{F}} = \frac{1}{\left|\hat{\beta}\right|} \hat{\sigma}_{\mathsf{Ig}N} \tag{B.10}$$

The estimated mean fatigue strength,  $F_{b}$ , is

$$F_{b} = \frac{1}{n_{s}} \sum_{j=1}^{n_{s}} F_{tj}$$
 (B.11)

where the number of tests,  $n_s$ , are 6 for the 14 F-N method, and 10 for the 24 F-N method.

#### **B.5** R–F–N curve

The mean R–F–N curve, at R = 50 % probability of survival, is defined by Equation (B.4) for the finite life area, and by Equation (B.11) for endurance at the staircase test area.

Using data collected by the 14 F–N test method, the R–F–N curve, at R = 90 % probability of survival, is defined by Equation (B.12) for the finite life area, and Equation (B.13) for endurance at the staircase test area. The value of q is 1,28.

Using data collected by the 24 F–N test method, the R–F–N curve, at R = 95 % probability of survival, is defined by Equation (B.12) for the finite life area, and Equation (B.13) for endurance at the staircase test area. The value of q is 1,64.

For either case, extrapolate the fatigue limit to 10<sup>7</sup> cycles using the method given in Annex G, link this point with the point at endurance, and extend that line to connect to a line at the finite life area.

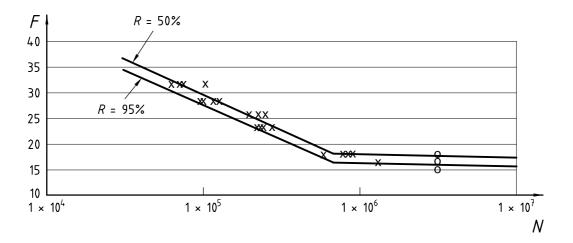
$$\lg N = \hat{\alpha} + \hat{\beta} F_{\mathsf{t}} - q \hat{\sigma}_{\lg N} \tag{B.12}$$

$$F_{0,90} \text{ or } _{0,95} = F_{b} - \frac{q}{\left|\hat{\beta}\right|} \, \hat{\sigma}_{IgN}$$
 (B.13)

## B.6 Sample test report and graph

	Fatigue test report										
		Report N	0.:	<u>1001</u>	<u>Pag</u>	ge 1 of 2	Rep	oort date: <u>2003-07-31</u>			
Chain:											
Brand:		Number:		Pitch:	Specin	nen length:	Other:				
ABC Chair	n	16A		25,4 mm	5P,ILE	E					
Mechanica	al properties	:		l	ı						
Not taken											
Test:											
Туре:		Endurance:		Temperatu	re:		Other:				
Combined	(24 <i>F–N</i> )	$3 \times 10^6$ cycle	es	Approx. 20	°C		Moderat	te humidity			
Machine:				·							
Brand:		Type:		No. used:	Calibra	tion date:	Force ve	erification and monitoring:			
XYZ		Servo-hydra	ulic	1	2000-0	7-12	Periodic	, strain-gauge bar			
Date	Test No.	Frequency	$F_{\sf max}$	$F_{min}$	$F_{t}$	Cycles, $N$	Failure	Remarks			
		Hz	kN	kN	kN						
03-06-05	001	13	33,3	1,80	32,55	7,055E4	IP				
03-06-05	002	13	24,9	1,80	23,87	2,381E5	IP				
03-06-05	003	13	30,5	1,80	29,66	1,104E5	IP				
03-06-06	004	13	30,5	1,80	29,66	8,980E4	IP				
03-06-06	005	13	24,9	1,80	23,87	2,510E5	IP				
03-06-06	006	13	27,7	1,80	26,77	2,236E5	IP				
03-06-07	007	13	33,3	1,80	32,55	9,895E4	IP				
03-06-07	008	13	24,9	1,80	23,87	2,885E5	IP				
03-06-08	009	13	33,3	1,80	32,55	6,891E4	IP				
03-06-08	010	13	33,3	1,80	32,55	6,036E4	IP				
03-06-08	011	13	30,5	1,80	29,66	9,309E4	IP				
03-06-08	012	13	30,5	1,80	29,66	1,242E5	IP				
03-06-09	013	13	27,7	1,80	26,77	1,905E5	IP				
03-06-09	014	13	27,7	1,80	26,77	2,379E5	IP				
Results an	nd conclusio	ns:									
$\alpha$ = 7,07											
,	$\beta$ = $-0.07$										
$\sigma_{IgN}$	$\sigma_{IgN}$ = 0,081										
$\sigma_{\!F}$ (s)	) = 1,188										
The results	The results of the staircase tests are plotted on the attached graph [see Figure B.1].										
		-									
Signed:											

	_	_	_	Fatigue	-		_	
		Report No	0.:	<u>1001</u>	<u>Pa</u>	ge 2 of 2	Rep	oort date: <u>2003-07-31</u>
Chain:		т		т	1		1	
Brand:		Number:		Pitch:	-	nen length:	Other:	
ABC Chair		16A		25,4 mm	5P,ILE	E		
	al properties:	:						
Not taken								
Test:		1		1			1	
Type:		Endurance:		Temperatu			Other:	
Combined	(24 <i>F–N</i> )	3 × 10 <sup>6</sup> cycle	<del>)</del> S	Approx. 20	°C		Moderat	te humidity
Machine:		<del></del>		т	<del> </del>		1	
Brand:		Type:		No. used:		ation date:		erification and monitoring:
XYZ		Servo-hydra	ı	1	2000-0	7-12	Periodic	c, strain-gauge bar
Date	Test No.	Frequency	$F_{\sf max}$	$F_{min}$	$F_{t}$	Cycles, $N$	Failure	Remarks
		Hz	kN	kN	kN			
03-06-12	015	13	19,6	1,80	18,40	8,471E5	IP	
03-06-13	016	13	18,4	1,80	17,16	3,000E6	NF	
03-06-16	017	13	19,6	1,80	18,40	5,581E5	IP	
03-06-19	018	13	18,4	1,80	17,16	1,240E6	IP	
03-06-20	019	13	17,2	1,80	15,92	3,000E6	NF	
03-06-23	020	13	18,4	1,80	17,16	3,000E6	NF	
03-06-26	021	13	19,6	1,80	18,40	8,124E5	IP	
03-06-27	022	13	18,4	1,80	17,16	3,000E6	NF	
03-06-30	023	13	19,6	1,80	18,40	3,000E6	NF	
	024	<u> </u>	20,8	1,80	19,64			Phantom point
		<u> </u>	<u> </u>					
Results an	nd conclusion	ns:						
$F_{t}$	Stairca	se l	Histog	ram				
19,64	<del></del>	#	#		_	F <sub>b</sub> =	= 17,78 kľ	N
18,40	) x x >	х о	X	xxo		σ <sub>F</sub> =	= 1,188 kl	N
17,16	6 o x o	o	0	хоо		$F_{0,9}$	<sub>95</sub> = 15,83	$3 \text{ kN } \text{ (at } 3 \times 10^6 \text{ cycles)}$
15,92	2 0		0			$F_{0,9}$	<sub>95</sub> = 15,16	6 kN (at 10 <sup>7</sup> cycles)
The results	s of the stair	case tests are	e plotte	ed on the att	tached g	graph [see Fi	gure B.1]	
						Signed:		John Smith



#### Key

- force, kN
- combined cycles to failure
- probability of survival

Figure B.1 — Sample CTM test results

## Annex C (informative)

### Justification for adding one step to fatigue limit in staircase analysis

#### C.1 Introduction

The staircase analyses in this International Standard utilize all test points, both failures and run-outs. The calculated minimum fatigue strength  $(F_{\rm b}-3{\it S})$  is always less than the lowest test force. By definition, all responses at the lowest test force must be run-outs. Consequently, the minimum fatigue strength, with a 0,135 % probability of failure, must be greater than the lowest test force in all cases.

#### C.2 Analysis

Staircases, having fifty to seventy-five tests, were constructed by combining several staircases with ten tests each. Means and standard deviations were calculated for all tests and failures only in each staircase. Calculations for 10A, 16A, and 24A chains, are presented in Tables C.1 to C.4. A graph of the four-step staircase analysis for 16A chain is shown in Figure C.1.

Table C.1 — Analysis of 10A chain, four-step staircase data

Force (N)	X	0	n = 75	d = 925		
8 810	7	0		Analysis of all da	ta points:	
7 885	21	8		$F_{\rm b}$ = 7 393	<i>S</i> = 747	$F_{b} - 3S = 5152$
6 960	8	23		Analysis of failur	es only:	
6 035	0	8		F <sub>b</sub> = 7 860	<i>S</i> = 596	$F_{b} - 3S = 6072$
Total	36	39		1,232 <i>S</i> = 0,995 <i>d</i> =	= Difference = 920	

Table C.2 — Analysis of 16A chain, four-step staircase data

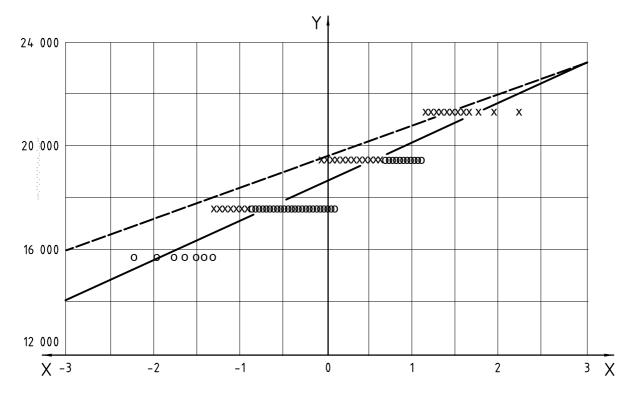
Force (N)	Х	0	n = 75	d = 1 855		
21 315	9	0		Analysis of all da	ta points:	
19 460	21	9		$F_{\rm b}$ = 18 620	S = 1 521	$F_{\rm b} - 3S = 14057$
17 605	7	22		Analysis of failure	es only:	
15 750	0	7		$F_{\rm b}$ = 19 563	S = 1 214	$F_{\rm b} - 3S = 15921$
Total	37	38		1,226S = 1,005d =	Difference = 1 864	

Table C.3 — Analysis of 16A chain, three-step staircase data

Force (N)	х	0	n = 50	d = 1 855		
21 315	9	0		Analysis of all data	a points:	
19 460	16	9		$F_{\rm b}$ = 19 203	S = 1 286	$F_{b} - 3S = 15345$
17 605	0	16		Analysis of failure	s only:	
Total	25	25		$F_{\rm b}$ = 20 128	S = 890	$F_{\rm b} - 3S = 17 \ 458$
				1,643 <i>S</i> = 1,139 <i>d</i> =	Difference = 2113	

Table C.4 — Analysis of 24A chain, five-step staircase data

Force (N)	х	0	n = 75	d = 3 240				
39 350	5	0		Analysis of all data points:				
36 110	14	5		$F_{\rm b}$ = 32 610	S = 3 540	$F_{\rm b} - 3S = 21~990$		
32 870	11	13		Analysis of failure	s only:			
29 630	9	10		$F_{\rm b}$ = 34 113	S = 3 167	$F_{b} - 3S = 24 612$		
26 390	0	8		0.741S = 0.809d = Difference = 2622				
Total	39	36						



#### Key

failure probability, standard normal transform units, Z

force, F, N

run-outs

failures

distribution, all data

distribution, failures only

Figure C.1 — 16A chain fatigue analysis

Analysis of 10A and 16A four-step staircases showed the calculated minimums for failures were 0,99 and 1,00 steps and 1,23 and 1,22 standard deviations higher than the calculated minimums for all tests. Analysis of a 16A three-step staircase showed that the calculated minimum for failures was 1,14 steps and 1,64 standard deviations higher than the calculated minimum for all tests. Analysis of the 24A five-step staircase showed that the calculated minimum for failures was 0,81 of a step and 0,74 of a standard deviation higher than the calculated minimum for all tests.

#### C.3 Conclusions

The following conclusions can be drawn from the foregoing.

- a) The fatigue limit, with 99,865 % survival (0,135 % probability of failure), is one step greater than the minimum fatigue strength calculated from all tests.
- The three-step and four-step staircase analyses support the first conclusion very well.
- c) The five-step staircase analysis does not support the first conclusion very well, probably because of the large variance.
- d) The fatigue limit, with 99,865 % survival (0,135 % probability of failure), is one standard deviation greater than the minimum fatigue strength calculated from all test points only when the standard deviation is equal to the step size.

## Annex D

(informative)

### Adding an additional "phantom" point at the end of staircase test

The rules for selecting the third and subsequent test force levels in a staircase dictate that the next test is to be run at a one-step-higher force level if the test just completed was a run-out, and at a one-step-lower force level if the test just completed was a failure. This permits the force level at which a test would be run after the final actual test in a staircase to be determined. Consequently, one data point may be added to the staircase series, after the final test point, even though a test at that point was not actually run.

The procedure is as follows: if the final test was a run-out, add a "phantom" point at one step higher test load; if the final test was a failure, add a phantom point at one step lower test load.

There is no way of knowing if the phantom test would be a failure or a run-out, so only one phantom point after the final test point can be determined.

## **Annex E** (informative)

### Reporting fatigue test results

#### E.1 General

This annex suggests ways of presenting the results of roller chain fatigue tests, and presents both tabular and graphical methods. Sample fatigue test report forms are presented and explained, and sample graphical methods of presenting fatigue test results are given.

#### E.2 Tabular presentation of results

This clause presents a format for reporting (see also Annexes B, E and H) the required data from 9.1, 9.2 and 9.3, and gives a brief description of each item of information that may be entered in the appropriate space of this fatigue test report, keyed to the (here) numbered spaces on the form (unnumbered spaces not being in need of explanation).

Fatigue test report										
	Report No.: Report date:									
Chain:										
Brand:		Number:		Pitch:	Specimen length:		Other:			
	1	2		3	4			5		
Mechanical properties: 6										
Test:										
Type:		Endurance:		Temperatu	re:		Other:			
,	7	8			9			10		
Machine:										
Brand:		Type:		No. used: Calibration date:			Force verification and monitoring:			
11		12			13			14		
Date	Test No.	Frequency	$F_{\sf max}$	$F_{min}$	$F_{t}$	$\mathbf{Cycles,}N$	Failure	Remarks		
		Hz	kN	kN	kN					
15	16	17	18	19	20	21	22	23		
Results and conclusions:										
	Signed:									

#### Key

- brand name or other identifying name or mark of the tested chain
- ISO number or manufacturer's number of the chain
- 3 nominal pitch of the chain
- length of test specimens, in free pitches a

- 5 other characteristics of the test chain that might be helpful (production batch identity, experimental chain designation, or non-standard design features)
- 6 results of tensile tests, or bush and pin press out force tests
- 7 type of test; conformity, staircase, survival, combined method, or finite life
- 8 declared endurance, in number of cycles, for a conformity, staircase, survival, or combined method test
- 9 mean ambient temperature, or range of minimum and maximum temperatures, during test
- 10 other environmental conditions (high humidity, etc.) that might affect test results
- 11 brand name or other identifying name or mark of the testing machine
- 12 type (harmonic spring, servo-hydraulic, electro-magnetic, etc.) of testing machine
- 13 date on which the machine was last calibrated
- 14 dynamometer and transducer used to verify and monitor the test force b
- 15 date the individual test was completed
- 16 sequence number of the test c
- 17 frequency at which the fluctuating force was applied
- 18 maximum value of the fluctuating force (see Table 1)
- 19 minimum value of the fluctuating force (see Table 1)
- 20 test force, corrected to zero minimum force (see Table 1)
- 21 number of cycles at which the test ended
- 22 component that failed inner plate (IP), outer plate (OP), Pin (PIN), or intermediate plate (ITP) d
- 23 any unique notes concerning the test, e.g. if a terminal connector link failed and was replaced during the test, it should be noted.
- 24 results and conclusions e
- a A note of inner link each end (ILEE) or outer link each end (OLEE) should also be given here.
- <sup>b</sup> There also should be a note as to whether the monitoring was periodic or continuous, and whether or not there was feedback control.
- <sup>c</sup> This may also be combined with machine reference number, if more than one testing machine was used.
- d If the test ran-out, "No Failure" (NF) may be entered.
- <sup>e</sup> For a conformity test, the information required by 9.3, and a statement of "Accepted" or "Not Accepted", explaining failure, if possible; for a staircase test, the information required by 9.3, and any supplemental information that might be helpful to the user; for a combined method test, the information required by Annex B, and any supplemental information that might be helpful to the user; for a finite life method test, the information required by Annex H, and any supplemental information that might be helpful to the user.

#### E.3 Graphical presentation, suggested forms

#### E.3.1 General

If sufficient data is generated, and the user so requests, the originator should present fatigue test results in a graphical form. Usually, only a combined test, a finite life test, or a finite life test paired with a staircase test on the same batch of chain, generates data suitable for graphical presentation.

#### E.3.2 Types of graph

The most common graphical methods of presenting fatigue test data are the F-Log N and Log F-Log N plots. The dependent variable (fatigue life in cycles) is plotted on the abscissa, a logarithmic scale. The independent variable (test force in kilonewtons), is plotted on the ordinate, an arithmetic or logarithmic scale.

#### E.3.3 F-Log N graph

In this presentation, force is assigned an arithmetic scale and life is assigned a logarithmic scale. A typical F-Log N plot for a finite life test is shown in Annex H.

#### ISO 15654:2004(E)

The failures (x) from finite life tests or staircase tests shall be plotted on the test force level at the number of cycles at which failure occurred. The run-outs (o) from staircase tests shall be plotted on the test force level at the predetermined number of cycles for endurance. When there are multiple run-outs at the same force level, the number of run-outs shall be noted just to the right of the symbol.

Transmission chain fatigue test results are acceptably represented by two-segment straight lines. One is a horizontal, or a nearly horizontal, line extending from the fatigue strength at 10<sup>7</sup> cycles to the fatigue strength at 10<sup>6</sup> cycles, at a slope determined by the procedure described in Annex G. The other is a regression line extending from the fatigue strength at 10<sup>6</sup> cycles to the fatigue strength at approximately 10<sup>4</sup> cycles, calculated from finite life test data as described in Annex H.

All test data points shall be plotted on graphs along with calculated or constructed regression lines.

#### E.3.4 Log F-Log N graph

In this presentation, both force and life are assigned a logarithmic scale. A typical Log F-Log N plot is shown in the sample form presented in E.4.

The failures (x) from finite life tests or staircase tests shall be plotted on the test force level at the number of cycles at which failure occurred. The run-outs (o) from staircase tests shall be plotted on the test force level at the predetermined number of cycles for endurance. When there are multiple run-outs at the same force level, the number of run-outs shall be noted just to the right of the symbol. The failures (x) and run-outs (o) shall be plotted as shown in the graph in Figure E.1.

The slope of the regression line, extending from the fatigue strength at 10<sup>7</sup> cycles to the fatigue strength at 10<sup>6</sup> cycles, is determined by the procedure described in Annex G. The other regression line, extending from the fatigue strength at 10<sup>6</sup> cycles to the fatigue strength at 10<sup>4</sup> cycles, is calculated from finite life test data as described in Annex H.

All test data points shall be plotted on graphs along with calculated regression lines.

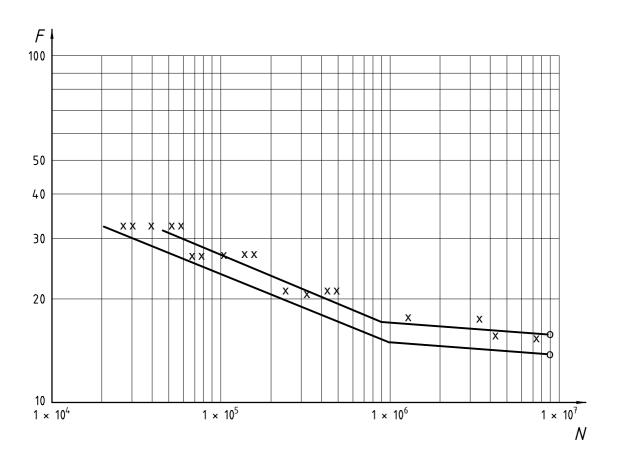
#### E.4 Sample test reports

A staircase test and a finite life test were conducted on one batch of "BCD Chain Company's" number 16A chain. Results of the staircase test are presented in the following sample test report. Results of the finite life test are given in Annex H. The results of the sample staircase test are shown together with the results of the finite life test from Annex H on the graph of Figure E.1.

A combined test was conducted on one batch of "ABC Chain" Company's number 16A chain. The results of that sample test are presented in Annex B.

A conformity test was also conducted on a batch of "BCD Chain Company's" number 16A chain. The results of that test are given in the sample test report concluding this annex.

	-			Fatigue te	est report				
		Report	No.:	1002	<u>Page</u>	e 1 of 1	Report date: <u>2003-07-20</u>		
Chain:									
Brand:		Number:		Pitch:	Specimen le	ength:	Other:		
BCD Chain	ı	16A		25,4 mm	13P,ILEE				
Mechanica	l properties				•				
Not taken									
Test:									
Туре:		Endurance:		Temperati	ure:	Other:			
Staircase		10 <sup>7</sup> cycles		Approx. 20	0°C	Moderate humidity			
Machine:									
Brand:		Type:		No. used:	Calibration	date:	Force verification and		
XYZ		Mech., harmo	nic spring	1	2000-07-29	)	monitoring:		
	<b>-</b>	<b>.</b>	F					train-gauge bar	
Date	Test No.	Frequency	$F_{\sf max}$	$F_{min}$	$F_{t}$	Cycles, N	Failure	Remarks	
		Hz	kN	kN	kN				
03-06-12	001	31	17,35	2,224	15,75	4,771E6	IP		
03-06-16	002	31	15,57	2,224	13,90	1,000E7	NF		
03-06-20	003	31	17,35	2,224	15,75	1,000E7	NF		
03-06-22	004	31	19,12	2,224	17,60	4,096E6	IP		
03-06-26	005	31	17,35	2,224	15,75	8,480E6	IP		
03-06-30	006	31	15,57	2,224	13,90	1,000E7	NF		
03-07-10	007	31	17,35	2,224	15,75	1,000E7	NF		
03-06-11	800	31	19,12	2,224	17,60	1,463E6	IP		
03-06-17	009	31	17,35	2,224	15,75	1,000E7	NF		
03-06-17	010		19,12	2,224	17,60			Phantom point	
	nd conclusi								
$F_{t}$	Stairca	ise		Histogra	m				
		x	x #	xx#	_	$F_{b}$	= 17,78 kN		
17,60							- 4 400 LAL		
17,60 15,75		o x o	0	XXXO		$\sigma_{\!F}$	= 1,188 kN		



#### Key

force, kN

life, cycles

Figure E.1 — Graph of sample staircase test and finite life test for a 16A chain (Log F/Log N plot)

			Fa	atigue test	report					
		Report	No.:	<u>1003</u>	Pa	ge 1 of 1	Repor	t date:	2003-07-20	
Chain:										
Brand:		Number:	Pitch:	Specii	men length:	Other:				
BCD Chain		16A	25,4 mm	5P,ILE	E					
Mechanica	al propertie	es:								
Not taken										
Test:										
Туре:		Endurance:	Temperatu	ıre:		Other:				
Conformit	У	$3 \times 10^6$ cycles	3	Approx. 20	)°C		Moderate	e humid	ity	
Machine:										
Brand:		Type:	No. used:	Calibr	ation date:	Force verification and				
XYZ		Mech., harmonic spring		1	2003-01-29		monitoring:			
						Periodic, strain-gauge bar				
Date	Test No.	Frequency	$F_{\sf max}$	$F_{min}$	$F_{t}$	Cycles, N	Failure		Remarks	
		Hz	kN	kN	kN					
03-07-18	026	31	11,39	2,224	9,55	3,000E6	NF			
03-07-20	027	31	11,39	2,224	9,55	3,000E6	NF			
03-07-22	028	31	11,39	2,224	9,55	3,000E6	NF			
Results a	nd conclu	sions:								
Acce	pted									
						Signed:J	igned: <u>John Smith</u>			

### Annex F

(informative)

### Establishing chain application fatigue ratings

#### F.1 Scope and general

This International Standard prescribes procedures for determining the fatigue limit of transmission chains by means of a staircase test under specified laboratory conditions. Some of the conditions are a five-pitch specimen length, all specimens from a single production batch and a ten-test staircase. In actual applications, the chain length usually is between fifty and two-hundred-fifty pitches, the chains used may be from several production batches, and the total production volume greatly exceeds that represented by only six or ten tests. Additional analysis methods clearly are needed to evaluate the differences between specified laboratory conditions and actual applications.

This annex presents possible methods for evaluating some of the differences between a chain's fatigue limit under specific laboratory conditions and that chain's fatigue rating for a variety of applications. Neither it nor this International Standard as a whole prescribes a method for establishing chain application fatigue ratings.

Instead, this annex describes some methods that may be used to evaluate the effects of three specific differences between the fatigue limit obtained from laboratory testing and a fatigue rating suitable for applications. Experience has shown these methods to be reasonably reliable in evaluating the differences between a five-pitch specimen length and a much longer drive chain length, the production quantity represented by a six-test or ten-test sample and a much larger production quantity, and one production batch and many production batches. Some other factors that should be considered are mentioned, but methods to evaluate them are beyond the scope of this annex. There also may be factors that should be considered that are not mentioned in this annex.

#### F.2 Methods

#### F.2.1 Chain length

One method for evaluating the effect of difference between test specimen length and drive chain length follows.

It can be shown that, for  $F_{bN}$  to be the median of the least of N values:

$$A^{N} = 0,50$$
 (F.1)

Similarly, for  $F_{b(-3SN)}$  to be the  $-3\sigma$  of N values:

$$A^{N} = 0,998 65$$
 (F.2)

For the purposes of this annex, N is the number of potential failure sites, or the number of inner plate apertures, in the given chain. Thus, N = 12 for a five-pitch test chain with an inner link at each end, and N = 200 for a one hundred-pitch drive chain. Calculated values of  $A^N$ , for selected values of N, are given in Table F.1 and shown in Figure F.1.

Then

$$F_{bN} = F_{b1} - Z_{(A,Fb)} S_{P}$$
 (F.3)

where

 $F_{\rm bN}$  is the median (mean) fatigue strength of a sample of chains, each with N inner link apertures;

 $F_{\rm b1}$  is the median (mean) fatigue strength of a sample of chains, each with one inner link aperture;

 $Z_{(A,Fb)}$  is the standard normal transform corresponding to  $A^N$  and  $F_{bN}$ ;

 $S_P$  is the estimated standard deviation of population when N = 1.

and

$$F_{b(-3SN)} = F_{b1} - Z_{(A,-3\sigma)} S_{P}$$
 (F.4)

where

 $F_{b(-3SN)}$  is the minimum (-3S) fatigue strength of a sample of chains, each with N inner link apertures;

 $F_{\rm b1}$  is the median (mean) fatigue strength of a sample of chains, each with one inner link aperture;

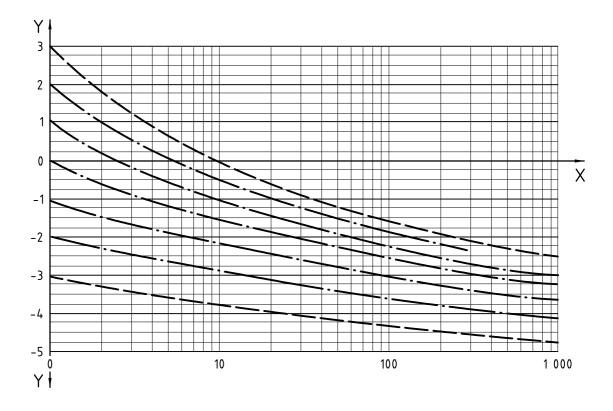
 $Z_{(A,-3\sigma)}$  is the standard normal transform corresponding to  $A^N$  and  $F_{b(-3SN)}$ .

The standard deviation of the population ( $S_P$ ) is estimated by simultaneously solving Equations (F.3) and (F.4). This calculation is an approximation of  $S_P$  because the interval between standard deviations is not uniform.

Finally, the mean and minimum fatigue limit of a chain of any length may be estimated by substituting the appropriate values for  $F_{\rm b1}$ ,  $S_{\rm P}$ ,  $Z_{(A,F{\rm b})}$ , and  $Z_{(A,-3\sigma)}$ .

Table F.1 — Adjusted probabilities ( $A^N$ ) for specimen size (N)

	+10	Z	350 3,000	1,790	82 0,872	815 0,157	81 –0,193	76 –0,417	648 -0,579	29 –0,704	908'0- 06	435 -0,891	313 –0,963	31 -1,027	20 –1,258	23 –1,410	59 –1,523	25 –1,611	99 –1,684	543 -1,745	01 –1,845	844 –1,924	215 -2,018	13 –2,093	617 –2,135	872 –2,222	
		$A^N$	0,001	0,036 742	0,191682	0,437	2 0,576 581	4 0,661 676	0,718	4 0,759 329	4 0,789 790	0,813	0,832	9 0,847 731	6 0,895 720	3 0,920 723	5 0,936 059	6 0,946 425	2 0,953 899	0,959	1 0,967 501	0,972	0,978	0,981813	0,983	0,986	
	$+2\sigma$	Z	50 2,000	31 1,033	70 0,284	93 -0,314	95 -0,612	26 –0,804	55 -0,945	33   -1,054	16 –1,144	96 –1,219	15 -1,283	55 -1,339	94 -1,546	11 -1,683	875 -1,785	35 -1,866	39 -1,932	32   -1,989	52 -2,081	30 –2,154	39 –2,240	16 –2,310	37 –2,349	32   -2,431	-
		$A^N$	0,022 750	0,150831	0,388 370	0,623 193	0,729 595	0,789 426	0,827 655	0,854 163	0,873 616	0,888 496	0,900 245	0,909 755	0,938 894	0,953 811	0,962 87	0,968 965	0,973 339	0,976 632	0,981 262	0,984 360	0,987 469	0,989 546	0,990 587	0,992 462	
٠٠٠	+3 $\sigma$	Z	55 1,000	16 0,258	22 –0,335	32 –0,822	71 –1,070	90 –1,234	59 -1,354	59 -1,448	34 –1,525	92 –1,590	16 –1,646	18 –1,696	32 –1,878	50   -2,000	58 –2,091	75 –2,164	36   -2,224	30   -2,275	37   -2,359	58 –2,426	32 –2,505	99 –2,569	38 –2,605	25 -2,681	
	•	$A^N$	0,158 655	0,398316	3 0,631 122	0,794432	3 0,857 771	0,891309	0,912 059	0,926 159	0,936 364	0,944 092	3 0,950 146	0,955 018	1 0,969 782	0,977 250	2 0,981 758	7 0,984 775	0,986 936	0,988 560	1 0,990 837	0,992 358	0,993 882	0,994 899	3 0,995408	0,996 325	
	$F_{b}$	Z	000'0 00	07   -0,545	96 -0,998	04 –1,385	74 –1,588	603 –1,724	936   -1,824	32   -1,904	549 –1,969	572 –2,025	30 –2,073	821 -2,116	14 –2,274	373 -2,381	92   -2,462	40 -2,527	61 -2,580	77   -2,626	40  2,701	16 –2,761	692 –2,833	76 –2,890	269 –2,923	15   -2,992	
		$A^N$	0 002:0 000	7 0,707 107	5 0,840 896	6 0,917 004	9 0,943 874	0,957	0,965	9 0,971 532	0,975	0,978	1 0,980 930	0,982	2 0,988 514	0,991	4 0,993 092	1 0,994 240	7   0,995 061	8 0,995 677	4 0,996 540	7 0,997 116	0,997	2 0,998 076	0,998	3 0,998 61	
	-10	Z	345 -1,000	.48   -1,387	31 -1,725	37 –2,026	.07 –2,189	.61 –2,299	.00   -2,382	28   -2,449	49 -2,503	16 –2,550	13 –2,591	90 -2,627	25 -2,762	43 -2,854	74 -2,924	161 –2,981	67 -3,027	121 -3,068	37 –3,134	.80 –3,187	.24 –3,251	20 -3,302	68 –3,332	55 -3,393	
		$A^N$	0,841	75 0,917 248	18 0,957 731	52 0,978 637	0,985 707	1 0,989 261	18 0,991 400	0,992 828	8 0,993 849	37 0,994 616	1 0,995 213	0,995 690	4 0,997 125	13 0,997 843	0,998 274	1 0,998 561	1 0,998 767	998 921 0,998	3 0,999 137	0,999 280	10,999 424	0,999 520	999 268	2 0,999 655	_
	$-2\sigma$	Z	250 -2,000	560 -2,275	263 –2,528	128 –2,762	)84 –2,892	563 –2,981	350 -3,048	)42 -3,103	178 –3,148	281 –3,187	361 -3,221	125 -3,251	317 –3,364	712 -3,443	770 -3,503	308 -3,551	336 -3,591	356 -3,626	385 -3,683	904 -3,730	323 –3,786	936 -3,830	942 –3,856	954 -3,912	
		$A^N$	0,977	0,988 560	9 0,994 263	128 0,997 128	9 0,998 084	1 0,998 563	0,998 850	3 0,999 042	0,999 178	0,999 281	198 0,999 361	16 0,999 425	79 0,999 617	14 0,999 712	0,999 770	808 666,0 88	75 0,999 836	0,999 856	9 0,999 885	96 0,999 904	3 0,999 923	0,999 936	0,999 942	15 0,999 954	
	$-3\sigma$	Z	50 -3,000	.25 -3,205	62 –3,399	31 –3,584	87 –3,689	16 –3,761	32 –3,816	44 -3,863	52 –3,900	158 -3,930	62 –3,958	986'E- 986	77 –4,079	183 -4,144	186 -4,200	189 -4,238	90 -4,275	92 -4,303	93 -4,359	94 -4,396	95 -4,433	96 –4,470	97 –4,508	97 -4,545	
		$A^N$	0,998 650	0,999 325	0,999 662	0,999 831	2 0,999 887	0,999 916	0,999 932	1 0,999 944	3 0,999 952	936 666 0	0,999 962	996 666'0	0,999 977	0,999 983	986 666'0 0	0,999 989	066 666'0 0	0   0,999 992	0   0,999 993	0 0,999 994	0,999 995	966 666'0 0	0 999 997	0   0,999 997	
	>	<b>^</b> 7	_	7	4	8	12	16	20	24	28	32	36	40	09	80	100	120	140	160	200	240	300	360	400	200	



#### Key

- X specimen size, N
- Y adjusted probability, standard normal transform units, Z

Figure F.1 — Adjusted probabilities ( $A^N$ ) for specimen size (N)

#### F.2.2 Sample size

When establishing chain application fatigue ratings, the sample selected for staircase testing should be sufficient to minimize statistical error.

## F.2.3 Sample representativeness

When establishing chain application fatigue ratings, the sample selected for staircase testing should be representative of more than one production batch.

A staircase test for establishing chain application fatigue ratings should contain at least thirty specimens, equally representing at least three different production batches.

## F.3 Other factors

#### F.3.1 Statistical limits

The definition of fatigue limit states that there is a 0,135 % probability of failure at 10<sup>7</sup> cycles. The probability of failure is small, but does exist. Either users should be warned of this possibility of fatigue failure, or the chain producer should make additional compensation for it.

## F.3.2 Fatigue life

Limited testing shows there are some link plate fatigue failures beyond 10<sup>7</sup> cycles, which indicates that the slope of the F-N line beyond 10<sup>7</sup> cycles may not be quite zero (or  $\infty$ ). A chain still may fail no matter how carefully selected and maintained. No clear directive can be given on this, but both users and producers should be aware of this possibility of fatigue failure.

#### F.3.3 Wear

Testing indicates that chain and sprocket wear can reduce the fatigue strength and life of transmission chain. Great variation virtually precludes the prediction of wear effects, but here again, both users and producers should be aware of the possibility of fatigue failure.

#### F.3.4 Unidentified factors

Many other factors, not listed here, may affect the fatigue life of transmission chain. One common way to treat them is by clearly enumerating the drive conditions under which the ratings apply and exclude everything else.

## F.4 Sample calculations

In this example, each of the three production batches had low variation (3-step staircases), but the means differed by about two steps. The constructed thirty-test staircase appears as follows:

Test force N														S	tair	cas	е													
19 450					х		х																							
17 600		х		0		0		х		х		х						х												
15 750	0		0						0		0		х		х		0		х		х		х				х			
13 900														0		o				0		0		х		0		х		О
12 050																									0				0	

Basic statistics for this staircase are

- mean fatigue strength,  $F_b$  = 15 688;
- standard deviation, S = 1880;
- minimum fatigue strength,  $F_{b-3S}$  = 10 048;
- fatigue limit:  $F_{b-3S} + d = 11898$ .

In this example, test chain length was 13 pitches, with inner link each end (N = 28). Adjustments for chain length are as follows.

15 688 = 
$$F_{h1}$$
 -1,969 $S_{p}$ 

15 688 = 
$$F_{b1}$$
 -1,969 $S_{p}$  a)  $F_{b1}$  = 15 688 + 1,969 (1 963)

11 898 = 
$$F_{b1}$$
 -3,900 $S_{p}$  b)  $F_{b1}$  = 19 553

b) 
$$F_{b1} = 19553$$

Subtracting b) from a) gives

$$3790 = 1,931S_P$$

$$1963 = S_{P}$$

So, for a drive chain one hundred pitches long:

- mean fatigue strength,  $F_{b200}$  = 19 553 2,701 (1 963) = 19 553 5 302 = 14 251;
- minimum fatigue limit,  $F_{b(-3S200)} = 19553 4,359(1963) = 19553 8557 = 10996$ .

And, for a drive chain one hundred twenty pitches long:

- mean fatigue strength,  $F_{b240}$  = 19 553 2,761 (1 963) = 19 553 5 420 = 14 133;
- minimum fatigue limit,  $F_{b(-3S240)} = 19553 4,396 (1963) = 19553 8629 = 10924$ .

## Annex G

(informative)

## Extrapolating fatigue strength from $3 \times 10^6$ cycles to $10^7$ cycles

#### G.1 General

Endurance for the conformity test is  $3 \times 10^6$  cycles, while endurance for the fatigue limit is  $10^7$  cycles. It follows then that a method is needed to extrapolate from a conformity test value at  $3 \times 10^6$  cycles to a corresponding fatigue limit at 10<sup>7</sup> cycles. This annex gives one method of doing that.

## G.2 Test data

Several staircase fatigue test series for 16A chain were selected, for nearly identical means and variances. Endurance for all test series was 10<sup>7</sup> cycles. All test chains were thirteen free pitches long with an inner link at each end.

The fatigue tests were run on a Schenck, 10-tonne, mechanical harmonic-spring, axial tensile fatigue testing unit. Minimum force was 2 225 N throughout all test series. Test forces, corrected to zero minimum force, were 13 900 N, 15 750 N, 17 600 N, 19 450 and 21 300 N. Step size was 1 850 N.

#### G.3 Constructed staircases

## **G.3.1 Phantom points**

All of the test data were from tests run to  $10^7$  cycles. Staircases, with endurance set at  $5 \times 10^6$  cycles and  $3 \times 10^6$  cycles, were synthesized from that original data. When endurance was set at  $5 \times 10^6$  cycles and  $3 \times 10^6$  cycles, some of the failures in the tests run to  $10^7$  cycles became run-outs at the lesser endurance.

There were not enough test points at higher force levels to complete a synthesized staircase, so phantom points were added. All phantom test points were assumed to be failures to make the analysis conservative.

Some data points at lower force levels had to be discarded because there were not sufficient data points at the next higher level to justify their inclusion in the synthesized staircase.

### G.3.2 Constructed staircase with endurance at 10<sup>7</sup> cycles

A staircase was constructed from the selected test data with endurance at 107 cycles. This constructed staircase contained seventy-six data points on four force levels.

## G.3.3 Constructed staircase with endurance at $5 \times 10^6$ cycles

Next, endurance was set at  $5 \times 10^6$  cycles for the staircase data in G.3.2. Two of the failures at the 19 450 N force level became run-outs, six of the failures at the 17 600 N force level became run-outs, and two of the failures at the 15 750 N force level became run-outs. Following the guidelines in G.3.1, two phantom points were added at the 21 300 N force level and eight phantom points were added at the 19 450 N force level. Eight tests were discarded at the 15 750 N force level and two tests were discarded at the 13 900 N force level.

### G.3.4 Constructed staircase with endurance at $3 \times 10^6$ cycles

Finally, endurance was set at  $3 \times 10^6$  cycles for the staircase data in G.3.2. Three of the failures at the 19 450 N force level became run-outs, eight of the failures at the 17 600 N force level became run-outs, and two of the failures at the 15 750 N force level became run-outs. Following the guidelines in G.3.1, three phantom points were added at the 21 300 N force level and ten phantom points were added at the 19 450 N force level. Ten tests were discarded at the 15 750 N force level and two tests were discarded at the 13 900 N force level.

#### G.3.5 Sample staircases and histograms

Sample staircases are shown in Figure G.1. Sample histograms are shown in Figure G.2.

## G.4 Staircase analysis

#### G.4.1 Means

Only the mean fatigue strength was calculated for each constructed staircase. Standard deviations were not calculated because the addition of the phantom points could make them unreliable.

The calculated mean fatigue strengths were 16 724 N for endurance at  $10^7$  cycles, 17 308 N for endurance at  $5 \times 10^6$  cycles, and 17 456 N for endurance at  $3 \times 10^6$  cycles.

#### G.4.2 Differences

Mean fatigue strength was 3,5 % higher with endurance at  $5 \times 10^6$  cycles, and 4,4 % higher with endurance at  $3 \times 10^6$  cycles. The slope of the Log F-Log N line could have been determined by taking the slope from  $3 \times 10^6$  to  $10^7$  cycles, the slope from  $5 \times 10^6$  to  $10^7$  cycles, or an average of the two. It was decided to use the slope from  $3 \times 10^6$  to  $10^7$  cycles because the dynamic strength requirements in ISO 10190 were set at  $3 \times 10^6$  cycles, and that slope appeared to best fit the failure data.

## G.4.3 Fatigue test staircases for 16A chain

Endurance =  $10^7$  cycles

AVG FS = 16 724

Staircase Force

Ν

19450	Т	П	Т	Τ	Х	Т	T	T	Τ	Х	(		Γ		1	K	Τ	Τ	Γ		X	T	Τ	Τ		X	Х		х	)	4	х		Т	Γ	П			Т	Τ		П	П		T	Τ	Γ	П	Τ	Τ	Τ		Т	Τ		1
17600	Τ	П	Τ	0	П	х	T	Τ	(	)	Х		Γ	П	0	)	¢	Τ	Γ	0		х	Τ	Γ	0	-	0	0		0	О		Х	Τ	Γ	Γ		х	)	(	х		х	1	Κ	Х		х	)	K	х		x	Х		X
15750	Τ	х	0		П		X	(	0	Ι	Ι	Х		0		Τ	)	Ċ	0			2	K	0			Τ		П	Ι	Τ			X	х		0	(	0	0	)	0		0	0	)	0		0	C	)	0	(	)	0	]
13900	0	П	0	Τ	П	T	-	0	T	Т	Τ	Γ	0	П	T	T	Τ	0	Г	Π	T	T	С	ī	Π	T	Т	Γ	Π	Т	Т	П	П	0	1	0	П	T	Т	Τ	Τ	П	Π	T	Т	Τ	Τ	П	Т	Т	Т	П	Т	Т	Π	1

a)

Endurance =  $5 \times 10^6$  cycles

AVG FS = 17 308

+3,5%

**Force** Staircase

Ν

21300	)	П	П	Τ	Ι	#				I	Τ	Ι	į	Ħ	Ι	Ι	Ι	Ι	Ι	Ι	Ι	Γ	Ι	Γ				Π	Ι	Τ	Ι	Τ					Ι	Ι	Ι	Γ	Γ					Ι	Ι	Ι	Γ				Τ	Ι			Τ	Ι	Ι	
19450	)	П	П	Τ	0		Х			Т	T	(	D	1	X	Τ	Τ	Ι	Ι	×	(	Γ	Ι	Γ	Γ	Х		T	T	Τ	)	4			Х		T	3	X	Γ	Γ	#	П		į	#	Τ	Ι	#				#	Τ		#	Т	Τ	#	П
17600	)	П	П	c	)			х		I	(	Ó	T	Ι	2	<	Τ	Ι	c	)	Х		Γ	Γ	0		X	Т	Ι	(	)	X		0		X	(	)	X	(	0		х		0	2	K	0	Γ	х		Ó	)	K	0		X	0	)	×
15750	1	х	П	0	Τ				х	1	0	Τ	T	Т	Τ	)	ď	C	1	Τ	Τ	х		0	Γ	Г	П	х	(	9	Τ	Τ	0			П	0	T	Τ	0		Γ	П	0	Т	T	0	)	Γ	Γ	0	П	T	C	)	П	(		Τ	П
13900	0	)	0	Ι	Ι					0	Ι	Ι	I	Ι	Ι	Ι	0	)	Ι	Ι	Ι	Ι	0	)					0	Ι	Ι	Ι					$\perp$	Ι	Ι	Ι	Γ	L				Ι	Ι	Ι	Ι				$\Box$	Ι			Ι	Ι	Ι	

b)

Endurance =  $3 \times 10^6$  cycles

AVG FS = 17 456

+4,4%

Staircase **Force** 

Ν

ſ	2130	0							#						T	T	;	¥								#														T			T	T	Τ	Τ		T											T								Τ
Г	1945	0						0		Х		Γ	Γ	Γ	Τ	(	Ó		X		П				0		X						Х			Т	Т	1	X	Τ	Τ	3	4	Τ	Τ	Ħ	ŧ	Τ	Γ	#			i	Ħ	T	T	į	¥	Τ	Τ	#	ŧ			#	Т	Τ
Г	1760						0			Г	х	Γ	Γ	Γ	C	)	T	Т		X	П		П	0				х				Ó		X		Т		0	)	(	(	Ó	)	(	Ó	)	>	(	0		Х		Ó	T	X	(	Ó	2	K	¢	)	Х		0		х	0
Г	1575	0		X		0		Г	Г	Γ	Г	Х		¢	)	Τ	T	Т	Т		X		0	П					х		0				Х		0	Т	Τ	(	0	Τ	Τ	0	Ó	Γ	Τ	C	)	Γ		0	П	Т	T	0	Τ	Τ	(	)	Τ	Γ	0			0	)
E	1390	0	0		0					Γ		Γ	Ó	)	Τ	T	T	1				0								0						0		T	T	Τ	T	T	T	Τ	Τ	Γ	Τ	Τ	Γ					T	T	T	T	T	T	T	Ι	Γ				Т	Τ

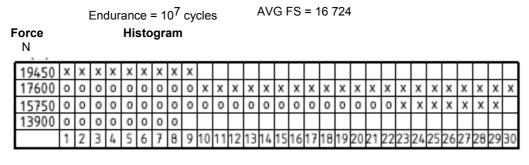
c)

## Key

- failure
- run-out
- assumed failure

Figure G.1 — Sample staircases

## G.4.4 Fatigue test histograms for 16A chain



a)

Endurance =  $5 \times 10^6$  cycles AVG FS = 17 308 +3.5% Force Histogram Ν 21300 # 19450 0 0 15750 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 x x х 13900 0 0 0 0 0 1 2 3 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27

b)

Endurance =  $3 \times 10^6$  cycles AVG FS = 17 456 +4,4%

Force Histogram

21300	#	#	#																											
19450	0	0	0	Х	Х	Х	Х	Х	Х	#	#	#	#	#	#	#	#	#	#											
17600	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	Х	Х	Х	Х	х	Х	х	Х	х	х	Х	х	Х
15750	0	0	0	0	0	0	0	0	0	0	0	0	0	0	х	Х	Х	Х	Х											
13900	0	0	0	0	0	0																								
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30

c)

## Key

- x failure
- o run-out
- # assumed failure

Figure G.2 — Sample histograms

# Annex H

(informative)

## Finite life testing and data analysis

#### H.1 General

Finite life testing and analysis is used to determine the relationship between force and cycles to failure at numbers of cycles less than the inflection point.

## **H.2 Test procedure**

## H.2.1 Test specimens

At least 14 test specimens shall be prepared in accordance with Clause 6. All test specimens shall be from the same production batch.

Additional test specimens should be provided for preliminary or invalid tests.

#### **H.2.2 Inflection point**

The inflection point is that point at which the cycles to failure begin to increase rapidly with a small decrease in force. It is near 10<sup>6</sup> cycles for roller chain.

#### H.2.3 Force levels

#### H.2.3.1 Number of force levels

There shall be at least two, but not more than four, force levels in a finite life test.

#### H.2.3.2 Values of force levels

The maximum test force shall not be more than 60 % of the minimum tensile strength listed in ISO 606 or ISO 10190.

The minimum test force shall be sufficient to produce all failures before endurance. The minimum test force should be sufficient to produce all failures before 10<sup>6</sup> cycles.

The interval between neighbouring force levels should be as nearly equal as possible.

#### H.2.4 Number of tests

A minimum of fourteen specimens shall be tested. As near an equal number of tests as possible shall be tested at each force level. Recommended numbers of tests at each force level are

- seven specimens at each of two force levels,
- five, five and four specimens at each of three force levels, and
- four, four, three and three specimens at each of four force levels.

## H.3 Data analysis

#### H.3.1 Data

The data for a finite life analysis shall be gathered in accordance with H.2.

#### H.3.2 Statistical distributions

The distribution of fatigue life, at a given force level, is well described by a log-normal distribution. The distribution of force, at a given fatigue life (number of cycles), is adequately described by either a normal or log-normal distribution. Either a normal or log-normal distribution of force may be chosen for analysis.

#### H.3.3 Determining force–life (F-N) lines

#### H.3.3.1 General relationships

The relationship between the force, or the logarithm of force, and the logarithm of fatigue life is essentially linear between 10<sup>4</sup> and 10<sup>6</sup> cycles. The relationship of fatigue life at any applied force within the stated limits may be estimated by a regression analysis.

#### H.3.3.2 Mean regression line: 0,50 probability of survival

#### H.3.3.2.1 Normal force distribution

If a normal distribution of force is chosen for analysis, the mean regression line shall be estimated by means of Equations (H.1), (H.2), and (H.3).

The relationship between mean fatigue life N and applied force  $F_a$ , between  $10^4$  and  $10^6$  cycles, is

$$N = \exp_{10} (\lg N_0 + m_{\rm F} F_{\rm a}) \tag{H.1}$$

The slope of the line is

$$m_{\mathsf{F}} = \frac{n_{\mathsf{f}} \Sigma F_{\mathsf{t}i} \lg N_{\mathsf{i}} - \Sigma F_{\mathsf{t}i} \Sigma \lg N_{\mathsf{i}}}{n_{\mathsf{\Sigma}} (F_{\mathsf{t}i})^2 - (\Sigma F_{\mathsf{t}i})^2} \tag{H.2}$$

and the X-intercept, or number of cycles, at zero force is

$$N_0 = \exp_{10}\left(\frac{\Sigma \lg N_i - m_F \Sigma F_{ti}}{n_f}\right) \tag{H.3}$$

#### H.3.3.2.2 Log-normal force distribution

If a log-normal distribution of force is chosen for analysis, the mean regression line shall be estimated by means of Equations (H.4), (H.5), and (H.6).

The relationship between mean fatigue life N and applied force  $F_a$ , between 10<sup>4</sup> and 10<sup>6</sup> cycles, is

$$N = \exp_{10} \left( \lg N_0 + m_{\rm LF} \lg F_a \right) \tag{H.4}$$

## ISO 15654:2004(E)

The slope of the line is

$$m_{\mathsf{LF}} = \frac{n_{\mathsf{f}} \Sigma (\lg F_{\mathsf{t}i} \lg N_i) - \Sigma \lg F_{\mathsf{t}i} \Sigma \lg N_i}{n_{\mathsf{f}} \Sigma (\lg F_{\mathsf{t}i})^2 - (\Sigma \lg F_{\mathsf{t}i})^2} \tag{H.5}$$

and the X-intercept, or number of cycles, at one unit force is

$$N_{1} = \exp_{10} \left[ \frac{\Sigma \lg N_{i} - m_{\text{LF}} \Sigma \lg F_{\text{t}i}}{n_{\text{f}}} \right]$$
 (H.6)

#### H.3.3.3 Minimum regression line: 0,97725 ( $-2\sigma$ ) probability of survival

#### H.3.3.3.1 Normal force distribution

If a normal distribution of force is chosen for analysis, the minimum regression line shall be estimated by means of Equations (H.7) and (H.8).

The standard deviation of the logarithm of fatigue life from the mean line, between 10<sup>4</sup> and 10<sup>6</sup> cycles, is

$$S_{\text{lg}N} = \left[\frac{\Sigma \lg N_i^2 - \lg N_0 \Sigma \lg N_i - m_F \Sigma \left(\lg N_i F_{ti}\right)}{n_f - 2}\right]^{0.5} \tag{H.7}$$

and the relationship between minimum fatigue life  $N_{min}$  and applied force  $F_a$ , between 10<sup>4</sup> and 10<sup>6</sup> cycles, with a 0,97725 probability of survival, is

$$N_{\min} = \exp_{10} \left( \lg N_0 - 2S_{\lg N} + m_F F_a \right)$$
 (H.8)

#### H.3.3.3.2 Log-normal force distribution

If a log normal distribution of force is chosen for analysis, the minimum regression line shall be estimated by means of Equations (H.9) and (H.10).

The standard deviation of the logarithm of fatigue life from the mean line, between 10<sup>4</sup> and 10<sup>6</sup> cycles, is

$$S_{\text{lg}N} = \left[ \frac{\Sigma \lg N_i^2 - \lg N_0 \Sigma \lg N_i - m_{\text{LF}} \Sigma \left( \lg N_i \lg F_{\text{t}i} \right)}{n_{\text{f}} - 2} \right]^{0.5} \tag{H.9}$$

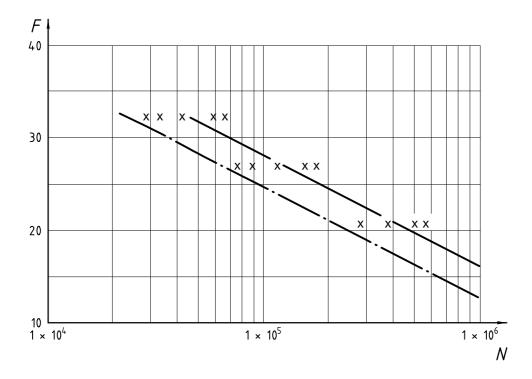
and the relationship between minimum fatigue life  $N_{L,min}$  and applied force  $F_a$  between 10<sup>4</sup> and 10<sup>6</sup> cycles, with a 0,97725 probability of survival, is

$$N_{L,min} = \exp_{10} \left( \lg N_0 - 2S_{\lg N} + m_{LF} \lg F_a \right)$$
 (H.10)

#### H.4 Sample test results

A finite life test was conducted on "BCD Company's" number 16A chain, consisting of 14 tests run on three force levels. The results are shown on the sample test result form which follows and, graphically, in Figures H.1 and H.2.

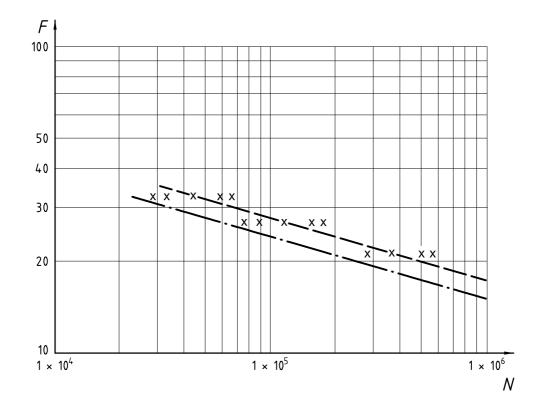
			Fa	itigue test r	eport				
		Repor	t No.:	<u>1002</u>	<u>Pag</u>	ge 1 of 1	Report of	date: <u>200</u>	03-06-9
Chain:									
Brand:		Number:		Pitch:	Specin	nen length:	Other:		
BCD Chain		16A		25,4 mm	13P,IL	EE			
Mechanical	properties:				•				
Not taken									
Test:									
Туре:		Endurance:		Temperatu	re:		Other:		
Finite life				Approx. 15	°C		Low humid	ity	
Machine:									
Brand:		Type:		No. used:	Calibra	ation date:	Force verif		d
XYZ		Mech., harm	onic spring	1	2002-0	8-26	monitoring:		
	T					l	Periodic, st		
Date	Test No.	Frequency	$F_{\sf max}$	$F_{min}$	$F_{t}$	Cycles, N	Failure	Rem	arks
		Hz	kN	kN	kN				
03-05-30	001	33	33,36	2,224	32,44	4,500E4	IP		
03-05-30	002	33	33,36	2,224	32,44	6,750E4	IP		
03-05-30	003	33	33,36	2,224	32,44	3,375E4	IP		
03-05-30	004	33	33,36	2,224	32,44	2,925E4	IP		
03-05-31	005	33	33,36	2,224	32,44	5,980E4	IP		
03-05-31	006	33	27,80	2,224	26,64	1,596E5	IP		
03-05-31	007	33	27,80	2,224	26,64	9,000E4	IP		
03-06-01	800	33	27,80	2,224	26,64	7,800E4	IP		
03-06-01	009	33	27,80	2,224	26,64	1,800E5	IP		
03-06-01	010	33	27,80	2,224	26,64	1,200E5	IP		
03-06-05	011	33	22,24	2,224	20,85	3,845E5	IP		
03-06-05	012	33	22,24	2,224	20,85	2,884E5	IP		
03-06-06	013	33	22,24	2,224	20,85	5,770E5	IP		
03-06-07	014	33	22,24	2,224	20,85	5,114E5	IP		
Results an	d conclusion	ons:							
m	<i>i</i> <sub>F</sub> = -	0,083 94				$m_{LF}$	= -5,094 2	25	
lg	$y N_0 = 7$	7,353 5				$\lg\!N_1$	= 12,345 (	06	
S	$_{lgN}$ = 0	,143 88				$S_{lgN}$	= 0,143 88	3	
	•	-life test are pl	otted on the	attached gr	aphs [se	ū	.1 and H.2].		
		•		-			-		
					Sianed	l: <u>John Sm</u>	nith		



## Key

F force, kN N life, cycles

Figure H.1 — Typical F-Log N graph for 16A chain



#### Key

F force, kN N life, cycles

Figure H.2 — Typical Log F-Log N graph for 16A chain

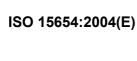
# **Bibliography**

- [1] ISO 10823, Guidelines for the selection of roller chain drives 1)
- [2] ISO 1099, Metallic materials Fatigue testing Axial force controlled method <sup>2)</sup>

47

<sup>1)</sup> To be published. (Revision of ISO 10823:1996)

<sup>2)</sup> To be published. (Revision of ISO 1099:1975)



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