# INTERNATIONAL STANDARD

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# Calculation of load capacity of spur and helical gears —

Part 3: Calculation of tooth bending strength

dentures droite et hélicoïdale —

Calcul de la capacité de charge des engrenages cylindriques à

Partie 3: Calcul de la résistance à la flexion en pied de dent



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Case postale 56 • CH-1211 Geneva 20
Tel. + 41 22 749 01 11
Fax + 41 22 749 09 47
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#### **Foreword**

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 2.

The main task of technical committees is to prepare International Standards. Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75 % of the member bodies casting a vote.

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights.

ISO 6336-3 was prepared by Technical Committee ISO/TC 60, Gears, Subcommittee SC 2, Gear capacity calculation.

This second edition cancels and replaces the first edition (ISO 6336-3:1996), Clauses 5 and Clause 9 of which have been technically revised, with a new Clause 8 having been added to this new edition. It also incorporates the Technical Corrigendum ISO 6336-3:1996/Cor.1:1999.

ISO 6336 consists of the following parts, under the general title *Calculation of load capacity of spur and helical gears*:

- Part 1: Basic principles, introduction and general influence factors
- Part 2: Calculation of surface durability (pitting)
- Part 3: Calculation of tooth bending strength
- Part 5: Strength and quality of materials
- Part 6: Calculation of service life under variable load

This corrected version incorporates the following corrections:

- Figure 3 has been updated;
- in Equation (17), the missing lines denoting the absolute value,  $Z_n$ , have been inserted;
- minus signs missing from Equations (18) and (19) have been inserted;
- Equation (50) has been corrected.

#### Introduction

The maximum tensile stress at the tooth root (in the direction of the tooth height), which may not exceed the permissible bending stress for the material, is the basis for rating the bending strength of gear teeth. The stress occurs in the "tension fillets" of the working tooth flanks. If load-induced cracks are formed, the first of these often appears in the fillets where the compressive stress is generated, i.e. in the "compression fillets", which are those of the non-working flanks. When the tooth loading is unidirectional and the teeth are of conventional shape, these cracks seldom propagate to failure. Crack propagation ending in failure is most likely to stem from cracks initiated in tension fillets.

The endurable tooth loading of teeth subjected to a reversal of loading during each revolution, such as "idler gears", is less than the endurable unidirectional loading. The full range of stress in such circumstances is more than twice the tensile stress occurring in the root fillets of the loaded flanks. This is taken into consideration when determing permissible stresses (see ISO 6336-5).

When gear rims are thin and tooth spaces adjacent to the root surface narrow (conditions which can particularly apply to some internal gears), initial cracks commonly occur in the compression fillet. Since, in such circumstances, gear rims themselves can suffer fatigue breakage, special studies are necessary. See Clause 1.

Several methods for calculating the critical tooth root stress and evaluating some of the relevant factors have been approved. See ISO 6336-1.

# Calculation of load capacity of spur and helical gears —

#### Part 3:

# Calculation of tooth bending strength

IMPORTANT — The user of this part of ISO 6336 is cautioned that when the method specified is used for large helix angles and large pressure angles, the calculated results should be confirmed by experience as by Method A.

#### 1 Scope

This part of ISO 6336 specifies the fundamental formulae for use in tooth bending stress calculations for involute external or internal spur and helical gears with a rim thickness  $s_R > 0.5 h_t$  for external gears and  $s_R > 1.75 m_n$  for internal gears. In service, internal gears can experience failure modes other than tooth bending fatigue, i.e. fractures starting at the root diameter and progressing radially outward. This part of ISO 6336 does not provide adequate safety against failure modes other than tooth bending fatigue. All load influences on tooth stress are included in so far as they are the result of loads transmitted by the gears and in so far as they can be evaluated quantitatively.

The given formulae are valid for spur and helical gears with tooth profiles in accordance with the basic rack standardized in ISO 53. They may also be used for teeth conjugate to other basic racks if the virtual contact ratio  $\varepsilon_{on}$  is less than 2,5.

The load capacity determined on the basis of permissible bending stress is termed "tooth bending strength". The results are in good agreement with other methods for the range, as indicated in the scope of ISO 6336-1.

#### 2 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 53:1998, Cylindrical gears for general and heavy engineering — Standard basic rack tooth profile

ISO 1122-1:1998, Vocabulary of gear terms — Part 1: Definitions related to geometry

ISO 6336-1:2006, Calculation of load capacity of spur and helical gears — Part 1: Basic principles, introduction and general influence factors

ISO 6336-5:2003, Calculation of load capacity of spur and helical gears — Part 5: Strength and quality of material

#### 3 Terms, definitions, symbols and abbreviated terms

For the purposes of this document, the terms, definitions, symbols and abbreviated terms given in ISO 1122-1 and ISO 6336-1 apply.

#### 4 Tooth breakage and safety factors

Tooth breakage usually ends the service live of a transmission. Sometimes, the destruction of all gears in a transmission can be a consequence of the breakage of one tooth. In some instances, the transmission path beween input and output shafts is broken. As a consequence, the chosen value of the safety factor  $S_F$  against tooth breakage should be larger than the safety factor against pitting.

General comments on the choice of the minimum safety factor can be found in ISO 6336-1:2006, 4.1.7. It is recommended that manufacturer and customer agree on the value of the minimum safety factor.

This part of ISO 6336 does not apply at stress levels above those permissible for 10<sup>3</sup> cycles, since stresses in this range may exceed the elastic limit of the gear tooth.

#### 5 Basic formulae

The actual tooth root stress  $\sigma_F$  and the permissible (tooth root) bending stress  $\sigma_{FP}$  shall be calculated separately for pinion and wheel;  $\sigma_F$  shall be less than  $\sigma_{FP}$ .

#### 5.1 Safety factor for bending strength (safety against tooth breakage), $S_{\mathsf{F}}$

Calculate  $S_{\mathsf{F}}$  separately for pinion and wheel:

$$S_{\mathsf{F1}} = \frac{\sigma_{\mathsf{FG1}}}{\sigma_{\mathsf{F1}}} \geqslant S_{\mathsf{Fmin}} \tag{1}$$

$$S_{\mathsf{F2}} = \frac{\sigma_{\mathsf{FG2}}}{\sigma_{\mathsf{F2}}} \geqslant S_{\mathsf{Fmin}} \tag{2}$$

 $\sigma_{F1}$  and  $\sigma_{F2}$  are derived from Equations (3) and (4). The values of  $\sigma_{FG}$  for reference stress and static stress are calculated in accordance with 5.3.2.1 and 5.3.2.2, using Equation (5). For limited life,  $\sigma_{FG}$  is determined in accordance with 5.3.3.

The values of tooth root stress limit  $\sigma_{FG}$ , of permissible stress  $\sigma_{FP}$  and of tooth root stress  $\sigma_{F}$  may each be determined by different methods. The method used for each value shall be stated in the calculation report.

NOTE Safety factors in accordance with the present clause are relevant to transmissible torque.

See ISO 6336-1:2006, 4.1.7 for comments on numerical values for the minimum safety factor and risk of damage.

#### 5.2 Tooth root stress, $\sigma_{\rm F}$

Tooth root stress  $\sigma_{\rm F}$  is the maximum tensile stress at the surface in the root.

#### 5.2.1 Method A

In principle, the maximum tensile stress can be determined by any appropriate method (finite element analysis, integral equations, conformal mapping procedures or experimentally by strain measurement, etc.). In order to determine the maximum tooth root stress, the effects of load distribution over two or more engaging teeth and changes of stress with changes of meshing phase shall be taken into consideration.

Method A is only used in special cases and, because of the great effort involved, is only justifiable in such cases.

#### 5.2.2 Method B

According to this part of ISO 6336, the local tooth root stress is determined as the product of nominal tooth root stress and a stress correction factor <sup>1)</sup>.

This method involves the assumption that the determinant tooth root stress occurs with application of load at the outer point of single pair tooth contact of spur gears or of the virtual spur gears of helical gears. However, in the latter case, the "transverse load" shall be replaced by the "normal load", applied over the facewidth of the actual gear of interest.

For gears having virtual contact ratios in the range  $2 \leqslant \varepsilon_{\alpha n} < 2.5$ , it is assumed that the determinant stress occurs with application of load at the inner point of triple pair tooth contact. In ISO 6336, this assumption is taken into consideration by the deep tooth factor,  $Y_{\text{DT}}$ . In the case of helical gears, the factor,  $Y_{\beta}$ , accounts for deviations from these assumptions.

Method B is suitable for general calculations and is also appropriate for computer programming and for the analysis of pulsator tests (with a given point of application of loading).

The total tangential load in the case of gear trains with multiple transmission paths (planetary gear trains, split-path gear trains) is not quite evenly distributed over the individual meshes (depending on design, tangential speed and manufacturing accuracy). This is to be taken into consideration by inserting a mesh load factor,  $K_{\nu}$  to follow  $K_{\rm A}$  in Equation (3), in order to adjust as necessary the average load per mesh.

$$\sigma_{\mathsf{F}} = \sigma_{\mathsf{F}0} \ K_{\mathsf{A}} \ K_{\mathsf{V}} \ K_{\mathsf{F}\beta} \ K_{\mathsf{F}\alpha} \tag{3}$$

where

 $\sigma_{\text{F0}}$  is the nominal tooth root stress, which is the maximum local principal stress produced at the tooth root when an error-free gear pair is loaded by the static nominal torque and without any pre-stress such as shrink fitting, i.e. stress ratio R = 0 [see Equation (4)];

 $\sigma_{\text{FP}}$  is the permissible bending stress (see 5.3);

*K*<sub>A</sub> is the application factor (see ISO 6336-6), which takes into account load increments due to externally influenced variations of input or output torque;

 $K_{v}$  is the dynamic factor (see ISO 6336-1), which takes into account load increments due to internal dynamic effects;

 $K_{\text{F}\beta}$  is the face load factor for tooth root stress (see ISO 6336-1), which takes into account uneven distribution of load over the facewidth due to mesh-misalignment caused by inaccuracies in manufacture, elastic deformations, etc.;

 $K_{F\alpha}$  is the transverse load factor for tooth root stress (see ISO 6336-1), which takes into account uneven load distribution in the transverse direction, resulting, for example, from pitch deviations.

NOTE See ISO 6336-1:2006, 4.1.14, for the sequence in which factors  $K_A$ ,  $K_V$ ,  $K_{F\beta}$  and  $K_{F\alpha}$  are calculated.

$$\sigma_{\mathsf{F0}} = \frac{F_{\mathsf{t}}}{b_{m_{\mathsf{D}}}} \, Y_{\mathsf{F}} \, Y_{\mathsf{S}} \, Y_{\mathsf{\beta}} \, Y_{\mathsf{B}} \, Y_{\mathsf{DT}} \tag{4}$$

<sup>1)</sup> Stresses such as those caused by the shrink-fitting of gear rims, which are superimposed on stresses due to tooth loading, should be taken into consideration in the calculation of permissible tooth root stress  $\sigma_{\text{FP}}$ .

#### where

- $F_{\rm t}$  is the nominal tangential load, the transverse load tangential to the reference cylinder<sup>2</sup>) (see ISO 6336-1);
- b is the facewidth (for double helical gears  $b = 2 b_B)^{3}$ ;
- $m_{\rm p}$  is the normal module;
- Y<sub>F</sub> is the form factor (see Clause 6), which takes into account the influence on nominal tooth root stress of the tooth form with load applied at the outer point of single pair tooth contact;
- Y<sub>S</sub> is the stress correction factor (see Clause 7), which takes into account the influence on nominal tooth root stress, determined for application of load at the outer point of single pair tooth contact, to the local tooth root stress, and thus, by means of which, are taken into account;
  - i) the stress amplifying effect of change of section at the tooth root, and
  - ii) the fact that evaluation of the true stress system at the tooth root critical section is more complex than the simple system evaluation presented;
- $Y_{\beta}$  is the helix angle factor (see Clause 8), which compensates for the fact that the bending moment intensity at the tooth root of helical gears is, as a consequence of the oblique lines of contact, less than the corresponding values for the virtual spur gears used as bases for calculation;
- $Y_{\mathsf{B}}$  is the rim thickness factor (see Clause 9), which adjusts the calculated tooth root stress for thin rimmed gears;
- $Y_{\text{DT}}$  is the deep tooth factor (see Clause 10), which adjusts the calculated tooth root stress for high precision gears with a contact ratio in the range of  $2 \le \varepsilon_{on} < 2.5$ .

#### 5.3 Permissible bending stress, $\sigma_{FP}$

The limit value of tooth root stresses (see Clause 11) should preferably be derived from material tests using gears as test pieces, since in this way the effects of test piece geometry, such as the effect of the fillet at the tooth roots, are included in the results. The calculation methods provided constitute empirical means for comparing stresses in gears of different dimensions with experimental results. The closer test gears and test conditions resemble the service gears and service conditions, the lesser will be the influence of inaccuracies in the formulation of the calculation expressions.

# 5.3.1 Methods for determination of permissible bending stress, $\sigma_{\rm FP}$ — Principles, assumptions and application

Several procedures for the determination of permissible bending stress  $\sigma_{FP}$  are acceptable. The method adopted shall be validated by carrying out careful comparative studies of well-documented service histories of a number of gears.

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<sup>2)</sup> In all cases, even when  $\varepsilon_{\alpha n} > 2$ , it is necessary to substitute the relevant total tangential load as  $F_t$ . Reasons for the choice of load application at the reference cylinder are given in 6.3. See ISO 6336-1, 4.2, for definition of  $F_t$  and comments on particular characteristics of double helical gears.

<sup>3)</sup> The value b, of mating gears, is the facewidth at the root circle, ignoring any intentional transverse chamfers or tooth-end rounding. If the facewidths of the pinion and wheel are not equal, it can be assumed that the load bearing width of the wider facewidth is equal to the smaller facewidth plus such extension of the wider that does not exceed 1  $\times$  the module at each end of the teeth.

#### 5.3.1.1 Method A

By this method, the values for  $\sigma_{FP}$  or for the tooth root stress limit,  $\sigma_{FG}$ , are obtained using Equations (3) and (4) from the S-N curve or damage curve derived from results of testing facsimiles of the actual gear pair, under the appropriate service conditions.

The cost required for this method is, in general, only justifiable for the development of new products, failure of which would have serious consequences (e.g. for manned space flights).

Similarly, in line with this method, the allowable stress values may be derived from consideration of dimensions, service conditions and performance of carefully monitored reference gears.

#### 5.3.1.2 Method B

Damage curves characterized by the nominal stress number (bending),  $\sigma_{\rm F\ lim}$ , and the factor  $Y_{\rm NT}$  have been determined for a number of common gear materials and heat treatments from results of gear load or pulsator testing of standard reference test gears. Material values so determined are converted to suit the dimensions of the gears of interest, using the relative influence factors for notch sensitivity,  $Y_{\delta\ {\rm rel\ T}}$ , for surface roughness,  $Y_{\rm R\ rel\ T}$ , and for size,  $Y_{\rm X}$ .

Method B is recommended for the calculation of reasonably accurate gear ratings whenever bending strength values are available from gear tests, from special tests or, if the material is similar, from ISO 6336-5.

#### 5.3.2 Permissible bending stress, $\sigma_{EP}$ : Method B

Subject to the reservations given in 5.3.2.1 and 5.3.2.2, Equation (5) is to be used for this calculation:

$$\sigma_{\mathsf{FP}} = \frac{\sigma_{\mathsf{Flim}} Y_{\mathsf{ST}} Y_{\mathsf{NT}}}{S_{\mathsf{Fmin}}} Y_{\mathcal{S}\,\mathsf{rel}\,\mathsf{T}} Y_{\mathsf{R}\,\mathsf{rel}\,\mathsf{T}} Y_{\mathsf{X}} = \frac{\sigma_{\mathsf{FE}} Y_{\mathsf{NT}}}{S_{\mathsf{Fmin}}} Y_{\mathcal{S}\,\mathsf{rel}\,\mathsf{T}} Y_{\mathsf{R}\,\mathsf{rel}\,\mathsf{T}} Y_{\mathsf{X}} = \frac{\sigma_{\mathsf{FG}}}{S_{\mathsf{Fmin}}}$$
(5)

where

 $\sigma_{\text{F lim}}$  is the nominal stress number (bending) from reference test gears (see ISO 6336-5), which is the bending stress limit value relevant to the influences of the material, the heat treatment and the surface roughness of the test gear root fillets;

 $\sigma_{\text{FE}}$  is the allowable stress number for bending, corresponding to the basic bending strength of the un-notched test piece, under the assumption that the material condition (including heat treatment) is fully elastic

$$\sigma_{\text{FE}} = (\sigma_{\text{F lim}} Y_{\text{ST}});$$

 $Y_{ST}$  is the stress correction factor, relevant to the dimensions of the reference test gears (see 7.4);

*Y*<sub>NT</sub> is the life factor for tooth root stress, relevant to the dimensions of the reference test gear (see Clause 12), which takes into account the higher load capacity for a limited number of load cycles;

 $\sigma_{\rm FG}$  is the tooth root stress limit;

$$\sigma_{FG} = (\sigma_{FP} S_{F \min});$$

 $S_{\text{F min}}$  is the minimum required safety factor for tooth root stress (see Clause 4 and 5.1);

 $Y_{\delta \, \text{rel T}}$  is the relative notch sensitivity factor, which is the quotient of the notch sensitivity factor of the gear of interest divided by the standard test gear factor (see Clause 13) and which enables the influence of the notch sensitivity of the material to be taken into account;

- Y<sub>R rel T</sub> is the relative surface factor, which is the quotient of the surface roughness factor of tooth root fillets of the gear of interest divided by the tooth root fillet factor of the reference test gear (see Clause 14) and which enables the relevant surface roughness of tooth root fillet influences to be taken into account;
- $Y_X$  is the size factor relevant to tooth root strength (see Clause 15), which is used to take into account the influence of tooth dimensions on tooth bending strength.

#### 5.3.2.1 Permissible bending stress (reference)

The permissible bending stress (reference),  $\sigma_{\text{FP ref}}$ , is derived from Equation (5), with  $Y_{\text{NT}} = 1$  and influence factors  $\sigma_{\text{F lim}}$ ,  $Y_{\text{ST}}$ ,  $Y_{\text{O rel T}}$ ,  $Y_{\text{R rel T}}$ ,  $Y_{\text{X}}$  and  $S_{\text{F min}}$  calculated in accordance with the specified Method B.

#### 5.3.2.2 Permissible bending stress (static)

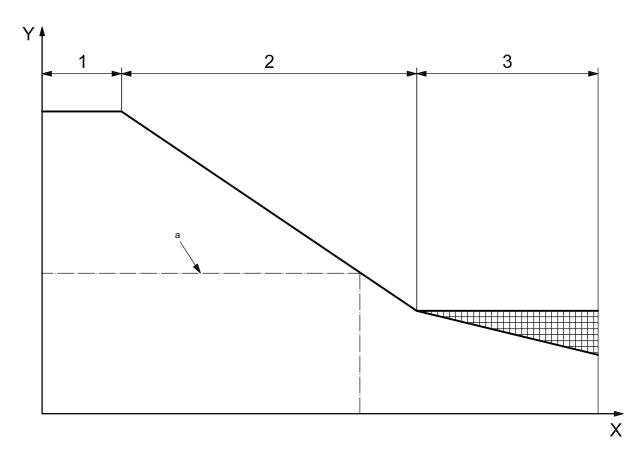
The permissible bending stress (static),  $\sigma_{\text{FP stat}}$ , is determined in accordance with Equation (5), with factors  $\sigma_{\text{F lim}}$ ,  $Y_{\text{NT}}$ ,  $Y_{\text{ST}}$ ,  $Y_{\text{ST}}$ ,  $Y_{\text{R rel T}}$ ,  $Y_{\text{X}}$  and  $S_{\text{F min}}$  calculated in accordance with the specified Method B (for static stress).

#### 5.3.3 Permissible bending stress, $\sigma_{\text{FP}}$ , for limited and long life: Method B

 $\sigma_{\text{FP}}$  for a given number of load cycles,  $N_{\text{L}}$ , is determined by means of graphical or calculated linear interpolation along the S-N curve on a log-log scale, between the value obtained for reference stress in accordance with 5.3.2.1 and the value obtained for static stress in accordance with 5.3.2.2. Also see Clause 12.

#### 5.3.3.1 Graphical values

Calculate  $\sigma_{\text{FP ref}}$  for the reference stress and  $\sigma_{\text{FP stat}}$  for the static stress in accordance with 5.3.2 and plot the S-N curve corresponding to life factor  $Y_{\text{NT}}$ . See Figure 1 for the principle.  $\sigma_{\text{FP}}$  for the relevant number of load cycles  $N_{\text{L}}$  can be read from this graph.



- X number of load cycles,  $N_L$  (log)
- Y permissible bending stress,  $\sigma_{FP}$  (log)
- 1 static
- 2 limited life
- 3 long life
- <sup>a</sup> Example: permissible bending stress,  $\sigma_{FP}$ , for a given number of load cycles.

Figure 1 — Graphical determination of permissible bending stress for limited life, in accordance with Method B

#### 5.3.3.2 Determination by calculation

Calculate  $\sigma_{\text{FP ref}}$  for the reference stress and  $\sigma_{\text{FP stat}}$  for the static stress in accordance with 5.3.2 and, using these results, determine  $\sigma_{\text{FP}}$  for the relevant number of load cycles  $N_{\text{L}}$  in the limited life range, as follows (see ISO 6336-1:2006, Table 2, for an explanation of the abbreviations used).

$$\sigma_{\text{FP}} = \sigma_{\text{FP ref}} \ Y_{\text{N}} = \sigma_{\text{FP ref}} \left( \frac{3 \times 10^6}{N_{\text{L}}} \right)^{\text{exp}}$$
 (6)

a) For St, V, GGG (perl., bai.) or GTS (perl.), limited life range as shown in Figure 9,  $10^4 < N_1 \le 3 \times 10^6$ :

$$\exp = 0{,}4037\log\frac{\sigma_{\text{FP stat}}}{\sigma_{\text{FP ref}}} \tag{7}$$

b) For IF, Eh, NT (nitr.), NV (nitr.), NV (nitrocar.), GGG (ferr.) or GG, limited life range as shown in Figure 9,  $10^3 < N_1 \le 3 \times 10^6$ :

$$\exp = 0.287 \ 6 \log \frac{\sigma_{\text{FP stat}}}{\sigma_{\text{FP ref}}}$$
 (8)

Corresponding calculations may be determined for the range of long life.

#### 6 Form factor, $Y_{\mathsf{F}}$

#### 6.1 General

 $Y_{\mathsf{F}}$  is the factor by which the influence of tooth form on nominal tooth root stress is taken into account. See 5.2.1 for principles, assumptions and details of use.  $Y_{\mathsf{F}}$  is relevant to application of load at the outer point of single pair tooth contact (Method B).

The chord between the points at which the 30° tangents contact the root fillets for external gears, or at which the 60° tangents contact the root fillets for internal gears, defines the section to be used as the basis for calculation (see Figures 3 to 4).

Determination of the values  $Y_F$  and  $Y_S$  is based on the nominal tooth form with the profile shift coefficient x. In general, the effect of reduction of tooth thickness on the tooth bending strength of finished-cut cylindrical gears may be ignored. Since the tooth roots of ground or shaved gear teeth are usually generated by cutting tools such as hobs, their shapes and dimensions are usually determined by the cutting depth settings.

Because of material allowances for finishing processes such as profile grinding, it is usually the case that the depth setting of the roughing tool, relative to the gear axis, includes the amount of nominal profile shift,  $xm_n$ , plus a tolerance designed to ensure that the finishing allowance will be greater instead of less than the requisite minimum. Because of this, calculated values of tooth root stresses usually err on the side of safety.

If the tooth thickness deviation near the root results in a thickness reduction of more than 0,05  $m_{\rm n}$ , this shall be taken into account in the stress calculation, by taking the generated profile,  $x_{\rm E}$ , relative to rack shift amount  $m_{\rm n}$  instead of the nominal profile.

The equations in this part of ISO 6336 apply to all basic rack profiles (see Figure 2) with and without undercut, but with the following restrictions:

- a) the contact point of the 30° (60°) tangent shall lie on the tooth root fillet generated by the root fillet of the basic rack;
- b) the basic rack profile of the gear shall have a root fillet with  $\rho_{fP} > 0$ ;
- c) the teeth shall be generated using tools such as hobs or rack type cutters;
- d) since calculated ratings refer to finished tooth forms, profile grinding and similar allowances, including tooth thickness allowances, can be neglected, and in practice it can be assumed that the dimensions of the basic rack of the tool are the same as those of the counterpart basic rack of the gear;
- e) for internal gears, a virtual basic rack profile is used which differs from the basic rack profile in the root radius  $\rho_{\text{FP}}$  [see Equation (11)].

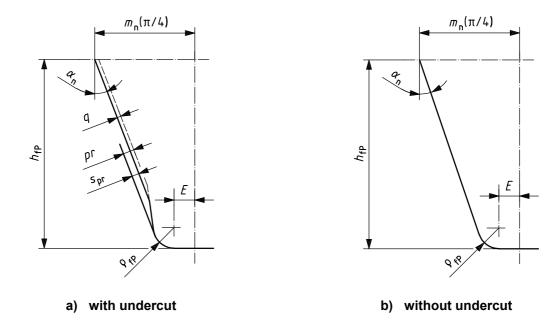


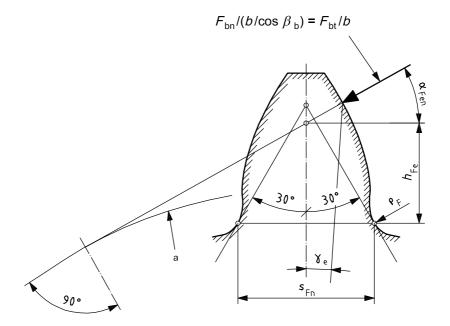
Figure 2 — Dimensions and basic rack profile of the teeth (finished profile)

The above comments apply to straight spur and helical gears. The value  $Y_{\rm F}$  is determined for the virtual spur gears of helical gears; the virtual number of teeth  $z_{\rm n}$  can be determined using Equation (21) or (22).  $Y_{\rm F}$  is determined separately for the pinion and the wheel.

NOTE For a description of symbols and abbreviations, see ISO 6336-1:2006, Table 1.

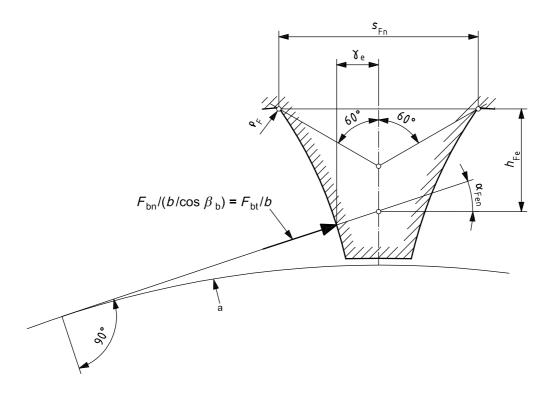
#### 6.2 Calculation of the form factor, $Y_F$ : Method B

The determination of the normal chordal dimension  $s_{\rm Fn}$  of the tooth root critical section and the bending moment arm  $h_{\rm Fe}$  relevant to load application at the outer point of single pair gear tooth contact for Method B is shown in Figures 3 and 4.



a Base circle.

Figure 3 — Determination of normal chordal dimensions of tooth root critical section for Method B (external gears)



a Base circle.

Figure 4 — Determination of normal chordal dimensions of tooth root critical section for Method B (internal gears)

The following equation uses the symbols illustrated in Figures 3 and 4:

$$Y_{\mathsf{F}} = \frac{\frac{6 \ h_{\mathsf{Fe}}}{m_{\mathsf{n}}} \cos \alpha_{\mathsf{Fen}}}{\left(\frac{s_{\mathsf{Fn}}}{m_{\mathsf{n}}}\right)^{2} \cos \alpha_{\mathsf{n}}} \tag{9}$$

In order to evaluate precise values,  $s_{\rm Fn}$  and  $\alpha_{\rm Fen}$ , of  $h_{\rm Fe}$  it is first necessary to derive a value of  $\theta$  which is reasonably accurate, usually after five iterations of Equation (14). Determination of  $Y_{\rm F}$  by graphical means is not recommended.

#### 6.2.1 Tooth root normal chord, $s_{\rm Fn}$ , radius of root fillet, $\rho_{\rm F}$ , bending moment arm, $h_{\rm Fe}$ <sup>4)</sup>

First, determine the auxiliary values for Equation (9):

$$E = \frac{\pi}{4} m_{\rm n} - h_{\rm fP} \tan \alpha_{\rm n} + \frac{s_{\rm pr}}{\cos \alpha_{\rm n}} - \left(1 - \sin \alpha_{\rm n}\right) \frac{\rho_{\rm fP}}{\cos \alpha_{\rm n}} \tag{10}$$

10

<sup>4)</sup> If the tip of the tooth has been rounded or chamfered, it is necessary to replace the tip diameter  $d_a$  in the calculation by  $d_{Na}$  the "effective tip diameter".  $d_{Na}$  is the diameter of a circle near the tip cylinder, containing limits of the usable gear flanks.

with

 $s_{pr} = pr - q$  (see Figure 2);

 $s_{\rm pr} = 0$  when gears are not undercut;

 $\rho_{\text{fPv}} = \rho_{\text{fP}}$  for external gears, or

$$\rho_{\text{fPv}} \approx \rho_{\text{fP}} + m_{\text{n}} \frac{\left(x_0 + h_{\text{fP}} / m_{\text{n}} - \rho_{\text{fP}} / m_{\text{n}}\right)^{1,95}}{3.156 \cdot 1.036^{z_0}}$$
 for internal gears (11)

where

 $x_0$  is the pinion-cutter shift coefficient;

 $z_0$  is the number of teeth of the pinion cutter;

$$G = \frac{\rho_{\text{fPV}}}{m_{\text{p}}} - \frac{h_{\text{fP}}}{m_{\text{p}}} + x \tag{12}$$

$$H = \frac{2}{z_{\rm p}} \left( \frac{\pi}{2} - \frac{E}{m_{\rm p}} \right) - T \tag{13}$$

with

 $T = \pi/3$  for external gears;

 $T = \pi/6$  for internal gears;

$$\theta = \frac{2G}{z_n} \tan \theta - H \tag{14}$$

The value  $\theta = \pi/6$  for external gears and  $\theta = \pi/3$  for internal gears may be used as a seed value in the iteration of the transcendental Equation (14). Generally, the function converges after five iterations.

- a) Tooth root normal chord s<sub>Fn</sub>
  - For external gears:

$$\frac{s_{\text{Fn}}}{m_{\text{n}}} = z_{\text{n}} \sin\left(\frac{\pi}{3} - \theta\right) + \sqrt{3} \left(\frac{G}{\cos\theta} - \frac{\rho_{\text{fPv}}}{m_{\text{n}}}\right)$$
 (15)

— For internal gears:

$$\frac{s_{\text{Fn}}}{m_{\text{n}}} = z_{\text{n}} \sin\left(\frac{\pi}{6} - \theta\right) + \left(\frac{G}{\cos\theta} - \frac{\rho_{\text{fPv}}}{m_{\text{n}}}\right) \tag{16}$$

b) Radius of root fillet  $\rho_{\rm F}$  (see Figures 3 and 4)

$$\frac{\rho_{\mathsf{F}}}{m_{\mathsf{n}}} = \frac{\rho_{\mathsf{fPv}}}{m_{\mathsf{n}}} + \frac{2G^2}{\cos\theta \left( |z_{\mathsf{n}}| \cos^2\theta - 2G \right)} \tag{17}$$

- c) Bending moment arm  $h_{Fe}$ 
  - For external gears:

$$\frac{h_{\text{Fe}}}{m_{\text{n}}} = \frac{1}{2} \left[ (\cos \gamma_{\text{e}} - \sin \gamma_{\text{e}} \tan \alpha_{\text{Fen}}) \frac{d_{\text{en}}}{m_{\text{n}}} - z_{\text{n}} \cos \left( \frac{\pi}{3} - \theta \right) - \left( \frac{G}{\cos \theta} - \frac{\rho_{\text{fPv}}}{m_{\text{n}}} \right) \right]$$
(18)

— For internal gears:

$$\frac{h_{\text{Fe}}}{m_{\text{D}}} = \frac{1}{2} \left[ (\cos \gamma_{\text{e}} - \sin \gamma_{\text{e}} \tan \alpha_{\text{Fen}}) \frac{d_{\text{en}}}{m_{\text{D}}} - z_{\text{n}} \cos \left( \frac{\pi}{6} - \theta \right) - \sqrt{3} \left( \frac{G}{\cos \theta} - \frac{\rho_{\text{fPv}}}{m_{\text{D}}} \right) \right]$$
(19)

#### 6.2.2 Parameters of virtual gears

These are as follows.

$$\beta_{\rm b} = \arccos\sqrt{1 - \left(\sin\beta\cos\alpha_{\rm n}\right)^2} = \arcsin\left(\sin\beta\cos\alpha_{\rm n}\right)$$
 (20)

$$z_{\mathsf{n}} = \frac{z}{\cos^2 \beta_{\mathsf{b}} \cos \beta} \tag{21}$$

Approximation:

$$z_{\mathsf{n}} \approx \frac{z}{\cos^3 \beta} \tag{22}$$

$$\varepsilon_{\alpha n} = \frac{\varepsilon_{\alpha}}{\cos^2 \beta_{b}} \tag{23}$$

$$d_{\mathsf{n}} = \frac{d}{\cos^2 \beta_{\mathsf{h}}} = m_{\mathsf{n}} \ z_{\mathsf{n}} \tag{24}$$

$$p_{\rm bn} = \pi \, m_{\rm n} \cos \, \alpha_{\rm n} \tag{25}$$

$$d_{\rm bn} = d_{\rm n} \cos \alpha_{\rm n} \tag{26}$$

$$d_{\mathsf{an}} = d_{\mathsf{n}} + d_{\mathsf{a}} - d \tag{27}$$

$$d_{\text{en}} = 2 \frac{z}{|z|} \sqrt{\left[\sqrt{\left(\frac{d_{\text{an}}}{2}\right)^2 - \left(\frac{d_{\text{bn}}}{2}\right)^2} - \frac{\pi d \cos \beta \cos \alpha_n}{|z|} \left(\varepsilon_{\alpha n} - 1\right)\right]^2 + \left(\frac{d_{\text{bn}}}{2}\right)^2}$$
(28)

The number of teeth, z, is positive for external gears and negative for internal gears.

$$\alpha_{\text{en}} = \arccos\left(\frac{d_{\text{bn}}}{d_{\text{en}}}\right)$$
 (29)

$$\gamma_{e} = \frac{0.5 \pi + 2 \tan \alpha_{n} x}{z_{n}} + \text{inv } \alpha_{n} - \text{inv } \alpha_{en}$$
(30)

$$\alpha_{\text{Fen}} = \alpha_{\text{en}} - \gamma_{\text{e}} = \tan \alpha_{\text{en}} - \text{inv } \alpha_{\text{n}} - \frac{0.5 \pi + 2 \tan \alpha_{\text{n}} x}{z_{\text{n}}}$$
 (31)

#### 6.3 Derivations of determinant normal tooth load for spur gears

Nominal bending stress =  $\frac{\text{bending moment}}{\text{section modulus of gear at } s_{\text{Fn}}}$  in accordance with the following equation, with symbols in accordance with Figures 3 and 4.

$$\sigma = \frac{F_{\rm b} \cos \alpha_{\rm Fen}}{\frac{1}{6} \left( b \, s_{\rm Fn}^2 \right)} \, h_{\rm Fe} \tag{32}$$

$$F_{\rm b} \frac{d_{\rm b}}{2} = F_{\rm t} \frac{d}{2} = F_{\rm w} \frac{d_{\rm w}}{2} \tag{33}$$

where

 $d_{\mathsf{b}}$  is the base diameter;

d is the reference diameter;

 $d_{\rm w}$  is the pitch diameter;

 $F_{t}$  is the nominal tangential load at the reference cylinder;

 $F_{\rm W}$   $\,$  is the nominal tangential load at the pitch cylinder.

$$F_{\rm b} = \frac{F_{\rm t}}{\cos \alpha} = \frac{F_{\rm w}}{\cos \alpha_{\rm w}} \tag{34}$$

$$\sigma = \left[ \frac{\frac{h_{\text{Fe}}}{m} \cos \alpha_{\text{Fen}}}{\frac{1}{6} \left( \frac{s_{\text{Fn}}}{m} \right)^2 \cos \alpha} \right] \frac{F_{\text{t}}}{b \, m} = \frac{F_{\text{t}}}{b \, m} \, Y_{\text{F}}$$
(35)

where

 $\alpha$  is the pressure angle of the basic rack profile;

 $\alpha_{\rm W}$   $\,$  is the working pressure angle.

When  $\sigma$  is expressed as a function of  $F_t$ , a form factor,  $Y_F$ , can be derived from Equation (35).

### 7 Stress correction factor, $Y_S$

#### 7.1 Basic uses

The stress correction factor,  $Y_S$ , is used to convert the nominal tooth root stress to local tooth root stress and, by means of this factor, the following are taken into account:

- a) the stress amplifying effect of section change at the fillet radius at the tooth root 5);
- b) that evaluation of the true stress system at the tooth root critical section is more complex than the simple system evaluation presented, with evidence indicating that the intensity of the local stress at the tooth root consists of two components, one of which is directly influenced by the value of the bending moment and the other increasing with closer proximity to the critical section of the determinant position of load application.

 $Y_S$  is the factor for load application at the outer point of single pair tooth contact (Method B). See 5.2 for the principles, assumptions and application of Method B.

The formulae in this clause are based on data derived from the geometry of external spur gears with 20° pressure angle, by means of measurement and calculations using finite element and integral equation methods. The formulae can also be used to obtain approximate values for internal gears and for gears having other pressure angles.

The present instructions refer to spur and helical gears. See Clause 6 for explanatory notes and information on the calculation of the virtual numbers of teeth relevant to helical gears.

#### 7.2 Stress correction factor, $Y_S$ : Method B

The calculation of the stress correction factor,  $Y_S$ , is made in accordance with Equation (36), which is valid in the range:  $1 \le q_S < 8$ ; symbols are as illustrated in Figures 3 and 4.

$$Y_{S} = (1,2+0,13L) q_{S}$$
(36)

where

$$L = \frac{s_{\mathsf{Fn}}}{h_{\mathsf{F}e}} \tag{37}$$

with

 $s_{\mathsf{En}}$  from Equation (15) for external gears, Equation (16) for internal gears;

 $h_{\mbox{Fe}}$  from Equation (18) for external gears, Equation (19) for internal gears;

$$q_s = \frac{s_{\mathsf{Fn}}}{2\rho_{\mathsf{F}}} \tag{38}$$

with  $\rho_{\rm F}$  from Equation (17).

Determination of  $Y_S$  by graphical methods is not appropriate.

<sup>5)</sup> See 7.3 for the procedure to be followed when grinding notches are present in tooth fillets.

#### 7.3 Stress correction factor for gears with notches in fillets

A notch such as a grinding notch in the fillet of a gear near the critical section usually engenders a degree of stress concentration exceeding that of the fillet; thus, the stress correction factor is correspondingly greater. A fair estimate of  $Y_{Sg}$ , obtainable from Equation (39), can be substituted for  $Y_{Sg}$ , see Figure 5, if the notch is near the critical section. See also Reference [6].

$$Y_{Sg} = \frac{1,3 Y_{S}}{1,3 - 0.6 \sqrt{\frac{t_{g}}{\rho_{g}}}}$$
(39)

valid for 
$$\sqrt{\frac{t_g}{\rho_g}} < 2.0$$

The effect of the grinding notch is less than that implied in Equation (39) when the notch is above the contact point of the 30° tangent (external gears) or 60° tangent (internal gears).

 $Y_{\rm sg}$  also takes into consideration the reduction in the tooth root thickness.

Deep notches in the fillets of surface hardened steel gears severely reduce the bending strength of their teeth.

# 7.4 Stress correction factor, $Y_{\rm ST}$ , relevant to the dimensions of the standard reference test gears

The tooth root stress limit values for materials, according to ISO 6336-5, were derived from results of tests of standard reference test gears for which either  $Y_{ST} = 2.0$  or for which test results were recalculated to this value. See also Reference [6].

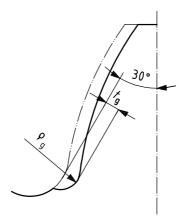


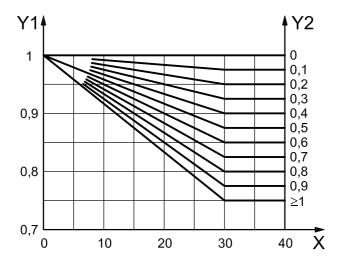
Figure 5 — Notch dimensions

# 8 Helix angle factor, $Y_{\beta}$

The tooth root stress of a virtual spur gear, calculated as a prelimary value, is converted by means of the helix factor  $Y_{\beta}$  to that of the corresponding helical gear. By this means, the oblique orientation of the lines of mesh contact is taken into account (less tooth root stress).

#### 8.1 Graphical value

 $Y_{\beta}$  may be read from Figure 6 as a function of the helix angle,  $\beta$ , and the overlap ratio,  $\varepsilon_{\beta}$ .



#### Key

X reference helix angle,  $\beta$ , degrees

Y1 helix factor,  $Y_{\beta}$ 

Y2 overlap ratio,  $\varepsilon_{\beta}$ 

Helix factors  $Y_{\beta} > 25^{\circ}$  shall be confirmed by experience.

Figure 6 — Helix factor,  $Y_{\beta}$ 

#### 8.2 Determination by calculation

The factor  $Y_{\beta}$  can be calculated using Equation (40), which is consistent with the curves illustrated in Figure 6.

$$Y_{\beta} = 1 - \varepsilon_{\beta} \frac{\beta}{120^{\circ}} \tag{40}$$

where  $\beta$  is the reference helix angle, in degrees.

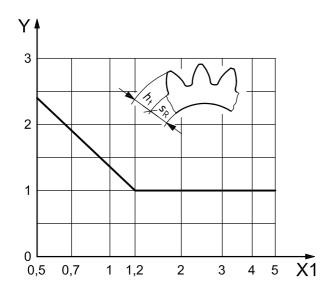
The value 1,0 is substituted for  $\varepsilon_{\beta}$  when  $\varepsilon_{\beta} > 1,0$ , and 30° is substituted for  $\beta$  when  $\beta > 30$ °.

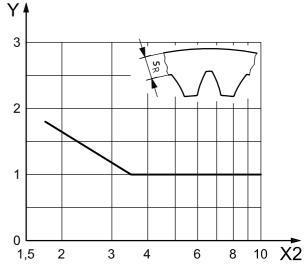
#### 9 Rim thickness factor, $Y_{B}$

Where the rim thickness is not sufficient to provide full support for the tooth root, the location of bending fatigue failure may be through the gear rim, rather than at the root fillet. The rim thickness factor  $Y_B$  is a simplified factor used to de-rate thin rimmed gears when detailed calculations of stresses in both tension and compression or experience are not available. For critically loaded applications this method should be replaced by a more comprehensive analysis.

#### 9.1 Graphical values

 $Y_{\rm B}$  can be taken from Figure 7 as a function of the backup ratio  $s_{\rm R}/h_{\rm t}$  for external gears and as a function of the rim thickness  $s_{\rm R}/m_{\rm n}$  for internal gears.





X1 backup ratio,  $s_R/h_t$ 

X2 rim thickness,  $s_R/m_n$ 

Y rim thickness factor,  $Y_{\rm B}$ 

Figure 7 — Rim thickness factor,  $Y_{\rm B}$ 

#### 9.2 Determination by calculation

#### 9.2.1 External gears

 $Y_{\rm B}$  can be calculated using Equations (41) to (42). These are consistent with the curve in Figure 7.

a) If  $s_R/h_t \geqslant 1.2$ , then

$$Y_{\rm B} = 1.0$$
 (41)

b) If  $s_R/h_t > 0.5$  and  $s_R/h_t < 1.2$ , then

$$Y_{\rm B} = 1.6 \ln \left( 2.242 \, \frac{h_{\rm t}}{s_{\rm R}} \right)$$
 (42)

c) The case  $s_R/h_t \leqslant$  0,5 shall be avoided.

#### 9.2.2 Internal gears

 $Y_{\rm B}$  can be calculated using Equations (43) to (44). These are consistent with the curve in Figure 7.

a) If  $s_R/m_n \geqslant 3.5$ , then

$$Y_{\rm B} = 1.0$$
 (43)

b) If  $s_R/m_n > 1,75$  and  $s_R/m_n < 3,5$ , then

$$Y_{\rm B} = 1,15 \ln \left( 8,324 \, \frac{m_{\rm n}}{S_{\rm R}} \right)$$
 (44)

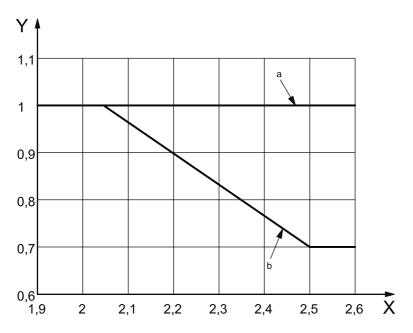
c) The case  $s_R/m_n \leq 1,75$  shall be avoided.

#### 10 Deep tooth factor, $Y_{DT}$

For gears of high precision (accuracy grade  $\leq$  4) with contact ratios in the range of  $2 \leq \varepsilon_{\alpha n} < 2.5$  and with applied actual profile modification to obtain a trapezoidal load distribution along the path of contact, the nominal tooth root stress  $\sigma_{\text{F0}}$  is adjusted by the deep tooth factor  $Y_{\text{DT}}$ .

#### 10.1 Graphical values

 $Y_{\rm DT}$  may be read from Figure 8 as a function of the contact ratio  $\varepsilon_{an}$ 



#### Key

- X virtual contact ratio,  $\varepsilon_{\alpha n}$
- Y deep tooth factor,  $Y_{DT}$
- a Accuracy grade > 4.
- b Accuracy grade ≤ 4.

Figure 8 — Deep tooth factor,  $Y_{DT}$ 

#### 10.2 Determination by calculation

 $Y_{\rm DT}$  can be calculated using Equations (45) to (47). These are consistent with the curves in Figure 8.

a) If  $\varepsilon_{\alpha n} \le 2.05$  or if  $\varepsilon_{\alpha n} > 2.05$  and the accuracy grade > 4, then

$$Y_{\mathsf{DT}} = 1.0 \tag{45}$$

b) If  $2.05 < \varepsilon_{\alpha n} \le 2.5$  and the accuracy grade  $\le 4$ , then

$$Y_{\rm DT} = -0,666 \ \varepsilon_{\alpha n} + 2,366$$
 (46)

c) If  $\varepsilon_{\alpha n} > 2.5$  and the accuracy grade  $\leq 4$ , then

$$Y_{\mathsf{DT}} = 0.7 \tag{47}$$

#### 11 Reference stress for bending

See 5.3 for general notes on the determination of limit values for tooth root stress.

#### 11.1 Reference stress for Method A

Method A is consistent with the determination of tooth root stress reference stress according to 5.3.1.1.

#### 11.2 Reference stress, with values $\sigma_{\rm F \, lim}$ and $\sigma_{\rm FF}$ for Method B

See 5.3.1.2 and 5.3.2 for information. See Equation (5) for definitions of  $\sigma_{\rm F \, lim}$  and  $\sigma_{\rm FE}$ .

NOTE ISO 6336-5 provides information, derived from the results of testing standard reference test gears, on values of  $\sigma_{\text{F lim}}$  and  $\sigma_{\text{FE}}$  for the more popular gear materials, heat treatment processes and the influence of the material quality on those values. ISO 6336-5 also includes requirements for quality grades ML, MQ and ME concerning material and heat treatment. Material quality grade MQ is usually chosen for gears unless otherwise agreed upon.

#### 12 Life factor, $Y_{NT}$

The life factor,  $Y_{NT}$ , accounts for the higher tooth root stress, which may be tolerable for a limited life (number of load cycles), as compared with the allowable stress at  $3 \times 10^6$  cycles.

The principal influence factors are:

- a) material and heat treatment (see ISO 6336-5),
- b) number of load cycles (service life),  $N_{\rm I}$ ,
- c) failure criteria,
- d) smoothness of operation required,
- e) cleanness of gear material,
- f) material ductility and fracture toughness, and
- g) residual stress.

For the purposes of this part of ISO 6336, the number of load cycles,  $N_{\rm L}$ , is defined as the number of mesh contacts, under load, of the gear tooth being analysed. The allowable stress numbers are established for  $3 \times 10^6$  tooth load cycles at 99 % reliability.

A  $Y_{\rm NT}$  value of unity may be used, where justified by experience, beyond  $3 \times 10^6$  cycles. However, consideration should be given to the use of optimum material quality and manufacturing, with selection of an appropriate safety factor.

#### 12.1 Life factor, $Y_{NT}$ : Method A

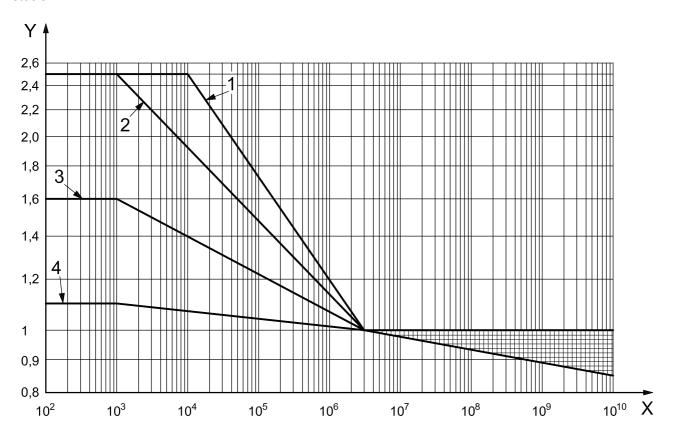
The S-N curve or damage curve derived from facsimiles of the actual gear is determinant for the establishment of the limited life. Since under such circumstances factors  $Y_{\delta \text{rel T}}$ ,  $Y_{\text{R rel T}}$  and  $Y_{\text{X}}$  are in effect already included in the S-N or damage curves, the value 1,0 is substituted for each in the calculation of permissible stress.

#### 12.2 Life factor, $Y_{NT}$ : Method B

For this method, life factor  $Y_{NT}$  of the standard reference test gear is used as an aid in the evaluation of permissible stress for limited life or reliability (see 5.3).

#### 12.2.1 Graphical values

 $Y_{\rm NT}$  may be read from Figure 9 for the static stress and reference stress as a function of material and heat treatment. Values from a large number of tests are presented as typical damage or crack initiation curves for surface-hardened and nitride-hardened steels, or curves of yield stress for structural and through-hardened steels.



#### Key

- X number of load cycles,  $N_L$
- Y life factor,  $Y_{NT}$
- 1 GTS (perl.), St, V, GGG (perl. bai.)
- 2 Eh, IF (root)
- 3 NT, NV (nitr.), GGG (ferr.), GG
- 4 NV (nitrocar.)

Figure 9 — Life factor,  $Y_{\rm NT}$ , for reference test gears (see ISO 6336-1:2006, Table 2, for explanation of abbreviations used)

#### 12.2.2 Determination by calculation

The data of  $Y_{\rm NT}$  for static stress and reference stress can be taken from Table 1.

Life factor  $Y_{NT}$  for limited-life stress is determined by means of interpolation on a log-log scale between the values for reference and static stress limits as defined in 5.3.2. Evaluation of  $Y_{NT}$  is according to 5.3.3.

Material <sup>a</sup>	Number of load cycles, $N_{L}$	Life Factor, Y <sub>NT</sub>
	$N_{\rm L} \leqslant 10^4$ , static	2,5
St, V,GGG (perl. bai.), GTS (perl.),	$N_{L}=3\times10^{6}$	1,0
W - 77	$N_{\rm L} = 10^{10}$	0,85 up to 1,0 b
	$N_{L} \leqslant 10^3$ , static	2,5
Eh, IF (root)	$N_{L} = 3 \times 10^6$	1,0
	$N_{\rm L} = 10^{10}$	0,85 up to 1,0 b
GG, GGG (ferr.), NT, NV (nitr.)	$N_{L} \leqslant 10^3$ , static	1,6
	$N_{\rm L}=3\leqslant 10^6$	1,0
	$N_{\rm L}=10^{10}$	0,85 up to 1,0 b
NV (nitrocar.)	$N_{L} \leqslant 10^3$ , static	1,1
	$N_{\rm L}=3\leqslant 10^6$	1,0
	$N_{\rm L} = 10^{10}$	0,85 up to 1,0 b

Table 1 — Life factor,  $Y_{NT}$ 

## 13 Sensitivity factor, $Y_{\delta T}$ , and relative notch sensitivity factor, $Y_{\delta \text{ rel } T}$

#### 13.1 Basic uses

The extent to which the calculated tooth root stress deemed to have caused fatigue or overload breakage exceeds the relevant material stress limit is indicated by the dynamic or the static sensitivity factor,  $Y_{\mathcal{S}}$  It characterizes the notch sensitivity of the material, and its values depend on the material and the stress gradient. Its values for dynamic stresses are different from its value for static stress. This applies to  $Y_{\mathcal{S}T}$  in relation to breakage of a standard reference test gear tooth. It applies also to the relative sensitivity factors which relate the sensitivity of a gear of interest to that of a standard reference test gear ( $Y_{\mathcal{S}\text{rel }T}$ ).

#### 13.2 Determination of the sensitivity factors

Comments on these factors given in 5.3 apply in principle.

#### 13.2.1 Method A

The tooth root stress limits are determined by testing facsimiles of the gear of interest (or closely similar test gears), in which case the relative sensitivity factor is equal to 1,0. However, a careful analysis — by means of which the relative sensitivity factor for the relevant material and relevant tooth form will be established — has yet to be undertaken.

#### 13.2.2 Method B

When the reference and static stress limit values are derived with Method B using reference test gears with notch parameters  $q_{\rm sT}=2.5$ , the factor  $Y_{\delta\,{\rm rel}\,{\rm T}}$  relevant to the reference and static stress limits of any gear seldom deviates much from 1,0. This is because the value  $q_{\rm sT}=2.5$  is in the mid-range of common gear designs. The reference value  $Y_{\delta\,{\rm rel}\,{\rm T}}=1.0$  for the standard reference test gear coincides with the stress correction factor  $Y_{\rm S}=2.0$  (see Figures 11 and 13).

a See ISO 6336-1:2006, Table 2, for an explanation of the abbreviations used.

The lower value of  $Z_{NT}$  may be used for critical service, where pitting must be minimal. Values between 0,85 and 1,0 may be used for general purpose gearing. With optimum lubrication, material, manufacturing and experience 1,0 may be used.

#### 13.3 Relative notch sensitivity factor, $Y_{\delta \text{ rel } T}$ : Method B

#### 13.3.1 Graphical values

#### 13.3.1.1 $Y_{\delta \text{ rel T}}$ for reference stress

 $Y_{\mathcal{S}\,\mathrm{rel}\,\mathrm{T}}$  can be read from Figure 10 as a function of  $q_{\mathrm{S}}$  or  $Y_{\mathrm{S}}$  and the material. The curves in this graph for each of the materials were derived from Figure 12 by subtracting from the absolute value  $Y_{\mathcal{S}}$  appropriate to each value of  $q_{\mathrm{S}}$ , the value of  $Y_{\mathcal{S}\mathrm{T}}$  for that material corresponding to the notch parameter  $q_{\mathrm{S}}=2.5$  (the notch parameter of the standard reference test gear). For any gear of interest,  $q_{\mathrm{S}}$  can be calculated using Equation (38).

#### 13.3.1.2 $Y_{\delta \text{ rel T}}$ for static stress

 $Y_{\delta \, {\rm rel} \, {\rm T}}$  may be taken from Figure 11 as a function of stress correction factor  $Y_{\rm S}$  and the material. The curves in this graph for each of the materials were derived from Figure 13 by subtracting from the absolute value  $Y_{\delta}$  appropriate to each value of  $Y_{\rm S}$ , the value of  $Y_{\delta {\rm T}}$  for that material corresponding to  $Y_{\rm ST} = 2.0$  (the stress correction factor of the standard reference test gear). For any gear of interest,  $Y_{\rm S}$  can be calculated using Equation (36).

#### 13.3.2 Determination by calculation

#### 13.3.2.1 $Y_{Srel\ T}$ for reference stress

 $Y_{\delta \text{ rel T}}$  can be calculated using Equation (48). This is consistent with the curves in Figure 10.

$$Y_{\delta \text{ rel T}} = \frac{Y_{\delta}}{Y_{\delta T}} = \frac{1 + \sqrt{\rho' \chi^*}}{1 + \sqrt{\rho' \chi_T^*}}$$

$$\tag{48}$$

The slip-layer thickness  $\rho'$  can be taken from Table 2 as a function of the material.

The relative stress gradient can be calculated using the Equation (49) 6):

$$\chi^* = \chi_P^* (1 + 2 q_s)$$

with

$$\chi_{\mathsf{P}}^* = \frac{1}{5} \tag{49}$$

The value of  $\chi^*_T$  for the standard reference test gear is obtained similarly by substituting  $q_{sT} = 2.5$  for  $q_s$  in Equation (49).

22

<sup>6)</sup> Applies for module m = 5 mm. The influence of size is covered by the factor  $Y_X$  (see Clause 15).

Item	Material <sup>a</sup>	ρ' [mm]		
1	GG $\sigma_{\rm B}=$ 150 N/mm <sup>2</sup>	0,312 4		
2	GG, GGG (ferr.); $\sigma_{\rm B}=300~{\rm N/mm^2}$	0,309 5		
3	NT, NV; for all hardness	0,100 5		
4	St; $\sigma_{\rm S} = 300 \text{ N/mm}^2$	0,083 3		
5	St; $\sigma_{\rm S} = 400 \text{ N/mm}^2$	0,044 5		
6	V, GTS, GGG (perl. bai.); $\sigma_{\rm S} = 500 \ {\rm N/mm^2}$	0,028 1		
7	V, GTS, GGG (perl. bai.); $\sigma_{\rm S} = 600 \ {\rm N/mm^2}$	0,019 4		
8	V, GTS, GGG (perl. bai.); $\sigma_{0,2} = 800 \text{ N/mm}^2$	0,006 4		
9	V, GTS, GGG (perl. bai.); $\sigma_{0,2} = 1000 \text{ N/mm}^2$	0,001 4		
10	Eh, IF (root); for all hardness	0,003 0		
a See ISO 6336-	See ISO 6336-1:2006, Table 2, for an explanation of the abbreviations used.			

Table 2 — Values for slip-layer thickness  $\rho'$ 

## 13.3.2.1.1 $Y_{\delta \, { m rel} \, \, { m T}}$ for static stress

 $Y_{\delta \, {\rm rel} \, {\rm T}}$  can be calculated using Equations (50) to (54). These are consistent with the curves in Figure 11 (see ISO 6336-1:2006, Table 2, for an explanation of the abbreviations used).

a) For St with well defined yield point:

$$Y_{\delta \text{ rel T}} = \frac{1 + 0.93 (Y_{S} - 1) \sqrt[4]{\frac{200}{\sigma_{S}}}}{1 + 0.93 \sqrt[4]{\frac{200}{\sigma_{S}}}}$$
(50)

For St with steadily increasing elongation curve and 0,2 % proof stress, V and GGG (perl., bai.):

$$Y_{S \text{ rel T}} = \frac{1 + 0.82 (Y_S - 1) \sqrt[4]{\frac{300}{\sigma_{0,2}}}}{1 + 0.82 \sqrt[4]{\frac{300}{\sigma_{0,2}}}}$$
(51)

These values are only valid if the local stresses do not reach the yield point.

c) For Eh and IF(root) with stress up to crack initiation:

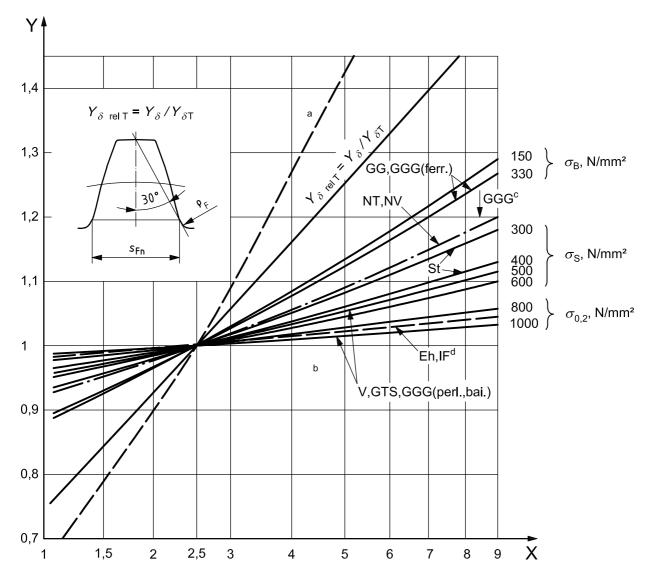
$$Y_{Srel T} = 0.44 Y_S + 0.12$$
 (52)

d) For NT and NV with stress up to crack initiation:

$$Y_{\delta \text{ rel T}} = 0.20 \ Y_{\text{S}} + 0.60$$
 (53)

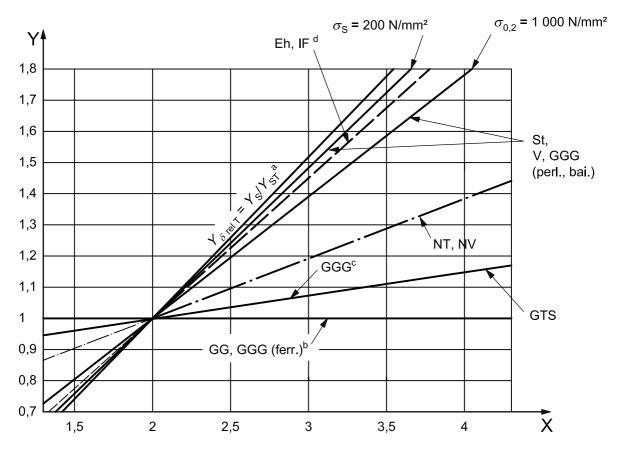
e) For GG and GGG (ferr.) with stress up to fracture limit:

$$Y_{\delta \text{ rel T}} = 1.0 \tag{54}$$



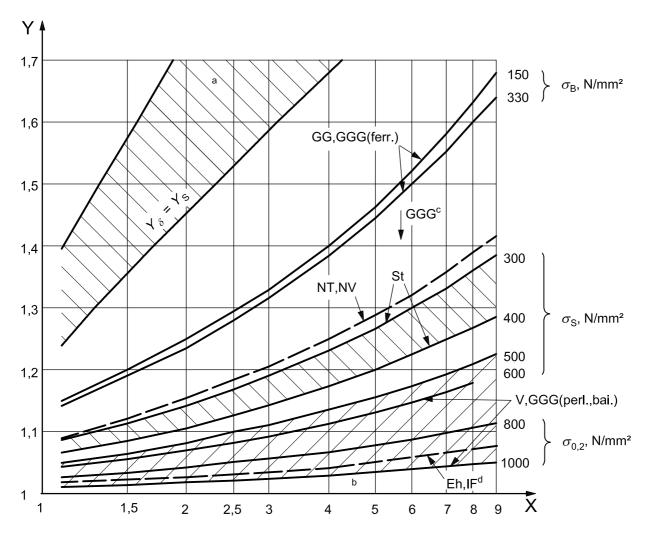
- X notch parameter,  $q_s = s_{Fn}/2\rho_F$
- Y relative notch sensitivity factor,  $Y_{\delta\,\mathrm{rel}\,\mathrm{T}}$ , for reference stress
- NOTE 1 Values of  $\sigma$  in newtons per square millimetre (N/mm<sup>2</sup>).
- NOTE 2 See ISO 6336-1:2006, Table 2, for an explanation of the abbreviations used.
- NOTE 3 Based on bending flat bar complying with VDI 2226<sup>[7]</sup>.
- a Fully insensitive to notches.
- b Fully sensitive to notches.
- <sup>c</sup> With increasingly pearlitic structure.
- d (root).

Figure 10 — Relative notch sensivity factor,  $Y_{\delta \, \mathrm{rel} \, \mathrm{T}}$ , for reference stress



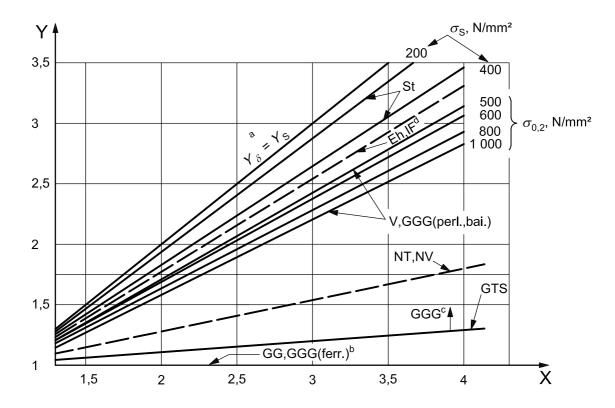
- X stress correction factor,  $Y_S$
- Y relative notch sensitivity factor,  $Y_{\delta \, {\rm rel} \, {\rm T}}$ , for static stress
- NOTE 1 See ISO 6336-1:2006, Table 2, for an explanation of the abbreviations used.
- NOTE 2 Based on bending flat bar complying with VDI 2226<sup>[7]</sup>.
- a Fully insensitive to notches.
- b Fully sensitive to notches.
- <sup>c</sup> With increasingly pearlitic structure.
- d (root).

Figure 11 — Relative notch sensivity factor,  $Y_{\delta \, \mathrm{rel} \, \mathrm{T}}$ , for static stress



- ${\rm X} \quad {\rm notch \ parameter,} \ q_{\rm S}$
- Y sensitivity factor,  $Y_{\delta}$ , for reference stress
- NOTE 1 See ISO 6336-1:2006, Table 2, for an explanation of the abbreviations used.
- NOTE 2 Based on bending flat bar complying with VDI 2226<sup>[7]</sup>.
- a Fully insensitive to notches.
- b Fully sensitive to notches.
- <sup>c</sup> With increasingly pearlitic structure.
- d (root).

Figure 12 — Relative notch sensivity factor,  $Y_{\partial}$  for reference stress



- X stress correction factor,  $Y_S$
- Y sensitivity factor,  $Y_{\delta}$  for static stress

NOTE 1 See ISO 6336-1:2006, Table 2, for an explanation of the abbreviations used.

NOTE 2 Based on bending flat bar complying with VDI 2226<sup>[7]</sup>.

- a Fully insensitive to notches.
- b Fully sensitive to notches.
- <sup>c</sup> With increasingly pearlitic structure.
- d (root).

Figure 13 — Relative notch sensivity factor,  $Y_{\mathfrak{P}}$  for static stress

# 14 Surface factors, $Y_R$ , $Y_{RT}$ , and relative surface factor, $Y_{R \text{ rel } T}$

#### 14.1 Influence of surface condition

The surface factor,  $Y_{\rm R}$ , accounts for the influence on tooth root stress of the surface condition in the tooth roots. This is dependent on the material and the surface roughness in the tooth root fillets (see Note, below).  $Y_{\rm R}$  for static stress is different from  $Y_{\rm R}$  for dynamic stresses. This is also true for  $Y_{\rm RT}$ , the surface factor of the standard reference test gear. These factors are compared to that of a plain, polished test piece. Relative surface factors represent the relationship of the surface factor of a gear of interest to that of the standard reference test gear ( $Y_{\rm R}$  rel T).

NOTE The influence of surface condition on tooth root bending strength does not depend solely on the surface roughness in the tooth root fillets, but also on the size and shape (the problem of "notches within a notch"). This subject has not to date been sufficiently well studied for it to be taken into account in this part of ISO 6336. The method applied here is only valid when scratches or similar defects deeper than 2Rz are not present (2Rz is a prelimary estimated value).

Besides surface texture, other influences on tooth bending strength are known, and include residual compressive stresses (shot peening), grain boundary oxidation and chemical effects. When fillets are shot-peened and/or are perfectly shaped, a value slightly greater than that obtained from the graph should be substituted for  $Y_{R \text{ rel } T}$ . When grain boundary oxidation or chemical effects are present, a smaller value than that indicated by the graph should be substituted for  $Y_{R \text{ rel } T}$ .

#### 14.2 Determination of surface factors and relative surface factors

The comments in 5.3 apply in principle for the determination of these factors.

#### 14.2.1 Method A

In Method A the tooth root stress limit is determined by testing the gear of interest or testing closely similar test gears. By this approach, the relative surface factor is equal, or approximately equal, to 1,0. In order to determine the material surface factor relative to that of the gear tested, a careful analysis shall be undertaken.

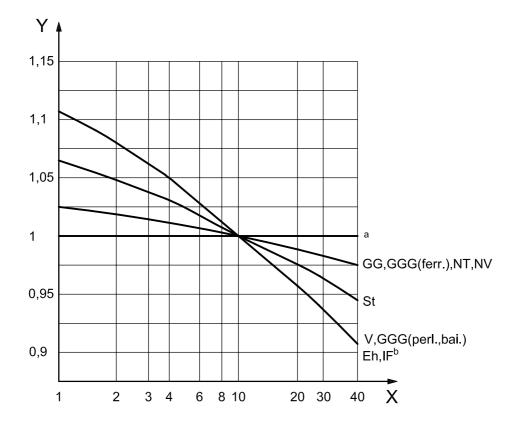
#### 14.2.2 Method B

The material strength values provided are derived in accordance with Method B, from results of tests of standard reference test gears of which  $Rz_T = 10 \, \mu \text{m}$ . In general, the value  $Y_{\text{R rel T}}$  relevant to the reference stress of any gear of interest differs little from 1,0, since  $Rz_T = 10 \, \mu \text{m}$  is a common mean value.  $Y_{\text{R rel T}}$  for static stress may also be made equal to 1,0.

#### 14.3 Relative surface factor, $Y_{R \text{ rel } T}$ : Method B

#### 14.3.1 Graphical values

 $Y_{\mathsf{R}\;\mathsf{rel}\;\mathsf{T}}$  can be taken from Figure 14 as a function of the material and Rz, the peak-to-valley roughness in the tooth root fillets of the gear of interest. This graph is derived from Figure A.1.



X roughness, Rz, μm

Y relative surface factor,  $Y_{R \text{ rel T}}$ 

NOTE See ISO 6336-1:2006, Table 2, for an explanation of the abbreviations used.

a For static stress and all materials.

b (root).

Figure 14 — Relative surface factor,  $Y_{\text{R rel T}}$  (derived from Figure A.1)

#### 14.3.2 Determination by calculation

#### 14.3.2.1 $Y_{R \text{ rel T}}$ for reference stress

 $Y_{\text{R rel T}}$  can be calculated using Equations (55) to (61). These are consistent with the curves in Figure 14 (see ISO 6336-1:2006, Table 2, for an explanation of the abbreviations used).

- a) Reference stress in the range  $Rz < 1 \mu m$ 
  - for V, GGG (perl., bai.), Eh and IF (root):

$$Y_{R \text{ rel } T} = 1,12$$
 (55)

- for St:

$$Y_{R \text{ rel T}} = 1,07$$
 (56)

— for GG, GGG (ferr.) and NT, NV:

$$Y_{\text{R rel T}} = 1,025$$
 (57)

- b) Reference stress in the range 1  $\mu$ m  $\leq Rz \leq$  40  $\mu$ m
  - for V, GGG (perl., bai.), Eh and IF (root):

$$Y_{\text{R rel T}} = 1,674 - 0,529 (Rz + 1)^{0,1}$$
 (58)

— for St:

$$Y_{R, rel, T} = 5,306 - 4,203 (Rz + 1)^{0,01}$$
 (59)

— for GG, GGG (ferr.) and NT, NV:

$$Y_{\text{R rel T}} = 4,299 - 3,259 (Rz + 1)^{0,005 8}$$
 (60)

#### 14.3.2.1.1 $Y_{R \text{ rel T}}$ for static stress

$$Y_{R \text{ rel } T} = 1,0.$$
 (61)

### 15 Size factor, $Y_X$

The size factor,  $Y_X$ , is used to take into consideration the influence of size on the probable distribution of weak points in the structure of the material, the stress gradients, which, in accordance with strength of materials theory, decrease with increasing dimensions, the quality of the material as determined by the extent and effectiveness of forging, the presence of defects, etc.

The following have significant influence:

- a) material, its cleanliness, chemistry, and forging process;
- b) heat-treatment, depth and uniformity of hardening;
- c) module, in the case of surface-hardening: case depth in relation to tooth size (core support effect).

Size factor  $Y_X$  shall be determined separately for the pinion and wheel.

#### 15.1 Size factor, $Y_X$ : Method A

The value of size factor  $Y_X$  shall be based on reliable experience or testing under the relevant operating conditions of a range of different sizes of gears in each material of interest, appropriately heat-treated. The provisions given in ISO 6336-1:2006, 4.1.12, are relevant.

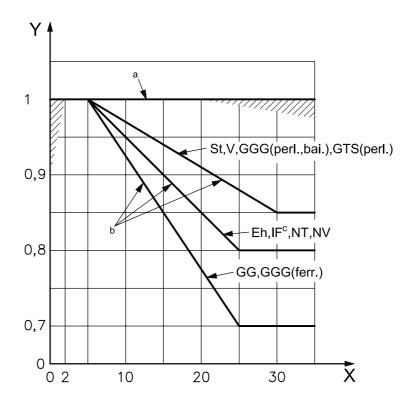
#### 15.2 Size factor, $Y_X$ : Method B

The values provided are based on the results of testing gears and bending strength test pieces of different sizes, due regard being paid to the current standards and practices of established heat-treatment practitioners.

#### 15.2.1 Size factor, $Y_{\chi}$ , for reference stress and static stress

#### 15.2.1.1 Graphical values

The value of  $Y_X$  may be taken from Figure 15 as a function of the module, material and heat-treatment.



#### Key

- X normal module,  $m_n$ , mm
- Y size factor,  $Y_X$

NOTE 1 See ISO 6336-1:2006, Table 2, for an explanation of the abbreviations used.

NOTE 2 Shaded area is in the range of scatter for static stress.

- a Static stress (all materials).
- b Reference stress.
- c (root).

Figure 15 — Size factor,  $Y_{\chi}$ , for tooth bending strength

#### 15.2.1.2 Determination by calculation

 $Y_X$  may be calculated using the equations in Table 3, which are consistent with the curves given in Figure 15.

## 15.2.2 Size factor, $Y_X$ , for limited life

 $Y_{\rm X}$  is obtained by means of linear interpolation between the values for the reference stress and the static stress as determined in accordance with 5.3.2. This formulation is included in the determination of permissible stress for limited life, according to 5.3.3.

Table 3 — Size factor (root),  $Y_{\chi}$ 

Material <sup>a</sup>		Normal module, $m_{n}$	Size factor, $Y_X$			
St, V, GGG (perl., bai.), GTS (perl.),		$m_{n} \leqslant 5$ $5 < m_{n} < 30$ $30 \leqslant m_{n}$	$Y_X = 1.0$ $Y_X = 1.03 - 0.006 m_0$ $Y_X = 0.85$			
Eh, IF (root), NT, NV	For 3 × 10 <sup>6</sup> cycles	$m_{n} \leqslant 5$ $5 < m_{n} < 25$ $25 \leqslant m_{n}$	$Y_{X} = 1.0$ $Y_{X} = 1.05 - 0.01 m_{n}$ $Y_{X} = 0.8$			
GG, GGG (ferr.)		$m_{n} \leqslant 5$ $5 < m_{n} < 25$ $25 \leqslant m_{n}$	$Y_{X} = 1.0$ $Y_{X} = 1.075 - 0.015 m_{n}$ $Y_{X} = 0.7$			
All materials for static stress	·	_	$Y_{X} = 1,0$			
<sup>a</sup> See ISO 6336-1:2006, Table 2 for an explanation of the abbreviations used.						

## Annex A

(normative)

# Permissible bending stress, $\sigma_{\rm FP}$ , obtained from notched, flat or plain polished test pieces

## A.1 Methods for determining permissible bending stress, $\sigma_{\rm FP}$ — Principles, assumptions and application

#### A.1.1 Method B<sub>k</sub>

The permissible bending stress is to be derived from the bending stress number  $\sigma_{\rm k\;lim}$  and life factor  $Y_{\rm Nk}$  results, usually presented as S-N or damage curves, of the pulsator fatigue testing of notched, flat test pieces. As in the case for Method B, the test data shall be transformed to suit the gears of interest, using the influence factors appropriate to both the method and the test piece:  $Y_{\delta\;{\rm rel}\;k}$  for notch sensitivity,  $Y_{\rm R\;rel\;k}$  for surface roughness and size factor  $Y_{\rm X}$  in accordance with Method B.

This method can be applied when values obtained from test gears are not available, and is particularly suitable for evaluating, relative to one another, the tooth root strength values for different materials.

## A.1.2 Method B<sub>p</sub>

The permissible bending stresses are to be derived from the bending stress number  $\sigma_{\rm p\ lim}$  and life factor  $Y_{\rm Np}$  results, usually presented as S-N or damage curves, of the pulsator fatigue testing of plain, polished test pieces. As in the case for Method B, the test data shall be transformed to suit the gears of interest, using the (absolute) influence factors appropriate to the method and the test piece:  $Y_{\delta}$  for notch sensitivity,  $Y_{\rm R}$  for surface roughness, and size factor  $Y_{\rm X}$  in accordance with Method B.

This method can be applied when values obtained from either gears or notched test pieces are not available, and is particularly suitable for evaluating, relative to one another, the tooth root strength values for different materials.

#### A.2 Permissible bending stress, $\sigma_{FP}$ : Method B<sub>k</sub>

#### A.2.1 $\sigma_{FP}$ for static stress and reference stress

Using these methods, the permissible bending stress is calculated on the basis of the strength of a notched test piece from Equation (A.1):

$$\sigma_{\text{FP}} = \frac{\sigma_{\text{k lim}} Y_{\text{Sk}} Y_{\text{Nk}}}{S_{\text{Fmin}}} Y_{\text{S rel K}} Y_{\text{R rel k}} Y_{\text{X}} = \frac{\sigma_{\text{FG}}}{S_{\text{Fmin}}}$$
(A.1)

where

 $\sigma_{\rm k\ lim}$  is the nominal notched-bar stress number (bending), which is the bending stress limit value of the notched-bar test piece relevant to its material, heat treatment and surface condition in relation to its dimensions (see recommendation below);

 $Y_{Sk}$  is the stress correction factor, relevant to the notched test piece;

 $Y_{Nk}$  is the life factor for tooth root stress, relevant to the notched test piece, which is used to take into account the higher load bearing capacity for a limited number of load cycles;

- $Y_{\delta \, \text{rel k}}$  is the relative notch sensitivity factor, which is the quotient of the notch sensitivity factor of the gear of interest divided by the notched test piece factor (see A.6), and which enables the influence of the notch sensitivity of the material to be taken into account;
- Y<sub>R rel k</sub> is the relative roughness factor, which is the quotient of the tooth root fillet roughness factor of the gear of interest divided by the notched test piece factor (see A.7), and which enables relevant surface roughness of tooth root fillet influences to be taken into account.

For  $\sigma_{k \text{ lim}}$ , differences between the properties of the heat treated materials, application of stresses and sections of test piece and gear of interest due to conditions of manufacture should be taken into consideration.

Other relevant symbols are defined in 5.3.2.

The values of the factors related to the notched test piece ( $\sigma_{\rm k\ lim}$ ,  $Y_{\rm Sk}$  and  $Y_{\rm Nk}$ ) shall be determined by tests or to be taken from literature (see A.5). Evaluations of  $\sigma_{\rm k\ lim}$ , and all corresponding influence factors shall be based on values of static stress and reference stress appropriate to the notched test piece.

The influence factors shall be determined in accordance with 5.3.2.

#### A.2.2 $\sigma_{FP}$ for limited life

The value of  $\sigma_{\text{FP}}$  shall be determined in accordance with 5.3.3.

## A.3 Permissible bending stress, $\sigma_{FP}$ : Method B<sub>D</sub>

For these methods the permissible bending stress is calculated on the basis of the strength of a plain, polished test piece from Equation (A.2):

$$\sigma_{\mathsf{FP}} = \frac{\sigma_{\mathsf{P}\,\mathsf{lim}} \, Y_{\mathsf{Np}}}{S_{\mathsf{Fmin}}} \, Y_{\mathcal{S}} \, Y_{\mathsf{R}} \, Y_{\mathsf{X}} = \frac{\sigma_{\mathsf{FG}}}{S_{\mathsf{Fmin}}} \tag{A.2}$$

where

- $\sigma_{\text{p lim}}$  is the nominal plain-bar stress number (bending), which is the bending stress limit value of the plain-bar test piece relevant to its material and heat treatment in relation to its dimensions (see recommendations, below);
- $Y_{\text{Np}}$  is the life factor for tooth root stress, relevant to the plain, polished test piece which is used in order to take into account the higher load capacity for a limited number of cycles;
- $Y_{\delta}$  is the notch sensitivity factor of the gear of interest, as related to a plain, polished test piece, which enables the influence of the notch sensitivity of the material to be taken into account;
- $Y_{\mathsf{R}}$  is the surface factor of the gear of interest, as related to the plain, polished test piece, which enables relevant surface roughness influences to be taken into account.

For  $\sigma_{k \text{ lim}}$ , differences between the properties of the heat treated materials of the test piece and gear of interest due to conditions of manufacture should be taken into consideration.

Other relevant terms and symbols are defined in 5.3.2.

Evaluations of  $\sigma_{\rm p\ lim}$  and  $Y_{\rm Np}$  for plain test pieces shall be based on tests or obtained from the literature (see A.5). Evaluations of  $\sigma_{\rm p\ lim}$  and all corresponding influence factors shall be based on values of static stress and reference stress.

The influence factors shall be determined in accordance with 5.3.2 and 5.3.3.

## A.4 Safety factor for bending strength (safety against tooth breakage), $S_F$

### A.4.1 Method B<sub>k</sub>

This procedure follows the methods described in 5.1, with  $\sigma_{FG}$  calculated in accordance with A.2.

#### A.4.2 Method B<sub>p</sub>

This procedure follows the methods according to 5.1, with  $\sigma_{FG}$  calculated in accordance with A.3.

## A.5 Reference stress for bending, with values $\sigma_{\rm k \; lim}$ and $\sigma_{\rm p \; lim}$ for Methods B<sub>k</sub> and B<sub>p</sub>

Refer to A.1.1 and A.1.2 for information on these values. The bending stress numbers  $\sigma_{k \text{ lim}}$  and  $\sigma_{p \text{ lim}}$  are derived from the results of pulsator bending tests of notched or plain test pieces, or else can be found in the literature.

## A.6 Sensivity factor, $Y_{\delta k}$ and relative notch sensivity Factor $Y_{\delta \text{ rel } k}$

#### A.6.1 Basic uses

The comments made in 13.1 apply to  $Y_{\partial k}$  in relation to breakage of a notched test piece. Those comments also apply to the relative sensitivity factors which relate the sensitivity of a gear of interest to that of a notched test piece  $(Y_{\delta \text{ rel }k})$ .

#### A.6.2 Determination of the sensivity factors

#### A.6.2.1 Method B<sub>k</sub>

Since, by Method B<sub>k</sub>, material strength values are derived from notched test-piece tests, the more closely the value  $q_{\rm sk}$  of the notched test-piece approaches that of the gear of interest, the more closely the value of  $Y_{\delta \, {\rm rel} \, \, k}$  approaches 1,0.

#### A.6.2.2 Method B<sub>n</sub>

Since, by Method  $B_p$ , material strength values are derived from the tests of plain, polished test-pieces, it is necessary that in this method the absolute sensitivity factor  $Y_{\delta}$  be used.

#### A.6.3 Relative notch sensitivity factor, $Y_{\delta \text{ rel }k}$ : Method B<sub>k</sub>

#### A.6.3.1 Graphical values

#### A.6.3.1.1 $Y_{\delta \text{ rel } k}$ for reference stress

 $Y_{\delta}$  for the gear of interest and  $Y_{\delta k}$  for the notched test-piece are taken from Figure 12 as a function of  $q_{\delta}$  (the gear),  $q_{\delta k}$  (the test-piece) and for the appropriate material. These values are substituted in Equation (A.3) to obtain  $Y_{\delta rel k}$ :

$$Y_{\delta \text{ rel k}} = \frac{Y_{\delta}}{Y_{\delta k}} \tag{A.3}$$

## A.6.3.1.2 $Y_{\delta \text{rel k}}$ for static stress

 $Y_{\mathcal{S}}$  for the gear of interest and  $Y_{\mathcal{S}k}$  for the notched test-piece are taken from Figure 13 as a function of  $Y_{\mathcal{S}}$  (gear),  $Y_{\mathcal{S}k}$  (test-piece) and for the appropriate material. The values are to be substituted in Equation (A.3) to determine  $Y_{\mathcal{S}\text{rel }k}$  for static stress. Values of  $Y_{\mathcal{S}k}$ , the stress correction factor for the notched test-piece (corresponding to the form factor of the notch), can be obtained from the literature.

#### A.6.3.2 Determination by calculation

## A.6.3.2.1 $Y_{\delta \text{ rel } k}$ for reference stress

 $Y_{\delta \text{ rel k}}$  can be calculated using Equation (A.4) and numerical values given Table 2:

$$Y_{\delta \text{ rel k}} = \frac{Y_{\delta}}{Y_{\delta k}} = \frac{1 + \sqrt{\rho' \, \chi^*}}{1 + \sqrt{\rho' \, \chi^*_k}} \tag{A.4}$$

Where  $\chi_{\mathbf{k}}^{\star}$ , the relevant stress gradient in the notch root of the test-piece, is determined by substituting the test-piece value  $q_{\mathbf{sk}}$  in Equation (49) for  $q_{\mathbf{s}}$ .

#### A.6.3.2.2 $Y_{\delta \text{ rel k}}$ for static stress

 $Y_{\delta}$  can be calculated in accordance with A.6.4.2.2;  $Y_{\delta k}$  can be calculated using Equations (A.5) to (A.9), which are consistent with the curves in Figure 13. Substitution of the two values in Equation (A.4) gives  $Y_{\delta \text{ rel }k}$ .

a) For St with well defined yield point:

$$Y_{\delta k} = 1 + 0.93 (Y_{Sk} - 1) \sqrt[4]{\frac{200}{\sigma_S}}$$
 (A.5)

b) For St with steadily increasing elongation curve and 0,2 % proof stress, V and GGG (perl., bai.):

$$Y_{\delta k} = 1 + 0.82 (Y_{Sk} - 1) \sqrt[4]{\frac{300}{\sigma_{0,2}}}$$
 (A.6)

c) For Eh and IF(root) with stress up to crack initiation:

$$Y_{\partial k} = 0.77 \ Y_{sk} + 0.22$$
 (A.7)

d) For NT and NV with stress up to crack initiation:

$$Y_{\partial k} = 0.27 Y_{sk} + 0.72$$
 (A.8)

e) For GG and GGG (ferr.) with stress up to fracture limit:

$$Y_{Ak} = 1,0 \tag{A.9}$$

#### A.6.4 Determination of sensitivity factor, $Y_{\delta}$ : Method $B_{D}$

#### A.6.4.1 Graphical values

#### A.6.4.1.1 $Y_{\delta}$ for reference stress

 $Y_{\delta}$  can be taken from Figure 12 as a function of  $Y_{Sa}$  or  $q_{S}$  and the material, all relevant to the gear of interest.

#### A.6.4.1.2 $Y_{\delta}$ for static stress

 $Y_{\delta}$  can be taken from Figure 13 as a function of  $Y_{\delta}$ , the stress correction factor, and the material of the gear of interest.

#### A.6.4.2 Determination by calculation

#### A.6.4.2.1 $Y_{\delta}$ for reference stress

 $Y_{\delta}$  may be calculated using Equation (A.10) and the numerical values given in Table 2:

$$Y_{\mathcal{S}} = \frac{1 + \sqrt{\rho' \, \chi^*}}{1 + \sqrt{\rho' \, \chi^*_{p}}} \tag{A.10}$$

#### A.6.4.2.2 $Y_{\delta}$ for static stress

The maximum possible value of the static sensitivity factor is equal to that of the stress correction factor,  $Y_S$ . Such a value would imply that the material is in a fully plastic state (see ISO 6336-1:2006, Table 2, for an explanation of abbreviations used):

a) For St with well defined yield point:

$$Y_{\delta} = 1 + 0.93 (Y_{S} - 1) \sqrt[4]{\frac{200}{\sigma_{S}}}$$
 (A.11)

b) For St with steadily increasing elongation curve and 0,2 % proof stress, V and GGG (perl., bai.):

$$Y_{\mathcal{S}} = 1 + 0.82 (Y_{S} - 1) \sqrt[4]{\frac{300}{\sigma_{0,2}}}$$
 (A.12)

c) For Eh and IF(root) with stress up to crack initiation:

$$Y_{\delta} = 0.77 Y_{S} + 0.22$$
 (A.13)

d) For NT and NV with stress up to crack initiation:

$$Y_{\delta} = 0.27 Y_{S} + 0.72$$
 (A.14)

e) For GG and GGG (ferr.) with stress up to fracture limit:

$$Y_{3k} = 1,0$$
 (A.15)

## A.7 Surface factor, $Y_{Rk}$ , and relative surface factor, $Y_{R rel k}$

The surface factor,  $Y_{\rm Rk}$ , accounts for the influence on tooth root stress of the surface condition in the tooth roots. This is dependent on the material and the surface roughness in the tooth root fillets (see Note to, and final paragraph of, 14.1).  $Y_{\rm Rk}$ , the surface factor relevant to a rough notched test-piece for static stress is different from  $Y_{\rm Rk}$  for dynamic stress. These factors are compared to that of a plain, polished test piece. Relative surface factors represent the relationship of the surface factor of a gear of interest to that of a rough notched test-piece ( $Y_{\rm R rel \ k}$ ).

#### A.7.1 Determination of surface factor and relative surface factor

#### A.7.1.1 Method B<sub>k</sub>

Since by Method  $B_k$ , material strength values are derived from notched, rough, test piece tests, the more closely the values  $Rz_k$  and  $q_{sk}$  of the notched test-piece approach those of the gear of interest, the more closely the value of  $Y_{R rel k}$  approaches 1,0.

## A.7.1.2 Method B<sub>p</sub>

In Method  $B_p$ , material strength values are determined by testing plain polished test pieces, in which case it is necessary that the absolute surface factor  $Y_R$  be used in calculations. As roughness in a root fillet constitutes "notches within a notch", the influence of  $Y_R$  is somewhat reduced (see Note to, and final paragraph of 14.1):

$$Y_{R} = Y_{R0} + (1 - Y_{R0}) \left(\frac{Y_{S} - 1}{Y_{S}}\right)^{2}$$
 (A.16)

where  $Y_{R0}$  is the surface factor of the plain, polished test-piece.

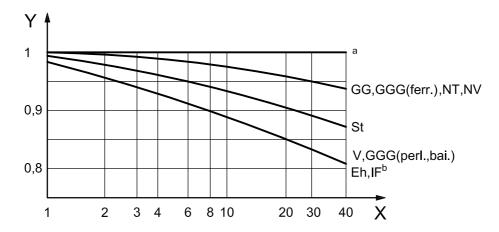
An approximate average value can be obtained when  $Y_S$  is made equal to 2,0. Figure A.1 has been plotted using this value.

## A.7.2 Relative surface factor, $Y_{R rel k}$ : Method $B_k$

#### A.7.2.1 Graphical values

Obtain from Figure A.1,  $Y_R$  for the gear of interest and  $Y_{Rk}$  for the notched test piece, as a function of

- a) the peak-to-valley roughnesses, Rz, of the gear tooth root or  $Rz_k$  of the test piece notch-root, and
- b) the material of interest.



#### Key

X roughness Rz,  $Rz_k$ ,  $\mu m$ 

Y surface factor,  $Y_R$ ,  $Y_{Rk}$ 

NOTE See ISO 6336-1:2006, Table 2, for an explanation of the abbreviations used.

- a For static stress and all materials.
- b (root).

Figure A.1 — Surface factor,  $Y_R$  and  $Y_{Rk}$  (related to the smooth polished test piece)

These values are to be substituted in Equation (A.17).

$$Y_{\mathsf{Rk}} = \frac{Y_{\mathsf{R}}}{Y_{\mathsf{Rk}}} \tag{A.17}$$

#### A.7.2.2 Determination by calculation

Obtain  $Y_R$  following the directions in A.7.3.2.2, and obtain  $Y_{Rk}$  using Equations (A.18) to (A.21), which are consistent with the curves in Figure A.1. Introduce these values in Equation (A.17).

#### A.7.2.2.1 $Y_{R \text{ rel } k}$ for static stress (in general) and reference stress in range $Rz_k < 1 \ \mu m$

$$Y_{\mathbf{Rk}} = 1.0 \tag{A.18}$$

## A.7.2.2.2 $Y_{R \text{ rel } k}$ for reference stress in the range 1 $\mu$ m < $Rz_k$ < 40 $\mu$ m

a) For V, GGG (perl., bai.,), Eh and IF (root):

$$Y_{Rk} = 1,490 - 0,471 (Rz_k + 1)^{0,1}$$
 (A.19)

b) For St:

$$Y_{\mathsf{Rk}} = 4,924 - 3,90 \left( Rz_{\mathsf{k}} + 1 \right)^{0,01}$$
 (A.20)

c) For GG, GGG (ferr.) and NT, NV:

$$Y_{\mathsf{Rk}} = 4,161 - 3,155 \left( Rz_{\mathsf{k}} + 1 \right)^{0,005}$$
 (A.21)

## A.7.3 Surface factor, $Y_R$ : Method $B_p$

#### A.7.3.1 Graphical values

 $Y_{\mathsf{R}}$  for reference stress and static stress can be taken from Figure A.1 as a function of Rz, the peak-to-valley roughness in the tooth root fillets of the gear of interest and of the material. The derivation of  $Y_{\mathsf{R}}$  for limited life follows, in principle, the procedure given in A.7.3.2.

## A.7.3.2 Determination by calculation

 $Y_{R}$  can be calculated using Equations (A.22) to (A.25), which are consistent with the curves in Figure A.1.

#### A.7.3.2.1 $Y_R$ for static stress (in general) and reference stress in range $Rz < 1 \ \mu m$

$$Y_{\mathsf{R}} = 1,0$$
 (A.22)

#### **A.7.3.2.2** $Y_R$ for reference stress in range 1 $\mu$ m $\leq Rz \leq 40 \mu$ m

a) For V, GGG (perl., bai.), Eh and IF (root):

$$Y_{R} = 1,490 - 0,471 (Rz + 1)^{0,1}$$
 (A.23)

b) For St:

$$Y_{\mathsf{R}} = 4,924 - 3,90 \left(Rz + 1\right)^{0,01}$$
 (A.24)

c) For GG, GGG (ferr.) and NT, NV:

$$Y_{R} = 4,161 - 3,155 (Rz + 1)^{0,005}$$
 (A.25)

## Annex B

(informative)

## Guide values for mean stress influence factor, $\emph{Y}_{\text{M}}$

NOTE This annex does not conform with ISO 6336-5, in which the influence of reverse loading is covered by a factor 0,7.

The mean stress influence factor,  $Y_{\text{M}}$ , takes into account the influence of working stress conditions other than pure pulsations, e.g. load reversings, idler gears or idler and planetary gears.

 $Y_{\text{M}}$  is defined as the ratio between the endurance (or static) strength with a stress ratio  $R \neq 0$ , and the endurance (or static) strength with R = 0 to be included in Equation (5).

 $Y_{\rm M}$  applies only to a calculation method which assesses the positive (tensile) stresses and which is therefore suitable for comparison between the calculated (positive) working stress  $\sigma_{\rm F}$  and the permissible stress  $\sigma_{\rm FP}$  multiplied with  $Y_{\rm M}$ . The following method may be used within a stress ratio 1 > R > 0.

#### B.1 Idler and planetary gears

The mean stress influence factor,  $Y_{\rm M}$ , can be calcutated as follows:

$$Y_{\mathsf{M}} = \frac{1}{1 - R \frac{1 - M}{1 + M}} \tag{B.1}$$

where

R is the stress ratio;

M considers the mean stress influence on the endurance (or static) strength amplitudes, and is defined as the reduction of the endurance strength amplitude for a certain increase of the mean stress divided by that increase of the mean stress (the values listed in Table B.1 may be used for M, see explanation below).

#### Simplification:

For designs with the same load applied both on forward- and back-flank, R may be assumed to equal -1,2. For designs with considerably different loads on forward- and back-flank, R may be assumed to be as follows:

$$R = -1.2 \frac{\text{load per unit facewidth of the lower loaded flank}}{\text{load per unit facewidth of the higher loaded flank}}$$

The listed values for M for the endurance limit are independent of the fillet shape, except for case hardening. In principle, there is a dependency of the static notch sensivity factor (and thereby indirectly  $Y_{\rm S}$ ), but wide variations usually only occur for case hardening, e.g. smooth semicircular versus grinding notches.

Table B.1 — Mean stress ratio,  ${\it M}$ 

	Endurance limit	Static strength
Case hardened	0,8 – 0,15 Y <sub>S</sub>	0,7
Case hardened and shot peened	0,4	0,6
Nitrided	0,3	0,3
Induction or flame hardened	0,4	0,6
Not surface hardened steels	0,3	0,5
Cast steels	0,4	0,6

## B.2 Gears with periodical change of rotational direction

For case hardened gears with full load applied periodically in both directions, the same equations for  $Y_{\rm M}$  as for idler gears (with R=1) may be used together with the values for M for the endurance limit. This simplified approach is valid when the number of changes of directions exceeds 100 and the total number of load cycles exceeds  $3\times10^6$ .

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