

NEWTON'S LAWS OF MOTION

4



? The standing child is pushing the child seated on the swing. Is the seated child pushing back? If so, is he pushing with the same amount of force or a different amount?

We've seen in the last two chapters how to describe motion in one, two, or three dimensions. But what are the underlying *causes* of motion? For example, how can a tugboat push a cruise ship that's much heavier than the tug? Why is it harder to control a car on wet ice than on dry concrete? The answers to these and similar questions take us into the subject of **dynamics**, the relationship of motion to the forces that cause it. In the two preceding chapters we studied *kinematics*, the language for *describing* motion. Now we are ready to think about what makes bodies move the way they do.

In this chapter we will use two new concepts, *force* and *mass*, to analyze the principles of dynamics. These principles can be wrapped up in just three statements that were clearly stated for the first time by Sir Isaac Newton (1642–1727), who published them in 1687 in his *Philosophiae Naturalis Principia Mathematica* (“Mathematical Principles of Natural Philosophy”). These three statements are called **Newton's laws of motion**. The first law states that when the net force on a body is zero, its motion doesn't change. The second law relates force to acceleration when the net force is *not* zero. The third law is a relationship between the forces that two interacting bodies exert on each other.

Newton's laws are not the product of mathematical derivations, but rather a synthesis of what physicists have learned from a multitude of *experiments* about how objects move. (Newton used the ideas and observations of many scientists before him, including Copernicus, Brahe, Kepler, and especially Galileo Galilei, who died the same year Newton was born.) These laws are truly fundamental, for they cannot be deduced or proved from other principles. Newton's laws are the foundation of **classical mechanics** (also called **Newtonian mechanics**); using them we can understand most familiar kinds of motion. Newton's laws need modification only for situations involving extremely high speeds (near the speed of light) or very small sizes (such as within the atom).

Newton's laws are very simple to state, yet many students find these laws difficult to grasp and to work with. The reason is that before studying physics,

LEARNING GOALS

By studying this chapter, you will learn:

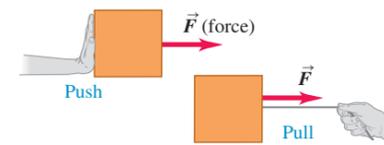
- What the concept of force means in physics, and why forces are vectors.
- The significance of the net force on an object, and what happens when the net force is zero.
- The relationship among the net force on an object, the object's mass, and its acceleration.
- How the forces that two bodies exert on each other are related.

you've spent years walking, throwing balls, pushing boxes, and doing dozens of things that involve motion. Along the way, you've developed a set of "common sense" ideas about motion and its causes. But many of these "common sense" ideas don't stand up to logical analysis. A big part of the job of this chapter—and of the rest of our study of physics—is helping you to recognize how "common sense" ideas can sometimes lead you astray, and how to adjust your understanding of the physical world to make it consistent with what experiments tell us.

4.1 Force and Interactions

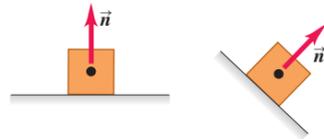
4.1 Some properties of forces.

- A force is a push or a pull.
- A force is an interaction between two objects or between an object and its environment.
- A force is a vector quantity, with magnitude and direction.

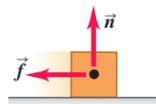


4.2 Four common types of forces.

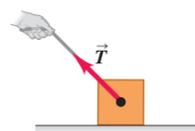
(a) **Normal force \vec{n} :** When an object rests or pushes on a surface, the surface exerts a push on it that is directed perpendicular to the surface.



(b) **Friction force \vec{f} :** In addition to the normal force, a surface may exert a frictional force on an object, directed parallel to the surface.



(c) **Tension force \vec{T} :** A pulling force exerted on an object by a rope, cord, etc.



(d) **Weight \vec{w} :** The pull of gravity on an object is a long-range force (a force that acts over a distance).



In everyday language, a **force** is a push or a pull. A better definition is that a force is an *interaction* between two bodies or between a body and its environment (Fig. 4.1). That's why we always refer to the force that one body *exerts* on a second body. When you push on a car that is stuck in the snow, you exert a force on the car; a steel cable exerts a force on the beam it is hoisting at a construction site; and so on. As Fig. 4.1 shows, force is a *vector* quantity; you can push or pull a body in different directions.

When a force involves direct contact between two bodies, such as a push or pull that you exert on an object with your hand, we call it a **contact force**. Figures 4.2a, 4.2b, and 4.2c show three common types of contact forces. The **normal force** (Fig. 4.2a) is exerted on an object by any surface with which it is contact. The adjective *normal* means that the force always acts perpendicular to the surface of contact, no matter what the angle of that surface. By contrast, the **friction force** (Fig. 4.2b) exerted on an object by a surface acts *parallel* to the surface, in the direction that opposes sliding. The pulling force exerted by a stretched rope or cord on an object to which it's attached is called a **tension force** (Fig. 4.2c). When you tug on your dog's leash, the force that pulls on her collar is a tension force.

In addition to contact forces, there are **long-range forces** that act even when the bodies are separated by empty space. The force between two magnets is an example of a long-range force, as is the force of gravity (Fig. 4.2d); the earth pulls a dropped object toward it even though there is no direct contact between the object and the earth. The gravitational force that the earth exerts on your body is called your **weight**.

To describe a force vector \vec{F} , we need to describe the *direction* in which it acts as well as its *magnitude*, the quantity that describes "how much" or "how hard" the force pushes or pulls. The SI unit of the magnitude of force is the *newton*, abbreviated N. (We'll give a precise definition of the newton in Section 4.3.) Table 4.1 lists some typical force magnitudes.

Table 4.1 Typical Force Magnitudes

Sun's gravitational force on the earth	3.5×10^{22} N
Thrust of a space shuttle during launch	3.1×10^7 N
Weight of a large blue whale	1.9×10^6 N
Maximum pulling force of a locomotive	8.9×10^5 N
Weight of a 250-lb linebacker	1.1×10^3 N
Weight of a medium apple	1 N
Weight of smallest insect eggs	2×10^{-6} N
Electric attraction between the proton and the electron in a hydrogen atom	8.2×10^{-8} N
Weight of a very small bacterium	1×10^{-18} N
Weight of a hydrogen atom	1.6×10^{-26} N
Weight of an electron	8.9×10^{-30} N
Gravitational attraction between the proton and the electron in a hydrogen atom	3.6×10^{-47} N

A common instrument for measuring force magnitudes is the *spring balance*. It consists of a coil spring enclosed in a case with a pointer attached to one end. When forces are applied to the ends of the spring, it stretches by an amount that depends on the force. We can make a scale for the pointer by using a number of identical bodies with weights of exactly 1 N each. When one, two, or more of these are suspended simultaneously from the balance, the total force stretching the spring is 1 N, 2 N, and so on, and we can label the corresponding positions of the pointer 1 N, 2 N, and so on. Then we can use this instrument to measure the magnitude of an unknown force. We can also make a similar instrument that measures pushes instead of pulls.

Figure 4.3 shows a spring balance being used to measure a pull or push that we apply to a box. In each case we draw a vector to represent the applied force. The labels indicate the magnitude and direction of the force. The length of the vector also shows the magnitude; the longer the vector, the greater the force magnitude.

Superposition of Forces

When you throw a ball, there are at least two forces acting on it: the push of your hand and the downward pull of gravity. Experiment shows that when two forces \vec{F}_1 and \vec{F}_2 act at the same time at a point A of a body (Fig. 4.4), the effect on the body's motion is the same as if a single force \vec{R} were acting equal to the *vector sum* of the original forces: $\vec{R} = \vec{F}_1 + \vec{F}_2$. More generally, *any number of forces applied at a point on a body have the same effect as a single force equal to the vector sum of the forces*. This important principle is called **superposition of forces**.

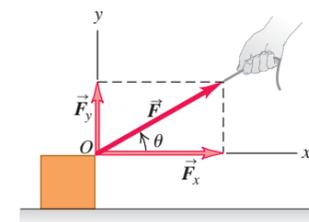
The experimental discovery that forces combine according to vector addition is of the utmost importance, and we will use this fact throughout our study of physics. It allows us to replace a force by its component vectors, as we did with displacements in Section 1.8. For example, in Fig. 4.5a, force \vec{F} acts on a body at point O. The component vectors of \vec{F} in the directions Ox and Oy are \vec{F}_x and \vec{F}_y . When \vec{F}_x and \vec{F}_y are applied simultaneously, as in Fig. 4.5b, the effect is exactly the same as the effect of the original force \vec{F} . Hence *any force can be replaced by its component vectors, acting at the same point*.

It's frequently more convenient to describe a force \vec{F} in terms of its x- and y-components F_x and F_y rather than by its component vectors (recall from Section 1.8 that *component vectors* are vectors, but *components* are just numbers). For the case shown in Fig. 4.5, both F_x and F_y are positive; for other orientations of the force \vec{F} , either F_x or F_y can be negative or zero.

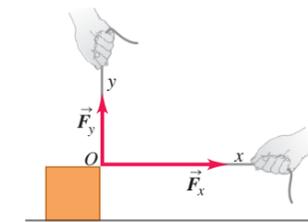
There is no law that says our coordinate axes have to be vertical and horizontal. Figure 4.6 shows a crate being pulled up a ramp by a force \vec{F} , represented by its components F_x and F_y parallel and perpendicular to the sloping surface of the ramp.

4.5 The force \vec{F} , which acts at an angle θ from the x-axis, may be replaced by its rectangular component vectors \vec{F}_x and \vec{F}_y .

(a) Component vectors: \vec{F}_x and \vec{F}_y
Components: $F_x = F \cos \theta$ and $F_y = F \sin \theta$

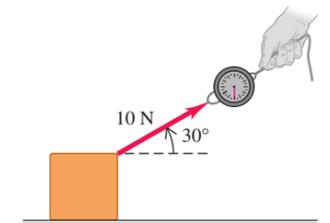


(b) Component vectors \vec{F}_x and \vec{F}_y together have the same effect as original force \vec{F} .

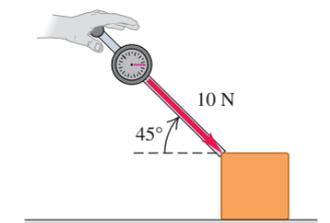


4.3 Using a vector arrow to denote the force that we exert when (a) pulling a block with a string or (b) pushing a block with a stick.

(a) A 10-N pull directed 30° above the horizontal

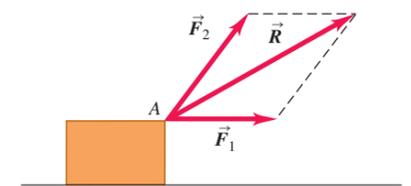


(b) A 10-N push directed 45° below the horizontal



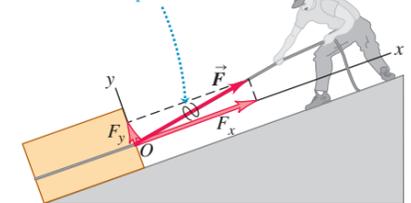
4.4 Superposition of forces.

Two forces \vec{F}_1 and \vec{F}_2 acting on a point A have the same effect as a single force \vec{R} equal to their vector sum.



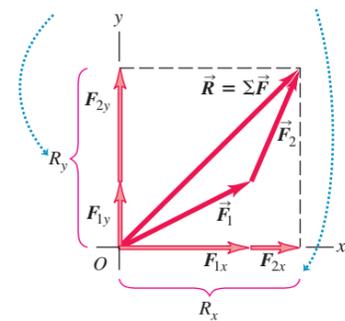
4.6 F_x and F_y are the components of \vec{F} parallel and perpendicular to the sloping surface of the inclined plane.

We cross out a vector when we replace it with its components.



4.7 Finding the components of the vector sum (resultant) \vec{R} of two forces \vec{F}_1 and \vec{F}_2 .

\vec{R} is the sum (resultant) of \vec{F}_1 and \vec{F}_2 .
The y-component of \vec{R} equals the sum of the y-components of \vec{F}_1 and \vec{F}_2 . The same goes for the x-components.



CAUTION Using a wiggly line in force diagrams In Fig. 4.6 we draw a wiggly line through the force vector \vec{F} to show that we have replaced it by its x - and y -components. Otherwise, the diagram would include the same force twice. We will draw such a wiggly line in any force diagram where a force is replaced by its components. Look for this wiggly line in other figures in this and subsequent chapters. ■

We will often need to find the vector sum (resultant) of *all* the forces acting on a body. We call this the **net force** acting on the body. We will use the Greek letter Σ (capital sigma, equivalent to the Roman S) as a shorthand notation for a sum. If the forces are labeled $\vec{F}_1, \vec{F}_2, \vec{F}_3,$ and so on, we abbreviate the sum as

$$\vec{R} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \dots = \Sigma \vec{F} \quad (4.1)$$

We read $\Sigma \vec{F}$ as “the vector sum of the forces” or “the net force.” The component version of Eq. (4.1) is the pair of component equations

$$R_x = \Sigma F_x \quad R_y = \Sigma F_y \quad (4.2)$$

Here ΣF_x is the sum of the x -components and ΣF_y is the sum of the y -components (Fig. 4.7). Each component may be positive or negative, so be careful with signs when you evaluate the sums in Eq. (4.2).

Once we have R_x and R_y , we can find the magnitude and direction of the net force $\vec{R} = \Sigma \vec{F}$ acting on the body. The magnitude is

$$R = \sqrt{R_x^2 + R_y^2}$$

and the angle θ between \vec{R} and the $+x$ -axis can be found from the relation $\tan \theta = R_y/R_x$. The components R_x and R_y may be positive, negative, or zero, and the angle θ may be in any of the four quadrants.

In three-dimensional problems, forces may also have z -components; then we add the equation $R_z = \Sigma F_z$ to Eq. (4.2). The magnitude of the net force is then

$$R = \sqrt{R_x^2 + R_y^2 + R_z^2}$$

Example 4.1 Superposition of forces

Three professional wrestlers are fighting over the same champion's belt. As viewed from above, they apply the three horizontal forces to the belt that are shown in Fig. 4.8a. The magnitudes of the three forces are $F_1 = 250$ N, $F_2 = 50$ N, and $F_3 = 120$ N. Find the x - and y -components of the net force on the belt, and find the magnitude and direction of the net force.

SOLUTION

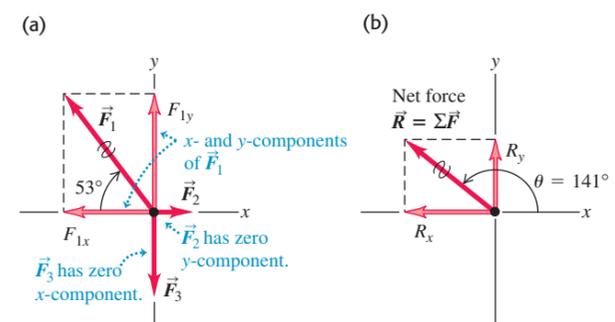
IDENTIFY: This example is just a problem in vector addition. The only new feature is that the vectors represent forces.

SET UP: We need to find the x - and y -components of the net force \vec{R} , so we'll use the component method of vector addition expressed by Eq. (4.2). Once we have the components of \vec{R} , we can find its magnitude and direction.

EXECUTE: From Fig. 4.8a, the angles between the three forces $\vec{F}_1, \vec{F}_2,$ and \vec{F}_3 and the $+x$ -axis are $\theta_1 = 180^\circ - 53^\circ = 127^\circ, \theta_2 = 0^\circ,$ and $\theta_3 = 270^\circ$. The x - and y -components of the three forces are

$$\begin{aligned} F_{1x} &= (250 \text{ N}) \cos 127^\circ = -150 \text{ N} \\ F_{1y} &= (250 \text{ N}) \sin 127^\circ = 200 \text{ N} \\ F_{2x} &= (50 \text{ N}) \cos 0^\circ = 50 \text{ N} \\ F_{2y} &= (50 \text{ N}) \sin 0^\circ = 0 \text{ N} \end{aligned}$$

4.8 (a) Three forces acting on a belt. (b) The net force $\vec{R} = \Sigma \vec{F}$ and its components.



$$\begin{aligned} F_{3x} &= (120 \text{ N}) \cos 270^\circ = 0 \text{ N} \\ F_{3y} &= (120 \text{ N}) \sin 270^\circ = -120 \text{ N} \end{aligned}$$

From Eq. (4.2) the net force $\vec{R} = \Sigma \vec{F}$ has components

$$\begin{aligned} R_x &= F_{1x} + F_{2x} + F_{3x} = (-150 \text{ N}) + 50 \text{ N} + 0 \text{ N} = -100 \text{ N} \\ R_y &= F_{1y} + F_{2y} + F_{3y} = 200 \text{ N} + 0 \text{ N} + (-120 \text{ N}) = 80 \text{ N} \end{aligned}$$

The net force has a negative x -component and a positive y -component, so it points to the left and toward the top of the page in Fig. 4.8b (that is, in the second quadrant).

The magnitude of the net force $\vec{R} = \Sigma \vec{F}$ is

$$R = \sqrt{R_x^2 + R_y^2} = \sqrt{(-100 \text{ N})^2 + (80 \text{ N})^2} = 128 \text{ N}$$

To find the angle between the net force and the $+x$ -axis, we use the relation $\tan \theta = R_y/R_x$, or

$$\theta = \arctan \frac{R_y}{R_x} = \arctan \left(\frac{80 \text{ N}}{-100 \text{ N}} \right) = \arctan(-0.80)$$

The two possible solutions are $\theta = -39^\circ$ and $\theta = -39^\circ + 180^\circ = 141^\circ$. Since the net force lies in the second quadrant, as mentioned earlier, the correct answer is 141° (see Fig. 4.8b).

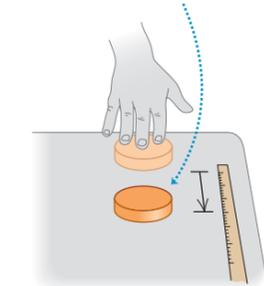
EVALUATE: In this situation the net force is *not* zero, and you can see intuitively that wrestler 1 (who exerts the largest force, \vec{F}_1 , on the belt) is likely to walk away with the belt at the end of the struggle. In Section 4.2 we will explore in detail what happens in situations in which the net force *is* zero.

Test Your Understanding of Section 4.1 Figure 4.6 shows a force \vec{F} acting on a crate. With the x - and y -axes shown in the figure, which statement about the components of the *gravitational* force that the earth exerts on the crate (the crate's weight) is *correct*? (i) The x - and y -components are both positive. (ii) The x -component is zero and the y -component is positive. (iii) The x -component is negative and the y -component is positive. (iv) The x - and y -components are both negative. (v) The x -component is zero and the y -component is negative. (vi) The x -component is positive and the y -component is negative.

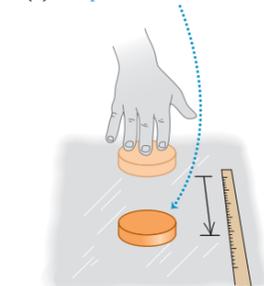


4.9 The slicker the surface, the farther a puck slides after being given an initial velocity. On an air-hockey table (c) the friction force is practically zero, so the puck continues with almost constant velocity.

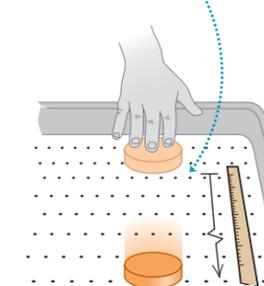
(a) Table: puck stops short.



(b) Ice: puck slides farther.



(c) Air-hockey table: puck slides even farther.



4.2 Newton's First Law

We have discussed some of the properties of forces, but so far have said nothing about how forces affect motion. To begin, let's consider what happens when the net force on a body is *zero*. You would almost certainly agree that if a body is at rest, and if no net force acts on it (that is, no net push or pull), that body will remain at rest. But what if there is zero net force acting on a body in *motion*?

To see what happens in this case, suppose you slide a hockey puck along a horizontal tabletop, applying a horizontal force to it with your hand (Fig. 4.9a). After you stop pushing, the puck *does not* continue to move indefinitely; it slows down and stops. To keep it moving, you have to keep pushing (that is, applying a force). You might come to the “common sense” conclusions that bodies in motion naturally come to rest and that a force is required to sustain motion.

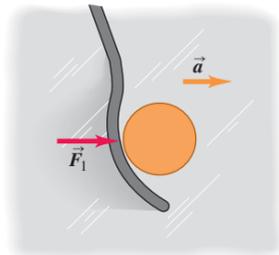
But now imagine pushing the puck across a smooth surface of ice (Fig. 4.9b). After you quit pushing, the puck will slide a lot farther before it stops. Put it on an air-hockey table, where it floats on a thin cushion of air, and it moves still farther (Fig. 4.9c). In each case, what slows the puck down is *friction*, an interaction between the lower surface of the puck and the surface on which it slides. Each surface exerts a frictional force on the puck that resists the puck's motion; the difference in the three cases is the magnitude of the frictional force. The ice exerts less friction than the tabletop, so the puck travels farther. The gas molecules of the air-hockey table exert the least friction of all. If we could eliminate friction completely, the puck would never slow down, and we would need no force at all to keep the puck moving once it had been started. Thus the “common sense” idea that a force is required to sustain motion is *incorrect*.

Experiments like the ones we've just described show that when no net force acts on a body, the body either remains at rest or moves with constant velocity in a straight line. Once a body has been set in motion, no net force is needed to keep it moving. We now call this observation *Newton's first law of motion*:

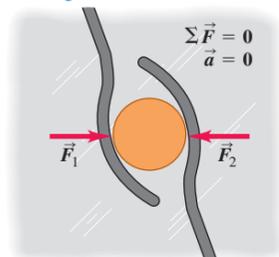
Newton's first law of motion: A body acted on by no net force moves with constant velocity (which may be zero) and zero acceleration.

4.10 (a) A hockey puck accelerates in the direction of a net applied force \vec{F}_1 . (b) When the net force is zero, the acceleration is zero, and the puck is in equilibrium.

(a) A puck on a frictionless surface accelerates when acted on by a single horizontal force.



(b) An object acted on by forces whose vector sum is zero behaves as though no forces act on it.



The tendency of a body to keep moving once it is set in motion results from a property called **inertia**. You use inertia when you try to get ketchup out of a bottle by shaking it. First you start the bottle (and the ketchup inside) moving forward; when you jerk the bottle back, the ketchup tends to keep moving forward and, you hope, ends up on your burger. The tendency of a body at rest to remain at rest is also due to inertia. You may have seen a tablecloth yanked out from under the china without breaking anything. The force on the china isn't great enough to make it move appreciably during the short time it takes to pull the tablecloth away.

It's important to note that the *net* force is what matters in Newton's first law. For example, a physics book at rest on a horizontal tabletop has two forces acting on it: an upward supporting force, or normal force, exerted by the tabletop (see Fig. 4.2a) and the downward force of the earth's gravitational attraction (a long-range force that acts even if the tabletop is elevated above the ground; see Fig. 4.2d). The upward push of the surface is just as great as the downward pull of gravity, so the *net* force acting on the book (that is, the vector sum of the two forces) is zero. In agreement with Newton's first law, if the book is at rest on the tabletop, it remains at rest. The same principle applies to a hockey puck sliding on a horizontal, frictionless surface: The vector sum of the upward push of the surface and the downward pull of gravity is zero. Once the puck is in motion, it continues to move with constant velocity because the *net* force acting on it is zero.

Here's another example. Suppose a hockey puck rests on a horizontal surface with negligible friction, such as an air-hockey table or a slab of wet ice. If the puck is initially at rest and a single horizontal force \vec{F}_1 acts on it (Fig. 4.10a), the puck starts to move. If the puck is in motion to begin with, the force changes its speed, its direction, or both, depending on the direction of the force. In this case the net force is equal to \vec{F}_1 , which is *not* zero. (There are also two vertical forces: the earth's gravitational attraction and the upward normal force exerted by the surface. But as we mentioned earlier, these two forces cancel.)

Now suppose we apply a second force \vec{F}_2 (Fig. 4.10b), equal in magnitude to \vec{F}_1 but opposite in direction. The two forces are negatives of each other, $\vec{F}_2 = -\vec{F}_1$, and their vector sum is zero:

$$\sum \vec{F} = \vec{F}_1 + \vec{F}_2 = \vec{F}_1 + (-\vec{F}_1) = \mathbf{0}$$

Again, we find that if the body is at rest at the start, it remains at rest; if it is initially moving, it continues to move in the same direction with constant speed. These results show that in Newton's first law, *zero net force is equivalent to no force at all*. This is just the principle of superposition of forces that we saw in Section 4.1.

When a body is either at rest or moving with constant velocity (in a straight line with constant speed), we say that the body is in **equilibrium**. For a body to be in equilibrium, it must be acted on by no forces, or by several forces such that their vector sum—that is, the net force—is zero:

$$\sum \vec{F} = \mathbf{0} \quad (\text{body in equilibrium}) \quad (4.3)$$

For this to be true, each component of the net force must be zero, so

$$\sum F_x = 0 \quad \sum F_y = 0 \quad (\text{body in equilibrium}) \quad (4.4)$$

We are assuming that the body can be represented adequately as a point particle. When the body has finite size, we also have to consider *where* on the body the forces are applied. We will return to this point in Chapter 11.

Conceptual Example 4.2 Zero net force means constant velocity

In the classic 1950 science fiction film *Rocketship X-M*, a spaceship is moving in the vacuum of outer space, far from any planet, when its engine dies. As a result, the spaceship slows down and stops. What does Newton's first law say about this event?

SOLUTION

In this situation there are no forces acting on the spaceship, so according to Newton's first law, it will *not* stop. It continues to move in a straight line with constant speed. Some science fiction movies have made use of very accurate science; this was not one of them.

Conceptual Example 4.3 Constant velocity means zero net force

You are driving a Porsche Carrera GT on a straight testing track at a constant speed of 150 km/h. You pass a 1971 Volkswagen Beetle doing a constant 75 km/h. For which car is the net force greater?

SOLUTION

The key word in this question is “net.” Both cars are in equilibrium because their velocities are both constant; therefore the *net* force on each car is *zero*.

This conclusion seems to contradict the “common sense” idea that the faster car must have a greater force pushing it. It's true that

the forward force on your Porsche is much greater than that on the Volkswagen (thanks to your Porsche's high-power engine). But there is also a *backward* force acting on each car due to road friction and air resistance. The only reason these cars need engines is to counteract this backward force so that the vector sum of the forward and backward forces will be zero and the car will travel with constant velocity. The backward force on your Porsche is greater because of its greater speed, so its engine has to be more powerful than the Volkswagen's.

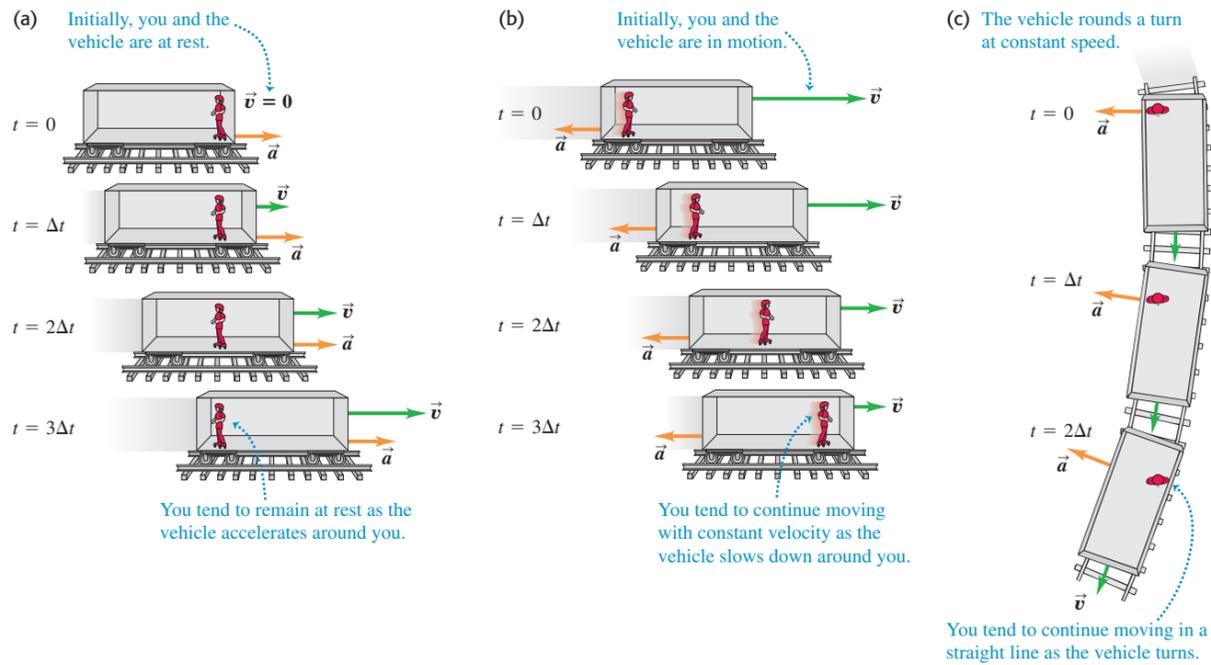
Inertial Frames of Reference

In discussing relative velocity in Section 3.5, we introduced the concept of *frame of reference*. This concept is central to Newton's laws of motion. Suppose you are in a bus that is traveling on a straight road and speeding up. If you could stand in the aisle on roller skates, you would start moving *backward* relative to the bus as the bus gains speed. If instead the bus was slowing to a stop, you would start moving forward down the aisle. In either case, it looks as though Newton's first law is not obeyed; there is no net force acting on you, yet your velocity changes. What's wrong?

The point is that the bus is accelerating with respect to the earth and is *not* a suitable frame of reference for Newton's first law. This law is valid in some frames of reference and not valid in others. A frame of reference in which Newton's first law *is* valid is called an **inertial frame of reference**. The earth is at least approximately an inertial frame of reference, but the bus is not. (The earth is not a completely inertial frame, owing to the acceleration associated with its rotation and its motion around the sun. These effects are quite small, however; see Exercises 3.29 and 3.32.) Because Newton's first law is used to define what we mean by an inertial frame of reference, it is sometimes called the *law of inertia*.

Figure 4.11 helps us understand what you experience when riding in a vehicle that's accelerating. In Fig. 4.11a, a vehicle is initially at rest and then begins to accelerate to the right. A passenger on roller skates (which nearly eliminate the effects of friction) has virtually no net force acting on her, so she tends to remain at rest relative to the inertial frame of the earth. As the vehicle accelerates around her, she moves backward relative to the vehicle. In the same way, a passenger in a vehicle that is slowing down tends to continue moving with constant velocity relative to the earth, and so moves forward relative to the vehicle (Fig. 4.11b). A vehicle is also accelerating if it moves at a constant speed but is turning (Fig. 4.11c). In this case a passenger tends to continue moving relative to the earth at constant speed in a straight line; relative to the vehicle, the passenger moves to the side of the vehicle on the outside of the turn.

4.11 Riding in an accelerating vehicle.



In each case shown in Fig. 4.11, an observer in the vehicle's frame of reference might be tempted to conclude that there is a net force acting on the passenger, since the passenger's velocity relative to the vehicle changes in each case. This conclusion is simply wrong; the net force on the passenger is indeed zero. The vehicle observer's mistake is in trying to apply Newton's first law in the vehicle's frame of reference, which is *not* an inertial frame and in which Newton's first law isn't valid (Fig. 4.12). In this book we will use *only* inertial frames of reference.

We've mentioned only one (approximately) inertial frame of reference: the earth's surface. But there are many inertial frames. If we have an inertial frame of reference *A*, in which Newton's first law is obeyed, then *any* second frame of reference *B* will also be inertial if it moves relative to *A* with constant velocity $\vec{v}_{B/A}$. We can prove this using the relative velocity relation Eq. (3.36) from Section 3.5:

$$\vec{v}_{P/A} = \vec{v}_{P/B} + \vec{v}_{B/A}$$

Suppose that *P* is a body that moves with constant velocity $\vec{v}_{P/A}$ with respect to an inertial frame *A*. By Newton's first law the net force on this body is zero. The velocity of *P* relative to another frame *B* has a different value, $\vec{v}_{P/B} = \vec{v}_{P/A} - \vec{v}_{B/A}$. But if the relative velocity $\vec{v}_{B/A}$ of the two frames is constant, then $\vec{v}_{P/B}$ is constant as well. Thus *B* is also an inertial frame; the velocity of *P* in this frame is constant, and the net force on *P* is zero, so Newton's first law is obeyed in *B*. Observers in frames *A* and *B* will disagree about the velocity of *P*, but they will agree that *P* has a constant velocity (zero acceleration) and has zero net force acting on it.

There is no single inertial frame of reference that is preferred over all others for formulating Newton's laws. If one frame is inertial, then every other frame moving relative to it with constant velocity is also inertial. Viewed in this light, the state of rest and the state of motion with constant velocity are not very different; both occur when the vector sum of forces acting on the body is zero.

4.12 From the frame of reference of the car, it seems as though a force is pushing the crash test dummies forward as the car comes to a sudden stop. But there is really no such force: As the car stops, the dummies keep moving forward as a consequence of Newton's first law.



Test Your Understanding of Section 4.2 In which of the following situations is there zero net force on the body? (i) an airplane flying due north at a steady 120 m/s and at a constant altitude; (ii) a car driving straight up a hill with a 3° slope at a constant 90 km/h; (iii) a hawk circling at a constant 20 km/h at a constant height of 15 m above an open field; (iv) a box with slick, frictionless surfaces in the back of a truck as the truck accelerates forward on a level road at 5 m/s².

4.3 Newton's Second Law

Newton's first law tells us that when a body is acted on by zero net force, it moves with constant velocity and zero acceleration. In Fig. 4.13a, a hockey puck is sliding to the right on wet ice. There is negligible friction, so there are no horizontal forces acting on the puck; the downward force of gravity and the upward normal force exerted by the ice surface sum to zero. So the net force $\Sigma \vec{F}$ acting on the puck is zero, the puck has zero acceleration, and its velocity is constant.

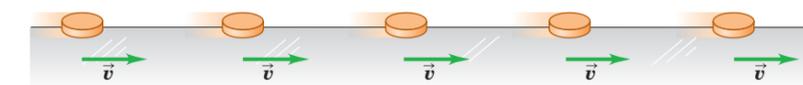
But what happens when the net force is *not* zero? In Fig. 4.13b we apply a constant horizontal force to a sliding puck in the same direction that the puck is moving. Then $\Sigma \vec{F}$ is constant and in the same horizontal direction as \vec{v} . We find that during the time the force is acting, the velocity of the puck changes at a constant rate; that is, the puck moves with constant acceleration. The speed of the puck increases, so the acceleration \vec{a} is in the same direction as \vec{v} and $\Sigma \vec{F}$.

In Fig. 4.13c we reverse the direction of the force on the puck so that $\Sigma \vec{F}$ acts opposite to \vec{v} . In this case as well, the puck has an acceleration; the puck moves more and more slowly to the right. The acceleration \vec{a} in this case is to the left, in the same direction as $\Sigma \vec{F}$. As in the previous case, experiment shows that the acceleration is constant if $\Sigma \vec{F}$ is constant.

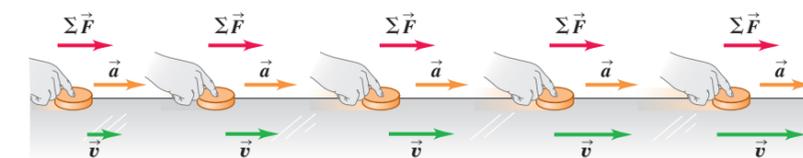
We conclude that *a net force acting on a body causes the body to accelerate in the same direction as the net force*. If the magnitude of the net force is constant, as in Figs. 4.13b and 4.13c, then so is the magnitude of the acceleration.

4.13 Exploring the relationship between the acceleration of a body and the net force acting on the body (in this case, a hockey puck on a frictionless surface).

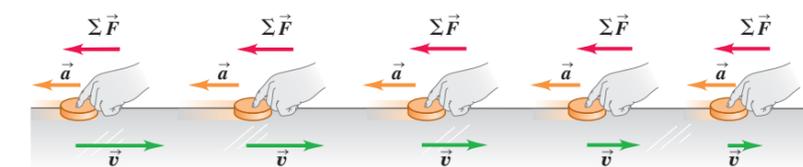
(a) A puck moving with constant velocity (in equilibrium): $\Sigma \vec{F} = 0$, $\vec{a} = 0$



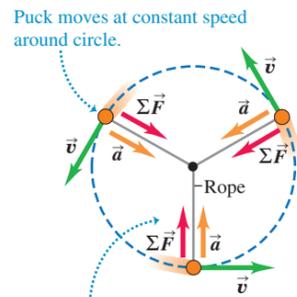
(b) A constant net force in the direction of motion causes a constant acceleration in the same direction as the net force.



(c) A constant net force opposite the direction of motion causes a constant acceleration in the same direction as the net force.

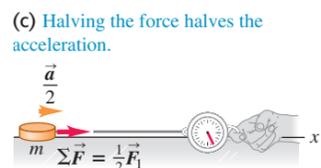
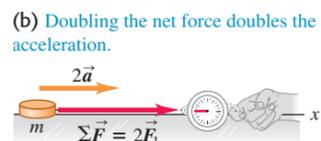
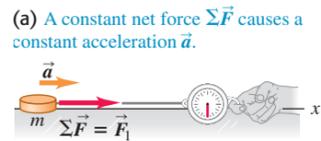


4.14 A top view of a hockey puck in uniform circular motion on a frictionless horizontal surface.



Puck moves at constant speed around circle.
At all points, the acceleration \vec{a} and the net force $\Sigma\vec{F}$ point in the same direction—always toward the center of the circle.

4.15 For a body of a given mass m , the magnitude of the body's acceleration is directly proportional to the magnitude of the net force acting on the body.



These conclusions about net force and acceleration also apply to a body moving along a curved path. For example, Fig. 4.14 shows a hockey puck moving in a horizontal circle on an ice surface of negligible friction. A rope attaching the puck to the ice exerts a tension force of constant magnitude toward the center of the circle. The result is a net force and an acceleration that are constant in magnitude and directed toward the center of the circle. The speed of the puck is constant, so this is uniform circular motion, as discussed in Section 3.4.

Figure 4.15a shows another experiment to explore the relationship between acceleration and net force. We apply a constant horizontal force to a puck on a frictionless horizontal surface, using the spring balance described in Section 4.1 with the spring stretched a constant amount. As in Figs. 4.13b and 4.13c, this horizontal force equals the net force on the puck. If we change the magnitude of the net force, the acceleration changes in the same proportion. Doubling the net force doubles the acceleration (Fig. 4.15b), halving the net force halves the acceleration (Fig. 4.15c), and so on. Many such experiments show that for any given body, the magnitude of the acceleration is directly proportional to the magnitude of the net force acting on the body.

Mass and Force

Our results mean that for a given body, the ratio of the magnitude $|\Sigma\vec{F}|$ of the net force to the magnitude $a = |\vec{a}|$ of the acceleration is constant, regardless of the magnitude of the net force. We call this ratio the *inertial mass*, or simply the **mass**, of the body and denote it by m . That is,

$$m = \frac{|\Sigma\vec{F}|}{a} \quad \text{or} \quad |\Sigma\vec{F}| = ma \quad \text{or} \quad a = \frac{|\Sigma\vec{F}|}{m} \quad (4.5)$$

Mass is a quantitative measure of inertia, which we discussed in Section 4.2. The last of the equations in Eq. (4.5) says that the greater its mass, the more a body “resists” being accelerated. When you hold a piece of fruit in your hand at the supermarket and move it slightly up and down to estimate its heft, you’re applying a force and seeing how much the fruit accelerates up and down in response. If a force causes a large acceleration, the fruit has a small mass; if the same force causes only a small acceleration, the fruit has a large mass. In the same way, if you hit a table-tennis ball and then a basketball with the same force, the basketball has much smaller acceleration because it has much greater mass.

The SI unit of mass is the **kilogram**. We mentioned in Section 1.3 that the kilogram is officially defined to be the mass of a cylinder of platinum–iridium alloy kept in a vault near Paris. We can use this standard kilogram, along with Eq. (4.5), to define the **newton**:

One newton is the amount of net force that gives an acceleration of 1 meter per second squared to a body with a mass of 1 kilogram.

This definition allows us to calibrate the spring balances and other instruments used to measure forces. Because of the way we have defined the newton, it is related to the units of mass, length, and time. For Eq. (4.5) to be dimensionally consistent, it must be true that

$$1 \text{ newton} = (1 \text{ kilogram})(1 \text{ meter per second squared})$$

or

$$1 \text{ N} = 1 \text{ kg} \cdot \text{m/s}^2$$

We will use this relationship many times in the next few chapters, so keep it in mind.

We can also use Eq. (4.5) to compare a mass with the standard mass and thus to *measure* masses. Suppose we apply a constant net force $\Sigma\vec{F}$ to a body having

a known mass m_1 and we find an acceleration of magnitude a_1 (Fig. 4.16a). We then apply the same force to another body having an unknown mass m_2 , and we find an acceleration of magnitude a_2 (Fig. 4.16b). Then, according to Eq. (4.5),

$$m_1 a_1 = m_2 a_2$$

$$\frac{m_2}{m_1} = \frac{a_1}{a_2} \quad (\text{same net force}) \quad (4.6)$$

For the same net force, the ratio of the masses of two bodies is the inverse of the ratio of their accelerations. In principle we could use Eq. (4.6) to measure an unknown mass m_2 , but it is usually easier to determine mass indirectly by measuring the body’s *weight*. We’ll return to this point in Section 4.4.

When two bodies with masses m_1 and m_2 are fastened together, we find that the mass of the composite body is always $m_1 + m_2$ (Fig. 4.16c). This additive property of mass may seem obvious, but it has to be verified experimentally. Ultimately, the mass of a body is related to the number of protons, electrons, and neutrons it contains. This wouldn’t be a good way to *define* mass because there is no practical way to count these particles. But the concept of mass is the most fundamental way to characterize the quantity of matter in a body.

Stating Newton’s Second Law

We’ve been careful to state that the *net* force on a body is what causes that body to accelerate. Experiment shows that if a combination of forces $\vec{F}_1, \vec{F}_2, \vec{F}_3$, and so on is applied to a body, the body will have the same acceleration (magnitude and direction) as when only a single force is applied, if that single force is equal to the vector sum $\vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \dots$. In other words, the principle of superposition of forces (see Fig. 4.4) also holds true when the net force is not zero and the body is accelerating.

Equation (4.5) relates the magnitude of the net force on a body to the magnitude of the acceleration that it produces. We have also seen that the direction of the net force is the same as the direction of the acceleration, whether the body’s path is straight or curved. Newton wrapped up all these relationships and experimental results in a single concise statement that we now call *Newton’s second law of motion*:

Newton’s second law of motion: If a net external force acts on a body, the body accelerates. The direction of acceleration is the same as the direction of the net force. The mass of the body times the acceleration of the body equals the net force vector.

In symbols,

$$\Sigma\vec{F} = m\vec{a} \quad (\text{Newton’s second law of motion}) \quad (4.7)$$

An alternative statement is that the acceleration of a body is in the same direction as the net force acting on the body, and is equal to the net force divided by the body’s mass:

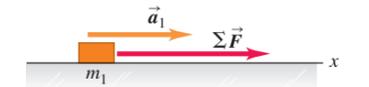
$$\vec{a} = \frac{\Sigma\vec{F}}{m}$$

Newton’s second law is a fundamental law of nature, the basic relationship between force and motion. Most of the remainder of this chapter and all of the next are devoted to learning how to apply this principle in various situations.

Equation (4.7) has many practical applications (Fig. 4.17). You’ve actually been using it all your life to measure your body’s acceleration. In your inner ear, microscopic hair cells sense the magnitude and direction of the force that they must exert to cause small membranes to accelerate along with the rest of your body. By Newton’s second law, the acceleration of the membranes—and hence

4.16 For a given net force $\Sigma\vec{F}$ acting on a body, the acceleration is inversely proportional to the mass of the body. Masses add like ordinary scalars.

(a) A known force $\Sigma\vec{F}$ causes an object with mass m_1 to have an acceleration \vec{a}_1 .



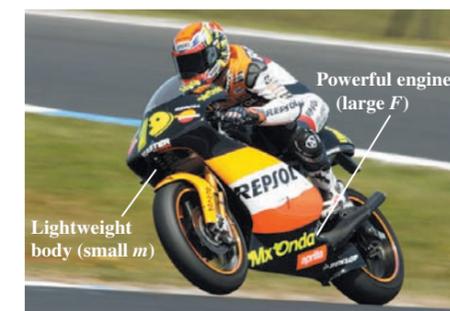
(b) Applying the same force $\Sigma\vec{F}$ to a second object and noting the acceleration allow us to measure the mass.



(c) When the two objects are fastened together, the same method shows that their composite mass is the sum of their individual masses.



4.17 The design of high-performance motorcycles depends fundamentally on Newton’s second law. To maximize the forward acceleration, the designer makes the motorcycle as light as possible (that is, minimizes the mass) and uses the most powerful engine possible (thus maximizing the forward force).



that of your body as a whole—is proportional to this force and has the same direction. In this way, you can sense the magnitude and direction of your acceleration even with your eyes closed!

Using Newton's Second Law

There are at least four aspects of Newton's second law that deserve special attention. First, Eq. (4.7) is a *vector* equation. Usually we will use it in component form, with a separate equation for each component of force and the corresponding acceleration:

$$\sum F_x = ma_x \quad \sum F_y = ma_y \quad \sum F_z = ma_z \quad \text{(Newton's second law of motion)} \quad (4.8)$$

This set of component equations is equivalent to the single vector equation (4.7). Each component of the net force equals the mass times the corresponding component of acceleration.

Second, the statement of Newton's second law refers to *external* forces. By this we mean forces exerted on the body by other bodies in its environment. It's impossible for a body to affect its own motion by exerting a force on itself; if it were possible, you could lift yourself to the ceiling by pulling up on your belt! That's why only external forces are included in the sum $\sum \vec{F}$ in Eqs. (4.7) and (4.8).

Third, Eqs. (4.7) and (4.8) are valid only when the mass m is *constant*. It's easy to think of systems whose masses change, such as a leaking tank truck, a rocket ship, or a moving railroad car being loaded with coal. But such systems are better handled by using the concept of momentum; we'll get to that in Chapter 8.

Finally, Newton's second law is valid only in inertial frames of reference, just like the first law. Thus it is not valid in the reference frame of any of the accelerating vehicles in Fig. 4.11; relative to any of these frames, the passenger accelerates even though the net force on the passenger is zero. We will usually assume that the earth is an adequate approximation to an inertial frame, although because of its rotation and orbital motion it is not precisely inertial.

CAUTION $m\vec{a}$ is not a force You must keep in mind that even though the vector $m\vec{a}$ is equal to the vector sum $\sum \vec{F}$ of all the forces acting on the body, the vector $m\vec{a}$ is not a force. Acceleration is a *result* of a nonzero net force; it is not a force itself. It's "common sense" to think that there is a "force of acceleration" that pushes you back into your seat when your car accelerates forward from rest. But *there is no such force*; instead, your inertia causes you to tend to stay at rest relative to the earth, and the car accelerates around you (see Fig. 4.11a). The "common sense" confusion arises from trying to apply Newton's second law where it isn't valid, in the noninertial reference frame of an accelerating car. We will always examine motion relative to *inertial* frames of reference only. ■

In learning how to use Newton's second law, we will begin in this chapter with examples of straight-line motion. Then in Chapter 5 we will consider more general cases and develop more detailed problem-solving strategies.

Example 4.4 Determining acceleration from force

A worker applies a constant horizontal force with magnitude 20 N to a box with mass 40 kg resting on a level floor with negligible friction. What is the acceleration of the box?

SOLUTION

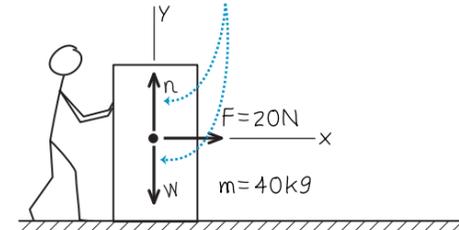
IDENTIFY: This problem involves force and acceleration. Whenever you encounter a problem of this kind, you should approach it using Newton's second law.

SET UP: In *any* problem involving forces, the first steps are to choose a coordinate system and then identify all of the forces acting on the body in question.

It's usually convenient to take one axis either along or opposite the direction of the body's acceleration, which in this case is horizontal. Hence we take the $+x$ -axis to be in the direction of the applied horizontal force (that is, the direction in which the box accelerates) and the $+y$ -axis to be upward (Fig. 4.18). In most

4.18 Our sketch for this problem. The tiles under the box are freshly waxed, so we assume that friction is negligible.

The box has no vertical acceleration, so the vertical components of the net force sum to zero. Nevertheless, for completeness, we show the vertical forces acting on the box.



force problems that you'll encounter (including this one), the force vectors all lie in a plane, so the z -axis isn't used.

The forces acting on the box are (i) the horizontal force \vec{F} exerted by the worker, of magnitude 20 N; (ii) the weight \vec{w} of the box—that is, the downward gravitational force exerted by the earth; and (iii) the upward supporting force \vec{n} exerted by the floor. As in Section 4.2, we call \vec{n} a *normal* force because it is normal (perpendicular) to the surface of contact. (We use an italic letter n to avoid confusion with the abbreviation N for newton.) We are told that friction is negligible, so no friction force is present.

Example 4.5 Determining force from acceleration

A waitress shoves a ketchup bottle with mass 0.45 kg to the right along a smooth, level lunch counter. The bottle leaves her hand moving at 2.8 m/s, then slows down as it slides because of the constant horizontal friction force exerted on it by the counter top. It slides a distance of 1.0 m before coming to rest. What are the magnitude and direction of the friction force acting on the bottle?

SOLUTION

IDENTIFY: Like Example 4.4, this problem involves forces and acceleration (the slowing of the ketchup bottle), so we'll use Newton's second law to solve it.

SET UP: As in Example 4.4, we first choose a coordinate system and then identify the forces acting on the body (in this case, the ketchup bottle). As Fig. 4.19 shows, we choose the $+x$ -axis to be in the direction that the bottle slides, and we take the origin to be where the bottle leaves the waitress's hand moving at 2.8 m/s. Figure 4.19 also shows the forces acting on the bottle. The friction force \vec{f} acts to slow the bottle down, so its direction must be opposite the direction of velocity (see Fig. 4.13c).

Our target variable is the magnitude f of the friction force. We'll find it using the x -component of Newton's second law from Eq. (4.8). To do so, we'll first need to know the x -component of the bottle's acceleration, a_x . We aren't told the value of a_x in the problem, but we are told that the friction force is constant. Hence the acceleration is constant as well, and we can calculate a_x by using one of the constant-acceleration formulas from Section 2.4. Since we know the bottle's initial x -coordinate and x -velocity ($x_0 = 0$,

Since the box doesn't move vertically at all, the y -acceleration is zero: $a_y = 0$. Our target variable is the x -component of acceleration, a_x . We'll find it using Newton's second law in component form as given by Eq. (4.8).

EXECUTE: From Fig. 4.18, only the 20-N force has a nonzero x -component. Hence the first relation in Eqs. (4.8) tells us that

$$\sum F_x = F = 20 \text{ N} = ma_x$$

Hence the x -component of acceleration is

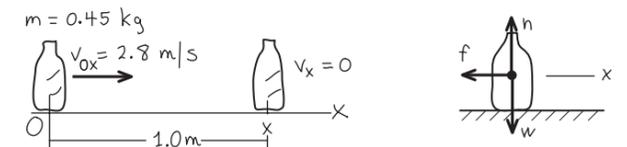
$$a_x = \frac{\sum F_x}{m} = \frac{20 \text{ N}}{40 \text{ kg}} = \frac{20 \text{ kg} \cdot \text{m/s}^2}{40 \text{ kg}} = 0.50 \text{ m/s}^2$$

EVALUATE: The acceleration is in the $+x$ -direction, the same direction as the net force. The net force is constant, so the acceleration is also constant. If we are given the initial position and velocity of the box, we can find the position and velocity at any later time from the equations of motion with constant acceleration we derived in Chapter 2.

Notice that to determine a_x , we didn't have to use the y -component of Newton's second law from Eq. (4.8), $\sum F_y = ma_y$. By using this equation, can you show that the magnitude n of the normal force in this situation is equal to the weight of the box?

4.19 Our sketch for this problem.

We draw one diagram for the bottle's motion and one showing the forces on the bottle.



$v_{0x} = 2.8 \text{ m/s}$) as well as its final x -coordinate and x -velocity ($x = 1.0 \text{ m}$, $v_x = 0$), the easiest equation to use to determine a_x is Eq. (2.13), $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$.

EXECUTE: From Eq. (2.13),

$$v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$$

$$a_x = \frac{v_x^2 - v_{0x}^2}{2(x - x_0)} = \frac{(0 \text{ m/s})^2 - (2.8 \text{ m/s})^2}{2(1.0 \text{ m} - 0 \text{ m})} = -3.9 \text{ m/s}^2$$

The negative sign means that the acceleration is toward the *left*; the velocity is in the opposite direction to acceleration, as it must be, since the bottle is slowing down. The net force in the x -direction is the x -component $-f$ of the friction force, so

$$\sum F_x = -f = ma_x = (0.45 \text{ kg})(-3.9 \text{ m/s}^2)$$

$$= -1.8 \text{ kg} \cdot \text{m/s}^2 = -1.8 \text{ N}$$

Continued

Again the negative sign shows that the force on the bottle is directed toward the left. The magnitude of the friction force is $f = 1.8$ N. Remember that magnitudes are *always* positive!

EVALUATE: We chose the $+x$ -axis to be in the direction of the bottle's motion, so that a_x was negative. As a check on the result, try

repeating the calculation with the $+x$ -axis directed *opposite* to the motion (to the left in Fig. 4.19) so that a_x is positive. In this case you should find that $\sum F_x$ is equal to $+f$ (because the friction force is now in the $+x$ -direction), which in turn is equal to $+1.8$ N. Your answers for the *magnitudes* of forces (which are always positive numbers) should never depend on your choice of coordinate axes!

4.20 Despite its name, the English unit of mass has nothing to do with the type of slug shown here. A common garden slug has a mass of about 15 grams, or about 10^{-3} slug.



Some Notes on Units

A few words about units are in order. In the cgs metric system (not used in this book), the unit of mass is the gram, equal to 10^{-3} kg, and the unit of distance is the centimeter, equal to 10^{-2} m. The cgs unit of force is called the *dyne*:

$$1 \text{ dyne} = 1 \text{ g} \cdot \text{cm/s}^2 = 10^{-5} \text{ N}$$

In the British system, the unit of force is the *pound* (or pound-force) and the unit of mass is the *slug* (Fig. 4.20). The unit of acceleration is 1 foot per second squared, so

$$1 \text{ pound} = 1 \text{ slug} \cdot \text{ft/s}^2$$

The official definition of the pound is

$$1 \text{ pound} = 4.448221615260 \text{ newtons}$$

It is handy to remember that a pound is about 4.4 N and a newton is about 0.22 pound. Next time you want to order a “quarter-pounder,” try asking for a “one-newtoner” and see what happens. Another useful fact: A body with a mass of 1 kg has a weight of about 2.2 lb at the earth's surface.

Table 4.2 summarizes the units of force, mass, and acceleration in the three systems.

Table 4.2 Units of Force, Mass, and Acceleration

System of Units	Force	Mass	Acceleration
SI	newton (N)	kilogram (kg)	m/s^2
cgs	dyne (dyn)	gram (g)	cm/s^2
British	pound (lb)	slug	ft/s^2

Test Your Understanding of Section 4.3 Rank the following situations in order of the magnitude of the object's acceleration, from lowest to highest. Are there any cases that have the same magnitude of acceleration? (i) a 2.0-kg object acted on by a 2.0-N net force; (ii) a 2.0-kg object acted on by an 8.0-N net force; (iii) an 8.0-kg object acted on by a 2.0-N net force; (iv) an 8.0-kg object acted on by a 8.0-N net force.



4.4 Mass and Weight

One of the most familiar forces is the *weight* of a body, which is the gravitational force that the earth exerts on the body. (If you are on another planet, your weight is the gravitational force that planet exerts on you.) Unfortunately, the terms *mass* and *weight* are often misused and interchanged in everyday conversation. It is absolutely essential for you to understand clearly the distinctions between these two physical quantities.

Mass characterizes the *inertial* properties of a body. Mass is what keeps the china on the table when you yank the tablecloth out from under it. The greater the mass, the greater the force needed to cause a given acceleration; this is reflected in Newton's second law, $\sum \vec{F} = m\vec{a}$.

Weight, on the other hand, is a *force* exerted on a body by the pull of the earth. Mass and weight are related: Bodies having large mass also have large weight. A large stone is hard to throw because of its large *mass*, and hard to lift off the ground because of its large *weight*.

To understand the relationship between mass and weight, note that a freely falling body has an acceleration of magnitude g . Newton's second law tells us that a force must act to produce this acceleration. If a 1-kg body falls with an acceleration of 9.8 m/s^2 , the required force has magnitude

$$F = ma = (1 \text{ kg})(9.8 \text{ m/s}^2) = 9.8 \text{ kg} \cdot \text{m/s}^2 = 9.8 \text{ N}$$

The force that makes the body accelerate downward is its weight. Any body near the surface of the earth that has a mass of 1 kg *must* have a weight of 9.8 N to give it the acceleration we observe when it is in free fall. More generally, a body with mass m must have weight with magnitude w given by

$$w = mg \quad (\text{magnitude of the weight of a body of mass } m) \quad (4.9)$$

Hence the magnitude w of a body's weight is directly proportional to its mass m . The weight of a body is a force, a vector quantity, and we can write Eq. (4.9) as a vector equation (Fig. 4.21):

$$\vec{w} = m\vec{g} \quad (4.10)$$

Remember that g is the *magnitude* of \vec{g} , the acceleration due to gravity, so g is always a positive number, by definition. Thus w , given by Eq. (4.9), is the *magnitude* of the weight and is also always positive.

CAUTION A body's weight acts at all times It is important to understand that the weight of a body acts on the body *all the time*, whether it is in free fall or not. If we suspend an object from a chain, it is in equilibrium, and its acceleration is zero. But its weight, given by Eq. (4.10), is still pulling down on it (Fig. 4.21). In this case the chain pulls up on the object, applying an upward force. The *vector sum* of the forces is zero, but the weight still acts.

Conceptual Example 4.6 Net force and acceleration in free fall

In Example 2.6 (Section 2.5) a one-euro coin was dropped from rest from the Leaning Tower of Pisa. If the coin falls freely, so that the effects of the air are negligible, how does the net force on the coin vary as it falls?

SOLUTION

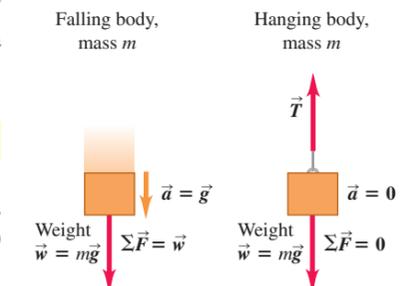
In free fall, the acceleration \vec{a} of the coin is constant and equal to \vec{g} . Hence by Newton's second law the net force $\sum \vec{F} = m\vec{a}$ is also constant and equal to $m\vec{g}$, which is the coin's weight \vec{w} (Fig. 4.22). The coin's velocity changes as it falls, but the net force acting on it remains constant. If this surprises you, perhaps you still believe in the erroneous “common sense” idea that greater speed implies greater force. If so, you should reread Conceptual Example 4.3.

The net force on a freely falling coin is constant even if you initially toss it upward. The force that your hand exerts on the coin to toss it is a contact force, and it disappears the instant that the coin

loses contact with your hand. From then on, the only force acting on the coin is its weight \vec{w} .

4.22 The acceleration of a freely falling object is constant, and so is the net force acting on the object.

4.21 The relationship of mass and weight.

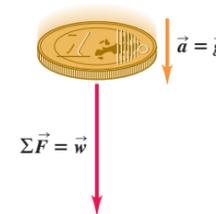


- The relationship of mass to weight: $\vec{w} = m\vec{g}$.
- This relationship is the same whether a body is falling or stationary.

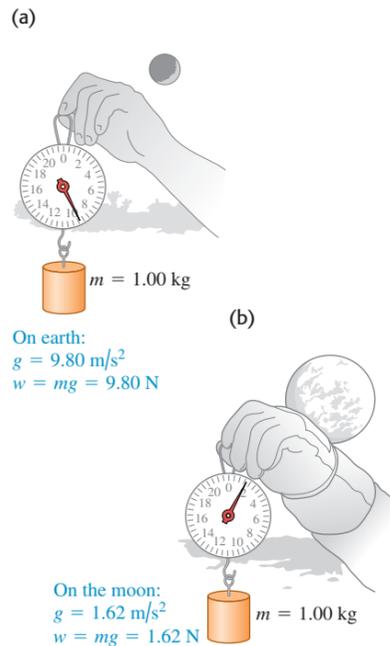
Variation of g with Location

We will use $g = 9.80 \text{ m/s}^2$ for problems on the earth (or, if the other data in the problem are given to only two significant figures, $g = 9.8 \text{ m/s}^2$). In fact, the value of g varies somewhat from point to point on the earth's surface, from about 9.78 to 9.82 m/s^2 , because the earth is not perfectly spherical and because of effects due to its rotation and orbital motion. At a point where $g = 9.80 \text{ m/s}^2$, the weight of a standard kilogram is $w = 9.80 \text{ N}$. At a different point, where $g = 9.78 \text{ m/s}^2$, the weight is $w = 9.78 \text{ N}$ but the mass is still 1 kg. The weight of a body varies from one location to another; the mass does not.

If we take a standard kilogram to the surface of the moon, where the acceleration of free fall (equal to the value of g at the moon's surface) is 1.62 m/s^2 , its



4.23 The weight of a 1-kilogram mass (a) on earth and (b) on the moon.



weight is 1.62 N, but its mass is still 1 kg (Fig. 4.23). An 80.0-kg astronaut has a weight on earth of $(80.0 \text{ kg})(9.80 \text{ m/s}^2) = 784 \text{ N}$, but on the moon the astronaut's weight would be only $(80.0 \text{ kg})(1.62 \text{ m/s}^2) = 130 \text{ N}$. In Chapter 12 we'll see how to calculate the value of g at the surface of the moon or on other worlds.

Measuring Mass and Weight

In Section 4.3 we described a way to compare masses by comparing their accelerations when subjected to the same net force. Usually, however, the easiest way to measure the mass of a body is to measure its weight, often by comparing with a standard. Equation (4.9) says that two bodies that have the same weight at a particular location also have the same mass. We can compare weights very precisely; the familiar equal-arm balance (Fig. 4.24) can determine with great precision (up to 1 part in 10^6) when the weights of two bodies are equal and hence when their masses are equal. (This method doesn't work in the apparent "zero-gravity" environment of outer space. Instead, we apply a known force to the body, measure its acceleration, and compute the mass as the ratio of force to acceleration. This method, or a variation of it, is used to measure the masses of astronauts in orbiting space stations as well as the masses of atomic and subatomic particles.)

The concept of mass plays two rather different roles in mechanics. The weight of a body (the gravitational force acting on it) is proportional to its mass; we call the property related to gravitational interactions *gravitational mass*. On the other hand, we call the inertial property that appears in Newton's second law the *inertial mass*. If these two quantities were different, the acceleration due to gravity might well be different for different bodies. However, extraordinarily precise experiments have established that in fact the two *are* the same to a precision of better than one part in 10^{12} .

CAUTION Don't confuse mass and weight The SI units for mass and weight are often misused in everyday life. Incorrect expressions such as "This box weighs 6 kg" are nearly universal. What is meant is that the *mass* of the box, probably determined indirectly by *weighing*, is 6 kg. Be careful to avoid this sloppy usage in your own work! In SI units, weight (a force) is measured in newtons, while mass is measured in kilograms. ■

Example 4.7 Mass and weight

A $2.49 \times 10^4 \text{ N}$ Rolls-Royce Phantom traveling in the $+x$ -direction makes a fast stop; the x -component of the net force acting on it is $-1.83 \times 10^4 \text{ N}$. What is its acceleration?

SOLUTION

IDENTIFY: Again we will use Newton's second law to relate force and acceleration. To use this relationship, we need to know the car's mass. However, because the newton is a unit for force, we know that $2.49 \times 10^4 \text{ N}$ is the car's weight, not its mass. So we'll also have to use the relationship between a body's mass and its weight.

SET UP: Our target variable is the x -component of acceleration of the car, a_x . (The motion is purely in the x -direction.) We use Eq. (4.9) to determine the car's mass from its weight and then use the x -component of Newton's second law from Eq. (4.8) to determine a_x .

EXECUTE: The mass m of the car is

$$m = \frac{w}{g} = \frac{2.49 \times 10^4 \text{ N}}{9.80 \text{ m/s}^2} = \frac{2.49 \times 10^4 \text{ kg} \cdot \text{m/s}^2}{9.80 \text{ m/s}^2} = 2540 \text{ kg}$$

Then $\sum F_x = ma_x$ gives

$$a_x = \frac{\sum F_x}{m} = \frac{-1.83 \times 10^4 \text{ N}}{2540 \text{ kg}} = \frac{-1.83 \times 10^4 \text{ kg} \cdot \text{m/s}^2}{2540 \text{ kg}} = -7.20 \text{ m/s}^2$$

EVALUATE: The negative sign means that the acceleration vector points in the negative x -direction. This makes sense: The car is moving in the positive x -direction and is slowing down.

Note that the acceleration can alternatively be written as $-0.735g$. It's of interest that -0.735 is also the ratio of $-1.83 \times 10^4 \text{ N}$ (the x -component of the net force) to $2.49 \times 10^4 \text{ N}$ (the weight). Indeed, the acceleration of a body expressed as a multiple of g is always equal to the ratio of the net force on the body to its weight. Can you see why?

Test Your Understanding of Section 4.4 Suppose an astronaut landed on a planet where $g = 19.6 \text{ m/s}^2$. Compared to earth, would it be easier, harder, or just as easy for her to walk around? Would it be easier, harder, or just as easy for her to catch a ball that is moving horizontally at 12 m/s ? (Assume that the astronaut's spacesuit is a light-weight model that doesn't impede her movements in any way.)

4.5 Newton's Third Law

A force acting on a body is always the result of its interaction with another body, so forces always come in pairs. You can't pull on a doorknob without the doorknob pulling back on you. When you kick a football, the forward force that your foot exerts on the ball launches it into its trajectory, but you also feel the force the ball exerts back on your foot. If you kick a boulder, the pain you feel is due to the force that the boulder exerts on your foot.

In each of these cases, the force that you exert on the other body is in the opposite direction to the force that body exerts on you. Experiments show that whenever two bodies interact, the two forces that they exert on each other are always *equal in magnitude* and *opposite in direction*. This fact is called *Newton's third law of motion*:

Newton's third law of motion: If body A exerts a force on body B (an "action"), then body B exerts a force on body A (a "reaction"). These two forces have the same magnitude but are opposite in direction. These two forces act on different bodies.

For example, in Fig. 4.25 $\vec{F}_{A \text{ on } B}$ is the force applied by body A (first subscript) on body B (second subscript), and $\vec{F}_{B \text{ on } A}$ is the force applied by body B (first subscript) on body A (second subscript). The mathematical statement of Newton's third law is

$$\vec{F}_{A \text{ on } B} = -\vec{F}_{B \text{ on } A} \quad (\text{Newton's third law of motion}) \quad (4.11)$$

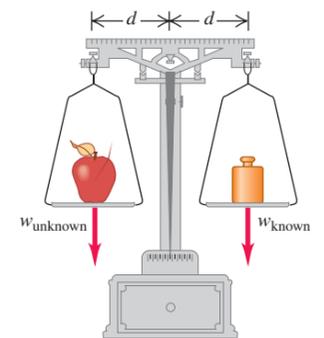
It doesn't matter whether one body is inanimate (like the soccer ball in Fig. 4.25) and the other is not (like the kicker): They necessarily exert forces on each other that obey Eq. (4.11).

In the statement of Newton's third law, "action" and "reaction" are the two opposite forces (in Fig. 4.25, $\vec{F}_{A \text{ on } B}$ and $\vec{F}_{B \text{ on } A}$); we sometimes refer to them as an **action-reaction pair**. This is *not* meant to imply any cause-and-effect relationship; we can consider either force as the "action" and the other as the "reaction." We often say simply that the forces are "equal and opposite," meaning that they have equal magnitudes and opposite directions.

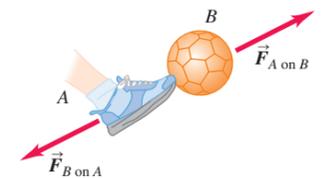
CAUTION The two forces in an action-reaction pair act on different bodies We stress that the two forces described in Newton's third law act on *different* bodies. This is important in problems involving Newton's first or second law, which involve the forces that act on a body. For instance, the net force acting on the soccer ball in Fig. 4.25 is the vector sum of the weight of the ball and the force $\vec{F}_{A \text{ on } B}$ exerted by the kicker. You would not include the force $\vec{F}_{B \text{ on } A}$ because this force acts on the kicker, not on the ball. ■

In Fig. 4.25 the action and reaction forces are *contact* forces that are present only when the two bodies are touching. But Newton's third law also applies to *long-range* forces that do not require physical contact, such as the force of gravitational attraction. A table-tennis ball exerts an upward gravitational force on the earth that's equal in magnitude to the downward gravitational force the earth exerts on the ball. When you drop the ball, both the ball and the earth accelerate toward each other. The net force on each body has the same magnitude, but the earth's acceleration is microscopically small because its mass is so great. Nevertheless, it does move!

4.24 An equal-arm balance determines the mass of a body (such as an apple) by comparing its weight to a known weight.



4.25 If body A exerts a force $\vec{F}_{A \text{ on } B}$ on body B , then body B exerts a force $\vec{F}_{B \text{ on } A}$ on body A that is equal in magnitude and opposite in direction: $\vec{F}_{A \text{ on } B} = -\vec{F}_{B \text{ on } A}$.



Conceptual Example 4.8 Which force is greater?

After your sports car breaks down, you start to push it to the nearest repair shop. While the car is starting to move, how does the force you exert on the car compare to the force the car exerts on you? How do these forces compare when you are pushing the car along at a constant speed?

SOLUTION

In *both* cases, the force you exert on the car is equal in magnitude and opposite in direction to the force the car exerts on you. It's true that you have to push harder to get the car going than to keep it going. But no matter how hard you push on the car, the car pushes just as hard back on you. Newton's third law gives the same result whether the two bodies are at rest, moving with constant velocity, or accelerating.

You may wonder how the car "knows" to push back on you with the same magnitude of force that you exert on it. It may help to remember that the forces you and the car exert on each other are really interactions between the atoms at the surface of your hand and the atoms at the surface of the car. These interactions are analogous to miniature springs between adjacent atoms, and a compressed spring exerts equally strong forces on both of its ends.

Fundamentally, though, the reason we know that objects of different masses exert equally strong forces on each other is that *experiment tells us so*. Never forget that physics isn't merely a collection of rules and equations; rather, it's a systematic description of the natural world based on experiment and observation.

Conceptual Example 4.9 Applying Newton's third law: Objects at rest

An apple sits on a table in equilibrium. What forces act on it? What is the reaction force to each of the forces acting on the apple? What are the action–reaction pairs?

SOLUTION

Figure 4.26a shows the forces acting on the apple. In the diagram, $\vec{F}_{\text{earth on apple}}$ is the weight of the apple—that is, the downward gravitational force exerted by the earth (first subscript) on the apple (second subscript). Similarly, $\vec{F}_{\text{table on apple}}$ is the upward force exerted by the table (first subscript) on the apple (second subscript).

As the earth pulls down on the apple, the apple exerts an equally strong upward pull $\vec{F}_{\text{apple on earth}}$ on the earth, as shown in Fig. 4.26b. $\vec{F}_{\text{apple on earth}}$ and $\vec{F}_{\text{earth on apple}}$ are an action–reaction pair, representing the mutual interaction of the apple and the earth, so

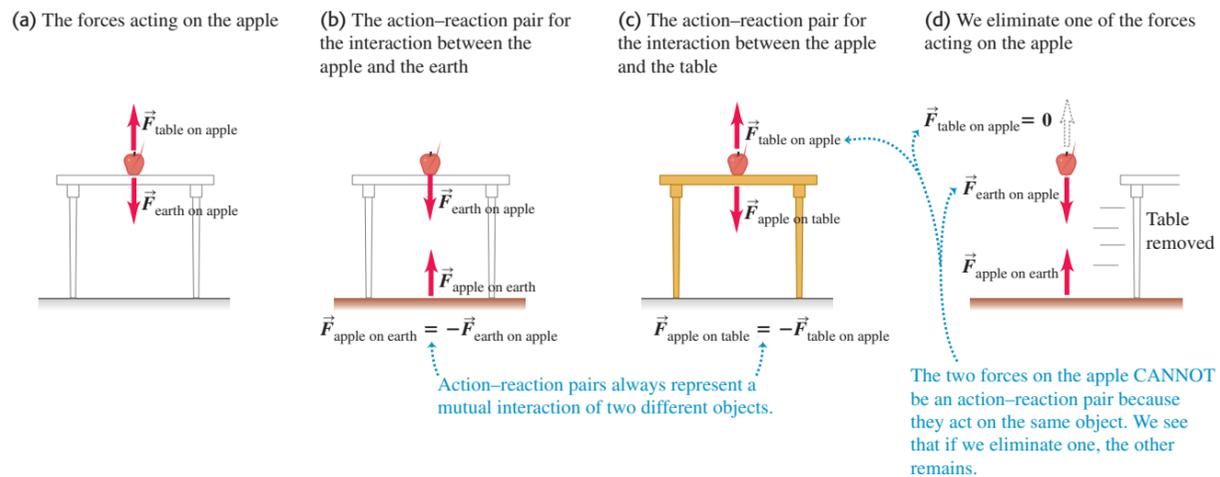
$$\vec{F}_{\text{apple on earth}} = -\vec{F}_{\text{earth on apple}}$$

Also, as the table pushes up on the apple with force $\vec{F}_{\text{table on apple}}$, the corresponding reaction is the downward force $\vec{F}_{\text{apple on table}}$ exerted by the apple on the table (Fig. 4.26c). So we have

$$\vec{F}_{\text{apple on table}} = -\vec{F}_{\text{table on apple}}$$

The two forces acting on the apple are $\vec{F}_{\text{table on apple}}$ and $\vec{F}_{\text{earth on apple}}$. Are they an action–reaction pair? No, they aren't, despite being equal and opposite. They do not represent the mutual interaction of two bodies; they are two different forces acting on the *same* body. *The two forces in an action–reaction pair never act on the same body.* Here's another way to look at it. Suppose we suddenly yank the table out from under the apple (Fig. 4.26d). The two forces $\vec{F}_{\text{apple on table}}$ and $\vec{F}_{\text{table on apple}}$ then become zero, but $\vec{F}_{\text{apple on earth}}$ and $\vec{F}_{\text{earth on apple}}$ are still there (the gravitational interaction is still present). Since $\vec{F}_{\text{table on apple}}$ is now zero, it can't be the negative of $\vec{F}_{\text{earth on apple}}$, and these two forces can't be an action–reaction pair.

4.26 The two forces in an action–reaction pair always act on different bodies.



Conceptual Example 4.10 Applying Newton's third law: Objects in motion

A stonemason drags a marble block across a floor by pulling on a rope attached to the block (Fig. 4.27a). The block may or may not be in equilibrium. How are the various forces related? What are the action–reaction pairs?

SOLUTION

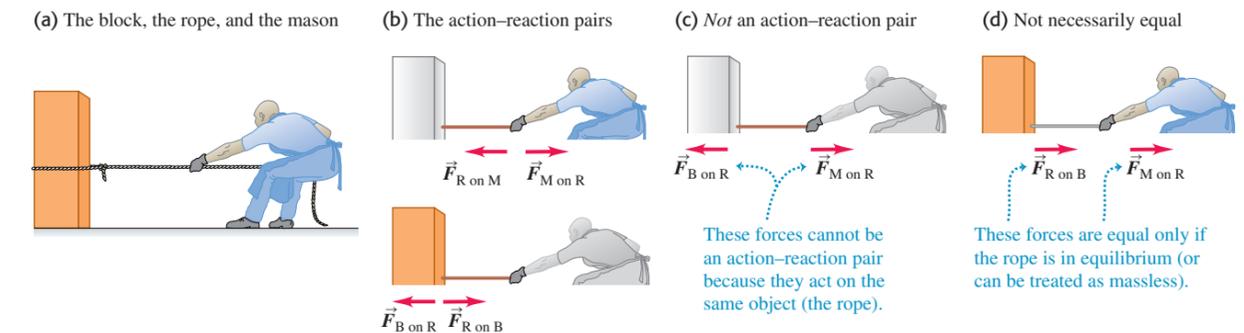
We'll use subscripts on all the forces to help explain things: B for the block, R for the rope, and M for the mason. Vector $\vec{F}_{\text{M on R}}$ represents the force exerted by the mason on the rope. Its reaction is the equal and opposite force $\vec{F}_{\text{R on M}}$ exerted by the rope on the mason. Vector $\vec{F}_{\text{R on B}}$ represents the force exerted by the rope on the block. The reaction to it is the equal and opposite force $\vec{F}_{\text{B on R}}$ exerted by the block on the rope. For these two action–reaction pairs (Fig. 4.27b), we have

$$\vec{F}_{\text{R on M}} = -\vec{F}_{\text{M on R}} \quad \text{and} \quad \vec{F}_{\text{B on R}} = -\vec{F}_{\text{R on B}}$$

Be sure you understand that the forces $\vec{F}_{\text{M on R}}$ and $\vec{F}_{\text{B on R}}$ are *not* an action–reaction pair (Fig. 4.27c) because both of these forces act on the *same* body (the rope); an action and its reaction *must* always act on *different* bodies. Furthermore, the forces $\vec{F}_{\text{M on R}}$ and $\vec{F}_{\text{B on R}}$ are not necessarily equal in magnitude. Applying Newton's second law to the rope, we get

$$\sum \vec{F} = \vec{F}_{\text{M on R}} + \vec{F}_{\text{B on R}} = m_{\text{rope}} \vec{a}_{\text{rope}}$$

4.27 Identifying the forces that act when a mason pulls on a rope attached to a block.



Conceptual Example 4.11 A Newton's third law paradox?

We saw in Conceptual Example 4.10 that the stonemason pulls as hard on the rope–block combination as that combination pulls back on him. Why, then, does the block move while the stonemason remains stationary?

SOLUTION

The way out of this seeming conundrum is to keep in mind the difference between Newton's *second* law and his *third* law. The only forces involved in Newton's second law are those that act *on* that body. The vector sum of these forces determines how the body accelerates (and whether it accelerates at all). By contrast, New-

ton's third law relates the forces that two *different* bodies exert on each other. The third law alone tells you nothing about the motion of either body.

If the rope–block combination is initially at rest, it begins to slide if the stonemason exerts a force $\vec{F}_{\text{M on R}}$ that is *greater* in magnitude than the friction force that the floor exerts on the block (Fig. 4.28). (The marble block has a smooth underside, which helps to minimize friction.) Hence there is a net force on the rope–block combination to the right, and so it accelerates to the right. By contrast, the stonemason *doesn't* move because the net force acting on him is *zero*. His shoes have nonskid soles that don't

accelerate. In the special case in which the rope is in equilibrium, the forces $\vec{F}_{\text{M on R}}$ and $\vec{F}_{\text{B on R}}$ are equal in magnitude. But this is an example of Newton's *first* law, not his *third*. Another way to look at this is that in equilibrium, $\vec{a}_{\text{rope}} = 0$ in the preceding equation. Then $\vec{F}_{\text{B on R}} = -\vec{F}_{\text{M on R}}$ because of Newton's first or second law.

This is also true if the rope is accelerating but has negligibly small mass compared to the block or the mason. In this case, $m_{\text{rope}} = 0$ in the above equation, so again $\vec{F}_{\text{B on R}} = -\vec{F}_{\text{M on R}}$. Since $\vec{F}_{\text{B on R}}$ *always* equals $-\vec{F}_{\text{R on B}}$ by Newton's third law (they are an action–reaction pair), in these same special cases, $\vec{F}_{\text{R on B}}$ also equals $\vec{F}_{\text{M on R}}$ (Fig. 4.27d). In other words, in these cases the force of the rope on the block equals the force of the mason on the rope, and we can then think of the rope as "transmitting" to the block, without change, the force the person exerts on the rope. This is a useful point of view, but you have to remember that it is valid *only* when the rope has negligibly small mass or is in equilibrium.

If you feel as though you're drowning in subscripts at this point, take heart. Go over this discussion again, comparing the symbols with the vector diagrams, until you're sure you see what's going on.

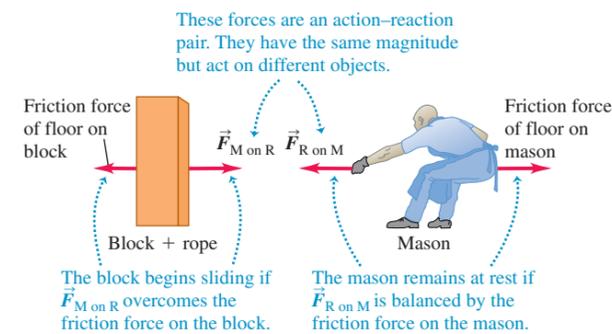
slip on the floor, so the friction force that the floor exerts on him is strong enough to exactly balance the pull of the rope, $\vec{F}_{R \text{ on } M}$. (Both the block and the stonemason also experience a downward force of gravity and an upward normal force exerted by the floor. These balance each other and cancel out, so we haven't included them in Fig. 4.28.)

Once the block is moving, the stonemason doesn't need to pull quite so hard; he need exert only enough force to exactly balance the friction force on the block. Then the net force on the moving block is zero, and the block continues to move toward the mason at a constant velocity in accordance with Newton's first law.

We conclude that the block moves while the stonemason doesn't because different amounts of friction act on them. If the floor were freshly waxed, so that there was little friction between the floor and the stonemason's shoes, pulling on the rope would start the block sliding to the right *and* start him sliding to the left.

The moral of this example is that when analyzing the motion of a body, remember that only forces acting *on* the body determine its

4.28 The horizontal forces acting on the block–rope combination (left) and the mason (right). (The vertical forces are not shown.)



motion. From this perspective, Newton's third law is merely a tool that can help you determine what those forces are.

A body, such as the rope in Fig. 4.27, that has pulling forces applied at its ends is said to be in *tension*. The **tension** at any point is the magnitude of force acting at that point (see Fig. 4.2c). In Fig. 4.27b the tension at the right end of the rope is the magnitude of $\vec{F}_{M \text{ on } R}$ (or of $\vec{F}_{R \text{ on } M}$), and the tension at the left end equals the magnitude of $\vec{F}_{B \text{ on } R}$ (or of $\vec{F}_{R \text{ on } B}$). If the rope is in equilibrium and if no forces act except at its ends, the tension is the *same* at both ends and throughout the rope. Thus, if the magnitudes of $\vec{F}_{B \text{ on } R}$ and $\vec{F}_{M \text{ on } R}$ are 50 N each, the tension in the rope is 50 N (*not* 100 N). The *total* force vector $\vec{F}_{B \text{ on } R} + \vec{F}_{M \text{ on } R}$ acting on the rope in this case is zero!

We emphasize once more a fundamental truth: The two forces in an action–reaction pair *never* act on the same body. Remembering this simple fact can often help you avoid confusion about action–reaction pairs and Newton's third law.

Test Your Understanding of Section 4.5 You are driving your car on a country road when a mosquito splatters itself on the windshield. Which has the greater magnitude, the force that the car exerted on the mosquito or the force that the mosquito exerted on the car? Or are the magnitudes the same? If they are different, how can you reconcile this fact with Newton's third law? If they are equal, why is the mosquito splattered while the car is undamaged?

4.6 Free-Body Diagrams

Newton's three laws of motion contain all the basic principles we need to solve a wide variety of problems in mechanics. These laws are very simple in form, but the process of applying them to specific situations can pose real challenges. In this brief section we'll point out three key ideas and techniques to use in any problems involving Newton's laws. You'll learn others in Chapter 5, which also extends the use of Newton's laws to cover more complex situations.

1. *Newton's first and second laws apply to a specific body.* Whenever you use Newton's first law, $\sum \vec{F} = \mathbf{0}$, for an equilibrium situation or Newton's second law, $\sum \vec{F} = m\vec{a}$, for a nonequilibrium situation, you must decide at the

beginning to which body you are referring. This decision may sound trivial, but it isn't.

2. *Only forces acting on the body matter.* The sum $\sum \vec{F}$ includes all the forces that act *on* the body in question. Hence, once you've chosen the body to analyze, you have to identify all the forces acting on it. Don't get confused between the forces acting on a body and the forces exerted by that body on some other body. For example, to analyze a person walking, you would include in $\sum \vec{F}$ the force that the ground exerts on the person as he walks, but *not* the force that the person exerts on the ground (Fig. 4.29). These forces form an action–reaction pair and are related by Newton's third law, but only the member of the pair that acts on the body you're working with goes into $\sum \vec{F}$.
3. *Free-body diagrams are essential to help identify the relevant forces.* A **free-body diagram** is a diagram showing the chosen body by itself, "free" of its surroundings, with vectors drawn to show the magnitudes and directions of all the forces applied to the body by the various other bodies that interact with it. We have already shown some free-body diagrams in Figs. 4.18, 4.19, 4.21, and 4.26a. Be careful to include all the forces acting *on* the body, but be equally careful *not* to include any forces that the body exerts on any other body. In particular, the two forces in an action–reaction pair must *never* appear in the same free-body diagram because they never act on the same body. Furthermore, forces that a body exerts on itself are never included, since these can't affect the body's motion.

CAUTION Forces in free-body diagrams When you have a complete free-body diagram, you *must* be able to answer for each force the question: What other body is applying this force? If you can't answer that question, you may be dealing with a nonexistent force. Be especially on your guard to avoid nonexistent forces such as "the force of acceleration" or "the $m\vec{a}$ force," discussed in Section 4.3.

When a problem involves more than one body, you have to take the problem apart and draw a separate free-body diagram for each body. For example, Fig. 4.27c shows a separate free-body diagram for the rope in the case in which the rope is considered massless (so that no gravitational force acts on it). Figure 4.28 also shows diagrams for the block and the mason, but these are *not* complete free-body diagrams because they don't show all the forces acting on each body. (We left out the vertical forces—the weight force exerted by the earth and the upward normal force exerted by the floor.)

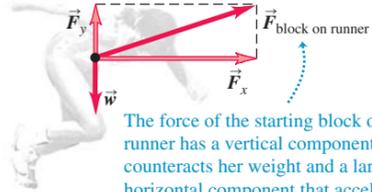
Figure 4.30 on page 128 presents some real-life situations and the corresponding complete free-body diagrams. Note that in each situation a person exerts a force on something in his or her surroundings, but the force that shows up in the person's free-body diagram is the surroundings pushing back *on* the person.

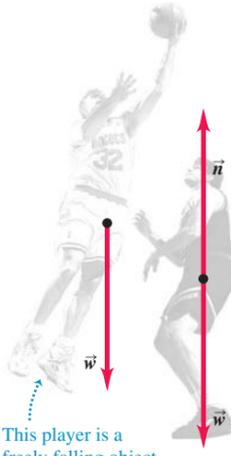
Test Your Understanding of Section 4.6 The buoyancy force shown in Fig. 4.30c is one half of an action–reaction pair. What force is the other half of this pair? (i) the weight of the swimmer; (ii) the forward thrust force; (iii) the backward drag force; (iv) the downward force that the swimmer exerts on the water; (v) the backward force that the swimmer exerts on the water by kicking.

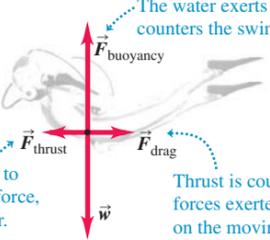
4.29 The simple act of walking depends crucially on Newton's third law. To start moving forward, you push backward on the ground with your foot. As a reaction, the ground pushes forward on your foot (and hence on your body as a whole) with a force of the same magnitude. This *external* force provided by the ground is what accelerates your body forward.



4.30 Examples of free-body diagrams. In each case, the free-body diagram shows all the external forces that act on the object in question.

(a)  
 The force of the starting block on the runner has a vertical component that counteracts her weight and a large horizontal component that accelerates her.

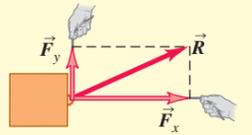
(b)  
 To jump up, this player will push down against the floor, increasing the upward reaction force \vec{n} of the floor on him.
 This player is a freely falling object.

(c)  
 The water exerts a buoyancy force that counters the swimmer's weight.
 Kicking causes the water to exert a forward reaction force, or thrust, on the swimmer.
 Thrust is countered by drag forces exerted by the water on the moving swimmer.

CHAPTER 4 SUMMARY

Force as a vector: Force is a quantitative measure of the interaction between two bodies. It is a vector quantity. When several forces act on a body, the effect on its motion is the same as when a single force, equal to the vector sum (resultant) of the forces, acts on the body. (See Example 4.1.)

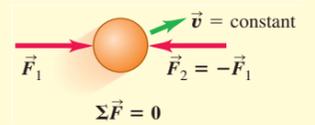
$$\vec{R} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \cdots = \sum \vec{F} \quad (4.1)$$



The net force on a body and Newton's first law: Newton's first law states that when the vector sum of all forces acting on a body (the *net force*) is zero, the body is in equilibrium and has zero acceleration. If the body is initially at rest, it remains at rest; if it is initially in motion, it continues to move with constant velocity. This law is valid only in inertial frames of reference. (See Examples 4.2 and 4.3.)

$$\sum \vec{F} = 0$$

(4.3)



Mass, acceleration, and Newton's second law: The inertial properties of a body are characterized by its *mass*. The acceleration of a body under the action of a given set of forces is directly proportional to the vector sum of the forces (the *net force*) and inversely proportional to the mass of the body. This relationship is Newton's second law. Like Newton's first law, this law is valid only in inertial frames of reference. The unit of force is defined in terms of the units of mass and acceleration. In SI units, the unit of force is the newton (N), equal to $1 \text{ kg} \cdot \text{m/s}^2$. (See Examples 4.4 and 4.5.)

$$\sum \vec{F} = m\vec{a}$$

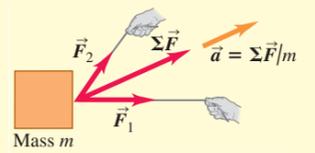
$$\sum F_x = ma_x$$

$$\sum F_y = ma_y$$

$$\sum F_z = ma_z$$

(4.7)

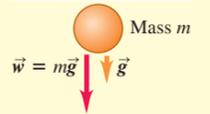
(4.8)



Weight: The weight \vec{w} of a body is the gravitational force exerted on it by the earth. Weight is a vector quantity. The magnitude of the weight of a body at any specific location is equal to the product of its mass m and the magnitude of the acceleration due to gravity g at that location. While the weight of a body depends on its location, the mass is independent of location. (See Examples 4.6 and 4.7.)

$$w = mg$$

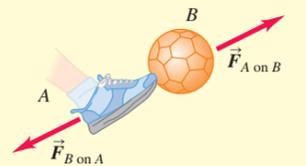
(4.9)



Newton's third law and action–reaction pairs: Newton's third law states that when two bodies interact, they exert forces on each other that at each instant are equal in magnitude and opposite in direction. These forces are called action and reaction forces. Each of these two forces acts on only one of the two bodies; they never act on the same body. (See Examples 4.8–4.11.)

$$\vec{F}_{A \text{ on } B} = -\vec{F}_{B \text{ on } A}$$

(4.11)



Key Terms

dynamics, 107
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 classical (Newtonian) mechanics, 107
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Answer to Chapter Opening Question ?

Newton's third law tells us that the seated child (who we'll call Ryder) pushes on the standing child (who we'll call Stan) just as hard as Stan pushes on Ryder, but in the opposite direction. This is true whether Ryder pushes on Stan "actively" (for instance, if Ryder pushed his hand against Stan's) or "passively" (if Ryder's back does the pushing, as in the photograph that opens the chapter). The force magnitudes would be greater in the "active" case than in the "passive" case, but either way Ryder's push on Stan is just as strong as Stan's push on Ryder.

Answers to Test Your Understanding Questions

4.1 Answer: (iv) The gravitational force on the crate points straight downward. In Fig. 4.6 the x -axis points up and to the right, and the y -axis points up and to the left. Hence the gravitational force has both an x -component and a y -component, and both are negative.

4.2 Answer: (i), (ii), and (iv) In (i), (ii), and (iv) the body is not accelerating, so the net force on the body is zero. [In (iv), the box remains stationary as seen in the inertial reference frame of the ground as the truck accelerates forward, like the skater in Fig. 4.11a.] In (iii), the hawk is moving in a circle; hence it is accelerating and is *not* in equilibrium.

4.3 Answer: (iii), (i) and (iv) (tie), (ii) The acceleration is equal to the net force divided by the mass. Hence the magnitude of the acceleration in each situation is

$$(i) a = (2.0 \text{ N}) / (2.0 \text{ kg}) = 1.0 \text{ m/s}^2;$$

$$(ii) a = (8.0 \text{ N}) / (2.0 \text{ kg}) = 4.0 \text{ m/s}^2;$$

$$(iii) a = (2.0 \text{ N}) / (8.0 \text{ kg}) = 0.25 \text{ m/s}^2;$$

$$(iv) a = (8.0 \text{ N}) / (8.0 \text{ kg}) = 1.0 \text{ m/s}^2.$$

4.4 It would take twice the effort for the astronaut to walk around because her weight on the planet would be twice as much as on the earth. But it would be just as easy to catch a ball moving horizontally. The ball's *mass* is the same as on earth, so the horizontal force the astronaut would have to exert to bring it to a stop (i.e., to give it the same acceleration) would also be the same as on earth.

4.5 By Newton's third law, the two forces have equal magnitudes. Because the car has much greater mass than the mosquito, it undergoes only a tiny, imperceptible acceleration in response to the force of the impact. By contrast, the mosquito, with its minuscule mass, undergoes a catastrophically large acceleration.

4.6 Answer: (iv) The buoyancy force is an *upward* force that the *water* exerts on the *swimmer*. By Newton's third law, the other half of the action–reaction pair is a *downward* force that the *swimmer* exerts on the *water* and has the same magnitude as the buoyancy force. It's true that the weight of the swimmer is also downward and has the same magnitude as the buoyancy force; however, the weight acts on the same body (the swimmer) as the buoyancy force, and so these forces aren't an action–reaction pair.

PROBLEMS

For instructor-assigned homework, go to www.masteringphysics.com 

Discussion Questions

Q4.1. Can a body be in equilibrium when only one force acts on it? Explain.

Q4.2. A ball thrown straight up has zero velocity at its highest point. Is the ball in equilibrium at this point? Why or why not?

Q4.3. A helium balloon hovers in midair, neither ascending nor descending. Is it in equilibrium? What forces act on it?

Q4.4. When you fly in an airplane at night in smooth air, there is no sensation of motion, even though the plane may be moving at 800 km/h (500 mi/h). Why is this?

Q4.5. If the two ends of a rope in equilibrium are pulled with forces of equal magnitude and opposite direction, why is the total tension in the rope not zero?

Q4.6. You tie a brick to the end of a rope and whirl the brick around you in a horizontal circle. Describe the path of the brick after you suddenly let go of the rope.

Q4.7. When a car stops suddenly, the passengers tend to move forward relative to their seats. Why? When a car makes a sharp turn, the passengers tend to slide to one side of the car. Why?

Q4.8. Some people say that the "force of inertia" (or "force of momentum") throws the passengers forward when a car brakes sharply. What is wrong with this explanation?

Q4.9. A passenger in a moving bus with no windows notices that a ball that has been at rest in the aisle suddenly starts to move toward the rear of the bus. Think of two different possible explanations, and devise a way to decide which is correct.

Q4.10. Suppose you chose the fundamental SI units to be force, length, and time instead of mass, length, and time. What would be the units of mass in terms of those fundamental units?

Q4.11. Some of the ancient Greeks thought that the "natural state" of an object was to be at rest, so objects would seek their natural state by coming to rest if left alone. Explain why this view can actually seem quite plausible in the everyday world.

Q4.12. Why is the earth only approximately an inertial reference frame?

Q4.13. Does Newton's second law hold true for an observer in a van as it speeds up, slows down, or rounds a corner? Explain.

Q4.14. Some students refer to the quantity $m\vec{a}$ as "the force of acceleration." Is it correct to refer to this quantity as a force? If so, what exerts this force? If not, what is a better description of this quantity?

Q4.15. The acceleration of a falling body is measured in an elevator traveling upward at a constant speed of 9.8 m/s. What result is obtained?

Q4.16. You can play catch with a softball in a bus moving with constant speed on a straight road, just as though the bus were at rest. Is this still possible when the bus is making a turn at constant speed on a level road? Why or why not?

Q4.17. Students sometimes say that the force of gravity on an object is 9.8 m/s^2 . What is wrong with this view?

Q4.18. The head of a hammer begins to come loose from its wooden handle. How should you strike the handle on a concrete sidewalk to reset the head? Why does this work?

Q4.19. Why can it hurt your foot more to kick a big rock than a small pebble? Must the big rock hurt more? Explain.

Q4.20. "It's not the fall that hurts you; it's the sudden stop at the bottom." Translate this saying into the language of Newton's laws of motion.

Q4.21. A person can dive into water from a height of 10 m without injury, but a person who jumps off the roof of a 10-m-tall building and lands on a concrete street is likely to be seriously injured. Why is there a difference?

Q4.22. Why are cars designed to crumple up in front and back for safety? Why not for side collisions and rollovers?

Q4.23. When a bullet is fired from a gun, what is the origin of the force that accelerates the bullet?

Q4.24. When a string barely strong enough lifts a heavy weight, it can lift the weight by a steady pull; but if you jerk the string, it will break. Explain in terms of Newton's laws of motion.

Q4.25. A large crate is suspended from the end of a vertical rope. Is the tension in the rope greater when the crate is at rest or when it is moving upward at constant speed? If the crate is traveling upward, is the tension in the rope greater when the crate is speeding up or when it is slowing down? In each case explain in terms of Newton's laws of motion.

Q4.26. Which feels a greater pull due to the earth's gravity, a 10-kg stone or a 20-kg stone? If you drop them, why does the 20-kg stone not fall with twice the acceleration of the 10-kg stone? Explain your reasoning.

Q4.27. Why is it incorrect to say that 1.0 kg *equals* 2.2 lb?

Q4.28. A horse is hitched to a wagon. Since the wagon pulls back on the horse just as hard as the horse pulls on the wagon, why does the wagon not remain in equilibrium, no matter how hard the horse pulls?

Q4.29. True or false? You exert a push P on an object and it pushes back on you with a force F . If the object is moving at constant velocity, then F is equal to P , but if the object is being accelerated, then P must be greater than F .

Q4.30. A large truck and a small compact car have a head-on collision. During the collision, the truck exerts a force $\vec{F}_{T \text{ on } C}$ on the car, and the car exerts a force $\vec{F}_{C \text{ on } T}$ on the truck. Which force has the larger magnitude, or are they the same? Does your answer depend on how fast each vehicle was moving before the collision? Why or why not?

Q4.31. When a car comes to a stop on a level highway, what force causes it to slow down? When the car increases its speed on the same highway, what force causes it to speed up? Explain.

Q4.32. A small compact car is pushing a large van that has broken down, and they travel along the road with equal velocities and accelerations. While the car is speeding up, is the force it exerts on the van larger than, smaller than, or the same magnitude as the force the van exerts on it? Which object, the car or the van, has the larger net force on it, or are the net forces the same? Explain.

Q4.33. Consider a tug-of-war between two people who pull in opposite directions on the ends of a rope. By Newton's third law, the force that A exerts on B is just as great as the force that B exerts on A . So what determines who wins? (*Hint:* Draw a free-body diagram showing all the forces that act on each person.)

Q4.34. On the moon, $g = 1.62 \text{ m/s}^2$. If a 2-kg brick drops on your foot from a height of 2 m, will this hurt more, or less, or the same if it happens on the moon instead of on the earth? Explain. If a 2-kg brick is thrown and hits you when it is moving horizontally at 6 m/s, will this hurt more, less, or the same if it happens on the moon instead of on the earth? Explain. (On the moon, assume that you are inside a pressurized structure, so you are not wearing a spacesuit.)

Q4.35. A manual for student pilots contains the following passage: "When an airplane flies at a steady altitude, neither climbing nor descending, the upward lift force from the wings equals the airplane's weight. When the airplane is climbing at a steady rate, the upward lift is greater than the weight; when the airplane is descending at a steady rate, the upward lift is less than the weight." Are these statements correct? Explain.

Q4.36. If your hands are wet and no towel is handy, you can remove some of the excess water by shaking them. Why does this get rid of the water?

Q4.37. If you are squatting down (such as when you are examining the books on the bottom shelf in a library or bookstore) and suddenly get up, you can temporarily feel light-headed. What do Newton's laws of motion have to say about why this happens?

Q4.38. When a car is hit from behind, the passengers can receive a whiplash. Use Newton's laws of motion to explain what causes this to occur.

Q4.39. In a head-on auto collision, passengers not wearing seat belts can be thrown through the windshield. Use Newton's laws of motion to explain why this happens.

Q4.40. In a head-on collision between a compact 1000-kg car and a large 2500-kg car, which one experiences the greater force? Explain. Which one experiences the greater acceleration? Explain why. Now explain why passengers in the smaller car are more likely to be injured than those in the large car, even if the bodies of both cars are equally strong.

Q4.41. Suppose you are in a rocket with no windows, traveling in deep space far from any other objects. Without looking outside the rocket or making any contact with the outside world, explain how you could determine if the rocket is (a) moving forward at a constant 80% of the speed of light and (b) accelerating in the forward direction.

Exercises

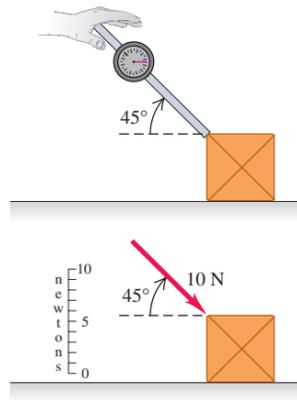
Section 4.1 Force and Interactions

4.1. Two forces have the same magnitude F . What is the angle between the two vectors if their sum has a magnitude of (a) $2F$? (b) $\sqrt{2}F$? (c) zero? Sketch the three vectors in each case.

4.2. Instead of using the x - and y -axes of Fig. 4.8 to analyze the situation of Example 4.1, use axes rotated 37.0° counterclockwise, so the y -axis is parallel to the 250-N force. (a) For these axes find the x - and y -components of the net force on the belt. (b) From the components computed in part (a) find the magnitude and direction of the net force. Compare your results to Example 4.1.

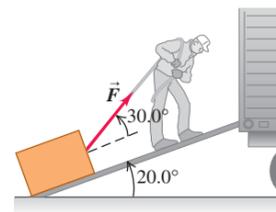
4.3. A warehouse worker pushes a crate along the floor, as shown in Fig. 4.31, with a force of 10 N that points downward at an angle of 45° below the horizontal. Find the horizontal and vertical components of the force.

Figure 4.31 Exercise 4.3.



4.4. A man is dragging a trunk up the loading ramp of a mover's truck. The ramp has a slope angle of 20.0° , and the man pulls upward with a force \vec{F} whose direction makes an angle of 30.0° with the ramp (Fig. 4.32). (a) How large a force \vec{F} is necessary for the component F_x parallel to the ramp to be 60.0 N? (b) How large will the component F_y perpendicular to the ramp then be?

Figure 4.32 Exercise 4.4.



4.5. Two dogs pull horizontally on ropes attached to a post; the angle between the ropes is 60.0° . If dog A exerts a force of 270 N and dog B exerts a force of 300 N, find the magnitude of the resultant force and the angle it makes with dog A's rope.

4.6. Two forces, \vec{F}_1 and \vec{F}_2 , act at a point. The magnitude of \vec{F}_1 is 9.00 N, and its direction is 60.0° above the x -axis in the second quadrant. The magnitude of \vec{F}_2 is 6.00 N, and its direction is 53.1° below the x -axis in the third quadrant. (a) What are the x - and y -components of the resultant force? (b) What is the magnitude of the resultant force?

Section 4.3 Newton's Second Law

4.7. If a net horizontal force of 132 N is applied to a person with mass 60 kg who is resting on the edge of a swimming pool, what horizontal acceleration is produced?

4.8. What magnitude of net force is required to give a 135-kg refrigerator an acceleration of magnitude 1.40 m/s^2 ?

4.9. A box rests on a frozen pond, which serves as a frictionless horizontal surface. If a fisherman applies a horizontal force with magnitude 48.0 N to the box and produces an acceleration of magnitude 3.00 m/s^2 , what is the mass of the box?

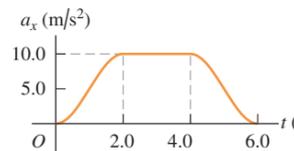
4.10. A dockworker applies a constant horizontal force of 80.0 N to a block of ice on a smooth horizontal floor. The frictional force is negligible. The block starts from rest and moves 11.0 m in 5.00 s. (a) What is the mass of the block of ice? (b) If the worker stops pushing at the end of 5.00 s, how far does the block move in the next 5.00 s?

4.11. A hockey puck with mass 0.160 kg is at rest at the origin ($x = 0$) on the horizontal, frictionless surface of the rink. At time $t = 0$ a player applies a force of 0.250 N to the puck, parallel to the x -axis; he continues to apply this force until $t = 2.00$ s. (a) What are the position and speed of the puck at $t = 2.00$ s? (b) If the same force is again applied at $t = 5.00$ s, what are the position and speed of the puck at $t = 7.00$ s?

4.12. A crate with mass 32.5 kg initially at rest on a warehouse floor is acted on by a net horizontal force of 140 N. (a) What acceleration is produced? (b) How far does the crate travel in 10.0 s? (c) What is its speed at the end of 10.0 s?

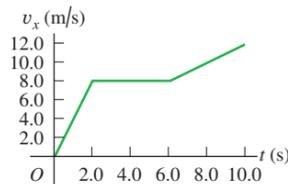
4.13. A 4.50-kg toy cart undergoes an acceleration in a straight line (the x -axis). The graph in Fig. 4.33 shows this acceleration as a function of time. (a) Find the maximum net force on this cart. When does this maximum force occur? (b) During what times is the net force on the cart a constant? (c) When is the net force equal to zero?

Figure 4.33 Exercise 4.13.



4.14. A 2.75-kg cat moves in a straight line (the x -axis). Figure 4.34 shows a graph of the x -component of this cat's velocity as a function of time. (a) Find the maximum net force on this cat. When does this force occur? (b) When is the net force on the cat equal to zero? (c) What is the net force at time 8.5 s?

Figure 4.34 Exercise 4.14.



4.15. A small 8.00-kg rocket burns fuel that exerts a time-varying upward force on the rocket. This force obeys the equation $F = A + Bt^2$. Measurements show that at $t = 0$, the force is 100.0 N, and at the end of the first 2.00 s, it is 150.0 N. (a) Find the constants A and B , including their SI units. (b) Find the net force on this rocket and its acceleration (i) the instant after the fuel ignites and (ii) 3.00 s after fuel ignition. (c) Suppose you were using this rocket in outer space, far from all gravity. What would its acceleration be 3.00 s after fuel ignition?

4.16. An electron (mass = 9.11×10^{-31} kg) leaves one end of a TV picture tube with zero initial speed and travels in a straight line to the accelerating grid, which is 1.80 cm away. It reaches the grid with a speed of 3.00×10^6 m/s. If the accelerating force is constant, compute (a) the acceleration; (b) the time to reach the grid; (c) the net force, in newtons. (You can ignore the gravitational force on the electron.)

Section 4.4 Mass and Weight

4.17. Superman throws a 2400-N boulder at an adversary. What horizontal force must Superman apply to the boulder to give it a horizontal acceleration of 12.0 m/s^2 ?

4.18. A bowling ball weighs 71.2 N (16.0 lb). The bowler applies a horizontal force of 160 N (36.0 lb) to the ball. What is the magnitude of the horizontal acceleration of the ball?

4.19. At the surface of Jupiter's moon Io, the acceleration due to gravity is $g = 1.81 \text{ m/s}^2$. A watermelon weighs 44.0 N at the surface of the earth. (a) What is the watermelon's mass on the earth's surface? (b) What are its mass and weight on the surface of Io?

4.20. An astronaut's pack weighs 17.5 N when she is on earth but only 3.24 N when she is at the surface of an asteroid. (a) What is the acceleration due to gravity on this asteroid? (b) What is the mass of the pack on the asteroid?

Section 4.5 Newton's Third Law

4.21. World-class sprinters can accelerate out of the starting blocks with an acceleration that is nearly horizontal and has magnitude 15 m/s^2 . How much horizontal force must a 55-kg sprinter exert on the starting blocks during a start to produce this acceleration? Which body exerts the force that propels the sprinter: the blocks or the sprinter herself?

4.22. Imagine that you are holding a book weighing 4 N at rest on the palm of your hand. Complete the following sentences: (a) A downward force of magnitude 4 N is exerted on the book by _____. (b) An upward force of magnitude _____ is exerted on _____ by your hand. (c) Is the upward force in part (b) the reaction to the downward force in part (a)? (d) The reaction to the force in part (a) is a force of magnitude _____, exerted on _____ by _____. Its direction is _____. (e) The reaction to the force in part (b) is a force of magnitude _____, exerted on _____ by _____. Its direction is _____. (f) The forces in parts (a) and (b) are equal and opposite because of Newton's _____ law. (g) The forces in parts (b) and (e) are equal and opposite because of Newton's _____ law. Now suppose that you exert an upward force of magnitude 5 N on the book. (h) Does the book remain in equilibrium? (i) Is the force exerted on the book by your hand equal and opposite to the force exerted on the book by the earth? (j) Is the force exerted on the book by the earth equal and opposite to the force exerted on the earth by the book? (k) Is the force exerted on the book by your hand equal and opposite to the force exerted on your hand by the book? Finally, suppose you snatch your hand away while the book is moving upward. (l) How many forces then act on the book? (m) Is the book in equilibrium?

4.23. A bottle is given a push along a tabletop and slides off the edge of the table. Do not ignore air resistance. (a) What forces are exerted on the bottle while it is falling from the table to the floor? (b) What is the reaction to each force; that is, on which body and by which body is the reaction exerted?

4.24. The upward normal force exerted by the floor is 620 N on an elevator passenger who weighs 650 N. What are the reaction forces to these two forces? Is the passenger accelerating? If so, what are the magnitude and direction of the acceleration?

4.25. A student with mass 45 kg jumps off a high diving board. Using 6.0×10^{24} kg for the mass of the earth, what is the acceleration of the earth toward her as she accelerates toward the earth with an acceleration of 9.8 m/s^2 ? Assume that the net force on the earth is the force of gravity she exerts on it.

Section 4.6 Free-Body Diagrams

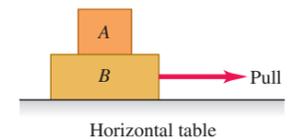
4.26. An athlete throws a ball of mass m directly upward, and it feels no appreciable air resistance. Draw a free-body diagram of this ball while it is free of the athlete's hand and (a) moving upward; (b) at its highest point; (c) moving downward. (d) Repeat

parts (a), (b), and (c) if the athlete throws the ball at a 60° angle above the horizontal instead of directly upward.

4.27. Two crates, A and B, sit at rest side by side on a frictionless horizontal surface. The crates have masses m_A and m_B . A horizontal force \vec{F} is applied to crate A and the two crates move off to the right. (a) Draw clearly labeled free-body diagrams for crate A and for crate B. Indicate which pairs of forces, if any, are third-law action–reaction pairs. (b) If the magnitude of force \vec{F} is less than the total weight of the two crates, will it cause the crates to move? Explain.

4.28. A person pulls horizontally on block B in Fig. 4.35, causing both blocks to move together as a unit. While this system is moving, make a carefully labeled free-body diagram of block A if (a) the table is frictionless and (b) there is friction between block B and the table and the pull is equal to the friction force on block B due to the table.

Figure 4.35 Exercise 4.28.



4.29. A ball is hanging from a long string that is tied to the ceiling of a train car traveling eastward on horizontal tracks. An observer inside the train car sees the ball hang motionless. Draw a clearly labeled free-body diagram for the ball if (a) the train has a uniform velocity, and (b) the train is speeding up uniformly. Is the net force on the ball zero in either case? Explain.

4.30. A large box containing your new computer sits on the bed of your pickup truck. You are stopped at a red light. The light turns green and you stomp on the gas and the truck accelerates. To your horror, the box starts to slide toward the back of the truck. Draw clearly labeled free-body diagrams for the truck and for the box. Indicate pairs of forces, if any, that are third-law action–reaction pairs. (The bed of the truck is not frictionless.)

4.31. A chair of mass 12.0 kg is sitting on the horizontal floor; the floor is not frictionless. You push on the chair with a force $F = 40.0$ N that is directed at an angle of 37.0° below the horizontal and the chair slides along the floor. (a) Draw a clearly labeled free-body diagram for the chair. (b) Use your diagram and Newton's laws to calculate the normal force that the floor exerts on the chair.

4.32. A skier of mass 65.0 kg is pulled up a snow-covered slope at constant speed by a tow rope that is parallel to the ground. The ground slopes upward at a constant angle of 26.0° above the horizontal, and you can ignore friction. (a) Draw a clearly labeled free-body diagram for the skier. (b) Calculate the tension in the tow rope.

4.33. A truck is pulling a car on a horizontal highway using a horizontal rope. The car is in neutral gear, so we can assume that there is no appreciable friction between its tires and the highway. As the truck is accelerating to highway speeds, draw a free-body diagram of (a) the car and (b) the truck. (c) What force accelerates this system forward? Explain how this force originates.

Problems

4.34. A .22 rifle bullet, traveling at 350 m/s, strikes a large tree, which it penetrates to a depth of 0.130 m. The mass of the bullet is 1.80 g. Assume a constant retarding force. (a) How much time is required for the bullet to stop? (b) What force, in newtons, does the tree exert on the bullet?

4.35. Two horses pull horizontally on ropes attached to a stump. The two forces \vec{F}_1 and \vec{F}_2 that they apply to the stump are such that the net (resultant) force \vec{R} has a magnitude equal to that of \vec{F}_1 and makes an angle of 90° with \vec{F}_1 . Let $F_1 = 1300$ N and $R = 1300$ N also. Find the magnitude of \vec{F}_2 and its direction (relative to \vec{F}_1).

4.36. You have just landed on Planet X. You take out a 100-g ball, release it from rest from a height of 10.0 m, and measure that it takes 2.2 s to reach the ground. You can ignore any force on the ball from the atmosphere of the planet. How much does the 100-g ball weigh on the surface of Planet X?

4.37. Two adults and a child want to push a wheeled cart in the direction marked x in Fig. 4.36.

The two adults push with horizontal forces \vec{F}_1 and \vec{F}_2 as shown in the figure. (a) Find the magnitude and direction of the *smallest* force that the child should exert. You can ignore the effects of friction. (b) If the child exerts the minimum force found in part (a), the cart accelerates at 2.0 m/s^2 in the $+x$ -direction. What is the weight of the cart?

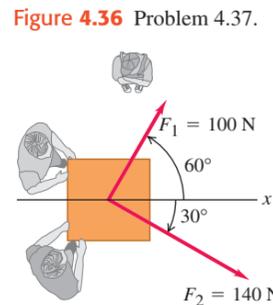
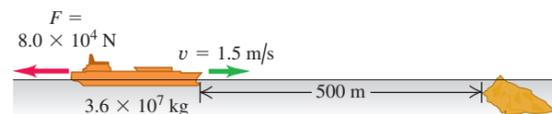


Figure 4.36 Problem 4.37.

4.38. An oil tanker's engines have broken down, and the wind is blowing the tanker straight toward a reef at a constant speed of 1.5 m/s (Fig. 4.37). When the tanker is 500 m from the reef, the wind dies down just as the engineer gets the engines going again. The rudder is stuck, so the only choice is to try to accelerate straight backward away from the reef. The mass of the tanker and cargo is $3.6 \times 10^7 \text{ kg}$, and the engines produce a net horizontal force of $8.0 \times 10^4 \text{ N}$ on the tanker. Will the ship hit the reef? If it does, will the oil be safe? The hull can withstand an impact at a speed of 0.2 m/s or less. You can ignore the retarding force of the water on the tanker's hull.

Figure 4.37 Problem 4.38.



4.39. A Standing Vertical Jump. Basketball player Darrell Griffith is on record as attaining a standing vertical jump of 1.2 m (4 ft). (This means that he moved upward by 1.2 m after his feet left the floor.) Griffith weighed 890 N (200 lb). (a) What is his speed as he leaves the floor? (b) If the time of the part of the jump before his feet left the floor was 0.300 s, what was his average acceleration (magnitude and direction) while he was pushing against the floor? (c) Draw his free-body diagram (see Section 4.6). In terms of the forces on the diagram, what is the net force on him? Use Newton's laws and the results of part (b) to calculate the average force he applied to the ground.

4.40. An advertisement claims that a particular automobile can "stop on a dime." What net force would actually be necessary to stop a 850-kg automobile traveling initially at 45.0 km/h in a distance equal to the diameter of a dime, which is 1.8 cm ?

4.41. A 4.80-kg bucket of water is accelerated upward by a cord of negligible mass whose breaking strength is 75.0 N . (a) Draw the free-body force diagram for the bucket. In terms of the forces on your diagram, what is the net force on the bucket? (b) Apply Newton's second law to the bucket and find the maximum upward acceleration that can be given to the bucket without breaking the cord.

4.42. A parachutist relies on air resistance (mainly on her parachute) to decrease her downward velocity. She and her parachute

have a mass of 55.0 kg , and air resistance exerts a total upward force of 620 N on her and her parachute. (a) What is the weight of the parachutist? (b) Draw a free-body diagram for the parachutist (see Section 4.6). Use that diagram to calculate the net force on the parachutist. Is the net force upward or downward? (c) What is the acceleration (magnitude and direction) of the parachutist?

4.43. Two crates, one with mass 4.00 kg and the other with mass 6.00 kg , sit on the frictionless surface of a frozen pond, connected by a light rope (Fig. 4.38). A woman wearing golf shoes (so she can get traction on the ice) pulls horizontally on the 6.00-kg crate with a force F that gives the crate an acceleration of 2.50 m/s^2 . (a) What is the acceleration of the 4.00-kg crate? (b) Draw a free-body diagram for the 4.00-kg crate. Use that diagram and Newton's second law to find the tension T in the rope that connects the two crates. (c) Draw a free-body diagram for the 6.00-kg crate. What is the direction of the net force on the 6.00-kg crate? Which is larger in magnitude, force T or force F ? (d) Use part (c) and Newton's second law to calculate the magnitude of the force F .

4.44. An astronaut is tethered by a strong cable to a spacecraft. The astronaut and her spacesuit have a total mass of 105 kg , while the mass of the cable is negligible. The mass of the spacecraft is $9.05 \times 10^4 \text{ kg}$. The spacecraft is far from any large astronomical

Figure 4.38 Problem 4.43.



bodies, so we can ignore the gravitational forces on it and the astronaut. We also assume that both the spacecraft and the astronaut are initially at rest in an inertial reference frame. The astronaut then pulls on the cable with a force of 80.0 N . (a) What force does the cable exert on the astronaut? (b) Since $\sum \vec{F} = m\vec{a}$, how can a "massless" ($m = 0$) cable exert a force? (c) What is the astronaut's acceleration? (d) What force does the cable exert on the spacecraft? (e) What is the acceleration of the spacecraft?

4.45. To study damage to aircraft that collide with large birds, you design a test gun that will accelerate chicken-sized objects so that their displacement along the gun barrel is given by $x = (9.0 \times 10^3 \text{ m/s}^2)t^2 - (8.0 \times 10^4 \text{ m/s}^3)t^3$. The object leaves the end of the barrel at $t = 0.025 \text{ s}$. (a) How long must the gun barrel be? (b) What will be the speed of the objects as they leave the end of the barrel? (c) What net force must be exerted on a 1.50-kg object at (i) $t = 0$ and (ii) $t = 0.025 \text{ s}$?

4.46. A spacecraft descends vertically near the surface of Planet X. An upward thrust of 25.0 kN from its engines slows it down at a rate of 1.20 m/s^2 , but it speeds up at a rate of 0.80 m/s^2 with an upward thrust of 10.0 kN . (a) In each case, what is the direction of the acceleration of the spacecraft? (b) Draw a free-body diagram for the spacecraft. In each case, speeding up or slowing down, what is the direction of the net force on the spacecraft? (c) Apply Newton's second law to each case, slowing down or speeding up, and use this to find the spacecraft's weight near the surface of Planet X.

4.47. A 6.50-kg instrument is hanging by a vertical wire inside a space ship that is blasting off at the surface of the earth. This ship starts from rest and reaches an altitude of 276 m in 15.0 s with constant acceleration. (a) Draw a free-body diagram for the instrument

during this time. Indicate which force is greater. (b) Find the force that the wire exerts on the instrument.

4.48. Suppose the rocket in Problem 4.47 is coming in for a vertical landing instead of blasting off. The captain adjusts the engine thrust so that the magnitude of the rocket's acceleration is the same as it was during blast-off. Repeat parts (a) and (b).

4.49. A gymnast of mass m climbs a vertical rope attached to the ceiling. You can ignore the weight of the rope. Draw a free-body diagram for the gymnast. Calculate the tension in the rope if the gymnast (a) climbs at a constant rate; (b) hangs motionless on the rope; (c) accelerates up the rope with an acceleration of magnitude $|\vec{a}|$; (d) slides down the rope with a downward acceleration of magnitude $|\vec{a}|$.

4.50. A loaded elevator with very worn cables has a total mass of 2200 kg , and the cables can withstand a maximum tension of $28,000 \text{ N}$. (a) Draw the free-body force diagram for the elevator. In terms of the forces on your diagram, what is the net force on the elevator? Apply Newton's second law to the elevator and find the maximum upward acceleration for the elevator if the cables are not to break. (b) What would be the answer to part (a) if the elevator were on the moon, where $g = 1.62 \text{ m/s}^2$?

4.51. Jumping to the Ground. A 75.0-kg man steps off a platform 3.10 m above the ground. He keeps his legs straight as he falls, but at the moment his feet touch the ground his knees begin to bend, and, treated as a particle, he moves an additional 0.60 m before coming to rest. (a) What is his speed at the instant his feet touch the ground? (b) Treating him as a particle, what is his acceleration (magnitude and direction) as he slows down, if the acceleration is assumed to be constant? (c) Draw his free-body diagram (see Section 4.6). In terms of the forces on the diagram, what is the net force on him? Use Newton's laws and the results of part (b) to calculate the average force his feet exert on the ground while he slows down. Express this force in newtons and also as a multiple of his weight.

4.52. A 4.9-N hammer head is stopped from an initial downward velocity of 3.2 m/s in a distance of 0.45 cm by a nail in a pine board. In addition to its weight, there is a 15-N downward force on the hammer head applied by the person using the hammer. Assume that the acceleration of the hammer head is constant while it is in contact with the nail and moving downward. (a) Draw a free-body diagram for the hammer head. Identify the reaction force to each action force in the diagram. (b) Calculate the downward force \vec{F} exerted by the hammer head on the nail while the hammer head is in contact with the nail and moving downward. (c) Suppose the nail is in hardwood and the distance the hammer head travels in coming to rest is only 0.12 cm . The downward forces on the hammer head are the same as on part (b). What then is the force \vec{F} exerted by the hammer head on the nail while the hammer head is in contact with the nail and moving downward?

4.53. A uniform cable of weight w hangs vertically downward, supported by an upward force of magnitude w at its top end. What is the tension in the cable (a) at its top end; (b) at its bottom end; (c) at its middle? Your answer to each part must include a free-body diagram. (Hint: For each question choose the body to analyze to be a section of the cable or a point along the cable.) (d) Graph the tension in the rope versus the distance from its top end.

4.54. The two blocks in Fig. 4.39 are connected by a heavy uniform rope with a mass of 4.00 kg . An upward force of 200 N is applied as shown. (a) Draw three free-body diagrams, one for the 6.00-kg block, one for the 4.00-kg rope, and another one for the 5.00-kg block. For each force, indicate what body exerts that force. (b) What

is the acceleration of the system? (c) What is the tension at the top of the heavy rope? (d) What is the tension at the midpoint of the rope?

4.55. An athlete whose mass is 90.0 kg is performing weight-lifting exercises. Starting from the rest position, he lifts, with constant acceleration, a barbell that weighs 490 N . He lifts the barbell a distance of 0.60 m in 1.6 s . (a) Draw a clearly labeled free-body force diagram for the barbell and for the athlete. (b) Use the diagrams in part (a) and Newton's laws to find the total force that his feet exert on the ground as he lifts the barbell.

4.56. A hot-air balloon consists of a basket, one passenger, and some cargo. Let the total mass be M . Even though there is an upward lift force on the balloon, the balloon is initially accelerating downward at a rate of $g/3$. (a) Draw a free-body diagram for the descending balloon. (b) Find the upward lift force in terms of the initial total weight Mg . (c) The passenger notices that he is heading straight for a waterfall and decides he needs to go up. What fraction of the total weight must he drop overboard so that the balloon accelerates upward at a rate of $g/2$? Assume that the upward lift force remains the same.

4.57. A student tries to raise a chain consisting of three identical links. Each link has a mass of 300 g . The three-piece chain is connected to a string and then suspended vertically, with the student holding the upper end of the string and pulling upward. Because of the student's pull, an upward force of 12 N is applied to the chain by the string. (a) Draw a free-body diagram for each of the links in the chain and also for the entire chain considered as a single body. (b) Use the results of part (a) and Newton's laws to find (i) the acceleration of the chain and (ii) the force exerted by the top link on the middle link.

4.58. The position of a $2.75 \times 10^5 \text{ N}$ training helicopter under test is given by $\vec{r} = (0.020 \text{ m/s}^3)t^3\hat{i} + (2.2 \text{ m/s})t\hat{j} - (0.060 \text{ m/s}^2)t^2\hat{k}$. Find the net force on the helicopter at $t = 5.0 \text{ s}$.

4.59. An object with mass m moves along the x -axis. Its position as a function of time is given by $x(t) = At - Bt^3$, where A and B are constants. Calculate the net force on the object as a function of time.

4.60. An object with mass m initially at rest is acted on by a force $\vec{F} = k_1\hat{i} + k_2t^3\hat{j}$, where k_1 and k_2 are constants. Calculate the velocity $\vec{v}(t)$ of the object as a function of time.

Challenge Problems

4.61. If we know $F(t)$, the force as a function of time, for straight-line motion, Newton's second law gives us $a(t)$, the acceleration as a function of time. We can then integrate $a(t)$ to find $v(t)$ and $x(t)$. However, suppose we know $F(v)$ instead. (a) The net force on a body moving along the x -axis equals $-Cv^2$. Use Newton's second law written as $\sum F = m dv/dt$ and two integrations to show that $x - x_0 = (m/C) \ln(v_0/v)$. (b) Show that Newton's second law can be written as $\sum F = mv dv/dx$. Derive the same expression as in part (a) using this form of the second law and one integration.

4.62. An object of mass m is at rest in equilibrium at the origin. At $t = 0$ a new force $\vec{F}(t)$ is applied that has components

$$F_x(t) = k_1 + k_2y \quad F_y(t) = k_3t$$

where k_1 , k_2 , and k_3 are constants. Calculate the position $\vec{r}(t)$ and velocity $\vec{v}(t)$ vectors as functions of time.

Figure 4.39 Problem 4.54.

