

Summary of Equations to Accompany INTRODUCTORY CIRCUIT ANALYSIS, Eleventh Edition, by Robert L. Boylestad

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Introduction

Conversions 1 meter = 100 cm = 39.37 in., 1 in. = 2.54 cm,
 1 yd = 0.914 m = 3 ft, 1 mile = 5280 ft, $^{\circ}\text{F} = 9/5 \cdot ^{\circ}\text{C} + 32$, $^{\circ}\text{C} = 5/9(^{\circ}\text{F} - 32)$, $K = 273.15 + ^{\circ}\text{C}$ **Scientific notation** 10^{12} = tera = T, 10^9 = giga = G, 10^6 = mega = M, 10^3 = kilo = k, 10^{-3} = milli = m, 10^{-6} = micro = μ , 10^{-9} = nano = n, 10^{-12} = pico = p
Powers of ten $1/10^n = 10^{-n}$, $1/10^{-n} = 10^n$, $(10^n)(10^m) = 10^{n+m}$, $10^n/10^m = 10^{n-m}$, $(10^n)^m = 10^{nm}$

Voltage and Current

Coulomb's law $F = kQ_1Q_2/r^2$, $k = 9 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2$,
Q = coulombs (C), **r** = meters (m) **Current** $I = Q/t$ (amperes),
t = seconds (s), $Q_e = 1.6 \times 10^{-19} \text{ C}$ **Voltage** $V = W/Q$ (volts),
W = joules (J)

Resistance

Circular wire $R = \rho l/A$ (ohms), ρ = resistivity, l = feet,
 $A_{\text{CM}} = (d_{\text{mil}})^2$, $\rho(\text{Cu}) = 10.37$ **Metric units** $l = \text{cm}$, $A = \text{cm}^2$,
 $\rho(\text{Cu}) = 1.724 \times 10^{-6} \text{ ohm-cm}$ **Temperature** $(|T| + T_1)R_1 = (|T| + T_2)R_2$, $R_1 = R_{20}[1 + \alpha_{20}(T_1 - 20^\circ\text{C})]$, $\alpha_{20}(\text{Cu}) = 0.00393$
Color code Bands 1-3: 0 = black, 1 = brown, 2 = red, 3 = orange,
 4 = yellow, 5 = green, 6 = blue, 7 = violet, 8 = gray, 9 = white,
 Band 3: 0.1 = gold, 0.01 = silver, Band 4: 5% = gold, 10% = silver,
 20% = no band, Band 5: 1% = brown, 0.1% = red, 0.01% = orange,
 0.001% = yellow **Conductance** $G = 1/R$ siemens (S)

Ohm's Law, Power, and Energy

Ohm's law $I = E/R$, $E = IR$, $R = E/I$ **Power** $P = W/t = VI = I^2R = V^2/R$ (watts), 1 hp = 746 W
Efficiency $\eta\% = (P_o/P_i) \times 100\%$, $\eta_T = \eta_1 \cdot \eta_2 \cdot \eta_3 \cdots \eta_n$
Energy $W = Pt$, W (kWh) = $[P(\text{W}) \cdot t(\text{h})]/1000$

Series Circuits

$R_T = R_1 + R_2 + R_3 + \cdots + R_N$, $R_T = NR$, $I = E/R_T$, $V = IR$
Kirchhoff's voltage law $\sum_{\text{C}} V = 0$, $\sum_{\text{C}} V_{\text{rises}} = \sum_{\text{C}} V_{\text{drops}}$
Voltage divider rule $V_x = R_x E/R_T$

Parallel dc Circuits

$R_T = 1/(1/R_1 + 1/R_2 + 1/R_3 + \cdots + 1/R_N)$, $R_T = R/N$,
 $R_T = R_1 R_2 / (R_1 + R_2)$, $I = EG_T = E/R_T$
Kirchhoff's current law $\sum I_{\text{entering}} = \sum I_{\text{leaving}}$
Current divider rule $I_x = (R_T/R_x)I$, (Two parallel elements):
 $I_1 = R_2 I / (R_1 + R_2)$, $I_2 = R_1 I / (R_1 + R_2)$

Series-Parallel Circuits

Potentiometer loading $R_L >> R_T$
Ammeter $R_{\text{shunt}} = R_m I_{CS} / (I_{\text{max}} - I_{CS})$
Voltmeter $R_{\text{series}} = (V_{\text{max}} - V_{\text{VS}}) / I_{CS}$
Ohmmeter $R_s = (E/I_{CS}) - R_m$ - zero-adjust/2

Methods of Analysis and Selected Topics (dc)

Source conversions $E = IR_p$, $R_s = R_p$, $I = E/R_s$

Determinants $D = \begin{vmatrix} a_1 & b_1 \\ a_2 & b_2 \end{vmatrix} = a_1 b_2 - a_2 b_1$

Bridge networks $R_1/R_3 = R_2/R_4$ **Δ -Y conversions** $R' = R_A + R_B + R_C$, $R_3 = R_A R_B / R'$, $R_2 = R_A R_C / R'$, $R_1 = R_B R_C / R'$, $R_Y = R_A / 3$
Y- Δ conversions $R'' = R_1 R_2 + R_1 R_3 + R_2 R_3$, $R_C = R'' / R_3$, $R_B = R'' / R_2$, $R_A = R'' / R_1$, $R_\Delta = 3R_Y$

Network Theorems

Superposition Voltage sources (short-circuit equivalent), current sources (open-circuit equivalent)

Thévenin's Theorem R_{Th} : (all sources to zero), E_{Th} : (open-circuit terminal voltage)

Maximum power transfer theorem $R_L = R_{Th} = R_N$, $P_{\text{max}} = E_{Th}^2 / 4R_{Th} = I_N^2 R_N / 4$

Capacitors

Capacitance $C = Q/V = eA/d = 8.85 \times 10^{-12} \epsilon_r A/d$ farads (F),
 $C = \epsilon_r C_0$ **Electric field strength** $E = V/d = Q/eA$ (volts/meter)

Transients (charging) $i_C = (E/R)e^{-t/\tau}$, $\tau = RC$, $v_C = E(1 - e^{-t/\tau})$, (discharge) $v_C = Ee^{-t/\tau}$, $i_C = (E/R)e^{-t/\tau RC}$ $i_C = i_{C_{\text{av}}} = C(\Delta v_C / \Delta t)$

Series $Q_T = Q_1 = Q_2 = Q_3$, $1/C_T = (1/C_1) + (1/C_2) + (1/C_3) + \cdots + (1/C_N)$, $C_T = C_1 C_2 / (C_1 + C_2)$ **Parallel** $Q_T = Q_1 + Q_2 + Q_3$, $C_T = C_1 + C_2 + C_3$ **Energy** $W_C = (1/2)CV^2$

Inductors

Self-inductance $L = N^2 \mu A/l$ (henries), $L = \mu_r L_0$

Induced voltage $e_{L_{\text{av}}} = L(\Delta i / \Delta t)$ **Transients** (storage) $i_L =$

$I_m(1 - e^{-t/\tau})$, $I_m = E/R$, $\tau = L/R$, $v_L = Ee^{-t/\tau}$ (decay), $v_L =$

$[1 + (R_2/R_1)]Ee^{-t/\tau'}$, $\tau' = L/(R_1 + R_2)$, $i_L = I_m e^{-t/\tau'}$, $I_m = E/R_1$

Series $L_T = L_1 + L_2 + L_3 + \cdots + L_N$ **Parallel** $1/L_T = (1/L_1) + (1/L_2) + (1/L_3) + \cdots + (1/L_N)$, $L_T = L_1 L_2 / (L_1 + L_2)$

Energy $W_L = 1/2(LI^2)$

Magnetic Circuits

Flux density $B = \Phi/A$ (webers/m²) **Permeability** $\mu = \mu_r \mu_0$

(Wb/A·m) **Reluctance** $\mathcal{R} = l/\mu A$ (rels)

Ohm's law $\Phi = \mathcal{F}/\mathcal{R}$ (webers)

Magnetomotive force $\mathcal{F} = NI$ (ampere-turns) **Magnetizing**

force $H = \mathcal{F}/l = NI/l$ **Ampère's circuital law** $\Sigma_C \mathcal{F} = 0$

Flux $\Sigma \Phi_{\text{entering}} = \Sigma \Phi_{\text{leaving}}$ **Air gap** $H_g = 7.96 \times 10^5 B_g$

Greek Alphabet

Letter	Capital	Lowercase	Letter	Capital	Lowercase
Alpha	A	α	Nu	N	ν
Beta	B	β	Xi	Ξ	ξ
Gamma	Γ	γ	Omicron	O	\omicron
Delta	Δ	δ	Pi	Π	π
Epsilon	E	ϵ	Rho	R	ρ
Zeta	Z	ζ	Sigma	Σ	σ
Eta	H	η	Tau	T	τ
Theta	Θ	θ	Upsilon	Υ	υ
Iota	I	ι	Phi	Φ	ϕ
Kappa	K	κ	Chi	X	χ
Lambda	Λ	λ	Psi	Ψ	ψ
Mu	M	μ	Omega	Ω	ω

Prefixes

Multiplication Factors	SI Prefix	SI Symbol
$1 \ 000 \ 000 \ 000 \ 000 \ 000 \ 000 = 10^{18}$	exa	E
$1 \ 000 \ 000 \ 000 \ 000 \ 000 = 10^{15}$	peta	P
$1 \ 000 \ 000 \ 000 \ 000 = 10^{12}$	tera	T
$1 \ 000 \ 000 \ 000 = 10^9$	giga	G
$1 \ 000 \ 000 = 10^6$	mega	M
$1 \ 000 = 10^3$	kilo	k
$0.001 = 10^{-3}$	milli	m
$0.000 \ 001 = 10^{-6}$	micro	μ
$0.000 \ 000 \ 001 = 10^{-9}$	nano	n
$0.000 \ 000 \ 000 \ 001 = 10^{-12}$	pico	p
$0.000 \ 000 \ 000 \ 000 \ 001 = 10^{-15}$	femto	f
$0.000 \ 000 \ 000 \ 000 \ 000 \ 001 = 10^{-18}$	atto	a

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ac

Sinusoidal Alternating Waveforms

Sine wave $v = V_m \sin \omega t$, $\alpha = \omega t = 2\pi ft$, $f = 1/T$, 1 radian = 57.3° , radians = $(\pi/180^\circ) \times (\text{degrees})$, degrees = $(180^\circ/\pi) \times (\text{radians})$

Identities $\sin(\omega t + 90^\circ) = \cos \omega t$, $\sin \omega t = \cos[\omega t - (\pi/2)]$, $\sin(-\omega t) = -\sin \omega t$, $\cos(-\omega t) = \cos \omega t$ **Average value** $G = \text{algebraic sum of areas}/\text{length of curve}$

Effective (rms) value $I_{\text{rms}} = 0.707I_m$, $I_m = \sqrt{2}I_{\text{rms}}$, $I_{\text{rms}} = \sqrt{\text{area } [i(t)]^2/T}$

The Basic Elements and Phasors

R: $I_m = V_m/R$, in phase **L:** $X_L = \omega L$, v_L leads i_L by 90°
C: $X_C = 1/\omega C$, i_C leads v_C by 90° **Power** $P = (V_m I_m/2) \cos \theta = V_{\text{rms}} I_{\text{rms}} \cos \theta$ **R:** $P = V_{\text{rms}} I_{\text{rms}} = I_{\text{rms}}^2 R = V_{\text{rms}}^2 / R$ **Power factor** $F_p = \cos \theta = P/V_{\text{rms}} I_{\text{rms}}$ **Rectangular form** $C = A \pm jB$
Polar form $C = C \angle \theta$ **Conversions** $C = \sqrt{A^2 + B^2}$, $\theta = \tan^{-1}(B/A)$, $A = C \cos \theta$, $B = C \sin \theta$ **Operations** $j = \sqrt{-1}$, $j^2 = -1$, $1/j = -j$, $C_1 \pm C_2 = (\pm A_1 \pm A_2) + j(\pm B_1 \pm B_2)$, $C_1 \cdot C_2 = C_1 C_2 \angle (\theta_1 + \theta_2)$, $C_1/C_2 = (C_1/C_2) \angle (\theta_1 - \theta_2)$

Series and Parallel ac Circuits

Elements $R \angle 0^\circ$, $X_L \angle 90^\circ$, $X_C \angle -90^\circ$

Series $Z_T = Z_1 + Z_2 + Z_3 + \dots + Z_N$, $I_s = E/Z_T$, $F_p = R/Z_T$
Voltage divider rule $V_x = Z_x E/Z_T$ **Parallel** $Y_T = Y_1 + Y_2 + Y_3 + \dots + Y_N$, $Z_T = Z_1 Z_2 / (Z_1 + Z_2)$, $G \angle 0^\circ$, $B_L \angle -90^\circ$, $B_C \angle 90^\circ$, $F_p = \cos \theta_T = G/Y_T$ **Current divider rule** $I_1 = Z_2 I_T / (Z_1 + Z_2)$, $I_2 = Z_1 I_T / (Z_1 + Z_2)$ **Equivalent circuits** $R_s = R_p X_p^2 / (X_p^2 + R_p^2)$, $X_s = R_p^2 X_p / (X_p^2 + R_p^2)$, $R_p = (R_s^2 + X_s^2)/R_s$, $X_p = (R_s^2 + X_s^2)/X_s$

Series-Parallel ac Networks:

Employ block impedances and obtain general solution for reduced network. Then substitute numerical values. General approach similar to that for dc networks.

Methods of Analysis and Selected Topics (ac)

Source conversions $E = IZ_p$, $Z_s = Z_p$, $I = E/Z_s$ **Bridge networks** $Z_1/Z_3 = Z_2/Z_4$ **Δ-Y, Y-Δ conversions** See dc coverage, replacing R by Z .

Network Theorems

Review dc content on other side.

Thévenin's theorem (dependent sources) $E_{oc} = E_{Th}$, $Z_{Th} = E_{oc}/I_{sc}$, $Z_{Th} = E_g/I_g$ **Norton's theorem** (dependent sources) $I_{sc} = I_N$, $Z_N = E_{oc}/I_{sc}$, $Z_N = E_g/I_g$ **Maximum power transfer theorem** $Z_L = Z_{Th}$, $\theta_L = -\theta_{ThZ}$, $P_{\text{max}} = E_{Th}^2/4R_{Th}$

Power (ac)

R: $P = VI = V_m I_m/2 = I^2 R = V^2/R$ **Apparent power** $S = VI$, $P = S \cos \theta$, $F_p = \cos \theta = P/S$ **Reactive power** $Q = VI \sin \theta$
L: $Q_L = VI = I^2 X_L = V^2/X_L$, **C:** $Q_C = VI = I^2 X_C = V^2/X_C$, $S_T = \sqrt{P_T^2 + Q_T^2}$, $F_p = P_T/S_T$

Resonance

Series $X_L = X_C$, $f_s = 1/(2\pi\sqrt{LC})$, $Z_{T_s} = R$, $Q_L = X_L/R$, $Q_S = X_L/R = (1/R)\sqrt{L/C}$, $V_{L_s} = Q_S E$, $V_{C_s} = Q_S E$, $P_{\text{HPF}} = (1/2)P_{\text{max}}$, $f_1 = (1/2\pi)(-R/2L + (1/2)\sqrt{(R/L)^2 + 4/LC})$, f_2 (use $+R/2L$), $BW = f_2 - f_1 = R/2\pi L = f_s/Q_s$ **Parallel** $X_{L_p} = X_C$, $X_{C_p} = (R_l^2 + X_L^2)/X_L$, $f_p = [1/(2\pi\sqrt{LC})]\sqrt{1 - (R_l^2 C/L)}$, $Z_{T_p} = R_s \| R_p$, $R_p = (R_l^2 + X_L^2)/R_l$, $Q_p = (R_s \| R_p)X_{L_p}$, $BW = f_2 - f_1 = f_p/Q_p$ **Q ≥ 10:** $Z_{T_p} \cong R_s \| Q^2 R_l$, $X_{L_p} \cong X_L$, $X_L = X_C$, $f_p \cong 1/(2\pi\sqrt{LC})$, $Q_p = Q_L$, $I_L = I_C \cong QI_L$, $BW = f_p/Q_p = R_l/2\pi L$

Decibels, Filters, and Bode Plots

Logarithms $N = b^x$, $x = \log_b N$, $\log_b x = 2.3 \log_{10} x$, $\log_{10} ab = \log_{10} a + \log_{10} b$, $\log_{10} a/b = \log_{10} a - \log_{10} b$, $\log_{10} a^n = n \log_{10} a$, $\text{dB} = 10 \log_{10} P_2/P_1$, $\text{dB}_v = 20 \log_{10} V_2/V_1$

R-C filters (high-pass) $f_c = 1/(2\pi RC)$, $V_o/V_i = R/\sqrt{R^2 + X_C^2}$
 $\angle \tan^{-1}(X_C/R)$ (low-pass) $f_c = 1/(2\pi RC)$, $V_o/V_i = X_C/\sqrt{R^2 + X_C^2}$
 $\angle -\tan^{-1} \frac{R}{X_C}$

Octave 2 : 1, 6 dB/octave **Decade** 10 : 1, 20 dB/decade

Transformers

Mutual inductance $M = k\sqrt{L_p L_s}$ **Iron-core** $E_p = 4.44fN_p \Phi_m$, $E_s = 4.44fN_s \Phi_m$, $E_p/E_s = N_p/N_s$, $a = N_p/N_s$, $I_p/I_s = N_s/N_p$, $Z_p = a^2 Z_L$, $E_p I_p = E_s I_s$, $P_i = P_o$ (ideal)
Air-core $Z_i = Z_p + [\omega M]^2 / (Z_s + Z_L)$

Polyphase Systems

Y-Y system $I_{\phi_g} = I_L = I_{\phi_L}$, $V_\phi = E_\phi$, $E_L = \sqrt{3} V_\phi$ **Y-Δ system** $V_\phi = E_L$, $I_L = \sqrt{3} I_\phi$ **Δ-Δ system** $V_\phi = E_L = E_\phi$, $I_L = \sqrt{3} I_\phi$ **Δ-Y system** $E_L = \sqrt{3} V_\phi$, $I_\phi = I_L$, $E_L = E_\phi$ **Power** $P_T = 3P_\phi$, $Q_T = 3Q_\phi$, $S_T = 3S_\phi = \sqrt{3} E_L I_L$, $F_p = P_T/S_T$

Pulse Waveforms and the R-C Response

% tilt = $[(V_1 - V_2)/V] \times 100\%$ with $V = (V_1 + V_2)/2$

Pulse repetition frequency (prf) = $1/T$

Duty cycle = $(t_p/T) \times 100\%$

$V_{av} = (\text{duty cycle})(\text{peak value}) + (1 - \text{duty cycle}) \times (V_b)$

R-C circuits $v_C = V_i + (V_f - V_i)(1 - e^{-t/RC})$

Compensated attenuator $R_p C_p = R_s C_s$

Nonsinusoidal Circuits

Fourier series $f(\alpha) = A_0 + A_1 \sin \omega t + A_2 \sin 2\omega t + \dots + A_n \sin n\omega t + B_1 \cos \omega t + B_2 \cos 2\omega t + \dots + B_n \cos n\omega t$

Even function $f(\alpha) = f(-\alpha)$, no B_n terms **Odd function** $f(\alpha) = -f(-\alpha)$, no A_n terms, no odd harmonics if $f(t) = f[(T/2) + t]$, no even harmonics if $f(t) = -f[(T/2) + t]$

Effective (rms) value $V_{(\text{rms})} = \sqrt{V_0^2 + (V_{m_1}^2 + \dots + V_{m_n}^2 + V_{m_1}^2 + \dots + V_{m_n}^2)/2}$

Power $P_T = V_0 I_0 + V_1 I_1 \cos \theta + \dots + V_n I_n \cos \theta_n = I_{\text{rms}}^2 R = V_{\text{rms}}^2 / R$

Standard Resistor Values

Ohms (Ω)	Kilohms (kΩ)	Megohms (MΩ)
0.10	1.0	100
0.11	1.1	110
0.12	1.2	120
0.13	1.3	130
0.15	1.5	150
0.16	1.6	160
0.18	1.8	180
0.20	2.0	200
0.22	2.2	220
0.24	2.4	240
0.27	2.7	270
0.30	3.0	300
0.33	3.3	330
0.36	3.6	360
0.39	3.9	390
0.43	4.3	430
0.47	4.7	470
0.51	5.1	510
0.56	5.6	560
0.62	6.2	620
0.68	6.8	680
0.75	7.5	750
0.82	8.2	820
0.91	9.1	910