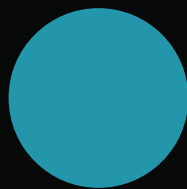


PEARSON NEW INTERNATIONAL EDITION



Digital Fundamentals
A Systems Approach
Thomas L. Floyd
First Edition

Pearson New International Edition

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A Systems Approach
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INTRODUCTION TO DIGITAL SYSTEMS

OUTLINE

- 1 Digital and Analog Signals and Systems
- 2 Binary Digits, Logic Levels, and Digital Waveforms
- 3 Logic Operations
- 4 Combinational and Sequential Logic Functions
- 5 Programmable Logic
- 6 Fixed-Function Logic Devices
- 7 A System
- 8 Measuring Instruments

OBJECTIVES

- Explain the basic differences between digital and analog quantities
- Show how voltage levels are used to represent digital quantities
- Describe various parameters of a pulse waveform such as rise time, fall time, pulse width, frequency, period, and duty cycle
- Explain the logic operations of NOT, AND, and OR
- Describe several types of logic functions
- Describe programmable logic, discuss the various types, and describe how PLDs are programmed using VHDL and Verilog with system software
- Describe the basics of a microcontroller
- Identify fixed-function digital integrated circuits according to their technology and the type of packaging

- Discuss how various logic functions are used in a digital system
- Recognize various instruments and understand how they are used in measurement and troubleshooting digital devices and systems

KEY TERMS

Key terms are in order of appearance in the chapter.

Analog	NOT
Digital	Inverter
Digital system	AND
Binary	OR
Bit	Programmable logic device
Pulse	SPLD
Duty cycle	CPLD
Clock	FPGA
Timing diagram	Compiler
Data	Microcontroller
Serial	Embedded system
Parallel	Integrated circuit (IC)
Logic	Fixed-function logic
Input	Troubleshooting
Output	
Gate	

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INTRODUCTION

The term *digital* is derived from the way operations are performed, by counting digits. For many years, applications of digital electronics were confined to computer systems. Today, digital technology is applied in a wide range of systems in addition to computers. Such applications as television, communications systems, radar, navigation and guidance systems, military systems, medical

instrumentation, industrial process control, and consumer electronics use digital techniques. Over the years digital technology has progressed from vacuum-tube circuits to fixed-function integrated circuits to programmable logic and embedded microcontrollers.

This chapter introduces you to digital electronics and provides a broad overview of many important concepts, applications, and methods.

1 DIGITAL AND ANALOG SIGNALS AND SYSTEMS

Electronic systems can be divided into two broad categories, **digital** and **analog**. **Digital** electronics involves quantities with discrete values, and **analog** electronics involves quantities with continuous values. Although you will be studying digital fundamentals in this text, you should also know something about analog because many applications require both; and interfacing between analog and digital is important.

After completing this section, you should be able to

- Define *analog*
- Define *digital*
- Explain the difference between digital and analog signals
- State the advantages of digital over analog
- Discuss modulation methods
- Describe two types of digital systems

An **analog*** quantity is one having continuous values. A **digital** quantity is one having a discrete set of values. Most things that can be measured quantitatively occur in nature in analog form. For example, the air temperature changes over a continuous range of values. During a given day, the temperature does not go from, say, 70° to 71° instantaneously; it takes on all the infinite values in between. If you graphed the temperature on a typical summer day, you would have a smooth, continuous curve similar to the curve in Figure 1. Other examples of analog quantities are time, pressure, distance, and sound.

Rather than graphing the temperature on a continuous basis, suppose you just take a temperature reading every hour. Now you have sampled values representing the temperature at discrete points in time (every hour) over a 24-hour period, as indicated in Figure 2. You have effectively converted an analog quantity to a form that can now be digitized by representing each sampled value by a digital code. It is important to realize that Figure 2 itself is not the digital representation of the analog quantity.

*The bold terms in color are key terms and are included in a Key Term glossary at the end of the chapter.

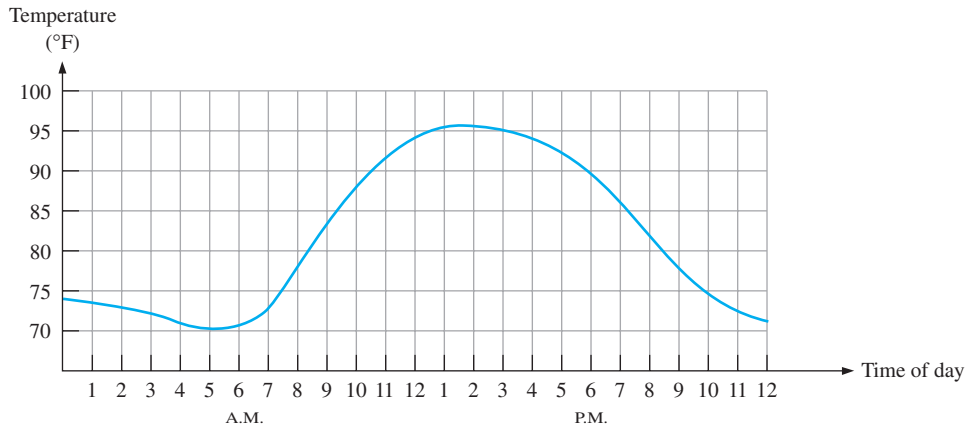


FIGURE 1 Graph of an analog quantity (temperature versus time).

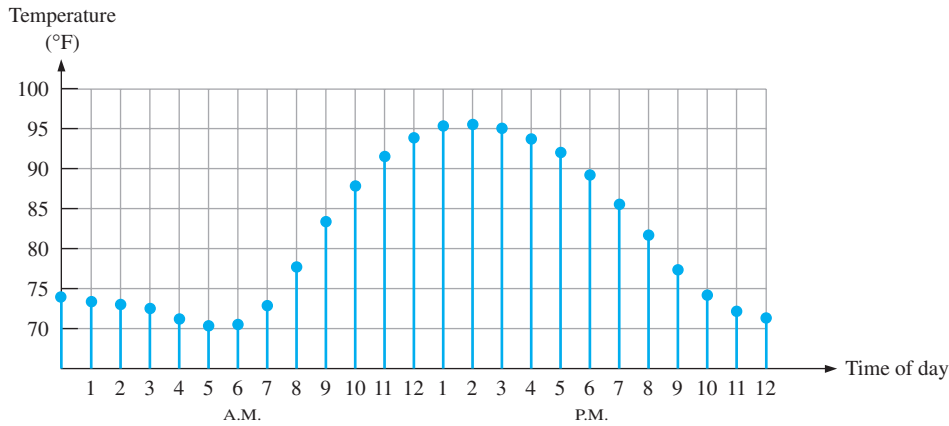


FIGURE 2 Sampled-value representation (quantization) of the analog quantity in Figure 1. Each value represented by a dot can be digitized by representing it as a digital code that consists of a series of 1s and 0s.

THE DIGITAL ADVANTAGE Digital representation has certain advantages over analog representation in electronics applications. For one thing, digital data can be processed and transmitted more efficiently and reliably than analog data. Also, digital data has a great advantage when storage is necessary. For example, music when converted to digital form can be stored more compactly and reproduced with greater accuracy and clarity than is possible when it is in analog form. Noise (unwanted voltage fluctuations) does not affect digital data nearly as much as it does analog signals.

Analog Signals

An analog quantity, such as voltage, that is repetitive or varies in a certain manner is an analog signal. An analog signal can be a repetitive waveform, such as the sine wave in Figure 3(a), or a continuously varying audio signal that carries information (music, the spoken word, or other sounds), as shown in part (b). Other examples of analog signals are amplitude-modulated signals (AM) and frequency-modulated signals (FM), as illustrated in parts (c) and (d). In AM, a lower-frequency information signal, such as voice, varies the amplitude of a high-frequency sine wave. In FM, the information signal varies the frequency of the sine wave.

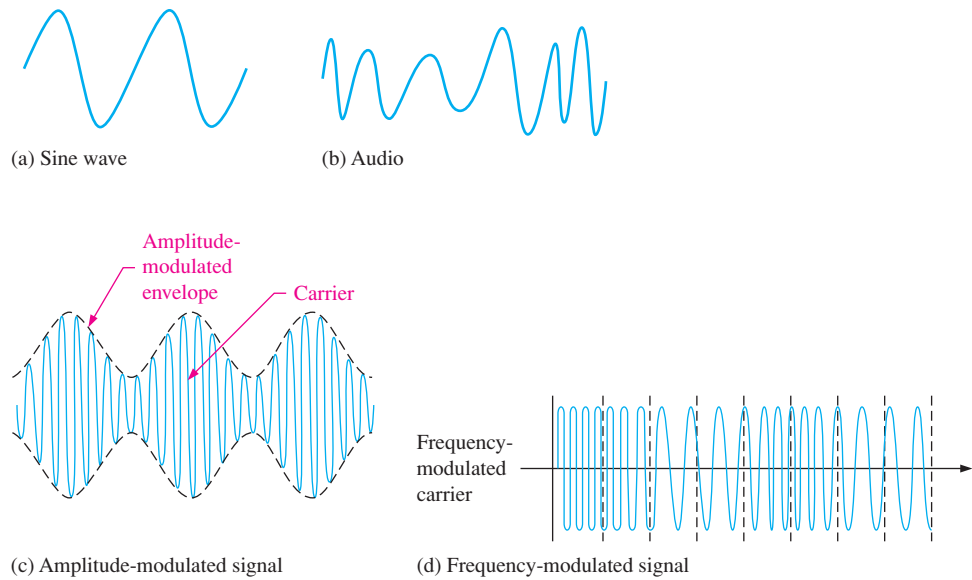


FIGURE 3 Examples of analog signals.

Digital Signals

A digital signal is a representation of a sequence of discrete values that are coded into a stream of 1s and 0s. A bit stream appears as a train of pulses or voltage levels where a high voltage level conveys a binary 1 and a low voltage level conveys a binary 0. Bit streams are used in telecommunications, computers, and other system applications. Figure 4 illustrates one type of digital signal. The duration of each bit (bit time) is indicated by the hash marks.

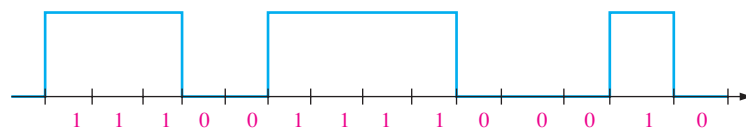


FIGURE 4 Example of a digital waveform.

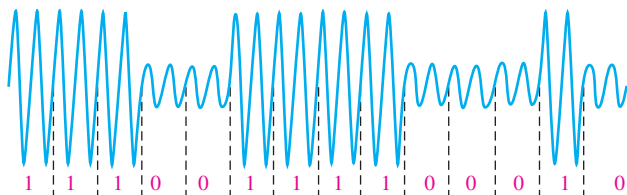


FIGURE 5 Example of a digital-modulated signal.

DIGITAL MODULATION In some applications, analog and digital signals are combined with a sine wave, called a *carrier*, by amplitude modulating the sine wave with the digital waveform. A common example is a modem that turns digital data from a computer into modulated signals in the voice frequency range for transmission over telephone lines. A digital-modulated signal is shown in Figure 5 where the digital signal (bit stream) in Figure 4 modulates the sine wave. Dashed lines mark the bit times. The frequency of the sine wave is shown arbitrarily low in relation to the digital-modulating signal for illustration.

PULSE-CODE MODULATION (PCM) A PCM signal represents sampled analog signals with a sequence of digital codes. It is used in computers for digital audio, in Blu-ray, compact disc and DVD formats, and in digital telephone systems. The sampling process results in a “stair-step” voltage as shown in Figure 6. The analog signal is sampled at each step, and each sampled value is converted (quantized) to a digital code. The

digital signal would be the time sequence of the digital codes where the binary numbers shown for each step appear in sequence beginning at the left. The more steps there are the more accurate is the digital representation. The length of the code depends on the number of steps.

Digital Systems

A **digital system** is an arrangement of the individual logic functions connected to perform a specified operation or produce a defined output. An example of a digital system is a computer, as shown in Figure 7 in basic block diagram form. A computer processes, transfers, and stores data in digital form (1s and 0s). To make a complete system, the computer is interfaced with peripheral devices such as a modem, a mouse, a keyboard, and a monitor.

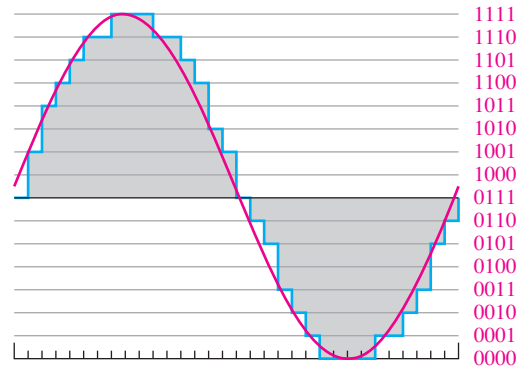


FIGURE 6 Illustration of pulse-code modulation.

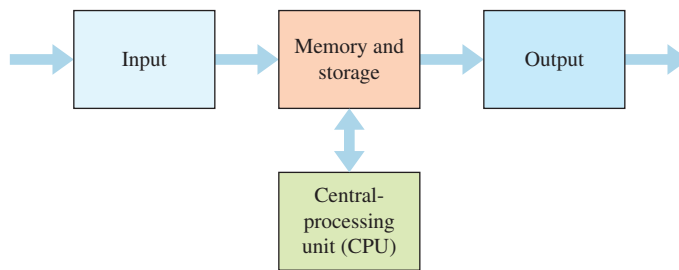


FIGURE 7 Basic block diagram of a computer.

Figure 8, another example of a digital system, shows the traffic light controller. All of the digital signals that the system uses to properly sequence the traffic light are internally generated, making the controller a type of finite state machine.

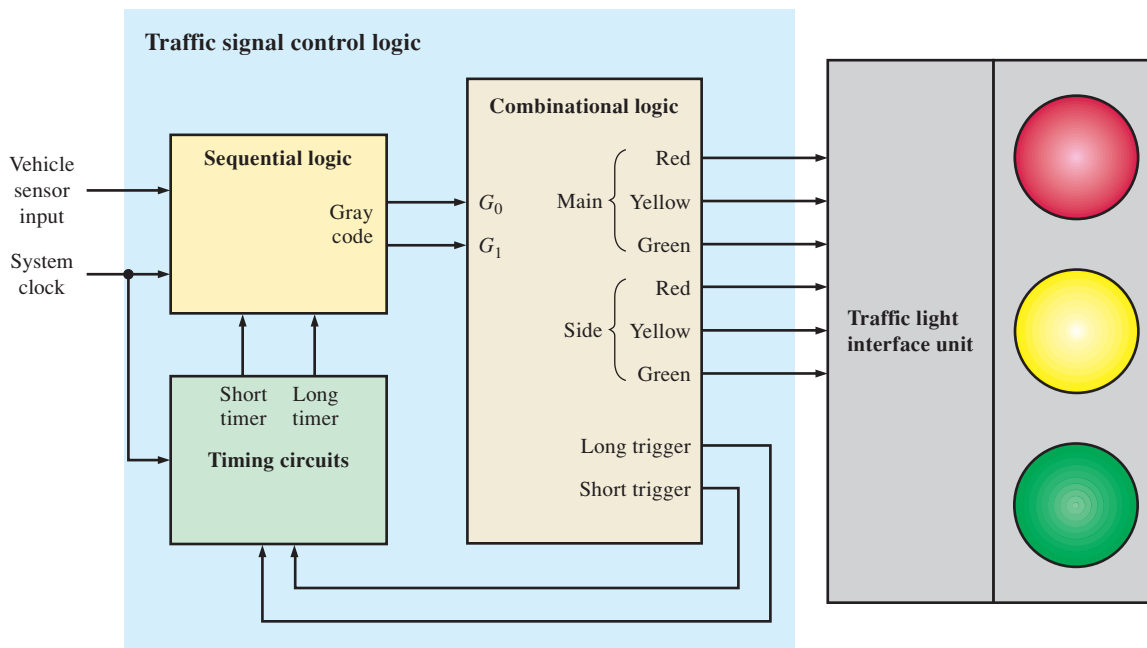


FIGURE 8 A digital traffic light controller.

Analog Systems

An **analog system** is one that processes data in analog form only. One example is a public address system, used to amplify sound so that it can be heard by a large audience. The basic diagram in Figure 9 illustrates that sound waves, which are analog in nature, are picked up by a microphone and converted to a small analog voltage called the audio signal. This voltage varies continuously as the volume and frequency of the sound changes and is applied to the input of a linear amplifier. The output of the amplifier, which is an increased reproduction of input voltage, goes to the speaker(s). The speaker changes the amplified audio signal back to sound waves that have a much greater volume than the original sound waves picked up by the microphone.

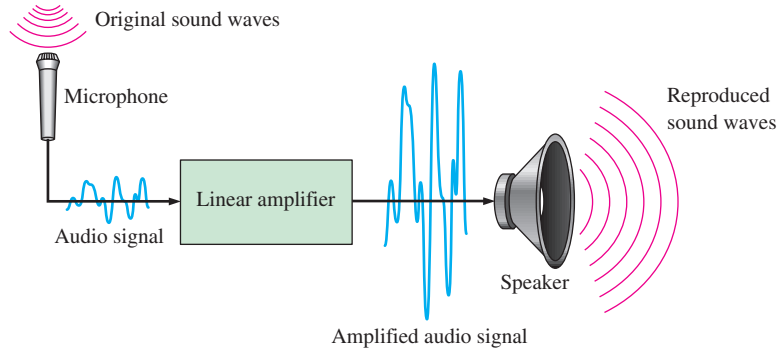


FIGURE 9 A basic audio public address system.

Another example of an analog system is the FM receiver. The system processes the incoming frequency-modulated carrier signal, extracts the audio signal for amplification, and produces audible sound waves. A block diagram is shown in Figure 10 with a representative signal shown at each point in the system.

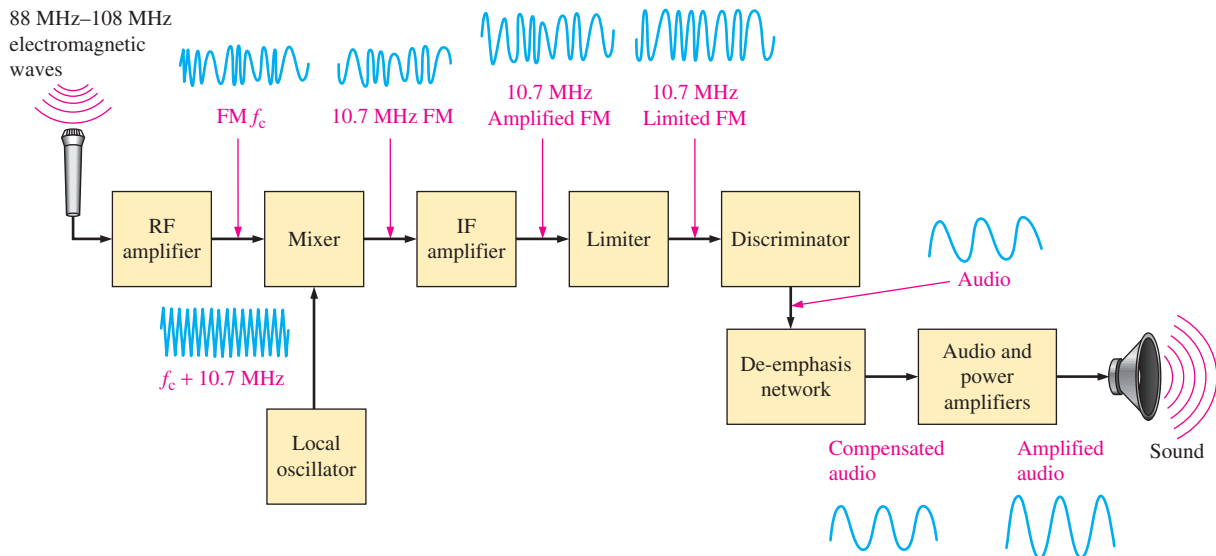


FIGURE 10 Block diagram of superheterodyne FM receiver.

A Combination Digital and Analog System

The compact disk (CD) player is an example of a system in which both digital and analog elements are used. The simplified block diagram in Figure 11 illustrates the basic system. Music in digital form is stored on the compact disk. A laser diode optical system picks up

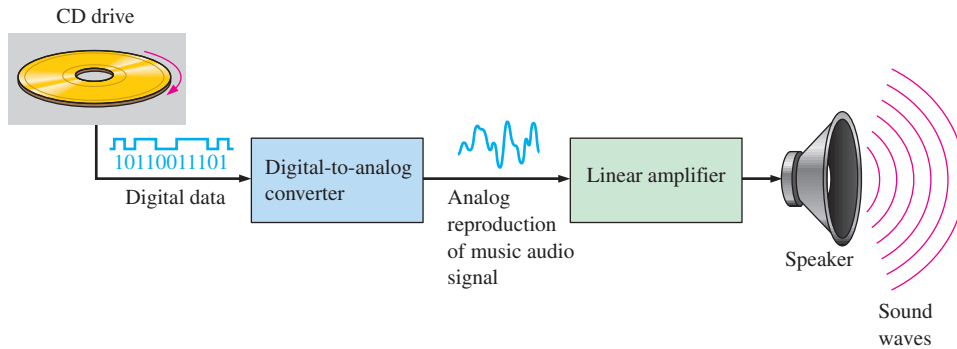


FIGURE 11 Simplified diagram of a compact disk player.

the digital data from the rotating disk and transfers it to the **digital-to-analog converter (DAC)**. The DAC changes the digital data into an analog signal that is an electrical reproduction of the original music. This signal is amplified and sent to the speaker for you to enjoy. When the music was originally recorded on the CD, a process, essentially the reverse of the one described here, using an **analog-to-digital converter (ADC)** was used.

SECTION 1 CHECKUP*

1. Define *analog*.
2. Define *digital*.
3. Explain the difference between a digital quantity and an analog quantity.
4. Give an example of a system that is analog and one that is a combination of both digital and analog. Name a system that is entirely digital.

*Answers are at the end of the chapter.

2 BINARY DIGITS, LOGIC LEVELS, AND DIGITAL WAVEFORMS

Digital systems involve operations in which there are only two possible states. These states are represented by two different voltage levels: A **HIGH** and a **LOW**. The two states can also be represented by current levels or pits and lands on a CD or DVD. In digital systems such as computers, combinations of the two states, called *codes*, are used to represent numbers, symbols, alphabetic characters, and other types of information. The two-state number system is called *binary*, and its two digits are 0 and 1. A binary digit is called a *bit*.

After completing this section, you should be able to

- Define *binary*
- Define *bit*
- Name the bits in a binary system
- Explain how voltage levels are used to represent bits
- Explain how voltage levels are interpreted by a digital circuit
- Describe the general characteristics of a pulse
- Determine the amplitude, rise time, fall time, and width of a pulse
- Identify and describe the characteristics of a digital waveform
- Determine the amplitude, period, frequency, and duty cycle of a digital waveform
- Explain what a timing diagram is and state its purpose
- Explain serial and parallel data transfer and state the advantage and disadvantage of each

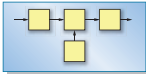
Binary Digits

Each of the two digits in the **binary** system, 1 and 0, is called a **bit**, which is a contraction of the words *binary digit*. In digital circuits, two different voltage levels are used to represent the two bits. Generally, 1 is represented by the higher voltage, which we will refer to as a HIGH, and a 0 is represented by the lower voltage level, which we will refer to as a LOW. This is called **positive logic**.

$$\text{HIGH} = 1 \quad \text{and} \quad \text{LOW} = 0$$

Another system in which a 1 is represented by a LOW and a 0 is represented by a HIGH is called *negative logic*.

Groups of bits (combinations of 1s and 0s), called *codes*, are used to represent numbers, letters, symbols, instructions, and anything else required in a given application.



The concept of a digital computer can be traced back to Charles Babbage, who developed a crude mechanical computation device in the 1830s. John Atanasoff was the first to apply electronic processing to digital computing in 1939. In 1946, an electronic digital computer called ENIAC was implemented with vacuum-tube circuits. Even though it took up an entire room, ENIAC didn't have the computing power of your handheld calculator.

SYSTEM NOTE

Logic Levels

The voltages used to represent a 1 and a 0 are called *logic levels*. Ideally, one voltage level represents a HIGH and another voltage level represents a LOW. In a practical digital circuit, however, a HIGH can be any voltage between a specified minimum value and a specified maximum value. Likewise, a LOW can be any voltage between a specified minimum and a specified maximum. There can be no overlap between the accepted range of HIGH levels and the accepted range of LOW levels.

Figure 12 illustrates the general range of LOWs and HIGHs for a digital circuit. The variable $V_{H(\max)}$ represents the maximum HIGH voltage value, and $V_{H(\min)}$ represents the minimum HIGH voltage value. The maximum LOW voltage value is represented by $V_{L(\max)}$, and the minimum LOW voltage value is represented by $V_{L(\min)}$. The voltage values between $V_{L(\max)}$ and $V_{H(\min)}$ are unacceptable for proper operation. A voltage in the unacceptable range can appear as either a HIGH or a LOW to a given circuit. For example, the HIGH input values for a certain type of digital circuit technology called CMOS may range from 2 V to 3.3 V and the LOW input values may range from 0 V to 0.8 V. If a voltage of 2.5 V is applied, the circuit will accept it as a HIGH or binary 1. If a voltage of 0.5 V is applied, the circuit will accept it as a LOW or binary 0. For this type of circuit, voltages between 0.8 V and 2 V are unacceptable.

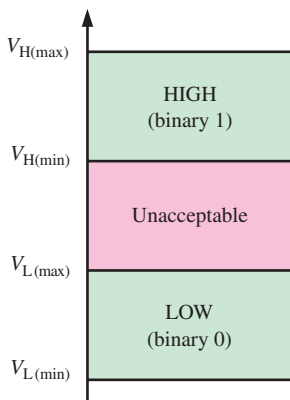


FIGURE 12 Logic level ranges of voltage for a digital circuit.

Digital Waveforms

Digital waveforms consist of voltage levels that are changing back and forth between the HIGH and LOW levels or states. Figure 13(a) shows that a single positive-going **pulse** is generated when the voltage (or current) goes from its normally LOW level to its HIGH level and then back to its LOW level. The negative-going pulse in Figure 13(b) is generated when the voltage goes from its normally HIGH level to its LOW level and back to its HIGH level. A digital waveform is made up of a series of pulses.

THE PULSE As indicated in Figure 13, a pulse has two edges: a **leading edge** that occurs first at time t_0 and a **trailing edge** that occurs last at time t_1 . For a positive-going pulse, the leading edge is a rising edge, and the trailing edge is a falling edge. The pulses

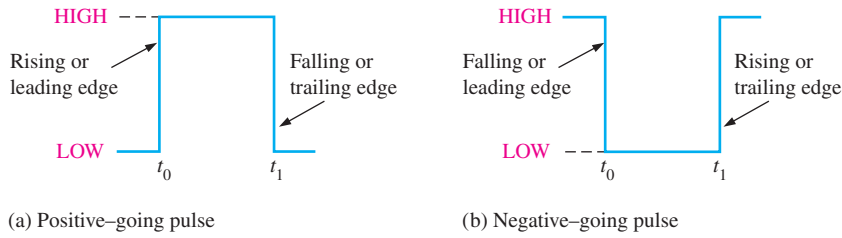


FIGURE 13 Ideal pulses.

in Figure 13 are ideal because the rising and falling edges are assumed to change in zero time (instantaneously). In practice, these transitions never occur instantaneously, although for most digital work you can assume ideal pulses.

Figure 14 shows a nonideal pulse. In reality, all pulses exhibit some or all of these characteristics. The overshoot and ringing are sometimes produced by stray inductive and capacitive effects. The droop can be caused by stray capacitance and circuit resistance, forming an RC circuit with a low time constant.

The time required for a pulse to go from its LOW level to its HIGH level is called the **rise time** (t_r), and the time required for the transition from the HIGH level to the LOW level is called the **fall time** (t_f). In practice, it is common to measure rise time from 10% of the pulse **amplitude** (height from baseline) to 90% of the pulse amplitude and to measure the fall time from 90% to 10% of the pulse amplitude, as indicated in Figure 14. The bottom 10% and the top 10% of the pulse are not included in the rise and fall times because of the nonlinearities in the waveform in these areas. The **pulse width** (t_{pw}) is a measure of the duration of the pulse and is often defined as the time interval between the 50% points on the rising and falling edges, as indicated in Figure 14.

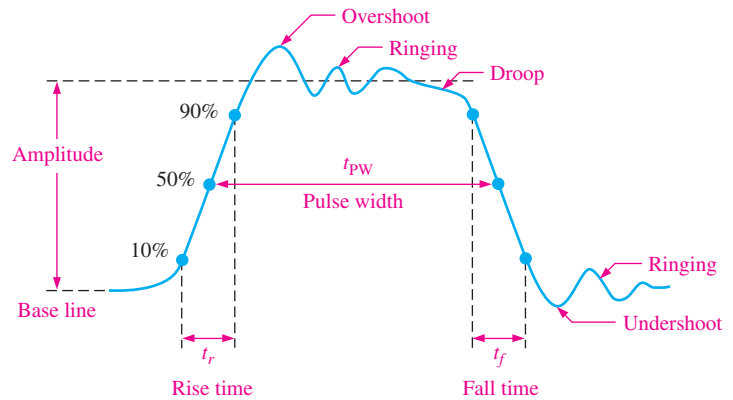


FIGURE 14 Nonideal pulse characteristics.

WAVEFORM CHARACTERISTICS Most waveforms encountered in digital systems are composed of series of pulses, sometimes called *pulse trains*, and can be classified as either periodic or nonperiodic. A **periodic** pulse waveform is one that repeats itself at a fixed interval, called a **period** (T). The **frequency** (f) is the rate at which it repeats itself and is measured in hertz (Hz). A nonperiodic pulse waveform, of course, does not repeat itself at fixed intervals and may be composed of pulses of randomly differing pulse widths and/or randomly differing time intervals between the pulses. An example of each type is shown in Figure 15.

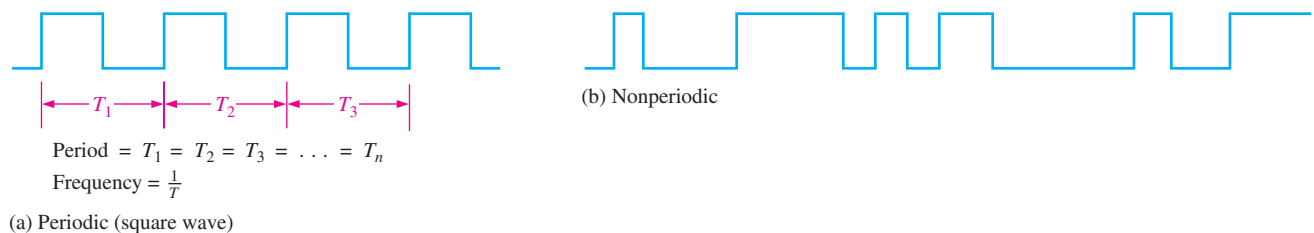


FIGURE 15 Examples of digital waveforms.

The frequency (f) of a pulse (digital) waveform is the reciprocal of the period. The relationship between frequency and period is expressed as follows:

$$f = \frac{1}{T} \quad (1)$$

$$T = \frac{1}{f} \quad (2)$$

An important characteristic of a periodic digital waveform is its **duty cycle**, which is the ratio of the pulse width (t_{PW}) to the period (T). It can be expressed as a percentage.

$$\text{Duty cycle} = \left(\frac{t_{PW}}{T} \right) 100\% \quad (3)$$

EXAMPLE 1

A portion of a periodic digital waveform is shown in Figure 16. The measurements are in milliseconds. Determine the following:

- (a) period (b) frequency (c) duty cycle

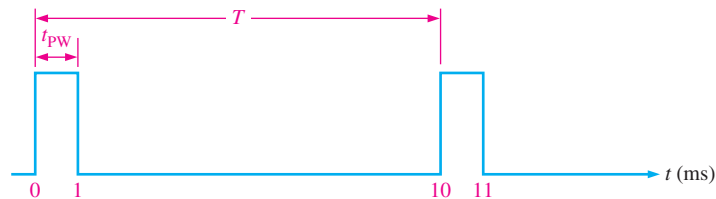


FIGURE 16

SOLUTION

- (a) The period is measured from the edge of one pulse to the corresponding edge of the next pulse. In this case T is measured from leading edge to leading edge, as indicated. T equals **10 ms**.

(b) $f = \frac{1}{T} = \frac{1}{10 \text{ ms}} = \mathbf{100 \text{ Hz}}$

(c) Duty cycle = $\left(\frac{t_{PW}}{T} \right) 100\% = \left(\frac{1 \text{ ms}}{10 \text{ ms}} \right) 100\% = \mathbf{10\%}$

RELATED PROBLEM*

A periodic digital waveform has a pulse width of $25 \mu\text{s}$ and a period of $150 \mu\text{s}$. Determine the frequency and the duty cycle.

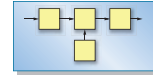
*Answers are at the end of the chapter.

A Digital Waveform Carries Binary Information

Binary information that is handled by digital systems appears as waveforms that represent sequences of bits. When the waveform is HIGH, a binary 1 is present; when the waveform is LOW, a binary 0 is present. Each bit in a sequence occupies a defined time interval called a **bit time**.

The speed at which a computer can operate depends on the type of microprocessor used in the system. The speed specification, for example 3.5 GHz, of a computer is the maximum clock frequency at which the microprocessor can run.

SYSTEM NOTE



THE CLOCK In digital systems, all waveforms are synchronized with a basic timing waveform called the **clock**. The clock is a periodic waveform in which each interval between pulses (the period) equals the time for one bit.

An example of a clock waveform is shown in Figure 17. Notice that, in this case, each change in level of waveform *A* occurs at the leading edge of the clock waveform. In other cases, level changes occur at the trailing edge of the clock. During each bit time of the clock, waveform *A* is either HIGH or LOW. These HIGHS and LOWs represent a sequence of bits as indicated. A group of several bits can be used as a piece of binary information, such as a number or a letter. The clock waveform itself does not carry information.

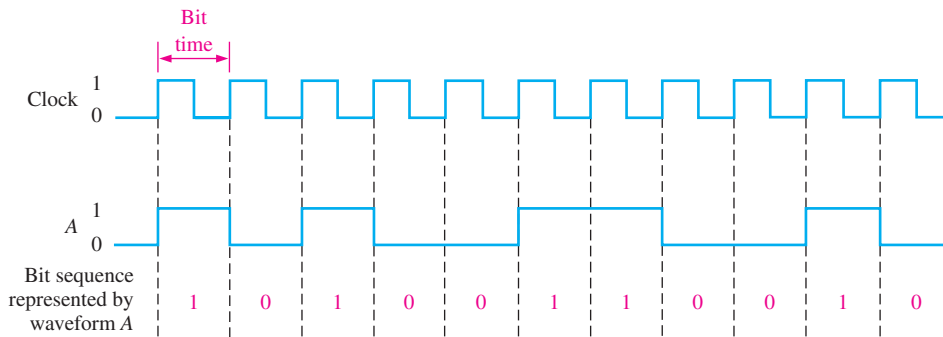


FIGURE 17 Example of a clock waveform synchronized with a waveform representation of a sequence of bits.

TIMING DIAGRAMS A **timing diagram** is a graph of digital waveforms showing the actual time relationship of two or more waveforms and how each waveform changes in relation to the others. By looking at a timing diagram, you can determine the states (HIGH or LOW) of all the waveforms at any specified point in time and the exact time that a waveform changes state relative to the other waveforms. Figure 18 is an example of a timing diagram made up of four waveforms. From this timing diagram you can see, for example, that the three waveforms *A*, *B*, and *C* are HIGH only during bit time 7 (shaded area) and they all change back LOW at the end of bit time 7.

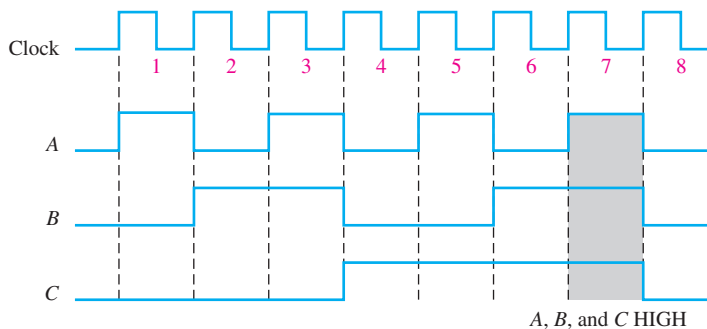


FIGURE 18 Example of a timing diagram.

Data Transfer

Data refers to groups of bits that convey some type of information. Binary data, which are represented by digital waveforms, must be transferred from one circuit to another within a digital system or from one system to another in order to accomplish a given purpose. For example, numbers stored in binary form in the memory of a computer must be transferred to the computer's central processing unit in order to be added. The sum of the addition must then be transferred to a monitor for display and/or transferred back to the memory. In computer systems, as illustrated in Figure 19, binary data are transferred in two ways: serial and parallel.

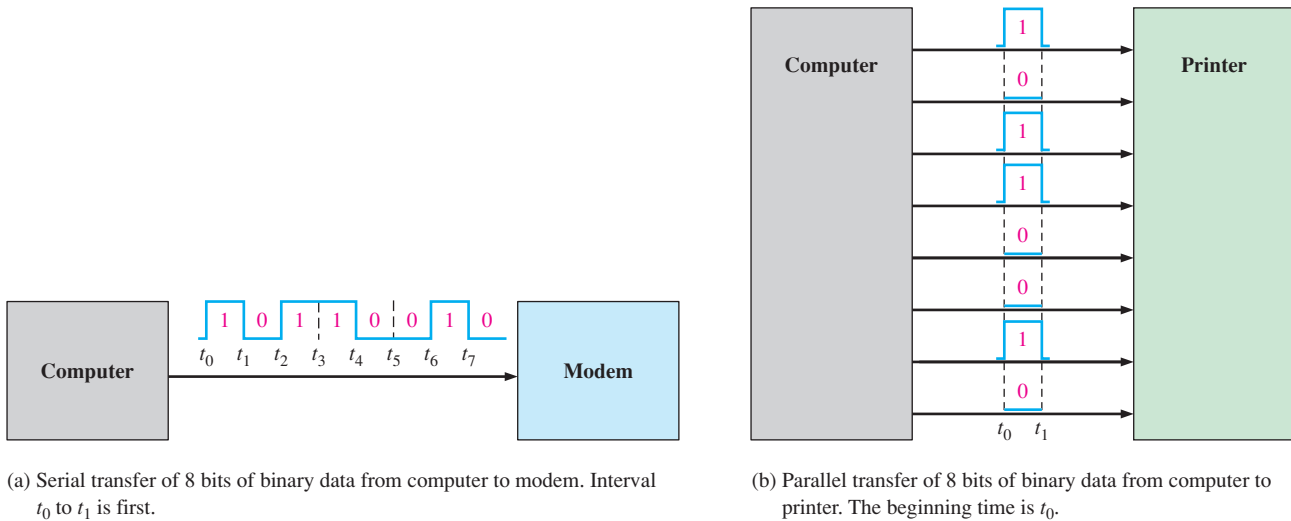
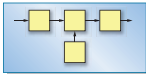


FIGURE 19 Illustration of serial and parallel transfer of binary data. Only the data lines are shown.

When bits are transferred in **serial** form from one point to another, they are sent one bit at a time along a single line, as illustrated in Figure 19(a) for the case of a computer-to-modem transfer. During the time interval from t_0 to t_1 , the first bit is transferred. During the time interval from t_1 to t_2 , the second bit is transferred, and so on. To transfer eight bits in series, it takes eight time intervals.

Universal Serial Bus (USB) is a serial bus standard for device interfacing. It was originally developed for the personal computer but has become widely used on many types of handheld and mobile devices. USB is expected to replace other serial and parallel ports. USB operated at 12 Mbps (million bits per second) when first introduced in 1995, but it now operates at up to 5 Gbps.



SYSTEM NOTE

When bits are transferred in **parallel** form, all the bits in a group are sent out on separate lines at the same time. There is one line for each bit, as shown in Figure 19(b) for the example of eight bits being transferred from a computer to a printer or other device. To transfer eight bits in parallel, it takes one time interval compared to eight time intervals for the serial transfer.

To summarize, an advantage of serial transfer of binary data is that a minimum of only one line is required. In parallel transfer, a number of lines equal to the number of bits to be transferred at one time is required. A disadvantage of serial transfer is that it can take longer to transfer a given number of bits than with parallel transfer at the same clock frequency. For example, if one bit can be transferred in $1 \mu s$, then it takes $8 \mu s$ to serially transfer eight bits but only $1 \mu s$ to parallel transfer eight bits. A disadvantage of parallel transfer is that it takes more lines than serial transfer.

EXAMPLE 2

- (a) Determine the total time required to serially transfer the eight bits contained in waveform A of Figure 20, and indicate the sequence of bits. The left-most bit is the first to be transferred. The 1 MHz clock is used as reference.
- (b) What is the total time to transfer the same eight bits in parallel?

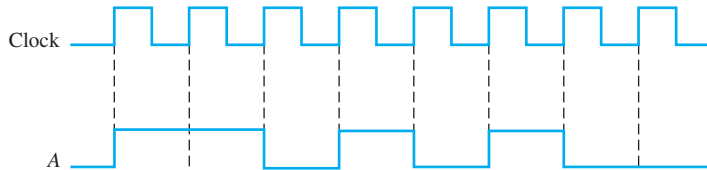


FIGURE 20

SOLUTION

- (a) Since the frequency of the clock is 1 MHz, the period is

$$T = \frac{1}{f} = \frac{1}{1 \text{ MHz}} = 1 \mu\text{s}$$

It takes $1 \mu\text{s}$ to transfer each bit in the waveform. The total transfer time for 8 bits is

$$8 \times 1 \mu\text{s} = \mathbf{8 \mu\text{s}}$$

To determine the sequence of bits, examine the waveform in Figure 20 during each bit time. If waveform A is HIGH during the bit time, a 1 is transferred. If waveform A is LOW during the bit time, a 0 is transferred. The bit sequence is illustrated in Figure 21. The left-most bit is the first to be transferred.



FIGURE 21

- (b) A parallel transfer would take $1 \mu\text{s}$ for all eight bits.

RELATED PROBLEM

If binary data are transferred on a USB at the rate of 480 million bits per second (480 Mbps), how long will it take to serially transfer 16 bits?

SECTION 2 CHECKUP

1. Define *binary*.
2. What does *bit* mean?
3. What are the bits in a binary system?
4. How are the rise time and fall time of a pulse measured?
5. Knowing the period of a waveform, how do you find the frequency?
6. Explain what a clock waveform is.
7. What is the purpose of a timing diagram?
8. What is the main advantage of parallel transfer over serial transfer of binary data?

3 LOGIC OPERATIONS

In its basic form, logic is the realm of human reasoning that tells you a certain proposition (declarative statement) is true if certain conditions are true. Propositions can be classified as true or false. Many situations and processes that you encounter in your daily life can be expressed in the form of propositional, or logic, functions. Since such functions are true/false or yes/no statements, digital circuits with their two-state characteristics are applicable.

After completing this section, you should be able to

- List three basic logic operations
- Define the NOT operation
- Define the AND operation
- Define the OR operation

Several propositions, when combined, form propositional, or logic, functions. For example, the propositional statement “The light is on” will be true if “The bulb is not burned out” is true and if “The switch is on” is true. Therefore, this logical statement can be made: *The light is on only if the bulb is not burned out and the switch is on.* In this example the first statement is true only if the last two statements are true. The first statement (“The light is on”) is then the basic proposition, and the other two statements are the conditions on which the proposition depends.

In the 1850s, the Irish logician and mathematician George Boole developed a mathematical system for formulating logic statements with symbols so that problems can be written and solved in a manner similar to ordinary algebra. Boolean algebra, as it is known today, is applied in the design and analysis of digital system.

The term **logic** is applied to digital circuits used to implement logic functions. Several kinds of digital logic **circuits** are the basic elements that form the building blocks for such complex digital systems as the computer. We will now look at these elements and discuss their functions in a very general way.

Three basic logic operations (NOT, AND, and OR) are indicated by standard distinctive shape symbols in Figure 22. The lines connected to each symbol are the **inputs** and **outputs**. The inputs are on the left of each symbol and the output is on the right. A circuit that performs a specified logic operation (AND, OR) is called a logic **gate**. AND and OR gates can have any number of inputs, as indicated by the dashes in the figure.

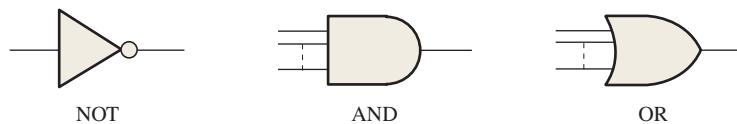


FIGURE 22 The basic logic operations and symbols.

In logic operations, the true/false conditions mentioned earlier are represented by a HIGH (true) and a LOW (false). Each of the three basic logic operations produces a unique response to a given set of conditions.

NOT

The **NOT** operation changes one logic level to the opposite logic level, as indicated in Figure 23. When the input is HIGH (1), the output is LOW (0). When the input is LOW,



FIGURE 23 The NOT operation.

the output is HIGH. In either case, the output is *not* the same as the input. The NOT operation is implemented by a logic circuit known as an **inverter**.

AND

The **AND** operation produces a HIGH output only when all the inputs are HIGH, as indicated in Figure 24 for the case of two inputs. When one input is HIGH *and* the other input is HIGH, the output is HIGH. When any or all inputs are LOW, the output is LOW. The AND operation is implemented by a logic circuit known as an *AND gate*.

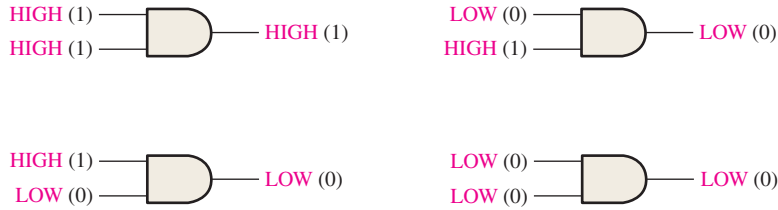


FIGURE 24 The AND operation.

OR

The **OR** operation produces a HIGH output when one or more inputs are HIGH, as indicated in Figure 25 for the case of two inputs. When one input is HIGH *or* the other input is HIGH *or* both inputs are HIGH, the output is HIGH. When both inputs are LOW, the output is LOW. The OR operation is implemented by a logic circuit known as an *OR gate*.

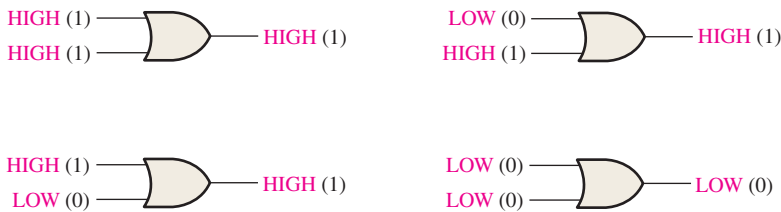


FIGURE 25 The OR operation.

SECTION 3 CHECKUP

1. When does the NOT operation produce a HIGH output?
2. When does the AND operation produce a HIGH output?
3. When does the OR operation produce a HIGH output?
4. What is an inverter?
5. What is a logic gate?

4 COMBINATIONAL AND SEQUENTIAL LOGIC FUNCTIONS

The three basic logic elements AND, OR, and NOT can be combined to form various types of logic functions: comparison, arithmetic, code conversion, encoding, decoding, data selection, counting, and storage. This section provides an overview of important logic functions and illustrates how they can be used in a specific system.

After completing this section, you should be able to

- List several types of logic functions
- Describe comparison and list the four arithmetic functions
- Describe code conversion, encoding, and decoding
- Describe multiplexing and demultiplexing
- Describe the counting function
- Describe the storage function

The Comparison Function

Magnitude comparison is performed by a logic circuit called a **comparator**. A comparator compares two quantities and indicates whether or not they are equal. For example, suppose you have two numbers and wish to know if they are equal or not equal and, if not equal, which is greater. The comparison function is represented in Figure 26. One number in binary form (represented by logic levels) is applied to input A , and the other number in binary form (represented by logic levels) is applied to input B . The outputs indicate the relationship of the two numbers by producing a HIGH level on the proper output line. Suppose that a binary representation of the number 2 is applied to input A and a binary representation of the number 5 is applied to input B . A HIGH level will appear on the $A < B$ (A is less than B) output, indicating the relationship between the two numbers (2 is less than 5). The wide arrows represent a group of parallel lines on which the bits are transferred.

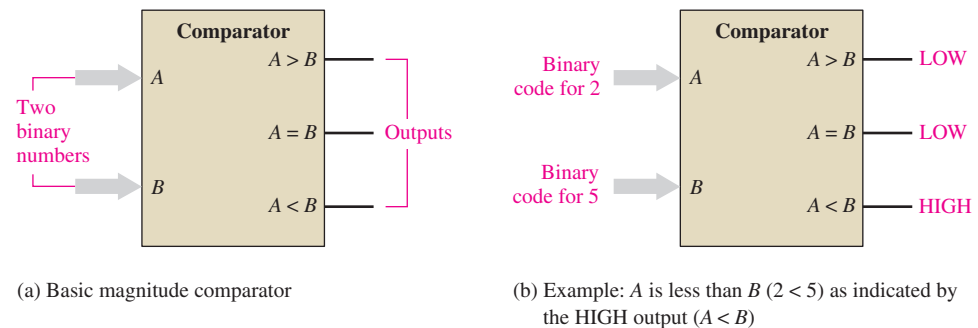


FIGURE 26 The comparison function.

The Arithmetic Functions

ADDITION Addition is performed by a logic circuit called an **adder**. An adder adds two binary numbers (on inputs A and B) with a carry input C_{in} and generates a sum (Σ) and a carry output (C_{out}), as shown in Figure 27(a). Figure 27(b) illustrates the addition of 3 and 9. You know that the sum is 12; the adder indicates this result by producing the code for 2 on the sum output and 1 on the carry output. Assume that the carry input in this example is 0.

SUBTRACTION Subtraction is also performed by a logic circuit. A **subtractor** requires three inputs: the two numbers that are to be subtracted and a borrow input. The

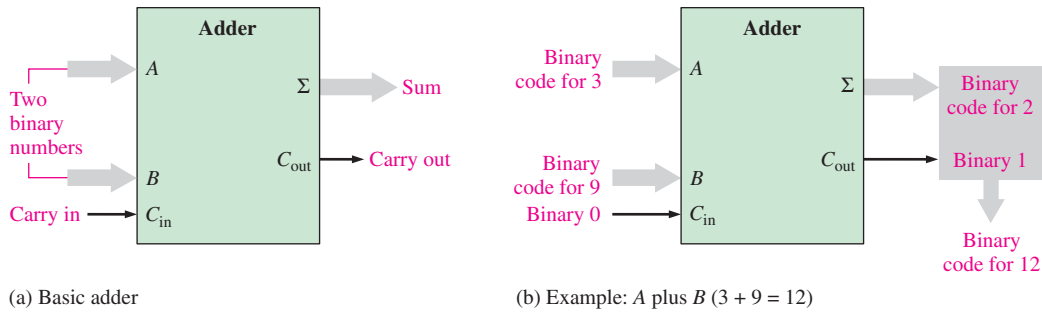


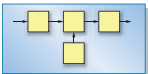
FIGURE 27 The addition function.

two outputs are the difference and the borrow output. When, for instance, 5 is subtracted from 8 with no borrow input, the difference is 3 with no borrow output.

MULTIPLICATION Multiplication is performed by a logic circuit called a *multiplier*. Numbers are always multiplied two at a time, so two inputs are required. The output of the multiplier is the product. Because multiplication is simply a series of additions with shifts in the positions of the partial products, it can be performed by using an adder in conjunction with other circuits.

In a microprocessor, the arithmetic logic unit (ALU) performs the operations of add, subtract, multiply, and divide as well as the logic operations on digital data as directed by a series of instructions. A typical ALU is constructed of many thousands of logic gates.

SYSTEM NOTE



DIVISION Division can be performed with a series of subtractions, comparisons, and shifts, and thus it can also be done using an adder in conjunction with other circuits. Two inputs to the divider are required, and the outputs generated are the quotient and the remainder.

The Code Conversion Function

A **code** is a set of bits arranged in a unique pattern and used to represent specified information. A code converter changes one form of coded information into another coded form. Examples are conversion between binary and other codes such as the binary coded decimal (BCD) and the Gray code.

The Encoding Function

The encoding function is performed by a logic circuit called an **encoder**. The encoder converts information, such as a decimal number or an alphabetic character, into some coded form. For example, one certain type of encoder converts each of the decimal digits, 0 through 9, to a binary code. A HIGH level on the input corresponding to a specific decimal digit produces logic levels that represent the proper binary code on the output lines.

Figure 28 is a simple illustration of an encoder used to convert (encode) a calculator keystroke into a binary code that can be processed by the calculator circuits.

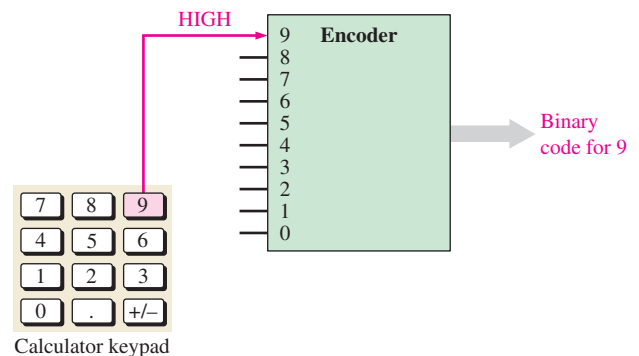


FIGURE 28 A calculator keystroke encoded into a binary code for processing by the calculator system.

The Decoding Function

The decoding function is performed by a logic circuit called a **decoder**. The decoder converts coded information, such as a binary number, into a noncoded form, such as a decimal form. For example, one particular type of decoder converts a 4-bit binary code into the appropriate decimal digit.

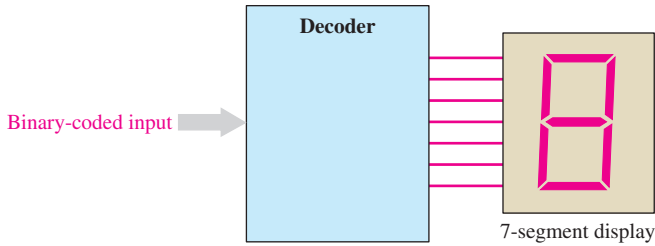


FIGURE 29 A decoder used to convert a special binary code into a 7-segment decimal readout.

Figure 29 is a simple illustration of one type of decoder that is used to activate a 7-segment display. Each of the seven segments of the display is connected to an output line from the decoder. When a particular binary code appears on the decoder inputs, the appropriate output lines are activated and light the proper segments to display the decimal digit corresponding to the binary code.

The Data Selection Function

Two types of circuits that select data are the multiplexer and the demultiplexer. The **multi-plexer**, or mux for short, is a logic circuit that switches digital data from several input lines onto a single output line in a specified time sequence. Functionally, a multiplexer can be represented by an electronic switch operation that sequentially connects each of the input lines to the output line. The **demultiplexer** (demux) is a logic circuit that switches digital data from one input line to several output lines in a specified time sequence. Essentially, the demux is a mux in reverse.

Multiplexing and demultiplexing are used when data from several sources are to be transmitted over one line to a distant location and redistributed to several destinations. Figure 30 illustrates this type of application where digital data from three sources are sent out along a single line to three terminals at another location.

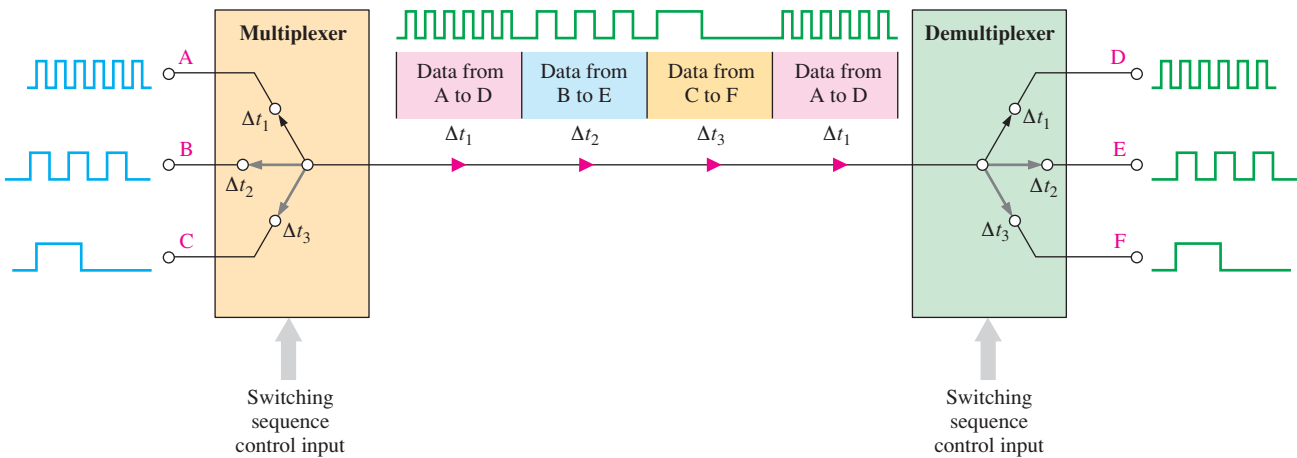


FIGURE 30 Illustration of a basic multiplexing/demultiplexing application.

In Figure 30, data from input A are connected to the output line during time interval Δt_1 and transmitted to the demultiplexer that connects them to output D. Then, during interval Δt_2 , the multiplexer switches to input B and the demultiplexer switches to output E. During interval Δt_3 , the multiplexer switches to input C and the demultiplexer switches to output F.

To summarize, during the first time interval, input A data go to output D. During the second time interval, input B data go to output E. During the third time interval, input C data go to output F. After this, the sequence repeats. Because the time is divided up among

several sources and destinations where each has its turn to send and receive data, this process is called *time division multiplexing* (TDM).

The Memory and Storage Functions

Memory and **storage** are functions that are required in most digital systems, and their purpose is to retain binary data for a period of time. Generally, *memory* refers to relatively short-term data retention, and *storage* refers to long-term data retention. A storage device can “memorize” a bit or a group of bits and retain the information as long as necessary. Memories include flip-flops, registers, and semiconductor memory. Storage includes magnetic disks (hard drives), optical disks (CDs), and magnetic tape.

FLIP-FLOPS A **flip-flop** is a bistable (two stable states) logic circuit that can store only one bit at a time, either a 1 or a 0. The output of a flip-flop indicates which bit it is storing. A HIGH output indicates that a 1 is stored and a LOW output indicates that a 0 is stored. Flip-flops are implemented with logic gates.

REGISTERS A **register** is formed by combining several flip-flops so that groups of bits can be stored. For example, an 8-bit register is constructed from eight flip-flops. In addition to storing bits, registers can be used to shift the bits from one position to another within the register or out of the register to another circuit; therefore, these devices are known as *shift registers*.

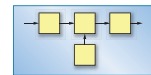
The two basic types of shift registers are serial and parallel. The bits are stored in a serial shift register one at a time. A good analogy to the serial shift register is loading passengers onto a bus single file through the door. They also exit the bus single file. The bits are stored in a parallel register simultaneously from parallel lines. For this case, a good analogy is loading and unloading passengers on a roller coaster where they enter all of the cars in parallel and exit in parallel.

SEMICONDUCTOR MEMORIES Semiconductor memories are devices typically used for storing large numbers of bits. In one type of memory, called the *read-only memory* or ROM, the binary data are permanently or semipermanently stored and cannot be readily changed. In the *random-access memory* or RAM, the binary data are temporarily stored and can be easily changed.

MAGNETIC MEMORIES Magnetic disk memories are used for mass storage of binary data. An example is the computer’s internal hard disk. Magneto-optical disks use laser beams to store and retrieve data. Magnetic tape is still used in memory applications and for backing up data from other storage devices.

The internal computer memories, RAM and ROM, as well as the smaller caches are semiconductor memories. The registers in a microprocessor are constructed of semiconductor flip-flops. Opto-magnetic disk memories are used in the internal hard drive and for the CD-ROM.

SYSTEM NOTE



The Counting Function

A **counter** is a sequential device and is a type of state machine because it has a unique internal sequence of states. The counting function is important in digital systems. There are many types of digital counters, but their basic purpose is to count events or to generate sequences represented by changing levels or pulses. To count, the counter must “remember” the present number so that it can go to the next proper number in sequence. Therefore, storage capability is an important characteristic of all counters, and flip-flops are generally used to implement them. Figure 31 illustrates the basic idea of counter operation.

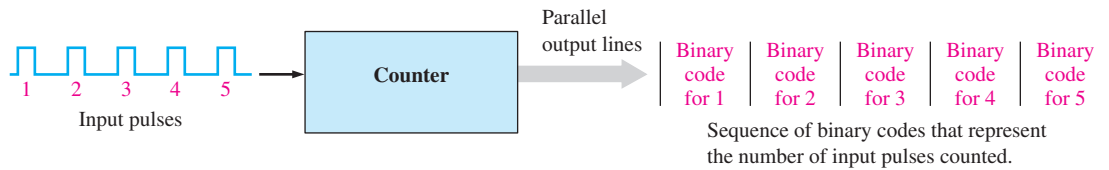


FIGURE 31 Illustration of basic counter operation.

SECTION 4 CHECKUP

1. What does a comparator do?
2. What are the four basic arithmetic operations?
3. Describe encoding and give an example.
4. Describe decoding and give an example.
5. Explain the basic purpose of multiplexing and demultiplexing.
6. Name four types of memory and storage devices.
7. What does a counter do?

5 PROGRAMMABLE LOGIC

A **programmable logic device (PLD)** is a type of integrated circuit (IC) that starts as a “blank slate” and into which a logic design is programmed. Programmable logic requires both hardware and software. PLDs can be programmed to perform specified logic functions by the manufacturer or by the user. One advantage of programmable logic over fixed-function logic is that the devices use much less board space for an equivalent amount of logic. Another advantage is that, with programmable logic, designs can be readily changed without rewiring or replacing components. Also, a logic design can generally be implemented faster and with less cost with programmable logic than with fixed-function ICs.

After completing this section, you should be able to

- State the major types of programmable logic and discuss the differences
- Discuss methods of programming
- List the major programming languages used for programmable logic
- Discuss the programmable logic design process

Types of Programmable Logic Devices (PLDs)

Many types of programmable logic devices are available, ranging from small devices that can replace a few fixed-function devices to complex high-density devices that can replace thousands of fixed-function devices. Two major categories of user-programmable logic are **PLD** (programmable logic device) and **FPGA** (field-programmable gate array), as indicated in Figure 32. PLDs are either SPLDs (simple PLDs) or CPLDs (complex PLDs).

SIMPLE PROGRAMMABLE LOGIC DEVICE (SPLD) The SPLD was the original PLD and is still available for small-scale applications. Generally, an **SPLD** can replace up to ten fixed-function ICs and their interconnections, depending on the type of functions and the specific SPLD. Most SPLDs are in one of two categories: PAL and GAL. A **PAL** (programmable array logic) is a device that can be programmed one time. It consists of a programmable array of AND gates and a fixed array of OR gates, as shown in Figure 33(a). A **GAL** (generic array logic) is a device that is basically a PAL that can be

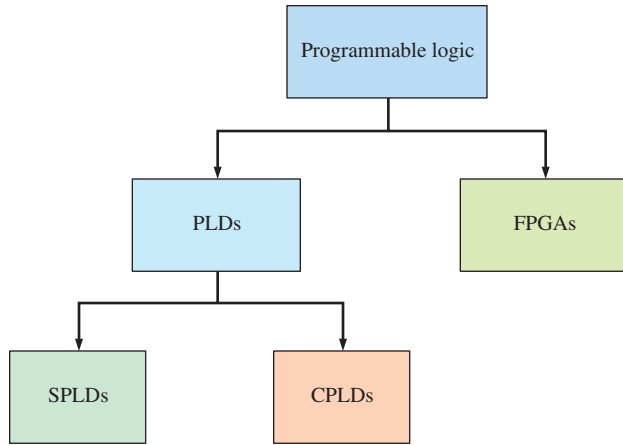


FIGURE 32 Programmable logic hierarchy.

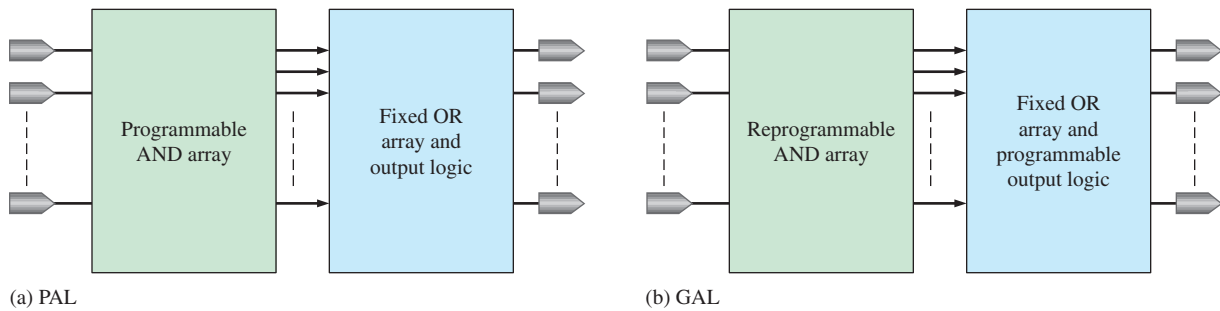


FIGURE 33 Block diagrams of simple programmable logic devices (SPLDs).

reprogrammed many times. It consists of a reprogrammable array of AND gates and a fixed array of OR gates with programmable outputs, as shown in Figure 33(b). A typical SPLD package is shown in Figure 34 and generally has from 24 to 28 pins.

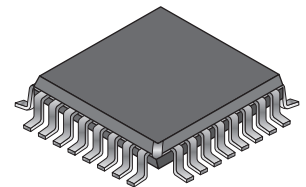


FIGURE 34 A typical SPLD package.

COMPLEX PROGRAMMABLE LOGIC DEVICE (CPLD) As technology progressed and the amount of circuitry that could be put on a chip (chip density) increased, manufacturers were able to put more than one SPLD on a single chip and the CPLD was born. Essentially, the **CPLD** is a device containing multiple SPLDs and can replace many fixed-function ICs. Figure 35 shows a basic CPLD block diagram with four logic array

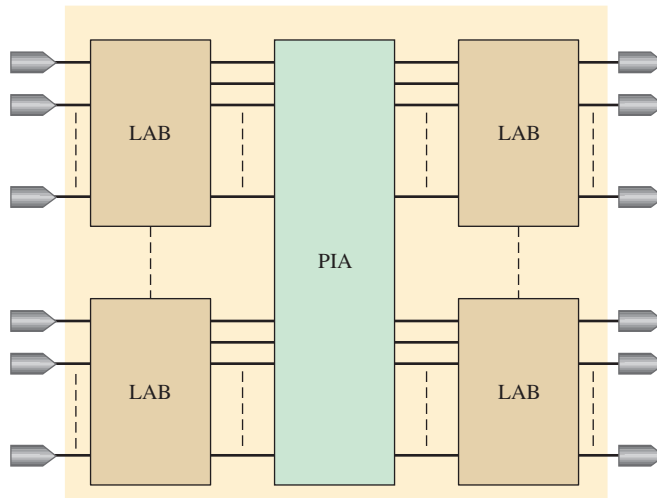


FIGURE 35 General block diagram of a CPLD.

blocks (LABs) and a programmable interconnection array (PIA). Depending on the specific CPLD, there can be from two to sixty-four LABs. Each logic array block is roughly equivalent to one SPLD.

Generally, CPLDs can be used to implement any of the logic functions discussed earlier, for example, decoders, encoders, multiplexers, demultiplexers, and adders. They are available in a variety of configurations, typically ranging from 44 to 160 pin packages. Examples of CPLD packages are shown in Figure 36.

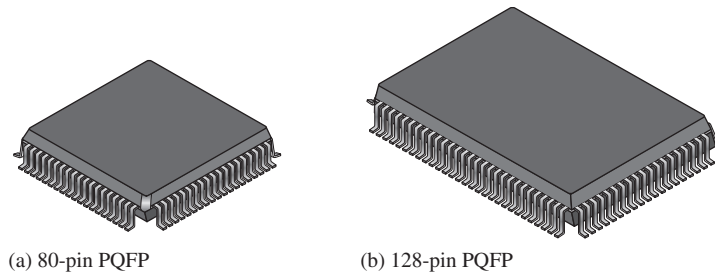


FIGURE 36 Typical CPLD packages.

FIELD-PROGRAMMABLE GATE ARRAY (FPGA) An **FPGA** is generally more complex and has a much higher density than a CPLD, although their applications can sometimes overlap. As mentioned, the SPLD and the CPLD are closely related because the CPLD basically contains a number of SPLDs. The FPGA, however, has a different internal structure (architecture), as illustrated in Figure 37. The three basic elements in an FPGA are the logic block, the programmable interconnections, and the input/output (I/O) blocks.

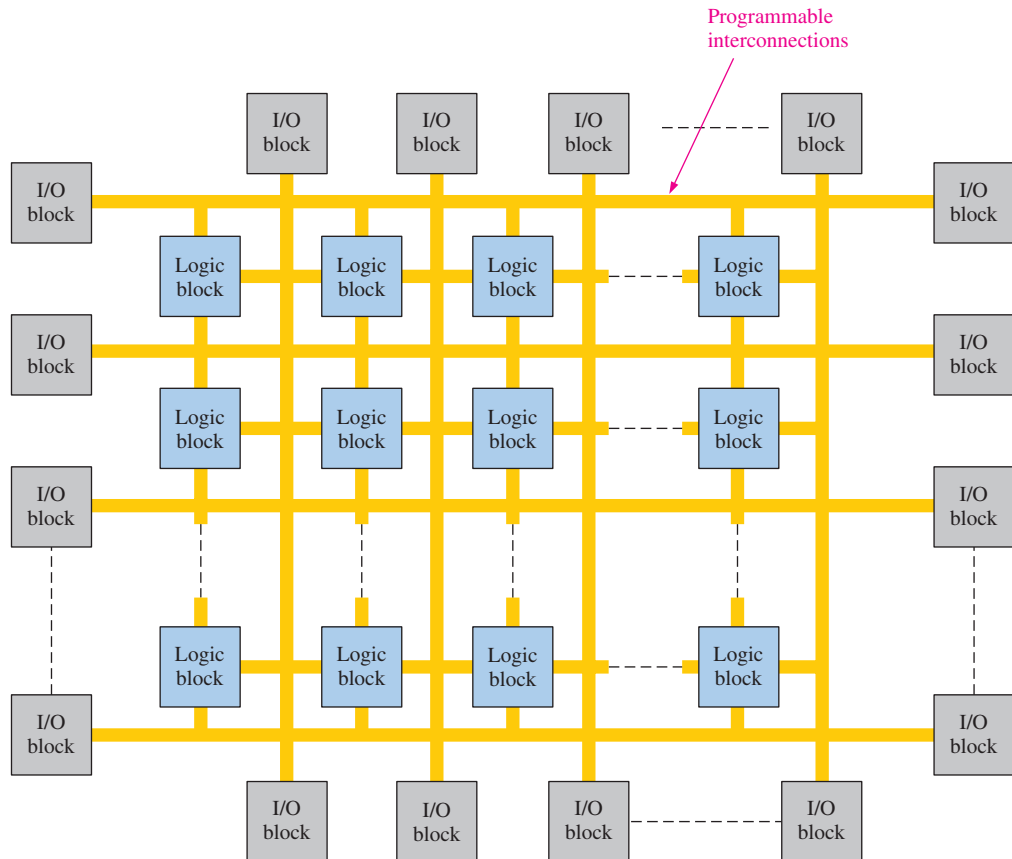


FIGURE 37 Basic structure of an FPGA.

The logic blocks in an FPGA are not as complex as the logic array blocks (LABs) in a CPLD, but generally there are many more of them. When the logic blocks are relatively simple, the FPGA architecture is called *fine-grained*. When the logic blocks are larger and more complex, the architecture is called *coarse-grained*. The I/O blocks are on the outer edges of the structure and provide individually selectable input, output, or bidirectional access to the outside world. The distributed programmable interconnection matrix provides for interconnection of the logic blocks and connection to inputs and outputs. Large FPGAs can have tens of thousands of logic blocks in addition to memory and other resources. A typical FPGA ball-grid array package is shown in Figure 38. These types of packages can have over 1000 input and output pins.

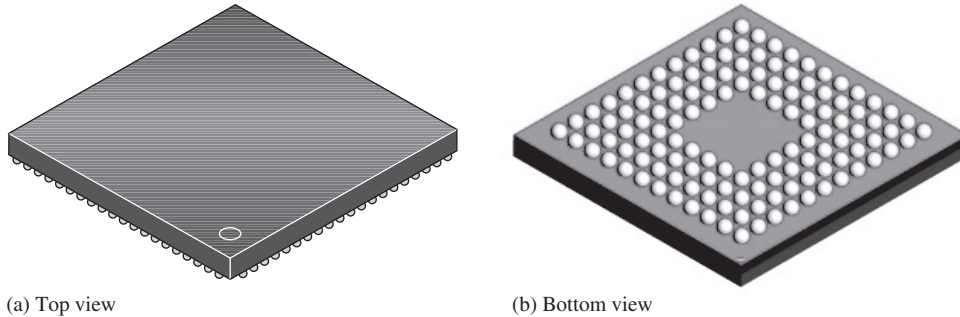


FIGURE 38 A typical ball-grid array (BGA) package.

The Programming Process

An SPLD, CPLD, or FPGA can be thought of as a “blank slate” on which you implement a specified system design using a certain process. This process requires a software development package installed on a computer to implement a circuit design in the programmable chip. The computer must be interfaced with a development board or programming fixture containing the device, as illustrated in Figure 39.

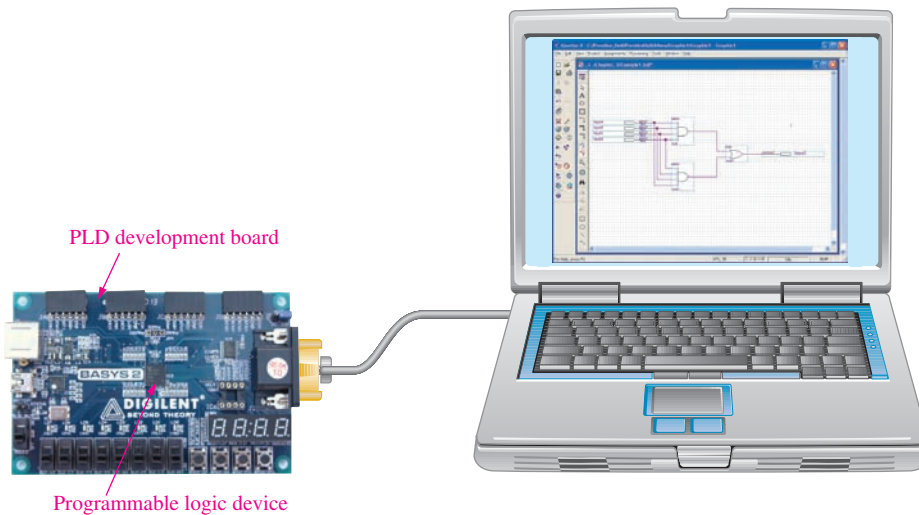


FIGURE 39 Basic setup for programming a PLD or FPGA. (Photo courtesy of Digilent, Inc.)

Several steps, called the *design flow*, are involved in the process of implementing a digital logic design in a programmable logic device. A block diagram of a typical programming process is shown in Figure 40. As indicated, the design flow has access to a design library.

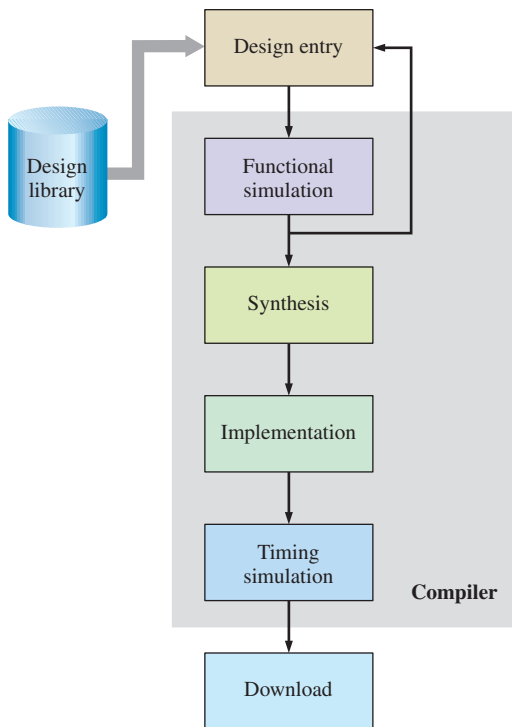


FIGURE 40 Basic programming flow block diagram.

DESIGN ENTRY This is the first programming step. The circuit or system design must be entered into the design application software using text-based entry, graphic entry (schematic capture), or state diagram description. Design entry is device independent. Text-based entry is accomplished with a hardware description language (HDL) such as VHDL, Verilog, or AHDL. Graphic (schematic) entry allows prestored logic functions from a library to be selected, placed on the screen, and then interconnected to create a logic design. State-diagram entry requires specification of both the states through which a sequential logic circuit progresses and the conditions that produce each state change.

Once a design has been entered, it is compiled. A **compiler** is a program that controls the design flow process and translates source code into object code in a format that can be logically tested or downloaded to a target device. The source code is created during design entry, and the object code is the final code that actually causes the design to be implemented in the programmable device.

FUNCTIONAL SIMULATION The entered and compiled design is simulated by software to confirm that the logic circuit functions as expected. The functional simulation will verify that correct outputs are produced for a specified set of inputs. A device-independent software tool for doing this is generally called a *waveform editor*. Any flaws demonstrated by the simulation would be corrected by going back to design entry and making appropriate changes.

SYNTHESIS **Synthesis** is where the design is translated into a netlist, which has a standard form and is device independent.

IMPLEMENTATION **Implementation** is where the logic structures described by the netlist are mapped into the actual structure of the specific device being programmed. The implementation process is called *fitting* or *place and route* and results in an output called a bitstream, which is device dependent.

TIMING SIMULATION This step comes after the design is mapped into the specific device. The timing simulation is basically used to confirm that there are no design flaws or timing problems due to propagation delays.

DOWNLOAD Once a bitstream has been generated for a specific programmable device, it has to be downloaded to the device to implement the software design in hardware. Some programmable devices have to be installed in a special piece of equipment called a *device programmer* or on a development board. Other types of devices can be programmed while in a system—called in-system programming (ISP)—using a standard JTAG (Joint Test Action Group) interface. Some devices are volatile, which means they lose their contents when reset or when power is turned off. In this case, the bitstream data must be stored in a memory and reloaded into the device after each reset or power-off. Also, the contents of an ISP device can be manipulated or upgraded while it is operating in a system. This is called “on-the-fly” reconfiguration.

The Microcontroller

A microcontroller is different than a PLD. The internal circuits of a microcontroller are fixed, and a program (series of instructions) directs the microcontroller operation in order to achieve a specific outcome. The internal circuitry of a PLD is programmed into it, and once programmed, the circuitry performs required operations. Thus, a program determines microcontroller operation, but in a PLD a program determines the logic function. Microcontrollers are generally programmed with either the C language or the BASIC language.

A **microcontroller** is basically a special-purpose small computer. Microcontrollers are generally used for embedded system applications. An **embedded system** is one that is designed to perform one or a few dedicated functions. By contrast, a general-purpose computer, such as a laptop, is designed to perform a wide range of functions and applications.

Embedded microcontrollers are used in many common applications. The embedded microcontroller is part of a complete system, which may include additional electronics and mechanical parts. For example, a microcontroller in a television set displays the input from the remote unit on the screen and controls the channel selection, audio, and various menu adjustments like brightness and contrast. In an automobile a microcontroller takes engine sensor inputs and controls spark timing and fuel mixture. Other applications include home appliances, thermostats, cell phones, and toys.

SECTION 5 CHECKUP

1. List three major categories of programmable logic devices and specify their acronyms.
2. How does a CPLD differ from an SPLD?
3. Name the steps in the programming process.
4. Briefly explain each step named in question 3.
5. What are the two main functional characteristics of a microcontroller?

6 FIXED-FUNCTION LOGIC DEVICES

All the logic elements and functions that have been discussed are generally available in **integrated circuit (IC)** form. A **fixed-function device** is one that cannot be programmed like a PLD. Digital systems have incorporated ICs for many years because of their small size, high reliability, low cost, and low power consumption. It is important to be able to recognize the IC packages and to know how the pin connections are numbered, as well as to be familiar with the way in which circuit complexities and circuit technologies determine the various IC classifications.

After completing this section, you should be able to

- Recognize the difference between through-hole devices and surface-mount fixed-function devices
- Identify dual in-line packages (DIP)
- Identify small-outline integrated circuit packages (SOIC)
- Identify plastic leaded chip carrier packages (PLCC)
- Identify leadless ceramic chip carrier packages (LCC)
- Determine pin numbers on various types of IC packages
- Explain the complexity classifications for fixed-function ICs

A monolithic **integrated circuit (IC)** is an electronic circuit that is constructed entirely on a single small chip of silicon. All the components that make up the circuit—transistors, diodes, resistors, and capacitors—are an integral part of that single chip. Fixed-function logic and programmable logic are two broad categories of digital ICs. In **fixed-function logic**, the logic functions are set by the manufacturer and cannot be altered.

Figure 41 shows a cutaway view of one type of fixed-function IC package with the circuit chip shown within the package. Points on the chip are connected to the package pins to allow input and output connections to the outside world.

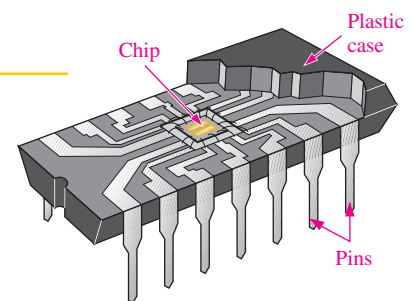


FIGURE 41 Cutaway view of one type of fixed-function surface-mount IC package, showing the chip mounted inside and connections to input and output pins.

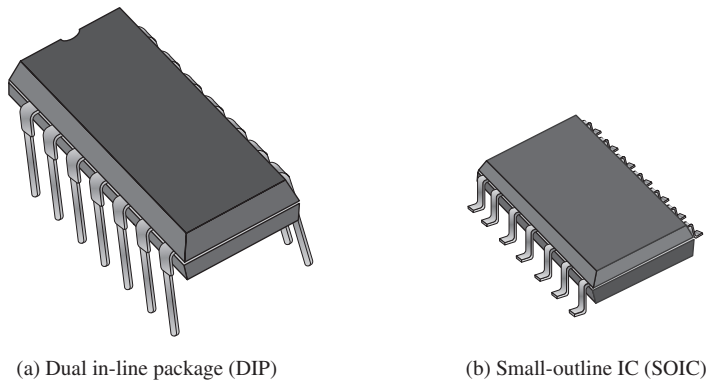


FIGURE 42 Examples of through-hole (DIP) and surface-mounted devices. The DIP is larger than the SOIC with the same number of leads.

IC Packages

Integrated circuit (IC) packages are classified according to the way they are mounted on printed circuit (PC) boards as either through-hole mounted or surface mounted. The through-hole type packages have pins (leads) that are inserted through holes in the PC board and can be soldered to conductors on the opposite side. The most common type of through-hole package is the dual in-line package (DIP) shown in Figure 42(a). The DIP is useful in lab work because it plugs in easily to a protoboard.

Most IC packages use surface-mount technology (SMT). Surface mounting is a space-saving alternative to through-hole mounting. The holes through the PC board are unnecessary for SMT. The pins of

surface-mounted packages are soldered directly to conductors on one side of the board, leaving the other side free for additional circuits. Also, for a circuit with the same number of pins, a surface-mounted package is much smaller than a dual in-line package because the pins are placed closer together. An example of a surface-mounted package is the small-outline integrated circuit (SOIC) shown in Figure 42(b).

Various types of SMT packages are available in a range of sizes, depending on the number of leads (more leads are required for more complex circuits and lead configurations). Examples of several types are shown in Figure 43. As you can see, the leads of the SSOP (shrink small-outline package) are formed into a “gull-wing” shape. The leads of the PLCC (plastic-leaded chip carrier) are turned under the package in a J-type shape. Instead of leads, the LCC (leadless ceramic chip) has metal contacts molded into its ceramic body. The LQFP also has gull-wing leads. Both the CSP (chip scale package) and the FBGA (fine-pitch ball grid array) have contacts embedded in the bottom of the package.

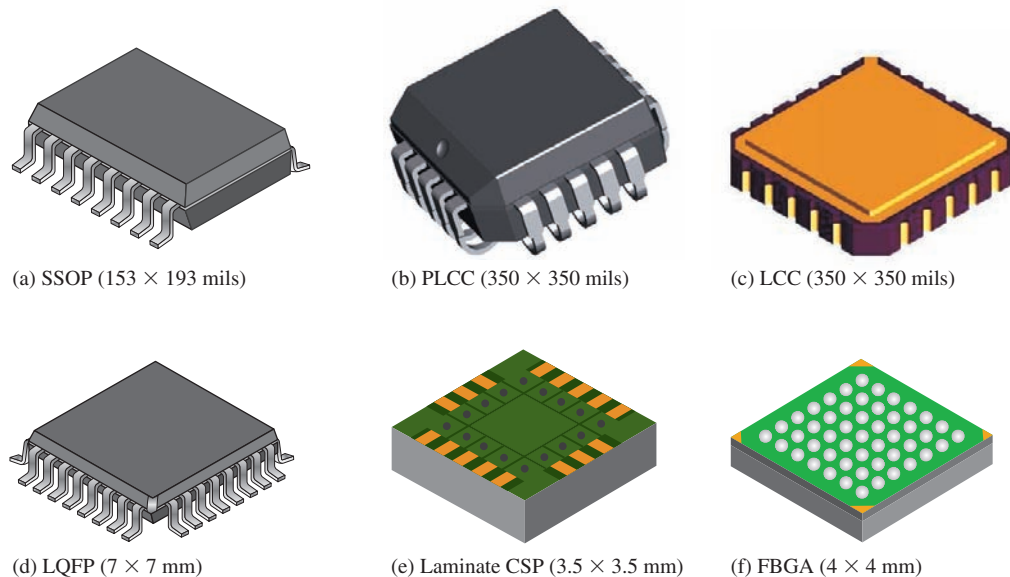


FIGURE 43 Typical SMT package configurations. Parts (e) and (f) show bottom views.

Pin Numbering

All IC packages have a standard format for numbering the pins (leads). The dual in-line packages (DIPs) and the shrink small-outline packages (SSOP) have the numbering arrangement illustrated in Figure 44(a) for a 16-pin package. Looking at the top of the package, pin 1 is indicated by an identifier that can be either a small dot, a notch, or a beveled

edge. The dot is always next to pin 1. Also, with the notch oriented upward, pin 1 is always the top left pin, as indicated. Starting with pin 1, the pin numbers increase as you go down, then across and up. The highest pin number is always to the right of the notch or opposite the dot.

The PLCC and LCC packages have leads arranged on all four sides. Pin 1 is indicated by a dot or other index mark and is located at the center of one set of leads. The pin numbers increase going counterclockwise as viewed from the top of the package. The highest pin number is always to the right of pin 1. Figure 44(b) illustrates this format for a 20-pin PLCC package.

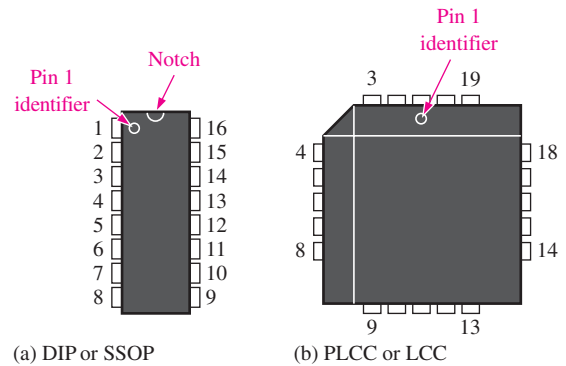


FIGURE 44 Pin numbering for standard types of IC packages. Top views are shown.

Complexity Classifications for Fixed-Function ICs

Fixed-function digital ICs are classified according to their complexity. They are listed here from the least complex to the most complex. The complexity figures stated here for SSI, MSI, LSI, VLSI, and ULSI are generally accepted, but definitions may vary from one source to another.

- **Small-scale integration (SSI)** describes fixed-function ICs that have up to ten equivalent gate circuits on a single chip, and they include basic gates and flip-flops.
- **Medium-scale integration (MSI)** describes integrated circuits that have from 10 to 100 equivalent gates on a chip. They include logic functions such as encoders, decoders, counters, registers, multiplexers, arithmetic circuits, small memories, and others.
- **Large-scale integration (LSI)** is a classification of ICs with complexities of from more than 100 to 10,000 equivalent gates per chip, including memories.
- **Very large-scale integration (VLSI)** describes integrated circuits with complexities of from more than 10,000 to 100,000 equivalent gates per chip.
- **Ultra large-scale integration (ULSI)** describes very large memories, larger **microprocessors**, and larger single-chip computers. Complexities of more than 100,000 equivalent gates per chip are classified as ULSI.

Integrated Circuit Technologies

The types of transistors with which all integrated circuits are implemented are either MOSFETs (metal-oxide semiconductor field-effect transistors) or bipolar junction transistors. A circuit technology that uses MOSFETs is **CMOS** (complementary MOS). **Bipolar** is a type of fixed-function digital circuit technology that uses bipolar junction transistors and is sometimes called **TTL** (transistor-transistor logic). **BiCMOS** uses a combination of both CMOS and bipolar. All the types of logic gates and logic functions that have been discussed are generally available as ICs.

All gates and other functions can be implemented with either type of circuit technology. SSI and MSI circuits are generally available in both CMOS and bipolar in the 74XX series, but CMOS is the most common.

SECTION 6 CHECKUP

1. What is an integrated circuit?
2. Define the terms DIP, SMT, SOIC, SSI, MSI, LSI, and VLSI.
3. Generally, in what classification does a fixed-function IC with the following number of equivalent gates fall?
(a) 10 (b) 75 (c) 500 (d) 15,000 (e) 200,000

7 A SYSTEM

A tablet-bottling system illustrates how the logic functions covered in this chapter can be used in a system environment. The functions used in this system are the encoder, decoder, code converter, adder, multiplexer, demultiplexer, register, and counter. This system could be implemented in three ways: with a PLD, with a microcontroller, or with fixed-function ICs. The first two are how all digital systems are currently implemented.

After completing this section, you should be able to

- Understand basic system operation and how certain components work together
- Explain the purpose of each logic function in the total system
- Describe the transfer of digital data throughout the system

A Process Control System

A system for bottling vitamin tablets is shown in the block diagram of Figure 45. To begin, the tablets are fed into a large funnel-type hopper. The narrow neck of the hopper creates a serial flow of tablets into a bottle on the conveyor belt below. Only one tablet at a time passes the sensor, so the tablets can be counted.

The system controls the number of tablets into each bottle and displays a continually updated readout of the total number of tablets bottled. This system utilizes all of the basic logic functions that have been introduced and illustrates how these functions can be connected to work together to produce a specified result. This system is purely for instructional purposes and is not intended to necessarily represent the most efficient or best way to implement the operation.

GENERAL OPERATION The maximum number of tablets per bottle is entered from the keypad, changed to a code by the *Encoder*, and stored in *Register A*. *Decoder A* changes the code stored in the register to a form appropriate for turning on the display. *Code converter A* changes the code to a binary number and applies it to the *A* input of the *Comparator (Comp)*.

An optical sensor in the neck of the hopper detects each tablet that passes and produces a pulse. This pulse goes to the *Counter* and advances it by one count; thus, any time during the filling of a bottle, the binary state of the counter represents the number of tablets in the bottle. The binary count is transferred from the counter to the *B* input of the comparator (*Comp*). The *A* input of the comparator is the binary number for the maximum tablets per bottle. Now, let's say that the present number of tablets per bottle is 50. When the binary number in the counter reaches 50, the $A = B$ output of the comparator goes HIGH, indicating that the bottle is full.

The HIGH output of the comparator causes the valve in the neck of the hopper to close and stop the flow of tablets. At the same time, the HIGH output of the comparator activates the conveyor, which moves the next empty bottle into place under the hopper. When the bottle is in place, the conveyor control issues a pulse that resets the counter to zero. As a result, the output of the comparator goes back LOW and causes the hopper valve to restart the flow of tablets.

For each bottle filled, the maximum binary number in the counter is transferred to the *A* input of the *Adder*. The *B* input of the adder comes from *Register B* that stores the total number of tablets bottled up through the last bottle filled. The adder produces a new cumulative sum that is then stored in register B, replacing the previous sum. This keeps a running total of the tablets bottled during a given run.

The cumulative sum stored in register B goes to *Decoder B*, which detects when register B has reached its maximum capacity and enables the *MUX*. The binary sum in register B is converted from parallel to serial form by the *MUX* and transmitted over the single line to the remote *Demultiplexer (DEMUX)*, which changes the number back to parallel form for storage in a remote computer for keeping track of the total tablets bottled in a specified time period.

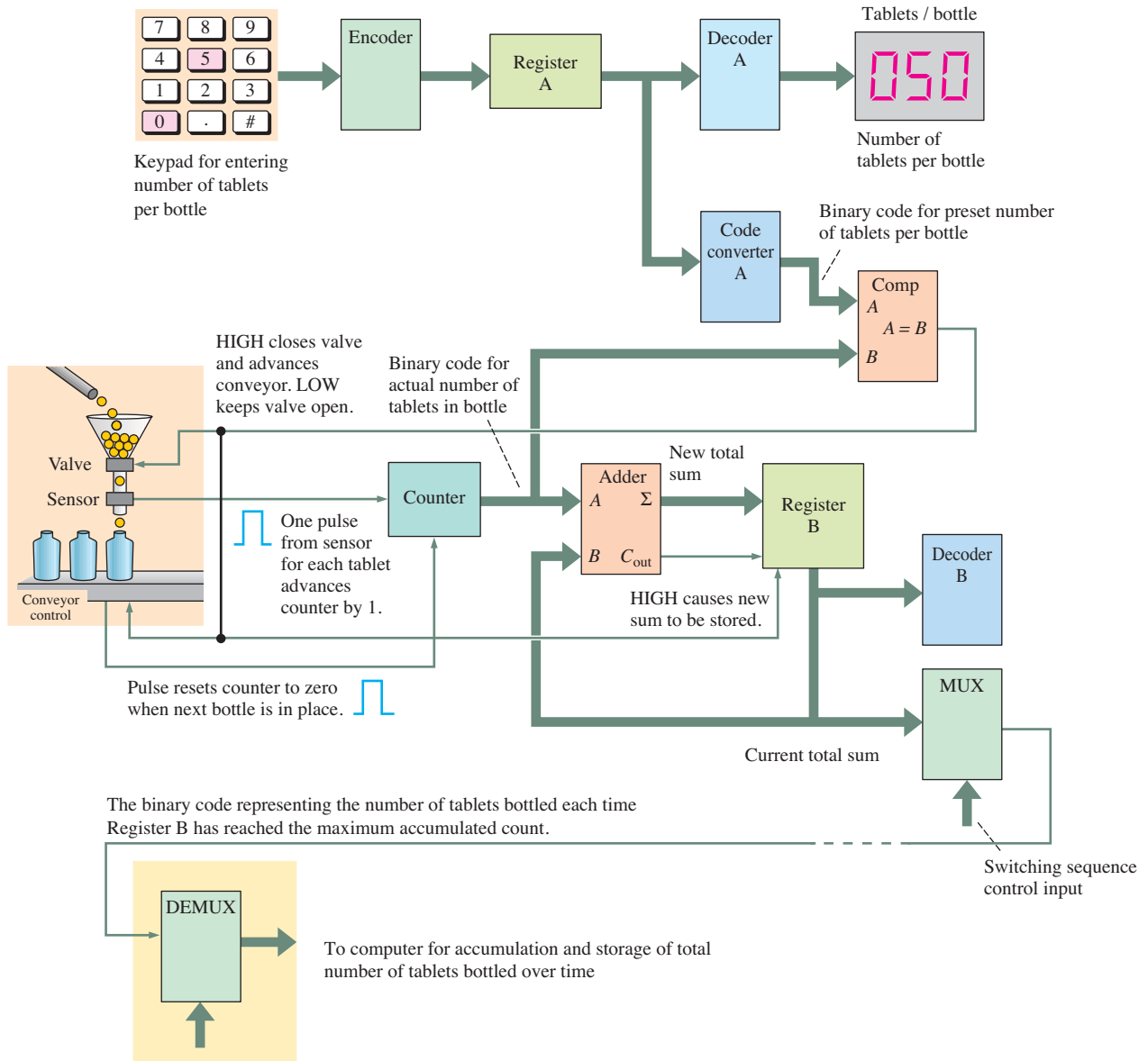


FIGURE 45 Block diagram of a tablet-bottling system.

SECTION 7 CHECKUP

1. How is the number of tablets per bottle entered into the system?
2. How does the system determine when a bottle is full?
3. When is the counter reset?

8 MEASURING INSTRUMENTS



Troubleshooting is the process of systematically isolating, identifying, and correcting a fault in a circuit or system. A variety of instruments are available for use in troubleshooting and testing. Some common types of instruments are introduced and discussed in this section.

After completing this section, you should be able to

- Distinguish between an analog and a digital oscilloscope
- Recognize common oscilloscope controls
- Determine amplitude, period, frequency, and duty cycle of a pulse waveform with an oscilloscope
- Discuss the logic analyzer and some common formats
- Describe the purpose of the data pattern generator, the digital multimeter (DMM), the dc power supply, the logic probe, and the logic pulser

The Oscilloscope

The oscilloscope (scope for short) is one of the most widely used instruments for general testing and troubleshooting. The scope is basically a graph-displaying device that traces the graph of a measured electrical signal on its screen. In most applications, the graph shows how signals change over time. The vertical axis of the display screen represents voltage, and the horizontal axis represents time. Amplitude, period, and frequency of a signal can be measured using the oscilloscope. Also, the pulse width, duty cycle, rise time, and fall time of a pulse waveform can be determined. Most scopes can display at least two, and many can display four signals on the screen at one time, enabling their time relationship to be observed. A typical 4-channel digital oscilloscope is shown in Figure 46.

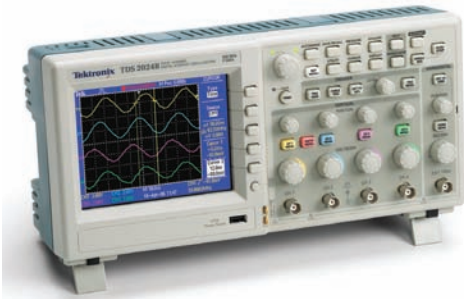


FIGURE 46 A digital oscilloscope. Used with permission from Tektronix, Inc.

Two basic types of oscilloscopes, analog and digital, can be used to view digital waveforms. An analog scope works by applying the measured waveform directly to control the up and down motion of the electron beam in the cathode-ray tube (CRT) as it sweeps across the display screen. As a result, the beam traces out the waveform pattern on the screen. A digital scope converts the measured waveform to digital information by a sampling process in an analog-to-digital converter (ADC). The digital information is then used to reconstruct the waveform on the screen.

The digital scope is more widely used than the analog scope. However, either type can be used in many applications; each has characteristics that make it more suitable for certain situations. An analog scope displays waveforms as they occur in “real time.” Digital scopes are useful for measuring transient pulses that may occur randomly or only once. Also, because information about the measured waveform can be stored in a digital scope, it may be viewed at some later time, printed out, or thoroughly analyzed by a computer or other means.

BASIC OPERATION OF ANALOG OSCILLOSCOPES To measure a voltage, a **probe** must be connected from the scope to the point in a circuit at which the voltage is present. Generally, a $\times 10$ probe is used that reduces (attenuates) the signal amplitude by ten. The signal goes through the probe into the vertical circuits where it is either further attenuated or amplified, depending on the actual amplitude and on where you set the vertical control of the scope. The vertical circuits then drive the vertical deflection plates of the CRT. Also, the signal goes to the trigger circuits that trigger the horizontal circuits to initiate repetitive horizontal sweeps of the electron beam across the screen using a sawtooth waveform. There are many sweeps per second so that the beam appears to form a solid line across the screen in the shape of the waveform. This basic operation is illustrated in Figure 47.

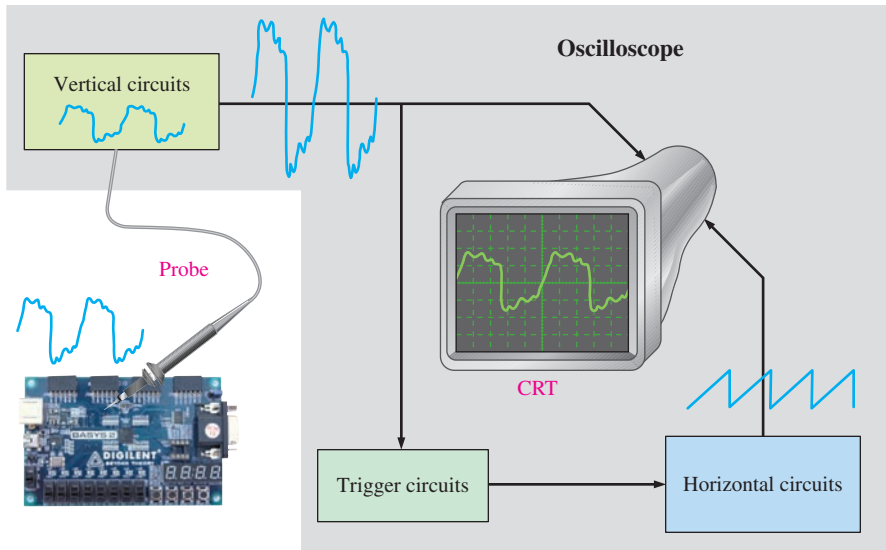


FIGURE 47 Block diagram of an analog oscilloscope. (Photo courtesy of Digilent, Inc.)

BASIC OPERATION OF DIGITAL OSCILLOSCOPES Some parts of a digital scope are similar to the analog scope. However, the digital scope is more complex than an analog scope and typically has an LCD screen rather than a CRT. Rather than displaying a waveform as it occurs, the digital scope first acquires the measured analog waveform and converts it to a digital format using an analog-to-digital converter (ADC). The digital data is stored and processed. The data then goes to the reconstruction and display circuits for display in its original analog form. Figure 48 shows a basic block diagram for a digital oscilloscope.

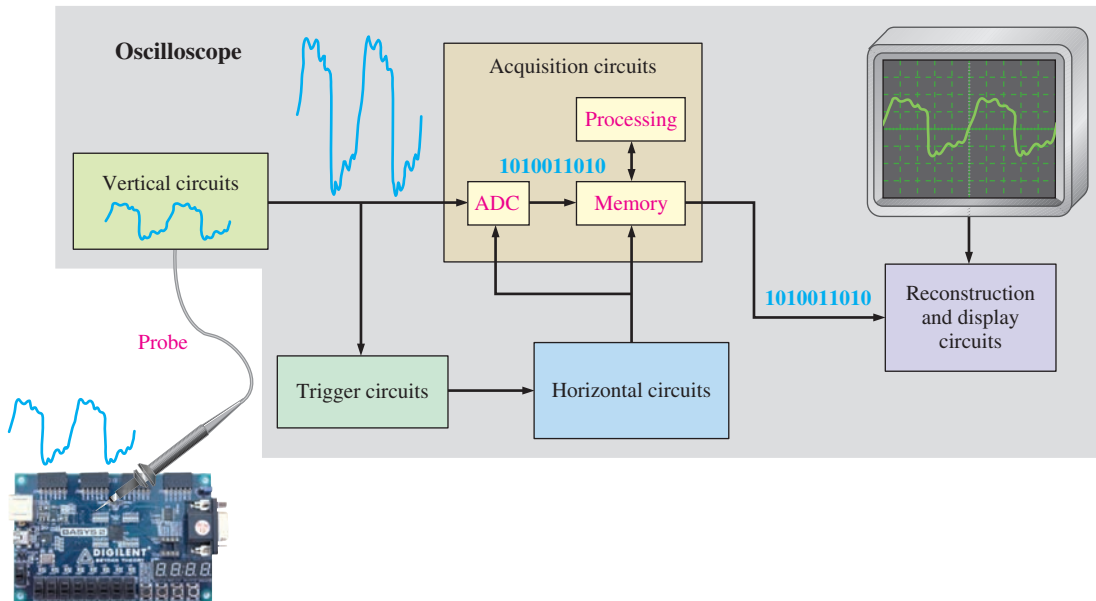


FIGURE 48 Block diagram of a digital oscilloscope. (Photo courtesy of Digilent, Inc.)

OSCILLOSCOPE CONTROLS A front panel view of a typical digital oscilloscope is shown in Figure 49. Instruments vary depending on model and manufacturer, but most have certain common features. For example, the four vertical sections contain a Position control, a channel menu button, and a volts/div control. The horizontal section contains a sec/div control.

Some of the main oscilloscope controls are now discussed. Refer to the user manual for complete details of your particular scope.

VERTICAL CONTROLS In the vertical section of the scope in Figure 49, there are identical controls for each of the four channels (1, 2, 3, and 4). The Position control lets you move a displayed waveform up or down vertically on the screen. The buttons on the right side of the screen provide for the selection of several items that appear on the screen, such as the coupling modes (ac, dc, or ground), coarse or fine adjustment for the volts/div, signal inversion, and other parameters. The volts/div control adjusts the number of volts represented by each vertical division on the screen. The volts/div setting for each channel is displayed on the bottom of the screen.

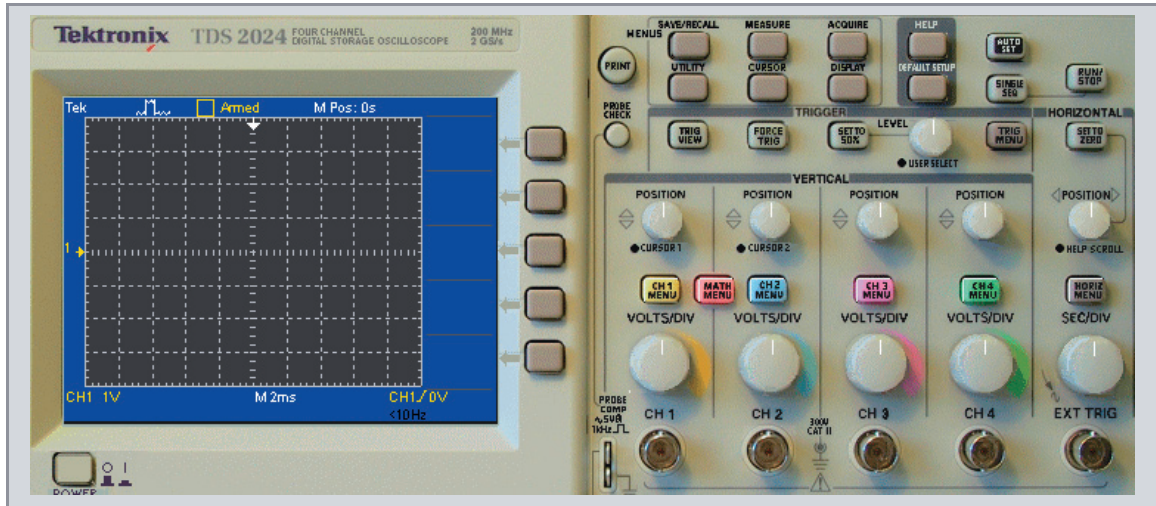
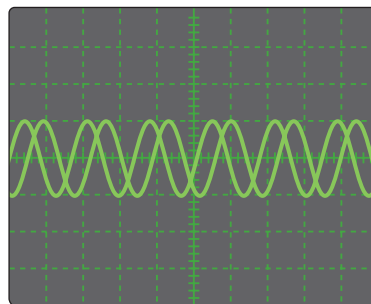


FIGURE 49 A digital oscilloscope front panel. Used with permission from Tektronix, Inc.

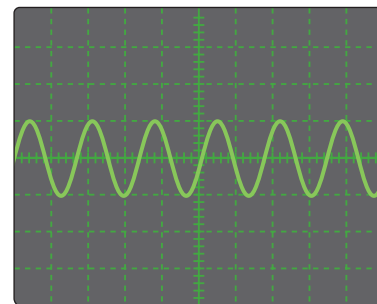
HORIZONTAL CONTROLS In the horizontal section, the controls apply to all channels. The Position control lets you move a displayed waveform left or right horizontally on the screen. The sec/div control adjusts the time represented by each horizontal division or main time base. The sec/div setting is displayed at the bottom of the screen.

TRIGGER CONTROLS In the Trigger control section, the Level control determines the point on the triggering waveform where triggering occurs to initiate the sweep to display input waveforms. The Menu button provides for the selection of several items that appear on the screen, including edge or slope triggering, trigger source, trigger mode, and other parameters. There is also an input for an external trigger signal.

Triggering stabilizes a waveform on the screen or properly triggers on a pulse that occurs only one time or randomly. Also, it allows you to observe time delays between two waveforms. Figure 50 compares a triggered to an untriggered signal. The untriggered signal tends to drift across the screen, producing what appears to be multiple waveforms.



(a) Untriggered waveform display



(b) Triggered waveform display

FIGURE 50 Comparison of an untriggered and a triggered waveform on an oscilloscope.

COUPLING A SIGNAL INTO THE SCOPE Coupling is the method used to connect a signal voltage to be measured into the oscilloscope. DC and AC coupling are usually selected from the Vertical menu on a scope. DC coupling allows a waveform including its dc component to be displayed. AC coupling blocks the dc component of a signal so that you see the waveform centered at 0 V. The Ground mode allows you to connect the channel input to ground to see where the 0 V reference is on the screen. Figure 51 illustrates the result of DC and AC coupling using a pulse waveform that has a dc component.

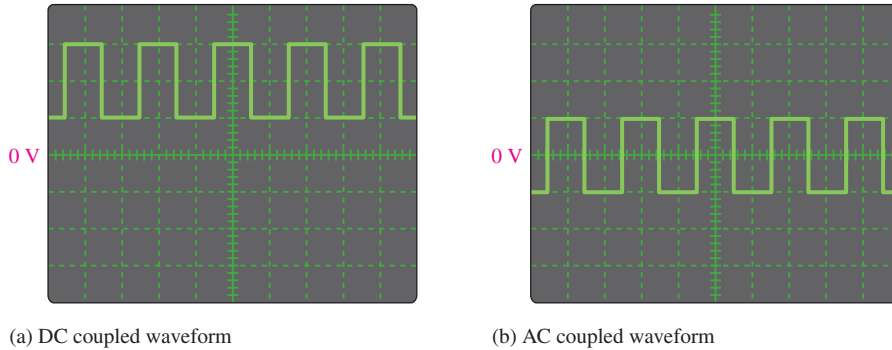


FIGURE 51 Displays of the same waveform having a dc component.

The voltage probe, shown in Figure 46, is essential for connecting a signal to the scope. Since all instruments tend to affect the circuit being measured due to loading, most scope probes provide a high series resistance to minimize loading effects. Probes that have a series resistance ten times larger than the input resistance of the scope are called $\times 10$ probes. Probes with no series resistance are called $\times 1$ probes. The oscilloscope adjusts its calibration for the attenuation of the type of probe being used. For most measurements, the $\times 10$ probe should be used. However, if you are measuring very small signals, a $\times 1$ may be the best choice.

The probe has an adjustment that allows you to compensate for the input capacitance of the scope. Most scopes have a probe compensation output that provides a calibrated square wave for probe compensation. Before making a measurement, you should make sure that the probe is properly compensated to eliminate any distortion introduced. Typically, there is a screw or other means of adjusting compensation on a probe. Figure 52 shows scope waveforms for three probe conditions: properly compensated, undercompensated, and overcompensated. If the waveform appears either over- or undercompensated, adjust the probe until the properly compensated square wave is achieved.

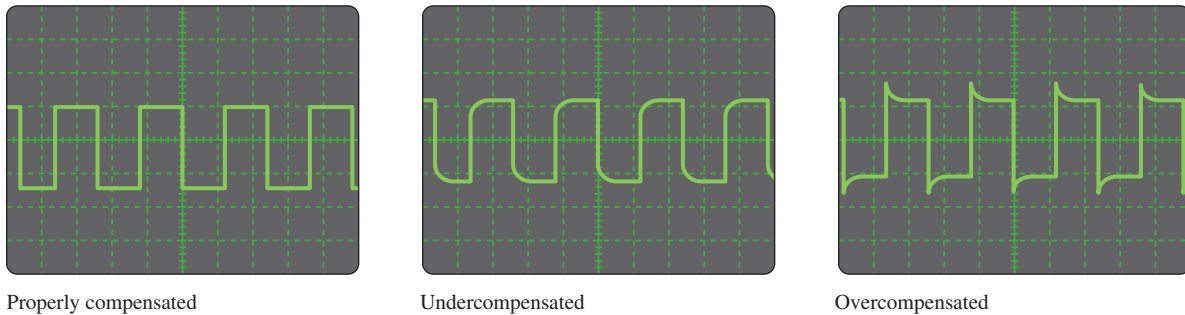


FIGURE 52 Probe compensation conditions.

EXAMPLE 3

Based on the readouts, determine the amplitude and the period of the pulse waveform on the screen of a digital oscilloscope as shown in Figure 53. Also, calculate the frequency.

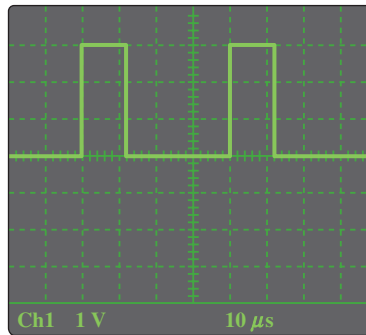


FIGURE 53

SOLUTION

The volts/div setting is 1 V. The pulses are three divisions high. Since each division represents 1 V, the pulse amplitude is

$$\text{Amplitude} = (3 \text{ div})(1 \text{ V/div}) = \mathbf{3 \text{ V}}$$

The sec/div setting is 10 μs . A full cycle of the waveform (from beginning of one pulse to the beginning of the next) covers four divisions; therefore, the period is

$$\text{Period} = (4 \text{ div})(10 \mu\text{s/div}) = \mathbf{40 \mu\text{s}}$$

The frequency is calculated as

$$f = \frac{1}{T} = \frac{1}{40 \mu\text{s}} = \mathbf{25 \text{ kHz}}$$

RELATED PROBLEM

For a volts/div setting of 4 V and sec/div setting of 2 ms, determine the amplitude and period of the pulse shown on the screen in Figure 53.



FIGURE 54 Typical logic analyzer. Used with permission from Tektronix, Inc.

The Logic Analyzer

Logic analyzers are used for measurements of multiple digital signals and measurement situations with difficult trigger requirements. Basically, the logic analyzer came about as a result of microprocessors in which troubleshooting or debugging required many more inputs than an oscilloscope offered. Many oscilloscopes have two input channels and some are available with four. Logic analyzers are available with from 34 to 136 input channels. Generally, an oscilloscope is used either when amplitude, frequency, and other timing parameters of a few signals at a time or when parameters such as rise and fall times, overshoot, and delay times need to be measured. The logic analyzer is used when the logic levels of a large number of signals need to be determined and for the correlation of simultaneous signals based on their timing relationships. A typical logic analyzer is shown in Figure 54, and a simplified block diagram is in Figure 55.

DATA ACQUISITION The large number of signals that can be acquired at one time is a major factor that distinguishes a logic analyzer from an oscilloscope. Generally, the two types of data acquisition in a logic analyzer are the timing acquisition and the state acquisition. Timing acquisition is used primarily when the timing relationships among the various signals need to be determined. State acquisition is used when you need to view the sequence of states as they appear in a system under test.

It is often helpful to have correlated timing and state data, and most logic analyzers can simultaneously acquire that data. For example, a problem may initially be detected as an invalid state. However, the invalid condition may be caused by a timing violation in the system under test. Without both types of information available at the same time, isolating the problem could be very difficult.

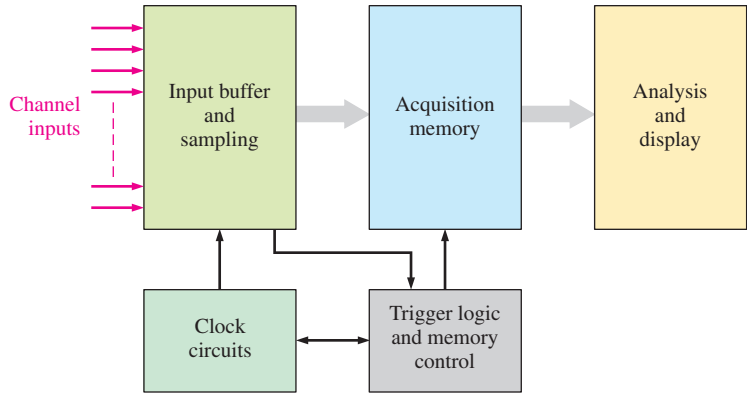


FIGURE 55 Simplified block diagram of a logic analyzer.

CHANNEL COUNT AND MEMORY DEPTH Logic analyzers contain a real-time acquisition memory in which sampled data from all the channels are stored as they occur. Two features that are of primary importance are the channel count and the memory depth. The acquisition memory can be thought of as having a width equal to the number of channels and a depth that is the number of bits that can be captured by each channel during a certain time interval.

Channel count determines the number of signals that can be acquired simultaneously. In certain types of systems, a large number of signals are present, such as on the data bus in a microprocessor-based system. The depth of the acquisition memory determines the amount of data from a given channel that you can view at any given time.

ANALYSIS AND DISPLAY Once data has been sampled and stored in the acquisition memory, it can typically be used in several different display and analysis modes. The waveform display is much like the display on an oscilloscope where you can view the time relationship of multiple signals. The listing display indicates the state of the system under test by showing the values of the input waveforms (1s and 0s) at various points in time (sample points). Typically, this data can be displayed in hexadecimal or other formats. Figure 56 shows simplified versions of these two display modes. The listing display samples correspond to the sampled points shown in red on the waveform display.

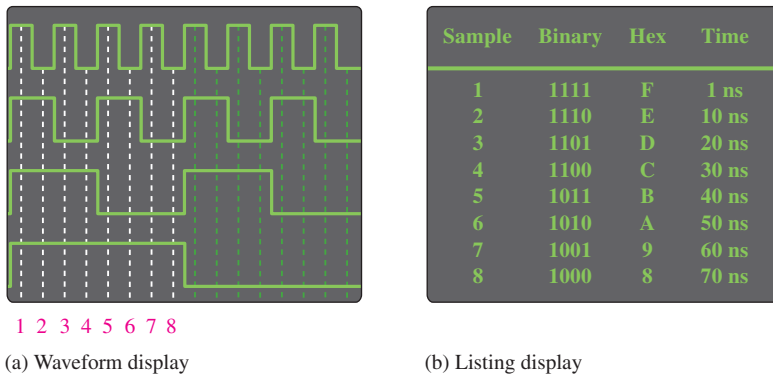


FIGURE 56 Two logic analyzer display modes.

Two more modes that are useful in computer and microprocessor-based system testing are the instruction trace and the source code debug. The instruction trace determines and displays instructions that occur, for example, on the data bus in a microprocessor-

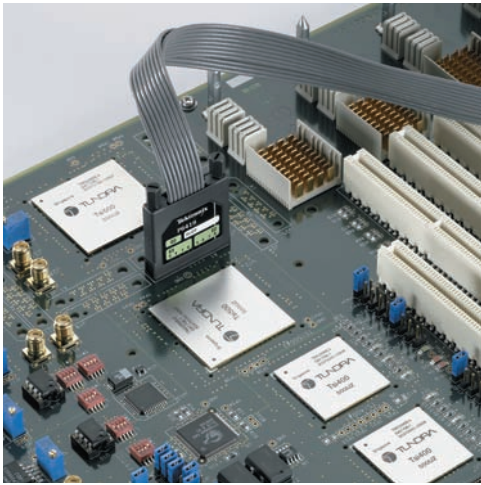


FIGURE 57 A typical multichannel logic analyzer probe. Used with permission from Tektronix, Inc.

based system. In this mode the op-codes and the mnemonics (English-like names) of instructions are generally displayed as well as their corresponding memory address. Many logic analyzers also include a source code debug mode, which essentially allows you to see what is actually going on in the system under test when a program instruction is executed.

PROBES Three basic types of probes are used with logic analyzers. One is a multichannel compression probe that can be attached to points on a circuit board, as shown in Figure 57. Another type of multichannel probe, similar to the one shown, plugs into dedicated sockets mounted on a circuit board. A third type is a single-channel clip-on probe.

Signal Generators

LOGIC SIGNAL SOURCE These instruments are also known as pulse generators and data pattern generators. They are specifically designed to generate digital signals with precise edge placement and amplitudes and to produce the streams of 1s and 0s needed to test computer buses, microprocessors, and other digital systems.

WAVEFORM AND DATA PATTERN GENERATORS The arbitrary waveform generator can be used to generate standard signals like sine waves, triangular waves, and pulses as well as signals with various shapes and characteristics. Waveforms can be defined by mathematical or graphical input. A typical arbitrary waveform generator is shown in Figure 58(a).

The data pattern generator, shown in Figure 58(b), provides digital waveforms with programmable bit patterns. The function generator, shown in part (c), provides pulse, sine, and triangular waveforms, often with programmable capability. Signal generators have logic-compatible outputs to provide the proper level and drive for inputs to digital circuits.



(a) Arbitrary waveform generator

(b) Data pattern generator

(c) Function generator

FIGURE 58 Typical signal generators. Used with permission from Tektronix, Inc.

The Digital Multimeter (DMM)

The digital multimeter (DMM) is a versatile instrument found on virtually all workbenches. All DMMs can make basic ac and dc voltage, current, and resistance measurements. Voltage and resistance measurements are the principal quantities measured with DMMs. For current measurements, the leads are switched to a separate set of jacks and placed in series with the current path. In this mode, the meter acts like a short circuit, so serious problems can occur if the meter is incorrectly placed in parallel.

In addition to the basic measurements, most DMMs can also test diodes and capacitors and frequently will have other capabilities such as frequency measurements. Most new DMMs have an autoranging feature, meaning that the user is not required to select a

range for making a measurement. If the range is not set automatically, the user needs to set the range switch for voltage measurements *higher* than the expected reading to avoid damage to the meter.

In digital systems, DMMs are the preferred instrument for setting dc power supply voltages or checking the supply voltage on various points in the circuit. Because digital signals are nonsinusoidal, the DMM is generally *not* used for measurements of digital signals (although the average or rms value can be determined in some cases). For signal measurements, the oscilloscope is the preferred instrument.

In addition, DMMs are used in digital systems for testing continuity between points in a circuit and checking resistors with the ohmmeter function. For checking a circuit path or looking for a short, DMMs are the instrument of choice. Many DMMs sound a beep or tone when there is continuity between the leads, making it handy to trace paths without having to look at the display. If the DMM is not equipped with a continuity test, the ohmmeter function can be used instead. Measurements of continuity or resistance are never done in “live” circuits, as any circuit voltage will disrupt the readings and can be dangerous.

Typical test bench and handheld DMMs are shown in Figure 59.



FIGURE 59 Typical DMMs. Courtesy of B&K Precision Corporation.

The DC Power Supply

This instrument is an indispensable instrument on any test bench. The power supply converts ac power from the standard wall outlet into regulated dc voltage. All digital circuits require dc voltage. Most logic circuits require from 1.2 V to 5 V to operate. The power supply is used to power circuits during design, development, and troubleshooting when in-system power is not available. Typical test bench dc power supplies are shown in Figure 60.



FIGURE 60 Typical dc power supplies. Courtesy of B&K Precision Corporation.

The Logic Probe and Logic Pulser

The logic probe is a convenient, inexpensive handheld tool that provides a means of troubleshooting a digital circuit by sensing various conditions at a point in a circuit. A probe can detect high-level voltage, low-level voltage, single pulses, repetitive pulses, and opens on a PC board. A probe lamp indicates the condition that exists at a certain point.

The logic pulser produces a repetitive pulse waveform that can be applied to any point in a circuit. You can apply pulses at one point in a circuit with the pulser and check another point for resulting pulses with a logic probe.

SECTION 8 CHECKUP

1. What is the main difference between a digital and an analog oscilloscope?
2. Name two main differences between a logic analyzer and an oscilloscope?
3. What does the volts/div control on an oscilloscope do?
4. What does the sec/div control on an oscilloscope do?
5. What is the purpose of a function generator?

SUMMARY

- An analog quantity has continuous values.
- A digital quantity has a discrete set of values.
- A binary digit is called a bit.
- A pulse is characterized by rise time, fall time, pulse width, and amplitude.
- The frequency of a periodic waveform is the reciprocal of the period. The formulas relating frequency and period are

$$f = \frac{1}{T} \quad \text{and} \quad T = \frac{1}{f}$$

- The duty cycle of a pulse waveform is the ratio of the pulse width to the period, expressed by the following formula as a percentage:

$$\text{Duty cycle} = \left(\frac{t_{PW}}{T} \right) 100\%$$

- A timing diagram is an arrangement of two or more waveforms showing their relationship with respect to time.
- Three basic logic operations are NOT, AND, and OR. The standard symbols for these are given in Figure 61.

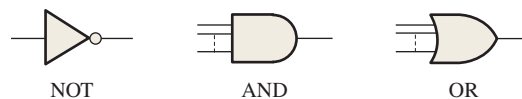


FIGURE 61

- The basic logic functions are comparison, arithmetic, code conversion, decoding, encoding, data selection, storage, and counting.
- PLDs are integrated circuits into which logic designs can be programmed.
- Two types of SPLDs (simple programmable logic devices) are PAL (programmable array logic) and GAL (generic array logic).
- The CPLD (complex programmable logic device) contains multiple SPLDs with programmable interconnections.
- The FPGA (field-programmable gate array) has a different internal structure than the CPLD and is generally used for more complex circuits and systems.
- Fixed-function logic consists of integrated circuits that are manufactured with logic elements that cannot be changed.
- The two broad physical categories of IC packages are through-hole mounted and surface mounted.
- Three families of fixed-function integrated circuits are CMOS, bipolar, and BiCMOS.
- Bipolar is also known as TTL (transistor-transistor logic).
- The categories of ICs in terms of circuit complexity are SSI (small-scale integration), MSI (medium-scale integration), LSI, VLSI, and ULSI (large-scale, very large-scale, and ultra large-scale integration).
- Common instruments used in testing and troubleshooting digital circuits are the oscilloscope, logic analyzer, arbitrary waveform generator, data pattern generator, function generator, dc power supply, digital multimeter, logic probe, and logic pulser.

KEY TERMS

Analog Being continuous or having continuous values.

AND A basic logic operation in which a true (HIGH) output occurs only when all the input conditions are true (HIGH).

Binary Having two values or states; describes a number system that has a base of two and utilizes 1 and 0 as its digits.

Bit A binary digit, which can be either a 1 or a 0.

Clock The basic timing signal in a digital system; a periodic waveform used to synchronize operation.

Compiler A program that controls the design flow process and translates source code into object code in a format that can be logically tested or downloaded to a target device.

CPLD A complex programmable logic device that consists basically of multiple SPLD arrays with programmable interconnections.

Data Information in numeric, alphabetic, or other form.

Digital Related to digits or discrete quantities; having a set of discrete values.

Digital system An arrangement of the individual logic functions connected to perform a specified operation or produce a defined output.

Duty cycle The ratio of the pulse width to the period of a digital waveform, expressed as a percentage.

Embedded system Generally, a single-purpose system, such as a processor, built into a larger system for the purpose of controlling the system.

Fixed-function logic A category of digital integrated circuits having functions that cannot be altered.

FPGA Field-programmable gate array.

Gate A logic circuit that performs a basic logic operation such as AND or OR.

Input The signal or line going into a circuit.

Integrated circuit (IC) A type of circuit in which all of the components are integrated on a single chip of semiconductive material of extremely small size.

Inverter A NOT circuit; a circuit that changes a HIGH to a LOW or vice versa.

Logic In digital electronics, the decision-making capability of gate circuits, in which a HIGH represents a true statement and a LOW represents a false one.

Microcontroller An integrated circuit consisting of a complete computer on a single chip and used for specified control functions.

NOT A basic logic operation that performs inversions.

OR A basic logic operation in which a true (HIGH) output occurs when one or more of the input conditions are true (HIGH).

Output The signal or line coming out of a circuit.

Parallel In digital systems, data occurring simultaneously on several lines; the transfer or processing of several bits simultaneously.

Programmable logic device A type of integrated circuit (IC) that starts as a “blank state” and into which a logic design is programmed.

Pulse A sudden change from one level to another, followed after a time, called the pulse width, by a sudden change back to the original level.

Serial Having one element following another, as in a serial transfer of bits; occurring in sequence rather than simultaneously.

SPLD Simple programmable logic device.

Timing diagram A graph of digital waveforms showing the time relationship of two or more waveforms.

Troubleshooting The technique or process of systematically identifying, isolating, and correcting a fault in a circuit or system.

TRUE/FALSE QUIZ

Answers are at the end of the chapter.

1. An analog signal is one having continuous values.
2. A digital quantity has ten discrete values.
3. There are two digits in the binary system.
4. The term *bit* is short for binary digit.
5. In positive logic, a LOW level represents a binary 1.
6. If the period of a pulse waveform increases, the frequency also increases.

7. A timing diagram shows the timing relationship of two or more digital waveforms.
8. The basic logic operations are AND, OR, and MAYBE.
9. If the input to an inverter is a 1, the output is a 0.
10. CPLD stands for *complex programmable logic device*.
11. FPGA stands for *functionally programmed gate array*.
12. An oscilloscope is used to observe, measure, and analyze waveforms.

SELF-TEST

Answers are at the end of the chapter.

1. A quantity having continuous values is
 - (a) a digital quantity
 - (b) an analog quantity
 - (c) a binary quantity
 - (d) a natural quantity
2. The term *bit* means
 - (a) a small amount of data
 - (b) a 1 or a 0
 - (c) binary digit
 - (d) both answers (b) and (c)
3. The time interval on the leading edge of a pulse between 10% and 90% of the amplitude is the
 - (a) rise time
 - (b) fall time
 - (c) pulse width
 - (d) period
4. A pulse in a certain waveform occurs every 10 ms. The frequency is
 - (a) 1 kHz
 - (b) 1 Hz
 - (c) 100 Hz
 - (d) 10 Hz
5. In a certain digital waveform, the period is twice the pulse width. The duty cycle is
 - (a) 100%
 - (b) 200%
 - (c) 50%
6. An inverter
 - (a) performs the NOT operation
 - (b) changes a HIGH to a LOW
 - (c) changes a LOW to a HIGH
 - (d) does all of the above
7. The output of an AND gate is HIGH when
 - (a) any input is HIGH
 - (b) all inputs are HIGH
 - (c) no inputs are HIGH
 - (d) both answers (a) and (b)
8. The output of an OR gate is HIGH when
 - (a) any input is HIGH
 - (b) all inputs are HIGH
 - (c) no inputs are HIGH
 - (d) both answers (a) and (b)
9. The device used to convert a binary number to a 7-segment display format is the
 - (a) multiplexer
 - (b) encoder
 - (c) decoder
 - (d) register
10. An example of a data storage device is
 - (a) the logic gate
 - (b) the flip-flop
 - (c) the comparator
 - (d) the register
 - (e) both answers (b) and (d)
11. A fixed-function IC package containing four AND gates is an example of
 - (a) MSI
 - (b) SMT
 - (c) SOIC
 - (d) SSI
12. An LSI device has a circuit complexity of from
 - (a) 10 to 100 equivalent gates
 - (b) more than 100 to 10,000 equivalent gates
 - (c) 2000 to 5000 equivalent gates
 - (d) more than 10,000 to 100,000 equivalent gates
13. VHDL is a
 - (a) logic device
 - (b) PLD programming language
 - (c) computer language
 - (d) very high density logic
14. A CPLD is a
 - (a) controlled program logic device
 - (b) complex programmable logic driver
 - (c) complex programmable logic device
 - (d) central processing logic device

15. An FPGA is a
- (a) field-programmable gate array
 - (b) fast programmable gate array
 - (c) field-programmable generic array
 - (d) flash process gate application

PROBLEMS

Answers to odd-numbered problems are at the end of the chapter.

SECTION 1 Digital and Analog Signals and Systems

1. Name two advantages of digital data as compared to analog data.
2. Name an analog quantity other than temperature and sound.
3. List three common products that can have either a digital or analog output.

SECTION 2 Binary Digits, Logic Levels, and Digital Waveforms

4. Explain the difference between positive and negative logic.
5. Define the sequence of bits (1s and 0s) represented by each of the following sequences of levels:
 - (a) HIGH, HIGH, LOW, HIGH, LOW, LOW, LOW, HIGH
 - (b) LOW, LOW, LOW, HIGH, LOW, HIGH, LOW, HIGH, LOW
6. List the sequence of levels (HIGH and LOW) that represent each of the following bit sequences:
 - (a) 1 0 1 1 1 0 1
 - (b) 1 1 1 0 1 0 0 1
7. For the pulse shown in Figure 62, graphically determine the following:
 - (a) rise time
 - (b) fall time
 - (c) pulse width
 - (d) amplitude
8. Determine the period of the digital waveform in Figure 63.
9. What is the frequency of the waveform in Figure 63?
10. Is the pulse waveform in Figure 63 periodic or nonperiodic?
11. Determine the duty cycle of the waveform in Figure 63.

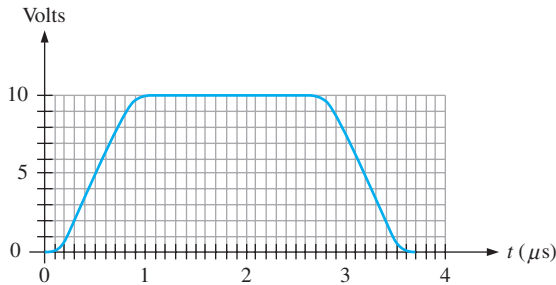


FIGURE 62

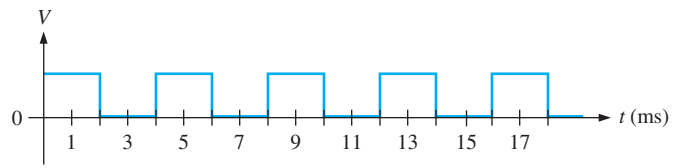


FIGURE 63

12. Determine the bit sequence represented by the waveform in Figure 64. A bit time is $1 \mu\text{s}$ in this case.
13. What is the total serial transfer time for the eight bits in Figure 64? What is the total parallel transfer time?
14. What is the period if the clock frequency is 3.5 GHz?

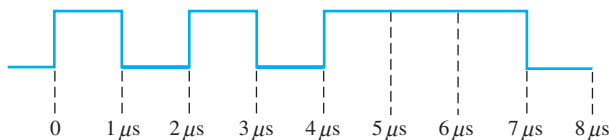


FIGURE 64

SECTION 3 Logic Operations

15. Form a single logical statement from the following information:
 - (a) The light is ON if SW1 is closed.
 - (b) The light is ON if SW2 is closed.
 - (c) The light is OFF if both SW1 and SW2 are open.
16. A logic circuit requires HIGHS on all its inputs to make the output HIGH. What type of logic circuit is it?
17. A basic 2-input logic circuit has a HIGH on one input and a LOW on the other input, and the output is LOW. Identify the circuit.
18. A basic 2-input logic circuit has a HIGH on one input and a LOW on the other input, and the output is HIGH. What type of logic circuit is it?

SECTION 4 Combinational and Sequential Logic Functions

19. Name the logic function of each block in Figure 65 based on your observation of the inputs and outputs.

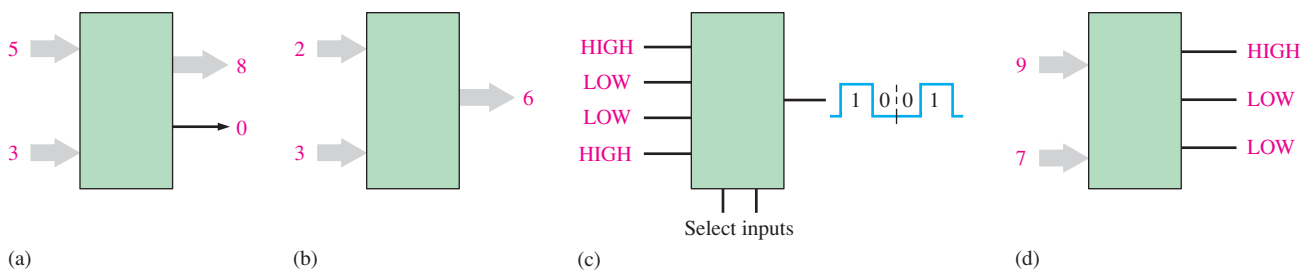


FIGURE 65

20. A pulse waveform with a frequency of 10 kHz is applied to the input of a counter. During 100 ms, how many pulses are counted?
21. Consider a register that can store eight bits. Assume that it has been reset so that it contains zeros in all positions. If you transfer four alternating bits (0101) serially into the register, beginning with a 1 and shifting to the right, what will the total content of the register be as soon as the fourth bit is stored?

SECTION 5 Programmable Logic

22. Which of the following acronyms do not describe a type of programmable logic?
PAL, GAL, SPLD, VHDL, CPLD, AHDL, FPGA
23. What do each of the following stand for?
(a) SPLD (b) CPLD (c) HDL (d) FPGA (e) GAL
24. Define each of the following PLD programming terms:
(a) design entry (b) simulation (c) compilation (d) download
25. Describe the process of place-and-route.

SECTION 6 Fixed-Function Logic Devices

26. A fixed-function digital IC chip has a complexity of 200 equivalent gates. How is it classified?
27. Explain the main difference between the DIP and SMT packages.
28. Label the pin numbers on the packages in Figure 66. Top views are shown.

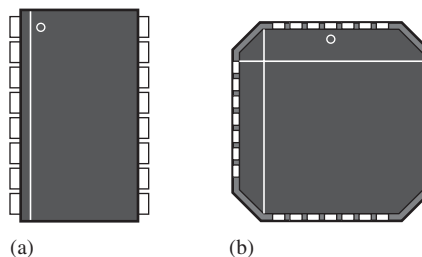


FIGURE 66

SECTION 7 A System

29. List three ways that the tablet-bottling system in Figure 45 can be implemented.
30. Which function(s) determines when each bottle is full?
31. Identify the purpose of each register in Figure 45.

SECTION 8 Measuring Instruments

32. A pulse is displayed on the screen of an oscilloscope, and you measure the base line as 1 V and the top of the pulse as 8 V. What is the amplitude?
33. A waveform is measured on the oscilloscope and its amplitude covers three vertical divisions. If the vertical control is set at 2 V/div, what is the total amplitude of the waveform?
34. The period of a pulse waveform measures four horizontal divisions on an oscilloscope. If the time base is set at 2 ms/div, what is the frequency of the waveform?

ANSWERS TO SECTION CHECKUPS**SECTION 1 Digital and Analog Signals and Systems**

1. *Analog* means continuous.
2. *Digital* means discrete.
3. A digital quantity has a discrete set of values and an analog quantity has continuous values.
4. A public address system is analog. A CD player is analog and digital. A computer is all digital.

SECTION 2 Binary Digits, Logic Levels, and Digital Waveforms

1. Binary means having two states or values.
2. A bit is a binary digit.
3. The bits are 1 and 0.
4. Rise time: from 10% to 90% of amplitude. Fall time: from 90% to 10% of amplitude.
5. Frequency is the reciprocal of the period.
6. A clock waveform is a basic timing waveform from which other waveforms are derived.
7. A timing diagram shows the time relationship of two or more waveforms.
8. Parallel transfer is faster than serial transfer.

SECTION 3 Logic Operations

1. When the input is LOW
2. When all inputs are HIGH
3. When any or all inputs are HIGH
4. An inverter is a NOT circuit.
5. A logic gate is a circuit that performs a logic operation (AND, OR).

SECTION 4 Combinational and Sequential Logic Functions

1. A comparator compares the magnitudes of two input numbers.
2. Add, subtract, multiply, and divide
3. Encoding is changing a familiar form such as decimal to a coded form such as binary.
4. Decoding is changing a code to a familiar form such as binary to decimal.
5. Multiplexing puts data from many sources onto one line. Demultiplexing takes data from one line and distributes it to many destinations.
6. Flip-flops, registers, semiconductor memories, magnetic disks
7. A counter counts events with a sequence of binary states.

SECTION 5 Programmable Logic

1. Simple programmable logic device (SPLD), complex programmable logic device (CPLD), and field-programmable gate array (FPGA)
2. A CPLD is made up of multiple SPLDs.

3. Design entry, functional simulation, synthesis, implementation, timing simulation, and download
4. *Design entry*: The logic design is entered using development software. *Functional simulation*: The design is software simulated to make sure it works logically. *Synthesis*: The design is translated into a netlist. *Implementation*: The logic developed by the netlist is mapped into the programmable device. *Timing simulation*: The design is software simulated to confirm that there are no timing problems. *Download*: The design is placed into the programmable device.
5. The microcontroller has fixed internal circuits, and its operation is directed by a program.

SECTION 6 Fixed-Function Logic Devices

1. An IC is an electronic circuit with all components integrated on a single silicon chip.
2. DIP—dual in-line package; SMT—surface-mount technology; SOIC—small-outline integrated circuit; SSI—small-scale integration; MSI—medium-scale integration; LSI—large-scale integration; VLSI—very large-scale integration.
3. (a) SSI (b) MSI (c) LSI (d) VLSI (e) ULSI

SECTION 7 A System

1. Number of tablets is entered via keypad.
2. The system counts tablets and compares to preset number to determine when a bottle is full.
3. Counter is reset after maximum count and when next bottle is in place.

SECTION 8 Measuring Instruments

1. The analog scope applies the measured waveform directly to the display circuits. The digital scope first converts the measured signal to digital form.
2. The logic analyzer has more channels than the oscilloscope and has more than one data display format.
3. The volts/div control sets the voltage for each division on the screen.
4. The sec/div control sets the time for each division on the screen.
5. The function generator produces various types of waveforms.

ANSWERS TO RELATED PROBLEMS FOR EXAMPLES

- 1 $f = 6.67 \text{ kHz}$; Duty cycle = 16.7%
- 2 Serial transfer: 3.33 ns
- 3 Amplitude = 12 V; $T = 8 \text{ ms}$

ANSWERS TO TRUE/FALSE QUIZ

1. T 2. F 3. T 4. T 5. F 6. F
7. T 8. F 9. T 10. T 11. F 12. T

ANSWERS TO SELF-TEST

1. (b) 2. (d) 3. (a) 4. (c) 5. (c) 6. (d) 7. (b) 8. (d)
9. (c) 10. (e) 11. (d) 12. (d) 13. (b) 14. (c) 15. (a)

ANSWERS TO ODD-NUMBERED PROBLEMS

1. Digital can be transmitted and stored more efficiently and reliably.
3. Clock
Thermometer
Speedometer
5. (a) 11010001 (b) 000101010
7. (a) 550 ns (b) 600 ns (c) 2.7 μ s (d) 10 V
9. 250 Hz
11. 50%
13. 8 μ s; 1 μ s
15. $L_{\text{on}} = SW1 + SW2 + SW1 \cdot SW2$
17. AND gate
19. (a) adder (b) multiplier
(c) multiplexer (d) comparator
21. 01010000
23. (a) Simple Programmable Logic Device
(b) Complex Programmable Logic Device
(c) Hardware Description Language
(d) Field-Programmable Gate Array
(e) Generic Array Logic
25. Place-and-route or fitting is the process where the logic structures described by the netlist are mapped into the actual structure of the specific target device. This results in an output called a bitstream.
27. DIP pins go through holes in a circuit board. SMT pins connect to surface pads.
29. The system can be implemented with a PLD, a microcontroller, or with fixed-function ICs.
31. Register A stores the maximum number of tablets/bottle. Register B stores the cumulative total of tablets bottled.
33. 6 V

NUMBER SYSTEMS, OPERATIONS, AND CODES

OUTLINE

- 1 The Decimal Number System
- 2 The Binary Number System
- 3 Decimal-to-Binary Conversion
- 4 Binary Arithmetic
- 5 1's and 2's Complements of Binary Numbers
- 6 Signed Numbers
- 7 Arithmetic Operations with Signed Numbers
- 8 Hexadecimal Numbers
- 9 Octal Numbers
- 10 Binary Coded Decimal (BCD)
- 11 Digital Codes
- 12 Error Detection Codes

OBJECTIVES

- Review the decimal number system
- Count in the binary number system
- Convert from decimal to binary and from binary to decimal
- Apply arithmetic operations to binary numbers
- Determine the 1's and 2's complements of a binary number
- Express signed binary numbers in sign-magnitude, 1's complement, 2's complement, and floating-point format
- Carry out arithmetic operations with signed binary numbers
- Convert between the binary and hexadecimal number systems

- Add numbers in hexadecimal form
- Convert between the binary and octal number systems
- Express decimal numbers in binary coded decimal (BCD) form
- Add BCD numbers
- Convert between the binary system and the Gray code
- Interpret the American Standard Code for Information Interchange (ASCII)
- Explain how to detect code errors
- Discuss the cyclic redundancy check (CRC)

KEY TERMS

LSB

MSB

Byte

Floating-point number

Hexadecimal

Octal

BCD

Alphanumeric

ASCII

Parity

Cyclic redundancy check (CRC)

INTRODUCTION

The binary number system and digital codes are fundamental to computers and to digital electronics in general. In this chapter, the binary number system and its relationship to

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Study aids for this chapter are available at <http://pearsonhighered.com/floyd>

other number systems such as decimal, hexadecimal, and octal is presented. Arithmetic operations with binary numbers are covered to provide a basis for understanding how computers and many other types of digital systems work. Also, digital codes such as binary coded decimal (BCD),

the Gray code, and the ASCII are covered. The parity method for detecting errors in codes is introduced. The tutorials on the use of the calculator in certain operations are based on the TI-36X calculator. The procedures shown may vary on other types.

1 THE DECIMAL NUMBER SYSTEM

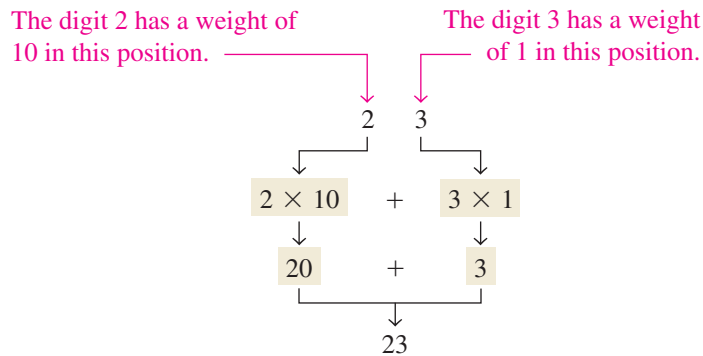
You are familiar with the decimal number system because you use decimal numbers every day. Although decimal numbers are commonplace, their weighted structure is often not understood. In this section, the structure of decimal numbers is reviewed. This review will help you more easily understand the structure of the binary number system, which is important in computers and digital electronics.

After completing this section, you should be able to

- Explain why the decimal number system is a weighted system
- Explain how powers of ten are used in the decimal system
- Determine the weight of each digit in a decimal number

The decimal number system has ten digits.

In the **decimal*** number system each of the ten digits, 0 through 9, represents a certain quantity. As you know, the ten symbols (**digits**) do not limit you to expressing only ten different quantities because you use the various digits in appropriate positions within a number to indicate the magnitude of the quantity. You can express quantities up through nine before running out of digits; if you wish to express a quantity greater than nine, you use two or more digits, and the position of each digit within the number tells you the magnitude it represents. If, for example, you wish to express the quantity twenty-three, you use (by their respective positions in the number) the digit 2 to represent the quantity twenty and the digit 3 to represent the quantity three, as illustrated below.



The decimal number system has a base of 10.

The position of each digit in a decimal number indicates the magnitude of the quantity represented and can be assigned a **weight**. The weights for whole numbers are positive powers of ten that increase from right to left, beginning with $10^0 = 1$.

$$\dots 10^5 10^4 10^3 10^2 10^1 10^0$$

For fractional numbers, the weights are negative powers of ten that decrease from left to right beginning with 10^{-1} .

$$10^2 10^1 10^0 . 10^{-1} 10^{-2} 10^{-3} \dots$$

Decimal point

*The bold terms in color are key terms and are included in a Key Term glossary at the end of the chapter.

The value of a decimal number is the sum of the digits after each digit has been multiplied by its weight, as Examples 1 and 2 illustrate.

The value of a digit is determined by its position in the number.

EXAMPLE 1

Express the decimal number 47 as a sum of the values of each digit.

SOLUTION

The digit 4 has a weight of 10, which is 10^1 , as indicated by its position. The digit 7 has a weight of 1, which is 10^0 , as indicated by its position.

$$\begin{aligned} 47 &= (4 \times 10^1) + (7 \times 10^0) \\ &= (4 \times 10) + (7 \times 1) = \mathbf{40 + 7} \end{aligned}$$

RELATED PROBLEM*

Determine the value of each digit in 939.

*Answers are at the end of the chapter.

EXAMPLE 2

Express the decimal number 568.23 as a sum of the values of each digit.

SOLUTION

The whole number digit 5 has a weight of 100, which is 10^2 , the digit 6 has a weight of 10, which is 10^1 , the digit 8 has a weight of 1, which is 10^0 , the fractional digit 2 has a weight of 0.1, which is 10^{-1} , and the fractional digit 3 has a weight of 0.01, which is 10^{-2} .

$$\begin{aligned} 568.23 &= (5 \times 10^2) + (6 \times 10^1) + (8 \times 10^0) + (2 \times 10^{-1}) + (3 \times 10^{-2}) \\ &= (5 \times 100) + (6 \times 10) + (8 \times 1) + (2 \times 0.1) + (3 \times 0.01) \\ &= \mathbf{500 + 60 + 8 + 0.2 + 0.03} \end{aligned}$$

RELATED PROBLEM

Determine the value of each digit in 67.924.

CALCULATOR TUTORIAL

Powers of Ten

EXAMPLE

Find the value of 10^3 .

TI-36X Step 1: **1** **0** y^x

Step 2: **3** **=**

1000

SECTION 1 CHECKUP*

- What weight does the digit 7 have in each of the following numbers?
(a) 1370 (b) 6725 (c) 7051 (d) 58.72
- Express each of the following decimal numbers as a sum of the products obtained by multiplying each digit by its appropriate weight:
(a) 51 (b) 137 (c) 1492 (d) 106.58

*Answers are at the end of the chapter.

2 THE BINARY NUMBER SYSTEM

The binary number system is another way to represent quantities. It is less complicated than the decimal system because it has only two digits. The decimal system with its ten digits is a base-ten system; the binary system with its two digits is a base-two system. The two binary digits (bits) are 1 and 0. The position of a 1 or 0 in a binary number indicates its weight, or value within the number, just as the position of a decimal digit determines the value of that digit. The weights in a binary number are based on powers of two.

After completing this section, you should be able to

- Count in binary
- Determine the largest decimal number that can be represented by a given number of bits
- Convert a binary number to a decimal number

Counting in Binary

The binary number system has two digits (bits).

Learning to count in binary will help you to basically understand how digital circuits can be used to count events. This can be anything from counting items on an assembly line to counting operations in a computer. To learn to count in the binary system, first look at how you count in the decimal system. You start at zero and count up to nine before you run out of digits. You then start another digit position (to the left) and continue counting 10 through 99. At this point you have exhausted all two-digit combinations, so a third digit position is needed to count from 100 through 999.

The binary number system has a base of 2.

A comparable situation occurs when you count in binary, except that you have only two digits, called *bits*. Begin counting: 0, 1. At this point you have used both digits, so include another digit position and continue: 10, 11. You have now exhausted all combinations of two digits, so a third position is required. With three digit positions you can continue to count: 100, 101, 110, and 111. Now you need a fourth digit position to continue, and so on. A binary count of zero through fifteen is shown in Table 1. Notice the patterns with which the 1s and 0s alternate in each column.

The value of a bit is determined by its position in the number.

As you can see in Table 1, four bits are required to count from zero to 15. In general, with n bits you can count up to a number equal to $2^n - 1$.

$$\text{Largest decimal number} = 2^n - 1$$

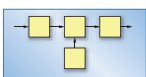
For example, with five bits ($n = 5$) you can count from zero to thirty-one.

$$2^5 - 1 = 32 - 1 = 31$$

With six bits ($n = 6$) you can count from zero to sixty-three.

$$2^6 - 1 = 64 - 1 = 63$$

A table of powers of two is given in the appendix “Conversions”.



In computer operations, there are many cases where adding or subtracting 1 to a number stored in a counter is necessary. Computers have special instructions that use less time and generate less machine code than the ADD or SUB instructions. For the Intel processors, the INC (increment) instruction adds 1 to a number. For subtraction, the corresponding instruction is DEC (decrement), which subtracts 1 from a number.

SYSTEM NOTE

TABLE 1				
DECIMAL NUMBER	BINARY NUMBER			
0	0	0	0	0
1	0	0	0	1
2	0	0	1	0
3	0	0	1	1
4	0	1	0	0
5	0	1	0	1
6	0	1	1	0
7	0	1	1	1
8	1	0	0	0
9	1	0	0	1
10	1	0	1	0
11	1	0	1	1
12	1	1	0	0
13	1	1	0	1
14	1	1	1	0
15	1	1	1	1

CALCULATOR TUTORIAL

Powers of Two

EXAMPLE

Find the value of 2^5 .

TI-36X Step 1: 2 y^x

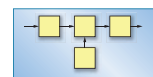
Step 2: 5 =

32

SYSTEM EXAMPLE 1

BALL-COUNTING SYSTEM

Figure 1 illustrates the counting of tennis balls that go into a box from a conveyor belt. Nine balls go into each box. The counter counts the pulses from a sensor that detects the passing of a ball and produces a sequence of logic levels (digital waveforms) on each of its four parallel outputs. Each set of logic levels represents a 4-bit binary number (HIGH = 1



and LOW = 0), as indicated. As the decoder receives these waveforms, it decodes each set of four bits and converts it to the corresponding decimal number in the 7-segment display. When the counter gets to the binary state of 1001, it has counted nine tennis balls, the display shows decimal 9, and a new box is moved under the conveyor. Then the counter goes back to its zero state (0000), and the process starts over. (The number 9 was used only in the interest of single-digit simplicity.)

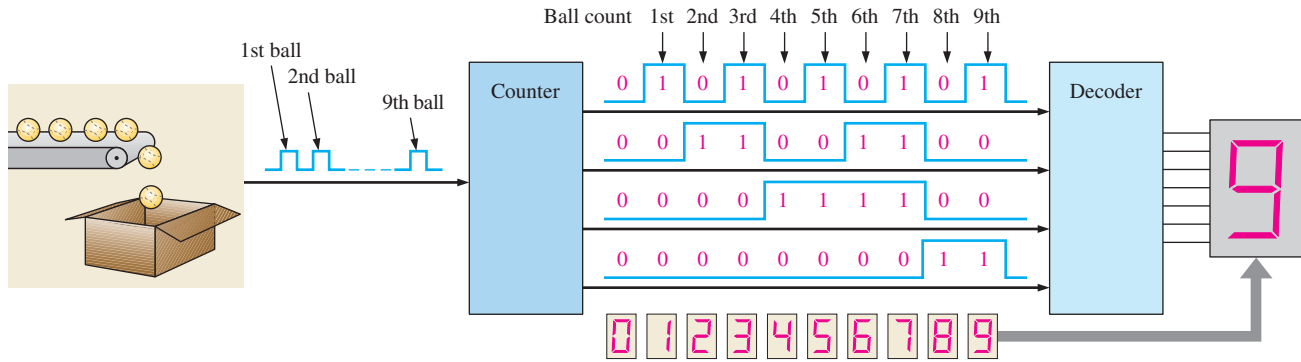


FIGURE 1 Illustration of a simple binary counting application.

The weight or value of a bit increases from right to left in a binary number.

The Weighting Structure of Binary Numbers

A binary number is a weighted number. The right-most bit is the **LSB** (least significant bit) in a binary whole number and has a weight of $2^0 = 1$. The weights increase from right to left by a power of two for each bit. The left-most bit is the **MSB** (most significant bit); its weight depends on the size of the binary number.

Fractional numbers can also be represented in binary by placing bits to the right of the binary point, just as fractional decimal digits are placed to the right of the decimal point. The left-most bit is the MSB in a binary fractional number and has a weight of $2^{-1} = 0.5$. The fractional weights decrease from left to right by a negative power of two for each bit.

The weight structure of a binary number is

$$2^{n-1} \dots 2^3 2^2 2^1 2^0 \cdot 2^{-1} 2^{-2} \dots 2^{-n}$$

↑ Binary point

where n is the number of bits from the binary point. Thus, all the bits to the left of the binary point have weights that are positive powers of two, as previously discussed for whole numbers. All bits to the right of the binary point have weights that are negative powers of two, or fractional weights.

Computers use binary numbers to select memory locations. Each location is assigned a unique number called an *address*. Some microprocessors, for example, have 32 address lines which can select 2^{32} (4,294,967,296) unique locations.

SYSTEM NOTE

The powers of two and their equivalent decimal weights for an 8-bit binary whole number and a 6-bit binary fractional number are shown in Table 2. Notice that the weight doubles for each positive power of two and that the weight is halved for each negative power of two. You can easily extend the table by doubling the weight of the most significant positive power of two and halving the weight of the least significant negative power of two; for example, $2^9 = 512$ and $2^{-7} = 0.0078125$.

TABLE 2 • Binary weights.

POSITIVE POWERS OF TWO (WHOLE NUMBERS)									NEGATIVE POWERS OF TWO (FRACTIONAL NUMBER)					
2^8	2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0	2^{-1}	2^{-2}	2^{-3}	2^{-4}	2^{-5}	2^{-6}
256	128	64	32	16	8	4	2	1	1/2	1/4	1/8	1/16	1/32	1/64
									0.5	0.25	0.125	0.625	0.03125	0.015625

Binary-to-Decimal Conversion

The decimal value of any binary number can be found by adding the weights of all bits that are 1 and discarding the weights of all bits that are 0.

Add the weights of all 1s in a binary number to get the decimal value.

EXAMPLE 3

Convert the binary whole number 1101101 to decimal.

SOLUTION

Determine the weight of each bit that is a 1, and then find the sum of the weights to get the decimal number.

$$\begin{array}{r}
 \text{Weight: } 2^6 \ 2^5 \ 2^4 \ 2^3 \ 2^2 \ 2^1 \ 2^0 \\
 \text{Binary number: } 1 \ 1 \ 0 \ 1 \ 1 \ 0 \ 1 \\
 1101101 = 2^6 + 2^5 + 2^3 + 2^2 + 2^0 \\
 = 64 + 32 + 8 + 4 + 1 = \mathbf{109}
 \end{array}$$

RELATED PROBLEM

Convert the binary number 10010001 to decimal.

EXAMPLE 4

Convert the fractional binary number 0.1011 to decimal.

SOLUTION

Determine the weight of each bit that is a 1, and then sum the weights to get the decimal fraction.

$$\begin{array}{r}
 \text{Weight: } 2^{-1} \ 2^{-2} \ 2^{-3} \ 2^{-4} \\
 \text{Binary number: } 0.1 \ 0 \ 1 \ 1 \\
 0.1011 = 2^{-1} + 2^{-3} + 2^{-4} \\
 = 0.5 + 0.125 + 0.0625 = \mathbf{0.6875}
 \end{array}$$

RELATED PROBLEM

Convert the binary number 10.111 to decimal.

SECTION 2 CHECKUP

1. What is the largest decimal number that can be represented in binary with eight bits?
2. Determine the weight of the 1 in the binary number 10000.
3. Convert the binary number 10111101.011 to decimal.

3 DECIMAL-TO-BINARY CONVERSION

In Section 2 you learned how to convert a binary number to the equivalent decimal number. Now you will learn two ways of converting from a decimal number to a binary number.

After completing this section, you should be able to

- Convert a decimal number to binary using the sum-of-weights method
- Convert a decimal whole number to binary using the repeated division-by-2 method
- Convert a decimal fraction to binary using the repeated multiplication-by-2 method

To get the binary number for a given decimal number, find the binary weights that add up to the decimal number.

Sum-of-Weights Method

One way to find the binary number that is equivalent to a given decimal number is to determine the set of binary weights whose sum is equal to the decimal number. An easy way to remember binary weights is that the lowest is 1, which is 2^0 , and that by doubling any weight, you get the next higher weight; thus, a list of seven binary weights would be 64, 32, 16, 8, 4, 2, 1 as you learned in the last section. The decimal number 9, for example, can be expressed as the sum of binary weights as follows:

$$9 = 8 + 1 \text{ or } 9 = 2^3 + 2^0$$

Placing 1s in the appropriate weight positions, 2^3 and 2^0 , and 0s in the 2^2 and 2^1 positions determines the binary number for decimal 9.

$$\begin{array}{cccc} 2^3 & 2^2 & 2^1 & 2^0 \\ 1 & 0 & 0 & 1 \end{array} \text{ Binary number for decimal 9}$$

EXAMPLE 5

Convert the following decimal numbers to binary:

- (a) 12 (b) 25 (c) 58 (d) 82

SOLUTION

$$\text{(a) } 12 = 8 + 4 = 2^3 + 2^2 \longrightarrow \mathbf{1100}$$

$$\text{(b) } 25 = 16 + 8 + 1 = 2^4 + 2^3 + 2^0 \longrightarrow \mathbf{11001}$$

$$\text{(c) } 58 = 32 + 16 + 8 + 2 = 2^5 + 2^4 + 2^3 + 2^1 \longrightarrow \mathbf{111010}$$

$$\text{(d) } 82 = 64 + 16 + 2 = 2^6 + 2^4 + 2^1 \longrightarrow \mathbf{1010010}$$

RELATED PROBLEM

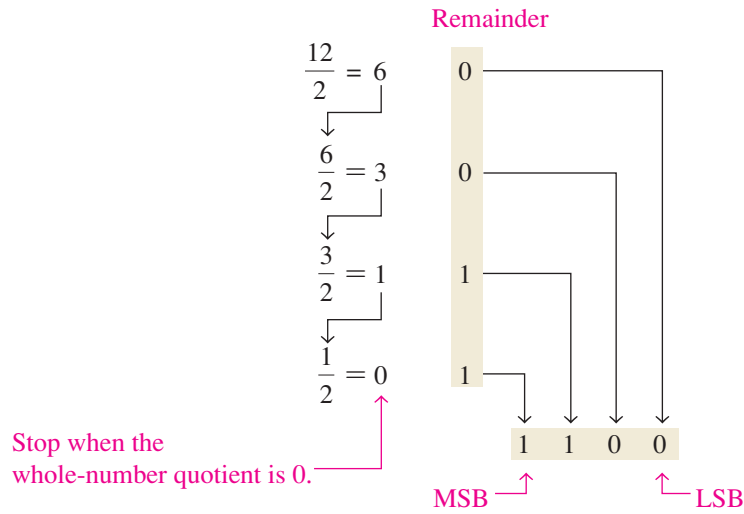
Convert the decimal number 125 to binary.

To get the binary number for a given decimal number, divide the decimal number by 2 until the quotient is 0. Remainders form the binary number.

Repeated Division-by-2 Method

A systematic method of converting whole numbers from decimal to binary is the *repeated division-by-2* process. For example, to convert the decimal number 12 to binary, begin by dividing 12 by 2. Then divide each resulting quotient by 2 until there is a 0 whole-number quotient. The **remainders** generated by each division form the binary number. The first remainder to be produced is the LSB (least significant bit) in the binary

number, and the last remainder to be produced is the MSB (most significant bit). This procedure is illustrated as follows for converting the decimal number 12 to binary.

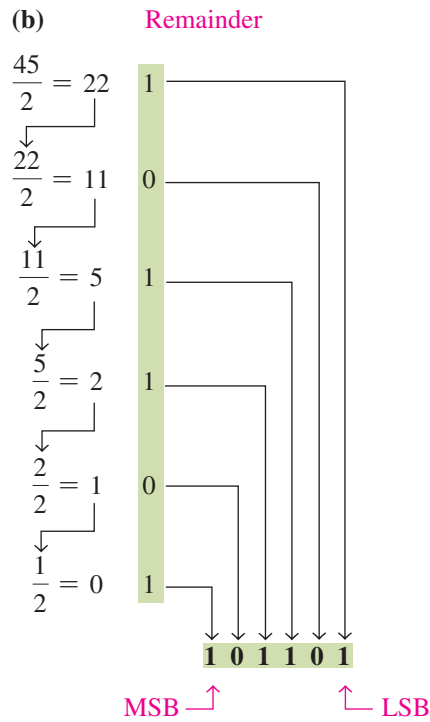
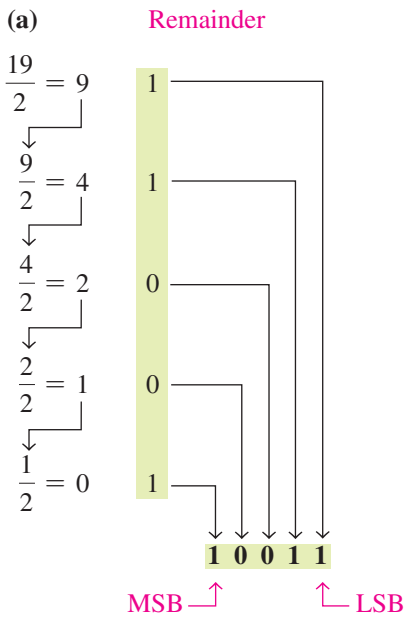


EXAMPLE 6

Convert the following decimal numbers to binary:

- (a) 19 (b) 45

SOLUTION



RELATED PROBLEM

Convert decimal number 39 to binary.

CALCULATOR TUTORIAL

Conversion of a Decimal Number to a Binary Number

EXAMPLE

Convert decimal 57 to binary.

TI-36X **Step 1:** 3rd EE DEC
 Step 2: 5 7
 Step 3: 3rd X BIN

111001

Converting Decimal Fractions to Binary

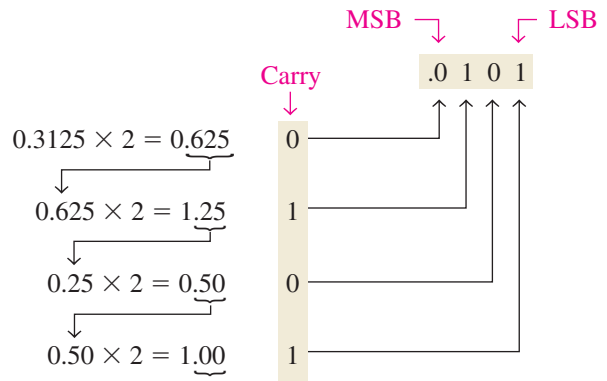
Examples 5 and 6 demonstrated whole-number conversions. Now let's look at fractional conversions. An easy way to remember fractional binary weights is that the most significant weight is 0.5, which is 2^{-1} , and that by halving any weight, you get the next lower weight; thus a list of four fractional binary weights would be 0.5, 0.25, 0.125, 0.0625.

SUM-OF-WEIGHTS The sum-of-weights method can be applied to fractional decimal numbers, as shown in the following example:

$$0.625 = 0.5 + 0.125 = 2^{-1} + 2^{-3} = 0.101$$

There is a 1 in the 2^{-1} position, a 0 in the 2^{-2} position, and a 1 in the 2^{-3} position.

REPEATED MULTIPLICATION BY 2 As you have seen, decimal whole numbers can be converted to binary by repeated division by 2. Decimal fractions can be converted to binary by repeated multiplication by 2. For example, to convert the decimal fraction 0.3125 to binary, begin by multiplying 0.3125 by 2 and then multiplying each resulting fractional part of the product by 2 until the fractional product is zero or until the desired number of decimal places is reached. The carry digits, or **carries**, generated by the multiplications produce the binary number. The first carry produced is the MSB, and the last carry is the LSB. This procedure is illustrated as follows:



Continue to the desired number of decimal places or stop when the fractional part is all zeros.

SECTION 3 CHECKUP

- Convert each decimal number to binary by using the sum-of-weights method:
 - 23
 - 57
 - 45.5
- Convert each decimal number to binary by using the repeated division-by-2 method (repeated multiplication-by-2 for fractions):
 - 14
 - 21
 - 0.375

4 BINARY ARITHMETIC

Binary arithmetic is essential in all digital computers and in many other types of digital systems. To understand digital systems, you must know the basics of binary addition, subtraction, multiplication, and division. This section provides an introduction that will be expanded in later sections.

After completing this section, you should be able to

- Add binary numbers
- Subtract binary numbers
- Multiply binary numbers
- Divide binary numbers

Binary Addition

The four basic rules for adding binary digits (bits) are as follows:

$0 + 0 = 0$	Sum of 0 with a carry of 0
$0 + 1 = 1$	Sum of 1 with a carry of 0
$1 + 0 = 1$	Sum of 1 with a carry of 0
$1 + 1 = 10$	Sum of 0 with a carry of 1

In binary $1 + 1 = 10$, not the decimal digit 2.

Notice that the first three rules result in a single bit and in the fourth rule the addition of two 1s yields a binary two (10). When binary numbers are added, the last condition creates a sum of 0 in a given column and a carry of 1 over to the next column to the left, as illustrated in the following addition of $11 + 1$:

$$\begin{array}{r}
 \text{Carry } 1 \quad \text{Carry } 1 \\
 \begin{array}{r}
 1 \leftarrow 1 \leftarrow 1 \\
 0 \quad 1 \quad 1 \\
 + 0 \quad 0 \quad 1 \\
 \hline
 1 \quad 0 \quad 0
 \end{array}
 \end{array}$$

In the right column, $1 + 1 = 0$ with a carry of 1 to the next column to the left. In the middle column, $1 + 1 + 0 = 0$ with a carry of 1 to the next column to the left. In the left column, $1 + 0 + 0 = 1$.

When there is a carry of 1, you have a situation in which three bits are being added (a bit in each of the two numbers and a carry bit). This situation is illustrated as follows:

Carry bits →

1	$+ 0 + 0 = 01$	Sum of 1 with a carry of 0
1	$+ 1 + 0 = 10$	Sum of 0 with a carry of 1
1	$+ 0 + 1 = 10$	Sum of 0 with a carry of 1
1	$+ 1 + 1 = 11$	Sum of 1 with a carry of 1

EXAMPLE 7

Add the following binary numbers:

- (a) $11 + 11$ (b) $100 + 10$ (c) $111 + 11$ (d) $110 + 100$

SOLUTION

The equivalent decimal addition is also shown for reference.

(a) $\begin{array}{r} 11 \\ +11 \\ \hline 110 \end{array}$	(b) $\begin{array}{r} 100 \\ +10 \\ \hline 110 \end{array}$	(c) $\begin{array}{r} 111 \\ +11 \\ \hline 1010 \end{array}$	(d) $\begin{array}{r} 110 \\ +100 \\ \hline 1010 \end{array}$
--	---	--	---

RELATED PROBLEM

Add 1111 and 1100.

In binary $10 - 1 = 1$,
not the decimal digit 9.

Binary Subtraction

The four basic rules for subtracting bits are as follows:

$$\begin{array}{l} 0 - 0 = 0 \\ 1 - 1 = 0 \\ 1 - 0 = 1 \\ 10 - 1 = 1 \quad 0 - 1 \text{ with a borrow of } 1 \end{array}$$

When subtracting numbers, you sometimes have to borrow from the next column to the left. A borrow is required in binary only when you try to subtract a 1 from a 0. In this case, when a 1 is borrowed from the next column to the left, a 10 is created in the column being subtracted, and the last of the four basic rules just listed must be applied. Examples 8 and 9 illustrate binary subtraction; the equivalent decimal subtractions are also shown.

EXAMPLE 8

Perform the following binary subtractions:

- (a) $11 - 01$ (b) $11 - 10$

SOLUTION

(a) $\begin{array}{r} 11 \\ -01 \\ \hline 10 \end{array}$	(b) $\begin{array}{r} 11 \\ -10 \\ \hline 01 \end{array}$
---	---

No borrows were required in this example. The binary number 01 is the same as 1.

RELATED PROBLEM

Subtract 100 from 111.

EXAMPLE 9

Subtract 011 from 101.

SOLUTION

$$\begin{array}{r} 101 \\ -011 \\ \hline 010 \end{array}$$

Let's examine exactly what was done to subtract the two binary numbers since a borrow is required. Begin with the right column.

Left column: When a 1 is borrowed, a 0 is left, so $0 - 0 = 0$.

Middle column: Borrow 1 from next column to the left, making a 10 in this column, then $10 - 1 = 1$.

Right column: $1 - 1 = 0$

$$\begin{array}{r} 0 \\ \cancel{1}01 \\ -011 \\ \hline 010 \end{array}$$

RELATED PROBLEM

Subtract 101 from 110.

Binary Multiplication

The four basic rules for multiplying bits are as follows:

- $0 \times 0 = 0$
- $0 \times 1 = 0$
- $1 \times 0 = 0$
- $1 \times 1 = 1$

Binary multiplication of two bits is the same as multiplication of the decimal digits 0 and 1.

Multiplication is performed with binary numbers in the same manner as with decimal numbers. It involves forming partial products, shifting each successive partial product left one place, and then adding all the partial products. Example 10 illustrates the procedure; the equivalent decimal multiplications are shown for reference.

EXAMPLE 10

Perform the following binary multiplications:

- (a) 11×11 (b) 101×111

SOLUTION

(a)

$\times 11$	11	3
\hline	11	9
Partial products {	$+11$	
	\hline	
	1001	

(b)

$\times 101$	111	7
\hline	111	35
Partial products {	000	
	$+111$	
	\hline	
	100011	

RELATED PROBLEM

Multiply 1101×1010 .

Binary Division

Division in binary follows the same procedure as division in decimal, as Example 11 illustrates. The equivalent decimal divisions are also given.

EXAMPLE 11

Perform the following binary divisions:

- (a) $110 \div 11$ (b) $110 \div 10$

SOLUTION

$\begin{array}{r} 10 \quad 2 \\ 11 \overline{)110} \quad 3 \overline{)6} \\ \underline{11} \quad \quad \underline{6} \\ 000 \quad \quad 0 \end{array}$	$\begin{array}{r} 11 \quad 3 \\ 10 \overline{)110} \quad 2 \overline{)6} \\ \underline{10} \quad \quad \underline{6} \\ 10 \quad \quad 0 \\ \underline{10} \\ 00 \end{array}$
--	---

RELATED PROBLEM

Divide 1100 by 100.

SECTION 4 CHECKUP

- | | |
|--|---|
| <p>1. Perform the following binary additions:</p> <p>(a) $1101 + 1010$ (b) $10111 + 01101$</p> <p>2. Perform the following binary subtractions:</p> <p>(a) $1101 - 0100$ (b) $1001 - 0111$</p> | <p>3. Perform the indicated binary operations:</p> <p>(a) 110×111 (b) $1100 \div 011$</p> |
|--|---|

5 1'S AND 2'S COMPLEMENTS OF BINARY NUMBERS

The 1's complement and the 2's complement of a binary number are important because they permit the representation of negative numbers. The method of 2's complement arithmetic is commonly used in computers to handle negative numbers.

After completing this section, you should be able to

- Convert a binary number to its 1's complement
- Convert a binary number to its 2's complement using either of two methods

Finding the 1's Complement

The 1's **complement** of a binary number is found by changing all 1s to 0s and all 0s to 1s, as illustrated below:

1 0 1 1 0 0 1 0	Binary number
↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓	
0 1 0 0 1 1 0 1	1's complement

The simplest way to obtain the 1's complement of a binary number with a digital circuit is to use parallel inverters (NOT circuits), as shown in Figure 2 for an 8-bit binary number.

Change each bit in a number to get the 1's complement.

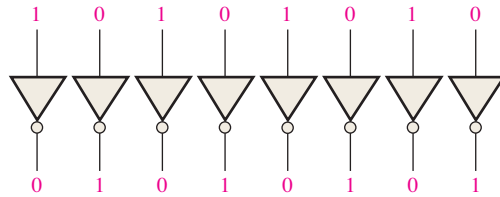


FIGURE 2 Example of inverters used to obtain the 1's complement of a binary number.

Finding the 2's Complement

The 2's complement of a binary number is found by adding 1 to the LSB of the 1's complement.

Add 1 to the 1's complement to get the 2's complement.

$$2's\ complement = (1's\ complement) + 1$$

EXAMPLE 12

Find the 2's complement of 10110010.

SOLUTION

10110010	Binary number
01001101	1's complement
+ 1	Add 1
01001110	2's complement

RELATED PROBLEM

Determine the 2's complement of 11001011.

An alternative method of finding the 2's complement of a binary number is as follows:

1. Start at the right with the LSB and write the bits as they are up to and including the first 1.
2. Take the 1's complements of the remaining bits.

Change all bits to the left of the least significant 1 to get 2's complement.

EXAMPLE 13

Find the 2's complement of 10111000 using the alternative method.

SOLUTION

	10111000	Binary number
1's complements of original bits	01001000	2's complement
		These bits stay the same.

RELATED PROBLEM

Find the 2's complement of 11000000.

The 2's complement of a negative binary number can be realized using inverters and an adder, as indicated in Figure 3. This illustrates how an 8-bit number can be converted to its 2's complement by first inverting each bit (taking the 1's complement) and then adding 1 to the 1's complement with an adder circuit.

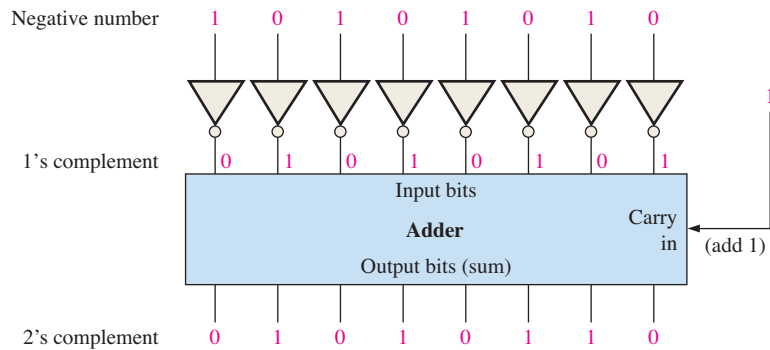


FIGURE 3 Example of obtaining the 2's complement of a negative binary number.

To convert from a 1's or 2's complement back to the true (uncomplemented) binary form, use the same two procedures described previously. To go from the 1's complement back to true binary, reverse all the bits. To go from the 2's complement form back to true binary, take the 1's complement of the 2's complement number and add 1 to the least significant bit.

SECTION 5 CHECKUP

- Determine the 1's complement of each binary number:
 (a) 00011010 (b) 11110111 (c) 10001101
- Determine the 2's complement of each binary number:
 (a) 00010110 (b) 11111100 (c) 10010001

6 SIGNED NUMBERS

Digital systems, such as the computer, must be able to handle both positive and negative numbers. A signed binary number consists of both sign and magnitude information. The sign indicates whether a number is positive or negative, and the magnitude is the value of the number. There are three forms in which signed integer (whole) numbers can be represented in binary: sign-magnitude, 1's complement, and 2's complement. Of these, the 2's complement is the most important and the sign-magnitude is the least used. Noninteger and very large or small numbers can be expressed in floating-point format.

After completing this section, you should be able to

- Express positive and negative numbers in sign-magnitude
- Express positive and negative numbers in 1's complement
- Express positive and negative numbers in 2's complement
- Determine the decimal value of signed binary numbers
- Express a binary number in floating-point format

The Sign Bit

The left-most bit in a signed binary number is the **sign bit**, which tells you whether the number is positive or negative.

A 0 sign bit indicates a positive number, and a 1 sign bit indicates a negative number.

Sign-Magnitude Form

When a signed binary number is represented in sign-magnitude, the left-most bit is the sign bit and the remaining bits are the magnitude bits. The magnitude bits are in true (uncomplemented) binary for both positive and negative numbers. For example, the decimal number +25 is expressed as an 8-bit signed binary number using the sign-magnitude form as

00011001
 Sign bit \leftarrow \leftarrow \leftarrow \leftarrow \leftarrow \leftarrow \leftarrow \leftarrow Magnitude bits

The decimal number -25 is expressed as

10011001

Notice that the only difference between +25 and -25 is the sign bit because the magnitude bits are in true binary for both positive and negative numbers.

In the sign-magnitude form, a negative number has the same magnitude bits as the corresponding positive number but the sign bit is a 1 rather than a zero.

1's Complement Form

Positive numbers in 1's complement form are represented the same way as the positive sign-magnitude numbers. Negative numbers, however, are the 1's complements of the corresponding positive numbers. For example, using eight bits, the decimal number -25 is expressed as the 1's complement of +25 (00011001) as

11100110

In the 1's complement form, a negative number is the 1's complement of the corresponding positive number.

2's Complement Form

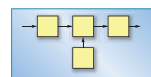
Positive numbers in 2's complement form are represented the same way as in the sign-magnitude and 1's complement forms. Negative numbers are the 2's complements of the corresponding positive numbers. Again, using eight bits, let's take decimal number -25 and express it as the 2's complement of +25 (00011001). Inverting each bit and adding 1, you get

$-25 = 11100111$

In the 2's complement form, a negative number is the 2's complement of the corresponding positive number.

Computers use the 2's complement for negative integer numbers in arithmetic operations. The reason is that subtraction of a number is the same as adding the 2's complement of the number. Computers form the 2's complement by inverting the bits and adding 1, using special instructions that produce the same result as the adder in Figure 3.

SYSTEM NOTE



EXAMPLE 14

Express the decimal number -39 as an 8-bit number in the sign-magnitude, 1's complement, and 2's complement forms.

SOLUTION

First, write the 8-bit number for $+39$.

$$00100111$$

In the *sign-magnitude form*, -39 is produced by changing the sign bit to a 1 and leaving the magnitude bits as they are. The number is

$$10100111$$

In the *1's complement form*, -39 is produced by taking the 1's complement of $+39$ (00100111).

$$11011000$$

In the *2's complement form*, -39 is produced by taking the 2's complement of $+39$ (00100111) as follows:

$$\begin{array}{r} 11011000 \quad 1's \text{ complement} \\ + \quad \quad 1 \\ \hline 11011001 \quad 2's \text{ complement} \end{array}$$

RELATED PROBLEM

Express $+19$ and -19 as 8-bit numbers in sign-magnitude, 1's complement, and 2's complement.

The Decimal Value of Signed Numbers

SIGN-MAGNITUDE Decimal values of positive and negative numbers in the sign-magnitude form are determined by summing the weights in all the magnitude bit positions where there are 1s and ignoring those positions where there are zeros. The sign is determined by examination of the sign bit.

EXAMPLE 15

Determine the decimal value of this signed binary number expressed in sign-magnitude: 10010101.

SOLUTION

The seven magnitude bits and their powers-of-two weights are as follows:

$$\begin{array}{ccccccc} 2^6 & 2^5 & 2^4 & 2^3 & 2^2 & 2^1 & 2^0 \\ 0 & 0 & 1 & 0 & 1 & 0 & 1 \end{array}$$

Summing the weights where there are 1s,

$$16 + 4 + 1 = 21$$

The sign bit is 1; therefore, the decimal number is **-21** .

RELATED PROBLEM

Determine the decimal value of the sign-magnitude number 01110111.

1'S COMPLEMENT Decimal values of positive numbers in the 1's complement form are determined by summing the weights in all bit positions where there are 1s and ignoring those positions where there are zeros. Decimal values of negative numbers are determined by assigning a negative value to the weight of the sign bit, summing all the weights where there are 1s, and adding 1 to the result.

EXAMPLE 16

Determine the decimal values of the signed binary numbers expressed in 1's complement:

- (a) 00010111 (b) 11101000

SOLUTION

- (a) The bits and their powers-of-two weights for the positive number are as follows:

$$\begin{array}{cccccccc}
 -2^7 & 2^6 & 2^5 & 2^4 & 2^3 & 2^2 & 2^1 & 2^0 \\
 0 & 0 & 0 & 1 & 0 & 1 & 1 & 1
 \end{array}$$

Summing the weights where there are 1s,

$$16 + 4 + 2 + 1 = +23$$

- (b) The bits and their powers-of-two weights for the negative number are as follows. Notice that the negative sign bit has a weight of -2^7 or -128 .

$$\begin{array}{cccccccc}
 -2^7 & 2^6 & 2^5 & 2^4 & 2^3 & 2^2 & 2^1 & 2^0 \\
 1 & 1 & 1 & 0 & 1 & 0 & 0 & 0
 \end{array}$$

Summing the weights where there are 1s,

$$-128 + 64 + 32 + 8 = -24$$

Adding 1 to the result, the final decimal number is

$$-24 + 1 = -23$$

RELATED PROBLEM

Determine the decimal value of the 1's complement number 11101011.

2'S COMPLEMENT Decimal values of positive and negative numbers in the 2's complement form are determined by summing the weights in all bit positions where there are 1s and ignoring those positions where there are zeros. The weight of the sign bit in a negative number is given a negative value.

EXAMPLE 17

Determine the decimal values of the signed binary numbers expressed in 2's complement:

- (a) 01010110 (b) 10101010

SOLUTION

- (a) The bits and their powers-of-two weights for the positive number are as follows:

$$\begin{array}{cccccccc}
 -2^7 & 2^6 & 2^5 & 2^4 & 2^3 & 2^2 & 2^1 & 2^0 \\
 0 & 1 & 0 & 1 & 0 & 1 & 1 & 0
 \end{array}$$

Summing the weights where there are 1s,

$$64 + 16 + 4 + 2 = +86$$

(b) The bits and their powers-of-two weights for the negative number are as follows. Notice that the negative sign bit has a weight of $-2^7 = -128$.

-2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
1	0	1	0	1	0	1	0

Summing the weights where there are 1s,

$$-128 + 32 + 8 + 2 = -86$$

RELATED PROBLEM

Determine the decimal value of the 2's complement number 11010111.

From these examples, you can see why the 2's complement form is preferred for representing signed integer numbers: To convert to decimal, it simply requires a summation of weights regardless of whether the number is positive or negative. The 1's complement system requires adding 1 to the summation of weights for negative numbers but not for positive numbers. Also, the 1's complement form is generally not used because two representations of zero (00000000 or 11111111) are possible.

Range of Signed Integer Numbers

The range of magnitude of a binary number depends on the number of bits (n).

We have used 8-bit numbers for illustration because the 8-bit grouping is common in most computers and has been given the special name **byte**. With one byte or eight bits, you can represent 256 different numbers. With two bytes or sixteen bits, you can represent 65,536 different numbers. With four bytes or 32 bits, you can represent $4,295 \times 10^9$ different numbers. The formula for finding the number of different combinations of n bits is

$$\text{Total combinations} = 2^n$$

For 2's complement signed numbers, the range of values for n -bit numbers is

$$\text{Range} = -(2^{n-1}) \text{ to } +(2^{n-1} - 1)$$

where in each case there is one sign bit and $n - 1$ magnitude bits. For example, with four bits you can represent numbers in 2's complement ranging from $-(2^3) = -8$ to $2^3 - 1 = +7$. Similarly, with eight bits you can go from -128 to $+127$, with sixteen bits you can go from $-32,768$ to $+32,767$, and so on. There is one less positive number than there are negative numbers because zero is represented as a positive number (all zeros).

Floating-Point Numbers

To represent very large **integer** (whole) numbers, many bits are required. There is also a problem when numbers with both integer and fractional parts, such as 23.5618, need to be represented. The floating-point number system, based on scientific notation, is capable of representing very large and very small numbers without an increase in the number of bits and also for representing numbers that have both integer and fractional components.

A **floating-point number** (also known as a *real number*) consists of two parts plus a sign. The **mantissa** is the part of a floating-point number that represents the magnitude of the number and is between 0 and 1. The **exponent** is the part of a floating-point number that represents the number of places that the decimal point (or binary point) is to be moved.

A decimal example will be helpful in understanding the basic concept of floating-point numbers. Let's consider a decimal number which, in integer form, is 241,506,800. The mantissa is .2415068 and the exponent is 9. When the integer is expressed as a floating-point number, it is normalized by moving the decimal point to the left of all the digits so

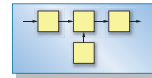
that the mantissa is a fractional number and the exponent is the power of ten. The floating-point number is written as

$$0.2415068 \times 10^9$$

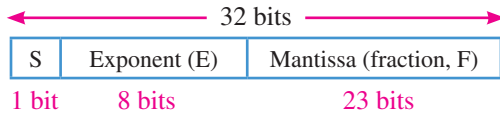
For binary floating-point numbers, the format is defined by ANSI/IEEE Standard 754-1985 in three forms: *single-precision*, *double-precision*, and *extended-precision*. These all have the same basic formats except for the number of bits. Single-precision floating-point numbers have 32 bits, double-precision numbers have 64 bits, and extended-precision numbers have 80 bits. We will restrict our discussion to the single-precision floating-point format.

In addition to the CPU (central processing unit), computers use *coprocessors* to perform complicated mathematical calculations using floating-point numbers. The purpose is to increase performance by freeing up the CPU for other tasks. The mathematical coprocessor is also known as the floating-point unit (FPU).

SYSTEM NOTE



SINGLE-PRECISION FLOATING-POINT BINARY NUMBERS In the standard format for a single-precision binary number, the sign bit (S) is the left-most bit, the exponent (E) includes the next eight bits, and the mantissa or fractional part (F) includes the remaining 23 bits, as shown next.



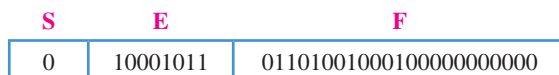
In the mantissa or fractional part, the binary point is understood to be to the left of the 23 bits. Effectively, there are 24 bits in the mantissa because in any binary number the left-most (most significant) bit is always a 1. Therefore, this 1 is understood to be there although it does not occupy an actual bit position.

The eight bits in the exponent represent a *biased exponent*, which is obtained by adding 127 to the actual exponent. The purpose of the bias is to allow very large or very small numbers without requiring a separate sign bit for the exponents. The biased exponent allows a range of actual exponent values from -126 to $+128$.

To illustrate how a binary number is expressed in floating-point format, let's use 1011010010001 as an example. First, it can be expressed as 1 plus a fractional binary number by moving the binary point 12 places to the left and then multiplying by the appropriate power of two.

$$1011010010001 = 1.011010010001 \times 2^{12}$$

Assuming that this is a positive number, the sign bit (S) is 0. The exponent, 12, is expressed as a biased exponent by adding it to 127 ($12 + 127 = 139$). The biased exponent (E) is expressed as the binary number 10001011. The mantissa is the fractional part (F) of the binary number, .011010010001. Because there is always a 1 to the left of the binary point in the power-of-two expression, it is not included in the mantissa. The complete floating-point number is



Next, let's see how to evaluate a binary number that is already in floating-point format. The general approach to determining the value of a floating-point number is expressed by the following formula:

$$\text{Number} = (-1)^S(1 + F)(2^{E-127})$$

To illustrate, let's consider the following floating-point binary number:

S	E	F
1	10010001	100011100010000000000000

The sign bit is 1. The biased exponent is $10010001 = 145$. Applying the formula, we get

$$\begin{aligned} \text{Number} &= (-1)^1 (1.10001110001)(2^{145-127}) \\ &= (-1)(1.10001110001)(2^{18}) = -11000111000100000000 \end{aligned}$$

This floating-point binary number is equivalent to $-407,688$ in decimal. Since the exponent can be any number between -126 and $+128$, extremely large and small numbers can be expressed. A 32-bit floating-point number can replace a binary integer number having 129 bits. Because the exponent determines the position of the binary point, numbers containing both integer and fractional parts can be represented.

There are two exceptions to the format for floating-point numbers: The number 0.0 is represented by all 0s, and infinity is represented by all 1s in the exponent and all 0s in the mantissa.

EXAMPLE 18

Convert the decimal number 3.248×10^4 to a single-precision floating-point binary number.

SOLUTION

Convert the decimal number to binary.

$$3.248 \times 10^4 = 32480 = 111111011100000_2 = 1.11111011100000 \times 2^{14}$$

The MSB will not occupy a bit position because it is always a 1. Therefore, the mantissa is the fractional 23-bit binary number 11111011100000000000000 and the biased exponent is

$$14 + 127 = 141 = 10001101_2$$

The complete floating-point number is

0	10001101	11111011100000000000000
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RELATED PROBLEM

Determine the binary value of the following floating-point binary number:

$$0\ 10011000\ 10000100010100110000000$$

SECTION 6 CHECKUP

- Express the decimal number $+9$ as an 8-bit binary number in the sign-magnitude system.
- Express the decimal number -33 as an 8-bit binary number in the 1's complement system.
- Express the decimal number -46 as an 8-bit binary number in the 2's complement system.
- List the three parts of a signed, floating-point number.

7 ARITHMETIC OPERATIONS WITH SIGNED NUMBERS

In the last section, you learned how signed numbers are represented in three different forms. In this section, you will learn how signed numbers are added, subtracted, multiplied, and divided. Because the 2's complement form for representing signed numbers is the most widely used in computers and microprocessor-based systems, the coverage in this section is limited to 2's complement arithmetic. The processes covered can be extended to the other forms if necessary.

After completing this section, you should be able to

- Add signed binary numbers
- Define *overflow*
- Explain how computers add strings of numbers
- Subtract signed binary numbers
- Multiply signed binary numbers using the direct addition method
- Multiply signed binary numbers using the partial products method
- Divide signed binary numbers

Addition

The two numbers in an addition are the **addend** and the **augend**. The result is the **sum**. There are four cases that can occur when two signed binary numbers are added.

1. Both numbers positive
2. Positive number with magnitude larger than negative number
3. Negative number with magnitude larger than positive number
4. Both numbers negative

Let's take one case at a time using 8-bit signed numbers as examples. The equivalent decimal numbers are shown for reference.

Both numbers positive:

$$\begin{array}{r} 00000111 \quad 7 \\ +00000100 \quad +4 \\ \hline 00001011 \quad 11 \end{array}$$

Addition of two positive numbers yields a positive number.

The sum is positive and is therefore in true (uncomplemented) binary.

Positive number with magnitude larger than negative number:

$$\begin{array}{r} 00001111 \quad 15 \\ + 1111010 \quad + -6 \\ \hline 1 \quad 00001001 \quad 9 \end{array}$$

Discard carry →

Addition of a positive number and a smaller negative number yields a positive number.

The final carry bit is discarded. The sum is positive and therefore in true (uncomplemented) binary.

Negative number with magnitude larger than positive number:

$$\begin{array}{r} 00010000 \quad 16 \\ + 11101000 \quad + -24 \\ \hline 11110000 \quad -8 \end{array}$$

Addition of a positive number and a larger negative number or two negative numbers yields a negative number in 2's complement.

The sum is negative and therefore in 2's complement form.

Both numbers negative:

$$\begin{array}{r} 11111011 \quad -5 \\ + 11110111 \quad + -9 \\ \hline 1 \quad 11110010 \quad -14 \end{array}$$

Discard carry →

The final carry bit is discarded. The sum is negative and therefore in 2's complement form.

In a computer, the negative numbers are stored in 2's complement form so, as you can see, the addition process is very simple: *Add the two numbers and discard any final carry bit.*

OVERFLOW CONDITION When two numbers are added and the number of bits required to represent the sum exceeds the number of bits in the two numbers, an **overflow** results as indicated by an incorrect sign bit. An overflow can occur only when both numbers are positive or both numbers are negative. If the sign bit of the result is different than the sign bit of the numbers that are added, overflow is indicated. The following 8-bit example will illustrate this condition.

$$\begin{array}{r}
 01111101 \quad 125 \\
 + 00111010 \quad + 58 \\
 \hline
 10110111 \quad 183
 \end{array}$$

Sign incorrect
Magnitude incorrect

In this example the sum of 183 requires eight magnitude bits. Since there are seven magnitude bits in the numbers (one bit is the sign), there is a carry into the sign bit which produces the overflow indication.

NUMBERS ADDED TWO AT A TIME Now let's look at the addition of a string of numbers, added two at a time. This can be accomplished by adding the first two numbers, then adding the third number to the sum of the first two, then adding the fourth number to this result, and so on. This is how computers add strings of numbers. The addition of numbers taken two at a time is illustrated in Example 19.

EXAMPLE 19

Add the signed numbers: 01000100, 00011011, 00001110, and 00010010.

SOLUTION

The equivalent decimal additions are given for reference.

68	01000100	
+ 27	+ 00011011	Add 1st two numbers
95	01011111	1st sum
+ 14	+ 00001110	Add 3rd number
109	01101101	2nd sum
+ 18	+ 00010010	Add 4th number
127	01111111	Final sum

RELATED PROBLEM

Add 00110011, 10111111, and 01100011. These are signed numbers.

Subtraction

Subtraction is a special case of addition. For example, subtracting +6 (the **subtrahend**) from +9 (the **minuend**) is equivalent to adding -6 to +9. Basically, *the subtraction operation changes the sign of the subtrahend and adds it to the minuend.* The result of a subtraction is called the **difference**.

The sign of a positive or negative binary number is changed by taking its 2's complement.

Subtraction is addition with the sign of the subtrahend changed.

For example, when you take the 2's complement of the positive number 00000100 (+4), you get 11111100, which is -4 as the following sum-of-weights evaluation shows:

$$-128 + 64 + 32 + 16 + 8 + 4 = -4$$

As another example, when you take the 2's complement of the negative number 11101101 (-19), you get 00010011, which is +19 as the following sum-of-weights evaluation shows:

$$16 + 2 + 1 = 19$$

Since subtraction is simply an addition with the sign of the subtrahend changed, the process is stated as follows:

To subtract two signed numbers, take the 2's complement of the subtrahend and add. Discard any final carry bit.

Example 20 illustrates the subtraction process.

When doing binary subtraction with the 2's complement method, it is very important that both numbers have the same number of bits.

EXAMPLE 20

Perform each of the following subtractions of the signed numbers:

- (a) 00001000 - 00000011 (b) 00001100 - 11110111
 (c) 11100111 - 00010011 (d) 10001000 - 11100010

SOLUTION

Like in other examples, the equivalent decimal subtractions are given for reference.

- (a) In this case, $8 - 3 = 8 + (-3) = 5$.

$$\begin{array}{r} 00001000 \quad \text{Minuend (+8)} \\ + 11111101 \quad \text{2's complement of subtrahend (-3)} \\ \hline \text{Discard carry} \longrightarrow 1 \quad \mathbf{00000101} \quad \text{Difference (+5)} \end{array}$$

- (b) In this case, $12 - (-9) = 12 + 9 = 21$.

$$\begin{array}{r} 00001100 \quad \text{Minuend (+12)} \\ + 00001001 \quad \text{2's complement of subtrahend (+9)} \\ \hline 00010101 \quad \text{Difference (+21)} \end{array}$$

- (c) In this case, $-25 - (+19) = -25 + (-19) = -44$.

$$\begin{array}{r} 11100111 \quad \text{Minuend (-25)} \\ + 11101101 \quad \text{2's complement of subtrahend (-19)} \\ \hline \text{Discard carry} \longrightarrow 1 \quad \mathbf{11010100} \quad \text{Difference (-44)} \end{array}$$

- (d) In this case, $-120 - (-30) = -120 + 30 = -90$.

$$\begin{array}{r} 10001000 \quad \text{Minuend (-120)} \\ + 00011110 \quad \text{2's complement of subtrahend (+30)} \\ \hline \mathbf{10100110} \quad \text{Difference (-90)} \end{array}$$

RELATED PROBLEM

Subtract 01000111 from 01011000.

Multiplication

The numbers in a multiplication are the **multiplicand**, the **multiplier**, and the **product**. These are illustrated in the following decimal multiplication:

$$\begin{array}{r} 8 \quad \text{Multiplicand} \\ \times 3 \quad \text{Multiplier} \\ \hline 24 \quad \text{Product} \end{array}$$

Multiplication is equivalent to adding a number to itself a number of times equal to the multiplier.

The multiplication operation in most computers is accomplished using addition. As you have already seen, subtraction is done with an adder; now let's see how multiplication is done.

Direct addition and *partial products* are two basic methods for performing multiplication using addition. In the direct addition method, you add the multiplicand a number of times equal to the multiplier. In the previous decimal example (8×3), three multiplicands are added: $8 + 8 + 8 = 24$. The disadvantage of this approach is that it becomes very lengthy if the multiplier is a large number. For example, to multiply 350×75 , you must add 350 to itself 75 times. Incidentally, this is why the term *times* is used to mean multiply.

When two binary numbers are multiplied, both numbers must be in true (uncomplemented) form. The direct addition method is illustrated in Example 21 adding two binary numbers at a time.

EXAMPLE 21

Multiply the signed binary numbers: 01001101 (multiplicand) and 00000100 (multiplier) using the direct addition method.

SOLUTION

Since both numbers are positive, they are in true form, and the product will be positive. The decimal value of the multiplier is 4, so the multiplicand is added to itself four times as follows:

01001101	1st time
+ 01001101	2nd time

10011010	Partial sum
+ 01001101	3rd time

11100111	Partial sum
+ 01001101	4th time

100110100	Product

Since the sign bit of the multiplicand is 0, it has no effect on the outcome. All of the bits in the product are magnitude bits.

RELATED PROBLEM

Multiply 01100001 by 00000110 using the direct addition method.

The partial products method is perhaps the more common one because it reflects the way you multiply longhand. The multiplicand is multiplied by each multiplier digit beginning with the least significant digit. The result of the multiplication of the multiplicand by a multiplier digit is called a *partial product*. Each successive partial product is moved (shifted) one place to the left and when all the partial products have been produced, they are added to get the final product. Here is a decimal example.

239	Multiplicand
× 123	Multiplier

717	1st partial product (3×239)
478	2nd partial product (2×239)
+ 239	3rd partial product (1×239)

29,397	Final product

The sign of the product of a multiplication depends on the signs of the multiplicand and the multiplier according to the following two rules:

- **If the signs are the same, the product is positive.**
- **If the signs are different, the product is negative.**

The basic steps in the partial products method of binary multiplication are as follows:

- Step 1:** Determine if the signs of the multiplicand and multiplier are the same or different. This determines what the sign of the product will be.
- Step 2:** Change any negative number to true (uncomplemented) form. Because most computers store negative numbers in 2's complement, a 2's complement operation is required to get the negative number into true form.
- Step 3:** Starting with the least significant multiplier bit, generate the partial products. When the multiplier bit is 1, the partial product is the same as the multiplicand. When the multiplier bit is 0, the partial product is zero. Shift each successive partial product one bit to the left.
- Step 4:** Add each successive partial product to the sum of the previous partial products to get the final product.
- Step 5:** If the sign bit that was determined in step 1 is negative, take the 2's complement of the product. If positive, leave the product in true form. Attach the sign bit to the product.

EXAMPLE 22

Multiply the signed binary numbers: 01010011 (multiplicand) and 11000101 (multiplier).

SOLUTION

Step 1: The sign bit of the multiplicand is 0 and the sign bit of the multiplier is 1. The sign bit of the product will be 1 (negative).

Step 2: Take the 2's complement of the multiplier to put it in true form.

$$11000101 \longrightarrow 00111011$$

Step 3 and 4: The multiplication proceeds as follows. Notice that only the magnitude bits are used in these steps.

1010011	Multiplicand
× 0111011	Multiplier
1010011	1st partial product
+ 1010011	2nd partial product
11111001	Sum of 1st and 2nd
+ 0000000	3rd partial product
011111001	Sum
+ 1010011	4th partial product
1110010001	Sum
+ 1010011	5th partial product
100011000001	Sum
+ 1010011	6th partial product
1001100100001	Sum
+ 0000000	7th partial product
1001100100001	Final product

Step 5: Since the sign of the product is a 1 as determined in step 1, take the 2's complement of the product.

$$1001100100001 \longrightarrow 0110011011111$$

Attach the sign bit

$$\mathbf{1\ 0110011011111}$$

RELATED PROBLEM

Verify the multiplication is correct by converting to decimal numbers and performing the multiplication.

Division

The numbers in a division are the **dividend**, the **divisor**, and the **quotient**. These are illustrated in the following standard division format.

$$\frac{\text{dividend}}{\text{divisor}} = \text{quotient}$$

The division operation in computers is accomplished using subtraction. Since subtraction is done with an adder, division can also be accomplished with an adder.

The result of a division is called the *quotient*; the quotient is the number of times that the divisor will go into the dividend. This means that the divisor can be subtracted from the dividend a number of times equal to the quotient, as illustrated by dividing 21 by 7.

21	Dividend
<u>− 7</u>	1st subtraction of divisor
14	1st partial remainder
<u>− 7</u>	2nd subtraction of divisor
7	2nd partial remainder
<u>− 7</u>	3rd subtraction of divisor
0	Zero remainder

In this simple example, the divisor was subtracted from the dividend three times before a remainder of zero was obtained. Therefore, the quotient is 3.

The sign of the quotient depends on the signs of the dividend and the divisor according to the following two rules:

- **If the signs are the same, the quotient is positive.**
- **If the signs are different, the quotient is negative.**

When two binary numbers are divided, both numbers must be in true (uncomplemented) form. The basic steps in a division process are as follows:

- Step 1:** Determine if the signs of the dividend and divisor are the same or different. This determines what the sign of the quotient will be. Initialize the quotient to zero.
- Step 2:** Subtract the divisor from the dividend using 2's complement addition to get the first partial remainder and add 1 to the quotient. If this partial remainder is positive, go to step 3. If the partial remainder is zero or negative, the division is complete.
- Step 3:** Subtract the divisor from the partial remainder and add 1 to the quotient. If the result is positive, repeat for the next partial remainder. If the result is zero or negative, the division is complete.

Continue to subtract the divisor from the dividend and the partial remainders until there is a zero or a negative result. Count the number of times that the divisor is subtracted and you have the quotient. Example 23 illustrates these steps using 8-bit signed binary numbers.

EXAMPLE 23

Divide 01100100 by 00011001.

SOLUTION

- Step 1:** The signs of both numbers are positive, so the quotient will be positive. The quotient is initially zero: 00000000.

Step 2: Subtract the divisor from the dividend using 2's complement addition (remember that final carries are discarded).

$$\begin{array}{r}
 01100100 \quad \text{Dividend} \\
 + 11100111 \quad \text{2's complement of divisor} \\
 \hline
 01001011 \quad \text{Positive 1st partial remainder}
 \end{array}$$

Add 1 to quotient: $00000000 + 00000001 = 00000001$.

Step 3: Subtract the divisor from the 1st partial remainder using 2's complement addition.

$$\begin{array}{r}
 01001011 \quad \text{1st partial remainder} \\
 + 11100111 \quad \text{2's complement of divisor} \\
 \hline
 00110010 \quad \text{Positive 2nd partial remainder}
 \end{array}$$

Add 1 to quotient: $00000001 + 00000001 = 00000010$.

Step 4: Subtract the divisor from the 2nd partial remainder using 2's complement addition.

$$\begin{array}{r}
 00110010 \quad \text{2nd partial remainder} \\
 + 11100111 \quad \text{2's complement of divisor} \\
 \hline
 00011001 \quad \text{Positive 3rd partial remainder}
 \end{array}$$

Add 1 to quotient: $00000010 + 00000001 = 00000011$.

Step 5: Subtract the divisor from the 3rd partial remainder using 2's complement addition.

$$\begin{array}{r}
 00011001 \quad \text{3rd partial remainder} \\
 + 11100111 \quad \text{2's complement of divisor} \\
 \hline
 00000000 \quad \text{Zero remainder}
 \end{array}$$

Add 1 to quotient: $00000011 + 00000001 = \mathbf{00000100}$ (final quotient). The process is complete.

RELATED PROBLEM

Verify that the process is correct by converting to decimal numbers and performing the division.

SECTION 7 CHECKUP

- List the four cases when numbers are added.
- Add the signed numbers 00100001 and 10111100.
- Subtract the signed numbers 00110010 from 01110111.
- What is the sign of the product when two negative numbers are multiplied?
- Multiply 01111111 by 00000101.
- What is the sign of the quotient when a positive number is divided by a negative number?
- Divide 00110000 by 00001100.

8 HEXADECIMAL NUMBERS

The hexadecimal number system has sixteen characters; it is used primarily as a compact way of displaying or writing binary numbers because it is very easy to convert between binary and hexadecimal. As you are probably aware, long binary numbers are difficult to read and write because it is easy to drop or transpose a bit. Since computers and microprocessors understand only 1s and 0s, it is necessary to use these digits when you program in “machine language.” Imagine writing a sixteen bit instruction for a microprocessor system in 1s and 0s. It is much more efficient to use hexadecimal or octal; octal numbers are covered in Section 9. Hexadecimal is widely used in computer and microprocessor applications.

After completing this section, you should be able to

- List the hexadecimal characters
- Count in hexadecimal
- Convert from binary to hexadecimal
- Convert from hexadecimal to binary
- Convert from hexadecimal to decimal
- Convert from decimal to hexadecimal
- Add hexadecimal numbers
- Determine the 2’s complement of a hexadecimal number
- Subtract hexadecimal numbers

The hexadecimal number system consists of digits 0–9 and letters A–F.

The **hexadecimal** number system has a base of sixteen; that is, it is composed of 16 **numeric** and alphabetic **characters**. Most digital systems process binary data in groups that are multiples of four bits, making the hexadecimal number very convenient because each hexadecimal digit represents a 4-bit binary number (as listed in Table 3).

DECIMAL	BINARY	HEXADECIMAL
0	0000	0
1	0001	1
2	0010	2
3	0011	3
4	0100	4
5	0101	5
6	0110	6
7	0111	7
8	1000	8
9	1001	9
10	1010	A
11	1011	B
12	1100	C
13	1101	D
14	1110	E
15	1111	F

Ten numeric digits and six alphabetic characters make up the hexadecimal number system. The use of letters A, B, C, D, E, and F to represent numbers may seem strange at first, but keep in mind that any number system is only a set of sequential symbols. If you understand what quantities these symbols represent, then the form of the symbols themselves is less important once you get accustomed to using them. We will use the subscript 16 to designate hexadecimal numbers to avoid confusion with decimal numbers. Sometimes you may see an “h” following a hexadecimal number.

Counting in Hexadecimal

How do you count in hexadecimal once you get to F? Simply start over with another column and continue as follows:

... , E, F, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 1A, 1B, 1C, 1D, 1E, 1F,
20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 2A, 2B, 2C, 2D, 2E, 2F, 30, 31, ...

With two hexadecimal digits, you can count up to FF_{16} , which is decimal 255. To count beyond this, three hexadecimal digits are needed. For instance, 100_{16} is decimal 256, 101_{16} is decimal 257, and so forth. The maximum 3-digit hexadecimal number is FFF_{16} , or decimal 4095. The maximum 4-digit hexadecimal number is $FFFF_{16}$, which is decimal 65,535.

With computer memories in the gigabyte (GB) range, specifying a memory address in binary is quite cumbersome. For example, it takes 32 bits to specify an address in a 4 GB memory. It is much easier to express a 32-bit code using 8 hexadecimal digits.

SYSTEM NOTE



Binary-to-Hexadecimal Conversion

Converting a binary number to hexadecimal is a straightforward procedure. Simply break the binary number into 4-bit groups, starting at the right-most bit and replace each 4-bit group with the equivalent hexadecimal symbol.

EXAMPLE 24

Convert the following binary numbers to hexadecimal:

(a) 1100101001010111 (b) 11111000101101001

SOLUTION

(a) $\begin{array}{cccc} 1100 & 1010 & 0101 & 0111 \\ \downarrow & \downarrow & \downarrow & \downarrow \\ C & A & 5 & 7 \end{array} = CA57_{16}$ (b) $\begin{array}{ccccc} 0011 & 1111 & 0001 & 0110 & 1001 \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 3 & F & 1 & 6 & 9 \end{array} = 3F169_{16}$

Two zeros have been added in part (b) to complete a 4-bit group at the left.

RELATED PROBLEM

Convert the binary number 1001111011110011100 to hexadecimal.

Hexadecimal-to-Binary Conversion

To convert from a hexadecimal number to a binary number, reverse the process and replace each hexadecimal symbol with the appropriate four bits.

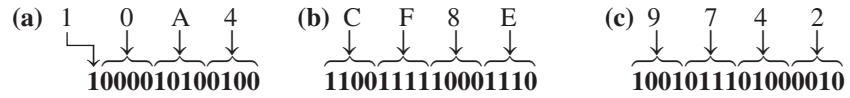
Hexadecimal is a convenient way to represent binary numbers.

EXAMPLE 25

Determine the binary numbers for the following hexadecimal numbers:

- (a) $10A4_{16}$ (b) $CF8E_{16}$ (c) 9742_{16}

SOLUTION



In part (a), the MSB is understood to have three zeros preceding it, thus forming a 4-bit group.

RELATED PROBLEM

Convert the hexadecimal number $6BD3$ to binary.

Conversion between hexadecimal and binary is direct and easy.

It should be clear that it is much easier to deal with a hexadecimal number than with the equivalent binary number. Since conversion is so easy, the hexadecimal system is widely used for representing binary numbers in programming, printouts, and displays.

Hexadecimal-to-Decimal Conversion

One way to find the decimal equivalent of a hexadecimal number is to first convert the hexadecimal number to binary and then convert from binary to decimal.

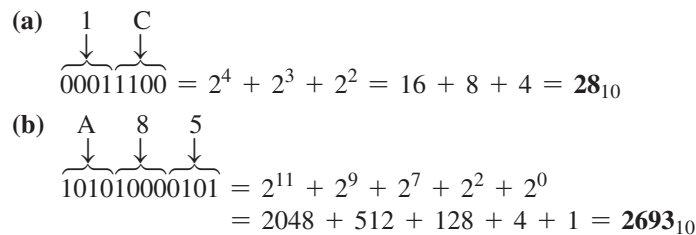
EXAMPLE 26

Convert the following hexadecimal numbers to decimal:

- (a) $1C_{16}$ (b) $A85_{16}$

SOLUTION

Remember, convert the hexadecimal number to binary first, then to decimal.



RELATED PROBLEM

Convert the hexadecimal number $6BD$ to decimal.

Another way to convert a hexadecimal number to its decimal equivalent is to multiply the decimal value of each hexadecimal digit by its weight and then take the sum of

these products. The weights of a hexadecimal number are increasing powers of 16 (from right to left). For a 4-digit hexadecimal number, the weights are

$$\begin{array}{cccc} 16^3 & 16^2 & 16^1 & 16^0 \\ 4096 & 256 & 16 & 1 \end{array}$$

EXAMPLE 27

Convert the following hexadecimal numbers to decimal:

- (a) $E5_{16}$ (b) $B2F8_{16}$

SOLUTION

Recall from Table 3 that letters A through F represent decimal numbers 10 through 15, respectively.

(a) $E5_{16} = (E \times 16) + (5 \times 1) = (14 \times 16) + (5 \times 1) = 224 + 5 = 229_{10}$

(b) $B2F8_{16} = (B \times 4096) + (2 \times 256) + (F \times 16) + (8 \times 1)$
 $= (11 \times 4096) + (2 \times 256) + (15 \times 16) + (8 \times 1)$
 $= 45,056 + 512 + 240 + 8 = 45,816_{10}$

RELATED PROBLEM

Convert $60A_{16}$ to decimal.

CALCULATOR TUTORIAL

Conversion of a Hexadecimal Number to a Decimal Number

EXAMPLE

Convert hexadecimal 28A to decimal.

TI-36X Step 1: $\overset{\text{HEX}}{\text{3rd}} \text{ ()}$

Step 2: $\overset{\text{A}}{\text{2}} \text{ 8 } \overset{\text{3rd}}{\text{1/x}}$

Step 3: $\overset{\text{DEC}}{\text{3rd}} \text{ EE}$ 650

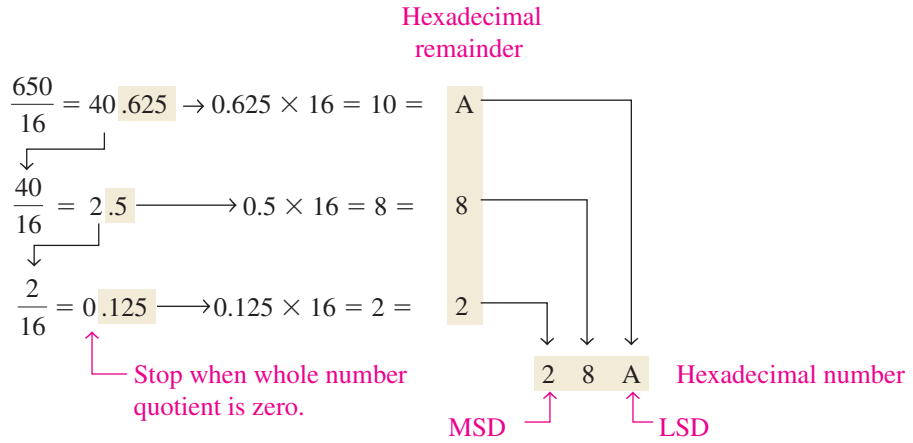
Decimal-to-Hexadecimal Conversion

Repeated division of a decimal number by 16 will produce the equivalent hexadecimal number, formed by the remainders of the divisions. The first remainder produced is the least significant digit (LSD). Each successive division by 16 yields a remainder that becomes a digit in the equivalent hexadecimal number. This procedure is similar to repeated division by 2 for decimal-to-binary conversion that was covered in Section 3. Example 28 illustrates the procedure. Note that when a quotient has a fractional part, the fractional part is multiplied by the divisor to get the remainder.

EXAMPLE 28

Convert the decimal number 650 to hexadecimal by repeated division by 16.

SOLUTION



RELATED PROBLEM

Convert decimal 2591 to hexadecimal.

Hexadecimal Addition

Addition can be done directly with hexadecimal numbers by remembering that the hexadecimal digits 0 through 9 are equivalent to decimal digits 0 through 9 and that hexadecimal digits A through F are equivalent to decimal numbers 10 through 15. When adding two hexadecimal numbers, use the following rules. (Decimal numbers are indicated by a subscript 10.)

1. In any given column of an addition problem, think of the two hexadecimal digits in terms of their decimal values. For instance, $5_{16} = 5_{10}$ and $C_{16} = 12_{10}$.
2. If the sum of these two digits is 15_{10} or less, bring down the corresponding hexadecimal digit.
3. If the sum of these two digits is greater than 15_{10} , bring down the amount of the sum that exceeds 16_{10} and carry a 1 to the next column.

CALCULATOR TUTORIAL

Conversion of a Decimal Number to a Hexadecimal Number

EXAMPLE

Convert decimal 650 to hexadecimal.



EXAMPLE 29

Add the following hexadecimal numbers:

- (a) $23_{16} + 16_{16}$ (b) $58_{16} + 22_{16}$
 (c) $2B_{16} + 84_{16}$ (d) $DF_{16} + AC_{16}$

SOLUTION

- (a) 23_{16} right column: $3_{16} + 6_{16} = 3_{10} + 6_{10} = 9_{10} = 9_{16}$
 $+16_{16}$ left column: $2_{16} + 1_{16} = 2_{10} + 1_{10} = 3_{10} = 3_{16}$
 39_{16}
- (b) 58_{16} right column: $8_{16} + 2_{16} = 8_{10} + 2_{10} = 10_{10} = A_{16}$
 $+22_{16}$ left column: $5_{16} + 2_{16} = 5_{10} + 2_{10} = 7_{10} = 7_{16}$
 $7A_{16}$
- (c) $2B_{16}$ right column: $B_{16} + 4_{16} = 11_{10} + 4_{10} = 15_{10} = F_{16}$
 $+84_{16}$ left column: $2_{16} + 8_{16} = 2_{10} + 8_{10} = 10_{10} = A_{16}$
 AF_{16}
- (d) DF_{16} right column: $F_{16} + C_{16} = 15_{10} + 12_{10} = 27_{10}$
 $+AC_{16}$ $27_{10} - 16_{10} = 11_{10} = B_{16}$ with a 1 carry
 $18B_{16}$ left column: $D_{16} + A_{16} + 1_{16} = 13_{10} + 10_{10} + 1_{10} = 24_{10}$
 $24_{10} - 16_{10} = 8_{10} = 8_{16}$ with a 1 carry

RELATED PROBLEM

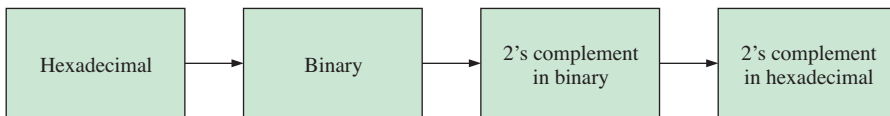
Add $4C_{16}$ and $3A_{16}$.

Hexadecimal Subtraction

As you have learned, the 2's complement allows you to subtract by adding binary numbers. Since a hexadecimal number can be used to represent a binary number, it can also be used to represent the 2's complement of a binary number.

There are three ways to get the 2's complement of a hexadecimal number. Method 1 is the most common and easiest to use. Methods 2 and 3 are alternate methods.

Method 1: Convert the hexadecimal number to binary. Take the 2's complement of the binary number. Convert the result to hexadecimal. This is illustrated in Figure 4.



Example:

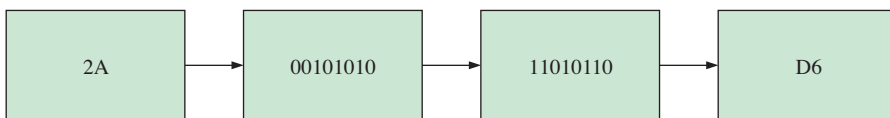


FIGURE 4 Getting the 2's complement of a hexadecimal number, Method 1.

Method 2: Subtract the hexadecimal number from the maximum hexadecimal number and add 1. This is illustrated in Figure 5.

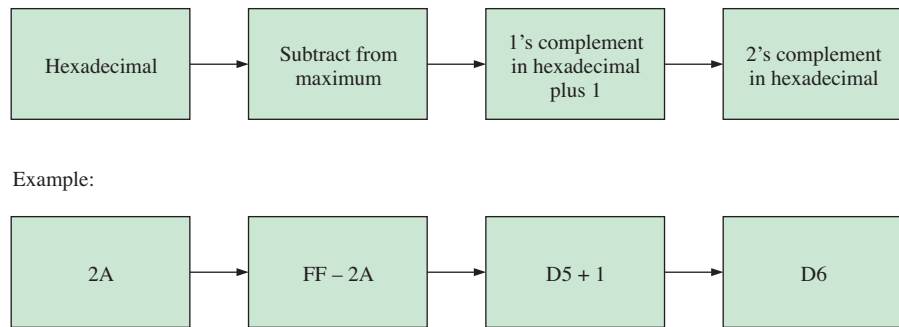


FIGURE 5 Getting the 2's complement of a hexadecimal number, Method 2.

Method 3: Write the sequence of single hexadecimal digits. Write the sequence in reverse below the forward sequence. The 1's complement of each hex digit is the digit directly below it. Add 1 to the resulting number to get the 2's complement. This is illustrated in Figure 6.

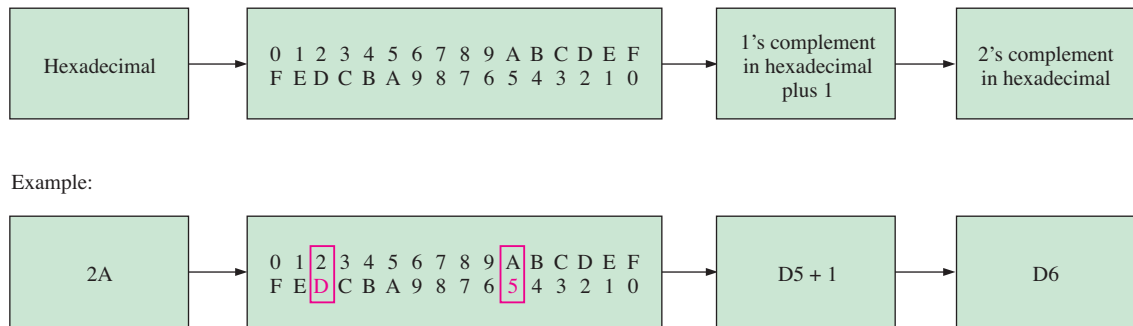


FIGURE 6 Getting the 2's complement of a hexadecimal number, Method 3.

EXAMPLE 30

Subtract the following hexadecimal numbers:

- (a) $84_{16} - 2A_{16}$ (b) $C3_{16} - 0B_{16}$

SOLUTION

- (a) $2A_{16} = 00101010$
 2's complement of $2A_{16} = 11010110 = D6_{16}$ (using Method 1)

$$\begin{array}{r}
 84_{16} \\
 +D6_{16} \quad \text{Add} \\
 \hline
 15A_{16} \quad \text{Drop carry, as in 2's complement addition}
 \end{array}$$

The difference is $5A_{16}$.

(b) $0B_{16} = 00001011$

2's complement of $0B_{16} = 11110101 = F5_{16}$ (using Method 1)

$$\begin{array}{r} C3_{16} \\ + F5_{16} \quad \text{Add} \\ \hline 1B8_{16} \quad \text{Drop carry} \end{array}$$

The difference is $B8_{16}$.

RELATED PROBLEM

Subtract 173_{16} from BCD_{16} .

SECTION 8 CHECKUP

- Convert the following binary numbers to hexadecimal:
(a) 10110011 (b) 110011101000
- Convert the following hexadecimal numbers to binary:
(a) 57_{16} (b) $3A5_{16}$ (c) $F80B_{16}$
- Convert $9B30_{16}$ to decimal.
- Convert the decimal number 573 to hexadecimal.
- Add the following hexadecimal numbers directly:
(a) $18_{16} + 34_{16}$ (b) $3F_{16} + 2A_{16}$
- Subtract the following hexadecimal numbers:
(a) $75_{16} - 21_{16}$ (b) $94_{16} - 5C_{16}$

9 OCTAL NUMBERS

Like the hexadecimal number system, the octal number system provides a convenient way to express binary numbers and codes. However, it is used less frequently than hexadecimal in conjunction with computers and microprocessors to express binary quantities for input and output purposes.

After completing this section, you should be able to

- Write the digits of the octal number system
- Convert from octal to decimal
- Convert from decimal to octal
- Convert from octal to binary
- Convert from binary to octal

The **octal** number system is composed of eight digits, which are

$$0, 1, 2, 3, 4, 5, 6, 7$$

To count above 7, begin another column and start over:

$$10, 11, 12, 13, 14, 15, 16, 17, 20, 21, \dots$$

Counting in octal is similar to counting in decimal, except that the digits 8 and 9 are not used. To distinguish octal numbers from decimal numbers or hexadecimal numbers, we will use the subscript 8 to indicate an octal number. For instance, 15_8 in octal is equivalent to 13_{10} in decimal and D in hexadecimal. Sometimes you may see an “o” or a “Q” following an octal number.

The octal number system has a base of 8.

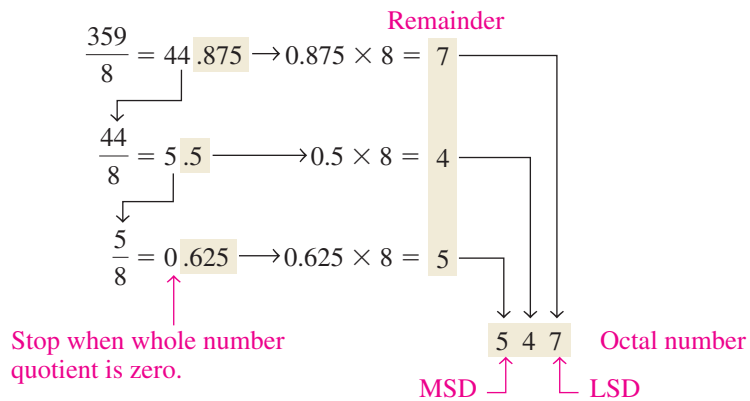
Octal-to-Decimal Conversion

Since the octal number system has a base of eight, each successive digit position is an increasing power of eight, beginning in the right-most column with 8^0 . The evaluation of an octal number in terms of its decimal equivalent is accomplished by multiplying each digit by its weight and summing the products, as illustrated here for 2374_8 .

$$\begin{aligned}
 \text{Weight: } & 8^3 \ 8^2 \ 8^1 \ 8^0 \\
 \text{Octal number: } & 2 \ 3 \ 7 \ 4 \\
 2374_8 = & (2 \times 8^3) + (3 \times 8^2) + (7 \times 8^1) + (4 \times 8^0) \\
 = & (2 \times 512) + (3 \times 64) + (7 \times 8) + (4 \times 1) \\
 = & 1024 + 192 + 56 + 4 = 1276_{10}
 \end{aligned}$$

Decimal-to-Octal Conversion

A method of converting a decimal number to an octal number is the repeated division-by-8 method, which is similar to the method used in the conversion of decimal numbers to binary or to hexadecimal. To show how it works, let's convert the decimal number 359 to octal. Each successive division by 8 yields a remainder that becomes a digit in the equivalent octal number. The first remainder generated is the least significant digit (LSD).



CALCULATOR TUTORIAL

Conversion of a Decimal Number to an Octal Number

EXAMPLE

Convert decimal 439 to octal.

TI-36X Step 1: DEC
3rd EE

Step 2: 4 3 9

Step 3: OCT
3rd ↓

667

Octal is a convenient way to represent binary numbers, but it is not as commonly used as hexadecimal.

Octal-to-Binary Conversion

Because each octal digit can be represented by a 3-bit binary number, it is very easy to convert from octal to binary. Each octal digit is represented by three bits as shown in Table 4.

TABLE 4 • Octal/binary conversion.								
OCTAL DIGIT	0	1	2	3	4	5	6	7
BINARY	000	001	010	011	100	101	110	111

To convert an octal number to a binary number, simply replace each octal digit with the appropriate three bits.

EXAMPLE 31

Convert each of the following octal numbers to binary:

- (a) 13_8 (b) 25_8 (c) 140_8 (d) 7526_8

SOLUTION

(a) $\begin{array}{cc} 1 & 3 \\ \downarrow & \downarrow \\ \underline{001} & \underline{011} \end{array}$ (b) $\begin{array}{cc} 2 & 5 \\ \downarrow & \downarrow \\ \underline{010} & \underline{101} \end{array}$ (c) $\begin{array}{ccc} 1 & 4 & 0 \\ \downarrow & \downarrow & \downarrow \\ \underline{001} & \underline{100} & \underline{000} \end{array}$ (d) $\begin{array}{cccc} 7 & 5 & 2 & 6 \\ \downarrow & \downarrow & \downarrow & \downarrow \\ \underline{111} & \underline{101} & \underline{010} & \underline{110} \end{array}$

RELATED PROBLEM

Convert each of the binary numbers to decimal and verify that each value agrees with the decimal value of the corresponding octal number.

Binary-to-Octal Conversion

Conversion of a binary number to an octal number is the reverse of the octal-to-binary conversion. The procedure is as follows: Start with the right-most group of three bits and, moving from right to left, convert each 3-bit group to the equivalent octal digit. If there are not three bits available for the left-most group, add either one or two zeros to make a complete group. These leading zeros do not affect the value of the binary number.

EXAMPLE 32

Convert each of the following binary numbers to octal:

- (a) 110101 (b) 101111001
 (c) 100110011010 (d) 11010000100

SOLUTION

(a) $\begin{array}{cc} 110101 \\ \downarrow \downarrow \\ 6 & 5 = 65_8 \end{array}$ (b) $\begin{array}{ccc} 101111001 \\ \downarrow \downarrow \downarrow \\ 5 & 7 & 1 = 571_8 \end{array}$

(c) $\begin{array}{cccc} 100110011010 \\ \downarrow \downarrow \downarrow \downarrow \\ 4 & 6 & 3 & 2 = 4632_8 \end{array}$ (d) $\begin{array}{cccc} 011010000100 \\ \downarrow \downarrow \downarrow \downarrow \\ 3 & 2 & 0 & 4 = 3204_8 \end{array}$

RELATED PROBLEM

Convert the binary number 1010101000111110010 to octal.

SECTION 9 CHECKUP

- Convert the following octal numbers to decimal:
 (a) 73_8 (b) 125_8
- Convert the following decimal numbers to octal:
 (a) 98_{10} (b) 163_{10}
- Convert the following octal numbers to binary:
 (a) 46_8 (b) 723_8 (c) 5624_8
- Convert the following binary numbers to octal:
 (a) 110101111 (b) 1001100010 (c) 10111111001

10 BINARY CODED DECIMAL (BCD)

Binary coded decimal (BCD) is a way to express each of the decimal digits with a binary code. There are only ten code groups in the BCD system, so it is very easy to convert between decimal and BCD. Because we like to read and write in decimal, the BCD code provides an excellent interface to binary systems. Examples of such interfaces are keypad inputs and digital readouts.

After completing this section, you should be able to

- Convert each decimal digit to BCD
- Express decimal numbers in BCD
- Convert from BCD to decimal
- Add BCD numbers

In BCD, 4 bits represent each decimal digit.

The 8421 BCD Code

The 8421 code is a common type of **BCD** (binary coded decimal) code. Binary coded decimal means that each decimal digit, 0 through 9, is represented by a binary code of four bits. The designation 8421 indicates the binary weights of the four bits ($2^3, 2^2, 2^1, 2^0$). The ease of conversion between 8421 code numbers and the familiar decimal numbers is the main advantage of this code. All you have to remember are the ten binary combinations that represent the ten decimal digits as shown in Table 5. The 8421 code is the predominant BCD code, and when we refer to BCD, we always mean the 8421 code unless otherwise stated.

TABLE 5 • Decimal/BCD conversion.

DECIMAL DIGIT	0	1	2	3	4	5	6	7	8	9
BCD	0000	0001	0010	0011	0100	0101	0110	0111	1000	1001

INVALID CODES You should realize that, with four bits, sixteen numbers (0000 through 1111) can be represented but that, in the 8421 code, only ten of these are used. The six code combinations that are not used—1010, 1011, 1100, 1101, 1110, and 1111—are invalid in the 8421 BCD code.

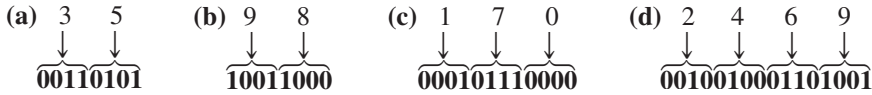
To express any decimal number in BCD, simply replace each decimal digit with the appropriate 4-bit code, as shown by Example 33.

EXAMPLE 33

Convert each of the following decimal numbers to BCD:

- (a) 35 (b) 98 (c) 170 (d) 2469

SOLUTION



RELATED PROBLEM

Convert the decimal number 9673 to BCD.

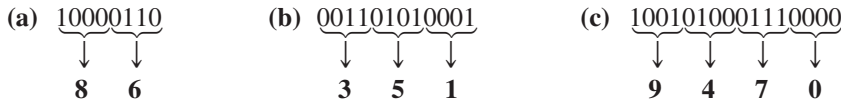
It is equally easy to determine a decimal number from a BCD number. Start at the right-most bit and break the code into groups of four bits. Then write the decimal digit represented by each 4-bit group.

EXAMPLE 34

Convert each of the following BCD codes to decimal:

- (a) 10000110 (b) 001101010001 (c) 1001010001110000

SOLUTION



RELATED PROBLEM

Convert the BCD code 10000010001001110110 to decimal.

APPLICATIONS Digital clocks, digital thermometers, digital meters, and other devices with seven-segment displays typically use BCD code to simplify the displaying of decimal numbers. BCD is not as efficient as straight binary for calculations, but it is particularly useful if only limited processing is required, such as in a digital thermometer.

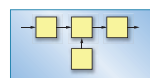
BCD Addition

BCD is a numerical code and can be used in arithmetic operations. Addition is the most important operation because the other three operations (subtraction, multiplication, and division) can be accomplished by the use of addition. Here is how to add two BCD numbers:

- Step 1:** Add the two BCD numbers, using the rules for binary addition in Section 4.
- Step 2:** If a 4-bit sum is equal to or less than 9, it is a valid BCD number.
- Step 3:** If a 4-bit sum is greater than 9, or if a carry out of the 4-bit group is generated, it is an invalid result. Add 6 (0110) to the 4-bit sum in order to skip the six invalid states and return the code to 8421. If a carry results when 6 is added, simply add the carry to the next 4-bit group.

BCD is sometimes used for arithmetic operations in computers. To represent BCD numbers in a computer, they usually are “packed,” so that eight bits has two BCD digits. Normally, a computer will add numbers as if they were straight binary. Special instructions are available for computer programmers to correct the results when BCD numbers are added or subtracted. For example, in Assembly Language, the programmer will include a DAA (Decimal Adjust for Addition) instruction to automatically correct the answer to BCD following an addition.

SYSTEM NOTE



Example 35 illustrates BCD additions in which the sum in each 4-bit column is equal to or less than 9, and the 4-bit sums are therefore valid BCD numbers. Example 36 illustrates the procedure in the case of invalid sums (greater than 9 or a carry).

An alternative method to add BCD numbers is to convert them to decimal, perform the addition, and then convert the answer back to BCD.

EXAMPLE 35

Add the following BCD numbers:

- (a) 0011 + 0100 (b) 00100011 + 00010101
 (c) 10000110 + 00010011 (d) 010001010000 + 010000010111

SOLUTION

The decimal number additions are shown for comparison.

- | | |
|--|---|
| <p>(a) $\begin{array}{r} 0011 \quad 3 \\ + 0100 \quad +4 \\ \hline \mathbf{1111} \quad 7 \end{array}$</p> | <p>(b) $\begin{array}{r} 0010 \quad 0011 \quad 23 \\ + 0001 \quad 0101 \quad +15 \\ \hline \mathbf{0011} \quad \mathbf{1000} \quad 38 \end{array}$</p> |
| <p>(c) $\begin{array}{r} 1000 \quad 0110 \quad 86 \\ + 0001 \quad 0011 \quad +13 \\ \hline \mathbf{1001} \quad \mathbf{1001} \quad \mathbf{99} \end{array}$</p> | <p>(d) $\begin{array}{r} 0100 \quad 0101 \quad 0000 \quad 450 \\ + 0100 \quad 0001 \quad 0111 \quad +417 \\ \hline \mathbf{1000} \quad \mathbf{0110} \quad \mathbf{0111} \quad \mathbf{867} \end{array}$</p> |

Note that in each case the sum in any 4-bit column does not exceed 9, and the results are valid BCD numbers.

RELATED PROBLEM

Add the BCD numbers: 1001000001000011 + 0000100100100101.

EXAMPLE 36

Add the following BCD numbers:

- (a) 1001 + 0100 (b) 1001 + 1001
 (c) 00010110 + 00010101 (d) 01100111 + 01010011

SOLUTION

The decimal number additions are shown for comparison.

- | | |
|--|--|
| <p>(a) $\begin{array}{r} 1001 \\ + 0100 \\ \hline 1101 \\ + 0110 \\ \hline \mathbf{0001} \quad \mathbf{0011} \\ \downarrow \quad \downarrow \\ 1 \quad 3 \end{array}$</p> | <p>$\begin{array}{r} 9 \\ +4 \\ \hline 13 \end{array}$
 Invalid BCD number (>9)
 Add 6
 Valid BCD number</p> |
| <p>(b) $\begin{array}{r} 1001 \\ + 1001 \\ \hline 1 \quad 0010 \\ + 0110 \\ \hline \mathbf{0001} \quad \mathbf{1000} \\ \downarrow \quad \downarrow \\ 1 \quad 8 \end{array}$</p> | <p>$\begin{array}{r} 9 \\ +9 \\ \hline 18 \end{array}$
 Invalid because of carry
 Add 6
 Valid BCD number</p> |

<p>(c)</p> $\begin{array}{r} 0001 \quad 0110 \\ + 0001 \quad 0101 \\ \hline 0010 \quad 1011 \\ + 0110 \\ \hline \mathbf{0011} \quad \mathbf{0001} \\ \downarrow \quad \downarrow \\ 3 \quad 1 \end{array}$	<p>Right group is invalid (>9), left group is valid. Add 6 to invalid code. Add carry, 0001, to next group. Valid BCD number</p>	$\begin{array}{r} 16 \\ + 15 \\ \hline 31 \end{array}$
<p>(d)</p> $\begin{array}{r} \quad 0110 \quad 0111 \\ + 0101 \quad 0011 \\ \hline 1011 \quad 1010 \\ + 0110 \quad + 0110 \\ \hline \mathbf{0001} \quad \mathbf{0010} \quad \mathbf{0000} \\ \downarrow \quad \downarrow \quad \downarrow \\ 1 \quad 2 \quad 0 \end{array}$	<p>Both groups are invalid (>9) Add 6 to both groups. Valid BCD number</p>	$\begin{array}{r} 67 \\ + 53 \\ \hline 120 \end{array}$

RELATED PROBLEM

Add the BCD numbers: 01001000 + 00110100.

SECTION 10 CHECKUP

1. What is the binary weight of each 1 in the following BCD numbers?

(a) 0010	(b) 1000
(c) 0001	(d) 0100
2. Convert the following decimal numbers to BCD:

(a) 6	(b) 15
(c) 273	(d) 849
3. What decimal numbers are represented by each BCD code?

(a) 10001001
(b) 001001111000
(c) 000101010111
4. In BCD addition, when is a 4-bit sum invalid?

11 DIGITAL CODES

Many specialized codes are used in digital systems. You have just learned about the BCD code; now let's look at a few others. Some codes are strictly numeric, like BCD, and others are alphanumeric; that is, they are used to represent numbers, letters, symbols, and instructions. The codes introduced in this section are the Gray code, the ASCII code, and the Unicode.

After completing this section, you should be able to

- Explain the advantage of the Gray code
- Convert between Gray code and binary
- Use the ASCII code
- Discuss the Unicode

The Gray Code

The single bit change characteristic of the Gray code minimizes the chance for error.

The **Gray code** is unweighted and is not an arithmetic code; that is, there are no specific weights assigned to the bit positions. The important feature of the Gray code is that *it exhibits only a single bit change from one code word to the next in sequence*. This property is important in many applications, such as shaft position encoders, where error susceptibility increases with the number of bit changes between adjacent numbers in a sequence.

Table 6 is a listing of the 4-bit Gray code for decimal numbers 0 through 15. Binary numbers are shown in the table for reference. Like binary numbers, *the Gray code can have any number of bits*. Notice the single-bit change between successive Gray code words. For instance, in going from decimal 3 to decimal 4, the Gray code changes from 0010 to 0110, while the binary code changes from 0011 to 0100, a change of three bits. The only bit change in the Gray code is in the third bit from the right: the other bits remain the same.

DECIMAL	BINARY	GRAY CODE	DECIMAL	BINARY	GRAY CODE
0	0000	0000	8	1000	1100
1	0001	0001	9	1001	1101
2	0010	0011	10	1010	1111
3	0011	0010	11	1011	1110
4	0100	0110	12	1100	1010
5	0101	0111	13	1101	1011
6	0110	0101	14	1110	1001
7	0111	0100	15	1111	1000

BINARY-TO-GRAY CODE CONVERSION Conversion between binary code and Gray code is sometimes useful. The following rules explain how to convert from a binary number to a Gray code word:

1. The most significant bit (left-most) in the Gray code is the same as the corresponding MSB in the binary number.
2. Going from left to right, add each adjacent pair of binary code bits to get the next Gray code bit. Discard carries.

For example, the conversion of the binary number 10110 to Gray code is as follows:

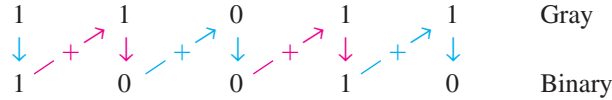


The Gray code is 11101.

GRAY-TO-BINARY CODE CONVERSION To convert from Gray code to binary, use a similar method; however, there are some differences. The following rules apply:

1. The most significant bit (left-most) in the binary code is the same as the corresponding bit in the Gray code.
2. Add each binary code bit generated to the Gray code bit in the next adjacent position. Discard carries.

For example, the conversion of the Gray code word 11011 to binary is as follows:



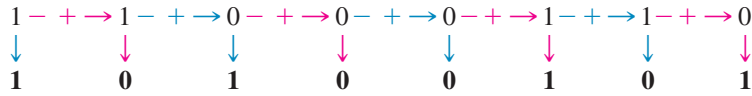
The binary number is 10010.

EXAMPLE 37

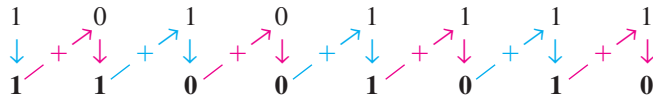
- (a) Convert the binary number 11000110 to Gray code.
- (b) Convert the Gray code 10101111 to binary.

SOLUTION

(a) Binary to Gray code:



(b) Gray code to binary:



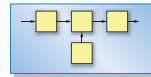
RELATED PROBLEM

- (a) Convert binary 101101 to Gray code.
- (b) Convert Gray code 100111 to binary.

SYSTEM EXAMPLE 2

SHAFT ENCODER

The concept of a 3-bit shaft position encoder is shown in Figure 7. Basically, there are three concentric rings that are segmented into eight sectors. The more sectors there are, the more accurately the position can be represented, but we are using only eight to illustrate. Each sector of each ring is either reflective or nonreflective. As the rings rotate with the shaft, they come under an IR emitter that produces three separate IR beams. A 1 is indicated where there is a reflected beam, and a 0 is indicated where there is no reflected beam. The IR detector senses the presence or absence of reflected beams and produces a corresponding 3-bit code. The IR emitter/detector is in a fixed position. As the shaft rotates counterclockwise through 360°, the eight sectors move under the three beams. Each beam is either reflected or absorbed by the sector surface to represent a binary or Gray code number that indicates the shaft position.



In Figure 7(a), the sectors are arranged in a straight binary pattern, so that the detector output goes from 000 to 001 to 010 to 011 and so on. When a beam is aligned over a reflective sector, the output is 1; when a beam is aligned over a nonreflective sector, the output is 0. If one beam is slightly ahead of the others during the transition from one sector to the next, an erroneous output can occur. Consider what happens when the beams are on the 111 sector and about to enter the 000 sector. If the MSB beam is slightly ahead, the position would be incorrectly indicated by a transitional 011 instead of a 111 or a 000. In this type of application, it is virtually impossible to maintain precise mechanical alignment

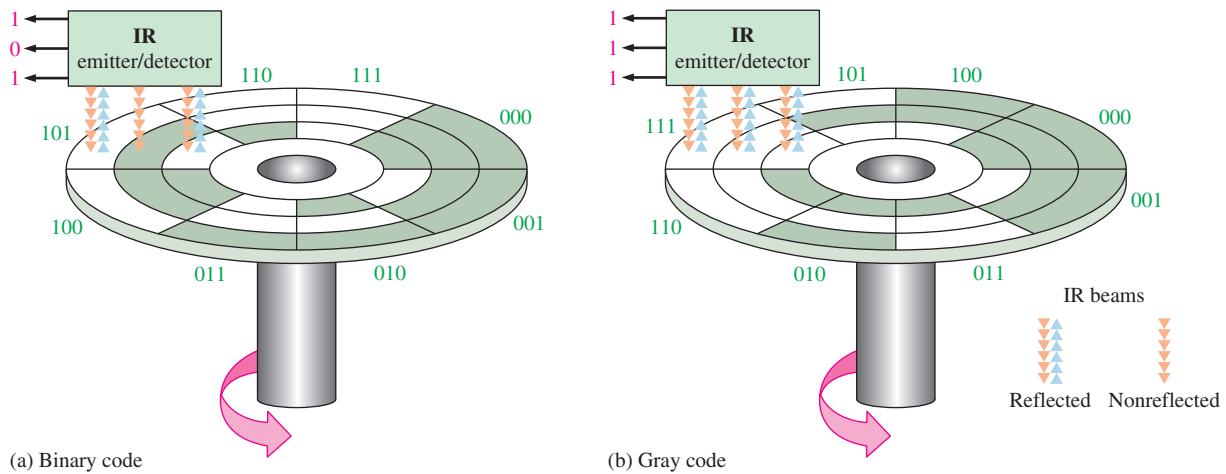


FIGURE 7 A simplified illustration of how the Gray code solves the error problem in shaft position encoders. Three bits are shown to illustrate the concept, although most shaft encoders use more than 10 bits to achieve a higher resolution.

of the IR emitter/detector beams; therefore, some error will usually occur at many of the transitions between sectors.

The Gray code is used to eliminate the error problem which is inherent in the binary code. As shown in Figure 7(b), the Gray code assures that only one bit will change between adjacent sectors. This means that even though the beams may not be in precise alignment, there will never be a transitional error. For example, let's again consider what happens when the beams are on the 111 sector and about to move into the next sector, 101. The only two possible outputs during the transition are 111 and 101, no matter how the beams are aligned. A similar situation occurs at the transitions between each of the other sectors.

Alphanumeric Codes

In order to communicate, you need not only numbers, but also letters and other symbols. In the strictest sense, **alphanumeric** codes are codes that represent numbers and alphabetic characters (letters). Most such codes, however, also represent other characters such as symbols and various instructions necessary for conveying information.

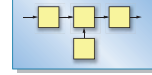
At a minimum, an alphanumeric code must represent 10 decimal digits and 26 letters of the alphabet, for a total of 36 items. This number requires six bits in each code combination because five bits are insufficient ($2^5 = 32$). There are 64 total combinations of six bits, so there are 28 unused code combinations. Obviously, in many applications, symbols other than just numbers and letters are necessary to communicate completely. You need spaces, periods, colons, semicolons, question marks, etc. You also need instructions to tell the receiving system what to do with the information. With codes that are six bits long, you can handle decimal numbers, the alphabet, and 28 other symbols. This should give you an idea of the requirements for a basic alphanumeric code. The ASCII is the most common alphanumeric code and is covered next.

ASCII

ASCII is the abbreviation for American Standard Code for Information Interchange. Pronounced "askee," ASCII is a universally accepted alphanumeric code used in most computers and other electronic equipment. Most computer keyboards are standardized with the ASCII. When you enter a letter, a number, or control command, the corresponding ASCII code goes into the computer.

A computer keyboard has a dedicated microprocessor that constantly scans keyboard circuits to detect when a key has been pressed and released. A unique scan code is produced by computer software representing that particular key. The scan code is then converted to an alphanumeric code (ASCII) for use by the computer.

SYSTEM NOTE



ASCII has 128 characters and symbols represented by a 7-bit binary code. Actually, ASCII can be considered an 8-bit code with the MSB always 0. This 8-bit code is 00 through 7F in hexadecimal. The first thirty-two ASCII characters are nongraphic commands that are never printed or displayed and are used only for control purposes. Examples of the control characters are “null,” “line feed,” “start of text,” and “escape.” The other characters are graphic symbols that can be printed or displayed and include the letters of the alphabet (lowercase and uppercase), the ten decimal digits, punctuation signs, and other commonly used symbols.

Table 7 is a listing of the ASCII code showing the decimal, hexadecimal, and binary representations for each character and symbol. The left section of the table lists the names of the 32 control characters (00 through 1F hexadecimal). The graphic symbols are listed in the rest of the table (20 through 7F hexadecimal).

EXAMPLE 38

Determine the binary ASCII codes that are entered from the computer’s keyboard when the following C language program statement is typed in. Also express each code in hexadecimal.

```
if (x > 5)
```

SOLUTION

The ASCII code for each symbol is found in Table 7.

Symbol	Binary	Hexadecimal
i	1101001	69 ₁₆
f	1100110	66 ₁₆
Space	0100000	20 ₁₆
(0101000	28 ₁₆
x	1111000	78 ₁₆
>	0111110	3E ₁₆
5	0110101	35 ₁₆
)	0101001	29 ₁₆

RELATED PROBLEM

Determine the sequence of ASCII codes required for the following C program statement and express them in hexadecimal:

```
if (y < 8)
```

TABLE 7 • American Standard Code for Information Interchange (ASCII).

CONTROL CHARACTERS				GRAPHIC SYMBOLS											
NAME	DEC	BINARY	HEX	SYMBOL	DEC	BINARY	HEX	SYMBOL	DEC	BINARY	HEX	SYMBOL	DEC	BINARY	HEX
NUL	0	0000000	00	space	32	0100000	20	@	64	1000000	40	`	96	1100000	60
SOH	1	0000001	01	!	33	0100001	21	A	65	1000001	41	a	97	1100001	61
STX	2	0000010	02	"	34	0100010	22	B	66	1000010	42	b	98	1100010	62
ETX	3	0000011	03	#	35	0100011	23	C	67	1000011	43	c	99	1100011	63
EOT	4	0000100	04	\$	36	0100100	24	D	68	1000100	44	d	100	1100100	64
ENQ	5	0000101	05	%	37	0100101	25	E	69	1000101	45	e	101	1100101	65
ACK	6	0000110	06	&	38	0100110	26	F	70	1000110	46	f	102	1100110	66
BEL	7	0000111	07	'	39	0100111	27	G	71	1000111	47	g	103	1100111	67
BS	8	0001000	08	(40	0101000	28	H	72	1001000	48	h	104	1101000	68
HT	9	0001001	09)	41	0101001	29	I	73	1001001	49	i	105	1101001	69
LF	10	0001010	0A	*	42	0101010	2A	J	74	1001010	4A	j	106	1101010	6A
VT	11	0001011	0B	+	43	0101011	2B	K	75	1001011	4B	k	107	1101011	6B
FF	12	0001100	0C	,	44	0101100	2C	L	76	1001100	4C	l	108	1101100	6C
CR	13	0001101	0D	-	45	0101101	2D	M	77	1001101	4D	m	109	1101101	6D
SO	14	0001110	0E	.	46	0101110	2E	N	78	1001110	4E	n	110	1101110	6E
SI	15	0001111	0F	/	47	0101111	2F	O	79	1001111	4F	o	111	1101111	6F
DLE	16	0010000	10	0	48	0110000	30	P	80	1010000	50	p	112	1110000	70
DC1	17	0010001	11	1	49	0110001	31	Q	81	1010001	51	q	113	1110001	71
DC2	18	0010010	12	2	50	0110010	32	R	82	1010010	52	r	114	1110010	72
DC3	19	0010011	13	3	51	0110011	33	S	83	1010011	53	s	115	1110011	73
DC4	20	0010100	14	4	52	0110100	34	T	84	1010100	54	t	116	1110100	74
NAK	21	0010101	15	5	53	0110101	35	U	85	1010101	55	u	117	1110101	75
SYN	22	0010110	16	6	54	0110110	36	V	86	1010110	56	v	118	1110110	76
ETB	23	0010111	17	7	55	0110111	37	W	87	1010111	57	w	119	1110111	77
CAN	24	0011000	18	8	56	0111000	38	X	88	1011000	58	x	120	1111000	78
EM	25	0011001	19	9	57	0111001	39	Y	89	1011001	59	y	121	1111001	79
SUB	26	0011010	1A	:	58	0111010	3A	Z	90	1011010	5A	z	122	1111010	7A
ESC	27	0011011	1B	;	59	0111011	3B	[91	1011011	5B	{	123	1111011	7B
FS	28	0011100	1C	<	60	0111100	3C	\	92	1011100	5C		124	1111100	7C
GS	29	0011101	1D	=	61	0111101	3D]	93	1011101	5D	}	125	1111101	7D
RS	30	0011110	1E	>	62	0111110	3E	^	94	1011110	5E	~	126	1111110	7E
US	31	0011111	1F	?	63	0111111	3F	_	95	1011111	5F	Del	127	1111111	7F

THE ASCII CONTROL CHARACTERS The first thirty-two codes in the ASCII table (Table 7) represent the control characters. These are used to allow devices such as a computer and printer to communicate with each other when passing information and data. Table 8 lists the control characters and the control key function that allows them to be entered directly from an ASCII keyboard by pressing the control key (CTRL) and the corresponding symbol. A brief description of each control character is also given. The

NAME	DECIMAL	HEX	KEYS	DESCRIPTION
NUL	0	00	CTRL @	null character
SOH	1	01	CTRL A	start of header
STX	2	02	CTRL B	start of text
ETX	3	03	CTRL C	end of text
EOT	4	04	CTRL D	end of transmission
ENQ	5	05	CTRL E	enquire
ACK	6	06	CTRL F	acknowledge
BEL	7	07	CTRL G	bell
BS	8	08	CTRL H	backspace
HT	9	09	CTRL I	horizontal tab
LF	10	0A	CTRL J	line feed
VT	11	0B	CTRL K	vertical tab
FF	12	0C	CTRL L	form feed (new page)
CR	13	0D	CTRL M	carriage return
SO	14	0E	CTRL N	shift out
SI	15	0F	CTRL O	shift in
DLE	16	10	CTRL P	data link escape
DC1	17	11	CTRL Q	device control 1
DC2	18	12	CTRL R	device control 2
DC3	19	13	CTRL S	device control 3
DC4	20	14	CTRL T	device control 4
NAK	21	15	CTRL U	negative acknowledge
SYN	22	16	CTRL V	synchronize
ETB	23	17	CTRL W	end of transmission block
CAN	24	18	CTRL X	cancel
EM	25	19	CTRL Y	end of medium
SUB	26	1A	CTRL Z	substitute
ESC	27	1B	CTRL [escape
FS	28	1C	CTRL /	file separator
GS	29	1D	CTRL]	group separator
RS	30	1E	CTRL ^	record separator
US	31	1F	CTRL _	unit separator

descriptions are based on obsolete teletype requirements, and the codes are generally used for different purposes than the description implies.

Extended ASCII Characters

In addition to the 128 standard ASCII characters, there are an additional 128 characters that were adopted by IBM for use in their PCs (personal computers). Because of the popularity of the PC, these particular extended ASCII characters are also used in applications other than PCs and have become essentially an unofficial standard.

The extended ASCII characters are represented by an 8-bit code series from hexadecimal 80 to hexadecimal FF and can be grouped into the following general categories: foreign (non-English) alphabetic characters, foreign currency symbols, Greek letters, mathematical symbols, drawing characters, bar graphing characters, and shading characters.

Unicode

Unicode provides the ability to encode all of the characters used for the written languages of the world by assigning each character a unique numeric value and name utilizing the universal character set (UCS). It is applicable in computer applications dealing with multi-lingual text, mathematical symbols, or other technical characters.

Unicode has a wide array of characters, and their various encoding forms have begun to supplant ASCII in many environments. While ASCII basically uses 7-bit codes, Unicode uses relatively abstract “code points”—non-negative integer numbers—that map sequences of one or more bytes, using different encoding forms and schemes. To permit compatibility, Unicode assigns the first 128 code points to the same characters as ASCII. One can, therefore, think of ASCII as a 7-bit encoding scheme for a very small subset of Unicode and of the UCS.

Unicode consists of about 100,000 characters, a set of code charts for visual reference, an encoding methodology and set of standard character encodings, and an enumeration of character properties such as uppercase and lowercase. It also consists of a number of related items, such as character properties, rules for text normalization, decomposition, collation, rendering, and bidirectional display order (for the correct display of text containing both right-to-left scripts, such as Arabic or Hebrew, and left-to-right scripts).

SECTION 11 CHECKUP

- Convert the following binary numbers to the Gray code:
(a) 1100 (b) 1010 (c) 11010
- Convert the following Gray codes to binary:
(a) 1000 (b) 1010 (c) 11101
- What is the ASCII representation for each of the following characters? Express each as a bit pattern and in hexadecimal notation.
(a) K (b) r (c) \$ (d) +

12 ERROR DETECTION CODES

In this section, two methods for adding bits to codes to detect a single-bit error are discussed. The parity method of error detection is introduced, and the cyclic redundancy check is discussed.

After completing this section, you should be able to

- Determine if there is an error in a code based on the parity bit
- Assign the proper parity bit to a code
- Explain the cyclic redundancy check (CRC)

Parity Method for Error Detection

Many systems use a parity bit as a means for bit **error detection**. Any group of bits contain either an even or an odd number of 1s. A parity bit is attached to a group of bits to make the total number of 1s in a group always even or always odd. An even parity bit makes the total number of 1s even, and an odd parity bit makes the total odd.

A parity bit tells if the number of 1s in a group of bits is odd or even.

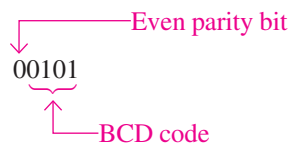
A given system operates with even or odd **parity**, but not both. For instance, if a system operates with even parity, a check is made on each group of bits received to make sure the total number of 1s in that group is even. If there is an odd number of 1s, an error has occurred.

As an illustration of how parity bits are attached to a code, Table 9 lists the parity bits for each BCD number for both even and odd parity. The parity bit for each BCD number is in the *P* column.

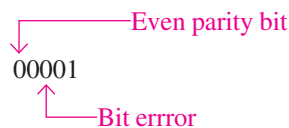
EVEN PARITY		ODD PARITY	
<i>P</i>	BCD	<i>P</i>	BCD
0	0000	1	0000
1	0001	0	0001
1	0010	0	0010
0	0011	1	0011
1	0100	0	0100
0	0101	1	0101
0	0110	1	0110
1	0111	0	0111
1	1000	0	1000
0	1001	1	1001

The parity bit can be attached to the code at either the beginning or the end, depending on system design. Notice that the total number of 1s, including the parity bit, is always even for even parity and always odd for odd parity.

DETECTING AN ERROR A parity bit provides for the detection of a single bit error (or any odd number of errors, which is very unlikely) but cannot check for two errors in one group. For instance, let's assume that we wish to transmit the BCD code 0101. (Parity can be used with any number of bits; we are using four for illustration.) The total code transmitted, including the even parity bit, is



Now let's assume that an error occurs in the third bit from the left (the 1 becomes a 0).



When this code is received, the parity check circuitry determines that there is only a single 1 (odd number), when there should be an even number of 1s. Because an even number of 1s does not appear in the code when it is received, an error is indicated.

An odd parity bit also provides in a similar manner for the detection of a single error in a given group of bits.

EXAMPLE 39

Assign the proper even parity bit to the following code groups:

- (a) 1010 (b) 111000 (c) 101101
 (d) 1000111001001 (e) 101101011111

SOLUTION

Make the parity bit either 1 or 0 as necessary to make the total number of 1s even. The parity bit will be the left-most bit (color).

- (a) **0**1010 (b) **1**111000 (c) **0**101101
 (d) **0**100011100101 (e) **1**101101011111

RELATED PROBLEM

Add an even parity bit to the 7-bit ASCII code for the letter K.

EXAMPLE 40

An odd parity system receives the following code groups: 10110, 11010, 110011, 110101110100, and 1100010101010. Determine which groups, if any, are in error.

SOLUTION

Since odd parity is required, any group with an even number of 1s is incorrect. The following groups are in error: **110011** and **1100010101010**.

RELATED PROBLEM

The following ASCII character is received by an odd parity system: 00110111. Is it correct?

Cyclic Redundancy Check

The **cyclic redundancy check (CRC)** is a widely used code used for detecting one- and two-bit transmission errors when digital data is transferred on a communication link. The communication link can be between two computers that are connected to a network or between a digital storage device (such as a CD, DVD, or a hard drive) and a PC. If it is properly designed, the CRC can also detect multiple errors for a number of bits in sequence (burst errors). In CRC, a certain number of check bits, sometimes called a *checksum*, are appended to the data bits (added to end) that are being transmitted. The transmitted data is tested by the receiver for errors using the CRC. Not every possible error can be identified, but the CRC is much more efficient than just a simple parity check.

CRC is often described mathematically as the division of two polynomials to generate a remainder. A polynomial is a mathematical expression that is a sum of terms with positive exponents. When the coefficients are limited to 1s and 0s, it is called a *univariate polynomial*. An example of a univariate polynomial is $1x^3 + 0x^2 + 1x^1 + 1x^0$ or simply $x^3 + x^1 + x^0$, which can be fully described by the 4-bit binary number 1011. Most cyclic redundancy checks use a 16-bit or larger polynomial, but for simplicity the process is illustrated here with four bits.

MODULO-2 OPERATIONS Simply put, CRC is based on the division of two binary numbers; and, as you know, division is just a series of subtractions and shifts. To do subtraction, a method called *modulo-2* addition can be used. Modulo-2 addition (or subtraction) is the same as binary addition with the carries discarded, as shown in the truth table in Table 10. **Truth tables** are widely used to describe the operation of

TABLE 10 •
Modulo-2 operation.

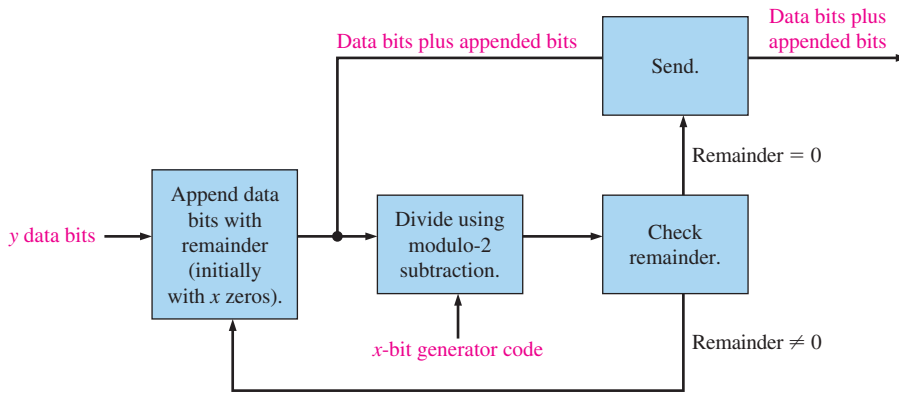
INPUT BITS	OUTPUT BIT
0 0	0
0 1	1
1 0	1
1 1	0

logic circuits. With two bits, there is a total of four possible combinations, as shown in the table. This particular table describes the modulo-2 operation also known as *exclusive-OR*. A simple rule for modulo-2 is that the output is 1 if the inputs are different; otherwise, it is 0.

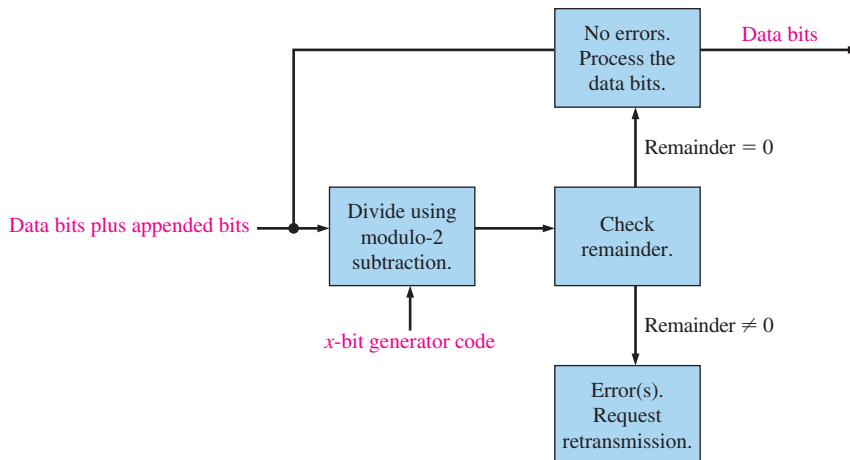
CRC PROCESS The process is as follows:

1. Select a fixed generator code; it can have fewer bits than the data bits to be checked. This code is understood in advance by both the sending and receiving devices and must be the same for both.
2. Append a number of 0s equal to the number of bits in the generator code to the data bits.
3. Divide the data bits including the appended bits by the generator code bits using modulo-2.
4. If the remainder is 0, the data and appended bits are sent as is.
5. If the remainder is not 0, the appended bits are made equal to the remainder bits in order to get a 0 remainder before data is sent.
6. At the receiving end, the receiver divides the incoming appended data bit code by the same generator code as used by the sender.
7. If the remainder is 0, there is no error detected (it is possible in rare cases for multiple errors to cancel). If the remainder is not 0, an error has been detected in the transmission and a retransmission is requested by the receiver.

Figure 8 illustrates the CRC process.



(a) Transmitting end of communication link



(b) Receiving end of communication link

FIGURE 8 The CRC process.

EXAMPLE 41

Determine the transmitted CRC for the following byte of data (D) and generator code (G). Verify that the remainder is 0.

D: 11010011

G: 1010

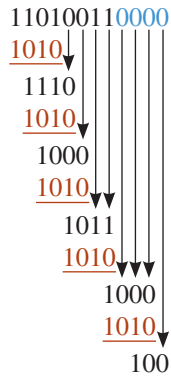
SOLUTION

Since the generator code has four data bits, add four 0s (blue) to the data byte. The appended data (D') is

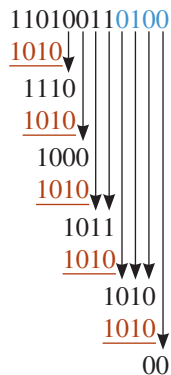
$$D' = 110100110000$$

Divide the appended data by the generator code (red) using the modulo-2 operation until all bits have been used.

$$\frac{D'}{G} = \frac{110100110000}{1010}$$



Remainder = 0100. Since the remainder is not 0, append the data with the four remainder bits (blue). Then divide by the generator code (red). The transmitted CRC is **110100110100**.



Remainder = 0

RELATED PROBLEM

Change the generator code to 1100 and verify that a 0 remainder results when the CRC process is applied to the data byte (11010011).

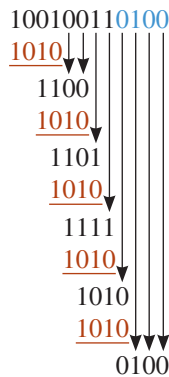
EXAMPLE 42

During transmission, an error occurs in the second bit from the left in the appended data byte generated in Example 41. The received data is

$$D' = 100100110100$$

Apply the CRC process to the received data to detect the error using the same generator code (1010).

SOLUTION



Remainder = 0100. Since it is not zero, an error is indicated.

RELATED PROBLEM

Assume two errors in the data byte as follows: 10011011. Apply the CRC process to check for the errors using the same received data and the same generator code.

SECTION 12 CHECKUP

1. Which odd-parity code is in error?
(a) 1011 (b) 1110 (c) 0101 (d) 1000
2. Which even-parity code is in error?
(a) 11000110 (b) 00101000
(c) 10101010 (d) 11111011
3. Add an even parity bit to the end of each of the following codes.
(a) 1010100 (b) 0100000
(c) 1110111 (d) 1000110
4. What does CRC stand for?
5. Apply modulo-2 operations to determine the following:
(a) 1 + 1 (b) 1 - 1 (c) 1 - 0 (d) 0 + 1

SUMMARY

- A binary number is a weighted number in which the weight of each whole number digit is a positive power of two and the weight of each fractional digit is a negative power of two. The whole number weights increase from right to left—from least significant digit to most significant.
- A binary number can be converted to a decimal number by summing the decimal values of the weights of all the 1s in the binary number.
- A decimal whole number can be converted to binary by using the sum-of-weights or the repeated division-by-2 method.
- A decimal fraction can be converted to binary by using the sum-of-weights or the repeated multiplication-by-2 method.

- The basic rules for binary addition are as follows:

$$\begin{aligned} 0 + 0 &= 0 \\ 0 + 1 &= 1 \\ 1 + 0 &= 1 \\ 1 + 1 &= 10 \end{aligned}$$

- The basic rules for binary subtraction are as follows:

$$\begin{aligned} 0 - 0 &= 0 \\ 1 - 1 &= 0 \\ 1 - 0 &= 1 \\ 10 - 1 &= 1 \end{aligned}$$

- The 1's complement of a binary number is derived by changing 1s to 0s and 0s to 1s.
- The 2's complement of a binary number can be derived by adding 1 to the 1's complement.
- Binary subtraction can be accomplished with addition by using the 1's or 2's complement method.
- A positive binary number is represented by a 0 sign bit.
- A negative binary number is represented by a 1 sign bit.
- For arithmetic operations, negative binary numbers are represented in 1's complement or 2's complement form.
- In an addition operation, an overflow is possible when both numbers are positive or when both numbers are negative. An incorrect sign bit in the sum indicates the occurrence of an overflow.
- The hexadecimal number system consists of 16 digits and characters, 0 through 9 followed by A through F.
- One hexadecimal digit represents a 4-bit binary number, and its primary usefulness is in simplifying bit patterns and making them easier to read.
- A decimal number can be converted to hexadecimal by the repeated division-by-16 method.
- The octal number system consists of eight digits, 0 through 7.
- A decimal number can be converted to octal by using the repeated division-by-8 method.
- Octal-to-binary conversion is accomplished by simply replacing each octal digit with its 3-bit binary equivalent. The process is reversed for binary-to-octal conversion.
- A decimal number is converted to BCD by replacing each decimal digit with the appropriate 4-bit binary code.
- The ASCII is a 7-bit alphanumeric code that is widely used in computer systems for input and output of information.
- A parity bit is used to detect an error in a code.
- The CRC (cyclic redundancy check) is based on polynomial division using modulo-2 operations.

KEY TERMS

Alphanumeric Consisting of numerals, letters, and other characters.

ASCII American Standard Code for Information Interchange; the most widely used alphanumeric code.

BCD Binary coded decimal; a digital code in which each of the decimal digits, 0 through 9, is represented by a group of four bits.

Byte A group of eight bits.

Cyclic redundancy check (CRC) A type of error detection code.

Floating-point number A number representation based on scientific notation in which the number consists of an exponent and a mantissa.

Hexadecimal Describes a number system with a base of 16.

LSB Least significant bit; the right-most bit in a binary whole number or code.

MSB Most significant bit; the left-most bit in a binary whole number or code.

Octal Describes a number system with a base of eight.

Parity In relation to binary codes, the condition of evenness or oddness of the number of 1s in a code group.

TRUE/FALSE QUIZ

Answers are at the end of the chapter.

1. The decimal number system is a weighted system with ten digits.
2. The binary number system is a weighted system with two digits.
3. LSB stands for lowest single bit.
4. In binary, $1 + 1 = 2$.
5. The 1's complement of the binary number 1010 is 0101.
6. The 2's complement of the binary number 0001 is 1110.
7. The right-most bit in a signed binary number is the sign bit.
8. The hexadecimal number system has 16 characters, six of which are alphabetic characters.
9. BCD stands for binary coded decimal.
10. ASCII stands for American standard code for information indication.
11. CRC stands for cyclic redundancy check.
12. The modulo-2 sum of 11 and 10 is 100.

SELF-TEST

Answers are at the end of the chapter.

1. $2 \times 10^1 + 8 \times 10^0$ is equal to
(a) 10 (b) 280 (c) 2.8 (d) 28
2. The binary number 1101 is equal to the decimal number
(a) 13 (b) 49 (c) 11 (d) 3
3. The binary number 11011101 is equal to the decimal number
(a) 121 (b) 221 (c) 441 (d) 256
4. The decimal number 17 is equal to the binary number
(a) 10010 (b) 11000 (c) 10001 (d) 01001
5. The decimal number 175 is equal to the binary number
(a) 11001111 (b) 10101110 (c) 10101111 (d) 11101111
6. The sum of 11010 + 01111 equals
(a) 101001 (b) 101010 (c) 110101 (d) 101000
7. The difference of $110 - 010$ equals
(a) 001 (b) 010 (c) 101 (d) 100
8. The 1's complement of 10111001 is
(a) 01000111 (b) 01000110 (c) 11000110 (d) 10101010
9. The 2's complement of 11001000 is
(a) 00110111 (b) 00110001 (c) 01001000 (d) 00111000
10. The decimal number +122 is expressed in the 2's complement form as
(a) 01111010 (b) 11111010 (c) 01000101 (d) 10000101
11. The decimal number -34 is expressed in the 2's complement form as
(a) 01011110 (b) 10100010 (c) 11011110 (d) 01011101
12. A single-precision floating-point binary number has a total of
(a) 8 bits (b) 16 bits (c) 24 bits (d) 32 bits
13. In the 2's complement form, the binary number 10010011 is equal to the decimal number
(a) -19 (b) +109 (c) +91 (d) -109

14. The binary number 101100111001010100001 can be written in octal as
 (a) 5471230₈ (b) 5471241₈ (c) 2634521₈ (d) 23162501₈
15. The binary number 10001101010001101111 can be written in hexadecimal as
 (a) AD467₁₆ (b) 8C46F₁₆ (c) 8D46F₁₆ (d) AE46F₁₆
16. The binary number for F7A9₁₆ is
 (a) 1111011110101001 (b) 1110111110101001
 (c) 111111101010001 (d) 1111011010101001
17. The BCD number for decimal 473 is
 (a) 111011010 (b) 110001110011 (c) 010001110011 (d) 010011110011
18. Refer to Table 7. The command STOP in ASCII is
 (a) 1010011101010010011111010000 (b) 1010010100110010011101010000
 (c) 1001010110110110011101010001 (d) 1010011101010010011101100100
19. The code that has an even-parity error is
 (a) 1010011 (b) 1101000 (c) 1001000 (d) 1110111
20. In the cyclic redundancy check, the absence of errors is indicated by
 (a) Remainder = generator code (b) Remainder = 0
 (c) Remainder = 1 (d) Quotient = 0

PROBLEMS

Answers to odd-numbered problems are at the end of the chapter.

SECTION 1 The Decimal Number System

1. What is the weight of the digit 6 in each of the following decimal numbers?
 (a) 1386 (b) 54,692 (c) 671,920
2. Express each of the following decimal numbers as a power of ten:
 (a) 10 (b) 100 (c) 10,000 (d) 1,000,000
3. Give the value of each digit in the following decimal numbers:
 (a) 471 (b) 9356 (c) 125,000
4. How high can you count with four decimal digits?

SECTION 2 The Binary Number System

5. Convert the following binary numbers to decimal:
 (a) 11 (b) 100 (c) 111 (d) 1000
 (e) 1001 (f) 1100 (g) 1011 (h) 1111
6. Convert the following binary numbers to decimal:
 (a) 1110 (b) 1010 (c) 11100 (d) 10000
 (e) 10101 (f) 11101 (g) 10111 (h) 11111
7. Convert each binary number to decimal:
 (a) 110011.11 (b) 101010.01 (c) 1000001.111
 (d) 1111000.101 (e) 1011100.10101 (f) 1110001.0001
 (g) 1011010.1010 (h) 1111111.11111
8. What is the highest decimal number that can be represented by each of the following numbers of binary digits (bits)?
 (a) two (b) three (c) four (d) five (e) six
 (f) seven (g) eight (h) nine (i) ten (j) eleven
9. How many bits are required to represent the following decimal numbers?
 (a) 17 (b) 35 (c) 49 (d) 68
 (e) 81 (f) 114 (g) 132 (h) 205
10. Generate the binary sequence for each decimal sequence:
 (a) 0 through 7 (b) 8 through 15 (c) 16 through 31
 (d) 32 through 63 (e) 64 through 75

SECTION 3 Decimal-to-Binary Conversion

11. Convert each decimal number to binary by using the sum-of-weights method:
 (a) 10 (b) 17 (c) 24 (d) 48
 (e) 61 (f) 93 (g) 125 (h) 186
12. Convert each decimal fraction to binary using the sum-of-weights method:
 (a) 0.32 (b) 0.246 (c) 0.0981
13. Convert each decimal number to binary using repeated division by 2:
 (a) 15 (b) 21 (c) 28 (d) 34
 (e) 40 (f) 59 (g) 65 (h) 73
14. Convert each decimal fraction to binary using repeated multiplication by 2:
 (a) 0.98 (b) 0.347 (c) 0.9028

SECTION 4 Binary Arithmetic

15. Add the binary numbers:
 (a) $11 + 01$ (b) $10 + 10$ (c) $101 + 11$
 (d) $111 + 110$ (e) $1001 + 101$ (f) $1101 + 1011$
16. Use direct subtraction on the following binary numbers:
 (a) $11 - 1$ (b) $101 - 100$ (c) $110 - 101$
 (d) $1110 - 11$ (e) $1100 - 1001$ (f) $11010 - 10111$
17. Perform the following binary multiplications:
 (a) 11×11 (b) 100×10 (c) 111×101
 (d) 1001×110 (e) 1101×1101 (f) 1110×1101
18. Divide the binary numbers as indicated:
 (a) $100 \div 10$ (b) $1001 \div 11$ (c) $1100 \div 100$

SECTION 5 1's and 2's Complements of Binary Numbers

19. What are two ways of representing zero in 1's complement form?
20. How is zero represented in 2's complement form?
21. Determine the 1's complement of each binary number:
 (a) 101 (b) 110 (c) 1010
 (d) 11010111 (e) 1110101 (f) 00001
22. Determine the 2's complement of each binary number using either method:
 (a) 10 (b) 111 (c) 1001 (d) 1101
 (e) 11100 (f) 10011 (g) 10110000 (h) 00111101

SECTION 6 Signed Numbers

23. Express each decimal number in binary as an 8-bit sign-magnitude number:
 (a) +29 (b) -85 (c) +100 (d) -123
24. Express each decimal number as an 8-bit number in the 1's complement form:
 (a) -34 (b) +57 (c) -99 (d) +115
25. Express each decimal number as an 8-bit number in the 2's complement form:
 (a) +12 (b) -68 (c) +101 (d) -125
26. Determine the decimal value of each signed binary number in the sign-magnitude form:
 (a) 10011001 (b) 01110100 (c) 10111111
27. Determine the decimal value of each signed binary number in the 1's complement form:
 (a) 10011001 (b) 01110100 (c) 10111111
28. Determine the decimal value of each signed binary number in the 2's complement form:
 (a) 10011001 (b) 01110100 (c) 10111111
29. Express each of the following sign-magnitude binary numbers in single-precision floating-point format:
 (a) 0111110000101011 (b) 100110000011000
30. Determine the values of the following single-precision floating-point numbers:
 (a) 1 10000001 0100100111000100000000
 (b) 0 11001100 10000111110100100000000

SECTION 7 Arithmetic Operations with Signed Numbers

31. Convert each pair of decimal numbers to binary and add using the 2's complement form:
 (a) 33 and 15 (b) 56 and -27 (c) -46 and 25 (d) -110 and -84
32. Perform each addition in the 2's complement form:
 (a) 00010110 + 00110011 (b) 01110000 + 10101111
33. Perform each addition in the 2's complement form:
 (a) 10001100 + 00111001 (b) 11011001 + 11100111
34. Perform each subtraction in the 2's complement form:
 (a) 00110011 - 00010000 (b) 01100101 - 11101000
35. Multiply 01101010 by 11110001 in the 2's complement form.
36. Divide 01000100 by 00011001 in the 2's complement form.

SECTION 8 Hexadecimal Numbers

37. Convert each hexadecimal number to binary:
 (a) 38_{16} (b) 59_{16} (c) $A14_{16}$ (d) $5C8_{16}$
 (e) 4100_{16} (f) $FB17_{16}$ (g) $8A9D_{16}$
38. Convert each binary number to hexadecimal:
 (a) 1110 (b) 10 (c) 10111
 (d) 10100110 (e) 1111110000 (f) 100110000010
39. Convert each hexadecimal number to decimal:
 (a) 23_{16} (b) 92_{16} (c) $1A_{16}$ (d) $8D_{16}$
 (e) $F3_{16}$ (f) EB_{16} (g) $5C2_{16}$ (h) 700_{16}
40. Convert each decimal number to hexadecimal:
 (a) 8 (b) 14 (c) 33 (d) 52
 (e) 284 (f) 2890 (g) 4019 (h) 6500
41. Perform the following additions:
 (a) $37_{16} + 29_{16}$ (b) $A0_{16} + 6B_{16}$ (c) $FF_{16} + BB_{16}$
42. Perform the following subtractions:
 (a) $51_{16} - 40_{16}$ (b) $C8_{16} - 3A_{16}$ (c) $FD_{16} - 88_{16}$

SECTION 9 Octal Numbers

43. Convert each octal number to decimal:
 (a) 12_8 (b) 27_8 (c) 56_8 (d) 64_8 (e) 103_8
 (f) 557_8 (g) 163_8 (h) 1024_8 (i) 7765_8
44. Convert each decimal number to octal by repeated division by 8:
 (a) 15 (b) 27 (c) 46 (d) 70
 (e) 100 (f) 142 (g) 219 (h) 435
45. Convert each octal number to binary:
 (a) 13_8 (b) 57_8 (c) 101_8 (d) 321_8 (e) 540_8
 (f) 4653_8 (g) 13271_8 (h) 45600_8 (i) 100213_8
46. Convert each binary number to octal:
 (a) 111 (b) 10 (c) 110111
 (d) 101010 (e) 1100 (f) 1011110
 (g) 101100011001 (h) 10110000011 (i) 111111101111000

SECTION 10 Binary Coded Decimal (BCD)

47. Convert each of the following decimal numbers to 8421 BCD:
 (a) 10 (b) 13 (c) 18 (d) 21 (e) 25 (f) 36
 (g) 44 (h) 57 (i) 69 (j) 98 (k) 125 (l) 156
48. Convert each of the decimal numbers in Problem 47 to straight binary, and compare the number of bits required with that required for BCD.
49. Convert the following decimal numbers to BCD:
 (a) 104 (b) 128 (c) 132 (d) 150 (e) 186
 (f) 210 (g) 359 (h) 547 (i) 1051

50. Convert each of the BCD numbers to decimal:
 (a) 0001 (b) 0110 (c) 1001
 (d) 00011000 (e) 00011001 (f) 00110010
 (g) 01000101 (h) 10011000 (i) 100001110000
51. Convert each of the BCD numbers to decimal:
 (a) 10000000 (b) 001000110111
 (c) 001101000110 (d) 010000100001
 (e) 011101010100 (f) 100000000000
 (g) 100101111000 (h) 0001011010000011
 (i) 1001000000011000 (j) 0110011001100111
52. Add the following BCD numbers:
 (a) 0010 + 0001 (b) 0101 + 0011
 (c) 0111 + 0010 (d) 1000 + 0001
 (e) 00011000 + 00010001 (f) 01100100 + 00110011
 (g) 01000000 + 01000111 (h) 10000101 + 00010011
53. Add the following BCD numbers:
 (a) 1000 + 0110 (b) 0111 + 0101
 (c) 1001 + 1000 (d) 1001 + 0111
 (e) 00100101 + 00100111 (f) 01010001 + 01011000
 (g) 10011000 + 10010111 (h) 010101100001 + 011100001000
54. Convert each pair of decimal numbers to BCD, and add as indicated:
 (a) 4 + 3 (b) 5 + 2 (c) 6 + 4 (d) 17 + 12
 (e) 28 + 23 (f) 65 + 58 (g) 113 + 101 (h) 295 + 157

SECTION 11 Digital Codes

55. In a certain application a 4-bit binary sequence cycles from 1111 to 0000 periodically. There are four bit changes, and because of circuit delays, these changes may not occur at the same instant. For example, if the LSB changes first, the number will appear as 1110 during the transition from 1111 to 0000 and may be misinterpreted by the system. Illustrate how the Gray code avoids this problem.
56. Convert each binary number to Gray code:
 (a) 11011 (b) 1001010 (c) 1111011101110
57. Convert each Gray code to binary:
 (a) 1010 (b) 00010 (c) 11000010001
58. Convert each of the following decimal numbers to ASCII. Refer to Table 7.
 (a) 1 (b) 3 (c) 6 (d) 10 (e) 18
 (f) 29 (g) 56 (h) 75 (i) 107
59. Determine each ASCII character. Refer to Table 7.
 (a) 0011000 (b) 1001010 (c) 0111101
 (d) 0100011 (e) 0111110 (f) 1000010
60. Decode the following ASCII coded message:
 1001000 1100101 1101100 1101100 1101111 0101110
 0100000 1001000 1101111 1110111 0100000 1100001
 1110010 1100101 0100000 1111001 1101111 1110101
 0111111
61. Write the message in Problem 60 in hexadecimal.
62. Convert the following statement to ASCII:
 30 INPUT A, B

SECTION 12 Error Detection Codes

63. Determine which of the following even parity codes are in error:
 (a) 100110010 (b) 011101010 (c) 10111111010001010
64. Determine which of the following odd parity codes are in error:
 (a) 11110110 (b) 00110001 (c) 01010101010101010
65. Attach the proper even parity bit to each of the following bytes of data:
 (a) 10100100 (b) 00001001 (c) 11111110
66. Apply modulo-2 to the following:
 (a) 1100 + 1011 (b) 1111 + 0100 (c) 10011001 + 100011100

67. Verify that modulo-2 subtraction is the same as modulo-2 addition by adding the result of each operation in problem 66 to either of the original numbers to get the other number. This will show that the result is the same as the difference of the two numbers.
68. Apply CRC to the data bits 10110010 using the generator code 1010 to produce the transmitted CRC code.
69. Assume that the code produced in problem 68 incurs an error in the most significant bit during transmission. Apply CRC to detect the error.

ANSWERS TO SECTION CHECKUPS

SECTION 1 The Decimal Number System

1. (a) 1370: 10 (b) 6725: 100 (c) 7051: 1000 (d) 58.72: 0.1
2. (a) $51 = (5 \times 10) + (1 \times 1)$ (b) $137 = (1 \times 100) + (3 \times 10) + (7 \times 1)$
 (c) $1492 = (1 \times 1000) + (4 \times 100) + (9 \times 10) + (2 \times 1)$
 (d) $106.58 = (1 \times 100) + (0 \times 10) + (6 \times 1) + (5 \times 0.1) + (8 \times 0.01)$

SECTION 2 The Binary Number System

1. $2^8 - 1 = 255$
2. Weight is 16.
3. $10111101.011 = 189.375$

SECTION 3 Decimal-to-Binary Conversion

1. (a) $23 = 10111$ (b) $57 = 111001$ (c) $45.5 = 101101.1$
2. (a) $14 = 1110$ (b) $21 = 10101$ (c) $0.375 = 0.011$

SECTION 4 Binary Arithmetic

1. (a) $1101 + 1010 = 10111$ (b) $10111 + 01101 = 100100$
2. (a) $1101 - 0100 = 1001$ (b) $1001 - 0111 = 0010$
3. (a) $110 \times 111 = 101010$ (b) $1100 \div 011 = 100$

SECTION 5 1's and 2's Complements of Binary Numbers

1. (a) 1's comp of 00011010 = 11100101 (b) 1's comp of 11110111 = 00001000
 (c) 1's comp of 10001101 = 01110010
2. (a) 2's comp of 00010110 = 11101010 (b) 2's comp of 11111100 = 00000100
 (c) 2's comp of 10010001 = 01101111

SECTION 6 Signed Numbers

1. Sign-magnitude: $+9 = 00001001$
2. 1's comp: $-33 = 11011110$
3. 2's comp: $-46 = 11010010$
4. Sign bit, exponent, and mantissa

SECTION 7 Arithmetic Operations with Signed Numbers

1. Cases of addition: positive number is larger, negative number is larger, both are positive, both are negative
2. $00100001 + 10111100 = 11011101$
3. $01110111 - 00110010 = 01000101$
4. Sign of product is positive.
5. $00000101 \times 01111111 = 01001111011$
6. Sign of quotient is negative.
7. $00110000 \div 00001100 = 00000100$

SECTION 8 Hexadecimal Numbers

1. (a) $10110011 = B3_{16}$ (b) $110011101000 = CE8_{16}$
2. (a) $57_{16} = 01010111$ (b) $3A5_{16} = 001110100101$
(c) $F80B_{16} = 1111100000001011$
3. $9B30_{16} = 39,728_{10}$
4. $573_{10} = 23D_{16}$
5. (a) $18_{16} + 34_{16} = 4C_{16}$ (b) $3F_{16} + 2A_{16} = 69_{16}$
6. (a) $75_{16} - 21_{16} = 54_{16}$ (b) $94_{16} - 5C_{16} = 38_{16}$

SECTION 9 Octal Numbers

1. (a) $73_8 = 59_{10}$ (b) $125_8 = 85_{10}$
2. (a) $98_{10} = 142_8$ (b) $163_{10} = 243_8$
3. (a) $46_8 = 100110$ (b) $723_8 = 111010011$ (c) $5624_8 = 101110010100$
4. (a) $110101111 = 657_8$ (b) $1001100010 = 1142_8$ (c) $10111111001 = 2771_8$

SECTION 10 Binary Coded Decimal (BCD)

1. (a) 0010: 2 (b) 1000: 8 (c) 0001: 1 (d) 0100: 4
2. (a) $6_{10} = 0110$ (b) $15_{10} = 00010101$ (c) $273_{10} = 001001110011$
(d) $849_{10} = 100001001001$
3. (a) $10001001 = 89_{10}$ (b) $001001111000 = 278_{10}$ (c) $000101010111 = 157_{10}$
4. A 4-bit sum is invalid when it is greater than 9_{10} .

SECTION 11 Digital Codes

1. (a) $1100_2 = 1010$ Gray (b) $1010_2 = 1111$ Gray (c) $11010_2 = 10111$ Gray
2. (a) 1000 Gray = 1111_2 (b) 1010 Gray = 1100_2 (c) 11101 Gray = 10110_2
3. (a) K: $1001011 \rightarrow 4B_{16}$ (b) r: $1110010 \rightarrow 72_{16}$
(c) $\$: 0100100 \rightarrow 24_{16}$ (d) $+: 0101011 \rightarrow 2B_{16}$

SECTION 12 Error Detection Codes

1. (c) 0101 has an error.
2. (d) 11111011 has an error.
3. (a) 1010100**1** (b) 0100000**1** (c) 1110111**0** (d) 1000110**1**
4. Cyclic redundancy check
5. (a) 0 (b) 0 (c) 1 (d) 1

ANSWERS TO RELATED PROBLEMS FOR EXAMPLES

- 1 9 has a value of 900, 3 has a value of 30, 9 has a value of 9.
- 2 6 has a value of 60, 7 has a value of 7, 9 has a value of 9/10 (0.9), 2 has a value of 2/100 (0.02), 4 has a value of 4/1000 (0.004).
- 3 $10010001 = 128 + 16 + 1 = 145$
- 4 $10.111 = 2 + 0.5 + 0.25 + 0.125 = 2.875$
- 5 $125 = 64 + 32 + 16 + 8 + 4 + 1 = 1111101$
- 6 $39 = 100111$
- 7 $1111 + 1100 = 11011$
- 8 $111 - 100 = 011$
- 9 $110 - 101 = 001$
- 10 $1101 \times 1010 = 10000010$
- 11 $1100 \div 100 = 11$

- 12 00110101
- 13 01000000
- 14 See Table 11.

TABLE 11			
	SIGN-MAGNITUDE	1'S COMP	2'S COMP
+19	00010011	00010011	00010011
-19	10010011	11101100	11101101

- 15 $01110111 = +119_{10}$
- 16 $11101011 = -20_{10}$
- 17 $11010111 = -41_{10}$
- 18 11000010001010011000000000
- 19 01010101
- 20 00010001
- 21 1001000110
- 22 $(83)(-59) = -4897$ (10110011011111 in 2's comp)
- 23 $100 \div 25 = 4$ (0100)
- 24 $4F79C_{16}$
- 25 0110101111010011₂
- 26 $6BD_{16} = 011010111101 = 2^{10} + 2^9 + 2^7 + 2^5 + 2^4 + 2^3 + 2^2 + 2^0$
 $= 1024 + 512 + 128 + 32 + 16 + 8 + 4 + 1 = 1725_{10}$
- 27 $60A_{16} = (6 \times 256) + (0 \times 16) + (10 \times 1) = 1546_{10}$
- 28 $2591_{10} = A1F_{16}$
- 29 $4C_{16} + 3A_{16} = 86_{16}$
- 30 $BCD_{16} - 173_{16} = A5A_{16}$
- 31 (a) $001011_2 = 11_{10} = 13_8$ (b) $010101_2 = 21_{10} = 25_8$
 (c) $001100000_2 = 96_{10} = 140_8$ (d) $111101010110_2 = 3926_{10} = 7526_8$
- 32 1250762_8 33 1001011001110011 34 $82,276_{10}$
- 35 1001100101101000 36 10000010 37 (a) 111011 (Gray) (b) 111010₂
- 38 The sequence of codes for if $(y < 8)$ is $69_{16}66_{16}20_{16}28_{16}79_{16}3C_{16}38_{16}29_{16}$
- 39 01001011
- 40 Yes
- 41 A 0 remainder results
- 42 Errors are indicated.

ANSWERS TO TRUE/FALSE QUIZ

- 1. T 2. T 3. F 4. F 5. T 6. F
- 7. F 8. T 9. T 10. F 11. T 12. F

ANSWERS TO SELF-TEST

- 1. (d) 2. (a) 3. (b) 4. (c) 5. (c) 6. (a) 7. (d) 8. (b)
- 9. (d) 10. (a) 11. (c) 12. (d) 13. (d) 14. (b) 15. (c) 16. (a)
- 17. (c) 18. (a) 19. (b) 20. (b)

ANSWERS TO ODD-NUMBERED PROBLEMS

1. (a) 1 (b) 100 (c) 100,000
3. (a) 400; 70; 1 (b) 9000; 300; 50; 6
(c) 100,000; 20,000; 5000; 0; 0; 0
5. (a) 3 (b) 4 (c) 7 (d) 8 (e) 9
(f) 12 (g) 11 (h) 15
7. (a) 51.75 (b) 42.25 (c) 65.875
(d) 120.625 (e) 92.65625 (f) 113.0625
(g) 90.625 (h) 127.96875
9. (a) 5 bits (b) 6 bits (c) 6 bits (d) 7 bits
(e) 7 bits (f) 7 bits (g) 8 bits (h) 8 bits
11. (a) 1010 (b) 10001 (c) 11000
(d) 110000 (e) 111101 (f) 1011101
(g) 1111101 (h) 10111010
13. (a) 1111 (b) 10101 (c) 11100
(d) 100010 (e) 101000 (f) 111011
(g) 1000001 (h) 1001001
15. (a) 100 (b) 100 (c) 1000
(d) 1101 (e) 1110 (f) 11000
17. (a) 1001 (b) 1000 (c) 100011
(d) 110110 (e) 10101001 (f) 10110110
19. all 0s or all 1s
21. (a) 010 (b) 001 (c) 0101
(d) 00101000 (e) 0001010 (f) 11110
23. (a) 00011101 (b) 11010101
(c) 01100100 (d) 11111011
25. (a) 00001100 (b) 10111100
(c) 01100101 (d) 10000011
27. (a) -102 (b) +116 (c) -64
29. (a) 0 10001101 11110000101011000000000
(b) 1 10001010 11000001100000000000000
31. (a) 00110000 (b) 00011101
(c) 11101011 (d) 100111110
33. (a) 11000101 (b) 11000000
35. 100111001010
37. (a) 00111000 (b) 01011001
(c) 101000010100 (d) 010111001000
(e) 0100000100000000 (f) 1111101100010111
(g) 1000101010011101
39. (a) 35 (b) 146 (c) 26 (d) 141
(e) 243 (f) 235 (g) 1474 (h) 1792
41. (a) 60_{16} (b) $10B_{16}$ (c) $1BA_{16}$
43. (a) 10 (b) 23 (c) 46 (d) 52 (e) 67
(f) 367 (g) 115 (h) 532 (i) 4085
45. (a) 001011 (b) 101111
(c) 001000001 (d) 011010001

NUMBER SYSTEMS, OPERATIONS, AND CODES

- (e) 101100000 (f) 100110101011
 (g) 001011010111001 (h) 100101110000000
 (i) 001000000010001011
47. (a) 00010000 (b) 00010011
 (c) 00011000 (d) 00100001
 (e) 00100101 (f) 00110110
 (g) 01000100 (h) 01010111
 (i) 01101001 (j) 10011000
 (k) 000100100101 (l) 000101010110
49. (a) 000100000100 (b) 000100101000
 (c) 000100110010 (d) 000101010000
 (e) 000110000110 (f) 001000010000
 (g) 001101011001 (h) 010101000111
 (i) 0001000001010001
51. (a) 80 (b) 237 (c) 346 (d) 421
 (e) 754 (f) 800 (g) 978 (h) 1683
 (i) 9018 (j) 6667
53. (a) 00010100 (b) 00010010
 (c) 00010111 (d) 00010110
 (e) 01010010 (f) 000100001001
 (g) 000110010101 (h) 0001001001101001
55. The Gray code makes only one bit change at a time when going from one number in the sequence to the next.
57. (a) 1100 (b) 00011 (c) 10000011110
59. (a) CAN (b) J (c) =
 (d) # (e) > (f) B
61. 48 65 6C 6C 6F 2E 20 48 6F 77 20 61 72 65 20 79 6F 75 3F
63. (b) is incorrect.
65. (a) 110100100 (b) 000001001 (c) 111111110
67. In each case, you get the other number.
69. The remainder is 10, indicating an error.

LOGIC GATES AND GATE COMBINATIONS

OUTLINE

- 1 Introduction to Boolean Algebra
- 2 The Inverter
- 3 The AND Gate
- 4 The OR Gate
- 5 The NAND Gate
- 6 The NOR Gate
- 7 The Exclusive-OR and Exclusive-NOR Gates
- 8 Gate Performance Characteristics and Parameters
- 9 Programmable Logic
- 10 Troubleshooting

OBJECTIVES

- Apply Boolean arithmetic
- Apply the basic laws and rules of Boolean algebra
- Describe the operation of the inverter, the AND gate, and the OR gate
- Describe the operation of the NAND gate and the NOR gate
- Express the operation of NOT, AND, OR, NAND, and NOR gates with Boolean algebra
- Describe the operation of the exclusive-OR and exclusive-NOR gates
- Recognize and use both the distinctive shape logic gate symbols and the rectangular outline logic gate symbols of ANSI/IEEE Standard 91-1984

- Construct timing diagrams showing the proper time relationships of inputs and outputs for the various logic gates
- Define *propagation delay time*, *power dissipation*, *speed-power product*, and *fan-out* in relation to logic gates
- Use each logic gate in simple applications
- Discuss the basic concepts of programmable logic and describe logic gates using VHDL and Verilog
- Describe basic troubleshooting methods

KEY TERMS

Boolean algebra

Variable

Complement

Sum term

Product term

Inverter

Truth table

Timing diagram

AND gate

OR gate

NAND gate

NOR gate

Exclusive-OR gate

Exclusive-NOR gate

Propagation delay time

Fan-out

Unit load

AND array

Fuse

Antifuse

EPROM

EEPROM

Flash

SRAM

Target device

JTAG

VHDL

Verilog

VISIT THE WEBSITE

Study aids for this chapter are available at <http://pearsonhighered.com/floyd>

INTRODUCTION

The emphasis in this chapter is on the operation, application, and troubleshooting of logic gates. The relationship of input and output waveforms of a gate using timing diagrams is thoroughly covered. Boolean algebra is introduced.

Logic symbols used to represent the logic gates are in accordance with ANSI/IEEE Standard 91-1984. This standard has been adopted by private industry and the

military for use in internal documentation as well as published literature.

Programmable logic is discussed in this chapter because of the widespread use of PLDs. Because integrated circuits (ICs) are used in applications, the logic function of a device is generally of much greater importance to the technician or technologist than the details of the component-level circuit operation within the IC package. Hardware description languages (HDLs) for programmable logic are introduced.

1 INTRODUCTION TO BOOLEAN ALGEBRA

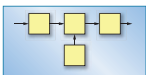
Boolean algebra is the mathematics of digital systems. A basic knowledge of Boolean algebra is indispensable to the study and analysis of logic circuits, such as NOT, AND, and OR.

After completing this section, you should be able to

- Define *variable*
- Define *literal*
- Identify a sum term
- Evaluate a sum term
- Identify a product term
- Evaluate a product term
- Explain Boolean addition
- Explain Boolean multiplication
- Apply the commutative laws of addition and multiplication
- Apply the associative laws of addition and multiplication
- Apply the distributive law
- Apply the rules of Boolean algebra

Boolean algebra* uses variables and operators to describe a logic circuit. *Variable*, *complement*, and *literal* are terms used in Boolean algebra. A **variable** is a symbol (usually an italic uppercase letter or word) used to represent an action, a condition, or data. Any single variable can have only a 1 or a 0 value. The **complement** is the inverse of a variable and is indicated by a bar over the variable (overbar). For example, the complement of the variable A is \bar{A} . If $A = 1$, then $\bar{A} = 0$. If $A = 0$, then $\bar{A} = 1$. The complement of the variable A is read as “not A ” or “ A bar.” Sometimes a prime symbol rather than an overbar is used to denote the complement of a variable; for example, B' indicates the complement of B . In this text, only the overbar is used. A **literal** is a constant value assigned to a variable or the complement of a variable.

In a microprocessor, the arithmetic logic unit (ALU) performs arithmetic and Boolean logic operations on digital data as directed by program instructions. Logical operations are equivalent to the basic gate operations that you are familiar with but deal with a minimum of 8 bits at a time. Examples of Boolean logic instructions are AND, OR, and NOT, which are called *mnemonics*. An assembly language program uses the mnemonics to specify an operation. Another program called an *assembler* translates the mnemonics into a binary code that can be understood by the microprocessor.



SYSTEM NOTE

*The bold terms in color are key terms and are included in a Key Term glossary at the end of the chapter.

Boolean Addition

Boolean addition is equivalent to the OR operation. The logical OR function of two variables is represented mathematically by a + between the two variables, for example, $A + B$. The plus sign is read as “OR.” Addition in Boolean algebra involves variables whose values are either binary 1 or binary 0. The basic rules of Boolean addition are illustrated in Figure 1 with their relation to the OR gate. Notice that Boolean addition differs from binary addition in the case where two 1s are added. There is no carry in Boolean addition.

In Boolean algebra, a **sum term** is a sum of literals. In logic circuits, a sum term is produced by an OR operation with no AND operations involved. Some examples of sum terms are $A + \bar{B}$, $A + B + \bar{C}$, and $\bar{A} + B + C + \bar{D}$. A sum term is equal to 1 when one or more of the literals in the term are 1. A sum term is equal to 0 only if each of the literals is 0.

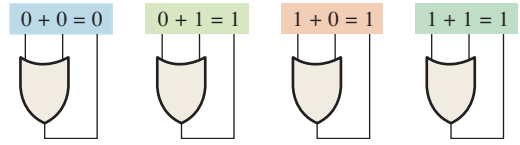


FIGURE 1

The OR operation is the Boolean form of addition.

EXAMPLE 1

Determine the values of A , B , C , and D that make the sum term $A + \bar{B} + C + \bar{D}$ equal to 0.

SOLUTION

For the sum term to be 0, each of the literals in the term must be 0. Therefore, $A = 0$, $B = 1$ so that $\bar{B} = 0$, $C = 0$, and $D = 1$ so that $\bar{D} = 0$.

$$A + \bar{B} + C + \bar{D} = 0 + \bar{1} + 0 + \bar{1} = 0 + 0 + 0 + 0 = 0$$

RELATED PROBLEM*

Determine the values of A and B that make the sum term $\bar{A} + B$ equal to 0.

*Answers are at the end of the chapter.

Boolean Multiplication

Boolean multiplication is equivalent to the AND operation. The logical AND function of two variables is represented mathematically either by placing a dot between the two variables, as $A \cdot B$, or by simply writing the adjacent letters without the dot, as AB . The variables are either binary 1 or binary 0, and the rules of binary multiplication apply to Boolean multiplication. The basic rules of Boolean multiplication are illustrated in Figure 2 with their relation to the AND gate.

In Boolean algebra, a **product term** is the product of literals. In logic circuits, a product term is produced by an AND operation with no OR operations involved. Some examples of product terms are $\bar{A}B$, ABC , and $\bar{A}BC\bar{D}$. A product term is equal to 1 only if each of the literals in the term is 1. A product term is equal to 0 when one or more of the literals are 0.

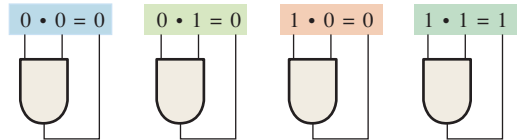


FIGURE 2

The AND operation is the Boolean form of multiplication.

EXAMPLE 2

Determine the values of A , B , C , and D that make the product term $\bar{A}BC\bar{D}$ equal to 1.

SOLUTION

For the product term to be 1, each of the literals in the term must be 1. Therefore, $A = 1$, $B = 0$ so that $\bar{B} = 1$, $C = 1$, and $D = 0$ so that $\bar{D} = 1$.

$$\bar{A}BC\bar{D} = 1 \cdot \bar{0} \cdot 1 \cdot \bar{0} = 1 \cdot 1 \cdot 1 \cdot 1 = 1$$

RELATED PROBLEM

Determine the values of A and B that make the product term $\bar{A}B$ equal to 1.

Laws of Boolean Algebra

The basic laws of Boolean algebra—the **commutative laws** for addition and multiplication, the **associative laws** for addition and multiplication, and the **distributive law**—are the same as in ordinary algebra. Each of the laws is illustrated with two or three variables, but the number of variables is not limited to this.

COMMUTATIVE LAWS The commutative law for the addition of two variables is written as

$$A + B = B + A \quad (1)$$

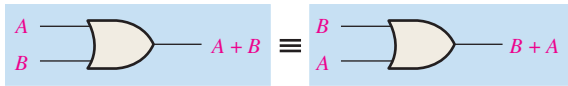


FIGURE 3 Application of the commutative law of addition.

This law states that the order in which the variables are ORed makes no difference. Figure 3 illustrates the commutative law as applied to the OR gate and shows that it doesn't matter to which input each variable is applied. (The symbol \equiv means "equivalent to.")

The commutative law for the multiplication of two variables is

$$AB = BA \quad (2)$$

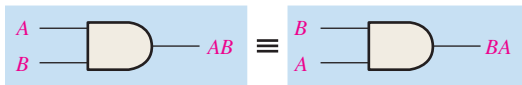


FIGURE 4 Application of the commutative law of multiplication.

This law states that the order in which the variables are ANDED makes no difference. Figure 4 illustrates this law as applied to the AND gate.

ASSOCIATIVE LAWS The associative law of addition is written as follows for three variables:

$$A + (B + C) = (A + B) + C \quad (3)$$

This law states that when ORing more than two variables, the result is the same regardless of the grouping of the variables. Figure 5 illustrates this law as applied to 2-input OR gates.

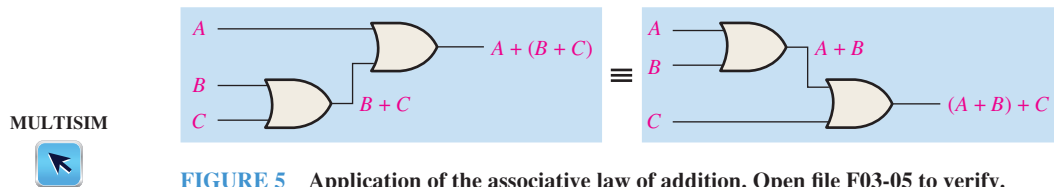


FIGURE 5 Application of the associative law of addition. Open file F03-05 to verify.

The associative law of multiplication is written as follows for three variables:

$$A(BC) = (AB)C \quad (4)$$

This law states that it makes no difference in what order the variables are grouped when ANDing more than two variables. Figure 6 illustrates this law as applied to 2-input AND gates.

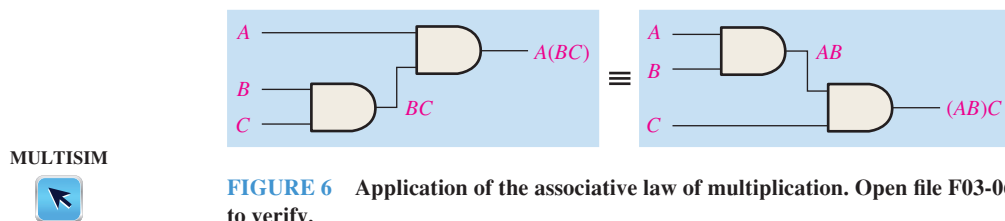


FIGURE 6 Application of the associative law of multiplication. Open file F03-06 to verify.

DISTRIBUTIVE LAW The distributive law is written for three variables as follows:

$$A(B + C) = AB + AC \quad (5)$$

This law states that ORing two or more variables and then ANDing the result with a single variable is equivalent to ANDing the single variable with each of the two or more variables and then ORing the products. The distributive law also expresses the process of *factoring* in which the common variable A is factored out of the product terms, for example, $AB + AC = A(B + C)$. Figure 7 illustrates the distributive law in terms of gate implementation.

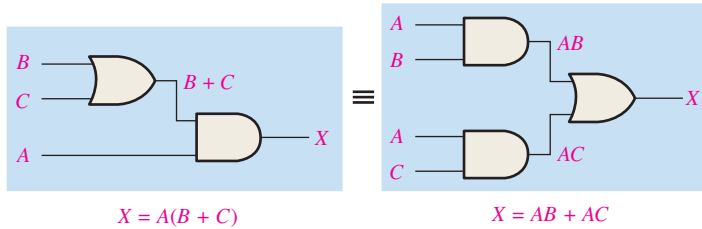


FIGURE 7 Application of distributive law. Open file F03-07 to verify.



Rules of Boolean Algebra

Table 1 lists 12 basic rules that are useful in manipulating and simplifying **Boolean expressions**. Rules 1 through 9 will be viewed in terms of their application to logic gates. Rules 10 through 12 will be derived in terms of the simpler rules and the laws previously discussed.

TABLE 1 • Basic rules of Boolean algebra.	
1. $A + 0 = A$	7. $A \cdot A = A$
2. $A + 1 = 1$	8. $A \cdot \bar{A} = 0$
3. $A \cdot 0 = 0$	9. $\bar{\bar{A}} = A$
4. $A \cdot 1 = A$	10. $A + AB = A$
5. $A + A = A$	11. $A + \bar{A}B = A + B$
6. $A + \bar{A} = 1$	12. $(A + B)(A + C) = A + BC$

$A, B,$ or C can represent a single variable or a combination of variables.

Rule 1: $A + 0 = A$ A variable ORed with 0 is always equal to the variable. If the input variable A is 1, the output variable X is 1, which is equal to A . If A is 0, the output is 0, which is also equal to A . This rule is illustrated in Figure 8, where the lower input is fixed at 0.

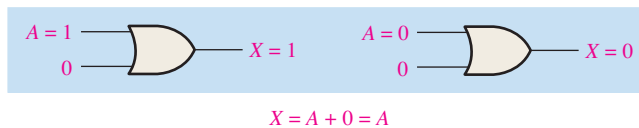


FIGURE 8

Rule 2: $A + 1 = 1$ A variable ORed with 1 is always equal to 1. A 1 on an input to an OR gate produces a 1 on the output, regardless of the value of the variable on the other input. This rule is illustrated in Figure 9, where the lower input is fixed at 1.

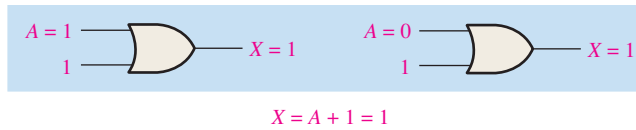


FIGURE 9

Rule 3: $A \cdot 0 = 0$ A variable ANDed with 0 is always equal to 0. Any time one input to an AND gate is 0, the output is 0, regardless of the value of the variable on the other input. This rule is illustrated in Figure 10, where the lower input is fixed at 0.

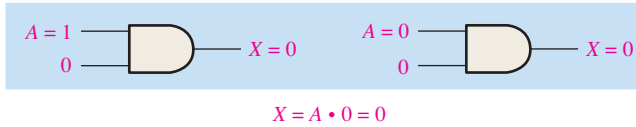


FIGURE 10

Rule 4: $A \cdot 1 = A$ A variable ANDed with 1 is always equal to the variable. If A is 0, the output of the AND gate is 0. If A is 1, the output of the AND gate is 1 because both inputs are now 1s. This rule is shown in Figure 11, where the lower input is fixed at 1.

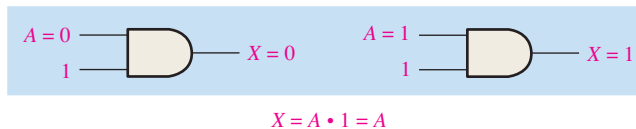


FIGURE 11

Rule 5: $A + A = A$ A variable ORed with itself is always equal to the variable. If A is 0, then $0 + 0 = 0$; and if A is 1, then $1 + 1 = 1$. This is shown in Figure 12, where both inputs are the same variable.

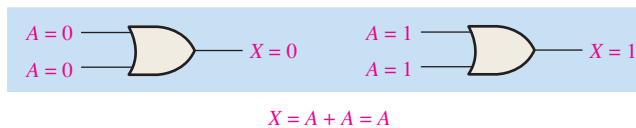


FIGURE 12

Rule 6: $A + \bar{A} = 1$ A variable ORed with its complement is always equal to 1. If A is 0, then $0 + \bar{0} = 0 + 1 = 1$. If A is 1, then $1 + \bar{1} = 1 + 0 = 1$. See Figure 13, where one input is the complement of the other.

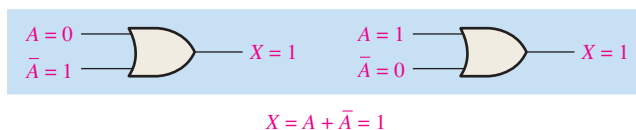


FIGURE 13

Rule 7: $A \cdot A = A$ A variable ANDed with itself is always equal to the variable. If $A = 0$, then $0 \cdot 0 = 0$; and if $A = 1$, then $1 \cdot 1 = 1$. Figure 14 illustrates this rule.

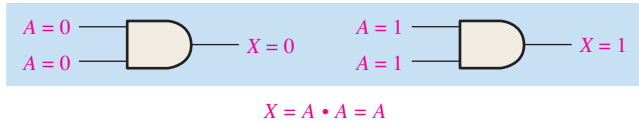


FIGURE 14

Rule 8: $A \cdot \bar{A} = 0$ A variable ANDed with its complement is always equal to 0. Either A or \bar{A} will always be 0; and when a 0 is applied to the input of an AND gate, the output will be 0 also. Figure 15 illustrates this rule.

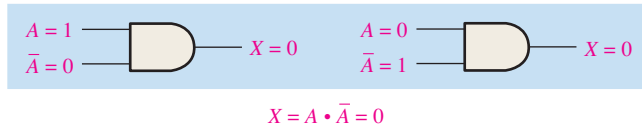


FIGURE 15

Rule 9: $\bar{\bar{A}} = A$ The double complement of a variable is always equal to the variable. If you start with the variable A and complement (invert) it once, you get \bar{A} . If you then take \bar{A} and complement (invert) it, you get A , which is the original variable. This rule is shown in Figure 16 using inverters.

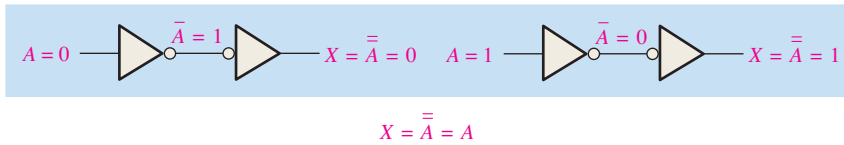


FIGURE 16

Rule 10: $A + AB = A$ This rule can be proved by applying the distributive law, rule 2, and rule 4 as follows:

$$\begin{aligned}
 A + AB &= A \cdot 1 + AB = A(1 + B) && \text{Factoring (distributive law)} \\
 &= A \cdot 1 && \text{Rule 2: } (1 + B) = 1 \\
 &= A && \text{Rule 4: } A \cdot 1 = A
 \end{aligned}$$

The proof is shown in Table 2, which shows the truth table and the resulting logic circuit simplification.

TABLE 2 • Rule 10: $A + AB = A$. Open file T03-02 to verify.			
A	B	AB	A + AB
0	0	0	0
0	1	0	0
1	0	0	1
1	1	1	1
↑		equal	↑

MULTISIM



Rule 11: $A + \bar{A}B = A + B$ This rule can be proved as follows:

$$\begin{aligned}
 A + \bar{A}B &= (A + AB) + \bar{A}B && \text{Rule 10: } A = A + AB \\
 &= (AA + AB) + \bar{A}B && \text{Rule 7: } A = AA \\
 &= AA + AB + \bar{A}A + \bar{A}B && \text{Rule 8: adding } \bar{A}A = 0 \\
 &= (A + \bar{A})(A + B) && \text{Factoring} \\
 &= 1 \cdot (A + B) && \text{Rule 6: } A + \bar{A} = 1 \\
 &= A + B && \text{Rule 4: drop the 1}
 \end{aligned}$$

The proof is shown in Table 3, which shows the truth table and the resulting logic circuit simplification.

MULTISIM



TABLE 3 • Rule 11: $A + \bar{A}B = A + B$. Open file T03-03 to verify.

A	B	$\bar{A}B$	$A + \bar{A}B$	$A + B$
0	0	0	0	0
0	1	1	1	1
1	0	0	1	1
1	1	0	1	1

↑ equal ↑

Rule 12: $(A + B)(A + C) = A + BC$ This rule can be proved as follows:

$$\begin{aligned}
 (A + B)(A + C) &= AA + AC + AB + BC && \text{Distributive law} \\
 &= A + AC + AB + BC && \text{Rule 7: } AA = A \\
 &= A(1 + C) + AB + BC && \text{Factoring (distributive law)} \\
 &= A \cdot 1 + AB + BC && \text{Rule 2: } 1 + C = 1 \\
 &= A(1 + B) + BC && \text{Factoring (distributive law)} \\
 &= A \cdot 1 + BC && \text{Rule 2: } 1 + B = 1 \\
 &= A + BC && \text{Rule 4: } A \cdot 1 = A
 \end{aligned}$$

The proof is shown in Table 4, which shows the truth table and the resulting logic circuit simplification.

MULTISIM



TABLE 4 • Rule 12: $(A + B)(A + C) = A + BC$. Open file T03-04 to verify.

A	B	C	$A + B$	$A + C$	$(A + B)(A + C)$	BC	$A + BC$
0	0	0	0	0	0	0	0
0	0	1	0	1	0	0	0
0	1	0	1	0	0	0	0
0	1	1	1	1	1	1	1
1	0	0	1	1	1	0	1
1	0	1	1	1	1	0	1
1	1	0	1	1	1	0	1
1	1	1	1	1	1	1	1

↑ equal ↑

SECTION 1 CHECKUP*

1. If $A = 0$, what does \bar{A} equal?
2. Determine the values of A , B , and C that make the sum term $\bar{A} + \bar{B} + C$ equal to 0.
3. Determine the values of A , B , and C that make the product term ABC equal to 1.
4. Apply the associative law of addition to the expression $A + (B + C + D)$.
5. Apply the distributive law to the expression $A(B + C + D)$.

*Answers are at the end of the chapter.

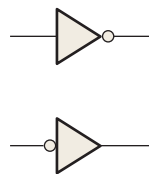
2 THE INVERTER

The inverter (NOT circuit) performs the operation called *inversion* or *complementation*. The inverter changes one logic level to the opposite level. In terms of bits, it changes a 1 to a 0 and a 0 to a 1.

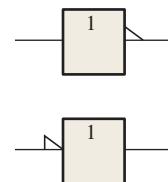
After completing this section, you should be able to

- Identify negation and polarity indicators
- Identify an inverter by either its distinctive shape symbol or its rectangular outline symbol
- Produce the truth table for an inverter
- Describe the logical operation of an inverter

Standard logic symbols for the **inverter** are shown in Figure 17. Part (a) shows the *distinctive shape* symbols, and part (b) shows the *rectangular outline* symbols. In this text, distinctive shape symbols are generally used; however, the rectangular outline symbols are found in many industry publications, and you should become familiar with them as well. (Logic symbols are in accordance with ANSI/IEEE Standard 91-1984.)



(a) Distinctive shape symbols with negation indicators



(b) Rectangular outline symbols with polarity indicators

The Negation and Polarity Indicators

The negation indicator is a “bubble” (○) that indicates **inversion** or *complementation* when it appears on the input or output of any logic element, as shown in Figure 17(a) for the inverter. Generally, inputs are on the left of a logic symbol and the output is on the right. When appearing on the input, the bubble means that a 0 is the active or *asserted* input state, and the input is called an active-LOW input. When appearing on the output, the bubble means that a 0 is the active or asserted output state, and the output is called an active-LOW output. The absence of a bubble on the input or output means that a 1 is the active or asserted state, and in this case, the input or output is called active-HIGH.

The polarity or level indicator is a “triangle” (▴) that indicates inversion when it appears on the input or output of a logic element, as shown in Figure 17(b). When appearing on the input, it means that a LOW level is the active or asserted input state. When appearing on the output, it means that a LOW level is the active or asserted output state.

Either indicator (bubble or triangle) can be used both on distinctive shape symbols and on rectangular outline symbols. Figure 17(a) indicates the principal inverter symbols used in this text. Note that a change in the placement of the negation or polarity indicator does not imply a change in the way an inverter operates.

FIGURE 17 Standard logic symbols for the inverter (ANSI/IEEE Std. 91-1984).

TABLE 5 • Inverter truth table.

INPUT	OUTPUT
LOW (0)	HIGH (1)
HIGH (1)	LOW (0)

A timing diagram shows how two or more waveforms relate in time.

Inverter Truth Table

When a HIGH level is applied to an inverter input, a LOW level will appear on its output. When a LOW level is applied to its input, a HIGH will appear on its output. This operation is summarized in Table 5, which shows the output for each possible input in terms of levels and corresponding bits. A table such as this is called a **truth table**.

Inverter Operation

Figure 18 shows the output of an inverter for a pulse input, where t_1 and t_2 indicate the corresponding points on the input and output pulse waveforms.

When the input is LOW, the output is HIGH; when the input is HIGH, the output is LOW, thereby producing an inverted output pulse.

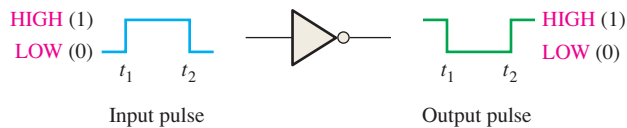


FIGURE 18 Inverter operation with a pulse input. Open file F03-18 to verify inverter operation.

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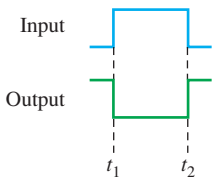


FIGURE 19 Timing diagram for the case in Figure 18.

Timing Diagrams

A **timing diagram** is basically a graph that accurately displays the relationship of two or more waveforms with respect to each other on a time basis. For example, the time relationship of the output pulse to the input pulse in Figure 18 can be shown with a simple timing diagram by aligning the two pulses so that the occurrences of the pulse edges appear in the proper time relationship. The rising edge of the input pulse and the falling edge of the output pulse occur at the same time (ideally). Similarly, the falling edge of the input pulse and the rising edge of the output pulse occur at the same time (ideally). This timing relationship is shown in Figure 19. In practice, there is a very small delay from the input transition until the corresponding output transition. Timing diagrams are especially useful for illustrating the time relationship of digital waveforms with multiple pulses.

EXAMPLE 3

A waveform is applied to an inverter in Figure 20. Determine the output waveform corresponding to the input and show the timing diagram. According to the placement of the bubble, what is the active output state?

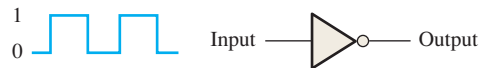


FIGURE 20

SOLUTION

The output waveform is exactly opposite to the input (inverted), as shown in Figure 21, which is the basic timing diagram. The active or asserted output state is **0**.

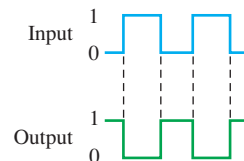


FIGURE 21

RELATED PROBLEM

If the inverter is shown with the negative indicator (bubble) on the input instead of the output, how is the timing diagram affected?

Logic Expression for an Inverter

As you have learned, in Boolean algebra a variable is generally designated by one or two letters although there can be more. Letters near the beginning of the alphabet usually designate inputs, while letters near the end of the alphabet usually designate outputs. The complement of a variable is designated by a bar over the letter. A variable can take on a value of either 1 or 0. If a given variable is 1, its complement is 0 and vice versa.

The operation of an inverter (NOT circuit) can be expressed as follows: If the input variable is called A and the output variable is called X , then

$$X = \bar{A}$$

This expression states that the output is the complement of the input, so if $A = 0$, then $X = 1$, and if $A = 1$, then $X = 0$. Figure 22 illustrates this. The complemented variable \bar{A} can be read as “A bar” or “not A.”

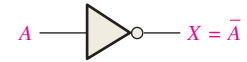


FIGURE 22 The inverter complements an input variable.

An Application

Figure 23 shows a circuit for producing the 1’s complement of an 8-bit binary number. The bits of the binary number are applied to the inverter inputs and the 1’s complement of the number appears on the outputs.

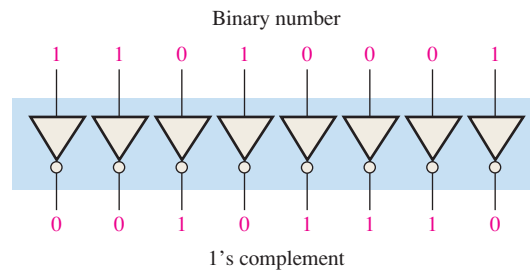


FIGURE 23 Example of a 1’s complement circuit using inverters.

SECTION 2 CHECKUP

1. When a 1 is on the input of an inverter, what is the output?
2. An active-HIGH pulse (HIGH level when asserted, LOW level when not) is required on an inverter input.
 - (a) Draw the appropriate logic symbol, using the distinctive shape and the negation indicator, for the inverter in this application.
 - (b) Describe the output when a positive-going pulse is applied to the input of an inverter.

3 THE AND GATE

The AND gate is one of the basic gates that can be combined to form any logic function. An AND gate can have two or more inputs and performs what is known as logical multiplication.

After completing this section, you should be able to

- Identify an AND gate by its distinctive shape symbol or by its rectangular outline symbol
- Describe the operation of an AND gate
- Generate the truth table for an AND gate with any number of inputs
- Produce a timing diagram for an AND gate with any specified input waveforms
- Write the logic expression for an AND gate with any number of inputs
- Discuss examples of AND gate applications

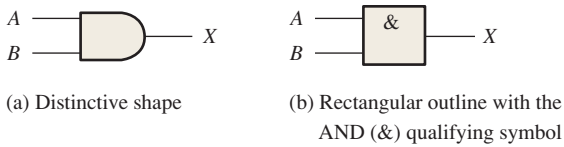
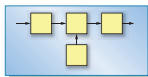


FIGURE 24 Standard logic symbols for the AND gate showing two inputs (ANSI/IEEE Std. 91-1984).

The term *gate* is used to describe a circuit that performs a basic logic operation. The AND gate is composed of two or more inputs and a single output, as indicated by the standard logic symbols shown in Figure 24. Inputs are on the left, and the output is on the right in each symbol. Gates with two inputs are shown; however, an AND gate can have any number of inputs greater than one. Although examples of both distinctive shape symbols and rectangular outline symbols are shown, the distinctive shape symbol, shown in part (a), is used predominantly in this text.

Logic gates are one of the fundamental building blocks of computers. Most of the functions in a computer, with the exception of certain types of memory, are implemented with logic gates used on a very large scale. For example, a microprocessor, which is the main part of a computer, is made up of hundreds of thousands or even millions of logic gates.

SYSTEM NOTE



An AND gate can have more than two inputs.

Operation of an AND Gate

An **AND gate** produces a HIGH output *only* when *all* of the inputs are HIGH. When any of the inputs is LOW, the output is LOW. Therefore, the basic purpose of an AND gate is to determine when certain conditions are simultaneously true, as indicated by HIGH levels on all of its inputs, and to produce a HIGH on its output to indicate that all these conditions are true. The inputs of the 2-input AND gate in Figure 24 are labeled *A* and *B*, and the output is labeled *X*. The gate operation can be stated as follows:

For a 2-input AND gate, output *X* is HIGH only when inputs *A* and *B* are HIGH; *X* is LOW when either *A* or *B* is LOW, or when both *A* and *B* are LOW.

For an AND gate, all HIGH inputs produce a HIGH output.

AND Gate Truth Table

The logical operation of a gate can be expressed with a truth table that lists all input combinations with the corresponding outputs, as illustrated in Table 6 for a 2-input AND gate. The truth table can be expanded to any number of inputs. Although the terms HIGH and LOW tend to give a “physical” sense to the input and output states, the truth table is shown with 1s and 0s; a HIGH is equivalent to a 1 and a LOW is equivalent to a 0 in positive logic. For any AND gate, regardless of the number of inputs, the output is HIGH *only* when *all* inputs are HIGH.

The total number of possible combinations of binary inputs to a gate is determined by the following formula:

$$N = 2^n \tag{6}$$

where *N* is the number of possible input combinations and *n* is the number of input variables. To illustrate,

For two input variables: $N = 2^2 = 4$ combinations

For three input variables: $N = 2^3 = 8$ combinations

For four input variables: $N = 2^4 = 16$ combinations

You can determine the number of input bit combinations for gates with any number of inputs by using Equation 6.

INPUTS		OUTPUT
<i>A</i>	<i>B</i>	<i>X</i>
0	0	0
0	1	0
1	0	0
1	1	1

1 = HIGH, 0 = LOW

EXAMPLE 4

- (a) Develop the truth table for a 3-input AND gate.
- (b) Determine the total number of possible input combinations for a 4-input AND gate.

SOLUTION

- (a) There are eight possible input combinations ($2^3 = 8$) for a 3-input AND gate. The input side of the truth table (Table 7) shows all eight combinations of three bits. The output side is all 0s except when all three input bits are 1s.

TABLE 7			
INPUTS			OUTPUT
A	B	C	X
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

- (b) $N = 2^4 = 16$. There are 16 possible combinations of input bits for a 4-input AND gate.

RELATED PROBLEM

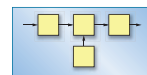
Develop the truth table for a 4-input AND gate.

Operation with Pulse Inputs

In most applications, the inputs to a gate are not stationary levels but are voltage waveforms that change frequently between HIGH and LOW logic levels. Now let's look at the operation of AND gates with pulse waveform inputs, keeping in mind that an AND gate obeys the truth table operation regardless of whether its inputs are constant levels or levels that change back and forth.

Computers can utilize all of the basic logic operations when it is necessary to selectively manipulate certain bits in one or more bytes of data. Selective bit manipulations are done with a *mask*. For example, to clear (make all 0s) the right four bits in a data byte but keep the left four bits, ANDing the data byte with 11110000 will do the job. Notice that any bit ANDed with zero will be 0 and any bit ANDed with 1 will remain the same. If 10101010 is ANDed with the mask 11110000, the result is 10100000.

SYSTEM NOTE



Let's examine the waveform operation of an AND gate by looking at the inputs with respect to each other in order to determine the output level at any given time. In Figure 25, inputs A and B are both HIGH (1) during the time interval, t_1 , making

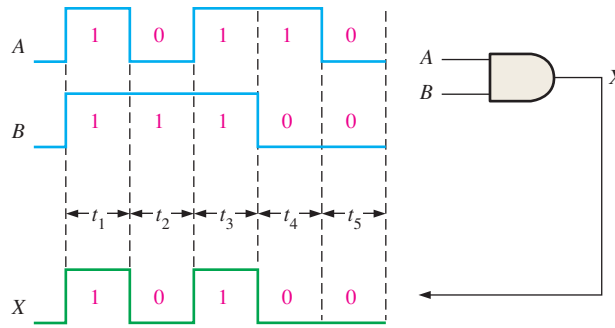


FIGURE 25 Example of AND gate operation with a timing diagram showing input and output relationships.

output X HIGH (1) during this interval. During time interval t_2 , input A is LOW (0) and input B is HIGH (1), so the output is LOW (0). During time interval t_3 , both inputs are HIGH (1) again, and therefore the output is HIGH (1). During time interval t_4 , input A is HIGH (1) and input B is LOW (0), resulting in a LOW (0) output. Finally, during time interval t_5 , input A is LOW (0), input B is LOW (0), and the output is therefore LOW (0). As you know, a diagram of input and output waveforms showing time relationships is called a *timing diagram*.

EXAMPLE 5

If two waveforms, A and B , are applied to the AND gate inputs as in Figure 26, what is the resulting output waveform?

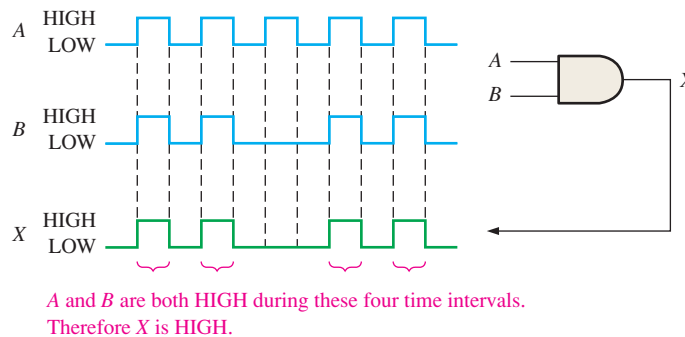


FIGURE 26

SOLUTION

The output waveform X is HIGH only when both A and B waveforms are HIGH as shown in the timing diagram in Figure 26.

RELATED PROBLEM

Determine the output waveform and show a timing diagram if the second and fourth pulses in waveform A of Figure 26 are replaced by LOW levels.

Remember, when observing the waveform operation of logic gates, it is important to pay careful attention to the time relationships of all the inputs with respect to each other and to the output.

EXAMPLE 6

For the two input waveforms, A and B , in Figure 27, show the output waveform with its proper relation to the inputs.

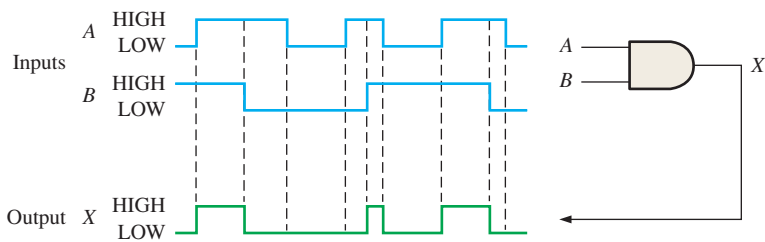


FIGURE 27

SOLUTION

The output waveform is HIGH only when both of the input waveforms are HIGH as shown in the timing diagram.

RELATED PROBLEM

Show the output waveform if the *B* input to the AND gate in Figure 27 is always HIGH.

EXAMPLE 7

For the 3-input AND gate in Figure 28, determine the output waveform in relation to the inputs.

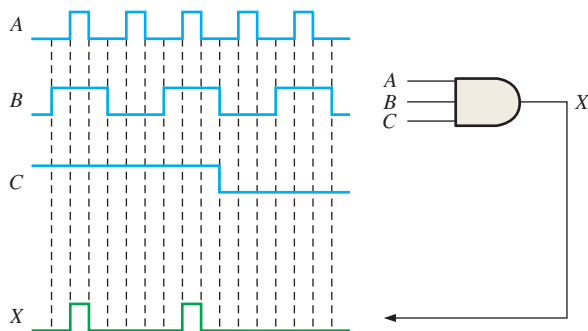


FIGURE 28

SOLUTION

The output waveform *X* of the 3-input AND gate is HIGH only when all three input waveforms *A*, *B*, and *C* are HIGH.

RELATED PROBLEM

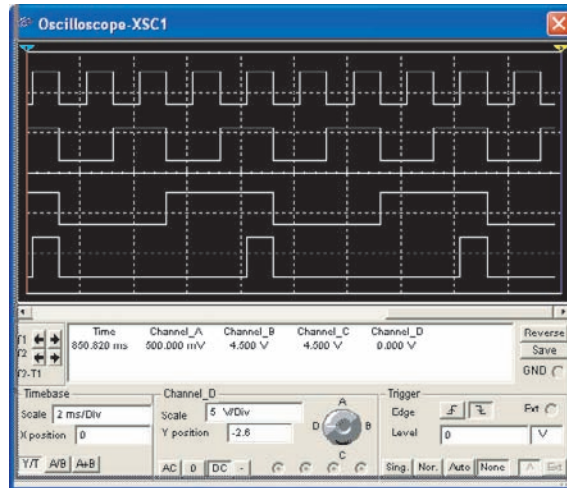
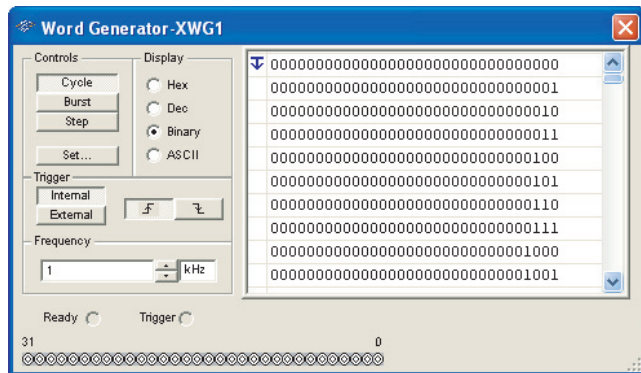
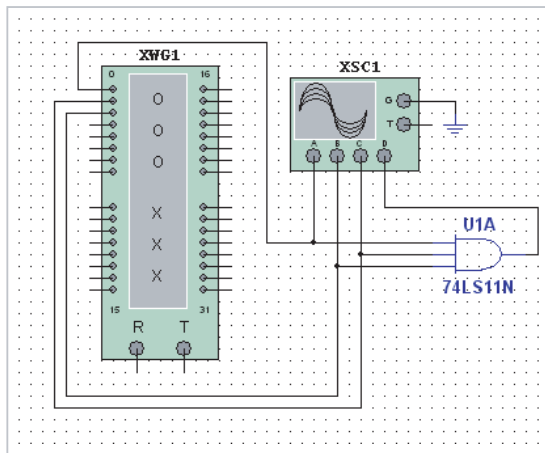
What is the output waveform of the AND gate in Figure 28 if the *C* input is always HIGH?

EXAMPLE 8

Use Multisim to simulate a 3-input AND gate with input waveforms that cycle through binary numbers 0 through 9.

SOLUTION

Use the Multisim word generator in the up counter mode to provide the combination of waveforms representing the binary sequence, as shown in Figure 29. The first three waveforms on the oscilloscope display are the inputs, and the bottom waveform is the output.



MULTISIM



FIGURE 29

RELATED PROBLEM

Use Multisim software to create the setup and simulate the 3-input AND gate as illustrated in this example. A Multisim tutorial is available at the website.

Logic Expressions for AND Gates

When variables are shown together like *ABC*, they are ANDed.

The operation of a 2-input AND gate can be expressed in equation form as follows: If one input variable is *A*, the other input variable is *B*, and the output variable is *X*, then the Boolean expression is

$$X = AB$$

Figure 30(a) shows the AND gate logic symbol with two input variables and the output variable indicated.

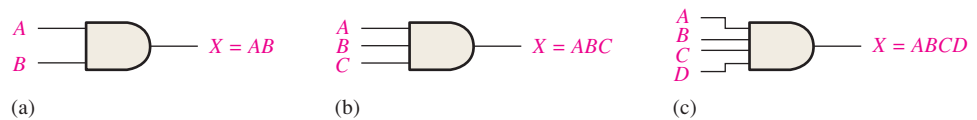


FIGURE 30 Boolean expressions for AND gates with two, three, and four inputs.

To extend the AND expression to more than two input variables, simply use a new letter for each input variable. The function of a 3-input AND gate, for example, can be expressed as $X = ABC$, where *A*, *B*, and *C* are the input variables. The expression for a

4-input AND gate can be $X = ABCD$, and so on. Parts (b) and (c) of Figure 30 show AND gates with three and four input variables, respectively.

You can evaluate an AND gate operation by using the Boolean expressions for the output. For example, each variable on the inputs can be either a 1 or a 0; so for the 2-input AND gate, make substitutions in the equation for the output, $X = AB$, as shown in Table 8. This evaluation shows that the output X of an AND gate is a 1 (HIGH) only when both inputs are 1s (HIGHS). A similar analysis can be made for any number of input variables.

A	B	$AB = X$
0	0	$0 \cdot 0 = 0$
0	1	$0 \cdot 1 = 0$
1	0	$1 \cdot 0 = 0$
1	1	$1 \cdot 1 = 1$

SYSTEM EXAMPLE 1

ENABLE/INHIBIT DEVICE

A common system application of the AND gate is to enable (that is, to allow) the passage of a signal (pulse waveform) from one point to another at certain times and to inhibit (prevent) the passage at other times. This particular use of an AND gate is shown in Figure 31, where the AND gate controls the passage of a signal (waveform A) to a digital counter. This system measures the frequency of waveform A. The enable pulse has a width of precisely 1 ms. When the enable pulse is HIGH, waveform A passes through the gate to the counter; and when the enable pulse is LOW, the signal is prevented from passing through the gate (inhibited).

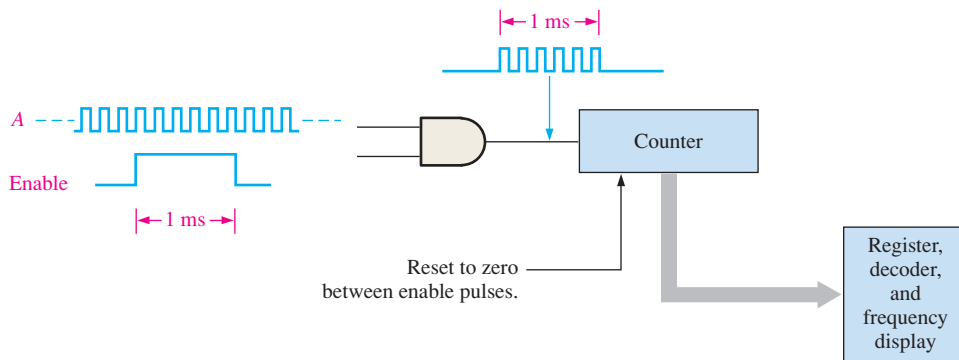
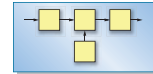


FIGURE 31 The AND gate performing an enable/inhibit function for a frequency counter.

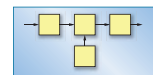
During the 1 millisecond (1 ms) interval of the enable pulse, pulses in waveform A pass through the AND gate to the counter. The number of pulses passing through during the 1 ms interval is equal to the frequency of waveform A. For example, Figure 31 shows six pulses in one millisecond, which is a frequency of 6 kHz. If 1000 pulses pass through the gate in the 1 ms interval of the enable pulse, there are 1000 pulses/ms, or a frequency of 1 MHz.

The counter counts the number of pulses per second and produces a binary output that goes to a decoding and display circuit to produce a readout of the frequency. The enable pulse repeats at certain intervals and a new updated count is made so that if the frequency changes, the new value will be displayed. Between enable pulses, the counter is reset so that it starts at zero each time an enable pulse occurs. The current frequency count is stored in a register so that the display is unaffected by the resetting of the counter.

SYSTEM EXAMPLE 2

SEAT BELT ALARM SYSTEM

In Figure 32, an AND gate is used in a simple automobile seat belt alarm system to detect when the ignition switch is on *and* the seat belt is unbuckled. If the ignition switch is on, a HIGH is produced on input A of the AND gate. If the seat belt is not properly buckled, a



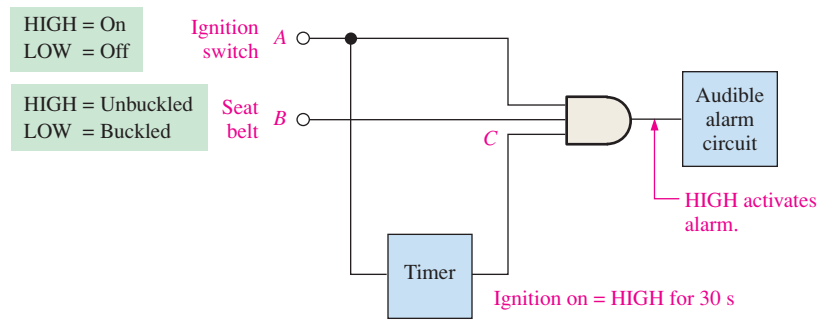


FIGURE 32 Simplified seat belt alarm system using an AND gate.

HIGH is produced on input *B* of the AND gate. Also, when the ignition switch is turned on, a timer is started that produces a HIGH on input *C* for 30 s. If all three conditions exist—that is, if the ignition is on *and* the seat belt is unbuckled *and* the timer is running—the output of the AND gate is HIGH, and an audible alarm is energized to remind the driver.

SECTION 3 CHECKUP

1. When is the output of an AND gate HIGH?
2. When is the output of an AND gate LOW?
3. Describe the truth table for a 5-input AND gate.

4 THE OR GATE

The OR gate is another of the basic gates from which all logic functions are constructed. An OR gate can have two or more inputs and performs what is known as logical addition.

After completing this section, you should be able to

- Identify an OR gate by its distinctive shape symbol or by its rectangular outline symbol
- Describe the operation of an OR gate
- Generate the truth table for an OR gate with any number of inputs
- Produce a timing diagram for an OR gate with any specified input waveforms
- Write the logic expression for an OR gate with any number of inputs
- Discuss an OR gate application

An OR gate can have more than two inputs.

An **OR gate** has two or more inputs and one output, as indicated by the standard logic symbols in Figure 33, where OR gates with two inputs are illustrated. An OR gate can have any number of inputs greater than one. Although both distinctive shape and rectangular outline symbols are shown, the distinctive shape OR gate symbol is used in this text.

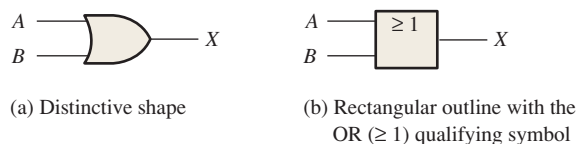


FIGURE 33 Standard logic symbols for the OR gate showing two inputs (ANSI/IEEE Std. 91-1984).

Operation of an OR Gate

An OR gate produces a HIGH on the output when *any* of the inputs is HIGH. The output is LOW only when all of the inputs are LOW. Therefore, an OR gate determines when one or more of its inputs are HIGH and produces a HIGH on its output to indicate this condition. The inputs of the 2-input OR gate in Figure 33 are labeled *A* and *B*, and the output is labeled *X*. The operation of the gate can be stated as follows:

For a 2-input OR gate, output *X* is HIGH when either input *A* or input *B* is HIGH, or when both *A* and *B* are HIGH; *X* is LOW only when both *A* and *B* are LOW.

The HIGH level is the active or asserted output level for the OR gate.

OR Gate Truth Table

The operation of a 2-input OR gate is described in Table 9. This truth table can be expanded for any number of inputs; but regardless of the number of inputs, the output is HIGH when one or more of the inputs are HIGH.

TABLE 9 • Truth table for a 2-input OR gate.		
INPUTS		OUTPUT
<i>A</i>	<i>B</i>	<i>X</i>
0	0	0
0	1	1
1	0	1
1	1	1

1 = HIGH, 0 = LOW

Operation with Pulse Inputs

Now let's look at the operation of an OR gate with pulse waveform inputs, keeping in mind its logical operation. Again, the important thing in the analysis of gate operation with pulse waveforms is the time relationship of all the waveforms involved. For example, in Figure 34, inputs *A* and *B* are both HIGH (1) during time interval t_1 , making output *X* HIGH (1). During time interval t_2 , input *A* is LOW (0), but because input *B* is HIGH (1), the output is HIGH (1). Both inputs are LOW (0) during time interval t_3 , so there is a LOW (0) output during this time. During time interval t_4 , the output is HIGH (1) because input *A* is HIGH (1).

In this illustration, we have applied the truth table operation of the OR gate to each of the time intervals during which the levels are nonchanging. Examples 9 through 11 further illustrate OR gate operation with waveforms on the inputs.

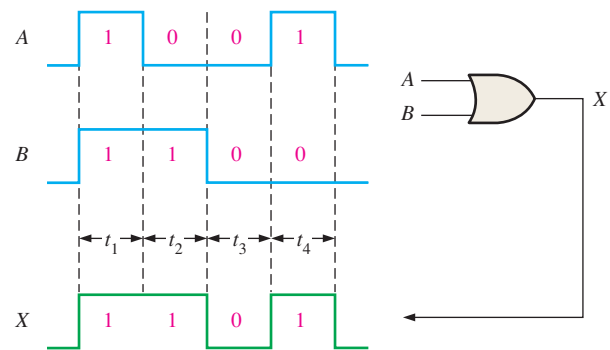


FIGURE 34 Example of OR gate operation with a timing diagram showing input and output time relationships.

EXAMPLE 9

If the two input waveforms, *A* and *B*, in Figure 35 are applied to the OR gate, what is the resulting output waveform?

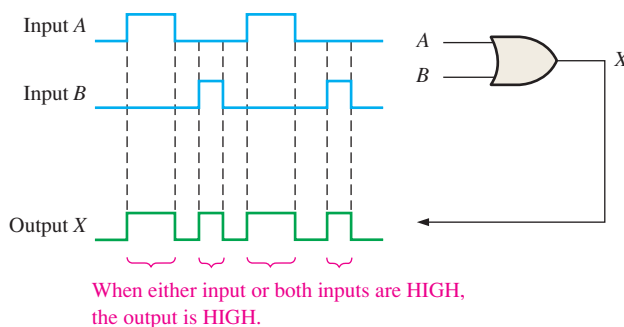


FIGURE 35

SOLUTION

The output waveform X of a 2-input OR gate is HIGH when either or both input waveforms are HIGH as shown in the timing diagram. In this case, both input waveforms are never HIGH at the same time.

RELATED PROBLEM

Determine the output waveform and show the timing diagram if input A is changed such that it is HIGH from the beginning of the existing first pulse to the end of the existing second pulse.

EXAMPLE 10

For the two input waveforms, A and B , in Figure 36, show the output waveform with its proper relation to the inputs.

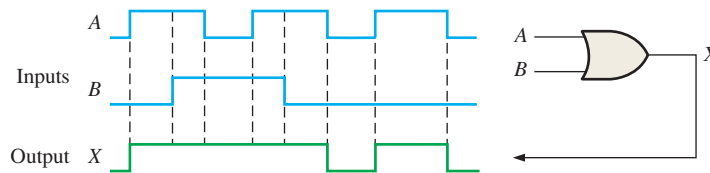


FIGURE 36

SOLUTION

When either or both input waveforms are HIGH, the output is HIGH as shown by the output waveform X in the timing diagram.

RELATED PROBLEM

Determine the output waveform and show the timing diagram if the middle pulse of input A is replaced by a LOW level.

EXAMPLE 11

For the 3-input OR gate in Figure 37, determine the output waveform in proper time relation to the inputs.

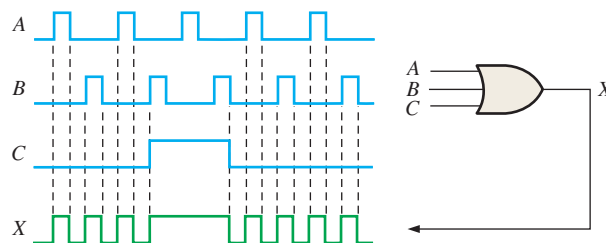


FIGURE 37

SOLUTION

The output is HIGH when one or more of the input waveforms are HIGH as indicated by the output waveform X in the timing diagram.

RELATED PROBLEM

Determine the output waveform and show the timing diagram if input C is always LOW.

Logic Expressions for OR Gates

The operation of a 2-input OR gate can be expressed as follows: If one input variable is A , if the other input variable is B , and if the output variable is X , then the Boolean expression is

$$X = A + B$$

Figure 38(a) shows the OR gate logic symbol with two input variables and the output variable labeled.

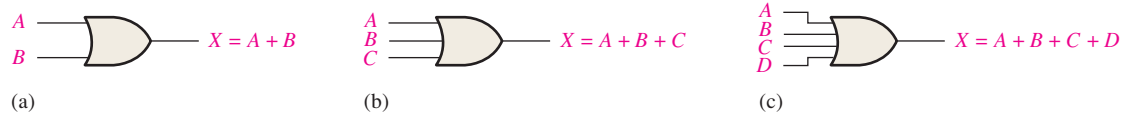


FIGURE 38 Boolean expressions for OR gates with two, three, and four inputs.

To extend the OR expression to more than two input variables, a new letter is used for each additional variable. For instance, the function of a 3-input OR gate can be expressed as $X = A + B + C$. The expression for a 4-input OR gate can be written as $X = A + B + C + D$, and so on. Parts (b) and (c) of Figure 38 show OR gates with three and four input variables, respectively.

OR gate operation can be evaluated by using the Boolean expressions for the output X by substituting all possible combinations of 1 and 0 values for the input variables, as shown in Table 10 for a 2-input OR gate. This evaluation shows that the output X of an OR gate is a 1 (HIGH) when any one or more of the inputs are 1 (HIGH). A similar analysis can be extended to OR gates with any number of input variables.

A	B	$A + B = X$
0	0	$0 + 0 = 0$
0	1	$0 + 1 = 1$
1	0	$1 + 0 = 1$
1	1	$1 + 1 = 1$

Another mask operation that is used in computer programming to selectively make certain bits in a data byte equal to 1 (called setting) while not affecting any other bit is done with the OR operation. A mask is used that contains a 1 in any position where a data bit is to be set. For example, if you want to force the sign bit in an 8-bit signed number to equal 1, but leave all other bits unchanged, you can OR the data byte with the mask 10000000.

SYSTEM NOTE



SYSTEM EXAMPLE 3

INTRUSION DETECTION

A simplified portion of an intrusion detection and alarm system is shown in Figure 39. This system could be used for one room in a home—a room with two windows and a door. The sensors are magnetic switches that produce a HIGH output when open and a LOW output when closed.

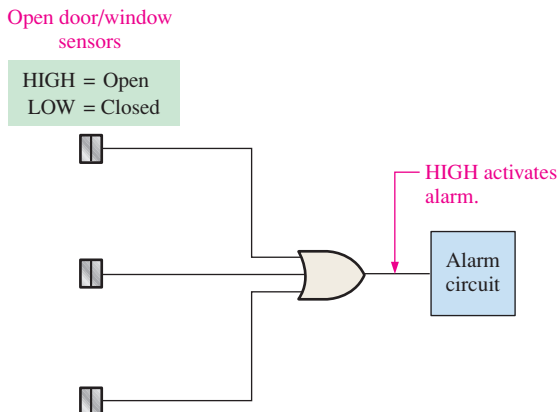
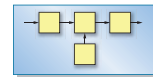


FIGURE 39 A simplified intrusion detection system using an OR gate.

output when closed. As long as the windows and the door are secured, the switches are closed and all three of the OR gate inputs are LOW. When one of the windows or the door is opened, a HIGH is produced on that input to the OR gate and the gate output goes HIGH. It then activates and latches an alarm circuit to warn of the intrusion.

SECTION 4 CHECKUP

1. When is the output of an OR gate HIGH?
2. When is the output of an OR gate LOW?
3. Describe the truth table for a 3-input OR gate.

5 THE NAND GATE

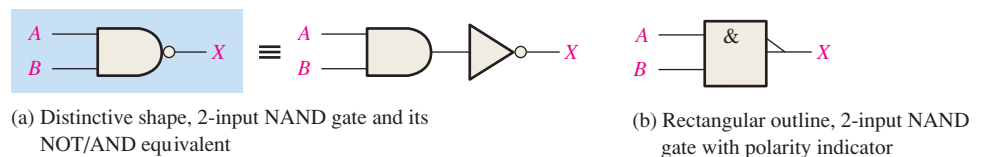
The NAND gate is a popular logic element because it can be used as a universal gate; that is, NAND gates can be used in combination to perform the AND, OR, and inverter operations.

After completing this section, you should be able to

- Identify a NAND gate by its distinctive shape symbol or by its rectangular outline symbol
- Describe the operation of a NAND gate
- Develop the truth table for a NAND gate with any number of inputs
- Produce a timing diagram for a NAND gate with any specified input waveforms
- Write the logic expression for a NAND gate with any number of inputs
- Describe NAND gate operation in terms of its negative-OR equivalent
- Discuss NAND gate applications

The NAND gate is the same as the AND gate except the output is inverted.

FIGURE 40 Standard NAND gate logic symbols (ANSI/IEEE Std. 91-1984).

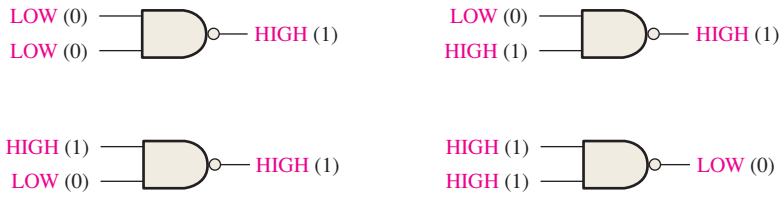


Operation of a NAND Gate

A **NAND gate** produces a LOW output only when all the inputs are HIGH. When any of the inputs is LOW, the output will be HIGH. For the specific case of a 2-input NAND gate, as shown in Figure 40 with the inputs labeled *A* and *B* and the output labeled *X*, the operation can be stated as follows:

For a 2-input NAND gate, output *X* is LOW only when inputs *A* and *B* are HIGH; *X* is HIGH when either *A* or *B* is LOW, or when both *A* and *B* are LOW.

This operation is opposite that of the AND in terms of the output level. In a NAND gate, the LOW level (0) is the active or asserted output level, as indicated by the bubble on the output. Figure 41 illustrates the operation of a 2-input NAND gate for all four input



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FIGURE 41 Operation of a 2-input NAND gate. Open file F03-41 to verify NAND gate operation.

combinations, and Table 11 is the truth table summarizing the logical operation of the 2-input NAND gate.

Operation with Pulse Inputs

Now let's look at the pulse waveform operation of a NAND gate. Remember from the truth table that the only time a LOW output occurs is when all of the inputs are HIGH.

TABLE 11 • Truth table for a 2-input NAND gate.

INPUTS		OUTPUT
A	B	X
0	0	1
0	1	1
1	0	1
1	1	0

1 = HIGH, 0 = LOW.

EXAMPLE 12

If the two waveforms *A* and *B* shown in Figure 42 are applied to the NAND gate inputs, determine the resulting output waveform.

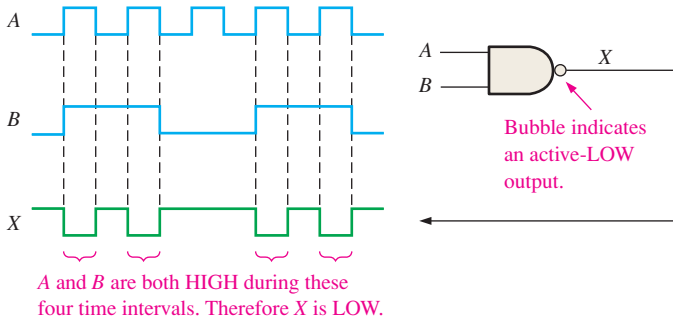


FIGURE 42

SOLUTION

Output waveform *X* is LOW only during the four time intervals when both input waveforms *A* and *B* are HIGH as shown in the timing diagram.

RELATED PROBLEM

Determine the output waveform and show the timing diagram if input waveform *B* is inverted.

EXAMPLE 13

Show the output waveform for the 3-input NAND gate in Figure 43 with its proper time relationship to the inputs.

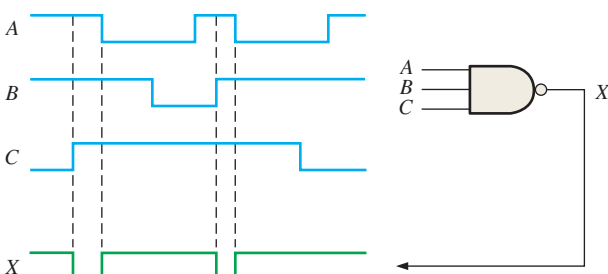


FIGURE 43

SOLUTION

The output waveform X is LOW only when all three input waveforms are HIGH as shown in the timing diagram.

RELATED PROBLEM

Determine the output waveform and show the timing diagram if input waveform A is inverted.

NEGATIVE-OR EQUIVALENT OPERATION OF A NAND GATE Inherent in a NAND gate's operation is the fact that one or more LOW inputs produce a HIGH output. Table 11 shows that output X is HIGH (1) when any of the inputs, A and B , is LOW (0). From this viewpoint, a NAND gate can be used for an OR operation that requires one or more LOW inputs to produce a HIGH output. This aspect of NAND operation is referred to as **negative-OR**. The term *negative* in this context means that the inputs are defined to be in the active or asserted state when LOW.

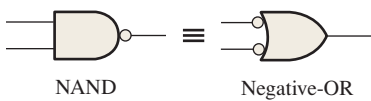
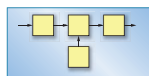


FIGURE 44 Standard symbols representing the two equivalent operations of a NAND gate.

For a 2-input NAND gate performing a negative-OR operation, output X is HIGH when either input A or input B is LOW, or when both A and B are LOW.

When a NAND gate is used to detect one or more LOWs on its inputs rather than all HIGHs, it is performing the negative-OR operation and is represented by the standard logic symbol shown in Figure 44. Although the two symbols in Figure 44 represent the same physical gate, they serve to define its role or mode of operation in a particular application.

SYSTEM EXAMPLE 4



STORAGE TANK HIGH-LEVEL DETECTION

Two tanks are used to store certain liquid chemicals that are required in a manufacturing process. Each tank has a sensor that detects when the chemical level drops to 25% of full. The sensors produce a HIGH level of 5 V when the tanks are more than one-quarter full.

When the volume of chemical in a tank drops to one-quarter full, the sensor puts out a LOW level of 0 V.

A single green light-emitting diode (LED) on an indicator panel show when both tanks are more than one-quarter full.

Figure 45 shows a NAND gate with its two inputs connected to the tank level sensors and its output connected to the indicator panel. The operation can be stated as follows: If tank A and tank B are above one-quarter full, the LED is on.

As long as both sensor outputs are HIGH (5 V), indicating that both tanks are more than one-quarter full, the NAND gate output is LOW (0 V). The green LED circuit is arranged so that a LOW voltage turns it on. The resistor limits the LED current. The system can be modified to monitor more than two tanks by increasing the number of NAND gate inputs to correspond to the number of tanks.

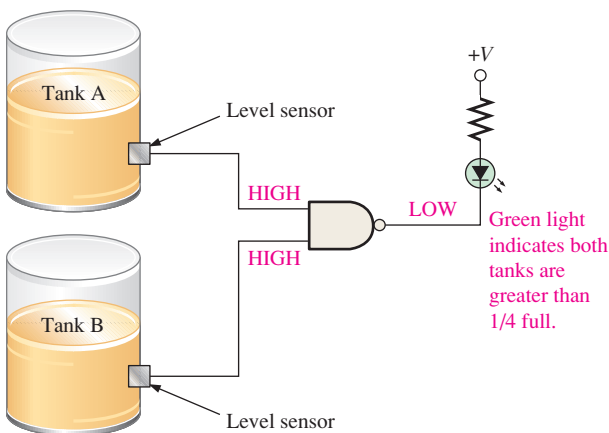


FIGURE 45

SYSTEM EXAMPLE 5

STORAGE TANK LOW-LEVEL DETECTION

An alternate approach to System Example 4 is a system in which a red LED display comes on when at least one of the tanks falls to the quarter-full level rather than have the green LED display indicate when both are above one quarter.

Figure 46 shows a NAND gate operating as a negative-OR gate to detect the occurrence of at least one LOW on its inputs. A sensor puts out a LOW voltage if the volume in its tank goes to one-quarter full or less. When this happens, the gate output goes HIGH. The red LED circuit in the panel is arranged so that a HIGH voltage turns it on. The operation can be stated as follows: If tank *A* or tank *B* or both are below one-quarter full, the LED is on.

Notice that, in this system example and in System Example 4, the same 2-input NAND gate is used, but a different gate symbol is used in the schematic, illustrating the different way in which the NAND and equivalent negative-OR operations can be used.

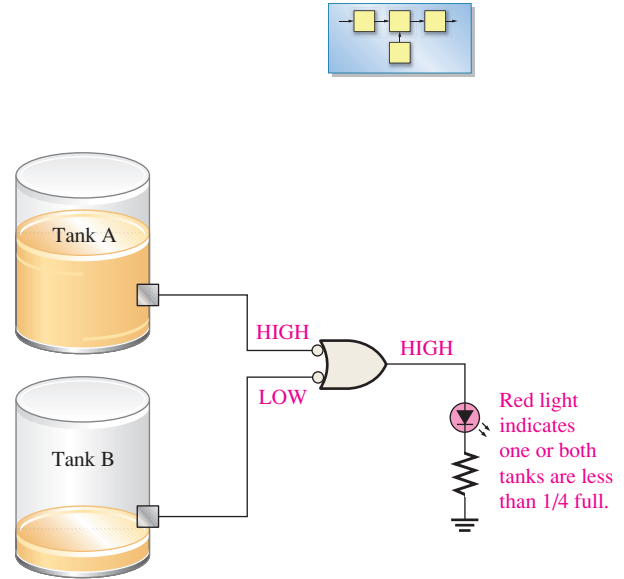


FIGURE 46

EXAMPLE 14

For the 4-input NAND gate in Figure 47, operating as a negative-OR gate, determine the output with respect to the inputs.

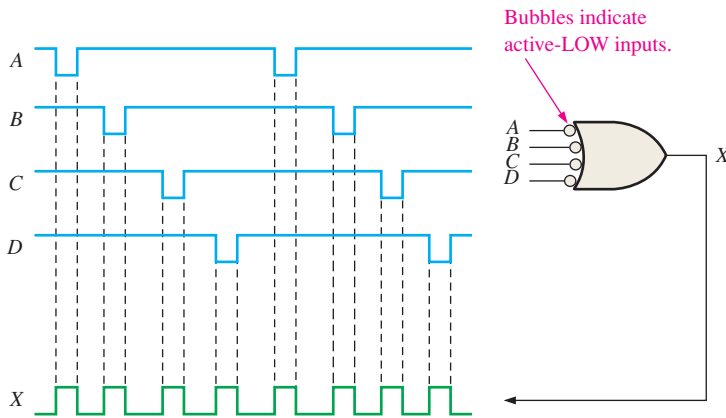


FIGURE 47

SOLUTION

The output waveform *X* is HIGH any time an input waveform is LOW as shown in the timing diagram.

RELATED PROBLEM

Determine the output waveform if input waveform *A* is inverted before it is applied to the gate.

A bar over a variable or variables indicates an inversion.

Logic Expressions for NAND Gates

The Boolean expression for the output of a 2-input NAND gate is

$$X = \overline{AB}$$

This expression says that the two input variables, A and B , are first ANDed and then complemented, as indicated by the bar over the AND expression. This is a description in equation form of the operation of a NAND gate with two inputs. Evaluating this expression for all possible values of the two input variables, you get the results shown in Table 12.

Once an expression is determined for a given logic function, that function can be evaluated for all possible values of the variables. The evaluation tells you exactly what the output of the logic circuit is for each of the input conditions, and it therefore gives you a complete description of the circuit's logic operation. The NAND expression can be extended to more than two input variables by including additional letters to represent the other variables.

TABLE 12		
A	B	$\overline{AB} = X$
0	0	$\overline{0 \cdot 0} = \overline{0} = 1$
0	1	$\overline{0 \cdot 1} = \overline{0} = 1$
1	0	$\overline{1 \cdot 0} = \overline{0} = 1$
1	1	$\overline{1 \cdot 1} = \overline{1} = 0$

SECTION 5 CHECKUP

- When is the output of a NAND gate LOW?
- When is the output of a NAND gate HIGH?
- Describe the functional differences between a NAND gate and a negative-OR gate. Do they both have the same truth table?
- Write the output expression for a NAND gate with inputs A , B , and C .

6 THE NOR GATE

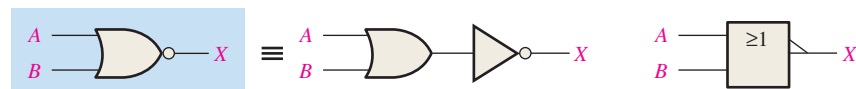
The NOR gate, like the NAND gate, is a useful logic element because it can also be used as a universal gate; that is, NOR gates can be used in combination to perform the AND, OR, and inverter operations.

After completing this section, you should be able to

- Identify a NOR gate by its distinctive shape symbol or by its rectangular outline symbol
- Describe the operation of a NOR gate
- Develop the truth table for a NOR gate with any number of inputs
- Produce a timing diagram for a NOR gate with any specified input waveforms
- Write the logic expression for a NOR gate with any number of inputs
- Describe NOR gate operation in terms of its negative-AND equivalent
- Discuss a NOR gate application

The NOR is the same as the OR except the output is inverted.

The term *NOR* is a contraction of NOT-OR and implies an OR function with an inverted (complemented) output. The standard logic symbol for a 2-input NOR gate and its equivalent OR gate followed by an inverter are shown in Figure 48(a). A rectangular outline symbol is shown in part (b).



(a) Distinctive shape, 2-input NOR gate and its NOT/OR equivalent

(b) Rectangular outline, 2-input NOR gate with polarity indicator

FIGURE 48 Standard NOR gate logic symbols (ANSI/IEEE Std. 91-1984).

Operation of a NOR Gate

A **NOR gate** produces a LOW output when *any* of its inputs is HIGH. Only when all of its inputs are LOW is the output HIGH. For the specific case of a 2-input NOR gate, as shown in Figure 48 with the inputs labeled *A* and *B* and the output labeled *X*, the operation can be stated as follows:

For a 2-input NOR gate, output *X* is LOW when either input *A* or input *B* is HIGH, or when both *A* and *B* are HIGH; *X* is HIGH only when both *A* and *B* are LOW.

This operation results in an output level opposite that of the OR gate. In a NOR gate, the LOW output is the active or asserted output level as indicated by the bubble on the output. Figure 49 illustrates the operation of a 2-input NOR gate for all four possible input combinations, and Table 13 is the truth table for a 2-input NOR gate.

TABLE 13 • Truth table for a 2-input NOR gate.

INPUTS		OUTPUT
<i>A</i>	<i>B</i>	<i>X</i>
0	0	1
0	1	0
1	0	0
1	1	0

1 = HIGH, 0 = LOW.

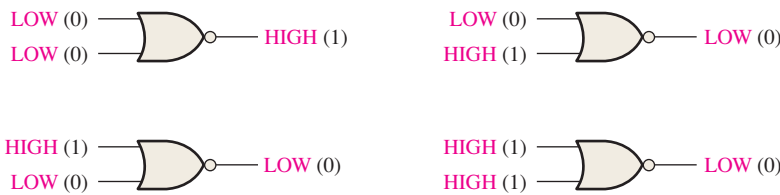


FIGURE 49 Operation of a 2-input NOR gate. Open file F03-49 to verify NOR gate operation.

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Operation with Pulse Inputs

The next two examples illustrate the operation of a NOR gate with pulse waveform inputs. Again, as with the other types of gates, we will simply follow the truth table operation to determine the output waveforms in the proper time relationship to the inputs.

EXAMPLE 15

If the two waveforms shown in Figure 50 are applied to a NOR gate, what is the resulting output waveform?

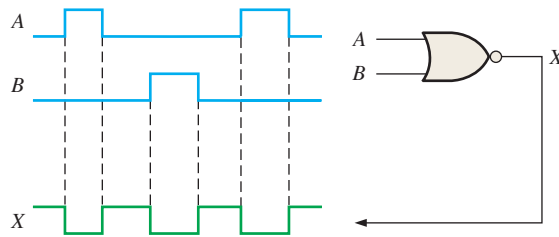


FIGURE 50

SOLUTION

Whenever any input of the NOR gate is HIGH, the output is LOW as shown by the output waveform *X* in the timing diagram.

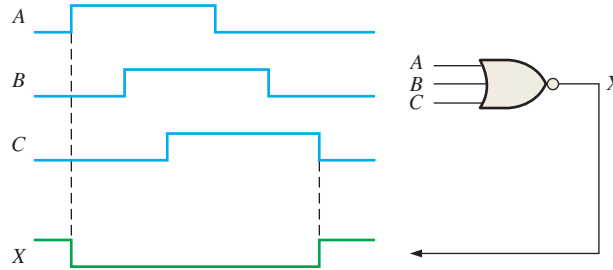
RELATED PROBLEM

Invert input *B* and determine the output waveform in relation to the inputs.

EXAMPLE 16

Show the output waveform for the 3-input NOR gate in Figure 51 with the proper time relation to the inputs.

FIGURE 51



SOLUTION

The output X is LOW when any input is HIGH as shown by the output waveform X in the timing diagram.

RELATED PROBLEM

With the B and C inputs inverted, determine the output and show the timing diagram.

NEGATIVE-AND EQUIVALENT OF THE NOR GATE A NOR gate, like the NAND, has another aspect of its operation that is inherent in the way it logically functions. Table 13 shows that a HIGH is produced on the gate output only when all of the inputs are LOW. From this viewpoint, a NOR gate can be used for an AND operation that requires all LOW inputs to produce a HIGH output. This aspect of NOR operation is called **negative-AND**. The term *negative* in this context means that the inputs are defined to be in the active or asserted state when LOW.

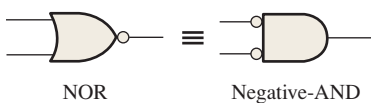
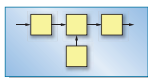


FIGURE 52 Standard symbols representing the two equivalent operations of a NOR gate.

For a 2-input NOR gate performing a negative-AND operation, output X is HIGH only when both inputs A and B are LOW.

When a NOR gate is used to detect all LOWs on its inputs rather than one or more HIGHS, it is performing the negative-AND operation and is represented by the standard symbol in Figure 52. Remember that the two symbols in Figure 52 represent the same physical gate and serve only to distinguish between the two modes of its operation.

SYSTEM EXAMPLE 6



LANDING GEAR STATUS MONITOR

As part of an aircraft’s functional monitoring system, a landing gear status monitor is required to indicate the status of the landing gears prior to landing. A green LED display turns on if all three gears are properly extended when the “gear down” switch has been activated in preparation for landing. A red LED display turns on if any of the gears fail to extend properly prior to landing. When a landing gear is extended, its sensor produces a LOW voltage. When a landing gear is retracted, its sensor produces a HIGH voltage.

Power is applied to the circuit only when the “gear down” switch is activated. A NOR gate is used for each of the two requirements as shown in Figure 53. One NOR gate operates as a negative-AND to detect a LOW from each of the three landing gear sensors. When all three of the gate inputs are LOW, the three landing gears are properly extended and the resulting HIGH output from the negative-AND gate turns on the green LED display. The other NOR gate operates as a NOR to detect if one or more of the

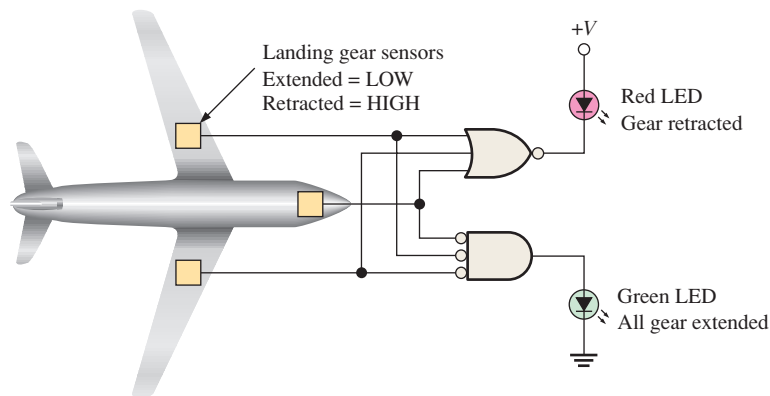


FIGURE 53

landing gears remain retracted when the “gear down” switch is activated. When one or more of the landing gears remain retracted, the resulting HIGH from the sensor is detected by the NOR gate, which produces a LOW output to turn on the red LED warning display.

EXAMPLE 17

For the 4-input NOR gate operating as a negative-AND in Figure 54, determine the output relative to the inputs.

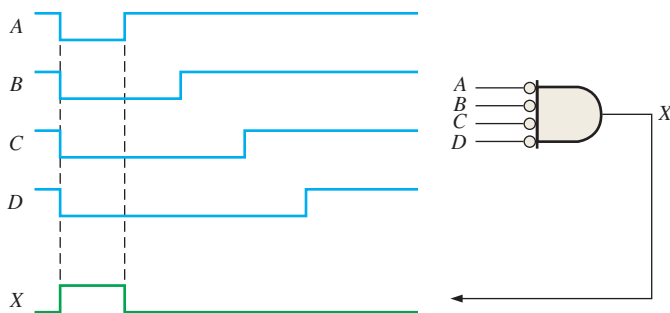


FIGURE 54

SOLUTION

Any time all of the input waveforms are LOW, the output is HIGH as shown by output waveform X in the timing diagram.

RELATED PROBLEM

Determine the output with input D inverted and show the timing diagram.



HANDS ON TIP

When driving a load such as an LED with a logic gate, consult the manufacturer’s data sheet for maximum drive capabilities (output current). A regular IC logic gate may not be capable of handling the current required by certain loads such as some LEDs. Logic gates with a buffered output, such as an open-collector (OC) or open-drain (OD) output, are available. The output current capability of typical logic gates is limited to the μA or relatively low mA range.

Logic Expressions for NOR Gates

The Boolean expression for the output of a 2-input NOR gate can be written as

$$X = \overline{A + B}$$

This equation says that the two input variables are first ORed and then complemented, as indicated by the bar over the OR expression. Evaluating this expression, you get the results shown in Table 14. The NOR expression can be extended to more than two input variables by including additional letters to represent the other variables.

TABLE 14		
A	B	$\overline{A + B} = X$
0	0	$\overline{0 + 0} = \overline{0} = 1$
0	1	$\overline{0 + 1} = \overline{1} = 0$
1	0	$\overline{1 + 0} = \overline{1} = 0$
1	1	$\overline{1 + 1} = \overline{1} = 0$

SECTION 6 CHECKUP

1. When is the output of a NOR gate HIGH?
2. When is the output of a NOR gate LOW?
3. Describe the functional difference between a NOR gate and a negative-AND gate. Do they both have the same truth table?
4. Write the output expression for a 3-input NOR gate with input variables A , B , and C .

7 THE EXCLUSIVE-OR AND EXCLUSIVE-NOR GATES

Exclusive-OR and exclusive-NOR gates are formed by a combination of AND gates, OR gates, and inverters. However, because of their fundamental importance in many applications, these gates are often treated as basic logic elements with their own unique symbols.

After completing this section, you should be able to

- Identify the exclusive-OR and exclusive-NOR gates by their distinctive shape symbols or by their rectangular outline symbols
- Describe the operations of exclusive-OR and exclusive-NOR gates
- Show the truth tables for exclusive-OR and exclusive-NOR gates
- Produce a timing diagram for an exclusive-OR or exclusive-NOR gate with any specified input waveforms

The Exclusive-OR Gate

Standard symbols for an exclusive-OR (XOR for short) gate are shown in Figure 55. The XOR gate has only two inputs. The **exclusive-OR gate** performs modulo-2 addition. The output of an exclusive-OR gate is HIGH *only* when the two inputs are at opposite logic levels. This operation can be stated as follows with reference to inputs A and B and output X :

For an exclusive-OR gate, output X is HIGH when input A is LOW and input B is HIGH, or when input A is HIGH and input B is LOW; X is LOW when A and B are both HIGH or both LOW.

For an exclusive-OR gate, opposite inputs make the output HIGH.

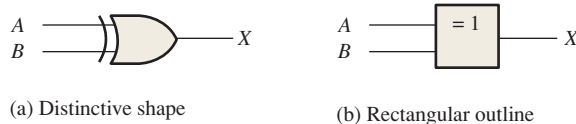
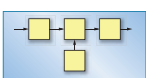


FIGURE 55 Standard logic symbols for the exclusive-OR gate.

Exclusive-OR gates connected to form an adder circuit allow a computer to perform addition, subtraction, multiplication, and division in its Arithmetic Logic Unit (ALU). An exclusive-OR gate combines basic AND, OR, and NOT logic.

SYSTEM NOTE



The four possible input combinations and the resulting outputs for an XOR gate are illustrated in Figure 56. The HIGH level is the active or asserted output level and occurs only when the inputs are at opposite levels. The operation of an XOR gate is summarized in the truth table shown in Table 15.

TABLE 15 • Truth table for an exclusive-OR gate.

INPUTS		OUTPUT
A	B	X
0	0	0
0	1	1
1	0	1
1	1	0

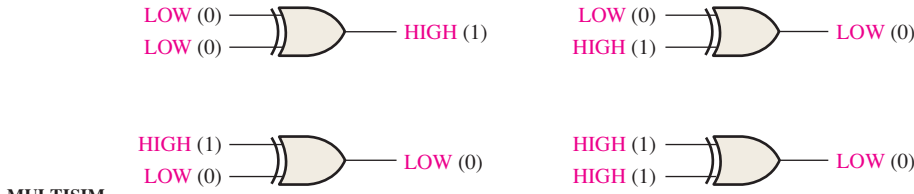


FIGURE 56 All possible logic levels for an exclusive-OR gate. Open file F03-56 to verify XOR gate operation.

SYSTEM EXAMPLE 7

CIRCUIT FAULT DETECTION

A certain system contains two identical circuits operating in parallel. As long as both are operating properly, the outputs of both circuits are always the same. If one of the circuits fails, the outputs will be at opposite levels at some time. This method is called *redundancy*.

The outputs of the circuits are connected to the inputs of an XOR gate as shown in Figure 57. A failure in either one of the circuits produces differing outputs, which cause the XOR inputs to be at opposite levels. This condition produces a HIGH on the output of the XOR gate, indicating a failure in one of the circuits.

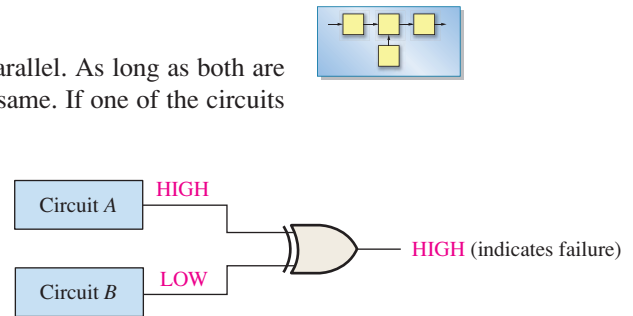


FIGURE 57

The Exclusive-NOR Gate

Standard symbols for an **exclusive-NOR (XNOR) gate** are shown in Figure 58. Like the XOR gate, an XNOR has only two inputs. The bubble on the output of the XNOR symbol indicates that its output is opposite that of the XOR gate. When the two input logic levels are opposite, the output of the exclusive-NOR gate is LOW. The operation can be stated as follows (*A* and *B* are inputs, *X* is the output):

For an exclusive-NOR gate, output *X* is LOW when input *A* is LOW and input *B* is HIGH, or when *A* is HIGH and *B* is LOW; *X* is HIGH when *A* and *B* are both HIGH or both LOW.

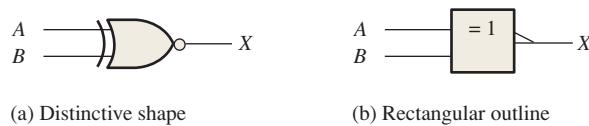


FIGURE 58 Standard logic symbols for the exclusive-NOR gate.

The four possible input combinations and the resulting outputs for an XNOR gate are shown in Figure 59. The operation of an XNOR gate is summarized in Table 16. Notice that the output is HIGH when the same level is on both inputs.

TABLE 16 • Truth table for an exclusive-NOR gate.

INPUTS		OUTPUT
A	B	X
0	0	1
0	1	0
1	0	0
1	1	1

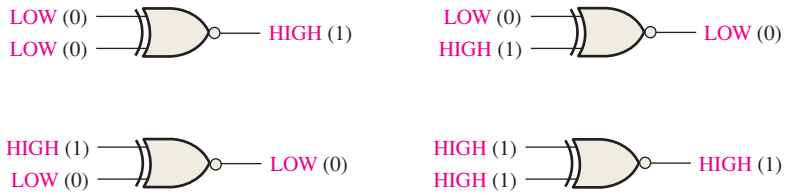


FIGURE 59 All possible logic levels for an exclusive-NOR gate. Open file F03-59 to verify XNOR gate operation.

Logic Expressions for the XOR and XNOR Gates

The Boolean expression for an exclusive-OR gate is

$$X = A \oplus B$$

and the expression for an exclusive-NOR gate is

$$X = \overline{A \oplus B}$$

Expressions for both the XOR and XNOR gates can also be written in terms of AND, OR, and NOT; for the XOR gate,

$$X = A\bar{B} + \bar{A}B$$

and for the XNOR gate,

$$X = \overline{A\bar{B} + \bar{A}B}$$

Operation with Pulse Inputs

As we have done with the other gates, let's examine the operation of XOR and XNOR gates with pulse waveform inputs. As before, we apply the truth table operation during each distinct time interval of the pulse waveform inputs, as illustrated in Figure 60 for an XOR gate. You can see that the input waveforms *A* and *B* are at opposite levels during time intervals *t*₂ and *t*₄. Therefore, the output *X* is HIGH during these two times. Since both inputs are at the same level, either both HIGH or both LOW, during time intervals *t*₁ and *t*₃, the output is LOW during those times as shown in the timing diagram.

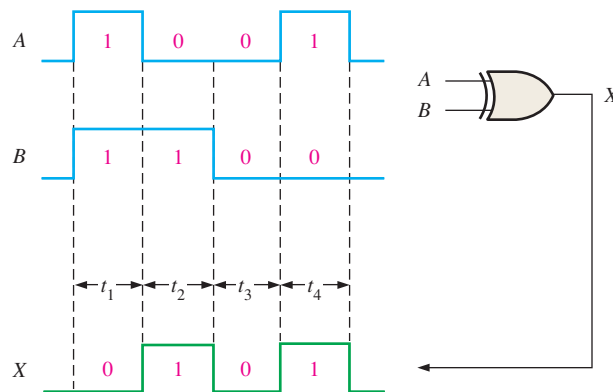


FIGURE 60 Example of exclusive-OR gate operation with pulse waveform inputs.

EXAMPLE 18

Determine the output waveforms for the XOR gate and for the XNOR gate, given the input waveforms, *A* and *B*, in Figure 61.

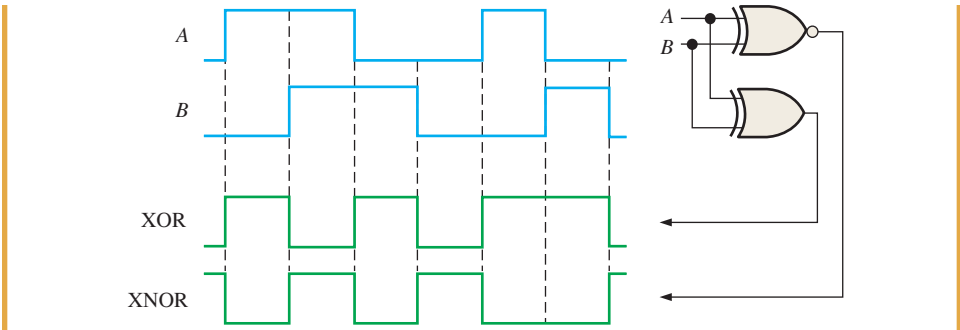


FIGURE 61

SOLUTION

The output waveforms are shown in Figure 61. Notice that the XOR output is HIGH only when both inputs are at opposite levels. Notice that the XNOR output is HIGH only when both inputs are the same.

RELATED PROBLEM

Determine the output waveforms if the two input waveforms, *A* and *B*, are inverted.

The XOR Gate as an Adder

An exclusive-OR gate can be used as a two-bit modulo-2 adder. The basic rules for binary addition are as follows: $0 + 0 = 0$, $0 + 1 = 1$, $1 + 0 = 1$, and $1 + 1 = 10$. An examination of the truth table for an XOR gate shows that its output is the binary sum of the two input bits. In the case where the inputs are both 1s, the output is the sum 0, but you lose the carry of 1. Later you will see how XOR gates are combined to make complete adding circuits. Table 17 illustrates an XOR gate used as a modulo-2 adder.

TABLE 17 • An XOR gate used to add two bits.

INPUT BITS		OUTPUT (SUM)
<i>A</i>	<i>B</i>	Σ
0	0	0
0	1	1
1	0	1
1	1	0 (without the 1 carry bit)

SECTION 7 CHECKUP

1. When is the output of an XOR gate HIGH?
2. When is the output of an XNOR gate HIGH?
3. How can you use an XOR gate to detect when two bits are different?

8 GATE PERFORMANCE CHARACTERISTICS AND PARAMETERS

Several things define the performance of a logic circuit. These performance characteristics are the switching speed measured in terms of the propagation delay time, the power dissipation, the fan-out or drive capability, the speed-power product, the dc supply voltage, and the input/output logic levels. Two major types of IC logic circuit families, CMOS and bipolar (TTL), will be referenced in this section.

After completing this section, you should be able to

- Define *propagation delay time*
- Define *power dissipation*
- Define *fan-out*
- Define *unit load*
- Define *speed-power product*

High-speed logic has a short propagation delay time.

PROPAGATION DELAY TIME This parameter is a result of the limitation on switching speed or frequency at which a logic circuit can operate. The terms *low speed* and *high speed*, applied to logic circuits, refer to the propagation delay time. The shorter the propagation delay, the higher the speed of the circuit and the higher the frequency at which it can operate.

Propagation delay time, t_p , of a logic gate is the time interval between the transition of an input pulse and the occurrence of the resulting transition of the output pulse. Two different measurements of propagation delay time are associated with a logic gate and apply to all the types of basic gates:

- t_{PHL} : The time between a specified reference point on the input pulse and a corresponding reference point on the resulting output pulse, with the output changing from the HIGH level to the LOW level (HL).
- t_{PLH} : The time between a specified reference point on the input pulse and a corresponding reference point on the resulting output pulse, with the output changing from the LOW level to the HIGH level (LH).

EXAMPLE 19

Show the propagation delay times of the inverter in Figure 62(a).

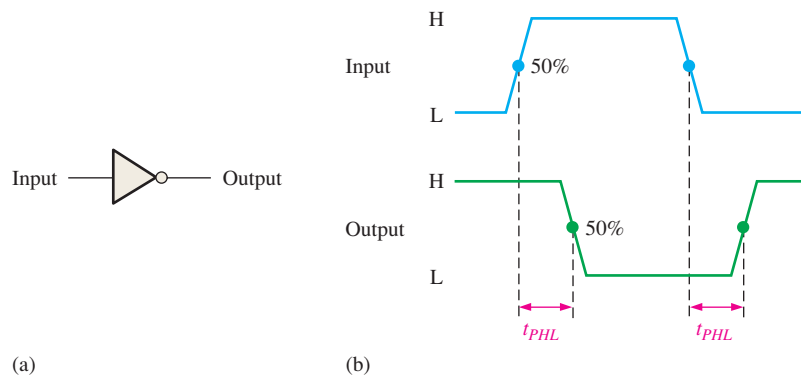


FIGURE 62

SOLUTION

The propagation delay times, t_{PHL} and t_{PLH} , are indicated in part (b) of the figure. In this case, the delays are measured between the 50% points of the corresponding

edges of the input and output pulses. The values of t_{PHL} and t_{PLH} are not necessarily equal but in many cases they are the same.

RELATED PROBLEM

One type of logic gate has a specified maximum t_{PLH} and t_{PHL} of 10 ns. For another type of gate the value is 4 ns. Which gate can operate at the highest frequency?

DC SUPPLY VOLTAGE (V_{CC}) The typical dc supply voltage for CMOS logic is either 5 V, 3.3 V, 2.5 V, or 1.8 V, depending on the category. An advantage of CMOS is that the supply voltages can vary over a wider range than for bipolar logic. Propagation delay time and power dissipation can be affected by variation in supply voltage. For example, the 5 V CMOS can tolerate supply variations from 2 V to 6 V and still operate properly although propagation delay time and power dissipation are significantly affected. The 3.3 V CMOS can operate with supply voltages from 2 V to 3.6 V. The typical dc supply voltage for bipolar logic is 5.0 V with a minimum of 4.5 V and a maximum of 5.5 V.

POWER DISSIPATION The **power dissipation**, P_D , of a logic gate is the product of the dc supply voltage and the average supply current. Normally, the supply current when the gate output is LOW is greater than when the gate output is HIGH. The manufacturer's data sheet usually designates the supply current for the LOW output state as I_{CCL} and for the HIGH state as I_{CCH} . The average supply current is determined based on a 50% duty cycle (output LOW half the time and HIGH half the time), so the average power dissipation of a logic gate is

A lower power dissipation means less current from the dc supply.

$$P_D = V_{CC} \left(\frac{I_{CCH} + I_{CCL}}{2} \right) \quad (7)$$

CMOS gates have very low power dissipations compared to the bipolar family. However, the power dissipation of CMOS is dependent on the frequency of operation. At zero frequency the quiescent power is typically in the microwatt/gate range, and at the maximum operating frequency it can be in the low milliwatt range; therefore, power is sometimes specified at a given frequency.

INPUT AND OUTPUT LOGIC LEVELS V_{IL} is the LOW level input voltage for a logic gate, and V_{IH} is the HIGH level input voltage. The 5 V CMOS accepts a maximum voltage of 1.5 V as V_{IL} and a minimum voltage of 3.5 V as V_{IH} . Bipolar logic accepts a maximum voltage of 0.8 V as V_{IL} and a minimum voltage of 2 V as V_{IH} .

V_{OL} is the LOW level output voltage and V_{OH} is the HIGH level output voltage. For 5 V CMOS, the maximum V_{OL} is 0.33 V and the minimum V_{OH} is 4.4 V. For bipolar logic, the maximum V_{OL} is 0.4 V and the minimum V_{OH} is 2.4 V. All values depend on operating conditions as specified on the data sheet for the specific device.

SPEED-POWER PRODUCT (SPP) This parameter (**speed-power product**) can be used as a measure of the performance of a logic circuit taking into account the propagation delay time and the power dissipation. It is especially useful for comparing the various logic gate series within the CMOS and bipolar families or for comparing a CMOS gate to a TTL gate.

The SPP of a logic circuit is the product of the propagation delay time and the power dissipation and is expressed in joules (J), which is the unit of energy. The formula is

$$SPP = t_p P_D \quad (8)$$

EXAMPLE 20

A certain gate has a propagation delay of 5 ns and $I_{CCH} = 1$ mA and $I_{CCL} = 2.5$ mA with a dc supply voltage of 5 V. Determine the speed-power product.

SOLUTION

$$P_D = V_{CC} \left(\frac{I_{CCH} + I_{CCL}}{2} \right) = 5 \text{ V} \left(\frac{1 \text{ mA} + 2.5 \text{ mA}}{2} \right) = 5 \text{ V}(1.75 \text{ mA})$$

$$= 8.75 \text{ mW}$$

$$SPP = (5 \text{ ns})(8.75 \text{ mW}) = \mathbf{43.75 \text{ pJ}}$$

RELATED PROBLEM

If the propagation delay of a gate is 15 ns and its *SPP* is 150 pJ, what is its average power dissipation?

A higher fan-out means that a gate output can be connected to more gate inputs.

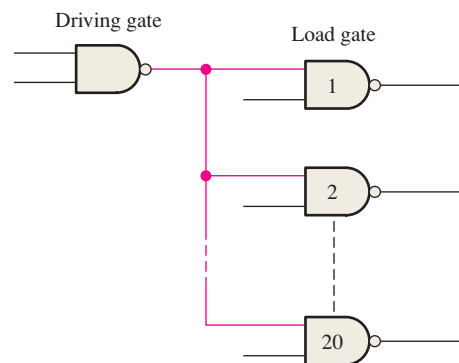
FAN-OUT AND LOADING The **fan-out** of a logic gate is the maximum number of inputs of the same series in an IC family that can be connected to a gate's output and still maintain the output voltage levels within specified limits. Fan-out is a significant parameter only for bipolar logic because of the type of circuit technology. Since very high impedances are associated with CMOS circuits, the fan-out is very high but depends on frequency because of capacitive effects.

Fan-out is specified in terms of **unit loads**. A unit load for a logic gate equals one input to a like circuit. For example, if the current from a LOW input (I_{IL}) of a certain gate is 0.4 mA and the current that a LOW output (I_{OL}) can accept is 8.0 mA, the number of unit loads that the gate can drive in the LOW state is

$$\text{Unit loads} = \frac{I_{OL}}{I_{IL}} = \frac{8.0 \text{ mA}}{0.4 \text{ mA}} = 20$$

Figure 63 shows a logic gate driving a number of other gates of the same circuit technology, where the number of gates depends on the particular circuit technology. For example, the maximum number of gate inputs (unit loads) that a certain series bipolar gate can drive is 20.

FIGURE 63 The NAND gate output fans out to a maximum number of NAND gates of the same type.


SECTION 8 CHECKUP

- Which IC logic technology generally has the lowest power dissipation?
- A positive pulse is applied to an inverter input. The time from the leading edge of the input to the leading edge of the output is 10 ns. The time from the trailing edge of the input to the trailing edge of the output is 8 ns. What are the values of t_{PLH} and t_{PHL} ?
- A certain gate has a propagation delay time of 6 ns and a power dissipation of 3 mW. Determine the speed-power product?
- Define I_{CCL} and I_{CCH} .
- Define V_{IL} and V_{IH} .
- Define V_{OL} and V_{OH} .

9 PROGRAMMABLE LOGIC

In this section, the basic concept of the programmable AND array, which forms the basis for most programmable logic, is discussed, and the major process technologies are covered. A programmable logic device (PLD) is one that does not initially have a fixed-logic function but that can be programmed to implement just about any logic design. As you have learned, two types of PLD are the SPLD and CPLD. In addition to the PLD, the other major category of programmable logic is the FPGA. For simplicity, all of these devices will be referred to as PLDs. Also, some important concepts in programming are discussed.

After completing this section, you should be able to

- Describe the concept of a programmable AND array
- Discuss various process technologies
- Discuss downloading a design to a programmable logic device
- Discuss text entry and graphic entry as two methods for programmable logic design
- Explain in-system programming
- Write simple VHDL and Verilog program code for logic gates

Basic Concept of the AND Array

Most types of PLDs use some form of **AND array**. Basically, this array consists of AND gates and a matrix of interconnections with programmable links at each cross point, as shown in Figure 64(a). The purpose of the programmable links is to either make or break a connection between a row line and a column line in the interconnection matrix. For each input to an AND gate, only one programmable link is left intact in order to connect the desired variable to the gate input. Figure 64(b) illustrates an array after it has been programmed.

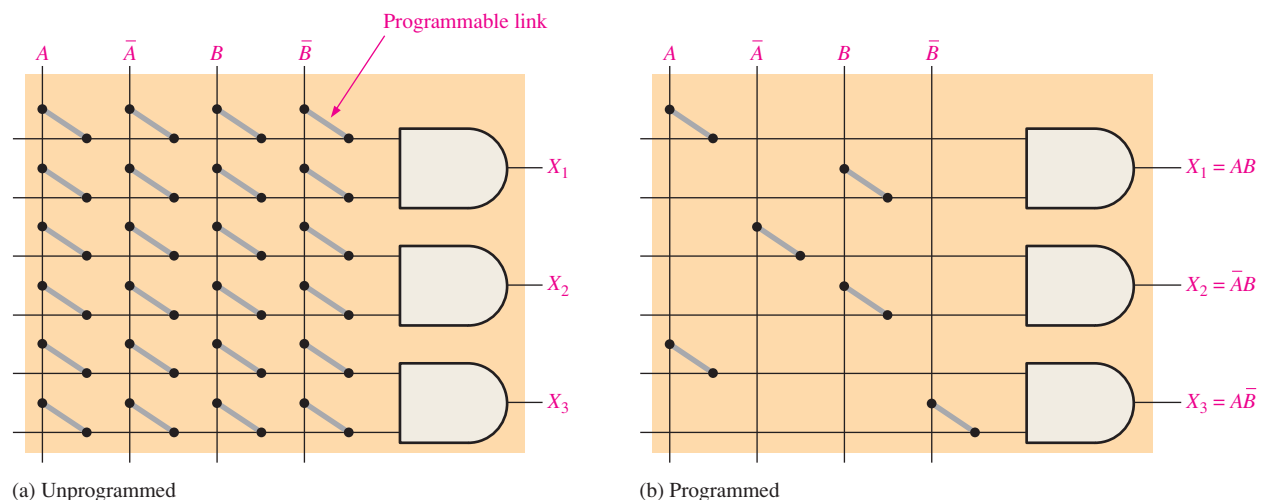


FIGURE 64 Basic concept of a programmable AND array.

EXAMPLE 21

Show the AND array in Figure 64(a) programmed for the following outputs:
 $X_1 = A\bar{B}$, $X_2 = \bar{A}B$, and $X_3 = \bar{A}\bar{B}$

SOLUTION

See Figure 65.

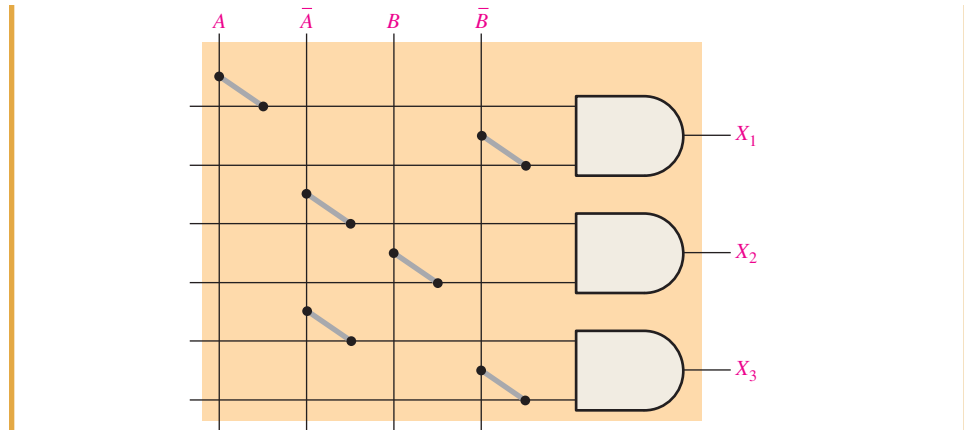


FIGURE 65

RELATED PROBLEM

How many rows, columns, and AND gate inputs are required for three input variables in a 3-AND gate array?

Programmable Link Process Technologies

Several different process technologies are used for programmable links in PLDs.

FUSE TECHNOLOGY

This was the original programmable link technology. It is still used in some SPLDs. The fuse is a metal link that connects a row and a column in the interconnection matrix. Before programming, there is a fused connection at each intersection. To program a device, the selected fuses are opened by passing a current through them sufficient to “blow” the fuse and break the connection. The intact fuses remain and provide a connection between the rows and columns. The fuse link is illustrated in Figure 66. Programmable logic devices that use fuse technology are one-time programmable (OTP).

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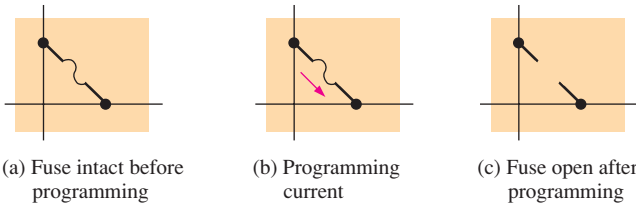


FIGURE 66 The programmable fuse link.

ANTIFUSE TECHNOLOGY

An antifuse programmable link is the opposite of a fuse link. Instead of breaking the connection, a connection is made during programming. An antifuse starts out as an open circuit whereas the fuse starts out as a short circuit. Before programming, there are no connections between the rows and columns in the interconnection matrix. An antifuse is basically two conductors separated by an insulator. To program a device with antifuse technology, a programmer tool applies a sufficient voltage across selected antifuses to break down the insulation between the two conductive materials, causing the insulator to become a low-resistance link. The antifuse link is illustrated in Figure 67. An antifuse device is also a one-time programmable (OTP) device.

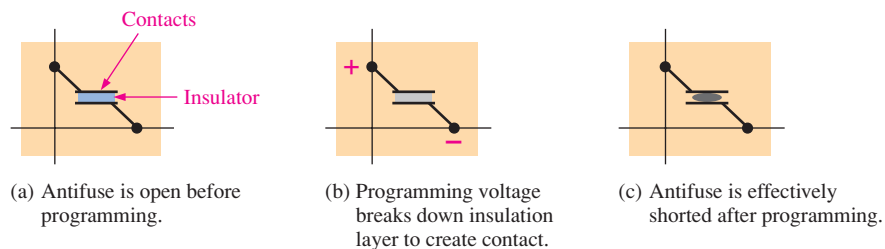


FIGURE 67 The programmable antifuse link.

EPROM TECHNOLOGY In certain programmable logic devices, the programmable links are similar to the memory cells in **EPROMs** (electrically programmable read-only memories). This type of PLD is programmed using a special tool known as a device programmer. The device is inserted into the programmer, which is connected to a computer running the programming software. Most EPROM-based PLDs are one-time programmable (OTP). However, those with windowed packages can be erased with UV (ultraviolet) light and reprogrammed using a standard PLD programming fixture. EPROM process technology uses a special type of MOS transistor, known as a floating-gate transistor, as the programmable link. The floating-gate device utilizes a process called Fowler-Nordheim tunneling to place electrons in the floating-gate structure.

In a programmable AND array, the floating-gate transistor acts as a switch to connect the row line to either a HIGH or a LOW, depending on the input variable. For input variables that are not used, the transistor is programmed to be permanently *off* (open). Figure 68 shows one AND gate in a simple array. Variable *A* controls the state of the transistor in the first column, and variable *B* controls the transistor in the third column. When a transistor is *off*, like an open switch, the input line to the AND gate is at +V (HIGH). When a transistor is *on*, like a closed switch, the input line is connected to ground (LOW). When variable *A* or *B* is 0 (LOW), the transistor is *on*, keeping the input line to the AND gate LOW. When *A* or *B* is 1 (HIGH), the transistor is *off*, keeping the input line to the AND gate HIGH.

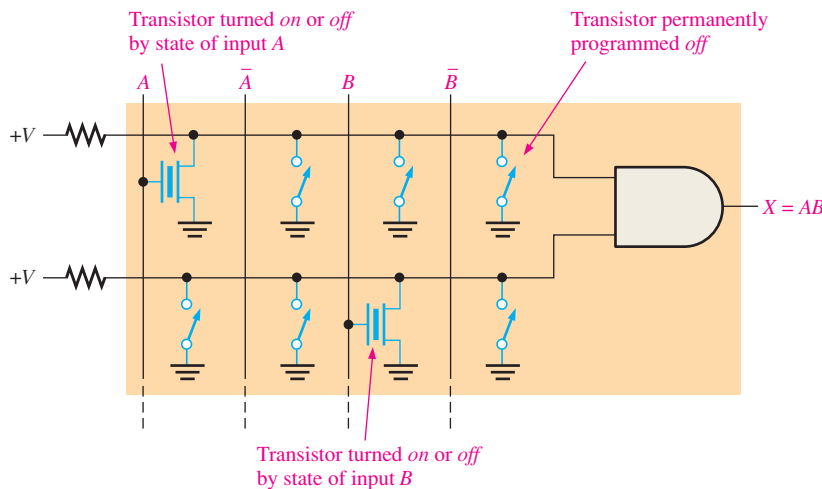


FIGURE 68 A simple AND array with EPROM technology. Only one gate in the array is shown for simplicity.

EEPROM TECHNOLOGY Electrically erasable programmable read-only memory technology is similar to EPROM because it also uses a type of floating-gate transistor in E²CMOS cells. The difference is that **EEPROM** can be erased and reprogrammed electrically without the need for UV light or special fixtures. An E²CMOS device can be programmed after being installed on a printed circuit board, and many can be reprogrammed while operating in a system. This is called **in-system programming (ISP)**. Figure 68 can also be used as an example to represent an AND array with EEPROM technology.

FLASH TECHNOLOGY **Flash** technology is based on a single transistor link and is both nonvolatile and reprogrammable. Flash elements are a type of EEPROM but are faster and result in higher density devices than the standard EEPROM link.

SRAM TECHNOLOGY Many FPGAs and some CPLDs use a process technology similar to that used in **SRAMs** (static random-access memories). The basic concept of

SRAM-based programmable logic arrays is illustrated in Figure 69(a). A SRAM-type memory cell is used to turn a transistor *on* or *off* to connect or disconnect rows and columns. For example, when the memory cell contains a 1 (green), the transistor is *on* and connects the associated row and column lines, as shown in part (b). When the memory cell contains a 0 (blue), the transistor is *off* so there is no connection between the lines, as shown in part (c).

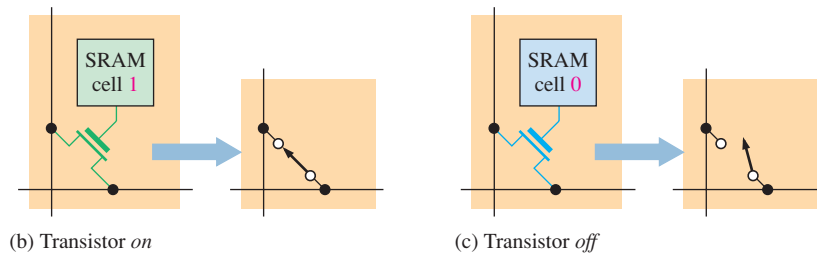
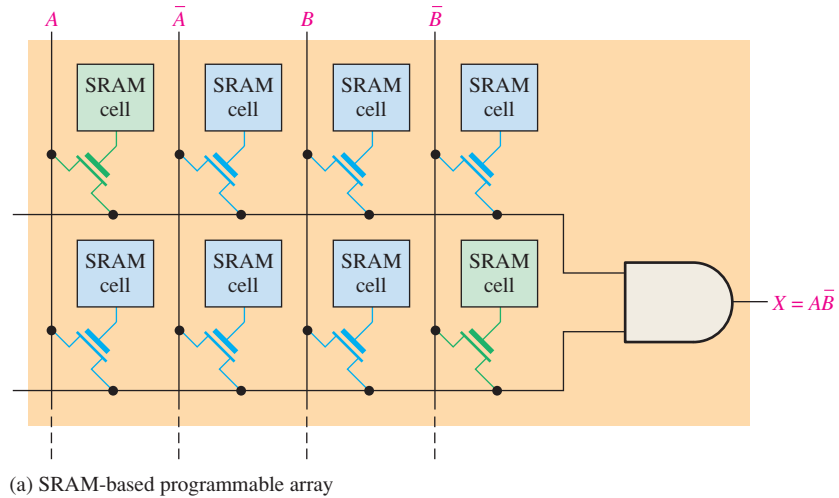
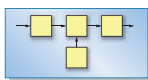


FIGURE 69 Basic concept of an AND array with SRAM technology.

SRAM technology is different from the other process technologies discussed because it is a volatile technology. This means that a SRAM cell does not retain data when power is turned *off*. The programming data must be loaded into a memory; and when power is turned *on*, the data from the memory reprograms the SRAM-based PLD.

Most system-level designs incorporate a variety of devices such as RAMs, ROMs, controllers, and processors that are interconnected by general-purpose logic devices often referred to as “glue” logic. PLDs have come to replace many of the SSI and MSI “glue” devices. The use of PLDs provides a reduction in package count.

For example, in computer memory systems, PLDs can be used for memory address decoding and to generate memory write signals as well as other functions.



SYSTEM NOTE

The fuse, antifuse, EPROM, EEPROM, and flash process technologies are nonvolatile, so they retain their programming when the power is *off*. A fuse is permanently open, an antifuse is permanently closed, and floating-gate transistors used in EPROM-based and EEPROM-based arrays can retain their *on* or *off* state indefinitely.

Device Programming

The general concept of programming has been discussed and you have seen how interconnections can be made in a simple array by opening or closing the programmable links. SPLDs, CPLDs, and FPGAs are programmed in essentially the same way. The devices with OTP (one-time programmable) process technologies (fuse, antifuse, or EPROM) must be programmed with a special hardware fixture called a *programmer*. The programmer is connected to a computer by a standard interface cable. Development software is installed on the computer, and the device is inserted into the programmer socket. Most programmers have adapters that allow different types of packages to be plugged in.

EEPROM, flash, and SRAM-based programmable logic devices are reprogrammable and can be reconfigured multiple times. Although a device programmer can be used for this type of device, it is generally programmed initially on a PLD development board, as shown in Figure 70. A logic design can be developed using this approach because any necessary changes during the design process can be readily accomplished by simply reprogramming the PLD. A PLD to which a software logic design can be downloaded is called a **target device**. In addition to the target device, development boards typically provide other circuitry and connectors for interfacing to the computer and other peripheral circuits. Also, test points and display devices for observing the operation of the programmed device are included on the development board.

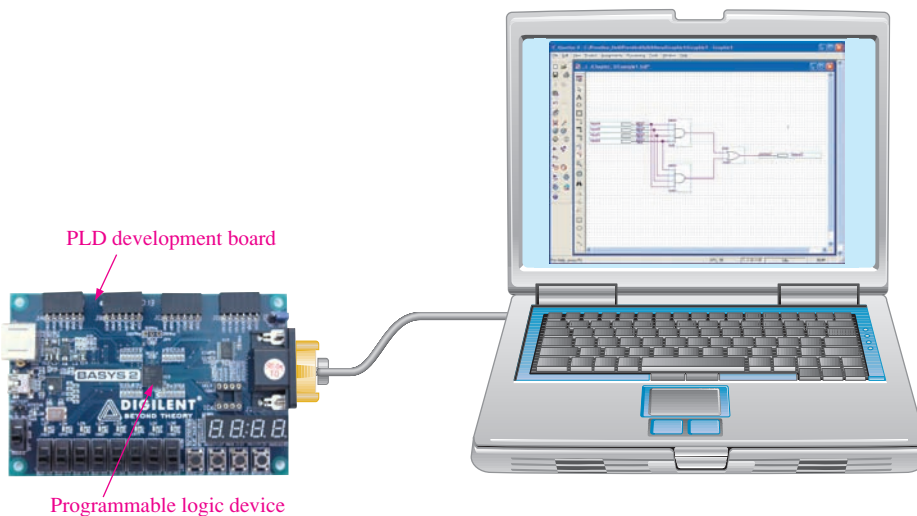


FIGURE 70 Programming setup for reprogrammable logic devices. (Photo courtesy of Digilent, Inc.)

DESIGN ENTRY Design entry is where the logic design is programmed using development software. The two main ways to enter a design are by text entry or graphic (schematic) entry, and manufacturers of programmable logic provide software packages to support their devices that allow for both methods.

Text entry in most development software, regardless of the manufacturer, supports two or more hardware development languages (**HDLs**). For example, all software packages support both IEEE standard HDLs, VHDL, and Verilog. Some software packages also support certain proprietary languages such as AHDL.

In **graphic (schematic) entry**, logic symbols such as AND gates and OR gates are placed on the screen and interconnected to form the desired circuit. In this method you use the familiar logic symbols, but the software actually converts each symbol and interconnections to a text file for the computer to use; you do not see this process. A simple example of two text entry screens and a graphic entry screen for an AND gate is shown in Figure 71. Graphic entry is generally used for less-complex logic circuits; and text entry, although it can also be used for very simple logic, is generally used for larger, more complex implementation.

```

Verilog1.v
module Verilog1(A, B, X);
  output X;
  input A, B;
  assign X = A && B;
endmodule

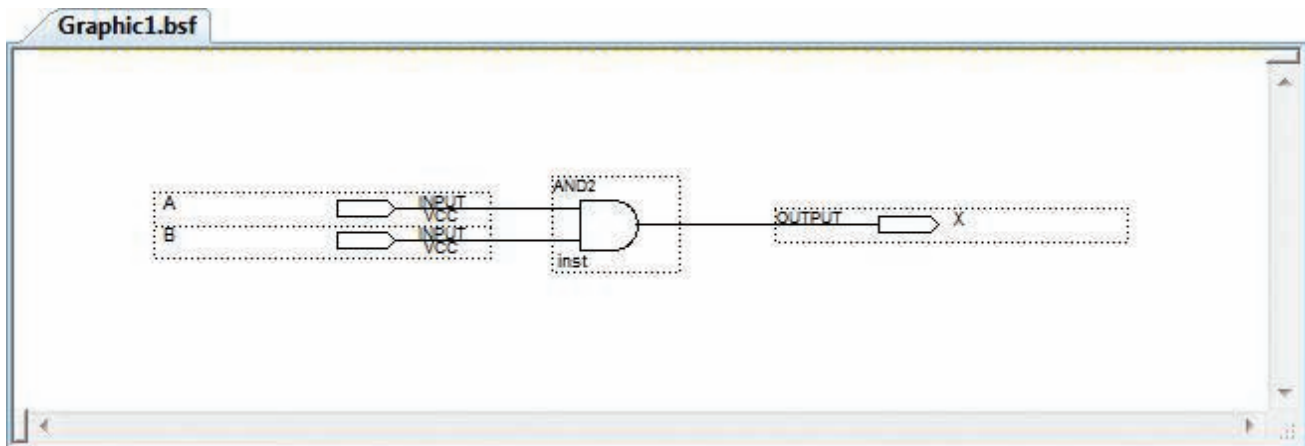
```

```

Vhdl1.vhd
entity VHDL1 is
  port(A, B: in bit; X: out bit);
end entity VHDL1;
architecture ANDfunction of VHDL1 is
begin
  X <= A and B;
end ANDfunction;

```

(a) Verilog and VHDL text entry



(b) Equivalent graphic (schematic) entry

FIGURE 71 Examples of design entry for an AND gate.

In-System Programming (ISP)

Certain CPLDs and FPGAs can be programmed after they have been installed on a system printed circuit board (PCB). After a logic design has been developed and fully tested on a development board, it can then be programmed into a “blank” device that is already soldered onto a system board in which it will be operating. Also, if a design change is required, the device on the system board can be reconfigured to incorporate the design modifications.

In a production situation, programming a device on the system board minimizes handling and eliminates the need for keeping stocks of preprogrammed devices. It also rules out the possibility of wrong parts being placed in a product. Unprogrammed (blank) devices can be kept in the warehouse and programmed on-board as needed. This minimizes the capital a business needs for inventories and enhances the quality of its products.

JTAG The standard established by the Joint Test Action Group is the commonly used name for IEEE Std. 1149.1. The **JTAG** standard was developed to provide a simple method, called boundary scan, for testing programmable devices for functionality as well as testing circuit boards for bad connections—shorted pins, open pins, bad traces, and the like. Also, JTAG has been used as a convenient way of configuring programmable devices in-system. As the demand for field-upgradable products increases, the use of JTAG as a convenient way of reprogramming CPLDs and FPGAs increases.

JTAG-compliant devices have internal dedicated hardware that interprets instructions and data provided by four dedicated signals. These signals are defined by the JTAG standard to be TDI (Test Data In), TDO (Test Data Out), TMS (Test Mode Select), and TCK (Test Clock). The dedicated JTAG hardware interprets instructions and data on the TDI and TMS signals, and drives data out on the TDO signal. The TCK signal is used to clock the process.

EMBEDDED PROCESSOR Another approach to in-system programming is the use of an embedded microprocessor and memory. The processor is embedded within the system along with the CPLD or FPGA and other circuitry, and it is dedicated to the purpose of in-system configuration of the programmable device.

As you have learned, SRAM-based devices are volatile and lose their programmed data when the power is turned *off*. It is necessary to store the programming data in a PROM (programmable read-only memory), which is nonvolatile. When power is turned *on*, the embedded processor takes control of transferring the stored data from the PROM to the CPLD or FPGA.

Also, an embedded processor is sometimes used for reconfiguration of a programmable device while the system is running. In this case, design changes are done with software, and the new data are then loaded into a PROM without disturbing the operation of the system. The processor controls the transfer of the data to the device “on-the-fly” at an appropriate time.

Introduction to VHDL and Verilog

Hardware description languages (HDLs), such as VHDL and Verilog, differ from software programming languages because they include ways of describing the propagation of time and other characteristics of the logic. An HDL implements a new logic design in hardware (PLD), whereas a software programming language such as C or BASIC instructs existing hardware what to do. The two standard hardware description languages (HDLs) used for programming PLDs are **VHDL** and **Verilog**. *Tutorials for both VHDL and Verilog are found on the website.*

HDL DESCRIPTIONS OF LOGIC GATES The logic gates covered in this chapter are described with VHDL and with Verilog in Figures 72 through 76. Two

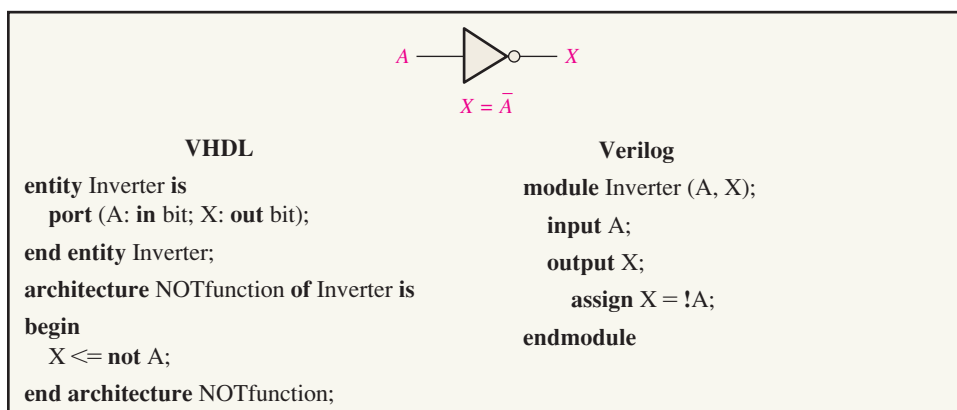


FIGURE 72 Inverter.

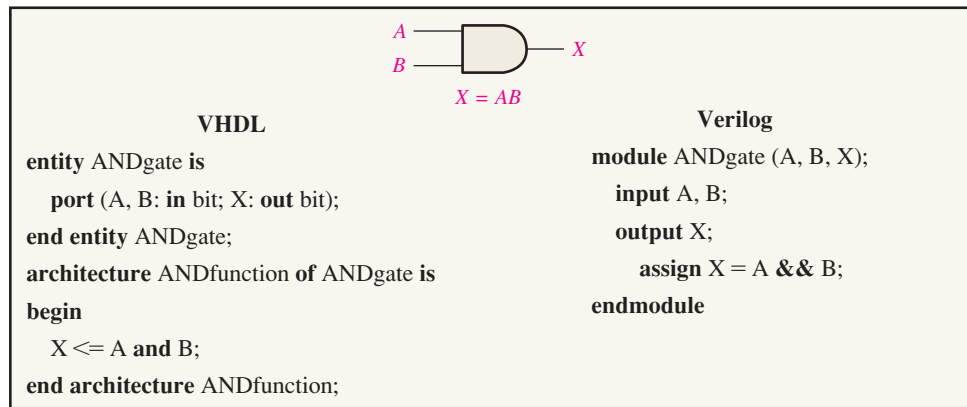


FIGURE 73 AND gate.

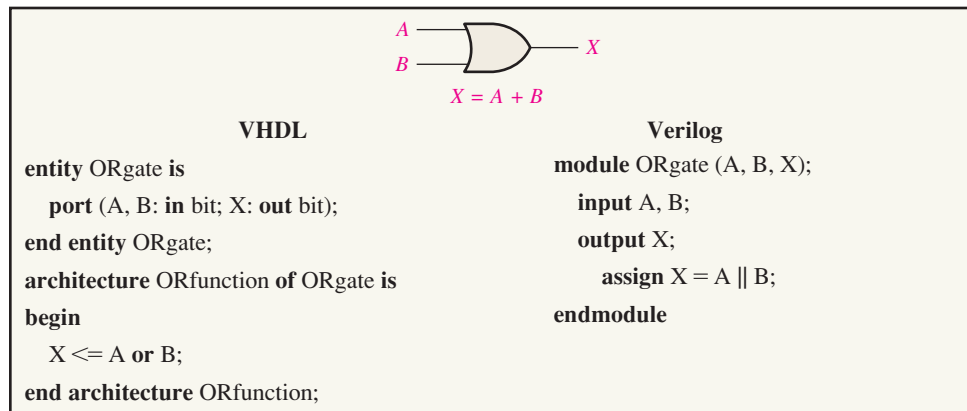


FIGURE 74 OR gate.

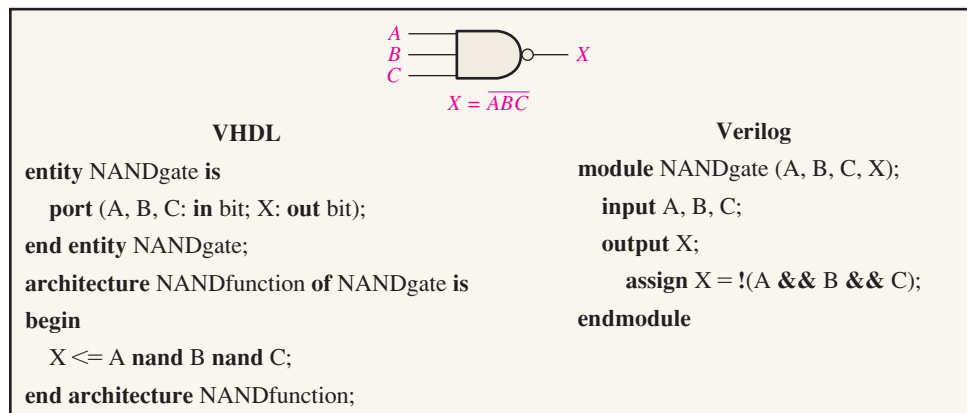


FIGURE 75 3-input NAND gate.

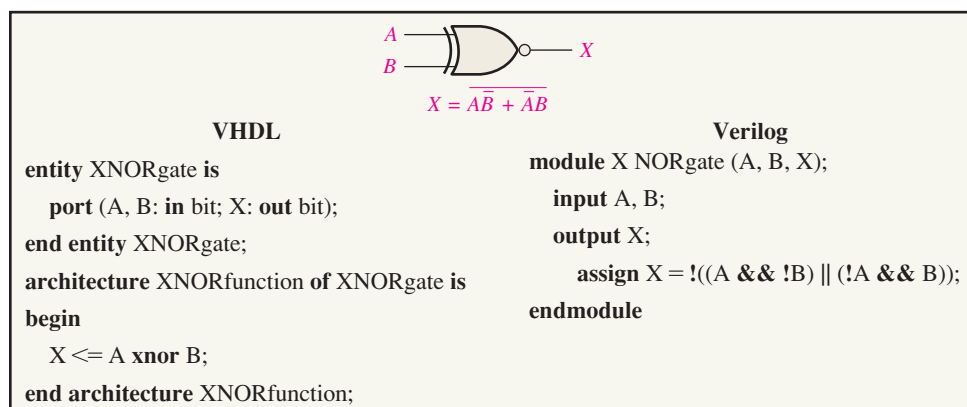


FIGURE 76 Exclusive-NOR gate.

gates are left as Checkup exercises. VHDL describes a function with an **entity/architecture** structure. Verilog uses a **module** structure to describe a function. Verilog logical operators are ! for NOT, && for AND, and || for OR. Keywords that are part of the language syntax are shown bold for clarity in both VHDL and Verilog.

SECTION 9 CHECKUP

1. List six process technologies used for programmable links in programmable logic.
2. What does the term *volatile* mean in relation to PLDs; which process technology is volatile?
3. What are two design entry methods for programming PLDs and FPGAs?
4. Define JTAG.
5. Write VHDL and Verilog descriptions of a NOR gate with three inputs.
6. Write VHDL and Verilog descriptions of an XOR gate.

10 TROUBLESHOOTING

Troubleshooting is the process of recognizing, isolating, and correcting a fault or failure in a system. To be an effective troubleshooter, you must understand how the system works and be able to recognize incorrect performance. Troubleshooting can be at the system level, the circuit board level, or the component level. Today, troubleshooting down to the board level is usually sufficient. Once a board is determined to be defective, it is usually replaced with a new one. However, if the circuit board is to be saved, component-level troubleshooting may be necessary.



After completing this section, you should be able to

- Describe the steps in a troubleshooting procedure
- Discuss the half-splitting method
- Discuss the signal-tracing method
- Describe the troubleshooting of a particular process control system

Basic Hardware Troubleshooting Methods

Troubleshooting at a system level requires good detective work. When a problem occurs, the list of potential causes is usually quite large. You must gather a sufficient amount of detailed information and systematically narrow the list of potential causes to determine the problem. As a general guide to troubleshooting a system, the following steps should be followed:

1. Gather information on the problem.
2. Identify the symptoms and possible failures.
3. Isolate point(s) of failure.
4. Apply proper tools to determine the cause of the problem.
5. Fix the problem.

CHECK THE OBVIOUS After collecting information on the problem, make sure to first check for obvious faults: absence of DC power, blown fuses, tripped circuit breakers, faulty burned out indicators such as lamps, loose connectors, broken or loose wires, switches in the wrong position, physical damages, boards not properly inserted, wire fragments or solder splashes shorting components, and poor quality contacts on printed circuit



HANDS ON TIP

Proper grounding is important when you set up to take measurements or work on a system. Properly grounding the oscilloscope protects you from shock, and grounding yourself protects circuits from damage. Grounding the oscilloscope means to connect it to earth ground by plugging the three-prong power cord into a grounded outlet. Grounding yourself means using a wrist-type grounding strap, particularly when you are working with CMOS logic. The wrist strap must have a high-value resistor between the strap and ground for protection against accidental contact with a voltage source.

For accurate measurements, make sure that the ground in the circuit you are testing is the same as the scope ground. This can be done by connecting the ground lead on the scope probe to a known ground point in the circuit, such as the metal chassis or a ground point on the circuit.

boards. For any troubleshooting task, you must have a system/circuit diagram. Other useful documents are a table of signal characteristics and a prewritten troubleshooting guide for the specific system.

REPLACEMENT Assume that a given system has multiple circuit boards. The simplest and quickest way to fix a problem is by replacing the circuit boards one by one with a known good board until the problem is corrected. This approach, of course, requires that duplicate boards be available. Another drawback to this approach is that an outside source may be causing the fault, such as a short in a connector; and by replacing the board, the fault is transferred to the new board.

REPRODUCING THE SYMPTOMS Once the symptoms of a faulty system are identified, find a way to reproduce the problem. If the problem can be reproduced, it can be isolated and resolved. In some systems, the symptom may be self-evident, but in others it may have to be induced by application of a level or signal at a given point. Once this is done, then a systematic approach can be used to isolate the cause or causes of a problem. You should always consider the possibility that there is more than one fault.

If the symptoms are intermittent, the task of troubleshooting becomes more difficult. For example, in some cases a component may be temperature sensitive and fail only when the temperature is too high or too low. In these cases, the temperature can be varied by the simple process of blowing cool air on the component of concern to lower the temperature or using a heat gun to raise it, while monitoring the operation of the system.

HALF-SPLITTING METHOD In this procedure, you check for the presence or absence of a signal at a point halfway between input and output. If the signal is present, you know the fault is in the second half. If the signal is absent, you know the fault is in the first half. Then you split the defective half in half and check for a signal. The process is continued until a certain area of the system has been isolated. This may be a single circuit board in a system with many circuit boards or a component on a given circuit board. In a large system, this procedure can save a lot of time over moving down the line checking each block or stage as you go. This method is usually best applied in large complex systems. Figure 77 is a simple illustration of this method. The system is represented with the four green blocks. Additional steps are added to left or right for additional blocks.

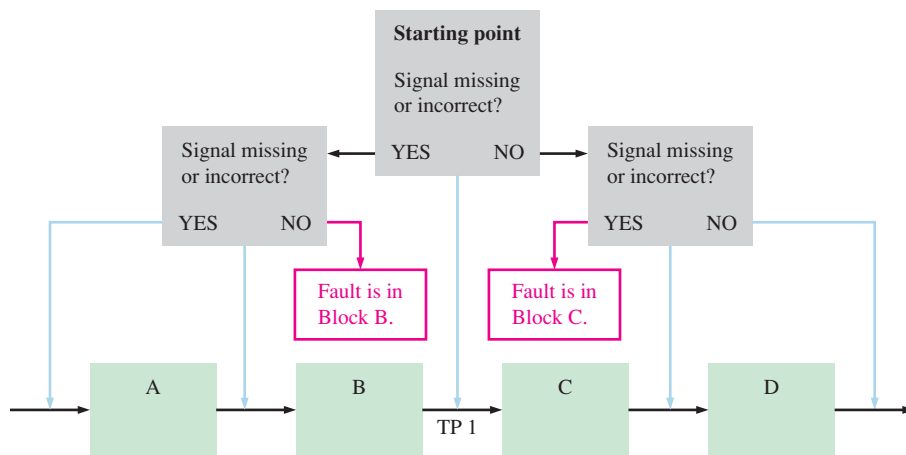


FIGURE 77 Concept of the half-splitting method. The blue arrows indicate the test points.

SIGNAL-TRACING METHOD Signal tracing is the procedure of tracking signals as they progress through a system from input to output. Signal tracing can be used with half-splitting, where you check for a signal at each point from where the absence of a signal was detected. Signal tracing can also begin at the output where there is an incorrect or absent signal and go back toward the input from point to point until a correct signal is

found. Also, you can begin at the input and check the signal and move toward the output from point to point until the correct signal is lost. In both cases, the fault would be between the point and the output. Of course, you must know what the signal is supposed to look like in order to know if anything is wrong. Figure 78 illustrates the concept of signal tracing.

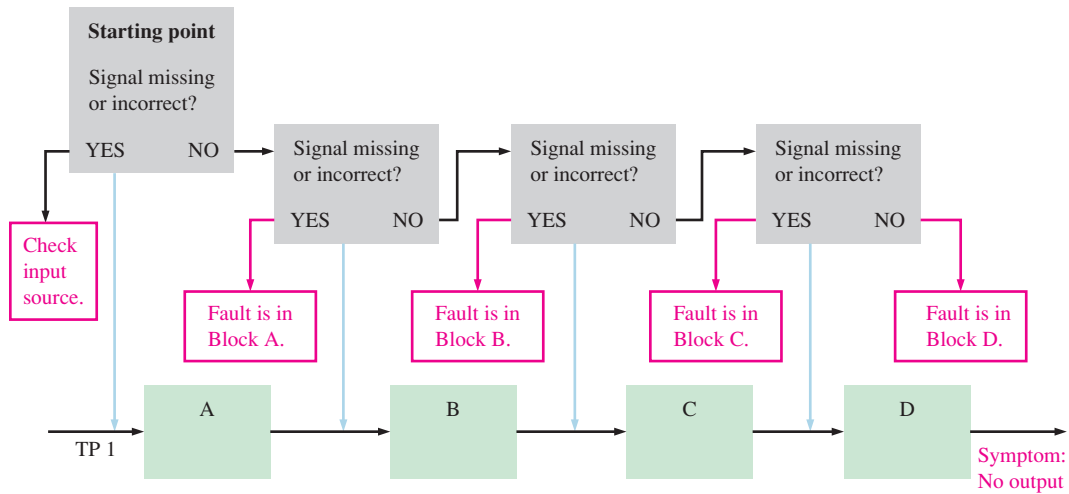


FIGURE 78 Concept of the signal-tracing method. Input to output is shown. The same applies if you start at the output and go toward the input.

SIGNAL SUBSTITUTION AND INJECTION Signal substitution is used when the system being tested has been separated from its signal source. A generator signal is used to replace the normal signal that comes from the source when the system or portion of a system is recombined with the part that normally produces the input signal. Signal injection can be used to insert a signal at certain points in the system using the half-splitting approach.

EXAMPLE 22

A simple generic self-contained system that is not software driven is used to illustrate the basic approach to troubleshooting. This system, which is a type of state machine, is used to control a sequential process in a variety of specific applications. A block diagram of the system is shown in Figure 79. It consists of four interdependent functional blocks. The outputs consist of four signals that sequentially initiate four processes in a given sequence. A sensor detects specified conditions in the process and causes the outputs to be altered to accommodate the condition.

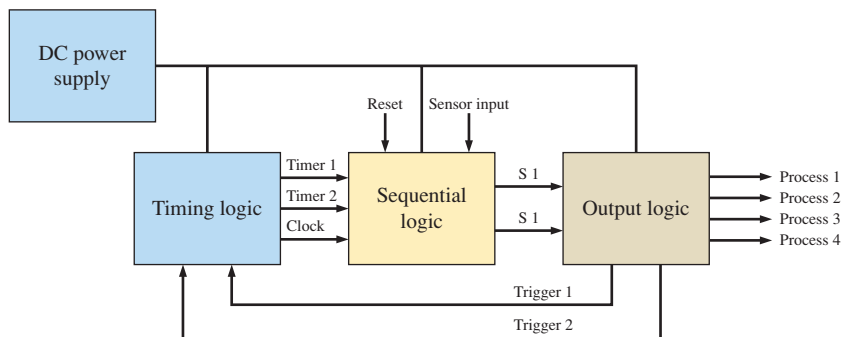


FIGURE 79 Block diagram of a process control system.

In a particular application, the system controls the packaging of golf balls into a tubular canister on an automated assembly line. A pulse on the Process 1 output moves the next canister into position, which starts the process. The pulse on the Process 2 output enables six balls to drop into the canister. When the canister is filled,

a pulse on the Process 3 output causes the canister lid to be attached and sealed. A pulse on the Process 4 output initiates the attachment of the label to the canister and sends it on its way down the line.

You observe that the canisters get jammed up on the assembly line and do not move past a certain point. As the troubleshooter, how would you proceed to troubleshoot this problem?

SOLUTION

Identify the symptom as follows: When the system reaches Process 3, the lid is not attached and the canister waits in position, keeping the next canister from moving into position. The cause is most likely either the absence of a pulse on the Process 3 output or the sequence is hanging up at Process 2 and not going to Process 3. It is difficult to narrow the cause down to one specific block because certain failures in any one block could result in the problem. The specification document for the system shows the proper operation in terms of a timing diagram, which is shown in Figure 80.

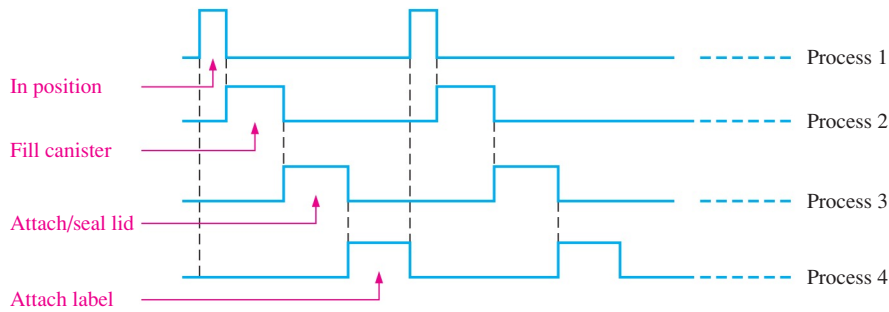


FIGURE 80 Correct timing diagram for the process control system.

The next step is to use an oscilloscope to look at the output waveforms. The setup is shown in Figure 81 with the physical system plugged into an electrical outlet.

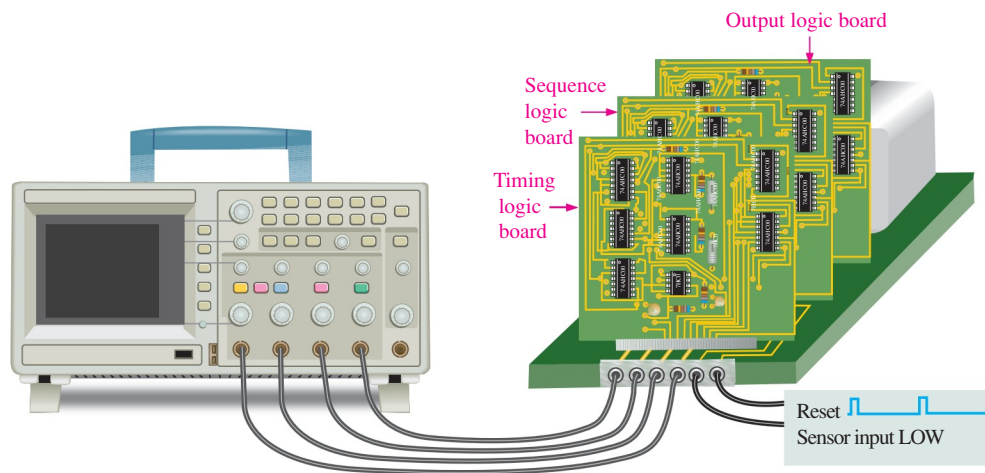


FIGURE 81 Test setup for troubleshooting the process control system.

After checking that DC power is going to all circuits and inspecting the system for obvious faults, connect the outputs and observe them on the scope. Process 1, 3, and 4 outputs are at a constant LOW level, and Process 2 is a constant HIGH level. This measurement confirms that Process 2 output is stuck in the HIGH state, so the system can't advance through its normal sequence.

A fault in the Sequential Logic board is causing the state machine to lock up in the Process 2 state. To verify this, observe the system sequencing through the first two states. In order to do this, the system must be reset periodically so that the incorrect sequence repeats itself. A pulse generator can generate reset pulses with the period set to exceed the normal cycle time of the system. The scope display shown in Figure 82 is observed during this test procedure. This shows that the state machine is recycling through states 1 and 2 instead of states 1, 2, 3, and 4. Without a reset, the system gets to state 2 and locks up. The reset forces it back to state 1 each time.

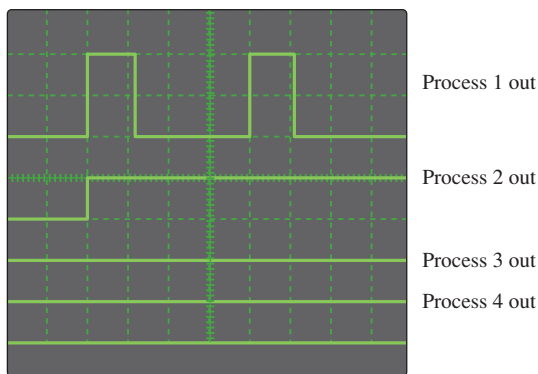


FIGURE 82 Repetitive waveforms when faulty system is periodically reset.

The final step is to replace the Sequential Logic board (middle board) in Figure 81 and run the system without the reset input. After doing the swap out, you find that the system works properly. The next decision to be made is whether to repair or discard the faulty board. If the board is to be saved, you would then begin the troubleshooting process at the board level to determine which component(s) is defective.

SECTION 10 CHECKUP

- List five steps in the troubleshooting procedure.
- Name two troubleshooting methods.
- List five obvious things to look for first in a failed system.
- Is it important to know about the relationship between a cause and a symptom?

SUMMARY

- Gate symbols and Boolean expressions for the outputs of an inverter and 2-input gates are shown in Figure 83.



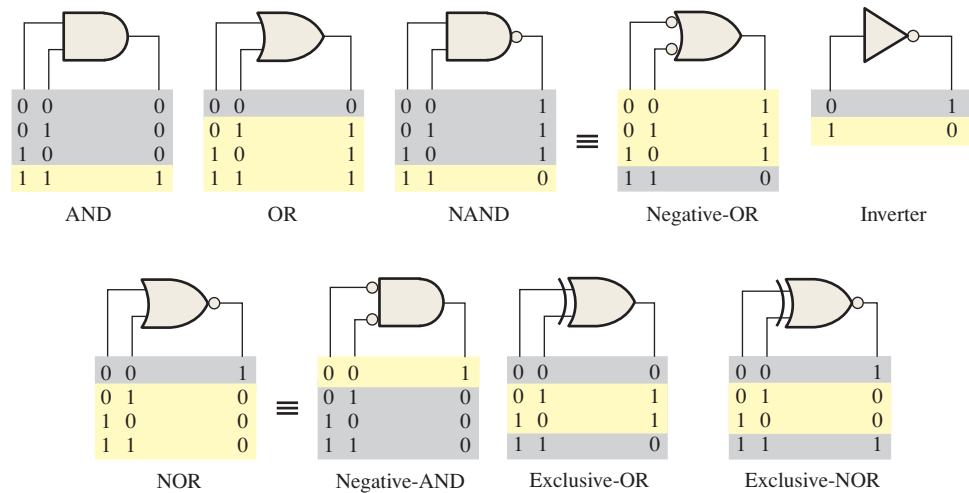
FIGURE 83

- Commutative laws: $A + B = B + A$
 $AB = BA$
- Associative laws: $A + (B + C) = (A + B) + C$
 $A(BC) = (AB)C$
- Distributive law: $A(B + C) = AB + AC$
- Boolean rules:

1. $A + 0 = A$	7. $A \cdot A = A$
2. $A + 1 = 1$	8. $A \cdot \bar{A} = 0$
3. $A \cdot 0 = 0$	9. $\bar{\bar{A}} = A$
4. $A \cdot 1 = A$	10. $A + AB = A$
5. $A + A = A$	11. $A + \bar{A}B = A + B$
6. $A + \bar{A} = 1$	12. $(A + B)(A + C) = A + BC$
- The inverter output is the complement of the input.
- The AND gate output is HIGH only when all the inputs are HIGH.

LOGIC GATES AND GATE COMBINATIONS

- The OR gate output is HIGH when any of the inputs is HIGH.
- The NAND gate output is LOW only when all the inputs are HIGH.
- The NAND can be viewed as a negative-OR whose output is HIGH when any input is LOW.
- The NOR gate output is LOW when any of the inputs is HIGH.
- The NOR can be viewed as a negative-AND whose output is HIGH only when all the inputs are LOW.
- The exclusive-OR gate output is HIGH when the inputs are not the same.
- The exclusive-NOR gate output is LOW when the inputs are not the same.
- Distinctive shape symbols and truth tables for various logic gates (limited to 2 inputs) are shown in Figure 84.



Note: Active states are shown in yellow.

FIGURE 84

- The average power dissipation of a logic gate is

$$P_D = V_{CC} \left(\frac{I_{CCH} + I_{CCL}}{2} \right)$$

- The speed-power product of a logic gate is

$$SPP = t_p P_D$$

- Most programmable logic devices (PLDs) are based on some form of AND array.
- Programmable link technologies are fuse, antifuse, EPROM, EEPROM, flash, and SRAM.
- A PLD can be programmed in a hardware fixture called a programmer or mounted on a development printed circuit board.
- PLDs have an associated software development package for programming.
- Two methods of design entry using programming software are text entry (HDL) and graphic (schematic) entry.
- ISP PLDs can be programmed after they are installed in a system, and they can be reprogrammed at any time.
- JTAG stands for Joint Test Action Group and is an interface standard (IEEE Std. 1149.1) used for programming and testing PLDs.
- An embedded processor is used to facilitate in-system programming of PLDs.
- CMOS is made with MOS field-effect transistors.
- Bipolar (TTL) is made with bipolar junction transistors.
- As a rule, CMOS has a lower power consumption than bipolar.

- VHDL and Verilog are hardware description languages used to describe a logic function for programming into a PLD.
- Half-splitting and signal tracing are two troubleshooting methods.

KEY TERMS

AND array An array of AND gates consisting of a matrix of programmable interconnections.

AND gate A logic gate that produces a HIGH output only when all of the inputs are HIGH.

Antifuse A type of PLD nonvolatile programmable link that can be left open or can be shorted once as directed by the program.

Boolean algebra The mathematics of logic circuits.

Complement The inverse or opposite of a number. In Boolean algebra, the inverse function, expressed with a bar over a variable. The complement of a 1 is 0, and vice versa.

EEPROM A type of nonvolatile PLD reprogrammable link based on electrically erasable programmable read-only memory cells and can be turned on or off repeatedly by programming.

EPROM A type of PLD nonvolatile programmable link based on electrically programmable read-only memory cells and can be turned either on or off once with programming.

Exclusive-NOR gate A logic gate that produces a LOW only when the two inputs are at opposite levels.

Exclusive-OR (XOR) gate A logic gate that produces a HIGH output only when its two inputs are at opposite levels.

Fan-out The number of equivalent gate inputs of the same family series that a logic gate can drive.

Flash A type of PLD nonvolatile reprogrammable link technology based on a single transistor cell.

Fuse A type of PLD nonvolatile programmable link that can be left shorted or can be opened once as directed by the program.

Inverter A logic circuit that inverts or complements its input.

JTAG Joint Test Action Group; an interface standard designated IEEE Std. 1149.1.

NAND gate A logic gate that produces a LOW output only when all the inputs are HIGH.

NOR gate A logic gate in which the output is LOW when one or more of the inputs are HIGH.

OR gate A logic gate that produces a HIGH output when one or more inputs are HIGH.

Propagation delay time The time interval between the occurrence of an input transition and the occurrence of the corresponding output transition in a logic circuit.

Product term The Boolean product of two or more literals equivalent to an AND operation.

SRAM A type of PLD volatile reprogrammable link based on static random-access memory cells and can be turned on or off repeatedly with programming.

Sum term The Boolean sum of two or more literals equivalent to an OR operation.

Target device A PLD mounted on a programming fixture or development board into which a software logic design is to be downloaded.

Timing diagram A diagram of waveforms showing the proper timing relationship of all the waveforms.

Truth table A table showing the inputs and corresponding output(s) of a logic circuit.

Unit load A measure of fan-out. One gate input represents one unit load to the output of a gate within the same IC family.

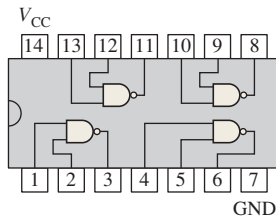
Variable A symbol used to represent an action, a condition, or data that can have a value of 1 or 0, usually designated by an italic letter or word.

Verilog A standard hardware description language that uses a module structure to describe a function.

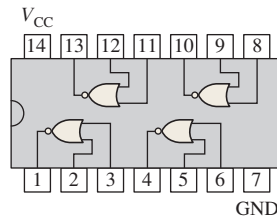
VHDL A standard hardware description language that describes a function with an entity/architecture structure.

FIXED-FUNCTION LOGIC DEVICES

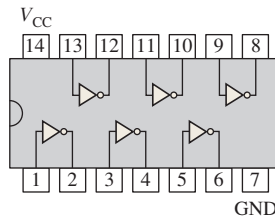
The diagrams shown are for CMOS and bipolar IC devices. The XX in each part number designates a particular IC family. For example, XX = HC stands for high-speed CMOS.



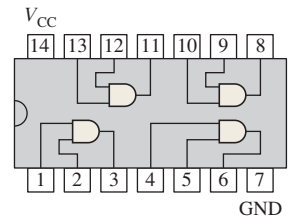
74XX00



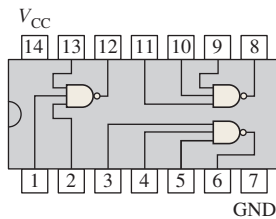
74XX02



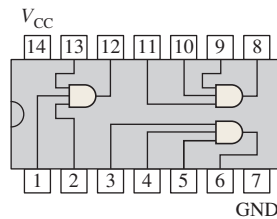
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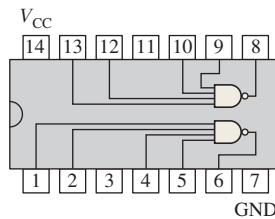
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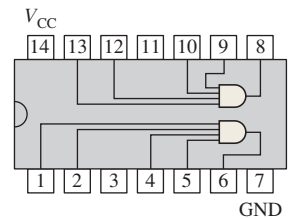
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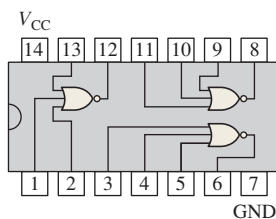
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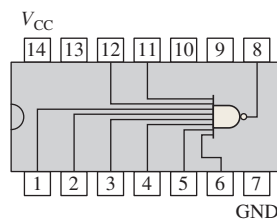
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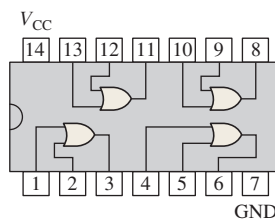
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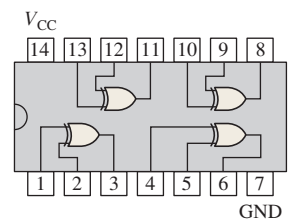
74XX27



74XX30



74XX32



74XX86

TRUE/FALSE QUIZ

Answers are at the end of the chapter.

1. An inverter performs the NOR operation.
2. An AND gate can have only two inputs.
3. If any input to an OR is 1, the output is 1.
4. If all inputs to an AND gate are 1, the output is 0.
5. A NAND gate has an output that is opposite the output of an AND gate.
6. A NOR gate can be considered as an OR gate followed by an inverter.
7. The output of an exclusive-OR is 0 if the inputs are opposite.
8. Two types of fixed-function logic integrated circuits are bipolar and NMOS.
9. BCD stands for binary coded decimal.
10. Fan-out is the number of similar gates that a given gate can drive.
11. Programmable logic devices are generally implemented with inverters.
12. VHDL is a type of programmable logic device.

SELF-TEST

Answers are at the end of the chapter.

1. Boolean addition represents the
 (a) inverter (b) AND gate (c) NOR gate (d) OR gate

2. Boolean multiplication represents the
 - (a) inverter
 - (b) AND gate
 - (c) NAND gate
 - (d) OR gate
3. The Boolean expression for a three-input AND gate is
 - (a) $A + B + C$
 - (b) $A + BC$
 - (c) ABC
 - (d) $ABC + ABC$
4. The output of an exclusive-OR gate is 1 when
 - (a) inputs are both 1
 - (b) the inputs are not the same
 - (c) the inputs are the same
 - (d) the inputs are both 0
5. When the input to an inverter is HIGH (1), the output is
 - (a) HIGH or 1
 - (b) LOW or 1
 - (c) HIGH or 0
 - (d) LOW or 0
6. An inverter performs an operation known as
 - (a) complementation
 - (b) assertion
 - (c) inversion
 - (d) both answers (a) and (c)
7. The output of an AND gate with inputs A , B , and C is a 1 (HIGH) when
 - (a) $A = 1, B = 1, C = 1$
 - (b) $A = 1, B = 0, C = 1$
 - (c) $A = 0, B = 0, C = 0$
8. The output of an OR gate with inputs A , B , and C is a 1 (HIGH) when
 - (a) $A = 1, B = 1, C = 1$
 - (b) $A = 0, B = 0, C = 1$
 - (c) $A = 0, B = 0, C = 0$
 - (d) answers (a), (b), and (c)
 - (e) only answers (a) and (b)
9. A pulse is applied to each input of a 2-input NAND gate. One pulse goes HIGH at $t = 0$ and goes back LOW at $t = 1$ ms. The other pulse goes HIGH at $t = 0.8$ ms and goes back LOW at $t = 3$ ms. The output pulse can be described as follows:
 - (a) It goes LOW at $t = 0$ and back HIGH at $t = 3$ ms.
 - (b) It goes LOW at $t = 0.8$ ms and back HIGH at $t = 3$ ms.
 - (c) It goes LOW at $t = 0.8$ ms and back HIGH at $t = 1$ ms.
 - (d) It goes LOW at $t = 0.8$ ms and back LOW at $t = 1$ ms.
10. A pulse is applied to each input of a 2-input NOR gate. One pulse goes HIGH at $t = 0$ and goes back LOW at $t = 1$ ms. The other pulse goes HIGH at $t = 0.8$ ms and goes back LOW at $t = 3$ ms. The output pulse can be described as follows:
 - (a) It goes LOW at $t = 0$ and back HIGH at $t = 3$ ms.
 - (b) It goes LOW at $t = 0.8$ ms and back HIGH at $t = 3$ ms.
 - (c) It goes LOW at $t = 0.8$ ms and back HIGH at $t = 1$ ms.
 - (d) It goes HIGH at $t = 0.8$ ms and back LOW at $t = 1$ ms.
11. A pulse is applied to each input of an exclusive-OR gate. One pulse goes HIGH at $t = 0$ and goes back LOW at $t = 1$ ms. The other pulse goes HIGH at $t = 0.8$ ms and goes back LOW at $t = 3$ ms. The output pulse can be described as follows:
 - (a) It goes HIGH at $t = 0$ and back LOW at $t = 3$ ms.
 - (b) It goes HIGH at $t = 0$ and back LOW at $t = 0.8$ ms.
 - (c) It goes HIGH at $t = 1$ ms and back LOW at $t = 3$ ms.
 - (d) both answers (b) and (c)
12. A positive-going pulse is applied to an inverter. The time interval from the leading edge of the input to the leading edge of the output is 7 ns. This parameter is
 - (a) speed-power product
 - (b) propagation delay, t_{PHL}
 - (c) propagation delay, t_{PLH}
 - (d) pulse width
13. The purpose of a programmable link in an AND array is to
 - (a) connect an input variable to a gate input
 - (b) connect a row to a column in the array matrix
 - (c) disconnect a row from a column in the array matrix
 - (d) do all of the above
14. The term OTP means
 - (a) open test point
 - (b) one-time programmable
 - (c) output test program
 - (d) output terminal positive
15. Types of PLD programmable link process technologies are
 - (a) antifuse
 - (b) flash
 - (c) ROM
 - (d) both (a) and (b)
 - (e) both (a) and (c)

16. A volatile programmable link technology is
 - (a) fuse
 - (b) EPROM
 - (c) SRAM
 - (d) EEPROM
17. Two ways to enter a logic design using PLD development software are
 - (a) text and numeric
 - (b) text and graphic
 - (c) graphic and coded
 - (d) compile and sort
18. JTAG stands for
 - (a) Joint Test Action Group
 - (b) Java Top Array Group
 - (c) Joint Test Array Group
 - (d) Joint Time Analysis Group
19. In-system programming of a PLD typically utilizes
 - (a) an embedded clock generator
 - (b) an embedded processor
 - (c) an embedded PROM
 - (d) both (a) and (b)
 - (e) both (b) and (c)
20. To measure the period of a pulse waveform, you must use
 - (a) a DMM
 - (b) a logic probe
 - (c) an oscilloscope
 - (d) a logic pulser
21. Once you measure the period of a pulse waveform, the frequency is found by
 - (a) using another setting
 - (b) measuring the duty cycle
 - (c) finding the reciprocal of the period
 - (d) using another type of instrument

PROBLEMS

Answers to odd-numbered problems are at the end of the chapter.

SECTION 1 Introduction to Boolean Algebra

1. Using Boolean notation, write an expression that is a 1 whenever one or more of its variables (A , B , C , and D) are 1s.
2. Write an expression that is a 1 only if all of its variables (A , B , C , D , and E) are 1s.
3. Write an expression that is a 1 when one or more of its variables (A , B , and C) are 0s.
4. Evaluate the following operations:
 - (a) $0 + 0 + 1$
 - (b) $1 + 1 + 1$
 - (c) $1 \cdot 0 \cdot 0$
 - (d) $1 \cdot 1 \cdot 1$
 - (e) $1 \cdot 0 \cdot 1$
 - (f) $1 \cdot 1 + 0 \cdot 1 \cdot 1$
5. Find the values of the variables that make each product term 1 and each sum term 0.
 - (a) AB
 - (b) \overline{ABC}
 - (c) $A + B$
 - (d) $\overline{A} + B + \overline{C}$
 - (e) $\overline{A} + \overline{B} + C$
 - (f) $\overline{A} + B$
 - (g) $\overline{AB} \overline{C}$
6. Find the value of X for all possible values of the variables.
 - (a) $X = (A + B)C + B$
 - (b) $X = (\overline{A} + \overline{B})C$
 - (c) $X = \overline{ABC} + AB$
 - (d) $X = (A + B)(\overline{A} + B)$
 - (e) $X = (A + BC)(\overline{B} + \overline{C})$
7. Identify the law of Boolean algebra upon which each of the following equalities is based:
 - (a) $\overline{AB} + CD + \overline{ACD} + B = B + \overline{AB} + \overline{ACD} + CD$
 - (b) $\overline{ABC}D + \overline{ABC} = D\overline{CBA} + \overline{CBA}$
 - (c) $AB(CD + \overline{EF} + GH) = ABCD + ABE\overline{F} + ABGH$
8. Identify the Boolean rule(s) on which each of the following equalities is based:
 - (a) $\overline{AB} + \overline{CD} + \overline{EF} = \overline{AB + CD + EF}$
 - (b) $A\overline{AB} + A\overline{BC} + A\overline{BB} = A\overline{BC}$
 - (c) $A(BC + \overline{BC}) + AC = A(BC) + AC$
 - (d) $AB(C + \overline{C}) + AC = AB + AC$
 - (e) $\overline{AB} + \overline{ABC} = \overline{AB}$
 - (f) $ABC + \overline{AB} + \overline{ABCD} = ABC + \overline{AB} + D$

SECTION 2 The Inverter

9. The input waveform shown in Figure 85 is applied to an inverter. Draw the timing diagram of the output waveform in proper relation to the input.



FIGURE 85

10. A network of cascaded inverters is shown in Figure 86. If a HIGH is applied to point A, determine the logic levels at points B through F.

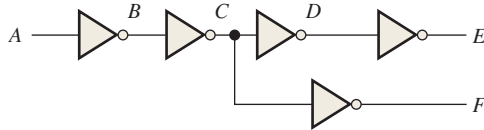


FIGURE 86

11. If the waveform in Figure 85 is applied to point A in Figure 86, determine the waveforms at points B through F.

SECTION 3 The AND Gate

12. Draw the rectangular outline symbol for a 4-input AND gate.
 13. Determine the output, X, for a 2-input AND gate with the input waveforms shown in Figure 87. Show the proper relationship of output to inputs with a timing diagram.

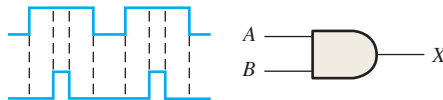


FIGURE 87

14. Repeat Problem 13 for the waveforms in Figure 88.

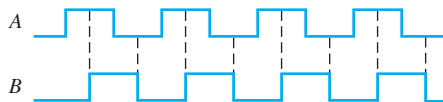


FIGURE 88

15. The input waveforms applied to a 3-input AND gate are as indicated in Figure 89. Show the output waveform in proper relation to the inputs with a timing diagram.

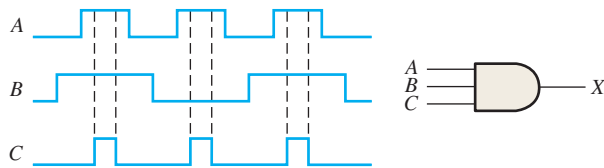


FIGURE 89

16. The input waveforms applied to a 4-input AND gate are as indicated in Figure 90. Show the output waveform in proper relation to the inputs with a timing diagram.

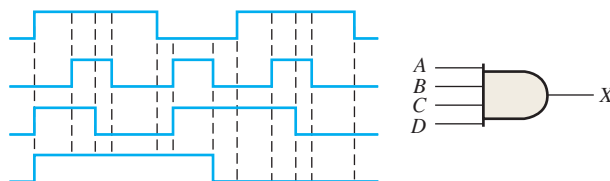


FIGURE 90

SECTION 4 The OR Gate

17. Determine the output for a 2-input OR gate when the input waveforms are as in Figure 88 and draw a timing diagram.
18. Repeat Problem 15 for a 3-input OR gate.
19. Repeat Problem 16 for a 4-input OR gate.
20. For the five input waveforms in Figure 91, determine the output if the five signals are ANDed. Determine the output if the five signals are ORed. Draw the timing diagram for each case.

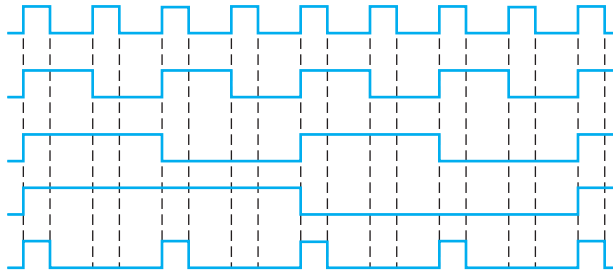


FIGURE 91

21. Draw the rectangular outline symbol for a 4-input OR gate.
22. Show the truth table for a 3-input OR gate.

SECTION 5 The NAND Gate

23. For the set of input waveforms in Figure 92, determine the output for the gate shown and draw the timing diagram.

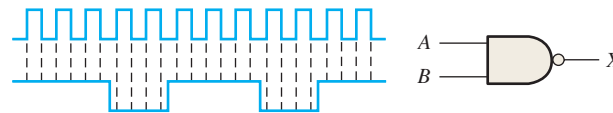


FIGURE 92

24. Determine the gate output for the input waveforms in Figure 93 and draw the timing diagram.

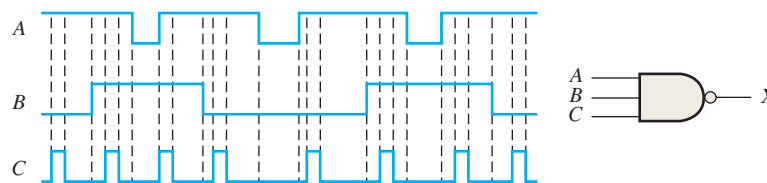


FIGURE 93

25. Determine the output waveform in Figure 94.

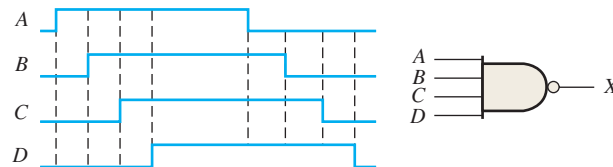


FIGURE 94

26. As you have learned, the two logic symbols shown in Figure 95 represent equivalent operations. The difference between the two is strictly from a functional viewpoint. For the NAND symbol, look for two HIGHS on the inputs to give a LOW output. For the negative-OR, look for at least one LOW on the inputs to give a HIGH on the output. Using these two functional viewpoints, show that each gate will produce the same output for the given inputs.

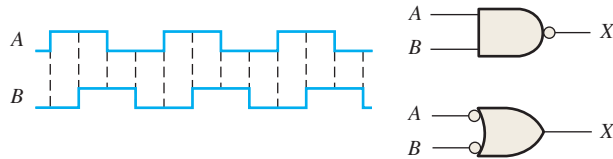


FIGURE 95

SECTION 6 The NOR Gate

- 27. Repeat Problem 23 for a 2-input NOR gate.
- 28. Determine the output waveform in Figure 96 and draw the timing diagram.

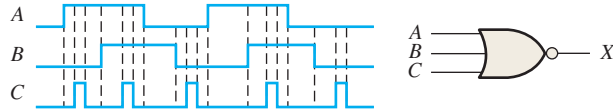


FIGURE 96

- 29. Repeat Problem 25 for a 4-input NOR gate.
- 30. The NAND and the negative-OR symbols represent equivalent operations, but they are functionally different. For the NOR symbol, look for at least one HIGH on the inputs to give a LOW on the output. For the negative-AND, look for two LOWs on the inputs to give a HIGH output. Using these two functional points of view, show that both gates in Figure 97 will produce the same output for the given inputs.

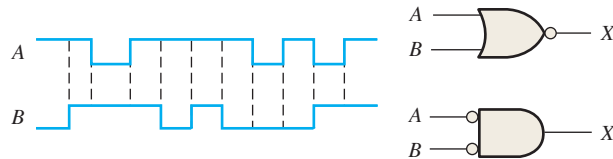


FIGURE 97

SECTION 7 The Exclusive-OR and Exclusive-NOR Gates

- 31. How does an exclusive-OR gate differ from an OR gate in its logical operation?
- 32. Repeat Problem 23 for an exclusive-OR gate.
- 33. Repeat Problem 23 for an exclusive-NOR gate.
- 34. Determine the output of an exclusive-OR gate for the inputs shown in Figure 88 and draw a timing diagram.

SECTION 8 Gate Performance Characteristics and Parameters

- 35. Determine t_{PLH} and t_{PHL} from the oscilloscope display in Figure 98. The readings indicate volts/div and sec/div for each channel.

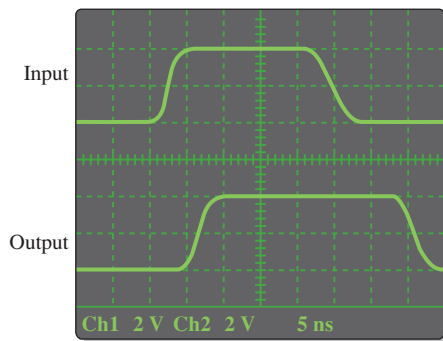


FIGURE 98

LOGIC GATES AND GATE COMBINATIONS

36. Gate A has $t_{PLH} = t_{PHL} = 6$ ns. Gate B has $t_{PLH} = t_{PHL} = 10$ ns. Which gate can be operated at a higher frequency?
37. If a logic gate operates on a dc supply voltage of +5 V and draws an average current of 4 mA, what is its power dissipation?
38. The variable I_{CCH} represents the dc supply current from V_{CC} when all outputs of an IC are HIGH. The variable I_{CCL} represents the dc supply current when all outputs are LOW. For a given 5 V IC with four NAND gates, what is the average power dissipation when all the gate outputs are HIGH for half the time and LOW for half the time? $I_{CCH} = 0.5$ mA and $I_{CCL} = 1$ mA.

SECTION 9 Programmable Logic

39. In the simple programmed AND array with programmable links in Figure 99, determine the Boolean output expressions.

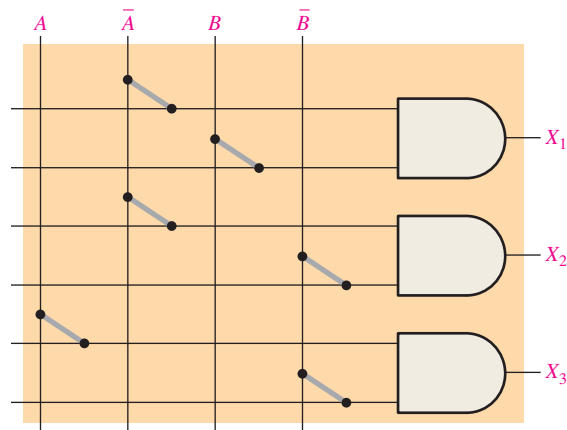


FIGURE 99

40. Determine by row and column number which fusible links must be blown in the programmable AND array of Figure 100 to implement each of the following product terms: $X_1 = \overline{A}BC$, $X_2 = ABC$, $X_3 = \overline{A}B\overline{C}$.

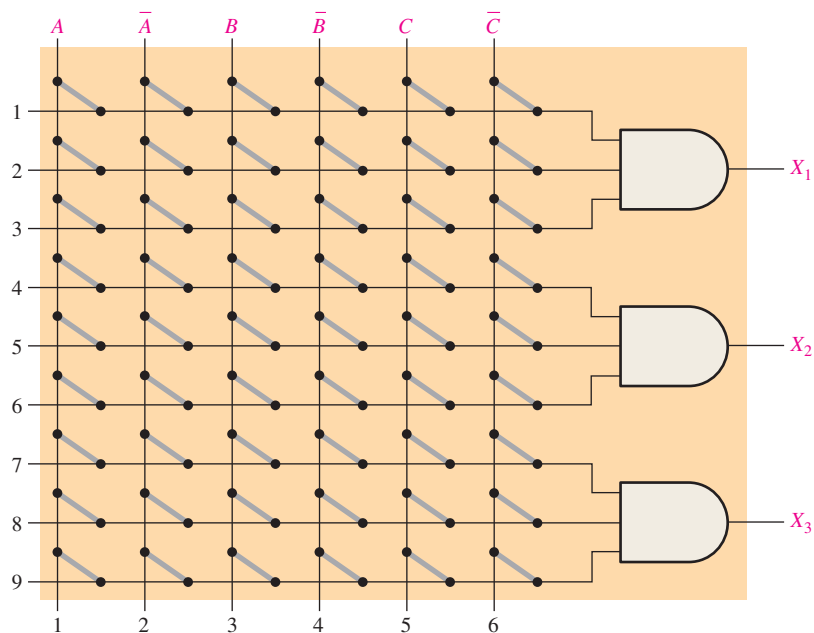


FIGURE 100

41. Describe a 4-input AND gate using VHDL.
42. Repeat Problem 41 using Verilog.
43. Describe a 5-input NOR gate using VHDL.
44. Repeat Problem 43 using Verilog.

SECTION 10 Troubleshooting

45. Define *troubleshooting*.
46. Explain the half-splitting method of troubleshooting.
47. Explain the signal-tracing method of troubleshooting.
48. Discuss signal substitution and injection.
49. Give some examples of the type of information that you look for when a system is reported to have failed.
50. If the symptom in a particular system is no output, name two possible general causes.
51. If the symptom of a particular system is an incorrect output, name two possible causes.
52. What obvious things should you look for before starting the troubleshooting process?
53. How would you isolate a fault in a system?
54. Name two common instruments used in troubleshooting.
55. Assume that you have isolated the problem down to a specific circuit board. What are your options at this point?

Special Problems

56. Sensors are used to monitor the pressure and the temperature of a chemical solution stored in a vat. The circuitry for each sensor produces a HIGH voltage when a specified maximum value is exceeded. An alarm requiring a LOW voltage input must be activated when either the pressure or the temperature is excessive. Develop a circuit for this application.
57. In a certain automated manufacturing process, electrical components are automatically inserted in a PC board. Before the insertion tool is activated, the PC board must be properly positioned, and the component to be inserted must be in the chamber. Each of these prerequisite conditions is indicated by a HIGH voltage. The insertion tool requires a LOW voltage to activate it. Develop a circuit to implement this process.
58. Modify the frequency counter in Figure 31 to operate with an enable pulse that is active-LOW rather than HIGH during the 1 ms interval.
59. Assume that the enable signal in Figure 31 has the waveform shown in Figure 101. Assume that waveform *B* is also available. Show how to produce an active-HIGH reset pulse to the counter only during the time that the enable signal is LOW.

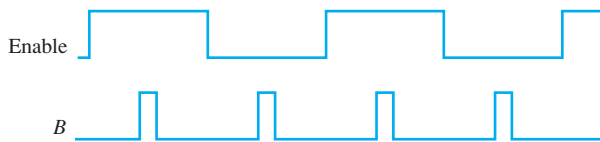


FIGURE 101

60. Develop a device to fit in the beige block of Figure 102 that will cause the headlights of an automobile to be turned off automatically 15 s after the ignition switch is turned off, if the light switch is left on. Assume that a LOW is required to turn the lights off.

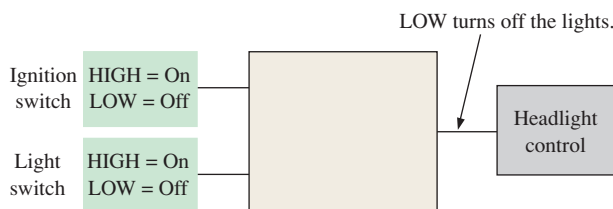


FIGURE 102

61. Modify the logic circuit for the intrusion alarm in Figure 39 so that two additional rooms, each with two windows and one door, can be protected.
62. Further modify the logic circuit from Problem 61 for a change in the input sensors where Open = LOW and Closed = HIGH.

MULTISIM



MULTISIM TROUBLESHOOTING PRACTICE

63. Open file P03-63, and follow the instructions given there.
64. Open file P03-64, and follow the instructions given there.
65. Open file P03-65, and follow the instructions given there.
66. Open file P03-66, and follow the instructions given there.

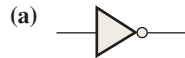
ANSWERS TO SECTION CHECKUPS

SECTION 1 Introduction to Boolean Algebra

1. $\bar{A} = \bar{0} = 1$
2. $A = 1, B = 1, C = 0; \bar{A} + \bar{B} + C = \bar{1} + \bar{1} + 0 = 0 + 0 + 0 = 0$
3. $A = 1, B = 0, C = 1; A\bar{B}C = 1 \cdot \bar{0} \cdot 1 = 1 \cdot 1 \cdot 1 = 1$
4. $A + (B + C + D) = (A + B + C) + D$
5. $A(B + C + D) = AB + AC + AD$

SECTION 2 The Inverter

1. When the inverter input is 1, the output is 0.



- (b) A negative-going pulse is on the output (HIGH to LOW and back HIGH).

SECTION 3 The AND Gate

1. An AND gate output is HIGH only when all inputs are HIGH.
2. An AND gate output is LOW when one or more inputs are LOW.
3. Five-input AND: $X = 1$ when $ABCDE = 11111$, and $X = 0$ for all other combinations of $ABCDE$.

SECTION 4 The OR Gate

1. An OR gate output is HIGH when one or more inputs are HIGH.
2. An OR gate output is LOW only when all inputs are LOW.
3. Three-input OR: $X = 0$ when $ABC = 000$, and $X = 1$ for all other combinations of ABC .

SECTION 5 The NAND Gate

1. A NAND output is LOW only when all inputs are HIGH.
2. A NAND output is HIGH when one or more inputs are LOW.
3. NAND: active-LOW output for all HIGH inputs; negative-OR: active-HIGH output for one or more LOW inputs. They have the same truth tables.
4. $X = \overline{ABC}$

SECTION 6 The NOR Gate

1. A NOR output is HIGH only when all inputs are LOW.
2. A NOR output is LOW when one or more inputs are HIGH.

3. NOR: active-LOW output for one or more HIGH inputs; negative-AND: active-HIGH output for all LOW inputs. They have the same truth tables.
4. $X = \overline{A + B + C}$

SECTION 7 The Exclusive-OR and Exclusive-NOR Gates

1. An XOR output is HIGH when the inputs are at opposite levels.
2. An XNOR output is HIGH when the inputs are at the same levels.
3. Apply the bits to the XOR inputs; when the output is HIGH, the bits are different.

SECTION 8 Gate Performance Characteristics and Parameters

1. Lowest power—CMOS
2. $t_{PLH} = 10 \text{ ns}$; $t_{PHL} = 8 \text{ ns}$
3. 18 pJ
4. I_{CCL} —dc supply current for LOW output state; I_{CCH} —dc supply current for HIGH output state
5. V_{IL} —LOW input voltage; V_{IH} —HIGH input voltage
6. V_{OL} —LOW output voltage; V_{OH} —HIGH output voltage

SECTION 9 Programmable Logic

1. Fuse, antifuse, EPROM, EEPROM, flash, and SRAM
2. Volatile means that all the data are lost when power is off and the PLD must be reprogrammed; SRAM-based
3. Text entry and graphic entry
4. JTAG is Joint Test Action Group; the IEEE Std. 1149.1 for programming and test interfacing.

5.

VHDL	Verilog
entity NORgate is	module NORgate (A, B, C, X);
port (A, B, C: in bit; X: out bit);	input A, B, C;
end entity NORgate;	output X;
architecture NORfunction of NORgate is	assign X = !(A B C);
begin	endmodule
X <= A nor B nor C;	
end architecture NORfunction;	

6.

VHDL	Verilog
entity XORgate is	module XORgate (A, B, X);
port (A, B: in bit; X: out bit);	input A, B;
end entity XORgate;	output X;
architecture XORfunction of XORgate is	assign X = (A && !B) (!A && B);
begin	endmodule
X <= A xor B;	
end architecture XORfunction;	

SECTION 10 Troubleshooting

1. Gather information, identify symptoms and possible causes, isolate point(s) of failure, apply proper tools to determine cause, and fix problem.
2. Half-splitting and signal tracing
3. Blown fuse, absence of DC power, loose connections, broken wires, loosely connected circuit board
4. Yes

ANSWERS TO RELATED PROBLEMS FOR EXAMPLES

- 1 $\bar{A} + B = 0$ when $A = 1$ and $B = 0$.
- 2 $\bar{A}\bar{B} = 1$ when $A = 0$ and $B = 0$.
- 3 The timing diagram is not affected.
- 4 See Table 18.

TABLE 18			
INPUTS	OUTPUT	INPUTS	OUTPUT
<i>ABCD</i>	<i>X</i>	<i>ABCD</i>	<i>X</i>
0000	0	1000	0
0001	0	1001	0
0010	0	1010	0
0011	0	1011	0
0100	0	1100	0
0101	0	1101	0
0110	0	1110	0
0111	0	1111	1

- 5 See Figure 103.

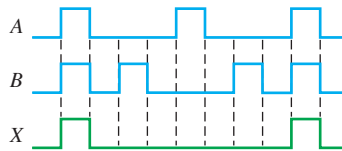


FIGURE 103

- 6 The output waveform is the same as input *A*.
- 7 See Figure 104.
- 8 Results are the same as example.
- 9 See Figure 105.

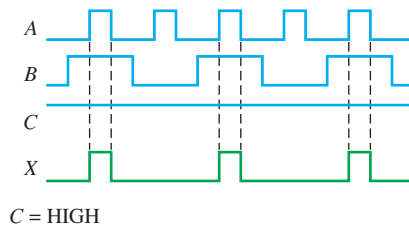


FIGURE 104

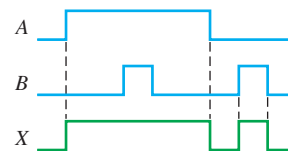


FIGURE 105

- 10 See Figure 106.
- 11 See Figure 107.

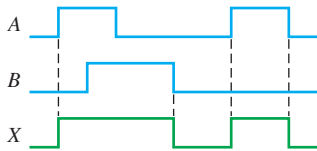


FIGURE 106

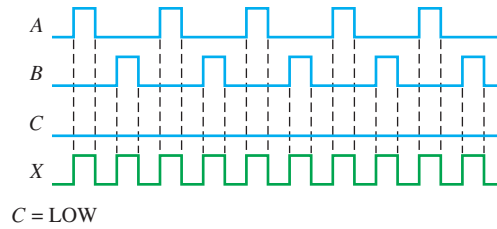


FIGURE 107

12 See Figure 108.

13 See Figure 109.

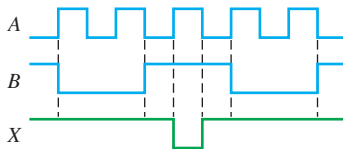


FIGURE 108

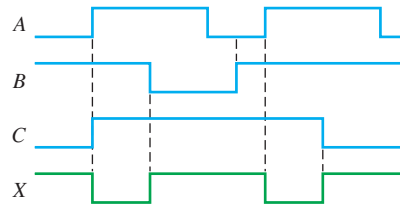


FIGURE 109

14 See Figure 110.

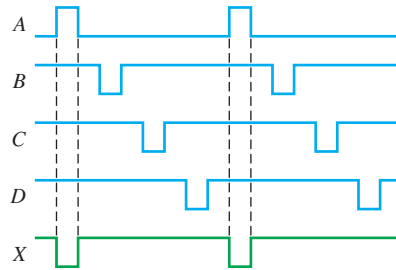


FIGURE 110

15 See Figure 111.

16 See Figure 112.

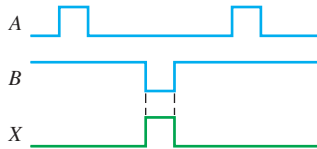


FIGURE 111

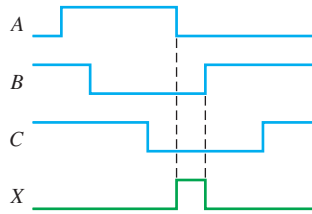


FIGURE 112

17 The output is always LOW. The output is a straight line.

18 The outputs are unaffected.

19 The gate with 4 ns t_{PLH} and t_{PHL} can operate at the highest frequency.

20 10 mW

21 6 columns, 9 rows, and 3 AND gates with three inputs each.

ANSWERS TO TRUE/FALSE QUIZ

1. F 2. F 3. T 4. F 5. T 6. T
 7. F 8. F 9. T 10. T 11. F 12. F

ANSWERS TO SELF-TEST

1. (d) 2. (b) 3. (c) 4. (b) 5. (d) 6. (d) 7. (a)
 8. (e) 9. (c) 10. (a) 11. (d) 12. (b) 13. (d) 14. (b)
 15. (d) 16. (c) 17. (b) 18. (a) 19. (d) 20. (c) 21. (c)

ANSWERS TO ODD-NUMBERED PROBLEMS

1. $X = A + B + C + D$
 3. $X = \bar{A} + \bar{B} + \bar{C}$
 5. (a) $AB = 1$ when $A = 1, B = 1$
 (b) $A\bar{B}C = 1$ when $A = 1, B = 0, C = 1$
 (c) $A + B = 0$ when $A = 0, B = 0$
 (d) $\bar{A} + B + \bar{C} = 0$ when $A = 1, B = 0, C = 1$
 (e) $\bar{A} + \bar{B} + C = 0$ when $A = 1, B = 1, C = 0$
 (f) $\bar{A} + B = 0$ when $A = 1, B = 0$
 (g) $\bar{A}\bar{B}\bar{C} = 1$ when $A = 1, B = 0, C = 0$
 7. (a) Commutative (b) Commutative (c) Distributive
 9. See Figure P-1.

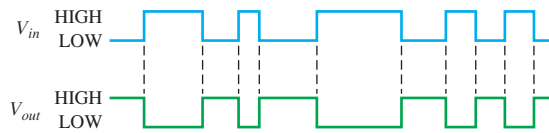


FIGURE P-1

11. See Figure P-2.

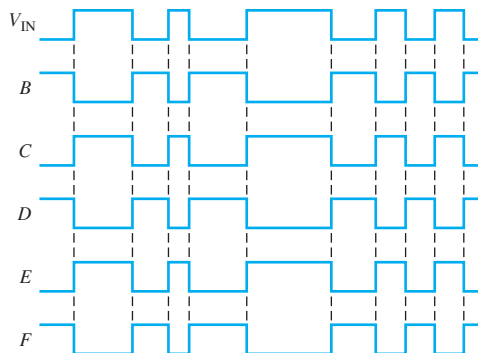


FIGURE P-2

13. See Figure P-3.

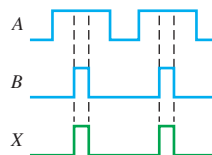


FIGURE P-3

15. See Figure P-4.

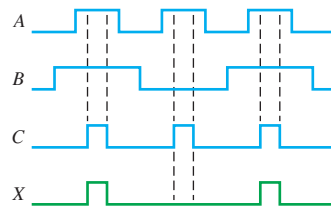


FIGURE P-4

17. See Figure P-5.

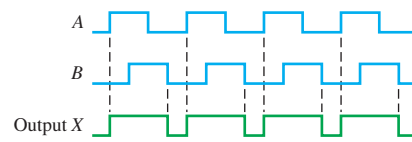


FIGURE P-5

19. See Figure P-6.

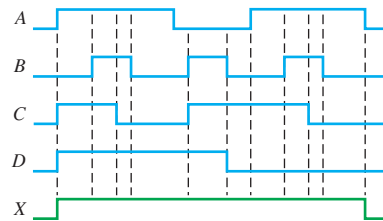


FIGURE P-6

21. See Figure P-7.

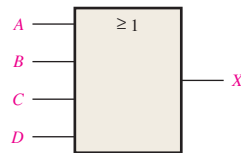


FIGURE P-7

23. See Figure P-8.

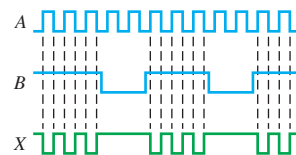


FIGURE P-8

25. See Figure P-9.

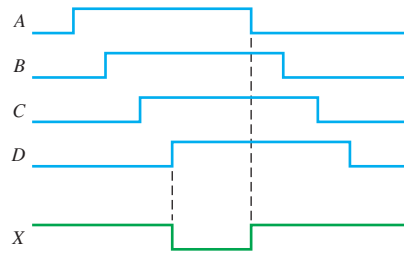


FIGURE P-9

27. See Figure P-10.

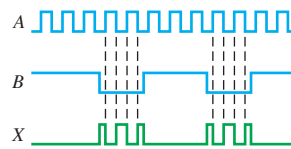


FIGURE P-10

29. See Figure P-11.

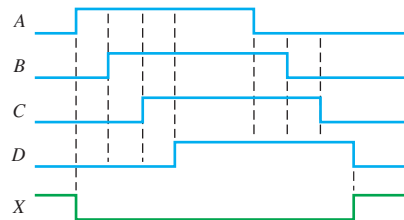


FIGURE P-11

31. $XOR = A\bar{B} + \bar{A}B$; $OR = A + B$

33. See Figure P-12.

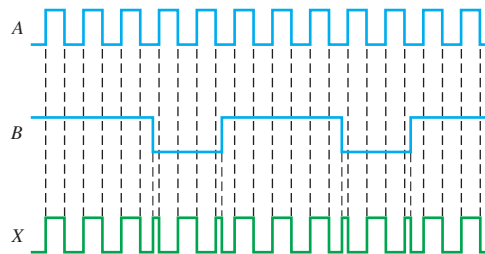


FIGURE P-12

35. $t_{PLH} = 4.3$ ns; $t_{PHL} = 10.5$ ns

37. 20 mW

39. $X_1 = \bar{A}B$, $X_2 = \bar{A}\bar{B}$, $X_3 = A\bar{B}$.

41. entity ANDgate is

port (A, B, C, D: in bit; X: out bit);

end entity ANDgate;

architecture ANDfunction of ANDgate is

begin

X <= A and B and C and D;

end architecture ANDfunction;

43. **entity** NORgate is

port (A, B, C, D, E: **in** bit; X: **out** bit);

end entity NORgate;

architecture NORfunction of NORgate is

begin

X <= not(A or B or C or D or E);

end architecture NORfunction;

- 45. Troubleshooting is the process of recognizing, isolating, and correcting a fault or failure in a system.
- 47. In the signal-tracing method, a signal is tracked as it progresses through a system until a point is found where the signal disappears or is incorrect.
- 49. When a failure is reported, determine when and how it failed and what are the symptoms.
- 51. An incorrect output can be caused by an incorrect dc supply voltage, improper ground, incorrect component value, or a faulty component.
- 53. To isolate a fault in a system, apply half-splitting or signal tracing.
- 55. When a fault has been isolated to a particular circuit board, the options are to repair the board or replace the board with a known good board.
- 57. See Figure P–13.

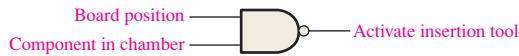


FIGURE P-13

59. See Figure P–14.

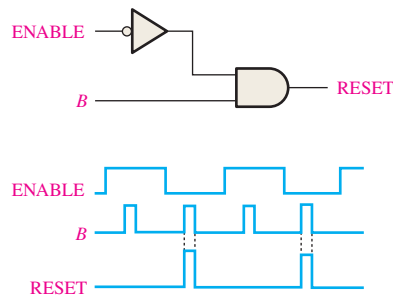


FIGURE P-14

61. See Figure P–15.

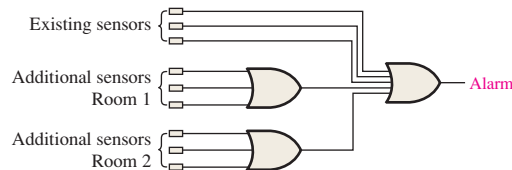


FIGURE P-15

LOGIC GATES AND GATE COMBINATIONS

63. **Circuit fault:** Input B of AND gate U1 shorted to ground.
Predicted effect of fault: Output X is always LOW.
Observed effect of introduced fault: Output X is always LOW.
65. **Observed operation:** Output X is LOW whenever input B is HIGH.
Suspected fault: Input A of NOR gate shorted to ground.
Effect of introduced fault: Output X is LOW whenever B is HIGH.

COMBINATIONAL LOGIC

OUTLINE

- 1 Basic Combinational Logic Circuits
- 2 Boolean Expressions and Truth Tables
- 3 DeMorgan's Theorems
- 4 The Universal Property of NAND and NOR Gates
- 5 Pulse Waveform Operation
- 6 Combinational Logic with VHDL and Verilog
- 7 A System
- 8 Troubleshooting

OBJECTIVES

- Study the operation of basic combinational logic circuits, such as AND-OR, AND-OR-Invert, exclusive-OR, and exclusive-NOR
- Write the Boolean output expression for any combinational logic circuit
- Develop a truth table from the output expression for a combinational logic circuit
- Apply DeMorgan's theorems to Boolean expressions
- Develop a combinational logic circuit for a given Boolean output expression
- Develop a combinational logic circuit for a given truth table
- Use NAND gates to implement any combinational logic function
- Use NOR gates to implement any combinational logic function
- Write VHDL and Verilog programs for simple logic circuits

- Apply combinational logic to a system application
- Troubleshoot faulty logic circuits
- Troubleshoot logic circuits by using signal tracing and waveform analysis

KEY TERMS

SOP	Signal
POS	Node
Universal gate	Signal tracing
Component	

INTRODUCTION

In this chapter, you will be introduced to SOP and POS implementations, which are basic forms of combinational logic. When logic gates are connected together to produce a specified output for certain specified combinations of input variables, with no storage involved, the resulting circuit is in the category of **combinational logic**.^{*} In combinational logic, the output level is at all times dependent on the combination of input levels. This chapter expands on the material introduced in earlier chapters with a coverage of the operation, implementation, and troubleshooting of various combinational logic circuits. The VHDL structural approach is introduced and applied to combinational logic. Corresponding Verilog programs are also covered.

VISIT THE WEBSITE

Study aids for this chapter are available at <http://pearsonhighered.com/floyd>

^{*}The bold terms in color are key terms and are included in a Key Term glossary at the end of the chapter.

1 BASIC COMBINATIONAL LOGIC CIRCUITS

Sum-of-product (SOP) expressions are implemented with an AND gate for each product term and one OR gate for summing all of the product terms. The SOP implementation is called AND-OR logic and is the basic form for realizing standard Boolean functions. In this section, the AND-OR and the AND-OR-Invert are examined; the exclusive-OR and exclusive-NOR gates, which are actually a form of AND-OR logic, are also covered.

After completing this section, you should be able to

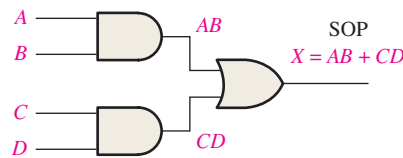
- Describe the operation of AND-OR and AND-OR-Invert circuits
- Describe the operation of exclusive-OR and exclusive-NOR gates

AND-OR Logic

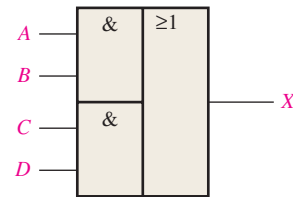
Figure 1(a) shows an AND-OR circuit using ANSI standard distinctive shape symbols consisting of two 2-input AND gates and one 2-input OR gate; Figure 1(b) is the ANSI standard rectangular outline symbol.

FIGURE 1 An example of AND-OR logic. Open file F04-01 to verify the operation.

MULTISIM



(a) Logic diagram (ANSI standard distinctive shape symbols)



(b) ANSI standard rectangular outline symbol

TABLE 1 • Truth table for the AND-OR logic in Figure 1.

INPUTS						OUTPUT
A	B	C	D	AB	CD	X
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	0	1	0	0	0	0
0	0	1	1	0	1	1
0	1	0	0	0	0	0
0	1	0	1	0	0	0
0	1	1	0	0	0	0
0	1	1	1	0	1	1
1	0	0	0	0	0	0
1	0	0	1	0	0	0
1	0	1	0	0	0	0
1	0	1	1	0	1	1
1	1	0	0	1	0	1
1	1	0	1	1	0	1
1	1	1	0	1	0	1
1	1	1	1	1	1	1

The truth table for a 4-input AND-OR logic circuit is shown in Table 1. The intermediate AND gate outputs (the AB and CD columns) are also shown in the table. The operation of the AND-OR circuit in Figure 1 is stated as follows:

For a 4-input AND-OR logic circuit, the output X is HIGH (1) if both input A and input B are HIGH (1) or both input C and input D are HIGH (1).

The term **SOP** shown above the output expression in Figure 1 stands for sum-of-products. The AND operation is Boolean multiplication, so when two or more variables are ANDed together, the result is a product. AB and CD are Boolean product terms. Also the OR operation is Boolean addition. When these two product terms are ORed together, the result is Boolean addition. Therefore, the expression $X = AB + CD$ is a sum-of-products (SOP), which is a standard form. An SOP expression can have any number of AND (product) terms ORed together.

AND-OR logic produces an SOP expression.

SYSTEM EXAMPLE 1

STORAGE TANK MONITOR

In a certain chemical-processing plant, a liquid chemical is used in a manufacturing process. The chemical is stored in three different tanks. A level sensor in each tank produces a HIGH voltage when the level of chemical in the tank drops below a specified point. The circuit monitors the chemical level in each tank and indicates when the level in any two of the tanks drops below the specified point.

The AND-OR circuit in Figure 2 has inputs from the sensors on tanks A , B , and C as shown. The AND gate G_1 checks the levels in tanks A and B , gate G_2 checks tanks A and C , and gate G_3 checks tanks B and C . When the chemical level in any two of the tanks gets too low, one of the AND gates will have HIGHS on both of its inputs, causing its output to be HIGH; and so the final output X from the OR gate is HIGH. This HIGH input is then used to activate an indicator such as a lamp or audible alarm, as shown in the figure.

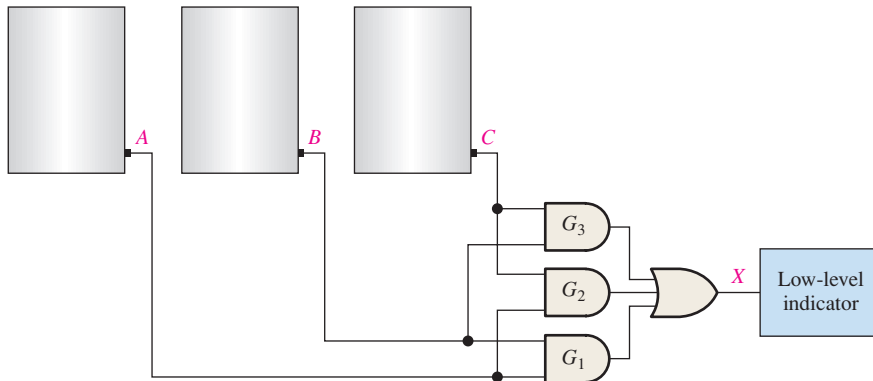
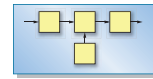


FIGURE 2

AND-OR-Invert Logic

When the output of an AND-OR circuit is complemented (inverted), it results in an AND-OR-Invert circuit. AND-OR logic directly implements SOP expressions. Product-of-sum (POS) expressions can be implemented with AND-OR-Invert logic. This is illustrated as follows, by developing the corresponding AND-OR-Invert (AOI) expression.

$$X = (\bar{A} + \bar{B})(\bar{C} + \bar{D}) = (\overline{AB})(\overline{CD}) = \overline{\overline{AB}}(\overline{CD}) = \overline{\overline{AB}} + \overline{\overline{CD}} = \overline{AB} + \overline{CD}$$

The logic diagram in Figure 3(a) shows an AND-OR-Invert circuit with four inputs. The ANSI standard rectangular outline symbol is shown in part (b).

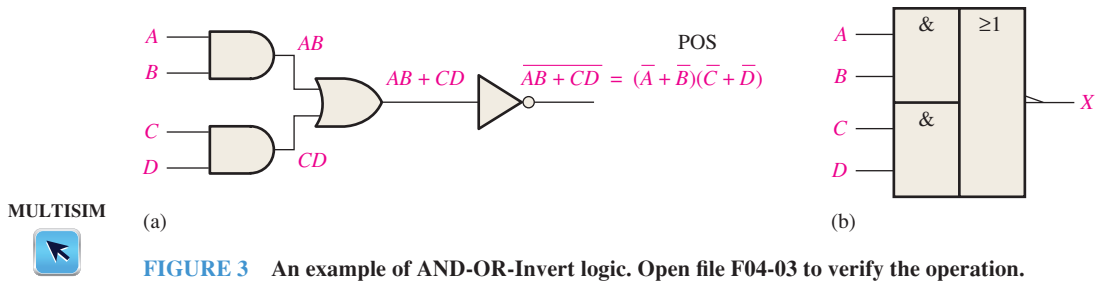


FIGURE 3 An example of AND-OR-Invert logic. Open file F04-03 to verify the operation.

The operation of the AND-OR-Invert circuit in Figure 3 is stated as follows:

For a 4-input AND-OR-Invert logic circuit, the output X is LOW (0) if both input A and input B are HIGH (1) or both input C and input D are HIGH (1).

A truth table can be developed from the AND-OR truth table in Table 1 by simply changing all 1s to 0s and all 0s to 1s in the output column.

The term **POS** shown above the output expression in Figure 3 (a) stands for product-of-sums. The OR operation is Boolean addition, so when two or more variables are ORED together, the result is a sum. $\bar{A} + \bar{B}$ and $\bar{C} + \bar{D}$ are Boolean sum terms. Also the AND operation is Boolean multiplication. When these two sum terms are ANDed together, the result is Boolean multiplication. Therefore, the expression $(\bar{A} + \bar{B})(\bar{C} + \bar{D})$ is a product-of-sums (POS), which is a standard form. A POS expression can have any number of OR (sum) terms ANDed together.

Exclusive-OR Logic

The XOR gate is actually a combination of other gates.

Although, because of the importance of exclusive-OR gate, this circuit is considered a type of logic gate with its own unique symbol, it is actually a combination of two AND gates, one OR gate, and two inverters, as shown in Figure 4(a). The two ANSI standard exclusive-OR logic symbols are shown in parts (b) and (c).

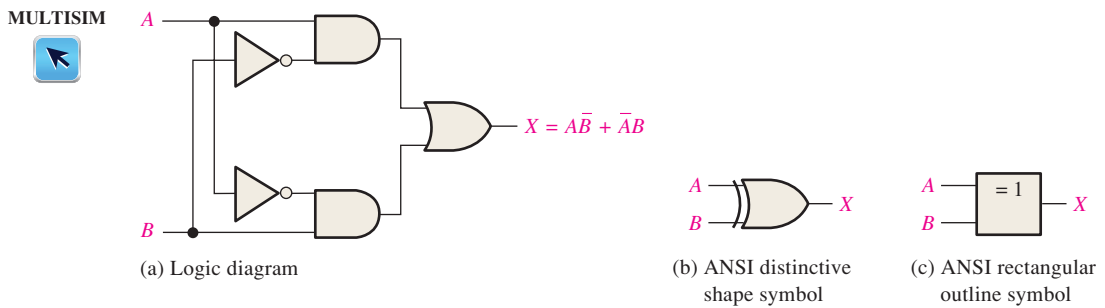


FIGURE 4 Exclusive-OR logic diagram and symbols. Open file F04-04 to verify the operation.

The output expression for the circuit in Figure 4 is

$$X = \bar{A}B + A\bar{B}$$

Evaluation of this expression results in the truth table in Table 2. Notice that the output is HIGH only when the two inputs are at opposite levels. A special exclusive-OR operator \oplus is often used, so the expression $X = \bar{A}B + A\bar{B}$ can be stated as “X is equal to A exclusive-OR B” and can be written as

$$X = A \oplus B$$

TABLE 2 • Truth table for an exclusive-OR.		
A	B	X
0	0	0
0	1	1
1	0	1
1	1	0

Exclusive-NOR Logic

As you know, the complement of the exclusive-OR function is the exclusive-NOR, which is derived as follows:

$$X = \overline{AB} + \overline{\overline{AB}} = \overline{(AB)(\overline{AB})} = \overline{(A + B)(A + \overline{B})} = \overline{A\overline{B}} + AB$$

Notice that the output X is HIGH only when the two inputs, A and B , are at the same level.

The exclusive-NOR can be implemented by simply inverting the output of an exclusive-OR, as shown in Figure 5(a), or by directly implementing the expression $\overline{A\overline{B}} + AB$, as shown in part (b).

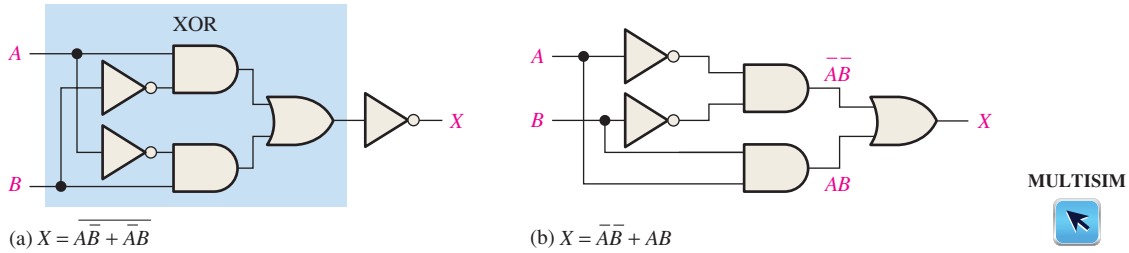


FIGURE 5 Two equivalent ways of implementing the exclusive-NOR. Open files F04-05 (a) and (b) to verify the operation.

SYSTEM EXAMPLE 2

DATA TRANSMISSION WITH ERROR DETECTION

A certain data transmission system uses exclusive-OR gates to implement even-parity generation and checking to detect an error in a 4-bit code. A parity bit is added to a binary code in order to provide error detection. For even parity, a parity bit is added to the original code to make the total number of 1s in the code even.

The parity generator circuit in Figure 6 produces a 1 output when there is an odd number of 1s on the inputs in order to make the total number of 1s in the output code even.

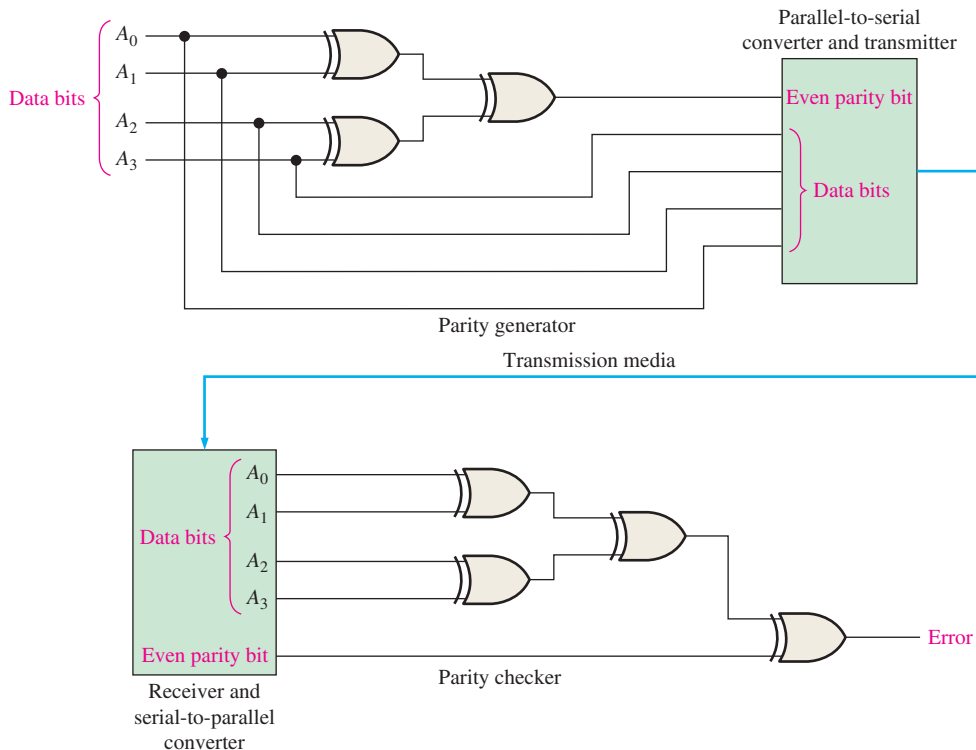


FIGURE 6

A 0 output is produced when there is an even number of 1s on the inputs. A total of five bits is converted to serial form and transmitted. At the receiving end, the transmitted code is converted back to parallel form. The parity checker produces a 1 output when there is an error in the five-bit code and a 0 when there is no error.

SECTION 1 CHECKUP*

- Determine the output (1 or 0) of a 4-variable AND-OR-Invert circuit for each of the following input conditions:
 - $A = 1, B = 0, C = 1, D = 0$
 - $A = 1, B = 1, C = 0, D = 1$
 - $A = 0, B = 1, C = 1, D = 1$
- Determine the output (1 or 0) of an exclusive-OR gate for each of the following input conditions:
 - $A = 1, B = 0$
 - $A = 1, B = 1$
- Develop the truth table for a certain 3-input logic circuit with the output expression $X = \overline{A}BC + \overline{A}BC + \overline{A}\overline{B}\overline{C} + ABC + ABC$.
- Draw the logic diagram for an exclusive-NOR circuit.

*Answers are at the end of the chapter.

2 BOOLEAN EXPRESSIONS AND TRUTH TABLES

In this section, examples are used to illustrate how to develop a logic circuit from a Boolean expression or a truth table.

After completing this section, you should be able to

- Develop a logic circuit from a Boolean expression
- Develop a logic circuit from a truth table

From a Boolean Expression to a Logic Circuit

For every Boolean expression there is a logic circuit, and for every logic circuit there is a Boolean expression.

Let's examine the following Boolean expression:

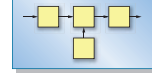
$$X = AB + CDE$$

A brief inspection shows that this expression is composed of two terms, AB and CDE , with a **domain** of five variables. The first term is formed by ANDing A with B , and the second term is formed by ANDing C , D , and E . The two terms are then ORed to form the output X . These operations are indicated in the structure of the expression as follows:

$$X = \overbrace{AB}^{\text{AND}} + \overbrace{CDE}^{\text{AND}} \quad \text{OR}$$

Many control programs require logic operations to be performed by a computer. A driver program is a control program that is used with computer peripherals. For example, a mouse driver requires logic tests to determine if a button has been pressed and further logic operations to determine if it has moved, either horizontally or vertically. Within the heart of a microprocessor is the arithmetic logic unit (ALU), which performs these logic operations as directed by program instructions. All of the logic described in this chapter can also be performed by the ALU, given the proper instructions.

SYSTEM NOTE



Note that in this particular expression, the AND operations forming the two individual terms, AB and CDE , must be performed *before* the terms can be ORed.

To implement this Boolean expression, a 2-input AND gate is required to form the term AB , and a 3-input AND gate is needed to form the term CDE . A 2-input OR gate is then required to combine the two AND terms. The resulting logic circuit is shown in Figure 7.

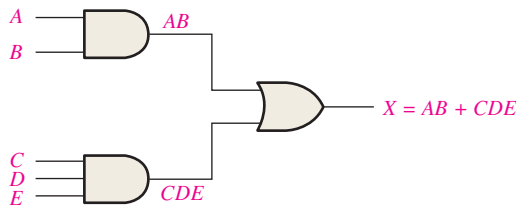
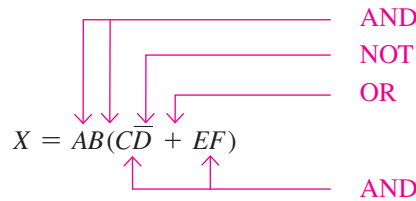


FIGURE 7 Logic circuit for $X = AB + CDE$.

As another example, let's implement the following expression:

$$X = AB(C\bar{D} + EF)$$

A breakdown of this expression shows that the terms AB and $(C\bar{D} + EF)$ are ANDed. The term $C\bar{D} + EF$ is formed by first ANDing C and \bar{D} and ANDing E and F , and then ORing these two terms. This structure is indicated in relation to the expression as follows:



Before you can implement the final expression, you must create the sum term $C\bar{D} + EF$; but before you can get this term; you must create the product terms $C\bar{D}$ and EF ; but before you can get the term $C\bar{D}$, you must create \bar{D} . So, as you can see, the logic operations must be done in the proper order.

The logic gates required to implement $X = AB(C\bar{D} + EF)$ are as follows:

1. One inverter to form \bar{D}
2. Two 2-input AND gates to form $C\bar{D}$ and EF
3. One 2-input OR gate to form $C\bar{D} + EF$
4. One 3-input AND gate to form X

The logic circuit for this expression is shown in Figure 8(a). Notice that there is a maximum of four gates and an inverter between an input and output in this circuit (from input D to output). Often the total propagation delay time through a logic circuit is a major consideration. Propagation delays are additive, so the more gates or inverters between input and output, the greater the propagation delay time.

COMBINATIONAL LOGIC

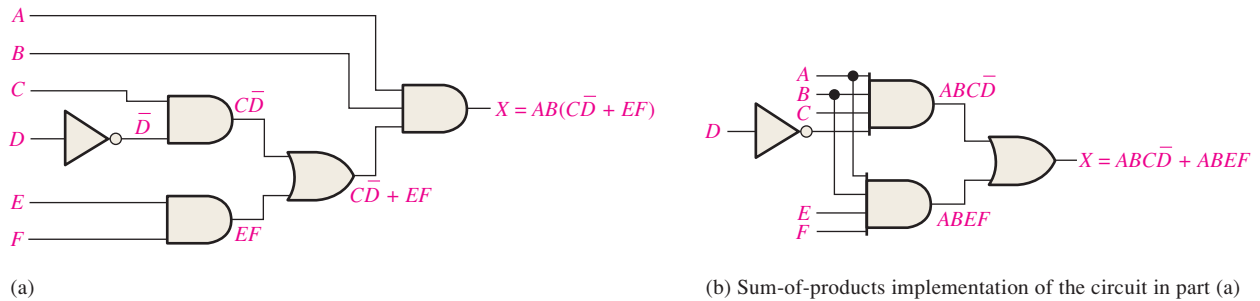


FIGURE 8 Logic circuits for $X = AB(\overline{CD} + EF) = ABC\overline{D} + ABEF$.

Unless an intermediate term, such as $\overline{CD} + EF$ in Figure 8(a), is required as an output for some other purpose, it is usually best to reduce a circuit to its SOP form in order to reduce the overall propagation delay time. The expression is converted to SOP as follows, and the resulting circuit is shown in Figure 8(b).

$$AB(\overline{CD} + EF) = ABC\overline{D} + ABEF$$

From a Truth Table to a Logic Circuit

If you begin with a truth table instead of an expression, you can write the SOP expression from the truth table and then implement the logic circuit. Table 3 specifies a logic function.

TABLE 3				
INPUTS			OUTPUT	PRODUCT TERM
A	B	C	X	
0	0	0	0	
0	0	1	0	
0	1	0	0	
0	1	1	1	$\overline{A}BC$
1	0	0	1	$A\overline{B}\overline{C}$
1	0	1	0	
1	1	0	0	
1	1	1	0	

The Boolean SOP expression obtained from the truth table by ORing the product terms for which $X = 1$ is

$$X = \overline{A}BC + A\overline{B}\overline{C}$$

The first term in the expression is formed by ANDing the three variables \overline{A} , B , and C . The second term is formed by ANDing the three variables A , \overline{B} , and \overline{C} .

The logic gates required to implement this expression are as follows: three inverters to form the \overline{A} , \overline{B} , and \overline{C} variables; two 3-input AND gates to form the terms $\overline{A}BC$ and $A\overline{B}\overline{C}$; and one 2-input OR gate to form the final output function, $\overline{A}BC + A\overline{B}\overline{C}$.

The implementation of this logic function is illustrated in Figure 9.

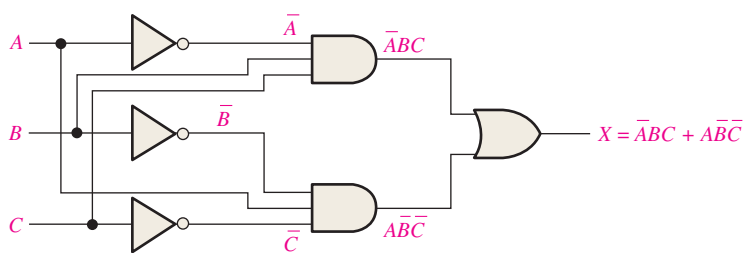


FIGURE 9 Logic circuit for $X = \bar{A}BC + A\bar{B}C$. Open file F04-09 to verify the operation.

MULTISIM



EXAMPLE 1

Develop the logic circuit for the operation specified in the truth table of Table 4.

TABLE 4				
INPUTS			OUTPUT	PRODUCT TERM
A	B	C	X	
0	0	0	0	
0	0	1	0	
0	1	0	0	
0	1	1	1	$\bar{A}BC$
1	0	0	0	
1	0	1	1	$A\bar{B}C$
1	1	0	1	$ABC\bar{C}$
1	1	1	0	

SOLUTION

Notice that $X = 1$ for only three of the input conditions. Therefore, the logic expression is

$$X = \bar{A}BC + A\bar{B}C + ABC\bar{C}$$

The logic gates required are three inverters, three 3-input AND gates and one 3-input OR gate. The logic circuit is shown in Figure 10.

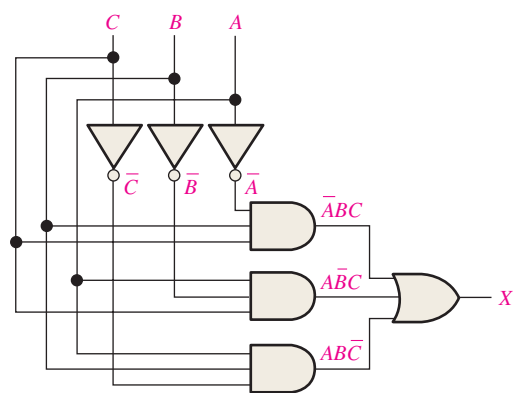


FIGURE 10 Open file F04-10 to verify the operation.

MULTISIM



RELATED PROBLEM*

If there were no complemented variables in the Boolean expression for the logic circuit of Figure 10, what would be the resulting circuit?

*Answers are at the end of the chapter.

EXAMPLE 2

Develop a logic circuit with four input variables that will only produce a 1 output when exactly three input variables are 1s.

SOLUTION

Out of sixteen possible combinations of four variables, the combinations in which there are exactly three 1s are listed in Table 5, along with the corresponding product term for each.

TABLE 5				
A	B	C	D	PRODUCT TERM
0	1	1	1	$\bar{A}BCD$
1	0	1	1	$A\bar{B}CD$
1	1	0	1	$AB\bar{C}D$
1	1	1	0	$ABC\bar{D}$

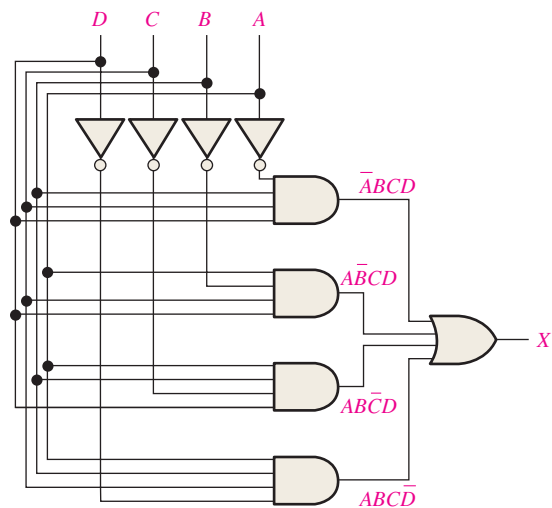
The product terms are ORed to get the following expression:

$$X = \bar{A}BCD + A\bar{B}CD + AB\bar{C}D + ABC\bar{D}$$

This expression is implemented in Figure 11 with AND-OR logic.

FIGURE 11 Open file F04-11 to verify the operation.

MULTISIM



RELATED PROBLEM

Show that the four cases in Table 5 are the only times there are three and only three 1s in the code.

Constructing a Truth Table for a Logic Circuit

Once you have determined the Boolean expression for a given logic circuit, you can develop a truth table that shows the output for all possible values of the input variables. The procedure requires that you evaluate the Boolean expression for all possible combinations of values for the input variables. In the case of the circuit in Figure 12, there are four input variables (*A*, *B*, *C*, and *D*) and therefore sixteen ($2^4 = 16$) combinations of values are possible.

A combinational logic circuit can be described by a truth table.

EVALUATING THE EXPRESSION To evaluate the expression $A(B + CD)$, first find the values of the variables that make the expression equal to 1, using the rules for Boolean addition and multiplication. In this case, the expression equals 1 only if $A = 1$ and $B + CD = 1$ because

$$A(B + CD) = 1 \cdot 1 = 1$$

Now determine when the $B + CD$ term equals 1. The term $B + CD = 1$ if either $B = 1$ or $CD = 1$ or if both B and CD equal 1 because

$$\begin{aligned} B + CD &= 1 + 0 = 1 \\ B + CD &= 0 + 1 = 1 \\ B + CD &= 1 + 1 = 1 \end{aligned}$$

The term $CD = 1$ only if $C = 1$ and $D = 1$.

To summarize, the expression $A(B + CD) = 1$ when $A = 1$ and $B = 1$ regardless of the values of C and D or when $A = 1$ and $C = 1$ and $D = 1$ regardless of the value of B . The expression $A(B + CD) = 0$ for all other value combinations of the variables.

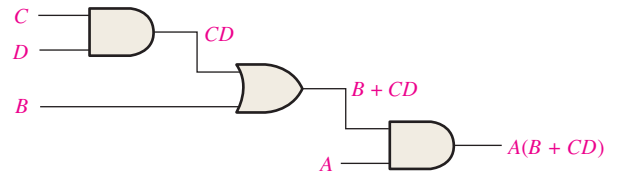


FIGURE 12 A combinational logic circuit showing the development of the Boolean expression for the output.

PUTTING THE RESULTS IN TRUTH TABLE FORMAT The first step is to list the sixteen input variable combinations of 1s and 0s in a binary sequence as shown in Table 6. Next, place a 1 in the output column for each combination of input variables that was determined in the evaluation. Finally, place a 0 in the output column for all other combinations of input variables. These results are shown in the truth table in Table 6.

TABLE 6 • Truth table for the logic circuit in Figure 12.				
A	INPUTS			OUTPUT $A(B + CD)$
	B	C	D	
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

EXAMPLE 3

Use Multisim to generate the truth table for the logic circuit in Figure 12.

SOLUTION

Construct the circuit in Multisim and connect the Multisim Logic Converter to the inputs and output, as shown in Figure 13. Click on the $\Rightarrow \rightarrow \overline{101}$ conversion bar, and the truth table appears in the display as shown.

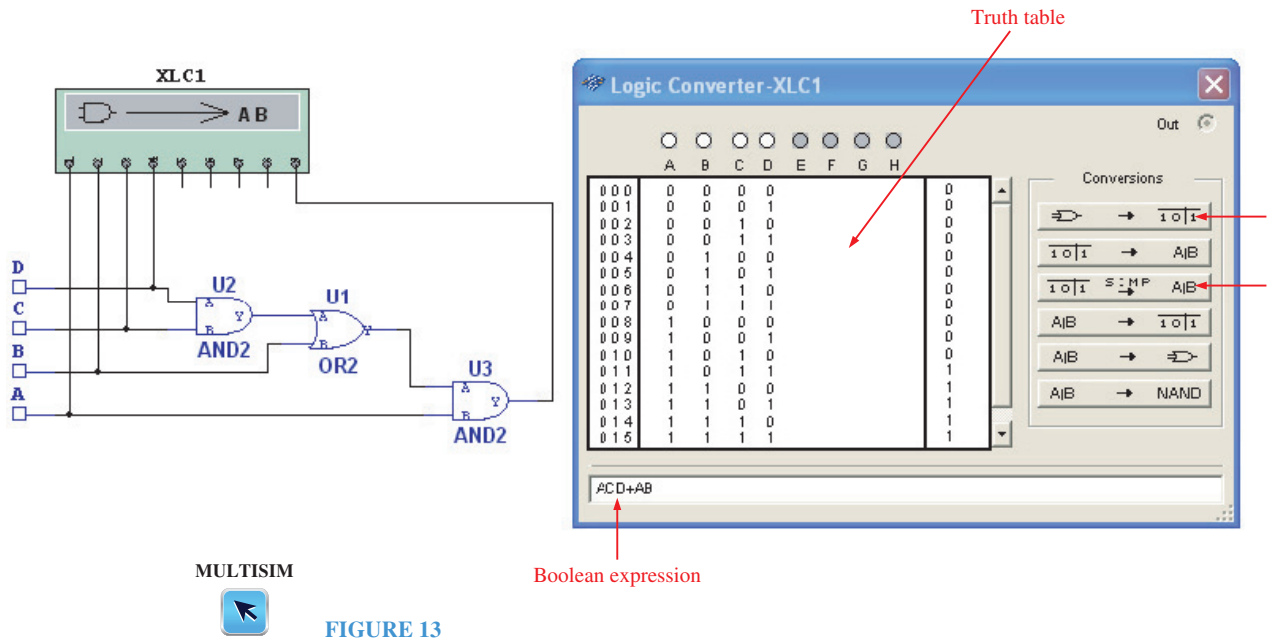


FIGURE 13

You can also generate the simplified Boolean expression from the truth table by clicking on $\overline{101} \xrightarrow{\text{SIMP}} A|B$

RELATED PROBLEM

Open Multisim and create the setup. Do the conversions shown in this example.

SECTION 2 CHECKUP

- Implement the following Boolean expressions as they are stated:
 - $X = ABC + AB + AC$
 - $X = AB(C + DE)$
- Develop a logic circuit that will produce a 1 on its output only when all three inputs are 1s or when all three inputs are 0s.
- Replace the AND gates with OR gates and the OR gate with an AND gate in Figure 12. Determine the Boolean expression for the output.
- Construct a truth table for the circuit in Question 2.

3 DEMORGAN'S THEOREMS

DeMorgan's theorems provide mathematical verification of the equivalency of the NAND and negative-OR gates and the equivalency of the NOR and negative-AND gates.

After completing this section, you should be able to

- State DeMorgan's theorems
- Relate DeMorgan's theorems to the equivalency of the NAND and negative-OR gates and to the equivalency of the NOR and negative-AND gates
- Apply DeMorgan's theorems to the simplification of Boolean expressions

DeMorgan's first theorem is stated as follows:

The complement of a product of variables is equal to the sum of the complements of the variables.

Stated another way,

The complement of two or more ANDed variables is equivalent to the OR of the complements of the individual variables.

The formula for expressing this theorem for two variables is

$$\overline{XY} = \bar{X} + \bar{Y} \quad (1)$$

DeMorgan's second theorem is stated as follows:

The complement of a sum of variables is equal to the product of the complements of the variables.

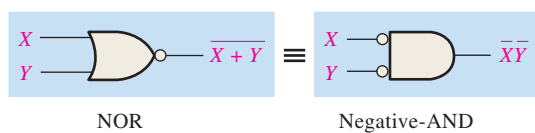
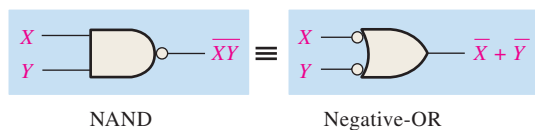
Stated another way,

The complement of two or more ORed variables is equivalent to the AND of the complements of the individual variables.

The formula for expressing this theorem for two variables is

$$\overline{X + Y} = \bar{X} \bar{Y} \quad (2)$$

Figure 14 shows the gate equivalencies and truth tables for Equations 1 and 2.



INPUTS		OUTPUT	
X	Y	\overline{XY}	$\bar{X} + \bar{Y}$
0	0	1	1
0	1	1	1
1	0	1	1
1	1	0	0

INPUTS		OUTPUT	
X	Y	$\overline{X + Y}$	$\bar{X} \bar{Y}$
0	0	1	1
0	1	0	0
1	0	0	0
1	1	0	0

FIGURE 14 Gate equivalencies and the corresponding truth tables that illustrate DeMorgan's theorems. Notice the equality of the two output columns in each table. This shows that the equivalent gates perform the same logic function.

As stated, DeMorgan's theorems also apply to expressions in which there are more than two variables. The following examples illustrate the application of DeMorgan's theorems to 3-variable and 4-variable expressions.

EXAMPLE 4

Apply DeMorgan's theorems to the expressions \overline{XYZ} and $\overline{X + Y + Z}$.

SOLUTION

$$\begin{aligned}\overline{XYZ} &= \overline{X} + \overline{Y} + \overline{Z} \\ \overline{X + Y + Z} &= \overline{X} \overline{Y} \overline{Z}\end{aligned}$$

RELATED PROBLEM

Apply DeMorgan's theorem to the expression $\overline{\overline{X} + \overline{Y} + \overline{Z}}$.

EXAMPLE 5

Apply DeMorgan's theorems to the expressions \overline{WXYZ} and $\overline{W + X + Y + Z}$.

SOLUTION

$$\begin{aligned}\overline{WXYZ} &= \overline{W} + \overline{X} + \overline{Y} + \overline{Z} \\ \overline{W + X + Y + Z} &= \overline{W} \overline{X} \overline{Y} \overline{Z}\end{aligned}$$

RELATED PROBLEM

Apply DeMorgan's theorem to the expression $\overline{\overline{W} \overline{X} \overline{Y} \overline{Z}}$.

Each variable in DeMorgan's theorems as stated in Equations 1 and 2 can also represent a combination of other variables. For example, X can be equal to the term $AB + C$, and Y can be equal to the term $A + BC$. So if you can apply DeMorgan's theorem for two variables as stated by $\overline{XY} = \overline{X} + \overline{Y}$ to the expression $\overline{(AB + C)(A + BC)}$, you get the following result:

$$\overline{(AB + C)(A + BC)} = \overline{(AB + C)} + \overline{(A + BC)}$$

Notice that in the preceding result you have two terms, $\overline{AB + C}$ and $\overline{A + BC}$, to each of which you can again apply DeMorgan's theorem $\overline{X + Y} = \overline{X} \overline{Y}$ individually, as follows:

$$\overline{(AB + C)} + \overline{(A + BC)} = (\overline{AB})\overline{C} + \overline{A}(\overline{BC})$$

Notice that you still have two terms in the expression to which DeMorgan's theorem can again be applied. These terms are \overline{AB} and \overline{BC} . A final application of DeMorgan's theorem gives the following result:

$$(\overline{AB})\overline{C} + \overline{A}(\overline{BC}) = (\overline{A} + \overline{B})\overline{C} + \overline{A}(\overline{B} + \overline{C})$$

Although this result can be simplified further by the use of Boolean rules and laws, DeMorgan's theorems cannot be applied further.

SECTION 3 CHECKUP

1. Apply DeMorgan's theorems to the following expressions:

(a) $\overline{ABC} + \overline{(D + E)}$

(b) $\overline{(A + B)C}$

(c) $\overline{A + B + C} + \overline{DE}$

4 THE UNIVERSAL PROPERTY OF NAND AND NOR GATES

Up to this point, you have studied combinational circuits implemented with AND gates, OR gates, and inverters. In this section, the universal property of the NAND gate and the NOR gate is discussed. The universality of the NAND gate means that it can be used as an inverter and that combinations of NAND gates can be used to implement the AND, OR, and NOR operations. Similarly, the NOR gate can be used to implement the inverter (NOT), AND, OR, and NAND operations.

After completing this section, you should be able to

- Use NAND gates to implement the inverter, the AND gate, the OR gate, and the NOR gate
- Use NOR gates to implement the inverter, the AND gate, the OR gate, and the NAND gate

The NAND Gate as a Universal Logic Element

The NAND gate is a **universal gate** because it can be used to produce the NOT, the AND, the OR, and the NOR functions. An inverter can be made from a NAND gate by connecting all of the inputs together and creating, in effect, a single input, as shown in Figure 15(a) for a 2-input gate. An AND function can be generated by the use of NAND gates alone, as shown in Figure 15(b). An OR function can be produced with only NAND gates, as illustrated in part (c). Finally, a NOR function is produced as shown in part (d).

Combinations of NAND gates can be used to produce any logic function.

In Figure 15(b), a NAND gate is used to invert (complement) a NAND output to form the AND function, as indicated in the following equation:

$$X = \overline{\overline{AB}} = AB$$

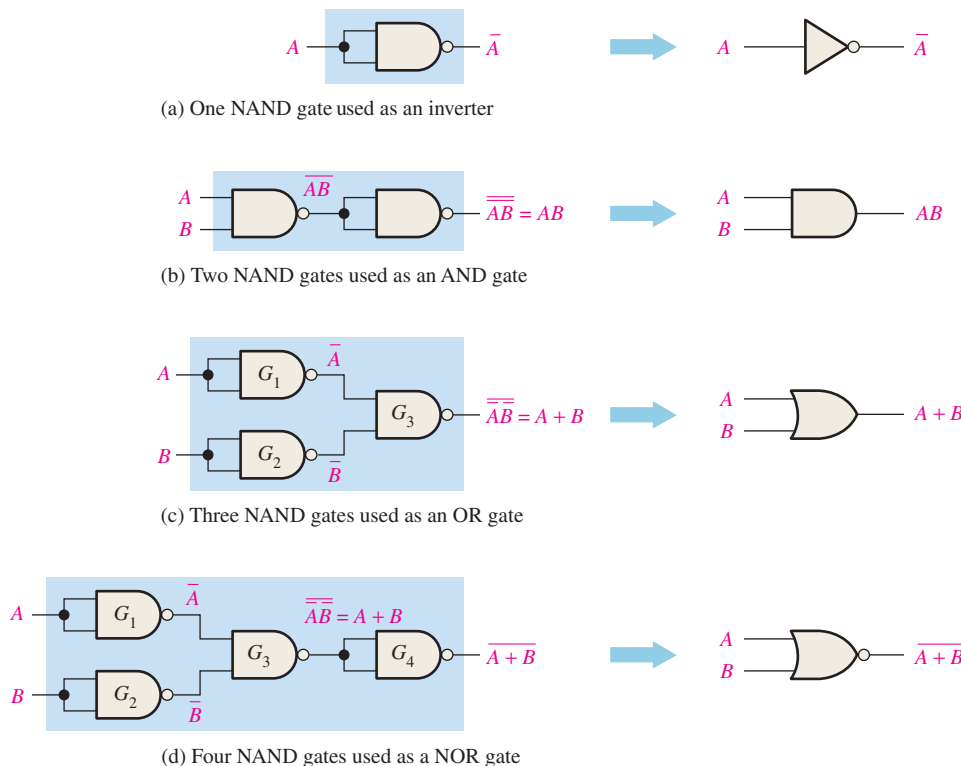


FIGURE 15 Universal application of NAND gates. Open files F04-15(a), (b), (c), and (d) to verify each of the equivalencies.



In Figure 15(c), NAND gates G_1 and G_2 are used to invert the two input variables before they are applied to NAND gate G_3 . The final OR output is derived as follows by application of DeMorgan's theorem:

$$X = \overline{\overline{A} \overline{B}} = A + B$$

In Figure 15(d), NAND gate G_4 is used as an inverter connected to the circuit of part (c) to produce the NOR operation $\overline{A + B}$.

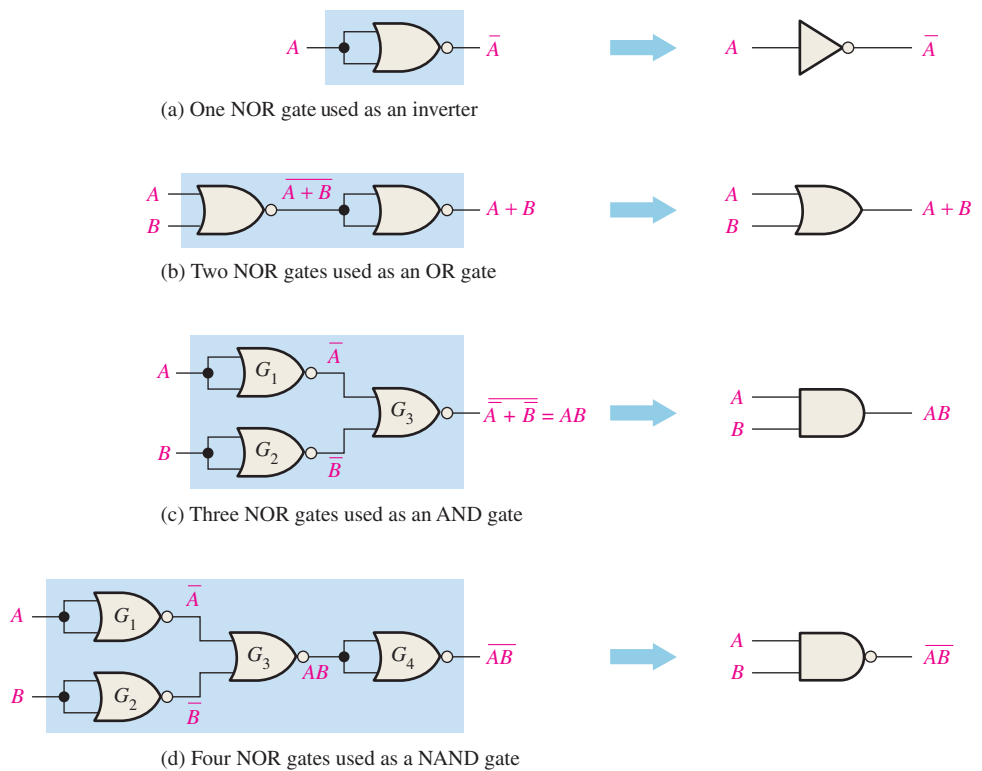
The NOR Gate as a Universal Logic Element

Combinations of NOR gates can be used to produce any logic function.

Like the NAND gate, the NOR gate can be used to produce the NOT, AND, OR, and NAND functions. A NOT circuit, or inverter, can be made from a NOR gate by connecting all of the inputs together to effectively create a single input, as shown in Figure 16(a) with a 2-input example. Also, an OR gate can be produced from NOR gates, as illustrated in Figure 16(b). An AND gate can be constructed by the use of NOR gates, as shown in Figure 16(c). In this case the NOR gates G_1 and G_2 are used as inverters, and the final output is derived by the use of DeMorgan's theorem as follows:

$$X = \overline{\overline{A} + \overline{B}} = AB$$

Figure 16(d) shows how NOR gates are used to form a NAND function.



MULTISIM



FIGURE 16 Universal application of NOR gates. Open files F04-16(a), (b), (c), and (d) to verify each of the equivalencies.

SECTION 4 CHECKUP

1. Use NAND gates to implement each expression:

(a) $X = \overline{A} + B$

(b) $X = A\overline{B}$

2. Use NOR gates to implement each expression:

(a) $X = \overline{A} + B$

(b) $X = A\overline{B}$

5 PULSE WAVEFORM OPERATION

General combinational logic with pulse waveform inputs is examined in this section. Keep in mind that the operation of each gate is the same for pulse waveform inputs as for constant-level inputs. The output of a logic circuit at any given time depends on the inputs at that particular time, so the relationship of the time-varying inputs is of primary importance.

After completing this section, you should be able to

- Predict behavior of combinational logic with pulse waveform inputs
- Develop a timing diagram for any given combinational logic circuit with specified inputs

The operation of any gate is the same regardless of whether its inputs are pulsed or constant levels. The nature of the inputs (pulsed or constant levels) does not alter the truth table of a circuit. The examples in this section illustrate the analysis of combinational logic circuits with pulse waveforms.

The following is a review of the operation of individual gates for use in understanding combinational circuits with pulse waveform inputs:

1. The output of an AND gate is HIGH only when all inputs are HIGH at the same time.
2. The output of an OR gate is HIGH only when at least one of its inputs is HIGH.
3. The output of a NAND gate is LOW only when all inputs are HIGH at the same time.
4. The output of a NOR gate is LOW only when at least one of its inputs is HIGH.

EXAMPLE 6

Determine the final output waveform X for the circuit in Figure 17, with input waveforms A , B , and C as shown.

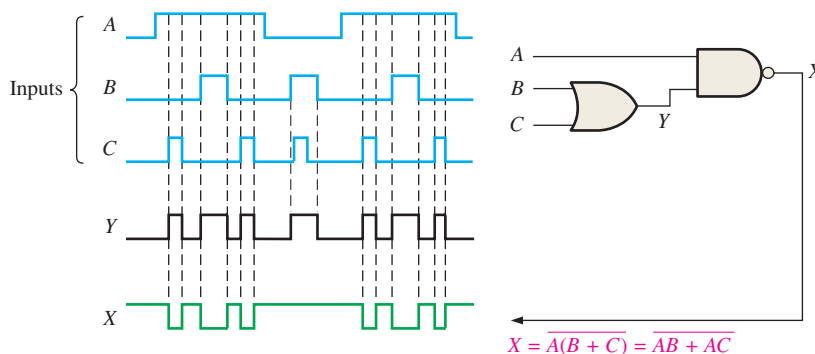


FIGURE 17

SOLUTION

The output expression, $\overline{A(B + C)}$, indicates that the output X is LOW when both A and B are HIGH or when both A and C are HIGH or when all inputs are HIGH. The output waveform X is shown in the timing diagram of Figure 17. The intermediate waveform Y at the output of the OR gate is also shown.

RELATED PROBLEM

Determine the output waveform if input A is a constant HIGH level.

EXAMPLE 7

Draw the timing diagram for the circuit in Figure 18 showing the outputs of G_1 , G_2 , and G_3 with the input waveforms, A , and B , as indicated.

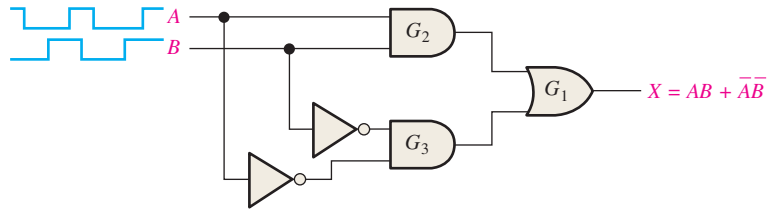


FIGURE 18

SOLUTION

When both inputs are HIGH or when both inputs are LOW, the output X is HIGH as shown in Figure 19. Notice that this is an exclusive-NOR circuit. The intermediate outputs of gates G_2 and G_3 are also shown in Figure 19.

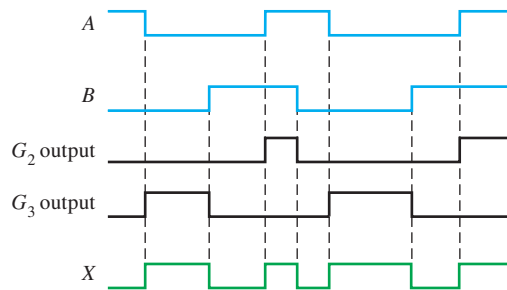


FIGURE 19

RELATED PROBLEM

Determine the output X in Figure 18 if input B is inverted.

EXAMPLE 8

Determine the output waveform X for the logic circuit in Figure 20(a) by first finding the intermediate waveform at each of points Y_1 , Y_2 , Y_3 , and Y_4 . The input waveforms are shown in Figure 20(b).

SOLUTION

All the intermediate waveforms and the final output waveform are shown in the timing diagram of Figure 20(c).

RELATED PROBLEM

Determine the waveforms Y_1 , Y_2 , Y_3 , Y_4 and X if input waveform A is inverted.

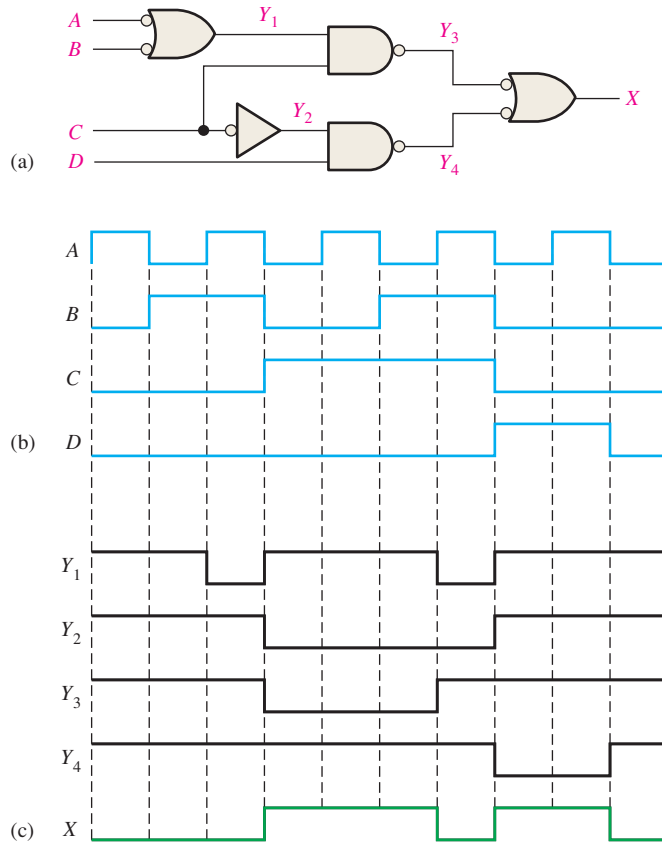


FIGURE 20

EXAMPLE 9

Determine the output waveform X for the circuit in Example 8, Figure 20(a), directly from the output expression.

SOLUTION

The output expression for the circuit is developed in Figure 21. The SOP form indicates that the output is HIGH when A is LOW and C is HIGH or when B is LOW and C is HIGH or when C is LOW and D is HIGH.

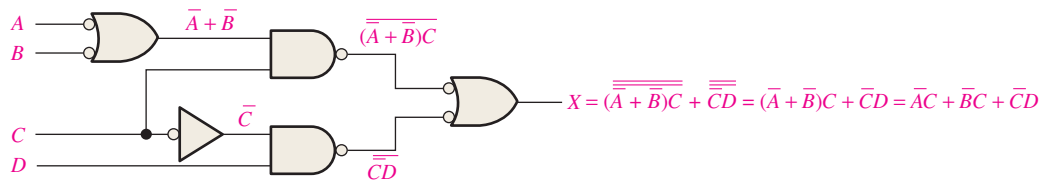


FIGURE 21

The result is shown in Figure 22 and is the same as the one obtained by the intermediate-waveform method in Example 8. The corresponding product terms for each waveform condition that results in a HIGH output are indicated.

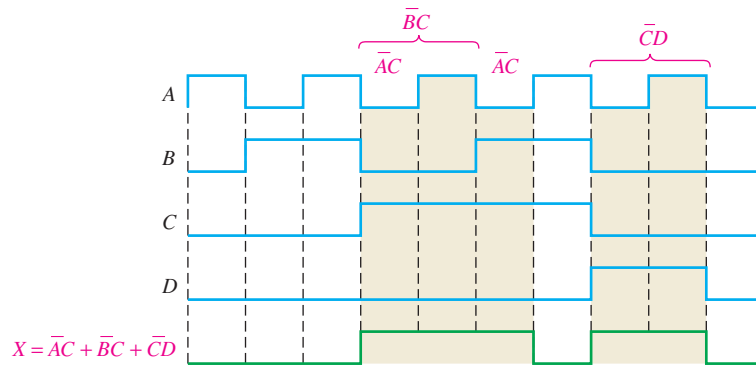


FIGURE 22

RELATED PROBLEM

Repeat this example if all the input waveforms are inverted.

SECTION 5 CHECKUP

1. One pulse with $t_W = 50 \mu s$ is applied to one of the inputs of an exclusive-OR circuit. A second positive pulse with $t_W = 10 \mu s$ is applied to the other input beginning $15 \mu s$ after the leading edge of the first pulse. Show the output in relation to the inputs.
2. The pulse waveforms A and B in Figure 17 are applied to the exclusive-NOR circuit in Figure 18. Develop a complete timing diagram.

6 COMBINATIONAL LOGIC WITH VHDL AND VERILOG

Three basic approaches to describing logic functions with VHDL are the data flow method, the structural method, and the behavioral method. In this section, the data flow method for combinational logic is discussed. The purpose of using VHDL or Verilog to describe a logic function is so that it can then be programmed into a PLD. *VHDL and Verilog tutorials are available on the website.*

After completing this section, you should be able to

- Explain the entity in VHDL
- Explain the architecture in VHDL
- Explain the module in Verilog

A VHDL data flow description of a logic function contains an entity and an architecture. The entity identifies the inputs and outputs of the function within a port statement, and the architecture describes the logic. In writing a VHDL program, both entity and architecture must be used together in what is called an entity/architecture pair. In Verilog, both of these are done in a single module. As mentioned before, both of these HDLs have their adherents and both claim that their choice is better. Actually, both VHDL and Verilog have certain pros and cons. Some say VHDL is more versatile but that Verilog is easier to learn. Keep in mind that with this coverage, we are only touching the tip of the iceberg.

VHDL and Verilog Descriptions from a Boolean Expression

In order to describe combinational logic, you should have either the Boolean expression or the truth table. Example 10 shows the use of the `std_logic` data type in VHDL. The `bit` data type is shown in the remaining programs.

EXAMPLE 10

Write the VHDL and the Verilog descriptions of AND-OR logic with two 2-input AND gates. The expression is

$$X = AB + CD$$

SOLUTION

Name assignments can be anything all run together or separated by an underscore.

VHDL

```
library ieee;
use ieee.std_logic_1164.all;
entity ANDORlogic is
    port (A, B, C, D: in std_logic; X: out std_logic);
end entity ANDORlogic;
architecture ANDORfunction of ANDORlogic is
begin
    X <= (A and B) or (C and D);
end architecture ANDORfunction;
```

Verilog

```
module ANDORlogic (A, B, C, D, X);
input A, B, C, D;
output X;
    assign X = (A && B) || (C && D);
endmodule
```

RELATED PROBLEM

If the AND-OR logic has four AND gates each with two inputs, modify the programs.

EXAMPLE 11

Write VHDL and Verilog programs for a logic function having the following Boolean expression:

$$X = (\bar{A}\bar{B} + C)(\bar{D}\bar{E} + F)$$

SOLUTION

VHDL

```
entity Combo_Logic is
    port (A, B, C, D, E, F: in bit; X: out bit);
end entity Combo_Logic;
architecture Logic_Function of Combo_Logic is
begin
    X <= ((not A and not B) or C) and ((not D
        and not E) or F);
end architecture Logic_Function;
```

Verilog

```
module Combo_Logic (A, B, C, D, E, F, X);
input A, B, C, D, E, F;
output X;
    assign X = ((!A && !B) || C) && ((!D
        && !E) || F);
endmodule
```

RELATED PROBLEM

How would the programs change if there were a bar over each of the parenthetical terms?

VHDL and Verilog Descriptions from a Truth Table

VHDL or Verilog descriptions can also be written directly from a truth table as Example 12 shows.

EXAMPLE 12

Write VHDL and Verilog programs for a logic function having the following truth table (Table 7).

TABLE 7				
INPUTS				OUTPUT
A	B	C	D	X
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

SOLUTION

As you know, the Boolean terms for the combination of inputs that produce a 1 output form the Boolean expression. In this case, there are five terms that can be written directly to the VHDL and Verilog programs.

VHDL

```
entity Table_7 is
  port (A, B, C, D: in bit; X: out bit);
end entity Table_7;
architecture Logic_Function of Table_7 is
begin
  X <= (A and not B and C and D) or (A and
    B and not C and not D) or (A and B
    and not C and D) or (A and B and C
    and not D) or (A and B and C and D);
end architecture Logic_Function;
```

Verilog

```
module Table_7 (A, B, C, D, X);
  input A, B, C, D;
  output X;
  assign X = (A && !B && C && D) ||
    (A && B && !C && !D) ||
    (A && B && !C && D) ||
    (A && B && C && !D) ||
    (A && B && C && D);
endmodule
```

RELATED PROBLEM

How would the programs change if an all 0s input also produced a 1 in the table?

Structural Approach to VHDL Programming

The structural approach to writing a VHDL description of a logic function can be compared to installing IC devices on a circuit board and interconnecting them with wires. With the structural approach, you describe logic functions and specify how they are connected together. The VHDL **component** is a way to predefine a logic function for repeated use in a program or in other programs. The component can be used to describe anything from a simple logic gate to a complex logic function. The VHDL **signal** can be thought of as a way to specify a “wire” connection between components.

A VHDL component describes predefined logic that can be stored as a package declaration in a VHDL library and called as many times as necessary in a program. You can use components to avoid repeating the same code over and over within a program. For example, you can create a VHDL component for an AND gate and then use it as many times as you wish without having to write a program for an AND gate every time you need one.

VHDL components are stored and are available for use when you write a program. This is similar to having, for example, a storage bin of ICs available when you are constructing a circuit. Every time you need to use one in your circuit, you reach into the storage bin and place it on the circuit board.

The VHDL program for any logic function can become a component and used whenever necessary in a larger program with the use of a component declaration of the following general form. **Component** is a VHDL keyword.

```
component name_of_component is
  port (port definitions);
end component name_of_component;
```

For simplicity, let’s assume that there are predefined VHDL data flow descriptions of a 2-input AND gate with the entity name AND_gate and a 2-input OR gate with the entity name OR_gate, as shown in Figure 23.

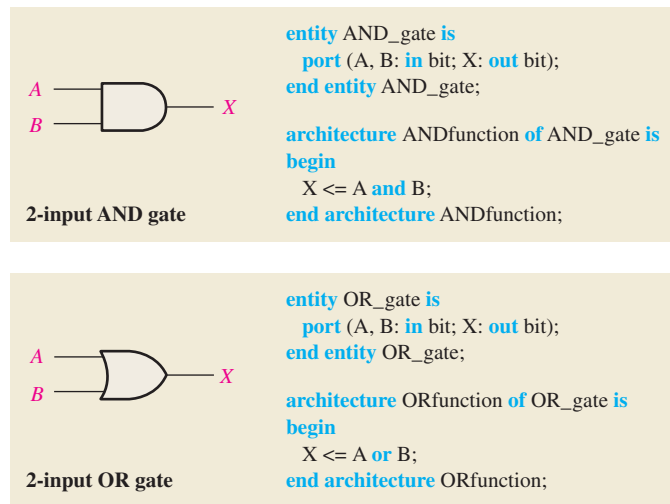


FIGURE 23 Predefined programs for a 2-input AND gate and a 2-input OR gate to be used as components in a larger program.

Next, assume that you are writing a program for a logic circuit that has several AND gates. Instead of rewriting the program in Figure 23 over and over, you can use a component declaration to specify the AND gate. The port statement in the component declaration must correspond to the port statement in the entity declaration of the AND gate.

```
component AND_gate is
  port (A, B: in bit; X: out bit);
end component AND_gate;
```

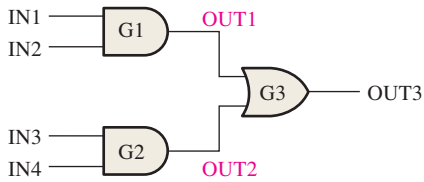


FIGURE 24

USING COMPONENTS IN A PROGRAM To use a component in a program, you must write a component instantiation statement for each instance in which the component is used. You can think of a component instantiation as a request or call for the component to be used in the main program. For example, the simple SOP logic circuit in Figure 24 has two AND gates and one OR gate. Therefore, the VHDL program for this circuit will have two components and three component instantiations or calls.

SIGNALS In VHDL, signals are analogous to wires that interconnect components on a circuit board. The signals in Figure 24 are named OUT1 and OUT2. Signals are the *internal* connections in the logic circuit and are treated differently than the inputs and outputs. Whereas the inputs and outputs are declared in the entity declaration using the port statement, the signals are declared within the architecture using the signal statement. **Signal** is a VHDL keyword.

THE PROGRAM The program for the logic in Figure 24 begins with an entity declaration as follows:

```
--Program for the logic circuit in Figure 24
entity AND_OR_Logic is
    port (IN1, IN2, IN3, IN4: in bit; OUT3: out bit);
end entity AND_OR_Logic;
```

The architecture declaration contains the component declarations for the AND gate and the OR gate, the signal definitions, and the component instantiations.

architecture LogicOperation of AND_OR_Logic is

```
component AND_gate is
    port (A, B: in bit; X: out bit);
end component AND_gate;
```

Component declaration for the AND gate

```
component OR_gate is
    port (A, B: in bit; X: out bit);
end component OR_gate;
```

Component declaration for the OR gate

```
signal OUT1, OUT2: bit;
```

Signal declaration

begin

```
G1: AND_gate port map (A => IN1, B => IN2, X => OUT1);
G2: AND_gate port map (A => IN3, B => IN4, X => OUT2);
G3: OR_gate port map (A => OUT1, B => OUT2, X => OUT3);
```

Component instantiations

end architecture LogicOperation;

COMPONENT INSTANTIATIONS Let's look at the component instantiations. First, notice that the component instantiations appear between the keyword **begin** and the **end** statement. For each instantiation an identifier is defined, such as G1, G2, and G3 in this case. Then the component name is specified. The port map essentially makes all the connections for the logic function using the operator =>. For example, the first instantiation,

```
G1: AND_gate port map (A => IN1, B => IN2, X => OUT1);
```

can be explained as follows: *Input A of AND gate G1 is connected to input IN1, input B of the gate is connected to input IN2, and the output X of the gate is connected to the signal OUT1.*

The three instantiation statements together completely describe the logic circuit in Figure 24, as illustrated in Figure 25.

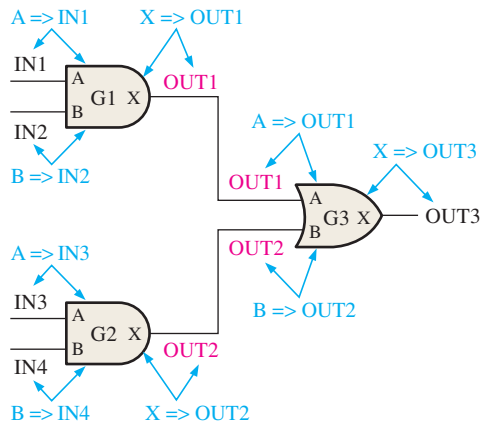


FIGURE 25 Illustration of the instantiation statements and port mapping applied to the AND-OR logic. Signals are shown in red.

Although the data flow approach using Boolean expressions would have been easier and probably the best way to describe this particular circuit, we have used this simple circuit to explain the concept of the structural approach. Example 13 compares the structural and data flow approaches to writing a VHDL program for an SOP logic circuit.

EXAMPLE 13

Write a VHDL program for the SOP logic circuit in Figure 26 using the structural approach and the data flow approach. Assume that VHDL components for a 3-input NAND gate and for a 2-input NAND are available. Notice the NAND gate G4 is shown as a negative-OR.

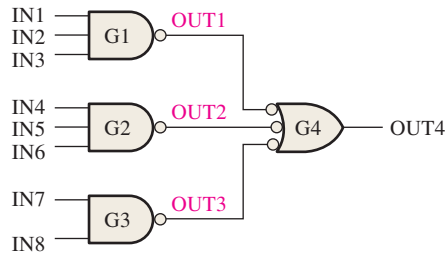


FIGURE 26

SOLUTION

The components and component instantiations are highlighted.

```
--Program for the logic circuit in Figure 26
entity SOP_Logic is
  port (IN1, IN2, IN3, IN4, IN5, IN6, IN7, IN8: in bit; OUT4: out bit);
end entity SOP_Logic;
architecture LogicOperation of SOP_Logic is
  --component declaration for 3-input NAND gate
  component NAND_gate3 is
    port (A, B, C: in bit; X: out bit);
  end component NAND_gate3;

  --component declaration for 2-input NAND gate
  component NAND_gate2 is
    port (A, B: in bit; X: out bit);
  end component NAND_gate;

  signal OUT1, OUT2, OUT3: bit;
```

begin

--component instantiations

```
G1: NAND_gate3 port map (A => IN1, B => IN2, C => IN3, X => OUT1);
G2: NAND_gate3 port map (A => IN4, B => IN5, C => IN6, X => OUT2);
G3: NAND_gate2 port map (A => IN7, B => IN8, X => OUT3);
G4: NAND_gate3 port map (A => OUT1, B => OUT2, C => OUT3, X => OUT4);
```

end architecture LogicOperation;

Using the data flow approach, the program for the logic circuit in Figure 26 is

entity SOP_Logic **is**

port (IN1, IN2, IN3, IN4, IN5, IN6, IN7, IN8: **in** bit; OUT4: **out** bit);

end entity SOP_Logic;

architecture LogicOperation **of** SOP_Logic **is**

begin

OUT4 <= (IN1 **and** IN2 **and** IN3) **or** (IN4 **and** IN5 **and** IN6) **or** (IN7 **and** IN8);

end architecture LogicOperation;

As you can see, the data flow approach results in a much simpler code for this particular logic function. However, in situations where a logic function consists of many blocks of complex logic, the structural approach might have an advantage over the data flow approach.

RELATED PROBLEM

If another NAND gate is added to the circuit in Figure 26 with inputs IN9 and IN10, write a component instantiation to add to the program.

SECTION 6 CHECKUP

1. What does an entity in VHDL do?
2. What does an architecture in VHDL do?
3. What performs the same function in Verilog as the entity/architecture pair in VHDL?
4. Name two approaches to writing a VHDL program.
5. What is a VHDL component?
6. State the purpose of a component instantiation in a program architecture.
7. How are interconnections made between components in VHDL?
8. The use of components in a VHDL program represents what approach?

7 A SYSTEM

A storage tank system for a pancake syrup manufacturing company is the focus of this section. The control logic allows a volume of corn syrup to be preheated to a specified temperature to achieve the proper viscosity prior to being sent to a mixing vat where ingredients such as sugar, flavoring, preservative, and coloring are added. Level and temperature sensors in the tank and the flow sensor provide the inputs for the logic.

After completing this section, you should be able to

- Explain how the system works
- Write VHDL and Verilog programs so that the system can be implemented in a PLD

System Operation

A tank that holds corn syrup for use in a pancake syrup manufacturing process is shown in Figure 27. In preparation for mixing, the temperature of the corn syrup when released from the tank into a mixing vat must be at a specified value for proper viscosity to produce required flow characteristics. This temperature can be selected via a keypad input. The control logic maintains the temperature at this value by turning a heater *on* and *off*. The analog output from the temperature transducer (T_{analog}) is converted to an 8-bit binary code by an analog-to-digital converter and then to an 8-bit BCD code. A temperature controller detects when the temperature falls below the specified value and turns the heater *on*. When the temperature reaches the specified value, the heater is turned *off*.

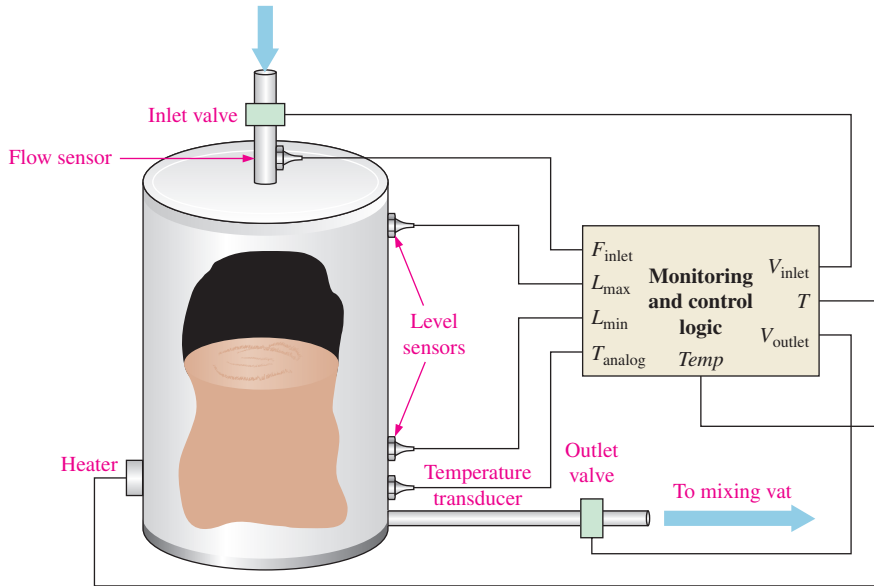


FIGURE 27 Tank with level and temperature sensors and controls.

The level sensors produce a HIGH when the corn syrup is at or above the minimum or at the maximum level. The valve control logic detects when the maximum level (L_{max}) or minimum level (L_{min}) has been reached and when solution is flowing into the tank (F_{inlet}). Based on these inputs, the control logic opens or closes each valve (V_{inlet} and V_{outlet}). New corn syrup can be added to the tank via the inlet valve only when the minimum level is reached. Once the inlet valve is opened, the level in the tank must reach the maximum point before the inlet valve is closed. Also, once the outlet valve is opened, the level must reach the minimum point before the outlet valve is closed. New syrup is always cooler than the syrup in the tank. Syrup cannot be released from the tank while it is being filled or its temperature is below the specified value.

INLET VALVE CONTROL The conditions for which the inlet valve is open, allowing the tank to fill, are

- The solution level is at minimum (L_{min}).
- The tank is filling (F_{inlet}) but the maximum level has not been reached (\bar{L}_{max}).

Table 8 is the truth table for the inlet valve. A HIGH (1) is the active level for the inlet valve to be open (*on*). From the truth table, an expression for the inlet valve control output can be written.

$$V_{\text{inlet}} = \bar{L}_{\text{max}}\bar{L}_{\text{min}}\bar{F}_{\text{inlet}} + \bar{L}_{\text{max}}\bar{L}_{\text{min}}F_{\text{inlet}} + \bar{L}_{\text{max}}L_{\text{min}}F_{\text{inlet}}$$

The SOP expression can be reduced to the following simplified expression using Boolean methods:

$$V_{\text{inlet}} = \bar{L}_{\text{min}} + \bar{L}_{\text{max}}F_{\text{inlet}}$$

TABLE 8 • Truth table for inlet valve control.

INPUTS			OUTPUT	DESCRIPTION
L_{\max}	L_{\min}	F_{inlet}	V_{inlet}	
0	0	0	1	Level below minimum. No inlet flow.
0	0	1	1	Level below minimum. Inlet flow.
0	1	0	0	Level above min and below max. No inlet flow.
0	1	1	1	Level above min and below max. Inlet flow.
1	0	0	X	Invalid.
1	0	1	X	Invalid.
1	1	0	0	Level at maximum. No inlet flow.
1	1	1	0	Level at maximum. Inlet flow.

OUTLET VALVE CONTROL The conditions for which the outlet valve is open allowing the tank to drain are

- The syrup level is above minimum and the tank is not filling.
- The temperature of the syrup is at the specified value.

Table 9 is the truth table for the outlet valve. A HIGH (1) is the active level for the outlet valve to be open (*on*). *Note: T* is both an input and an output ($T = \text{Temp}$).

TABLE 9 • Truth table for outlet valve control.

INPUTS				OUTPUT	DESCRIPTION
L_{\max}	L_{\min}	F_{inlet}	T	V_{outlet}	
0	0	0	0	0	Level below minimum. No inlet flow. Temp low.
0	0	0	1	0	Level below minimum. No inlet flow. Temp correct.
0	0	1	0	0	Level below minimum. Inlet flow. Temp low.
0	0	1	1	0	Level below minimum. Inlet flow. Temp correct.
0	1	0	0	0	Level above min and below max. No inlet flow. Temp low.
0	1	0	1	1	Level above min and below max. No inlet flow. Temp correct.
0	1	1	0	0	Level above min and below max. Inlet flow. Temp low.
0	1	1	1	0	Level above min and below max. Inlet flow. Temp correct.
1	0	0	0	X	Invalid.
1	0	0	1	X	Invalid.
1	0	1	0	X	Invalid.
1	0	1	1	X	Invalid.
1	1	0	0	0	Level at maximum. No inlet flow. Temp low.
1	1	0	1	1	Level at maximum. No inlet flow. Temp correct.
1	1	1	0	0	Level at maximum. Inlet flow. Temp low.
1	1	1	1	0	Level at maximum. Inlet flow. Temp correct.

From the truth table, an expression for the outlet valve control output can be written.

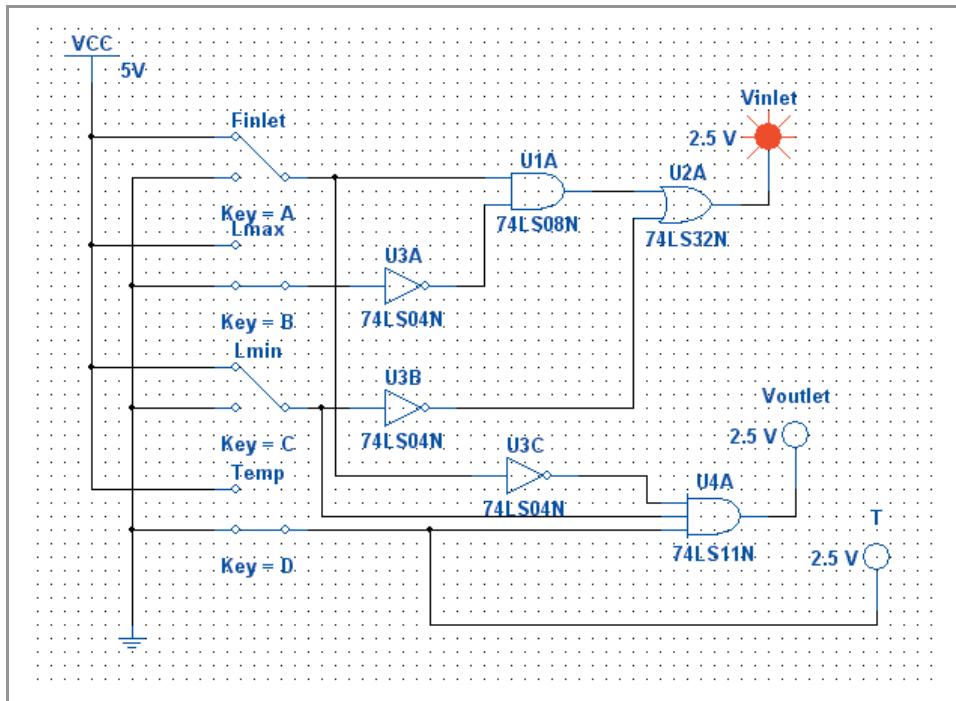
$$V_{\text{outlet}} = \bar{L}_{\text{max}}L_{\text{min}}\bar{F}_{\text{inlet}}T + L_{\text{max}}L_{\text{min}}\bar{F}_{\text{inlet}}T$$

The SOP expression can be reduced to the following simplified expression using Boolean methods:

$$V_{\text{outlet}} = L_{\text{min}}\bar{F}_{\text{inlet}}T$$

Simulation of the Valve Control Logic

The inlet and outlet valve control logic simulation screen is shown in Figure 28. SPDT switches are used to represent the level and flow sensor inputs and the temperature indication. Probes are used to indicate the output states.



MULTISIM



FIGURE 28 Multisim circuit screen for the valve control logic. Open file F04-28 and run the simulation.

TEMPERATURE CONTROL The temperature control logic accepts an 8-bit BCD code representing the measured temperature and compares it to the BCD code for the specified temperature. A block diagram is shown in Figure 29.

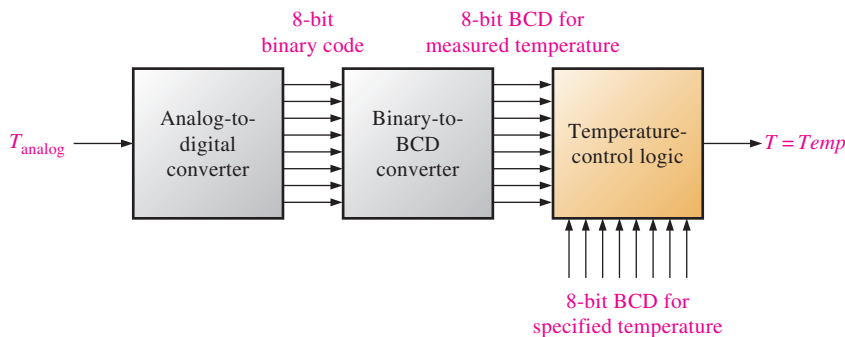


FIGURE 29 Block diagram for temperature control system.

When the measured temperature and the specified temperature are the same, the two BCD codes are equal and the T output is LOW (0). When the measured temperature falls below the specified value, there is a difference in the BCD codes and the T output is HIGH (1), which turns on the heater. The temperature control logic can be implemented with exclusive-OR gates, as shown in Figure 30. Each pair of corresponding bits from the two BCD codes is applied to an exclusive-OR gate. If the bits are the same, the output of the XOR gate is 0; and if they are different, the output of the XOR gate is 1. When one or more XOR outputs equal 1, the T output of the OR gate equals 1, causing the heater to turn on.

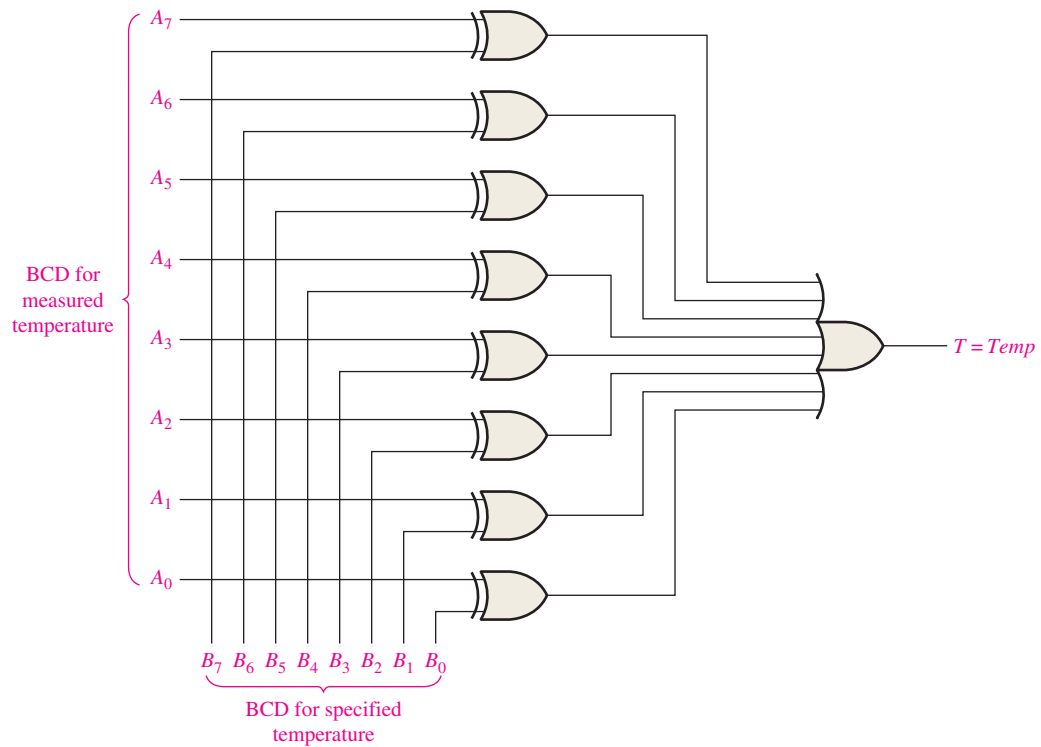


FIGURE 30 Logic diagram of the temperature control logic.

VHDL and Verilog for Inlet, Outlet, and Temperature Controls

In order to implement this control system in a PLD, a VHDL program is developed. This implementation does not include the analog-to-digital converter or the binary-to-BCD converter required for the temperature control.

First, assign input labels to the temperature control logic. The BCD for measured temperature inputs are assigned A0 through A7, as shown in Figure 30. The BCD for specified temperature inputs are assigned B0 through B7, as shown. The inlet and outlet valve controls in Figure 27 already have input label assignments. The VHDL program using the data flow approach is as follows.

```
entity TankControlLogic is
  port (Finlet, Lmax, Lmin, A0, A1, A2, A3,
        A4, A5, A6, A7, B0, B1, B2, B3, B4, B5,
        B6, B7: in bit; T: buffer bit; Vinlet, Voutlet: out bit);
end entity TankControlLogic;
architecture Logic_Function of TankControlLogic is
```

begin

```
T <= (A0 xor B0) or (A1 xor B1) or (A2 xor B2) or
      (A3 xor B3) or (A4 xor B4) or (A5 xor B5) or
      (A6 xor B6) or (A7 xor B7);
Vinlet <= not Lmin or not Lmax and Finlet;
Voutlet <= Lmin and not Finlet and Temp;
end architecture Logic_Function;
```

Alternately, the system logic can be programmed using Verilog.

```
module TankControlLogic (Finlet, Lmax, Lmin,
                        Vinlet, Voutlet, T, A0, A1, A2, A3, A4, A5, A6, A7, B0,
                        B1, B2, B3, B4, B5, B6, B7);
input Finlet Lmax, Lmin, Temp, A0, A1, A2, A3, A4,
        A5, A6, A7, B0, B1, B2, B3, B4, B5, B6, B7;
output Vinlet, Voutlet, T;
assign T = ((A0 && !B0) || (!A0 && B0)) || ((A1 && !B1) || (!A1 && B1)) ||
            ((A2 && !B2) || (!A2 && B2)) || ((A3 && !B3) || (!A3 && B3)) ||
            ((A3 && !B3) || (!A3 && B3)) || ((A4 && !B4) || (!A4 && B4)) ||
            ((A5 && !B5) || (!A5 && B5)) || ((A6 && !B6) || (!A6 && B6)) ||
            ((A7 && !B7) || (!A7 && B7))
assign Vinlet = !Lmin || (!Lmax && Finlet);
assign Voutlet = Lmin && !Finlet && Temp;
endmodule
```

Alternately, the expression for T in the Verilog program can be written in a more compact form using the Verilog bit-wise operator for XOR, ^, rather than the logical operators !, &&, and || as follows:

```
T = (A0 ^ B0) || (A1 ^ B1) || (A4 ^ B4) || (A5 ^ B5) || (A6 ^ B6) || (A7 ^ B7);
```

SECTION 7 CHECKUP

1. For how many input conditions is the inlet valve open?
2. For how many input conditions is the outlet valve open?
3. Why does the outlet valve control require four inputs and the inlet valve only three?
4. Once the level reaches maximum and the tank starts draining, when does the outlet valve turn off?

8 TROUBLESHOOTING



The preceding sections have given you some insight into the operation of combinational logic circuits and the relationships of inputs and outputs. This type of understanding is essential when you troubleshoot digital circuits and systems because you must know what logic levels or waveforms to look for throughout the circuit for a given set of input conditions. You have learned two basic troubleshooting methods and studied the troubleshooting of an example system. There were two options once the defective circuit board was identified: to repair or to not repair the board. Of course, a new board replaces the defective board in either case.

In this section, an oscilloscope is used to troubleshoot at the board level when a device output is connected to several device inputs. Also, an example of signal tracing and waveform analysis methods is presented using a scope for locating a fault in combinational logic.

After completing this section, you should be able to

- Define a circuit node
- Use an oscilloscope to find a faulty circuit node
- Use an oscilloscope to find an open gate output
- Use an oscilloscope to find a shorted gate input or output
- Use an oscilloscope for signal tracing



HANDS ON TIP

In addition to components, visual inspection should include connectors. Edge connectors are frequently used to bring power, ground, and signals to a circuit board. The mating surfaces of the connector need to be clean and have a good mechanical fit. A dirty connector can cause intermittent or complete failure of the circuit. Edge connectors can be cleaned with a common pencil eraser and wiped clean with a Q-tip soaked in alcohol. Also, all connectors should be checked for loose-fitting pins.

In a combinational logic circuit, the output of a driving device may be connected to two or more load devices as shown in Figure 31. The interconnecting paths share a common electrical point known as a **node**.

The driving device in Figure 31 is driving the node, and the other devices represent loads connected to the node. A driving device can drive a number of load device inputs up to its specified fan-out. Several types of failures are possible in this situation. Some of these failure modes are difficult to isolate to a single bad device because all the devices connected to the node are affected. Common types of failures are the following:

1. *Open output in driving device.* This failure will cause a loss of signal to all load devices.
2. *Open input in a load device.* This failure will not affect the operation of any of the other devices connected to the node, but it will result in loss of signal output from the faulty device.
3. *Shorted output in driving device.* This failure can cause the node to be stuck in the LOW state (short to ground) or in the HIGH state (short to V_{CC}).
4. *Shorted input in a load device.* This failure can also cause the node to be stuck in the LOW state (short to ground) or in the HIGH state (short to V_{CC}).

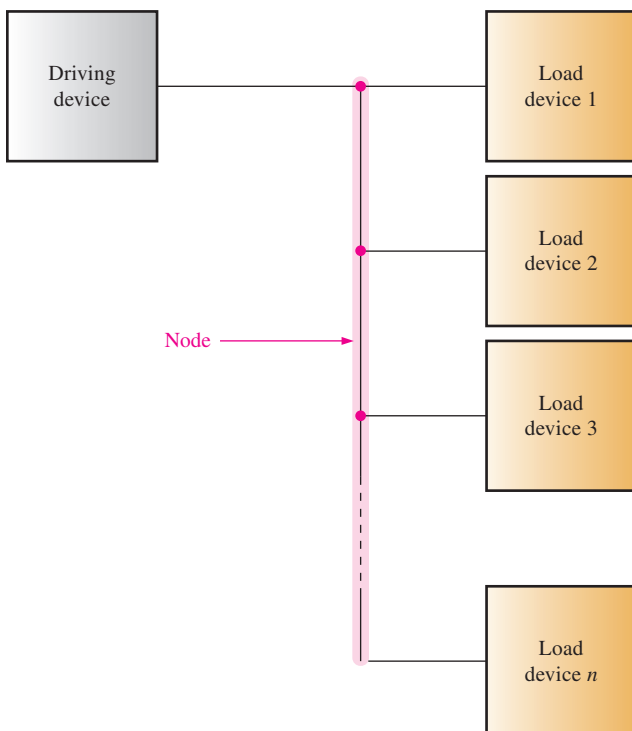
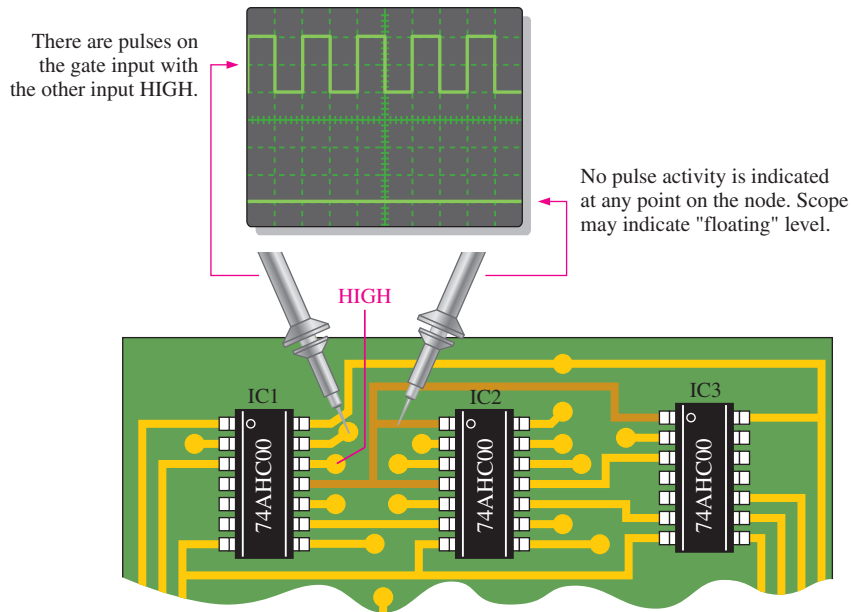


FIGURE 31 Illustration of a node in a logic circuit.

Troubleshooting Common Faults at the Board Level

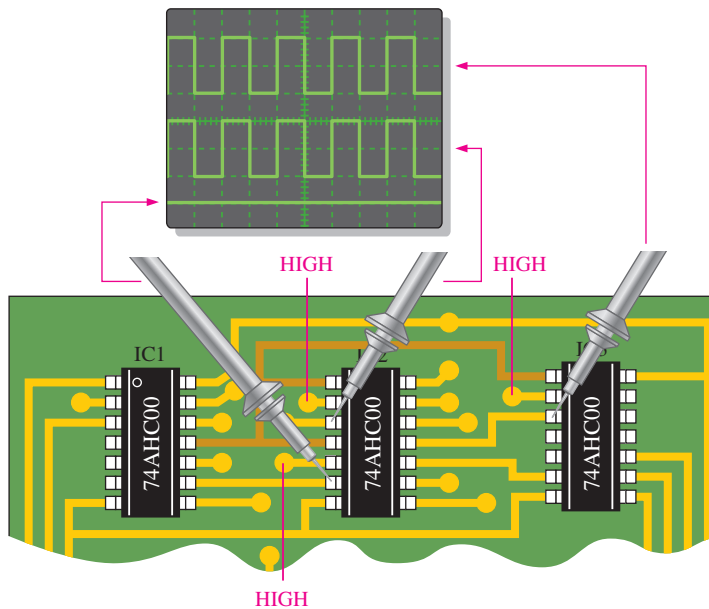
OPEN OUTPUT IN DRIVING DEVICE In this situation there is no pulse activity on the node. With circuit power on, an open node will normally result in a “floating” level, as illustrated in Figure 32.



If there is no pulse activity at the output pin on IC1, there is an internal open. If there is pulse activity directly on the output pin but not on the node interconnections, the connection between the pin and the board is open.

FIGURE 32 Open output in driving device. Assume a HIGH is on one input.

OPEN INPUT IN A LOAD DEVICE If the check for an open driver output in IC1 is negative (there is pulse activity), then a check for an open input in a load device should be performed. Check the output of each device for pulse activity, as illustrated in Figure 33. If one of the inputs that is normally connected to the node is open, no pulses will be detected on that device's output.



Check the output pin of each device connected to the node with other device inputs HIGH. No pulse activity on an output indicates an open input or open output.

FIGURE 33 Open input in a load device.

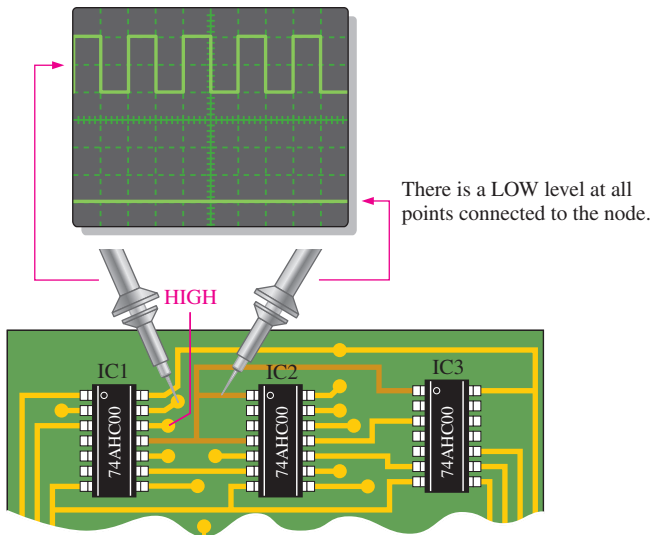


FIGURE 34 Shorted output in the driving device or shorted input in a load.

OUTPUT OR INPUT SHORTED TO GROUND

When the output is shorted to ground in the driving device or the input to a load device is shorted to ground, it will cause the node to be stuck LOW, as previously mentioned. A quick check with a scope probe will indicate this, as shown in Figure 34. A short to ground in the driving device's output or in any load input will cause this symptom, and further checks must therefore be made to isolate the short to a particular device.

Signal Tracing and Waveform Analysis

Although the methods of isolating an open or a short at a node point are very useful from time to time, the technique of **signal tracing** is of value in just about every troubleshooting situation. Waveform measurement is accomplished with an oscilloscope or a logic analyzer.

Basically, the signal tracing method requires that you observe the waveforms and their time relationships at all accessible points in the logic circuit. You can begin at the inputs and, from an analysis of the waveform timing diagram for each point, determine where an incorrect waveform first occurs. With this procedure you can usually isolate the fault to a specific device. A procedure beginning at the output and working back toward the inputs can also be used. In this approach, it is necessary to know what the signal should be based on a thorough knowledge of the circuit or on a documented troubleshooting procedure showing waveforms at various crucial points.

The general procedure for signal tracing starting at the inputs is outlined as follows:

- Within a system, define the section of logic that is suspected of being faulty.
- Start at the inputs to the section of logic under examination. We assume, for this discussion, that the input waveforms coming from other sections of the system have been found to be correct.
- For each device, beginning at the input and working toward the output of the logic circuit, observe the output waveform of the device and compare it with the input waveforms by using the oscilloscope or the logic analyzer.
- Determine if the output waveform is correct, using your knowledge of the logical operation of the device or from a troubleshooting procedure, if available.
- If the output is incorrect, the device under test may be faulty. Pull the IC device that is suspected of being faulty, and test it out-of-circuit. If the device is found to be faulty, replace the IC. If it works correctly, the fault is in the external circuitry or in another IC to which the tested one is connected.
- If the output is correct, go to the next device. Continue checking each device until an incorrect waveform is observed.

Figure 35 illustrates the general signal tracing procedure from inputs to output for simple combinational logic in the following steps:

- Step 1:** Observe the output at test point 5 (TP5) relative to the inputs at TP1 and TP2. If it is correct, go to step 2. If the inputs are correct and the output is not correct, the gate or its connections are bad; or, if the output is LOW, the input to gate G_2 may be shorted. In this case, the fault is in IC2. Replace it and recheck the operation.
- Step 2:** Observe the output of the inverter (TP6) relative to the input at TP3. If it is correct, go to Step 3. If the input is correct and the output is not correct, the



HANDS ON TIP

As you know, testing and troubleshooting logic circuits often require observing and comparing two digital waveforms simultaneously, such as an input and the output of a gate, on an oscilloscope. For digital waveforms, the scope should always be set to DC coupling on each channel input to avoid "shifting" the ground level. You should determine where the 0 V level is on the screen for both channels.

To compare the timing of the waveforms, the scope should be triggered from only one channel (don't use vertical mode or composite triggering). The channel selected for triggering should always be the one that has the lowest frequency waveform, if possible.

COMBINATIONAL LOGIC

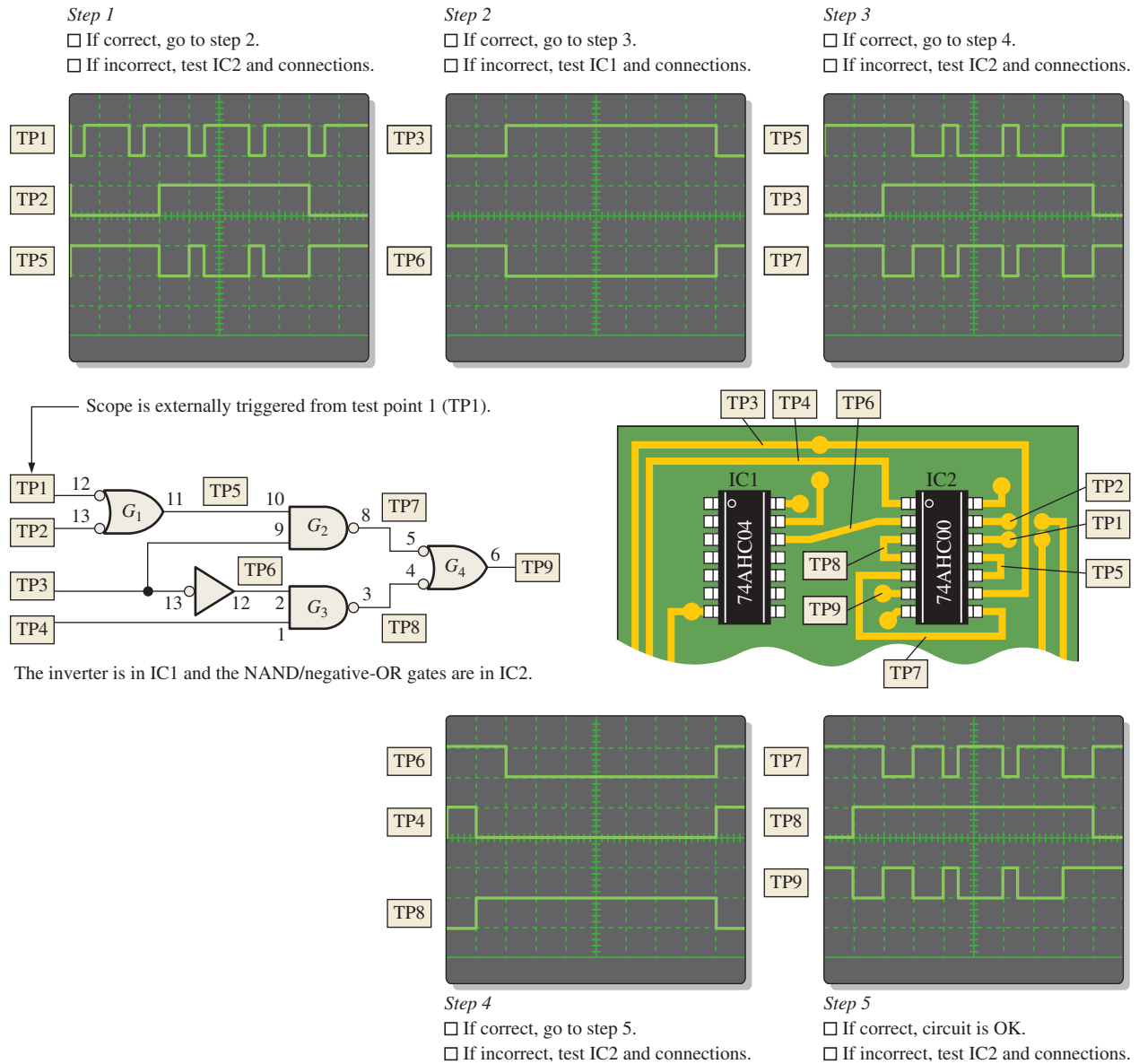


FIGURE 35 Example of signal tracing and waveform analysis in a portion of a printed circuit board. TP indicates test point. The correct waveforms are shown.

- inverter or its connections are bad; or, if the output is LOW, the input to gate G_3 may be shorted. In this case, you can't determine which IC is bad, so both IC1 and IC2 should be replaced and the operation rechecked.
- Step 3:** Observe the output of gate G_2 (TP7) relative to the inputs at TP3 and TP5. If it is correct, go to Step 4. If the output is not correct, the gate or its connections are bad; or, if the output is LOW, the input to gate G_4 may be shorted. In this case, the fault is in IC2. Replace it and recheck the operation.
- Step 4:** Observe the output of gate G_3 (TP8) relative to the inputs at TP4 and TP6. If it is correct, go to Step 5. If the output is not correct, the gate or its connections are bad; or, if the output is LOW, the input to gate G_4 (TP7) may be shorted. In this case, the fault is in IC2. Replace it and recheck the operation.
- Step 5:** Observe the output of gate G_4 (TP9) relative to the inputs at TP7 and TP8. If it is correct, the circuit is okay. If the output is not correct, the gate or its connections are bad or its load is shorted. Replace IC2 and see if that corrects the problem. If it doesn't, you will have to investigate further depending on where the G_4 output goes.

EXAMPLE 14

Determine the fault in the logic circuit of Figure 36(a) by using waveform analysis. You have observed the waveforms shown in green in Figure 36(b). The red waveforms are correct and are provided for comparison.

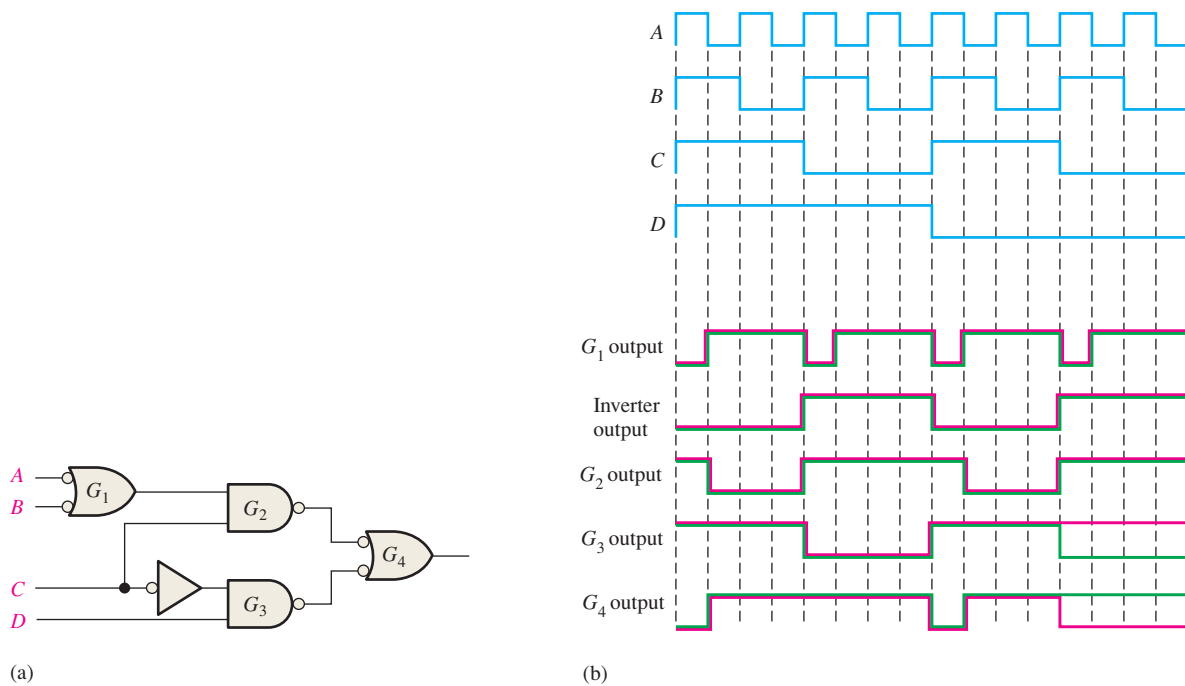


FIGURE 36

SOLUTION

1. Determine what the correct waveform should be for each gate. The correct waveforms are shown in red, superimposed on the actual measured waveforms, in Figure 36(b).
2. Compare waveforms gate by gate until you find a measured waveform that does not match the correct waveform.

In this example, everything tested is correct until gate G_3 is checked. The output of this gate is not correct as the differences in the waveforms indicate. An analysis of the waveforms indicates that if the D input to gate G_3 is open and acting as a HIGH, you will get the output waveform measured (shown in red). Notice that the output of G_4 is also incorrect due to the incorrect input from G_3 .

Replace the IC containing G_3 , and check the circuit's operation again.

RELATED PROBLEM

For the inputs in Figure 36(b), determine the output waveform for the logic circuit (output of G_4) if the inverter has an open output.

SECTION 8 CHECKUP

1. List four common internal failures in logic gates.
 - (a) one input to G_1 shorted to ground
 - (b) the inverter input shorted to ground
2. One input of a NOR gate is externally shorted to $+V_{CC}$. How does this condition affect the gate operation?
 - (c) an open output in G_3
3. Determine the output of gate G_4 in Figure 36(a), with inputs as shown in part (b), for the following faults:

SUMMARY

- AND-OR logic produces an output expression in SOP form.
- AND-OR-Invert logic produces a complemented SOP form, which is actually a POS form.
- The operational symbol for exclusive-OR is \oplus . An exclusive-OR expression can be stated in two equivalent ways:

$$A\bar{B} + \bar{A}B = A \oplus B$$

- To describe a logic circuit, start with the logic circuit, and develop the Boolean output expression or the truth table or both.
- Implementation of a logic circuit is the process in which you start with the Boolean output expressions or the truth table and develop a logic circuit that produces the output function.
- DeMorgan's theorems:
 1. The complement of a product is equal to the sum of the complements of the terms in the product.

$$\overline{XY} = \bar{X} + \bar{Y}$$

2. The complement of a sum is equal to the product of the complements of the terms in the sum.

$$\overline{X + Y} = \bar{X}\bar{Y}$$

- NAND and negative-OR operations are equivalent.
- NOR and negative-AND operations are equivalent.
- In the structural approach, a VHDL component is a predefined logic function stored for use throughout a program or in other programs.
- A component instantiation is used to call for a component in a program.
- A VHDL signal effectively acts as an internal interconnection in a VHDL structural description.

KEY TERMS

Component A VHDL feature that can be used to predefine a logic function for multiple use throughout a program or programs.

Node A common connection point in a circuit in which a gate output is connected to one or more gate inputs.

POS Product-of-sums; a form of Boolean expression that is basically the ANDing of ORed terms.

Signal A waveform; a type of VHDL object that holds data.

Signal tracing A troubleshooting technique in which waveforms are observed in a step-by-step manner beginning at the input and working toward the output or vice versa. At each point the observed waveform is compared with the correct signal for that point.

SOP Sum-of-products; a form of Boolean expression that is basically the ORing of ANDed terms.

Universal gate Either a NAND gate or a NOR gate. The term *universal* refers to the property of a gate that permits any logic function to be implemented by that gate or by a combination of that kind.

TRUE/FALSE QUIZ

Answers are at the end of the chapter.

1. AND-OR logic can have only two 2-input AND gates.
2. If the inputs of an exclusive-OR gate are the same, the output is HIGH (1).
3. If the inputs of an exclusive-NOR gate are different, the output is LOW (0).
4. A parity generator can be implemented using exclusive-OR gates.
5. NAND gates cannot be used to produce the OR function.
6. NOR gates can be used to produce the AND function.
7. Any SOP expression can be implemented using only NAND gates.

8. The dual symbol for a NAND gate is a negative-AND symbol.
9. Negative-OR is equivalent to NAND.
10. Data flow and structural are two approaches to writing VHDL programs.

SELF-TEST

Answers are at the end of the chapter.

1. The output expression for an AND-OR circuit having one AND gate with inputs $A, B, C,$ and D and one AND gate with inputs E and F is
 - (a) $ABCDEF$
 - (b) $A + B + C + D + E + F$
 - (c) $(A + B + C + D)(E + F)$
 - (d) $ABCD + EF$
2. A logic circuit with an output $X = A\bar{B}C + A\bar{C}$ consists of
 - (a) two AND gates and one OR gate
 - (b) two AND gates, one OR gate, and two inverters
 - (c) two OR gates, one AND gate, and two inverters
 - (d) two AND gates, one OR gate, and one inverter
3. To implement the expression $\bar{A}BCD + A\bar{B}CD + ABC\bar{D}$, it takes one OR gate and
 - (a) one AND gate
 - (b) three AND gates
 - (c) three AND gates and four inverters
 - (d) three AND gates and three inverters
4. The output expression for an AND-OR-Invert circuit having one AND gate with inputs $A, B, C,$ and D and one AND gate with inputs E and F is

(a) $ABCD + EF$	(b) $\bar{A} + \bar{B} + \bar{C} + \bar{D} + \bar{E} + \bar{F}$
(c) $(A + B + C + D)(E + F)$	(d) $(\bar{A} + \bar{B} + \bar{C} + \bar{D})(\bar{E} + \bar{F})$
5. An exclusive-OR function is expressed as

(a) $\bar{A}\bar{B} + AB$	(b) $\bar{A}B + A\bar{B}$
(c) $(\bar{A} + B)(A + \bar{B})$	(d) $(\bar{A} + \bar{B}) + (A + B)$
6. The AND operation can be produced with

(a) two NAND gates	(b) three NAND gates
(c) one NOR gate	(d) three NOR gates
7. The OR operation can be produced with

(a) two NOR gates	(b) three NAND gates
(c) four NAND gates	(d) both answers (a) and (b)
8. All Boolean expressions can be implemented with
 - (a) NAND gates only
 - (b) NOR gates only
 - (c) combinations of NAND and NOR gates
 - (d) combinations of AND gates, OR gates, and inverters
 - (e) any of these
9. A VHDL component
 - (a) can be used once in each program
 - (b) is a predefined description of a logic function
 - (c) can be used multiple times in a program
 - (d) is part of a data flow description
 - (e) answers (b) and (c)
10. A VHDL component is called for use in a program by using a
 - (a) signal
 - (b) variable
 - (c) component instantiation
 - (d) architecture declaration

PROBLEMS

Answers to odd-numbered problems are at the end of the chapter.

SECTION 1 Basic Combinational Logic Circuits

1. Draw the ANSI distinctive shape logic diagram for a 3-wide, 4-input AND-OR-Invert circuit. Also draw the ANSI standard rectangular outline symbol.
2. Write the output expression for each circuit in Figure 37.
3. Write the output expression for each circuit as it appears in Figure 38.

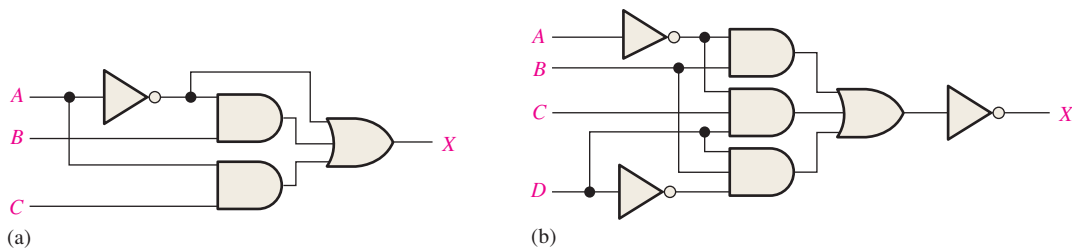


FIGURE 37

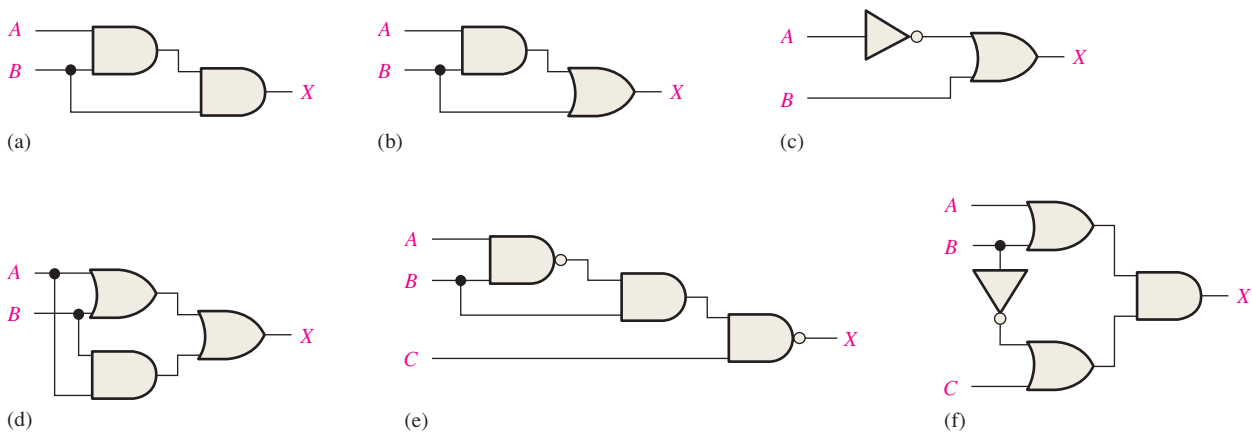


FIGURE 38

4. Develop the truth table for each circuit in Figure 38.
5. Develop the truth table for each circuit in Figure 39 on the next page.

SECTION 2 Boolean Expressions and Truth Tables

6. Develop an AND-OR-Invert logic circuit for a power saw that removes power (logic 0) if the guard is not in place (logic 0) and the switch is *on* (logic 1) or the switch is *on* and the motor is too hot (logic 1).
7. An AND-OR-Invert logic chip has two 4-input AND gates connected to a 2-input NOR gate. Write the Boolean expression for the circuit (assume the inputs are labeled *A* through *H*).
8. Use AND gates, OR gates, or combinations of both to implement the following logic expressions as stated:

(a) $X = AB$	(b) $X = A + B$
(c) $X = AB + C$	(d) $X = ABC + D$
(e) $X = A + B + C$	(f) $X = ABCD$
(g) $X = A(CD + B)$	(h) $X = AB(C + DEF) + CE(A + B + F)$
9. Use AND gates, OR gates, and inverters as needed to implement the following logic expressions as stated:

(a) $X = AB + \bar{B}C$	(b) $X = A(B + \bar{C})$
(c) $X = \bar{A}B + AB$	(d) $X = \bar{A}BC + B(EF + \bar{G})$
(e) $X = A[BC(A + B + C + D)]$	(f) $X = B(C\bar{D}E + \bar{E}FG)(\bar{A}B + C)$

COMBINATIONAL LOGIC

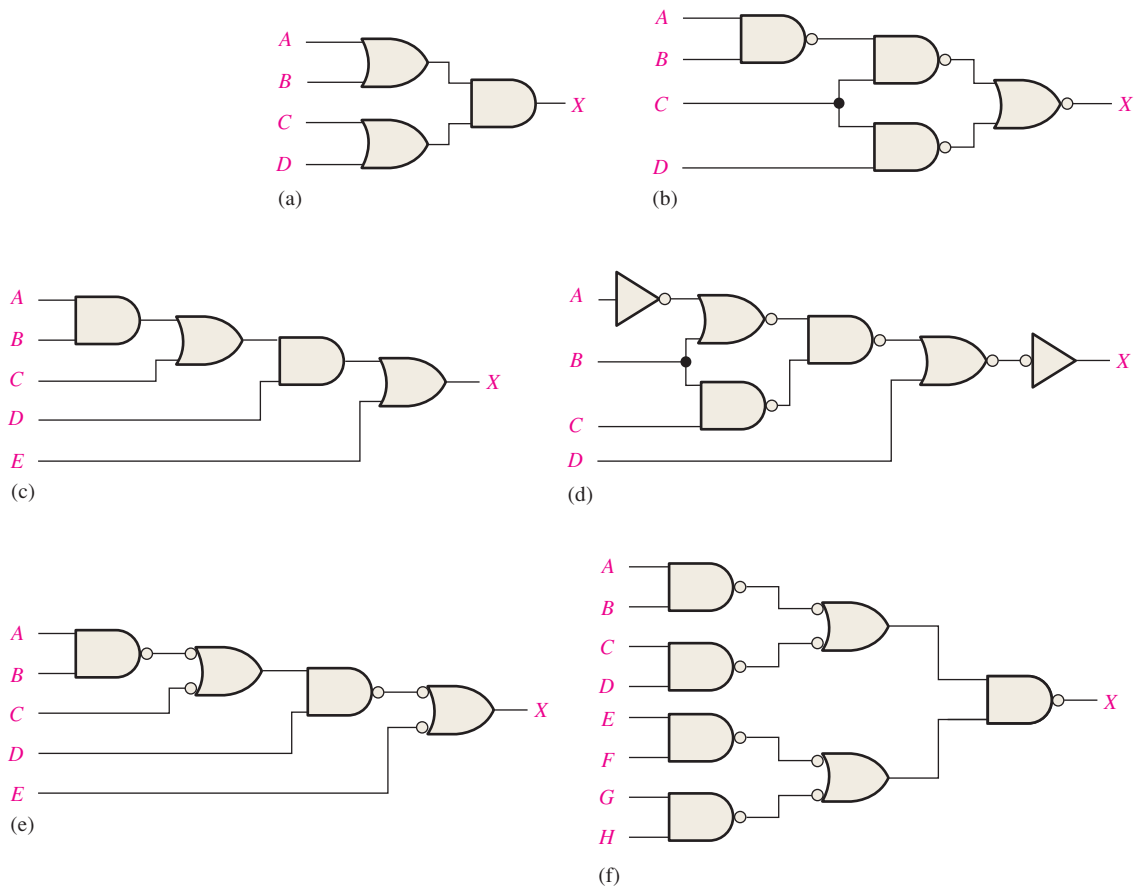


FIGURE 39

- 10.** Use NAND gates, NOR gates, or combinations of both to implement the following logic expressions as stated:
- (a) $X = \bar{A}B + CD + (\bar{A} + \bar{B})(ACD + \bar{B}E)$
 - (b) $X = ABC\bar{D} + D\bar{E}F + \bar{A}F$
 - (c) $X = \bar{A}[B + \bar{C}(D + E)]$
- 11.** Write the logic expression for the truth table in Table 10. Determine the number and the types of gates required.

TABLE 10			
INPUTS			OUTPUT
A	B	C	X
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	1

12. Write the logic expression for the truth table in Table 11. Determine the number and the types of gates required.

TABLE 11				
INPUTS				OUTPUT
A	B	C	D	X
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	1
0	1	0	0	1
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	1

13. Develop a truth table for each of the following standard SOP expressions:
 (a) $\overline{A}BC + \overline{A}B\overline{C} + ABC$ (b) $\overline{X}Y\overline{Z} + \overline{X}Y\overline{Z} + XY\overline{Z} + X\overline{Y}Z + \overline{X}YZ$
14. Develop a truth table for each of the following standard SOP expressions:
 (a) $\overline{A}BCD + \overline{A}BC\overline{D} + \overline{A}B\overline{C}D + \overline{A}B\overline{C}\overline{D}$
 (b) $WXYZ + WXY\overline{Z} + \overline{W}XYZ + W\overline{X}YZ + WX\overline{Y}Z$
15. For each truth table in Table 12 on page 214, derive a standard SOP and a standard POS expression.

SECTION 3 DeMorgan's Theorems

16. Apply DeMorgan's theorems to each expression:
 (a) $\overline{A + B}$
 (b) \overline{AB}
 (c) $\overline{A + B + C}$
 (d) \overline{ABC}
 (e) $\overline{A(B + C)}$
 (f) $\overline{AB + CD}$
 (g) $\overline{AB + CD}$
 (h) $\overline{(A + B)(C + D)}$
17. Apply DeMorgan's theorems to each expression:
 (a) $\overline{AB(C + D)}$
 (b) $\overline{AB(CD + EF)}$
 (c) $\overline{(A + B + C + D) + ABCD}$
 (d) $\overline{(\overline{A + B + C + D})(\overline{AB\overline{CD}})}$
 (e) $\overline{AB(CD + EF)(\overline{AB + CD})}$

TABLE 12																	
A	B	C	X	A	B	C	X	A	B	C	D	X	A	B	C	D	X
0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	
0	0	1	1	0	0	1	0	0	0	0	1	1	0	0	0	1	
0	1	0	0	0	1	0	0	0	0	1	0	0	0	0	1	0	
0	1	1	0	0	1	1	0	0	0	1	1	1	0	0	1	0	
1	0	0	1	1	0	0	0	0	1	0	0	0	0	1	0	0	
1	0	1	1	1	0	1	1	0	1	0	1	1	0	1	0	1	
1	1	0	0	1	1	1	0	1	0	1	0	1	0	1	0	0	
1	1	1	1	1	1	1	1	0	1	1	1	0	0	1	1	1	
								1	0	0	0	0	1	0	0	0	
								1	0	0	1	1	0	0	1	0	
								1	0	1	0	0	0	1	0	0	
								1	0	1	1	0	1	1	1	1	
								1	1	0	0	1	0	0	0	1	
								1	1	0	1	0	0	1	0	0	
								1	1	1	0	0	0	1	0	0	
								1	1	1	1	0	1	1	1	1	

(a)

(b)

(c)

(d)

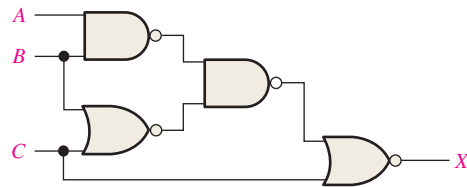
18. Apply DeMorgan's theorems to the following:

- (a) $\overline{(\overline{ABC})(\overline{EFG})} + \overline{(\overline{HIJ})(\overline{KLM})}$
- (b) $\overline{(A + \overline{BC} + CD) + \overline{BC}}$
- (c) $\overline{\overline{(A + B)(C + D)(E + F)(G + H)}}$

SECTION 4 The Universal Property of NAND and NOR Gates

- 19. Implement the logic circuits in Figure 37 using only NAND gates.
- 20. Implement the logic circuit in Figure 40 using only NAND gates.

FIGURE 40



- 21. Repeat Problem 19 using only NOR gates.
- 22. Repeat Problem 20 using only NOR gates.

SECTION 5 Pulse Waveform Operation

23. Given the logic circuit and the input waveforms in Figure 41, draw the output waveform.

FIGURE 41



COMBINATIONAL LOGIC

24. For the logic circuit in Figure 42, draw the output waveform in proper relationship to the inputs.

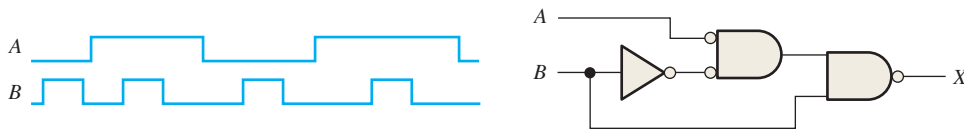


FIGURE 42

25. For the input waveforms in Figure 43, what logic circuit will generate the output waveform shown?

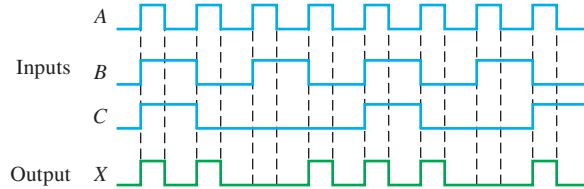


FIGURE 43

26. Repeat Problem 25 for the waveforms in Figure 44.

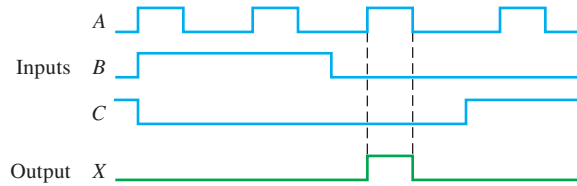


FIGURE 44

27. For the circuit in Figure 45, draw the waveforms at the numbered points in the proper relationship to each other.

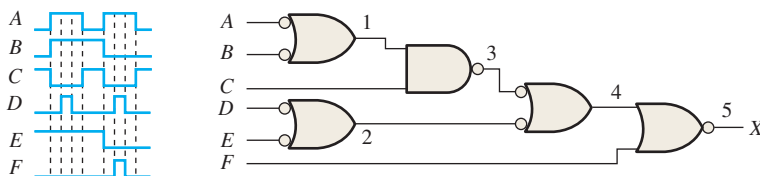


FIGURE 45

28. Assuming a propagation delay through each gate of 10 nanoseconds (ns), determine if the desired output waveform X in Figure 46 (a pulse with a minimum $t_{PW} = 25$ ns positioned as shown) will be generated properly with the given inputs.

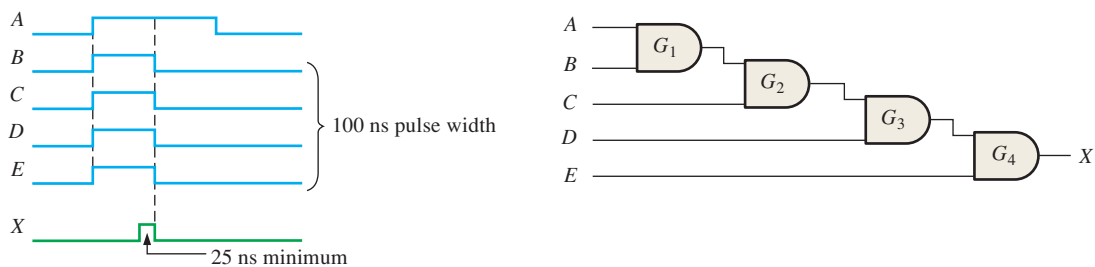


FIGURE 46

SECTION 6 Combinational Logic with VHDL and Verilog

29. Describe a 3-input AND gate with VHDL and Verilog.
30. Write a VHDL program using the data flow approach (Boolean expressions) to describe the logic circuit in Figure 37(b). Write a Verilog program.
31. Write VHDL programs using the data flow approach (Boolean expressions) for the logic circuits in Figure 38(e) and (f). Write a Verilog program for both circuits.
32. Write a VHDL program using the structural approach for the logic circuit in Figure 39(d). Assume component declarations for each type of gate are already available. Write a Verilog program.
33. Repeat Problem 32 for the logic circuit in Figure 39(f).
34. Describe the logic represented by the truth table in Table 10 using VHDL and Verilog.
35. Develop a VHDL program for the logic in Figure 47(a), using both the data flow and the structural approach. Compare the resulting programs. Write the program in Verilog.
36. Develop a VHDL program for the logic in Figure 47(b), using both the data flow and the structural approach. Compare the resulting programs. Write the program in Verilog.

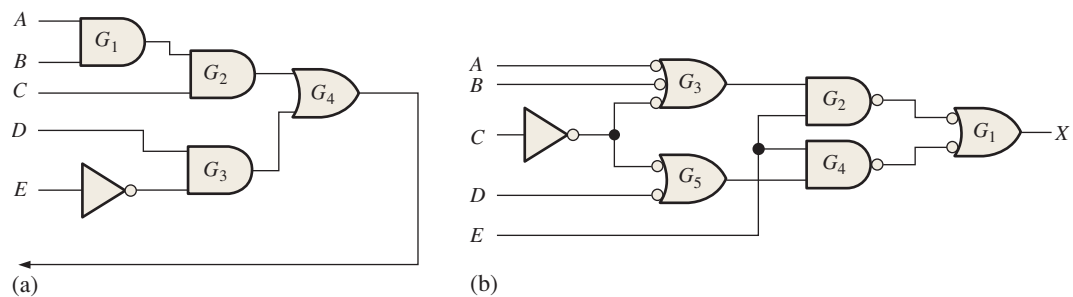


FIGURE 47

37. Given the following VHDL program, create the truth table that describes the logic circuit.

```

entity CombLogic is
    port (A, B, C, D: in bit; X: out bit);
end entity CombLogic;

architecture Example of CombLogic is
    begin
        X <= not((not A and not B) or (not A and not C) or (not A and not D) or
                (not B and not C) or (not B and not D) or (not D and not C));
    end architecture Example;
    
```

38. Describe the logic circuit shown in Figure 48 with a VHDL program, using the data flow approach.

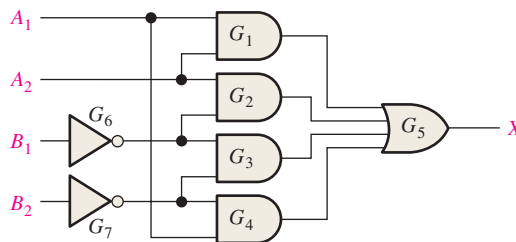


FIGURE 48

39. Repeat Problem 38 using the VHDL structural approach.

SECTION 7 A System

40. Implement the inlet valve logic using NOR gates and inverters.
41. Repeat Problem 40 for the outlet valve logic.

- 42. Implement the temperature control logic using XNOR gates.
- 43. Show a circuit to enable an additive to be introduced into the syrup through another inlet only when the temperature is at the specified value and the syrup is at the low-level sensor.

SECTION 8 Troubleshooting

- 44. For the logic circuit and the input waveforms in Figure 49, the indicated output waveform is observed. Determine if this is the correct output waveform.

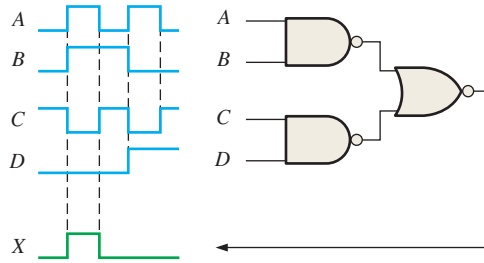


FIGURE 49

- 45. The output waveform in Figure 50 is incorrect for the inputs that are applied to the circuit. Assuming that one gate in the circuit has failed, with its output either an apparent constant HIGH or a constant LOW, determine the faulty gate and the type of failure (output open or shorted).

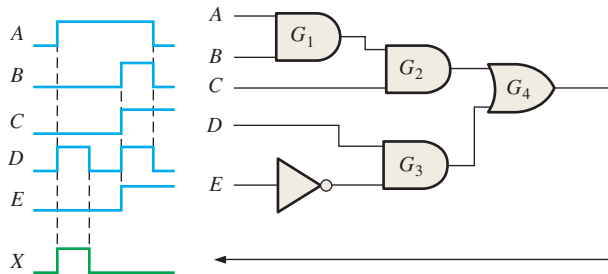


FIGURE 50

- 46. Repeat Problem 45 for the circuit in Figure 51, with input and output waveforms as shown.

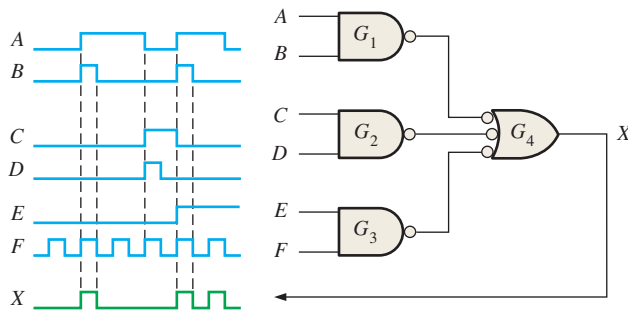


FIGURE 51

- 47. Figure 52(a) is a logic circuit under test. Figure 52(b) shows the waveforms as observed on a logic analyzer. The output waveform is incorrect for the inputs that are applied to the circuit. Assuming that one gate in the circuit has failed, with its output either an apparent constant HIGH or a constant LOW, determine the faulty gate and the type of failure.

COMBINATIONAL LOGIC

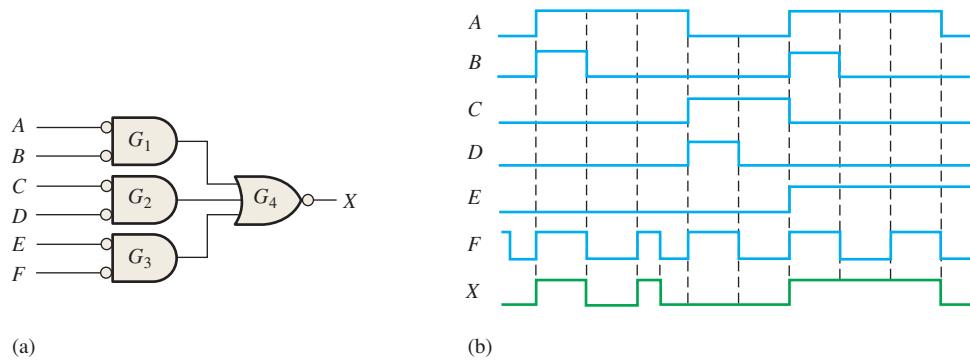


FIGURE 52

48. The logic circuit in Figure 53 has the input waveforms shown.
- Determine the correct output waveform in relation to the inputs.
 - Determine the output waveform if the output of gate G_3 is open.
 - Determine the output waveform if the upper input to gate G_5 is shorted to ground.

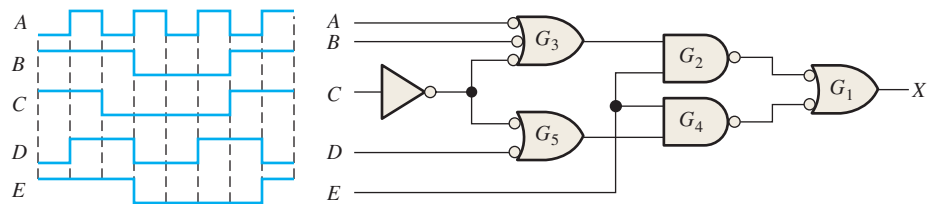


FIGURE 53

49. The logic circuit in Figure 54 has only one intermediate test point available besides the output, as indicated. For the inputs shown, you observe the indicated waveform at the test point. Is this waveform correct? If not, what are the possible faults that would cause it to appear as it does?

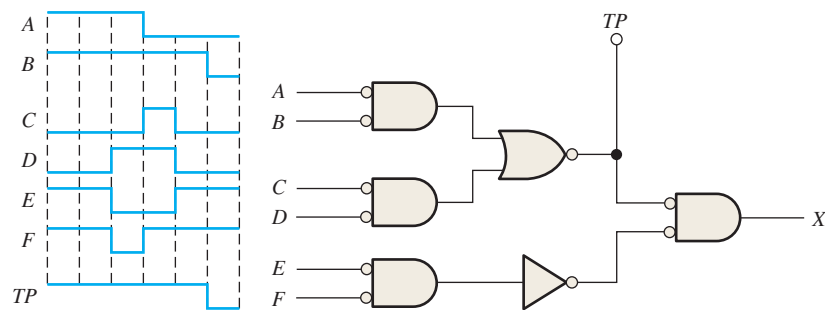


FIGURE 54

Special Problems

50. Develop a logic circuit to produce a HIGH output only if the input, represented by a 4-bit binary number, is greater than twelve or less than three. First develop the truth table and then draw the logic diagram.
51. Develop the logic circuit necessary to meet the following requirements:
A battery-powered lamp in a room is to be operated from two switches, one at the back door and one at the front door. The lamp is to be on if the front switch is on and the back switch is off, or if the front switch is off and the back switch is on. The lamp is to be off if both switches are off or if both switches are on. Let a HIGH output represent the on condition and a LOW output represent the off condition.
52. Develop the NAND logic for a hexadecimal keypad encoder that will convert each key closure to binary.

MULTISIM TROUBLESHOOTING PRACTICE

MULTISIM



53. Open file P04-53 and follow the instructions given there.
54. Open file P04-54 and follow the instructions given there.
55. Open file P04-55 and follow the instructions given there.
56. Open file P04-56 and follow the instructions given there.

ANSWERS TO SECTION CHECKUPS

SECTION 1 Basic Combinational Logic Circuits

1. (a) $\overline{AB} + \overline{CD} = \overline{1 \cdot 0} + \overline{1 \cdot 0} = 1$
 (b) $\overline{AB} + \overline{CD} = \overline{1 \cdot 1} + \overline{0 \cdot 1} = 0$
 (c) $\overline{AB} + \overline{CD} = 0 \cdot 1 + 1 \cdot 1 = 0$
2. (a) $\overline{AB} + \overline{AB} = 1 \cdot \overline{0} + \overline{1} \cdot 0 = 1$ (b) $\overline{AB} + \overline{AB} = 1 \cdot \overline{1} + \overline{1} \cdot 1 = 0$
 (c) $\overline{AB} + \overline{AB} = 0 \cdot \overline{1} + \overline{0} \cdot 1 = 1$ (d) $\overline{AB} + \overline{AB} = 0 \cdot \overline{0} + \overline{0} \cdot 0 = 0$
3. $X = 1$ when $ABC = 000, 011, 101, 110,$ and 111 ; $X = 0$ when $ABC = 001, 010,$ and 100
4. $X = AB + \overline{A}\overline{B}$; the circuit consists of two AND gates, one OR gate, and two inverters. See Figure 5(b) for diagram.

SECTION 2 Boolean Expressions and Truth Tables

1. (a) $X = ABC + AB + AC$: three AND gates, one OR gate
 (b) $X = AB(C + DE)$: three AND gates, one OR gate
2. $X = ABC + \overline{A}\overline{B}\overline{C}$; two AND gates, one OR gate, and three inverters
3. $A + B(C + D)$

4.

A	B	C	X
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

SECTION 3 DeMorgan's Theorems

1. (a) $\overline{A} + \overline{B} + \overline{C} + \overline{DE}$
 (b) $\overline{A}\overline{B}\overline{C}$
 (c) $\overline{A}\overline{B}\overline{C} + (D + E)$

SECTION 4 The Universal Property of NAND and NOR Gates

1. (a) $X = \overline{A} + B$: a 2-input NAND gate with A and \overline{B} on its inputs.
 (b) $X = \overline{AB}$: a 2-input NAND with A and \overline{B} on its inputs, followed by one NAND used as an inverter.
2. (a) $X = \overline{A} + B$: a 2-input NOR with inputs \overline{A} and B , followed by one NOR used as an inverter.
 (b) $X = \overline{AB}$: a 2-input NOR with \overline{A} and B on its inputs.

SECTION 5 Pulse Waveform Operation

1. The exclusive-OR output is a 15 μs pulse followed by a 25 μs pulse, with a separation of 10 μs between the pulses.
2. The output of the exclusive-NOR is HIGH when both inputs are HIGH or when both inputs are LOW.

SECTION 6 Combinational Logic with VHDL and Verilog

1. An entity defines inputs and outputs.
2. An architecture defines type of circuit.
3. Module
4. Data flow and structural (behavioral is a third type)
5. A VHDL component is a predefined program describing a specified logic function.
6. A component instantiation is used to call for a specified component in a program architecture.
7. Interconnections between components are made using VHDL signals.
8. Components are used in the structural approach.

SECTION 7 A System

1. Three
2. Two
3. The outlet valve control depends on the temperature where the inlet valve does not.
4. The outlet valve turns off when there is no inlet flow and the level is above minimum.

SECTION 8 Troubleshooting

1. Common gate failures are input or output open; input or output shorted to ground.
2. Input shorted to V_{CC} causes output to be stuck LOW.
3. (a) G_4 output is HIGH until rising edge of seventh pulse, then it goes LOW.
 (b) G_4 output is the same as input D .
 (c) G_4 output is the inverse of the G_2 output shown in Figure 36(b).

ANSWERS TO RELATED PROBLEMS FOR EXAMPLES

- 1 The same as Figure 10 without the inverters
- 2 There is only one complemented variable for each AND gate.
- 3 Multisim results should agree with Figure 13.
- 4 $\overline{\overline{X}} + \overline{\overline{Y}} + \overline{\overline{Z}} = XYZ$
- 5 $\overline{\overline{W}} \overline{\overline{X}} \overline{\overline{Y}} \overline{\overline{Z}} = W + X + Y + Z$
- 6 See Figure 55.
- 7 See Figure 56.

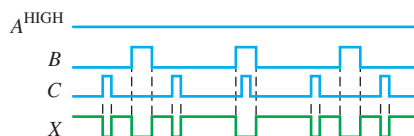


FIGURE 55

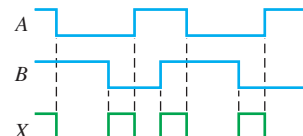


FIGURE 56

- 8 See Figure 57.
- 9 See Figure 58.

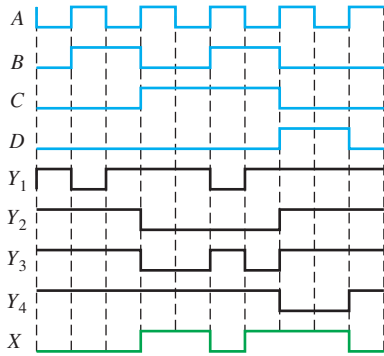


FIGURE 57

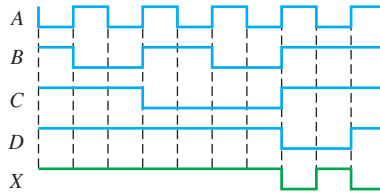


FIGURE 58

10

VHDL

```
entity ANDORlogic is
  port (A, B, C, D, E, F, G, H: in bit; X: out bit);
end entity ANDORlogic;
architecture ANDORfunction of ANDORLogic is
begin
  X <= (A and B) or (C and D) or (E and F) or
    (G and H);
end architecture ANDORfunction;
```

Verilog

```
module ANDORlogic (A, B, C, D, E, F, G, H, X);
  input A, B, C, D, E, F, G, H;
  output X;
  assign X = (A && B) || (C && D) || (E && F) ||
    (G && H);
endmodule
```

11

VHDL

```
entity Combo_Logic is
  port (A, B, C, D, E, F: in bit; X: out bit);
end entity Combo_Logic;
architecture Logic_Function of Combo_Logic is
begin
  X <= not(not(not A and not B) or C) and
    not(not(not D and not E) or F);
end architecture Logic_Function;
```

Verilog

```
module Combo_Logic (A, B, C, D, E, F, X);
  input A, B, C, D, E, F;
  output X;
  assign X = !(!(A && !B) || C) && !(!(D && !E) ||
    F);
endmodule
```

12

VHDL

```
entity Table_7 is
  port (A, B, C, D: in bit; X: out bit);
end entity Table_7;
architecture Logic_Function of Table_7 is begin
  X <= (not A and not B and not C and not D)
    or (A and not B and C and D) or (A and B
    and not C and not D) or (A and B and not C
    and D) or (A and B and C and not D) or (A
    and B and C and D);
end architecture Logic_Function;
```

Verilog

```
module Combo_Logic (A, B, C, D, X);
  input A, B, C, D;
  output X;
  assign X = (!A && !B && !C && !D) || (A && !B
    && C && D) || (A && B && !C && !D) || (A
    && B && !C && D) || (A && B && C &&
    !D) || (A && B && C && D);
endmodule
```

13 G5: NAND_gate2 port map (A => IN9, B => IN10, X => OUT5);

14 See Figure 59.

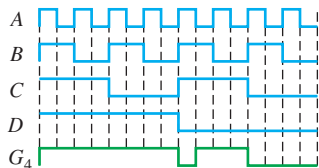


FIGURE 59

ANSWERS TO TRUE/FALSE QUIZ

1. F 2. F 3. T 4. T 5. F
 6. T 7. T 8. F 9. T 10. T

ANSWERS TO SELF-TEST

1. (d) 2. (b) 3. (c) 4. (d) 5. (b)
 6. (a) 7. (d) 8. (e) 9. (e) 10. (c)

ANSWERS TO ODD-NUMBERED PROBLEMS

1. See Figure P-16.

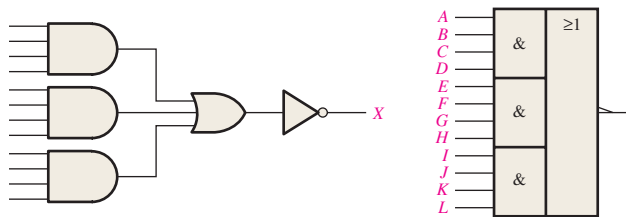


FIGURE P-16

3. (a) $X = ABB$
 (b) $X = AB + B$
 (c) $X = \bar{A} + B$
 (d) $X = (A + B) + AB$
 (e) $X = \overline{ABC}$
 (f) $X = (A + B)(\bar{B} + C)$

5. (a) See Table P-1. $X = (A + B)(C + D)$

TABLE P-1				
<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>X</i>
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

(b) See Table P-2. $X = \overline{\overline{ABC}} + \overline{CD}$

TABLE P-2				
<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>X</i>
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

COMBINATIONAL LOGIC

(c) See Table P-3. $X = (AB + C)D + E$

TABLE P-3					
<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>E</i>	<i>X</i>
0	0	0	0	0	0
0	0	0	0	1	1
0	0	0	1	0	0
0	0	0	1	1	1
0	0	1	0	0	0
0	0	1	0	1	1
0	0	1	1	0	1
0	0	1	1	1	1
0	1	0	0	0	0
0	1	0	0	1	1
0	1	0	1	0	0
0	1	0	1	1	1
0	1	1	0	0	0
0	1	1	0	1	1
0	1	1	1	0	1
0	1	1	1	1	1
1	0	0	0	0	0
1	0	0	0	1	1
1	0	0	1	0	0
1	0	0	1	1	1
1	0	1	0	0	0
1	0	1	0	1	1
1	0	1	1	0	1
1	0	1	1	1	1
1	1	0	0	0	0
1	1	0	0	1	1
1	1	0	1	0	1
1	1	0	1	1	1
1	1	1	0	0	0
1	1	1	0	1	1
1	1	1	1	0	1
1	1	1	1	1	1

(d) See Table P-4. $X = \overline{\overline{\overline{A + B}}(BC)} + D$

TABLE P-4				
<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>X</i>
0	0	0	0	1
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	1
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	0
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

(e) See Table P-5. $X = \overline{\overline{\overline{AB + C}}D} + \overline{E}$

TABLE P-5					
<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>E</i>	<i>X</i>
0	0	0	0	0	1
0	0	0	0	1	0
0	0	0	1	0	1
0	0	0	1	1	1
0	0	1	0	0	1
0	0	1	0	1	0
0	0	1	1	0	1
0	0	1	1	1	0
0	1	0	0	0	1
0	1	0	0	1	0
0	1	0	1	0	1
0	1	0	1	1	1

COMBINATIONAL LOGIC

TABLE P-5 (Continued)

<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>E</i>	<i>X</i>
0	1	1	0	0	1
0	1	1	0	1	0
0	1	1	1	0	1
0	1	1	1	1	0
1	0	0	0	0	1
1	0	0	0	1	0
1	0	0	1	0	1
1	0	0	1	1	1
1	0	1	0	0	1
1	0	1	0	1	0
1	0	1	1	0	1
1	0	1	1	1	0
1	1	0	0	0	1
1	1	0	0	1	0
1	1	0	1	0	1
1	1	0	1	1	1
1	1	1	0	0	1
1	1	1	0	1	0
1	1	1	1	0	1
1	1	1	1	1	1

5. (f) See Table P-6. $X = \overline{\overline{AB} + \overline{CD}}(\overline{EF} + \overline{GH})$

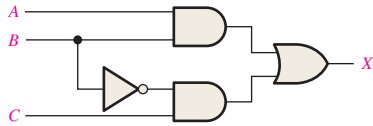
TABLE P-6

<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>E</i>	<i>F</i>	<i>G</i>	<i>H</i>	<i>X</i>
0	X	0	X	X	X	X	X	1
X	0	0	X	X	X	X	X	1
0	X	X	0	X	X	X	X	1
X	0	X	0	0	X	X	X	1
X	X	X	X	0	X	0	X	1
X	X	X	X	X	0	0	X	1
X	X	X	X	0	X	X	0	1
X	X	X	X	X	0	X	0	1

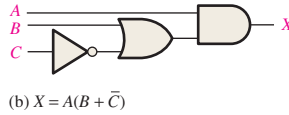
For all other entries $X = 0$.
X = don't care
 An abbreviated table is shown because
 there are 256 combinations.

7. $\overline{ABCD + EFGH}$

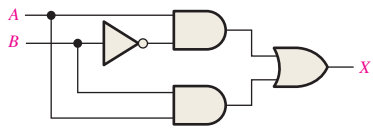
9. See Figure P-17.



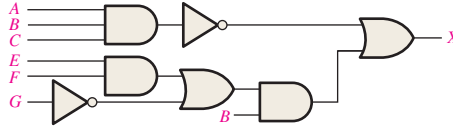
(a) $X = AB + \overline{B}C$



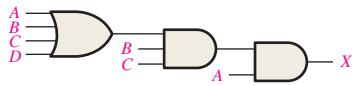
(b) $X = A(B + \overline{C})$



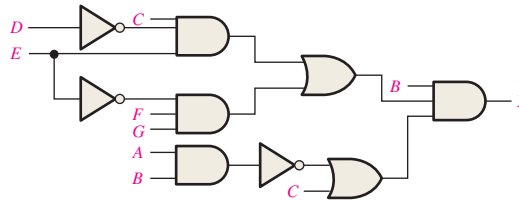
(c) $X = A\overline{B} + AB$



(d) $X = \overline{ABC} + B(EF + \overline{G})$



(e) $X = A[BC(A + B + C + D)]$



(f) $X = B(C\overline{D}E + \overline{E}FG)(\overline{A} + C)$

FIGURE P-17

11. $X = \overline{A}\overline{B}\overline{C} + \overline{A}\overline{B}C + \overline{A}B\overline{C} + A\overline{B}\overline{C} + ABC$
 Five 3-input AND gates, one 5-input OR gate, and three inverters.
13. (a) See Table P-7.
 (b) See Table P-8.

TABLE P-7			
A	B	C	X
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

TABLE P-8			
X	Y	Z	Q
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0

15. (a) $X = \overline{A}\overline{B}\overline{C} + \overline{A}\overline{B}C + \overline{A}B\overline{C} + ABC$
 $X = (A + B + C)(A + \overline{B} + C)(A + \overline{B} + \overline{C})(\overline{A} + \overline{B} + C)$
- (b) $X = ABC\overline{D} + \overline{A}\overline{B}C + ABC$
 $X = (A + B + C)(A + B + \overline{C})(A + \overline{B} + C)(A + \overline{B} + \overline{C})(\overline{A} + B + C)$
- (c) $X = \overline{A}\overline{B}\overline{C}\overline{D} + \overline{A}\overline{B}C\overline{D} + \overline{A}B\overline{C}\overline{D} + \overline{A}BC\overline{D} + \overline{A}B\overline{C}D + \overline{A}BCD + AB\overline{C}\overline{D} + ABC\overline{D}$
 $X = (A + B + \overline{C} + D)(A + \overline{B} + C + D)(A + \overline{B} + \overline{C} + \overline{D})(\overline{A} + B + C + D)(\overline{A} + B + \overline{C} + D)(\overline{A} + B + \overline{C} + \overline{D})(\overline{A} + B + C + \overline{D})(\overline{A} + B + C + D)$
- (d) $X = \overline{A}\overline{B}\overline{C}\overline{D} + \overline{A}\overline{B}C\overline{D} + \overline{A}B\overline{C}\overline{D} + \overline{A}BC\overline{D} + \overline{A}B\overline{C}D + \overline{A}BCD + AB\overline{C}\overline{D} + ABC\overline{D}$
 $X = (A + B + C + D)(A + B + C + \overline{D})(A + B + \overline{C} + \overline{D})(A + \overline{B} + \overline{C} + D)(\overline{A} + B + C + D)(\overline{A} + B + C + \overline{D})(\overline{A} + B + \overline{C} + D)(\overline{A} + B + C + D)$
17. (a) $\overline{A} + B + \overline{C}D$
 (b) $\overline{A} + \overline{B} + (\overline{C} + \overline{D})(\overline{E} + \overline{F})$

COMBINATIONAL LOGIC

- (c) $\bar{A}\bar{B}\bar{C}D + \bar{A} + \bar{B} + \bar{C} + D$
- (d) $\bar{A} + B + C + D + \bar{A}\bar{B}\bar{C}D$
- (e) $AB + (\bar{C} + \bar{D})(E + \bar{F}) + ABCD$

19. See Figure P-18.

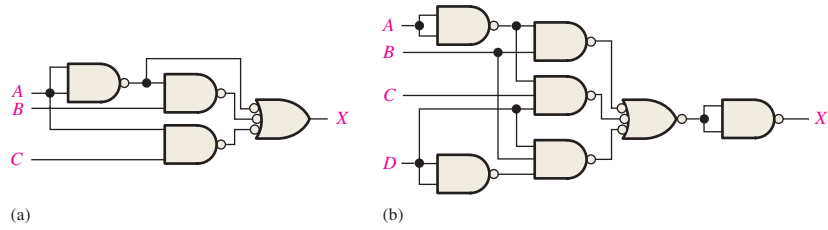


FIGURE P-18

21. See Figure P-19.

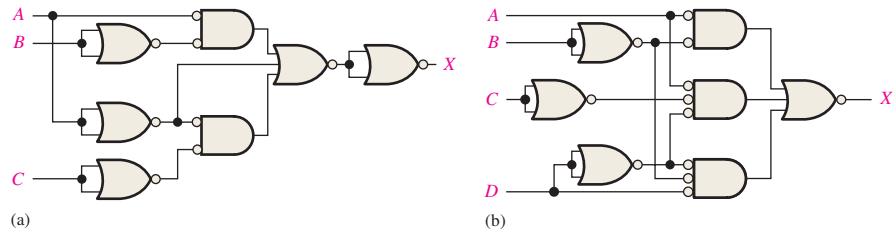


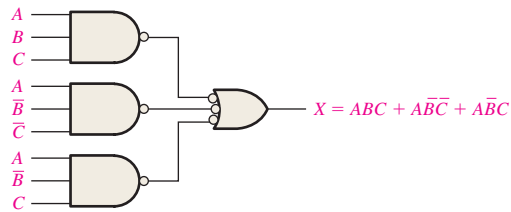
FIGURE P-19

23. $X = \overline{\bar{A} + \bar{B} + B} = \overline{A\bar{B}} = 0$
The output X is always LOW.

25. X is HIGH when ABC are all HIGH or when A is HIGH and B is LOW and C is LOW or when A is HIGH and B is LOW and C is HIGH.
 $X = ABC + \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C$

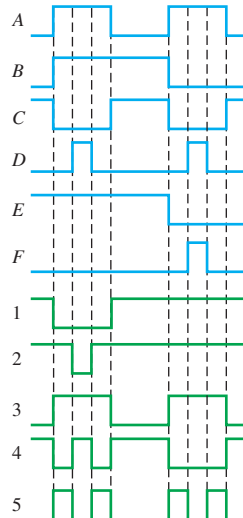
See Figure P-20.

FIGURE P-20



27. See Figure P-21.

FIGURE P-21



29. $X \leq A \text{ and } B \text{ and } C$; $X = A \ \&\& \ B \ \&\& \ C$;

31. VHDL for 38(e):

```
entity Circuit_4_38e is
```

```

    port (A, B, C: in bit; X: out bit);
end entity Circuit4_38e;
architecture LogicFunction of Circuit4_38e is
begin
    X <= ((A nand B) and B) nand C;
end architecture LogicFunction;

```

Verilog for Figure 38(e):

```

module Circuit4_38e (A, B, C, X);
input (A, B, C);
output X;
assign X = !(((A && B)) && B) && C);
endmodule

```

VHDL for 38(f):

```

entity Circuit4_38f is
    port (A, B, C: in bit; X: out bit);
end entity Circuit4_38f;
architecture LogicFunction of Circuit4_38f is
begin
    X <= (A or B) and (not B or C);
end architecture LogicFunction;

```

Verilog for Figure 38(f):

```

module Circuit4_38f (A, B, C, X);
input (A, B, C);
output X;
assign X = (A || B) && (! B || C);
endmodule

```

33. Number gates from top to bottom and left to right G1, G2, G3, etc. Relabel inputs IN1, IN2, IN3, etc. and output OUT.

```

entity Circuit4_39f is
    port (IN1, IN2, IN3, IN4, IN5, IN6, IN7, IN8: in bit;
        OUT: out bit);
end entity Circuit4_39f;
architecture LogicFunction of Circuit4_39f is
component NAND_gate is
    port (A, B: in bit; X: out bit);
end component NAND_gate;
    signal G1OUT, G2OUT, G3OUT, G4OUT, G5OUT,
        G6OUT: bit;
begin
    G1: NAND_gate port map (A => IN1, B => IN2, X => G1OUT);
    G2: NAND_gate port map (A => IN3, B => IN4, X => G2OUT);
    G3: NAND_gate port map (A => IN5, B => IN6, X => G3OUT);
    G4: NAND_gate port map (A => IN7, B => IN8, X => G4OUT);
    G5: NAND_gate port map (A => G1OUT, B => G2OUT, X => G5OUT);
    G6: NAND_gate port map (A => G3OUT, B => G4OUT, X => G6OUT);
    G7: NAND_gate port map (A => G5OUT, B => G6OUT, X => OUT);
end architecture LogicFunction;

```

Verilog for 39(f):

```

module Circuit4_39f (A, B, C, D, E, F, G, H, X);
input (A, B, C, D, E, F, G, H);
output X;
assign X = !(((A && B) || (C && D)) && ((E && F) || (G && H)));
endmodule

```

35. Data flow approach

```

entity Fig_47a is
    port (A, B, C, D, E: in bit; X: out bit);
end entity Fig_47a;
architecture DataFlow of Fig_47a is
begin

```

COMBINATIONAL LOGIC

```

X <= (A and B and C) or (D and not E);
end architecture DataFlow;
Structural approach
entity Fig_47a is
  port (IN1, IN2, IN3, IN4, IN5: in bit; OUT: out bit);
end entity Fig_47a;
architecture Structure of Fig_47a is
  component AND_gate is
    port (A, B: in bit; X: out bit);
  end component AND_gate;
  component OR_gate is
    port (A, B: in bit; X: out bit);
  end component OR_gate;
  component Inverter is
    port (A: in bit; X: out bit);
  end component Inverter;
  signal G1OUT, G2OUT, G3OUT, INVOUT: bit;
begin
  G1: AND_gate port map (A => IN1, B => IN2, X => G1OUT);
  G2: AND_gate port map (A => G1OUT, B => IN3, X => G2OUT);
  INV: Inverter port map (A => IN5, X => INVOUT);
  G3: AND_gate port map (A => IN4, B => INVOUT, X => G3OUT);
  G4: OR_gate port map (A => G2OUT, B => G3OUT, X => OUT);
end architecture Structure;

Verilog for 47(a):
module Circuit_47a (A, B, C, D, E, X);
input (A, B, C, D, E);
output X;
assign X = ((A && B) && C) || (D && !E);
endmodule

```

37. See Table P-9.

TABLE P-9				
INPUTS				OUTPUT
A	B	C	D	X
0	0	0	0	0
1	0	0	0	0
0	1	0	0	0
1	1	0	0	0
0	0	1	0	0
1	0	1	0	0
0	1	1	0	0
1	1	1	0	0
0	0	0	1	0
1	0	0	1	0
0	1	0	1	0
1	1	0	1	1
0	0	1	1	0
1	0	1	1	1
0	1	1	1	1
1	1	1	1	1

39. The AND gates are numbered top to bottom G1, G2, G3, G4. The OR gate is G5 and the inverters are, top to bottom, G6 and G7. Change A_1, A_2, B_1, B_2 to IN1, IN2, IN3, IN4 respectively. Change X to OUT.

```

entity Circuit4_48 is
  port (IN1, IN2, IN3, IN4: in bit; OUT: out bit);
end entity Circuit4_48;
architecture Logic of Circuit4_48 is
  component AND_gate is
    port (A, B: in bit; X: out bit);
  end component AND_gate;
  component OR_gate is
    port (A, B, C, D: in bit; X: out bit);
  end component OR_gate;
  component Inverter is
    port (A: in bit; X: out bit);
  end component Inverter;
  signal G1OUT, G2OUT, G3OUT, G4OUT, G5OUT, G6OUT, G7OUT: bit;
begin
  G1: AND_gate port map (A => IN1, B => IN2, X => G1OUT);
  G2: AND_gate port map (A => IN2, B => G6OUT, X => G2OUT);
  G3: AND_gate port map (A => G6OUT, B => G7OUT, X => G3OUT);
  G4: AND_gate port map (A => G7OUT, B => IN1, X => G4OUT);
  G5: OR_gate port map (A => G1OUT, B => G2OUT, C => G3OUT,
    D => G4OUT, X => OUT);
  G6: Inverter port map (A => IN3, X => G6OUT);
  G7: Inverter port map (A => IN4, X => G7OUT);
end architecture Logic;
  
```

41. See Figure P-22.

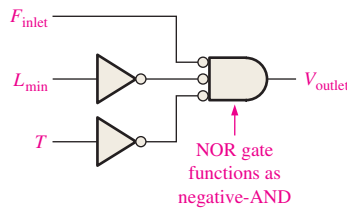


FIGURE P-22

43. See Figure P-23.



FIGURE P-23

45. $X = ABC + D\bar{E}$. Since X is the same as the G_3 output, either G_1 or G_2 has failed, with its output stuck LOW.
47. $X = \overline{AB} + \overline{CD} + \overline{EF} = (\overline{AB})(\overline{CD})(\overline{EF})$
 $= (A + B)(C + D)(E + F)$
 Since X does not go HIGH when C or D is HIGH, the output of gate G_2 must be stuck LOW.
49. No, the output of the \overline{CD} gate is stuck LOW.
51. $X = \text{lamp on}$, $A = \text{front door switch on}$, $B = \text{back door switch on}$. See Figure P-24.

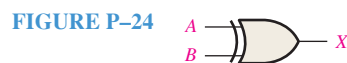


FIGURE P-24

COMBINATIONAL LOGIC

53. Circuit fault: Input C is shorted to ground.

Predicted effect of fault: X1 and X2 are always off. X3 is on only when both B and C are HIGH. X4 is on when either B or C is LOW.

Observed effect of introduced fault: X1 and X2 are always off. X3 is on only when both B and C are HIGH (switches B and C are both open).

55. Observed operation: X1 is on when either A or B is LOW. X2 is always off. X3 is on when both A and B are HIGH or when C is LOW. X4 is always ON. X5 is on when C is HIGH and either A or B is LOW.

Suspected fault: Output of U3 is shorted to ground.

Effect of introduced fault: X1 is on when either A or B is LOW. X2 is always off. X3 is on when both A and B are HIGH or when C is LOW. X4 is always ON. X5 is on when C is HIGH and either A or B is LOW.

FUNCTIONS OF COMBINATIONAL LOGIC

OUTLINE

- 1 A System
- 2 Half and Full Adders
- 3 Parallel Adders
- 4 Ripple Carry and Look-Ahead Carry Adders
- 5 Comparators
- 6 Decoders
- 7 Encoders
- 8 Code Converters
- 9 Multiplexers (Data Selectors)
- 10 Demultiplexers
- 11 Parity Generators/Checkers
- 12 Logic Functions with VHDL and Verilog
- 13 Troubleshooting

OBJECTIVES

- Explain a tablet-bottling control system
- Distinguish between half-adders and full-adders
- Use full-adders to implement multibit parallel binary adders
- Explain the differences between ripple carry and look-ahead carry parallel adders
- Use the magnitude comparator to determine the relationship between two binary numbers and use cascaded comparators to handle the comparison of larger numbers
- Implement a basic binary decoder
- Use BCD-to-7-segment decoders in display systems

- Apply a decimal-to-BCD priority encoder in a simple keyboard application
- Convert from binary to Gray code, and Gray code to binary by using logic devices
- Apply data selectors/multiplexers in multiplexed displays and as a function generator
- Use decoders as demultiplexers
- Explain the meaning of parity
- Use parity generators and checkers to detect bit errors in digital systems
- Implement a simple data communications system
- Write VHDL and Verilog programs for various combination logic functions
- Identify glitches, common bugs in digital systems

KEY TERMS

Half-adder

Full-adder

Cascading

Ripple carry

Look-ahead carry

Decoder

Encoder

Priority encoder

Multiplexer (MUX)

**Demultiplexer
(DEMUX)**

Parity bit

Glitch

VISIT THE WEBSITE

Study aids for this chapter are available at
<http://pearsonhighered.com/floyd>

INTRODUCTION

In this chapter, several types of combinational logic circuits are introduced including adders, comparators, decoders, encoders, code converters, multiplexers (data selectors), demultiplexers, and parity generators/checkers. The tablet-bottling system is discussed in relation

to the application of the logic functions covered. Programmable logic implementation of several logic functions using VHDL and Verilog is covered. Examples of fixed-function IC devices are included at the end of the chapter.

1 A SYSTEM

A tablet-bottling control system will be examined in more detail in this section. This particular system is somewhat simplified to illustrate how all the logic functions that will be covered in this chapter can be applied. As with most systems, there are other ways in which a system's function can be implemented. By studying this system and how it works, you will learn how the various logic functions can be interconnected and operate as a complete system to accomplish a given task.

After completing this section, you should be able to

- Explain the overall operation of the tablet-bottling control system
- Describe the purpose of each logic function

Figure 1 is a general block diagram of the tablet-bottling control system. The job of this system is simply to fill each bottle with a preset number of tablets, which is accomplished by counting the number of tablets going into a bottle and limiting the quantity to the preset number. The system is set for 50 tablets per bottle but with eight bits can accommodate up to 255 tablets per bottle. The system can store a binary number representing up to 255 total tablets before sending the accumulated sum to a computer where the total will be tallied over a specified time period. This limitation is because register B can store eight bits.

KEYPAD, ENCODER, AND REGISTER A The keypad has ten outputs, one for each of the decimal digits. When a key is pressed, the encoder changes the decimal input to the corresponding 4-bit BCD code, as shown in Figure 2. Register A stores 12 bits, which is three BCD digits. Because there are to be 50 tablets per bottle, a 0 is first entered on the keypad; and the BCD code for 0, which is 0000, is stored in the shift register. Next a 5 is entered, and the BCD code 0101 is stored in the register, as indicated. Finally, another 0 is entered.

DECODER A AND CODE CONVERTER A Decoder A transforms the BCD input from register A into a 3-digit 7-segment code for the "Tablets/bottle" display. Actually, decoder A consists of three BCD-to-7-segment decoders because three digits must be displayed at the same time (remember the number can be up to 255). Code converter A converts the BCD code to a 7-bit binary number for comparison with the actual binary tablet count. Figure 3 illustrates these functions.

COMPARATOR, COUNTER, ADDER, AND REGISTER B The set number of tablets per bottle (50) is applied to the comparator, which compares it to the actual number of tablets in a bottle at any point in time. The counter counts each tablet as it falls into a bottle, and the number in the counter is continuously compared to the set number. As long as the number of tablets counted is less than the set number, the valve remains open. When the count reaches the set number, the output of the comparator produces an output signal (HIGH) that closes the valve and advances the conveyer to the next bottle. The counter is reset to zero, the valve is opened when the comparator output goes back to zero, and the filling of the new bottle begins.

FUNCTIONS OF COMBINATIONAL LOGIC

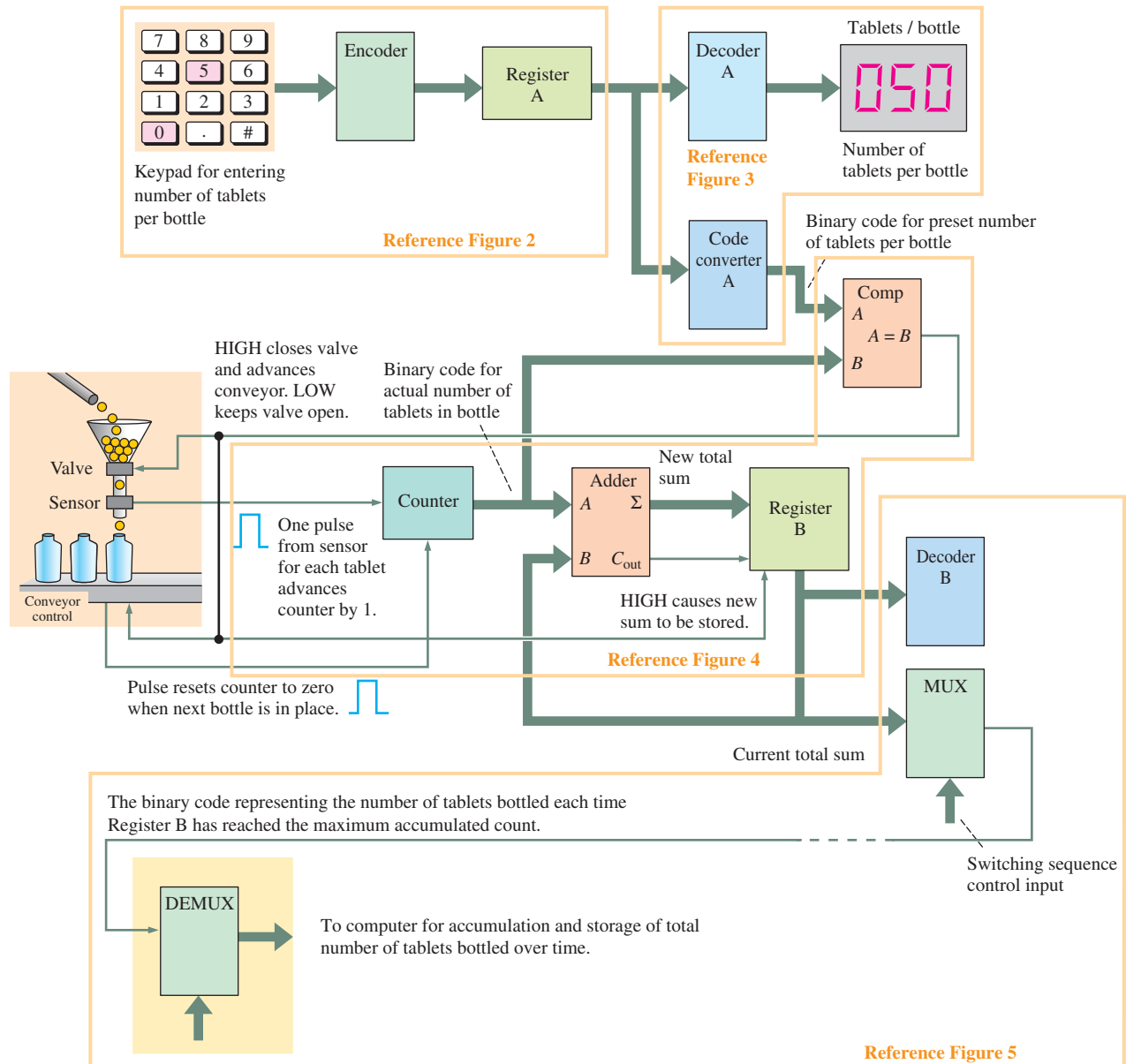


FIGURE 1 Tablet-bottling control system. Each segment is referenced to a following figure for more detail.

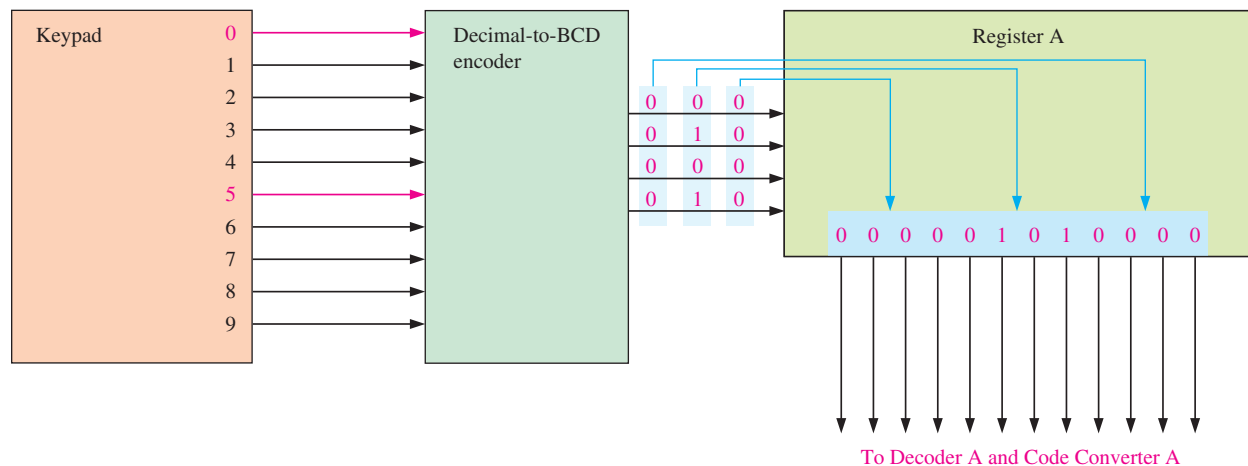


FIGURE 2

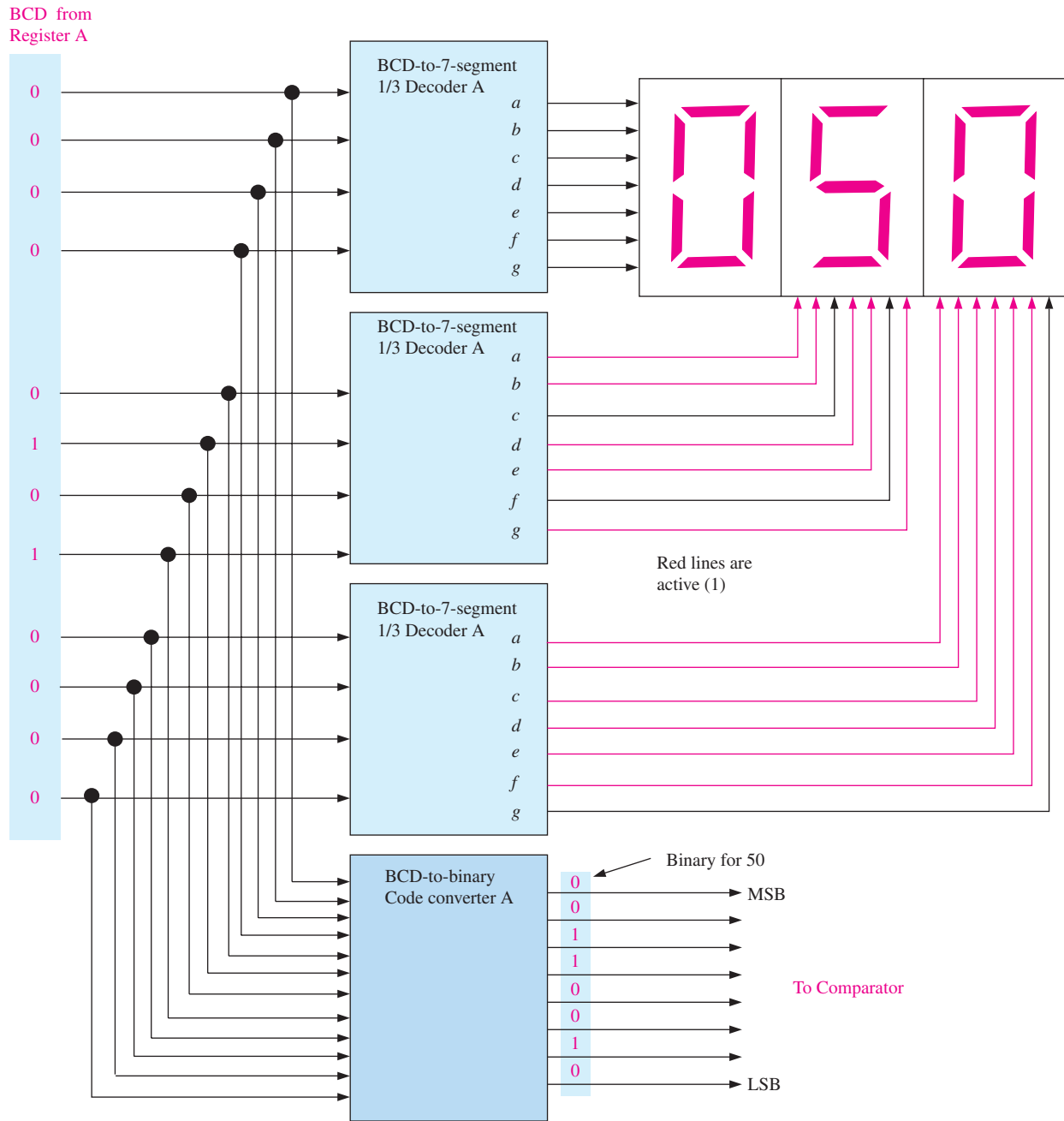


FIGURE 3

The number of tablets in the bottle is added to the previous total number of tablets stored in register B, and the new sum is stored back into register B. When the sum that is stored in the register reaches the limit of 250 (five bottles), as determined by decoder B, the parallel output of the register is multiplexed to the remote site where the sum is accumulated and stored in a computer. Figure 4 shows this operation at the point where the bottle is full with 50 tablets and the previous sum in register B is 100. The new sum of 150 replaces the previous sum of 100.

DECODER B, MUX, AND DEMUX Decoder B decodes the contents of register B to detect the binary code for 250 and enable the multiplexer. The multiplexer acts as a parallel-to-serial converter. The multiplexing sequence (source not shown) is initiated, and the eight data bits are sent serially to the demultiplexer at a remote location. The demultiplexer converts the serial data back to parallel format and sends it to a computer that accumulates the totals over an extended period of time, as illustrated in Figure 5.

FUNCTIONS OF COMBINATIONAL LOGIC

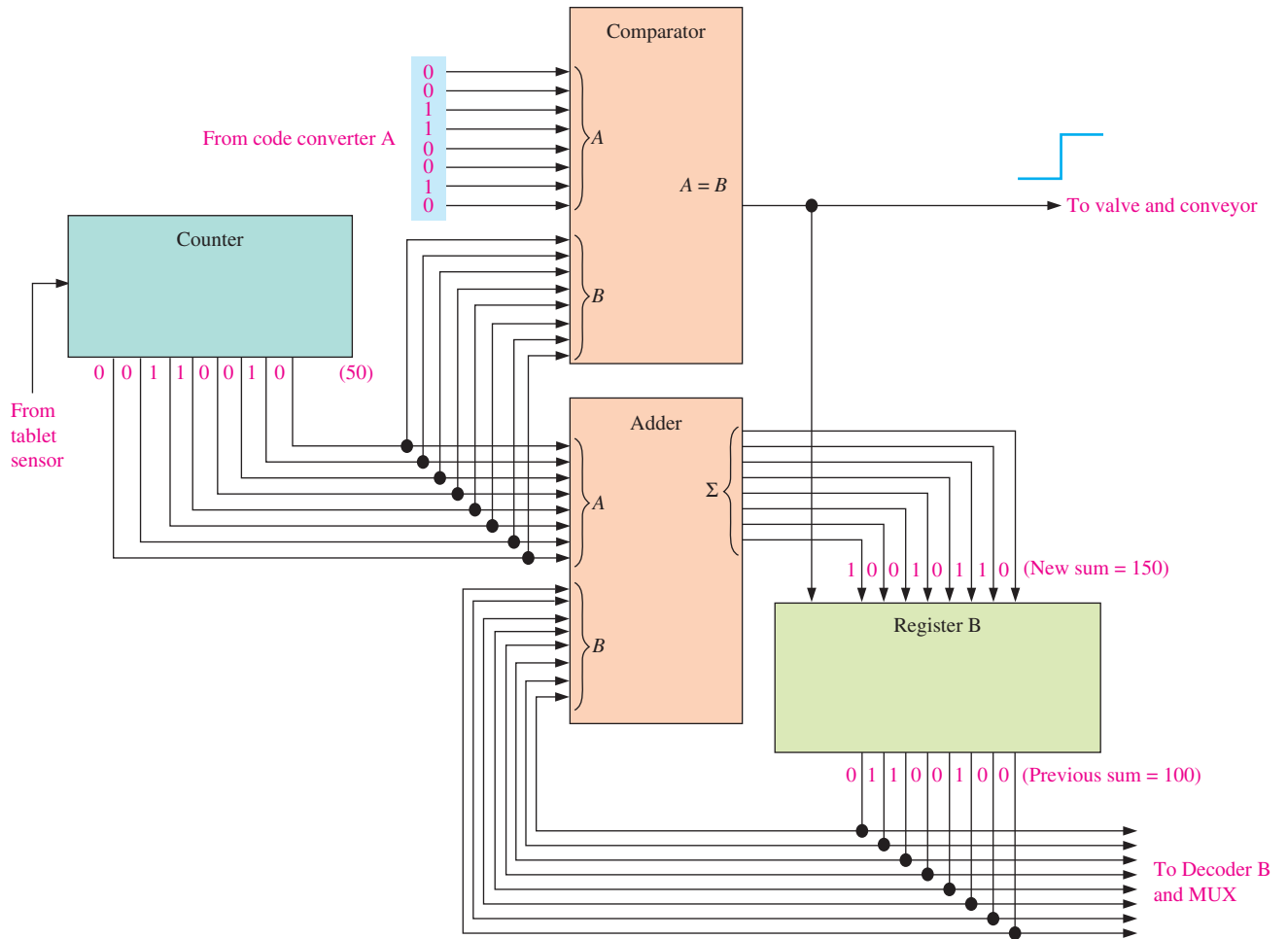


FIGURE 4

From Register B

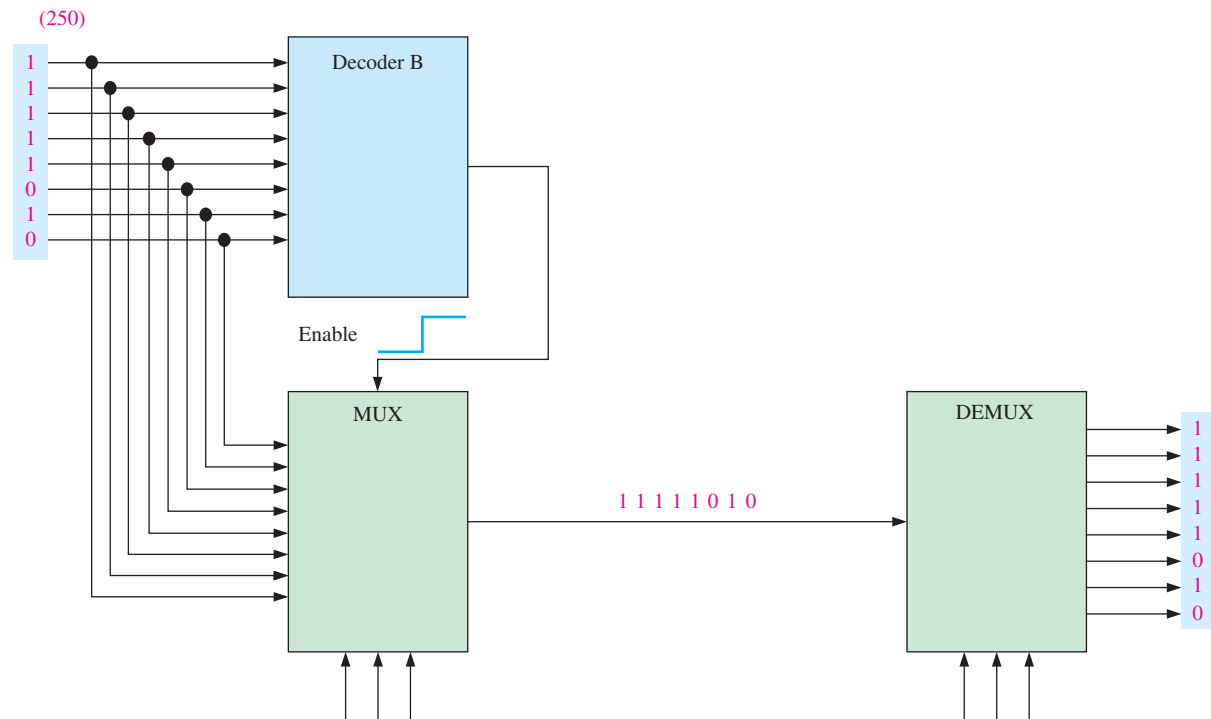


FIGURE 5

SECTION 1 CHECKUP*

1. After four bottles (50 tablets/bottle) have been filled, what are the binary numbers in Register A and Register B?
2. If the number of tablets per bottle is reset to 25, what are the binary numbers in Registers A and B after five bottles have been filled?
3. Explain the purpose of the comparator.
4. Explain the purpose of Decoder B.

*Answers are at the end of the chapter.

2 HALF AND FULL ADDERS

Adders are important in computers and also in other types of digital systems in which numerical data are processed, as you have seen. An understanding of the basic adder operation is fundamental to the study of digital systems. In this section, the half-adder and the full-adder are introduced.

After completing this section, you should be able to

- Describe the function of a half-adder
- Draw a half-adder logic diagram
- Describe the function of the full-adder
- Draw a full-adder logic diagram using half-adders
- Implement a full-adder using AND-OR logic

The Half-Adder

A half-adder adds two bits and produces a sum and an output carry.

The basic rules for binary addition are stated as follows:

$$\begin{array}{l} 0 + 0 = 0 \\ 0 + 1 = 1 \\ 1 + 0 = 1 \\ 1 + 1 = 10 \end{array}$$

The operations are performed by a logic circuit called a **half-adder**.

The half-adder accepts two binary digits on its inputs and produces two binary digits on its outputs—a sum bit and a carry bit.

A half-adder is represented by the logic symbol in Figure 6.

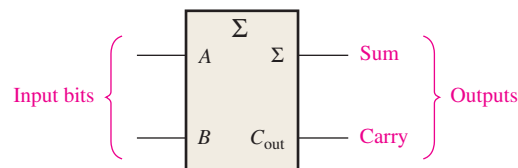


FIGURE 6 Logic symbol for a half-adder. Open file F05-06 to verify operation.

MULTISIM



HALF-ADDER LOGIC From the operation of the half-adder as stated in Table 1, expressions can be derived for the sum and the output carry as functions of the inputs.

TABLE 1 • Half-adder truth table.			
A	B	C _{out}	Σ
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

Σ = sum
 C_{out} = output carry
 A and B = input variables (operands)

Notice that the output carry (C_{out}) is a 1 only when both A and B are 1s; therefore, C_{out} can be expressed as the AND of the input variables.

$$C_{out} = AB \tag{1}$$

Now observe that the sum output (Σ) is a 1 only if the input variables, A and B, are not equal. The sum can therefore be expressed as the exclusive-OR of the input variables.

$$\Sigma = A \oplus B \tag{2}$$

From Equations 1 and 2, the logic implementation required for the half-adder function can be developed. The output carry is produced with an AND gate with A and B on the inputs, and the sum output is generated with an exclusive-OR gate, as shown in Figure 7. Remember that the exclusive-OR can be implemented with AND gates, an OR gate, and inverters.

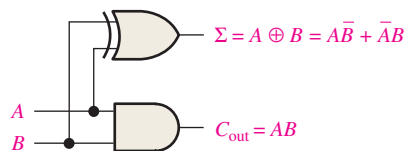


FIGURE 7 Half-adder logic diagram.

The Full-Adder

The second category of adder is the **full-adder**.*

The full-adder accepts two input bits and an input carry and generates a sum output and an output carry.

The basic difference between a full-adder and a half-adder is that the full-adder accepts an input carry. A logic symbol for a full-adder is shown in Figure 8, and the truth table in Table 2 shows the operation of a full-adder.

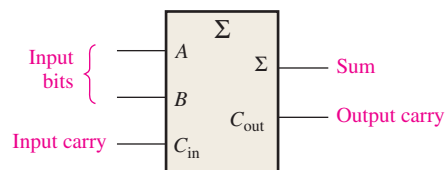


FIGURE 8 Logic symbol for a full-adder.
 Open file F05-08 to verify operation.

A full-adder has an input carry while the half-adder does not.

MULTISIM



FULL-ADDER LOGIC The full-adder must add the two input bits and the input carry. From the half-adder you know that the sum of the input bits A and B is the exclusive-OR

*The bold terms in color are key terms and are included in a Key Term glossary at the end of the chapter.

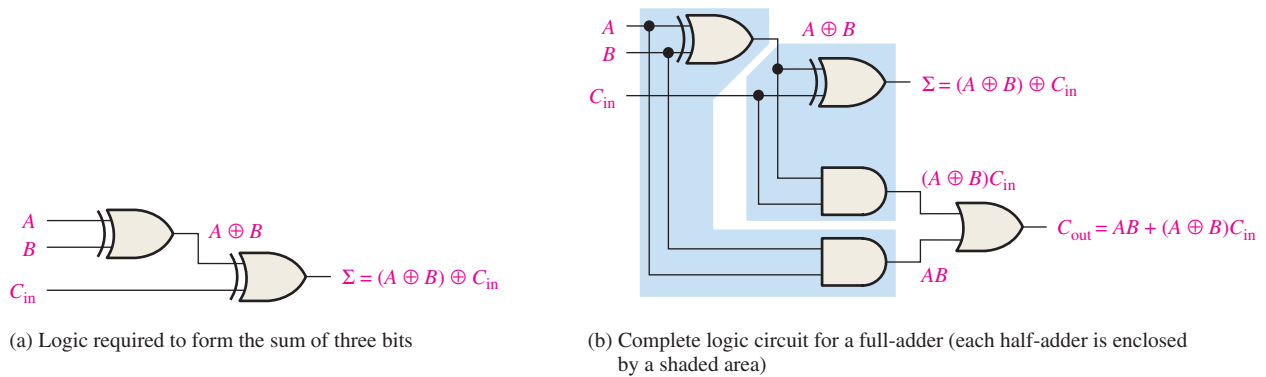
TABLE 2 • Full-adder truth table.				
<i>A</i>	<i>B</i>	<i>C_{in}</i>	<i>C_{out}</i>	Σ
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

C_{in} = input carry, sometimes designated as *CI*
C_{out} = output carry, sometimes designated as *CO*
 Σ = sum
A and *B* = input variables (operands)

of those two variables, $A \oplus B$. For the input carry (*C_{in}*) to be added to the input bits, it must be exclusive-ORed with $A \oplus B$, yielding the equation for the sum output of the full-adder.

$$\Sigma = (A \oplus B) \oplus C_{in} \tag{3}$$

This means that to implement the full-adder sum function, two 2-input exclusive-OR gates can be used. The first must generate the term $A \oplus B$, and the second has as its inputs the output of the first XOR gate and the input carry, as illustrated in Figure 9(a).



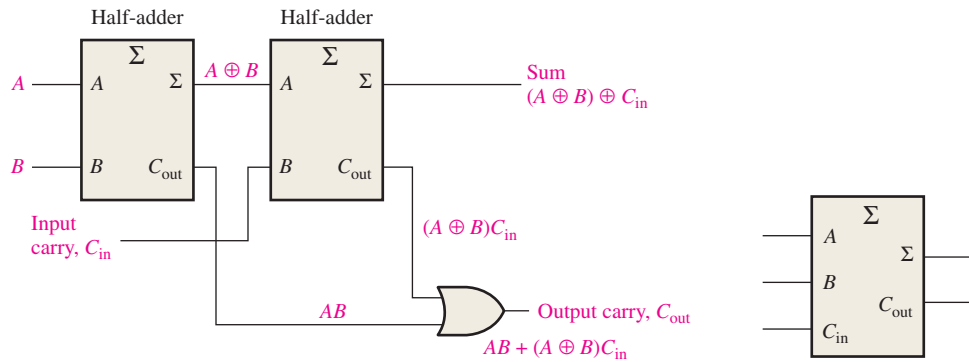
MULTISIM **FIGURE 9** Full-adder logic. Open file F05-09 to verify operation.



The output carry is a 1 when both inputs to the first XOR gate are 1s or when both inputs to the second XOR gate are 1s. You can verify this fact by studying Table 2. The output carry of the full-adder is therefore produced by input *A* ANDed with input *B* and $A \oplus B$ ANDed with *C_{in}*. These two terms are ORed, as expressed in Equation 4. This function is implemented and combined with the sum logic to form a complete full-adder circuit, as shown in Figure 9(b).

$$C_{out} = AB + (A \oplus B)C_{in} \tag{4}$$

Notice in Figure 9(b) there are two half-adders, connected as shown in the block diagram of Figure 10(a), with their output carries ORed. The logic symbol shown in Figure 10(b) will normally be used to represent the full-adder.



(a) Arrangement of two half-adders to form a full-adder

(b) Full-adder logic symbol

FIGURE 10 Full-adder implemented with half-adders.

EXAMPLE 1

For each of the three full-adders in Figure 11, determine the outputs for the inputs shown.

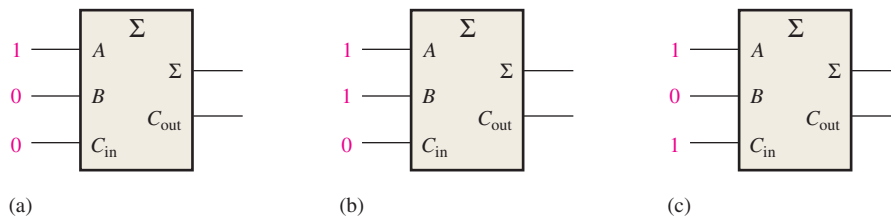


FIGURE 11

SOLUTION

(a) The input bits are $A = 1$, $B = 0$, and $C_{in} = 0$.

$$1 + 0 + 0 = 1 \text{ with no carry}$$

Therefore, $\Sigma = 1$ and $C_{out} = 0$.

(b) The input bits are $A = 1$, $B = 1$, and $C_{in} = 0$.

$$1 + 1 + 0 = 0 \text{ with a carry of } 1$$

Therefore, $\Sigma = 0$ and $C_{out} = 1$.

(c) The input bits are $A = 1$, $B = 0$, and $C_{in} = 1$.

$$1 + 0 + 1 = 0 \text{ with a carry of } 1$$

Therefore, $\Sigma = 0$ and $C_{out} = 1$.

RELATED PROBLEM*

What are the full-adder outputs for $A = 1$, $B = 1$, and $C_{in} = 1$?

*Answers are at the end of the chapter.

SECTION 2 CHECKUP

- Determine the sum (Σ) and the output carry (C_{out}) of a half-adder for each set of input bits:
(a) 01 (b) 00 (c) 10 (d) 11
- A full-adder has $C_{in} = 1$. What are the sum (Σ) and the output carry (C_{out}) when $A = 1$ and $B = 1$?

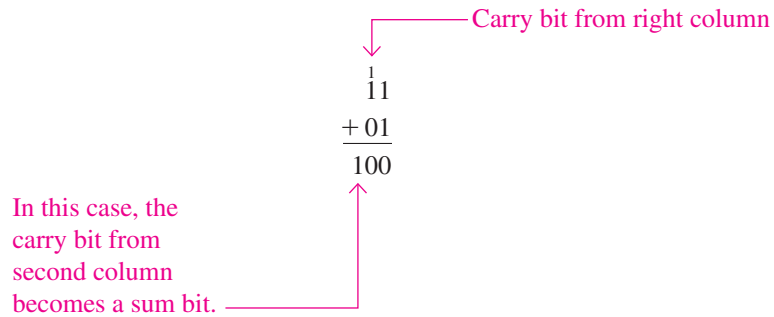
3 PARALLEL ADDERS

Two or more full-adders are connected to form parallel binary adders. In this section, you will learn the basic operation of this type of adder and its associated input and output functions.

After completing this section, you should be able to

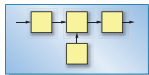
- Use full-adders to implement a parallel binary adder
- Explain the addition process in a parallel binary adder
- Use the truth table for a 4-bit parallel adder
- Expand the 4-bit adder to accommodate 8-bit or 16-bit addition

As you saw in Section 2, a single full-adder is capable of adding two 1-bit numbers and an input carry. To add binary numbers with more than one bit, you must use additional full-adders. When one binary number is added to another, each column generates a sum bit and a 1 or 0 carry bit to the next column to the left, as illustrated here with 2-bit numbers.



Addition is performed by computers on two numbers at a time, called *operands*. The *source operand* is a number that is to be added to an existing number called the *destination operand*, which is held in an ALU register, such as the accumulator. The sum of the two numbers is then stored back in the accumulator. Addition is performed on integer numbers or floating-point numbers using ADD or FADD instructions respectively.

SYSTEM NOTE



To add two binary numbers, a full-adder is required for each bit in the numbers. So for 2-bit numbers, two adders are needed; for 4-bit numbers, four adders are used; and so on. The carry output of each adder is connected to the carry input of the next higher-order adder, as shown in Figure 12 for a 2-bit adder. Notice that either a half-adder can be used for the least significant position or the carry input of a full-adder can be made 0 (grounded) because there is no carry input to the least significant bit position.

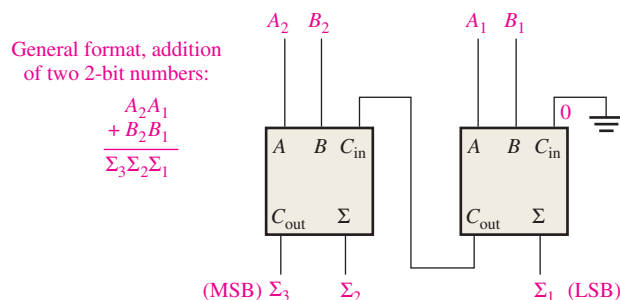


FIGURE 12 Block diagram of a 2-bit parallel adder using two full-adders. Open file F05-12 to verify operation.



In Figure 12 the least significant bits (LSB) of the two numbers are represented by A_1 and B_1 . The next higher-order bits are represented by A_2 and B_2 . The three sum bits are Σ_1 , Σ_2 , and Σ_3 . Notice that the output carry from the left-most full-adder becomes the most significant bit (MSB) in the sum, Σ_3 .

EXAMPLE 2

Determine the sum generated by the 3-bit parallel adder in Figure 13 and show the intermediate carries when the binary numbers 101 and 011 are being added.

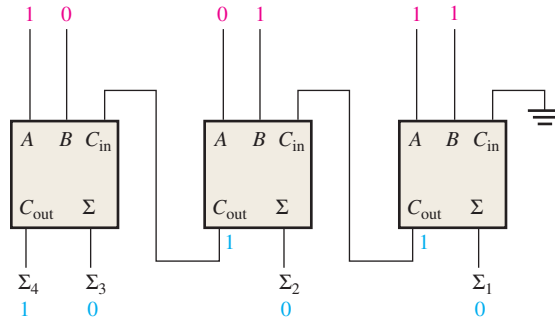


FIGURE 13

SOLUTION

The LSBs of the two numbers are added in the right-most full-adder. The sum bits and the intermediate carries are indicated in blue in Figure 13.

RELATED PROBLEM

What are the sum outputs when 111 and 101 are added by the 3-bit parallel adder?

Four-Bit Parallel Adders

A group of four bits is called a **nibble**. A basic 4-bit parallel adder is implemented with four full-adder stages as shown in Figure 14. Again, the LSBs (A_1 and B_1) in each number being added go into the right-most full-adder; the higher-order bits are applied as shown to the successively higher-order adders, with the MSBs (A_4 and B_4) in each number being applied to the left-most full-adder. The carry output of each adder is connected to the carry input of the next higher-order adder as indicated. These are called *internal carries*.

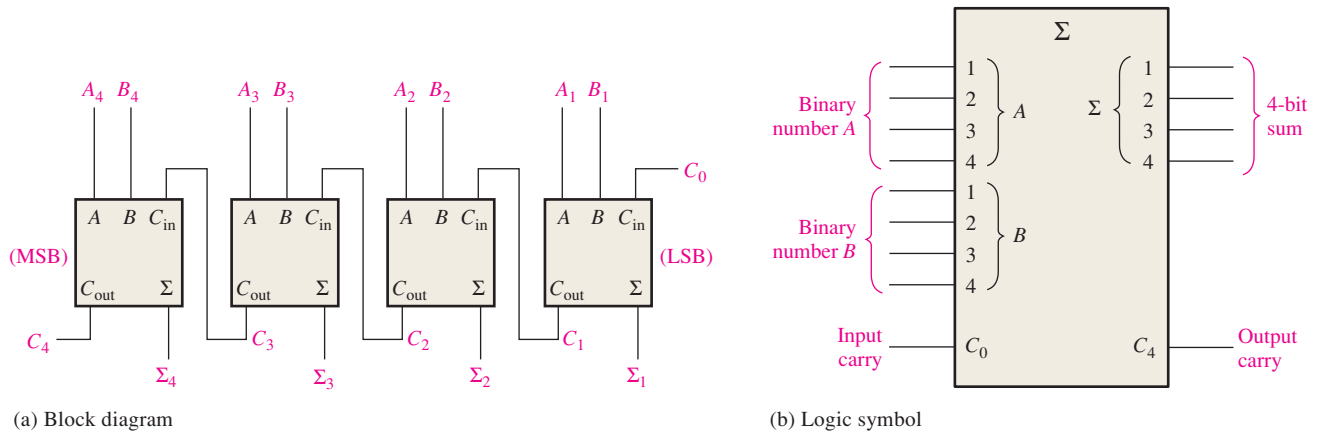


FIGURE 14 A 4-bit parallel adder.

In keeping with most manufacturers' data sheets, the input labeled C_0 is the input carry to the least significant bit adder; C_4 , in the case of four bits, is the output carry of the most significant bit adder; and Σ_1 (LSB) through Σ_4 (MSB) are the sum outputs. The logic symbol is shown in Figure 14(b).

In terms of the method used to handle carries in a parallel adder, there are two types: the *ripple carry* adder and the *carry look-ahead* adder. These are discussed in Section 4.

Truth Table for a 4-Bit Parallel Adder

Table 3 is the truth table for a 4-bit adder. On some data sheets, truth tables may be called *function tables* or *functional truth tables*. The subscript n represents the adder bits and can be 1, 2, 3, or 4 for the 4-bit adder. C_{n-1} is the carry from the previous adder. Carries C_1 , C_2 , and C_3 are generated internally. C_0 is an external carry input and C_4 is an output. Example 3 illustrates how to use Table 3.

C_{n-1}	A_n	B_n	Σ_n	C_n
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

EXAMPLE 3

Use the 4-bit parallel adder truth table (Table 3) to find the sum and output carry for the addition of the following two 4-bit numbers if the input carry (C_{n-1}) is 0:

$$A_4A_3A_2A_1 = 1100 \quad \text{and} \quad B_4B_3B_2B_1 = 1100$$

SOLUTION

For $n = 1$: $A_1 = 0$, $B_1 = 0$, and $C_{n-1} = 0$. From the 1st row of the table,

$$\Sigma_1 = 0 \quad \text{and} \quad C_1 = 0$$

For $n = 2$: $A_2 = 0$, $B_2 = 0$, and $C_{n-1} = 0$. From the 1st row of the table,

$$\Sigma_2 = 0 \quad \text{and} \quad C_2 = 0$$

For $n = 3$: $A_3 = 1$, $B_3 = 1$, and $C_{n-1} = 0$. From the 4th row of the table,

$$\Sigma_3 = 0 \quad \text{and} \quad C_3 = 1$$

For $n = 4$: $A_4 = 1$, $B_4 = 1$, and $C_{n-1} = 1$. From the last row of the table,

$$\Sigma_4 = 1 \quad \text{and} \quad C_4 = 1$$

C_4 becomes the output carry; the sum of 1100 and 1100 is 11000.

RELATED PROBLEM

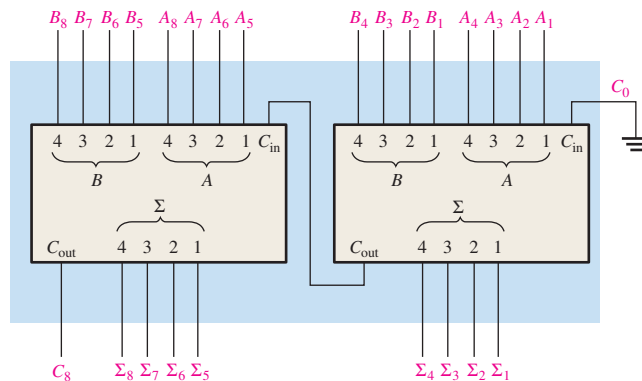
Use the truth table (Table 3) to find the result of adding the binary numbers 1011 and 1010.

Adder Expansion

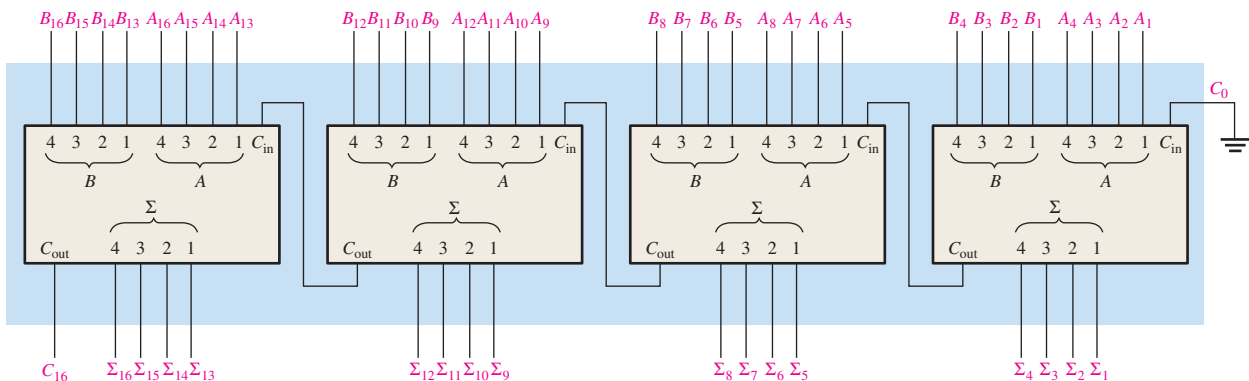
The 4-bit parallel adder can be expanded to handle the addition of two 8-bit numbers by using two 4-bit adders. The carry input of the low-order adder (C_0) is connected to ground because there is no carry into the least significant bit position, and the carry output of the low-order adder is connected to the carry input of the high-order adder, as shown in Figure 15(a). This process is known as **cascading**. Notice that, in this case, the output carry is designated C_8 because it is generated from the eighth bit position. The low-order adder is the one that adds the lower or less significant four bits in the numbers, and the high-order adder is the one that adds the higher or more significant four bits in the 8-bit numbers.

Adders can be expanded to handle more bits by cascading.

Similarly, four 4-bit adders can be cascaded to handle two 16-bit numbers as shown in Figure 15(b). Notice that the output carry is designated C_{16} because it is generated from the sixteenth bit position.



(a) Cascading of two 4-bit adders to form an 8-bit adder



(b) Cascading of four 4-bit adders to form a 16-bit adder

FIGURE 15 Examples of adder expansion.

EXAMPLE 4

Show the input and output states (1s and 0s) for the 8-bit adder in Figure 15(a) for the following 8-bit input numbers:

$$A_8A_7A_6A_5A_4A_3A_2A_1 = 10111001 \quad \text{and} \quad B_8B_7B_6B_5B_4B_3B_2B_1 = 10011110$$

SOLUTION

The sum of the two 8-bit numbers is

$$\Sigma_9\Sigma_8\Sigma_7\Sigma_6\Sigma_5\Sigma_4\Sigma_3\Sigma_2\Sigma_1 = 101010111$$

The input and output states are shown in Figure 16.

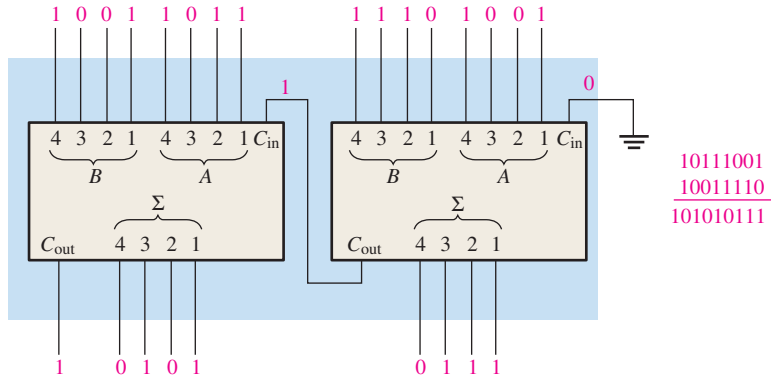
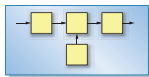


FIGURE 16

RELATED PROBLEM

Use 4-bit adders to implement a 12-bit parallel adder.

SYSTEM EXAMPLE 1



A VOTING SYSTEM

A simple voting system can be used to simultaneously provide the number of “yes” votes and the number of “no” votes. This type of voting system can be used where a group of people are assembled and there is a need for immediately determining opinions (for or against), making decisions, or voting on certain issues or other matters.

In its simplest form, the system includes a switch for “yes” or “no” selection at each position in the assembly and a digital display for the number of yes votes and one for the number of no votes. The basic system is shown in Figure 17 for a 6-position setup, but it can be expanded to any number of positions with additional 6-position modules and additional parallel adder and display circuits.

In Figure 17 each full-adder can produce the sum of up to three votes. The sum and output carry of each full-adder then goes to the two lower-order inputs of a parallel binary adder. The two higher-order inputs of the parallel adder are connected to ground (0) because there is never a case where the binary input exceeds 0011 (decimal 3). For this basic 6-position system, the outputs of the parallel adder go to a BCD-to-7-segment decoder that drives the 7-segment display. As mentioned, additional circuits must be included when the system is expanded.

The resistors from the inputs of each full-adder to ground assure that each input is LOW when the switch is in the neutral position (CMOS logic is used). When a switch is moved to the “yes” or to the “no” position, a HIGH level (V_{CC}) is applied to the associated full-adder input.

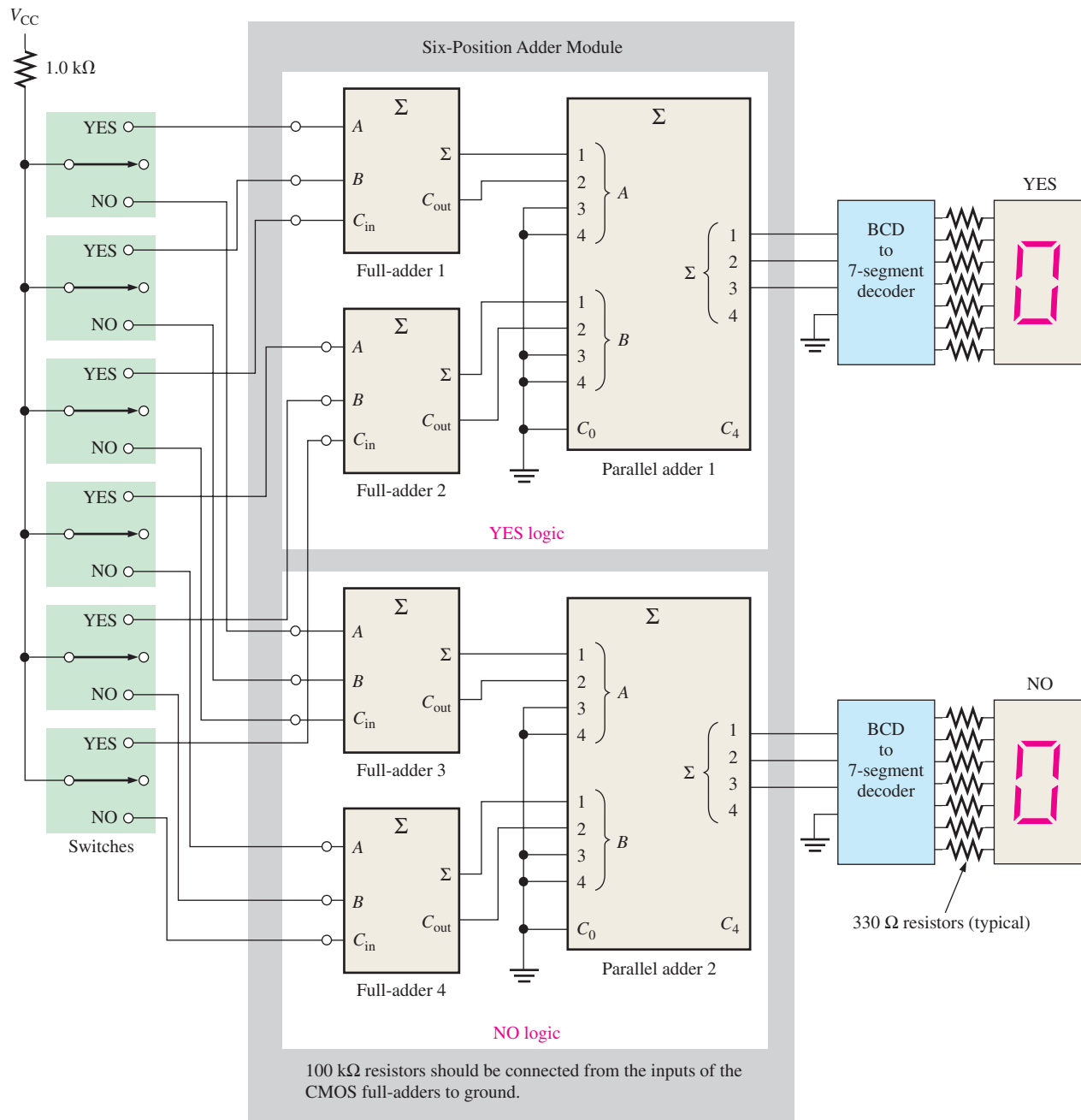


FIGURE 17

SECTION 3 CHECKUP

- Two 4-bit numbers (1101 and 1011) are applied to a 4-bit parallel adder. The input carry is 1. Determine the sum (Σ) and the output carry.
- How many 4-bit adders would be required to add two binary numbers each representing decimal numbers up through 1000_{10} ?

4 RIPPLE CARRY AND LOOK-AHEAD CARRY ADDERS

As mentioned in the last section, parallel adders can be placed into two categories based on the way in which internal carries from stage to stage are handled. Those categories are ripple carry and look-ahead carry. Externally, both types of adders are the same in terms of inputs and outputs. The difference is the speed at which they can add numbers. The look-ahead carry adder is much faster than the ripple carry adder.

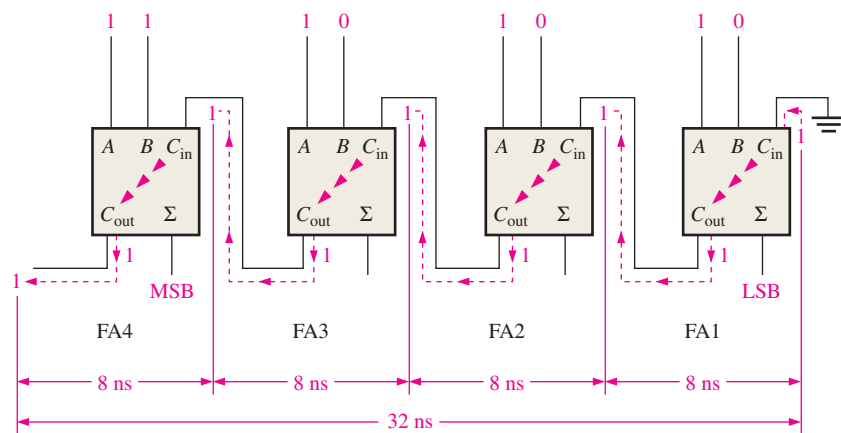
After completing this section, you should be able to

- Discuss the difference between a ripple carry adder and a look-ahead carry adder
- State the advantage of look-ahead carry addition
- Define *carry generation* and *carry propagation* and explain the difference
- Develop look-ahead carry logic

The Ripple Carry Adder

A **ripple carry** adder is one in which the carry output of each full-adder is connected to the carry input of the next higher-order stage (a stage is one full-adder). The sum and the output carry of any stage cannot be produced until the input carry occurs; this causes a time delay in the addition process, as illustrated in Figure 18. The carry propagation delay for each full-adder is the time from the application of the input carry until the output carry occurs, assuming that the *A* and *B* inputs are already present.

FIGURE 18 A 4-bit parallel ripple carry adder showing “worst-case” carry propagation delays.



Full-adder 1 (FA1) cannot produce a potential output carry until an input carry is applied. Full-adder 2 (FA2) cannot produce a potential output carry until FA1 produces an output carry. Full-adder 3 (FA3) cannot produce a potential output carry until an output carry is produced by FA1 followed by an output carry from FA2, and so on. As you can see in Figure 18, the input carry to the least significant stage has to ripple through all the adders before a final sum is produced. The cumulative delay through all the adder stages is a “worst-case” addition time. The total delay can vary, depending on the carry bit produced by each full-adder. If two numbers are added such that no carries (0) occur between stages, the addition time is simply the propagation time through a single full-adder from the application of the data bits on the inputs to the occurrence of a sum output; however, worst-case addition time must always be assumed.

The Look-Ahead Carry Adder

The speed with which an addition can be performed is limited by the time required for the carries to propagate, or ripple, through all the stages of a parallel adder. One method of

speeding up the addition process by eliminating this ripple carry delay is called **look-ahead carry** addition. The look-ahead carry adder anticipates the output carry of each stage, and based on the inputs, produces the output carry by either carry generation or carry propagation.

Carry generation occurs when an output carry is produced (generated) internally by the full-adder. A carry is generated only when both input bits are 1s. The generated carry, C_g , is expressed as the AND function of the two input bits, A and B .

$$C_g = AB \tag{5}$$

Carry propagation occurs when the input carry is rippled to become the output carry. An input carry may be propagated by the full-adder when either or both of the input bits are 1s. The propagated carry, C_p , is expressed as the OR function of the input bits.

$$C_p = A + B \tag{6}$$

The conditions for carry generation and carry propagation are illustrated in Figure 19. The three arrowheads symbolize ripple (propagation).

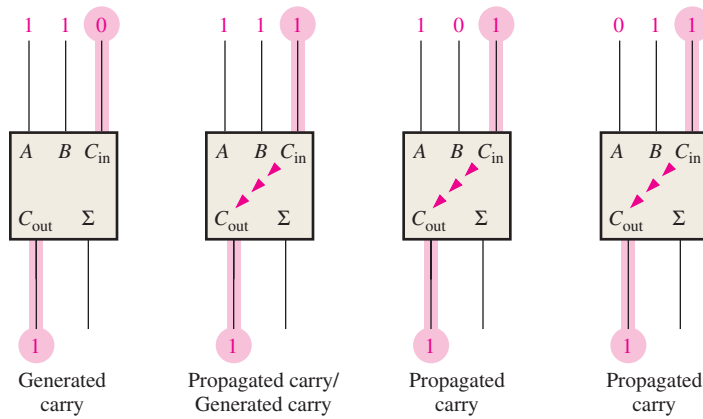


FIGURE 19 Illustration of conditions for carry generation and carry propagation.

The output carry of a full-adder can be expressed in terms of both the generated carry (C_g) and the propagated carry (C_p). The output carry (C_{out}) is a 1 if the generated carry is a 1 OR if the propagated carry is a 1 AND the input carry (C_{in}) is a 1. In other words, we get an output carry of 1 if it is generated by the full-adder ($A = 1$ AND $B = 1$) or if the adder propagates the input carry ($A = 1$ OR $B = 1$) AND $C_{in} = 1$. This relationship is expressed as

$$C_{out} = C_g + C_p C_{in} \tag{7}$$

Now let's see how this concept can be applied to a parallel adder, whose individual stages are shown in Figure 20 for a 4-bit example. For each full-adder, the output carry is

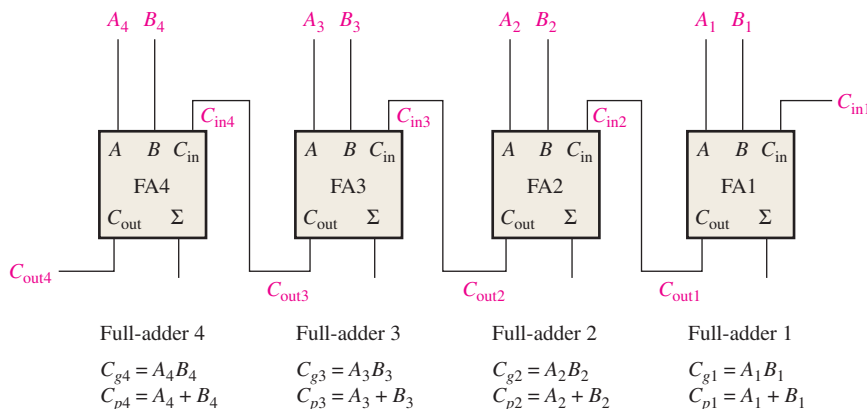


FIGURE 20 Carry generation and carry propagation in terms of the input bits to a 4-bit adder.

dependent on the generated carry (C_g), the propagated carry (C_p), and its input carry (C_{in}). The C_g and C_p functions for each stage are *immediately* available as soon as the input bits A and B and the input carry to the LSB adder are applied because they are dependent only on these bits. The input carry to each stage is the output carry of the previous stage.

Based on this analysis, we can now develop expressions for the output carry, C_{out} , of each full-adder stage for the 4-bit example.

Full-adder 1:

$$C_{out1} = C_{g1} + C_{p1}C_{in1}$$

Full-adder 2:

$$\begin{aligned} C_{in2} &= C_{out1} \\ C_{out2} &= C_{g2} + C_{p2}C_{in2} = C_{g2} + C_{p2}C_{out1} = C_{g2} + C_{p2}(C_{g1} + C_{p1}C_{in1}) \\ &= C_{g2} + C_{p2}C_{g1} + C_{p2}C_{p1}C_{in1} \end{aligned}$$

Full-adder 3:

$$\begin{aligned} C_{in3} &= C_{out2} \\ C_{out3} &= C_{g3} + C_{p3}C_{in3} = C_{g3} + C_{p3}C_{out2} = C_{g3} + C_{p3}(C_{g2} + C_{p2}C_{g1} + C_{p2}C_{p1}C_{in1}) \\ &= C_{g3} + C_{p3}C_{g2} + C_{p3}C_{p2}C_{g1} + C_{p3}C_{p2}C_{p1}C_{in1} \end{aligned}$$

Full-adder 4:

$$\begin{aligned} C_{in4} &= C_{out3} \\ C_{out4} &= C_{g4} + C_{p4}C_{in4} = C_{g4} + C_{p4}C_{out3} \\ &= C_{g4} + C_{p4}(C_{g3} + C_{p3}C_{g2} + C_{p3}C_{p2}C_{g1} + C_{p3}C_{p2}C_{p1}C_{in1}) \\ &= C_{g4} + C_{p4}C_{g3} + C_{p4}C_{p3}C_{g2} + C_{p4}C_{p3}C_{p2}C_{g1} + C_{p4}C_{p3}C_{p2}C_{p1}C_{in1} \end{aligned}$$

Notice that in each of these expressions, the output carry for each full-adder stage is dependent only on the initial input carry (C_{in1}), the C_g and C_p functions of that stage, and the C_g and C_p functions of the preceding stages. Since each of the C_g and C_p functions can be expressed in terms of the A and B inputs to the full-adders, all the output carries are immediately available (except for gate delays), and you do not have to wait for a carry to ripple through all the stages before a final result is achieved. Thus, the look-ahead carry technique speeds up the addition process.

The C_{out} equations are implemented with logic gates and connected to the full-adders to create a 4-bit look-ahead carry adder, as shown in Figure 21.

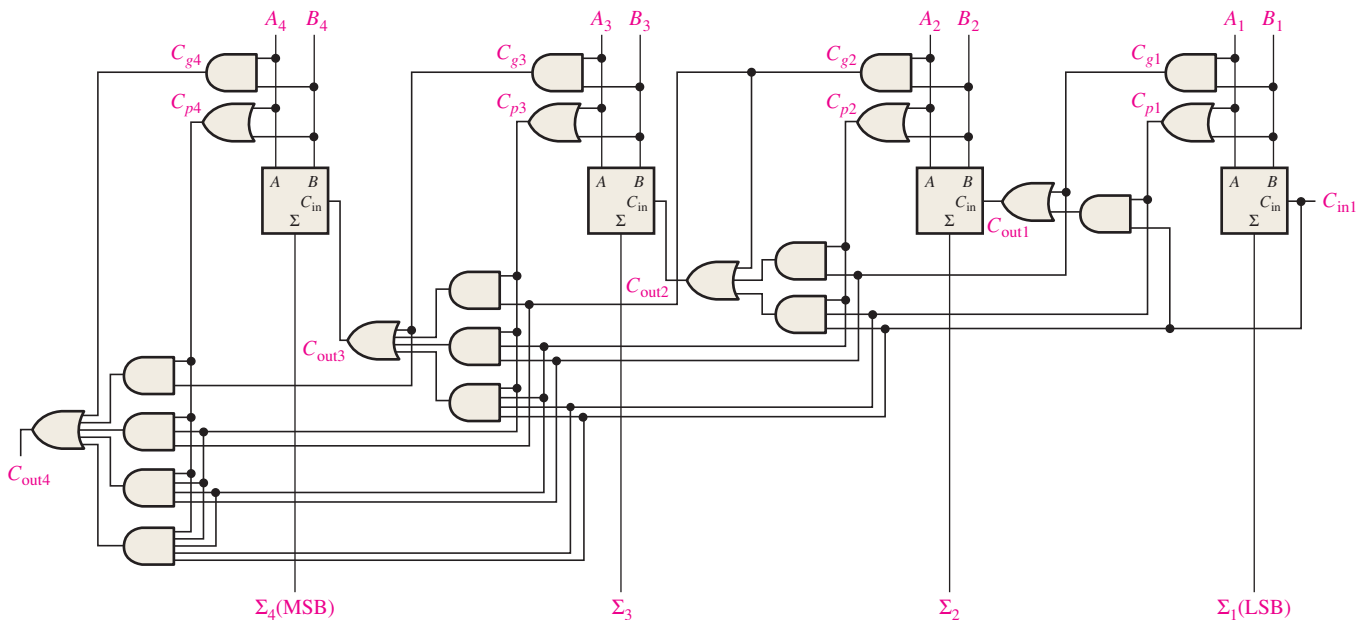


FIGURE 21 Logic diagram for a 4-stage look-ahead carry adder.

SECTION 4 CHECKUP

- The input bits to a full-adder are $A = 1$ and $B = 0$. Determine C_g and C_p .
- Determine the output carry of a full-adder when $C_{in} = 1$, $C_g = 0$, and $C_p = 1$.

5 COMPARATORS

The basic function of a comparator is to compare the magnitudes of two binary quantities to determine the relationship of those quantities. In its simplest form, a comparator circuit determines whether two numbers are equal.

After completing this section, you should be able to

- Use the exclusive-NOR gate as a basic comparator
- Explain the internal logic of a magnitude comparator that has both equality and inequality outputs
- Use a comparator to compare the magnitudes of two 4-bit numbers
- Apply cascading to expand a comparator to eight or more bits

Equality

The exclusive-NOR gate can be used as a basic comparator because its output is a 0 if the two input bits are not equal and a 1 if the input bits are equal. Figure 22 shows the exclusive-NOR gate as a 2-bit comparator.

A comparator determines if two binary numbers are equal or unequal.

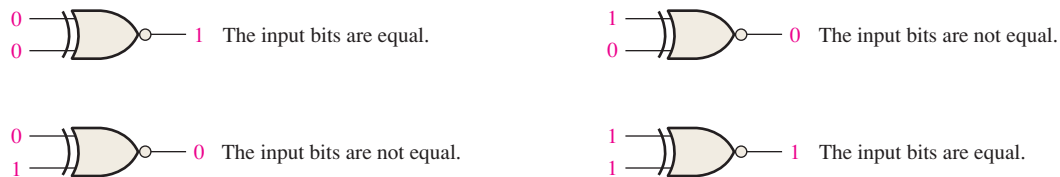


FIGURE 22 Basic comparator operation.

In order to compare binary numbers containing two bits each, an additional exclusive-NOR gate is necessary. The two least significant bits (LSBs) of the two numbers are compared by gate G_1 , and the two most significant bits (MSBs) are compared by gate G_2 , as shown in Figure 23. If the two numbers are equal, their corresponding bits are the same, and the output of each exclusive-NOR gate is a 1. If the corresponding sets of bits are not equal, a 0 occurs on that exclusive-NOR gate output.

In order to produce a single output indicating an equality or inequality of two numbers, an AND gate can be combined with XNOR gates, as shown in Figure 23. The output of each exclusive-NOR gate is applied to the AND gate input. When the two input bits for each exclusive-NOR are equal, the corresponding bits of the numbers are equal, producing a 1 on both inputs to the AND gate and thus a 1 on the output. When the two numbers are not equal, one or both sets of corresponding bits are unequal, and a 0 appears on at least one input to the AND gate to produce a 0 on its output. Thus, the output of the AND gate indicates equality (1) or inequality (0) of the two numbers. Example 5 illustrates this operation for two specific cases.

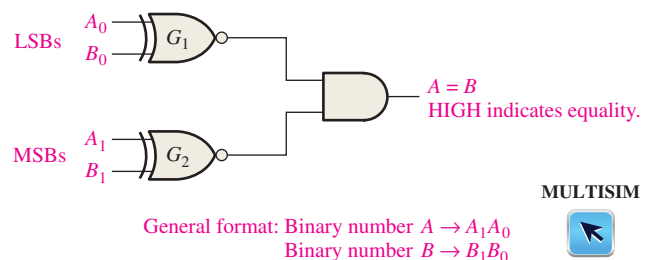


FIGURE 23 Logic diagram for equality comparison of two 2-bit numbers. Open file F05-23 to verify operation.

EXAMPLE 5

Apply each of the following sets of binary numbers to the comparator inputs in Figure 23, and determine the output by following the logic levels through the circuit.

- (a) 10 and 10 (b) 11 and 10

SOLUTION

- (a) The output is **1** for inputs 10 and 10, as shown in Figure 24(a).
 (b) The output is **0** for inputs 11 and 10, as shown in Figure 24(b).

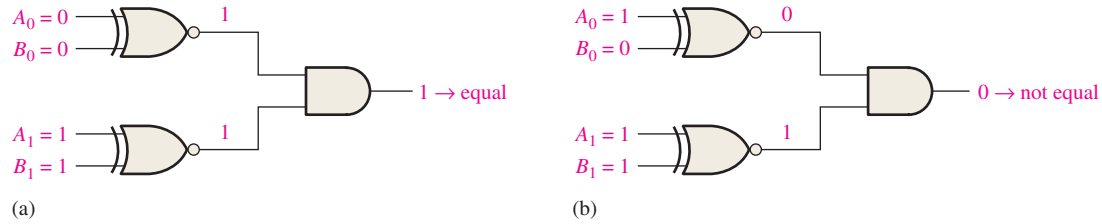
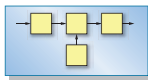


FIGURE 24

RELATED PROBLEM

Repeat the process for binary inputs of 01 and 10.

The basic comparator can be expanded to any number of bits. The AND gate sets the condition that all corresponding bits of the two numbers must be equal if the two numbers themselves are equal.



In a computer, the *cache* is a very fast intermediate memory between the central processing unit (CPU) and the slower main memory. The CPU requests data by sending out its *address* (unique location) in memory. Part of this address is called a *tag*. The *tag address comparator* compares the tag from the CPU with the tag from the cache directory. If the two agree, the addressed data is already in the cache and is retrieved very quickly. If the tags disagree, the data must be retrieved from the main memory at a much slower rate.

SYSTEM NOTE

Inequality

In addition to the equality output, many IC comparators provide additional outputs that indicate which of the two binary numbers being compared is the larger. That is, there is an output that indicates when number *A* is greater than number *B* ($A > B$) and an output that indicates when number *A* is less than number *B* ($A < B$), as shown in the logic symbol for a 4-bit comparator in Figure 25.

To determine an inequality of binary numbers *A* and *B*, you first examine the highest-order bit in each number. The following conditions are possible:

1. If $A_3 = 1$ and $B_3 = 0$, number *A* is greater than number *B*.
2. If $A_3 = 0$ and $B_3 = 1$, number *A* is less than number *B*.
3. If $A_3 = B_3$, then you must examine the next lower bit position for an inequality.

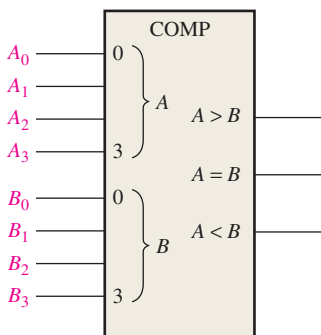


FIGURE 25 Logic symbol for a 4-bit comparator with inequality indication.

These three operations are valid for each bit position in the numbers. The general procedure used in a comparator is to check for an inequality in a bit position, starting with

the highest-order bits (MSBs). When such an inequality is found, the relationship of the two numbers is established, and any other inequalities in lower-order bit positions must be ignored because it is possible for an opposite indication to occur; *the highest-order indication must take precedence.*

EXAMPLE 6

Determine the $A = B$, $A > B$, and $A < B$ outputs for the input numbers shown on the comparator in Figure 26.

SOLUTION

The number on the A inputs is 0110 and the number on the B inputs is 0011. The $A > B$ output is **HIGH** and the other outputs are **LOW**.

RELATED PROBLEM

What are the comparator outputs when $A_3A_2A_1A_0 = 1001$ and $B_3B_2B_1B_0 = 1010$?

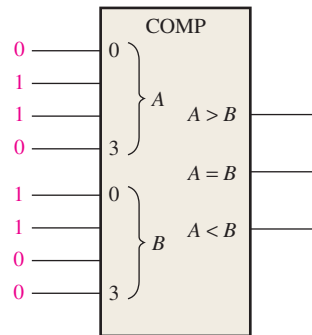


FIGURE 26



HANDS ON TIP

Most CMOS devices contain protection circuitry to guard against damage from high static voltages or electric fields. However, precautions must be taken to avoid applications of any voltages higher than maximum rated voltages. For proper operation, input and output voltages should be between ground and V_{CC} . Also, remember that unused inputs must always be connected to an appropriate logic level (ground or V_{CC}). Unused outputs may be left open.

SECTION 5 CHECKUP

1. The binary numbers $A = 1011$ and $B = 1010$ are applied to the inputs of the comparator in Figure 25. Determine the outputs.
2. The binary numbers $A = 11001011$ and $B = 11010100$ are applied to an 8-bit comparator. Determine the states of the outputs.

6 DECODERS

A **decoder** is a digital circuit that detects the presence of a specified combination of bits (code) on its inputs and indicates the presence of that code by a specified output level. In its general form, a decoder has n input lines to handle n bits and from one to 2^n output lines to indicate the presence of one or more n -bit combinations. In this section, several decoders are introduced. The basic principles can be extended to other types of decoders.

After completing this section, you should be able to

- Define *decoder*
- Develop a logic circuit to decode any combination of bits
- Expand decoders to accommodate larger numbers of bits in a code
- Discuss zero suppression in 7-segment displays
- Apply decoders to specific applications

The Basic Binary Decoder

Suppose you need to determine when a binary 1001 occurs on the inputs of a digital circuit. An AND gate can be used as the basic decoding element because it produces a HIGH output only when all of its inputs are HIGH. Therefore, you must make sure that all of the

In the representation of a binary number or other weighted code in this text, the LSB is the right-most bit in a horizontal arrangement and the topmost bit in a vertical arrangement, unless specified otherwise.

inputs to the AND gate are HIGH when the binary number 1001 occurs; this can be done by inverting the two middle bits (the 0s), as shown in Figure 27.

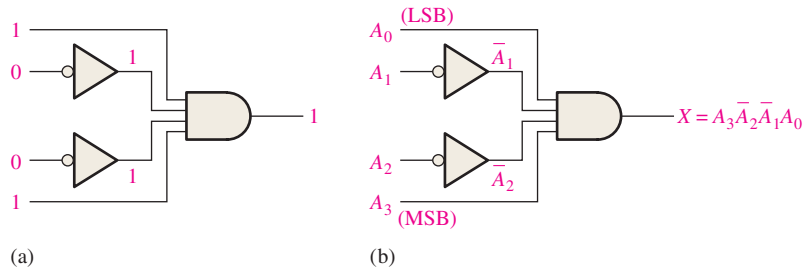


FIGURE 27 Decoding logic for the binary code 1001 with an active-HIGH output.

The logic equation for the decoder of Figure 27(a) is developed as illustrated in Figure 27(b). You should verify that the output is 0 except when $A_0 = 1, A_1 = 0, A_2 = 0,$ and $A_3 = 1$ are applied to the inputs. A_0 is the LSB and A_3 is the MSB.

If a NAND gate is used in place of the AND gate in Figure 27, a LOW output will indicate the presence of the proper binary code, which is 1001 in this case.



An *instruction* tells the computer what operation to perform. Instructions are in machine code (1s and 0s) and, in order for the computer to carry out an instruction, the instruction must be decoded. Instruction decoding is one of the steps in *instruction pipelining*, which are as follows: Instruction is read from the memory (instruction fetch), instruction is decoded, operand(s) is (are) read from memory (operand fetch), instruction is executed, and result is written back to memory. Basically, pipelining allows the next instruction to begin processing before the current one is completed.

SYSTEM NOTE

EXAMPLE 7

Determine the logic required to decode the binary number 1011 by producing a HIGH level on the output.

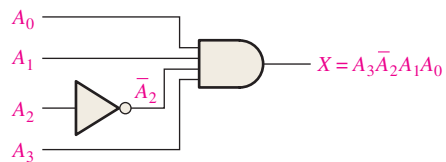
SOLUTION

The decoding function can be formed by complementing only the variables that appear as 0 in the desired binary number, as follows:

$$X = A_3\bar{A}_2A_1A_0 \quad (1011)$$

This function can be implemented by connecting the true (uncomplemented) variables $A_0, A_1,$ and A_3 directly to the inputs of an AND gate, and inverting the variable A_2 before applying it to the AND gate input. The decoding logic is shown in Figure 28.

FIGURE 28 Decoding logic for producing a HIGH output when 1011 is on the inputs.



RELATED PROBLEM

Develop the logic required to detect the binary code 10010 and produce an active-LOW output.

The 4-Bit Decoder

In order to decode all possible combinations of four bits, sixteen decoding gates are required ($2^4 = 16$). This type of decoder is commonly called either a *4-line-to-16-line decoder* because there are four inputs and sixteen outputs or a *1-of-16 decoder* because for any given code on the inputs, one of the sixteen outputs is activated. A list of the sixteen binary codes and their corresponding decoding functions is given in Table 4.

If an active-LOW output is required for each decoded number, the entire decoder can be implemented with NAND gates and inverters. In order to decode each of the sixteen binary codes, sixteen NAND gates are required (AND gates can be used to produce active-HIGH outputs).

A logic symbol for a 4-line-to-16-line (1-of-16) decoder with active-LOW outputs is shown in Figure 29. The BIN/DEC label indicates that a binary input makes the corresponding decimal output active. The input labels 8, 4, 2, and 1 represent the binary weights of the input bits ($2^3 2^2 2^1 2^0$).

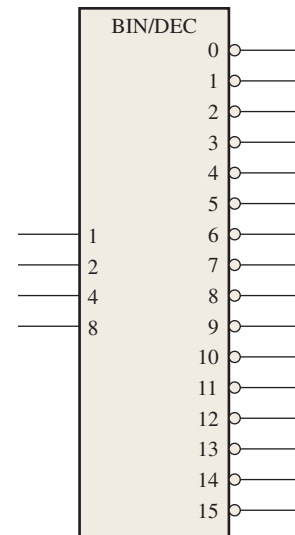


FIGURE 29 Logic symbol for a 4-line-to-16-line (1-of-16) decoder. Open file F05-29 to verify operation.

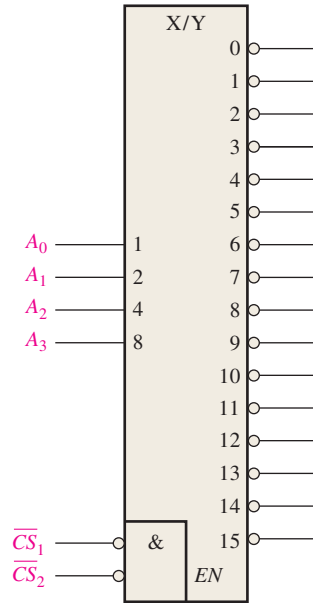


TABLE 4 • Decoding functions and truth table for a 4-line-to-16-line (1-of-16) decoder with active-LOW outputs.																					
DECIMAL DIGIT	BINARY INPUTS				DECODING FUNCTION	OUTPUTS															
	A ₃	A ₂	A ₁	A ₀		0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	0	0	0	$\bar{A}_3\bar{A}_2\bar{A}_1\bar{A}_0$	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
1	0	0	0	1	$\bar{A}_3\bar{A}_2\bar{A}_1A_0$	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	0	0	1	0	$\bar{A}_3\bar{A}_2A_1\bar{A}_0$	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1
3	0	0	1	1	$\bar{A}_3\bar{A}_2A_1A_0$	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1
4	0	1	0	0	$\bar{A}_3A_2\bar{A}_1\bar{A}_0$	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1
5	0	1	0	1	$\bar{A}_3A_2\bar{A}_1A_0$	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1
6	0	1	1	0	$\bar{A}_3A_2A_1\bar{A}_0$	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1
7	0	1	1	1	$\bar{A}_3A_2A_1A_0$	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1
8	1	0	0	0	$A_3\bar{A}_2\bar{A}_1\bar{A}_0$	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1
9	1	0	0	1	$A_3\bar{A}_2\bar{A}_1A_0$	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1
10	1	0	1	0	$A_3\bar{A}_2A_1\bar{A}_0$	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1
11	1	0	1	1	$A_3\bar{A}_2A_1A_0$	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1
12	1	1	0	0	$A_3A_2\bar{A}_1\bar{A}_0$	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1
13	1	1	0	1	$A_3A_2\bar{A}_1A_0$	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1
14	1	1	1	0	$A_3A_2A_1\bar{A}_0$	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1
15	1	1	1	1	$A_3A_2A_1A_0$	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0

EXAMPLE 8

A certain application requires that a 5-bit number be decoded. Use 4-bit decoders like the one in Figure 30 to implement the logic. Note the EN (enable) function. The binary number is represented by the format $A_4A_3A_2A_1A_0$.

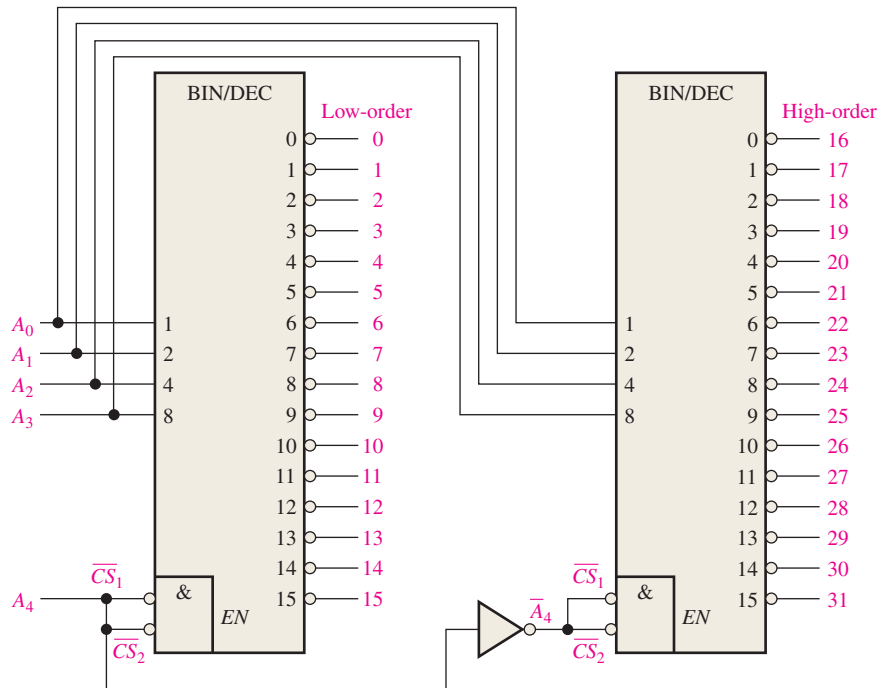
FIGURE 30



SOLUTION

Since each decoder can handle only four bits, two decoders must be used to decode five bits. The fifth bit, A_4 , is connected to the chip select inputs, \overline{CS}_1 and \overline{CS}_2 , of one decoder, and \overline{A}_4 is connected to the \overline{CS}_1 and \overline{CS}_2 inputs of the other decoder, as shown in Figure 31. When the decimal number is 15 or less, $A_4 = 0$, the low-order decoder is enabled, and the high-order decoder is disabled. When the decimal number is greater than 15, $A_4 = 1$ so $\overline{A}_4 = 0$, the high-order decoder is enabled, and the low-order decoder is disabled.

FIGURE 31



RELATED PROBLEM

Determine the output in Figure 31 that is activated for the binary input 10110.

SYSTEM EXAMPLE 2

INPUT/OUTPUT (I/O) PORT

A decoder is used in computers and other types of systems for input/output selection as depicted in the general diagram of Figure 32.

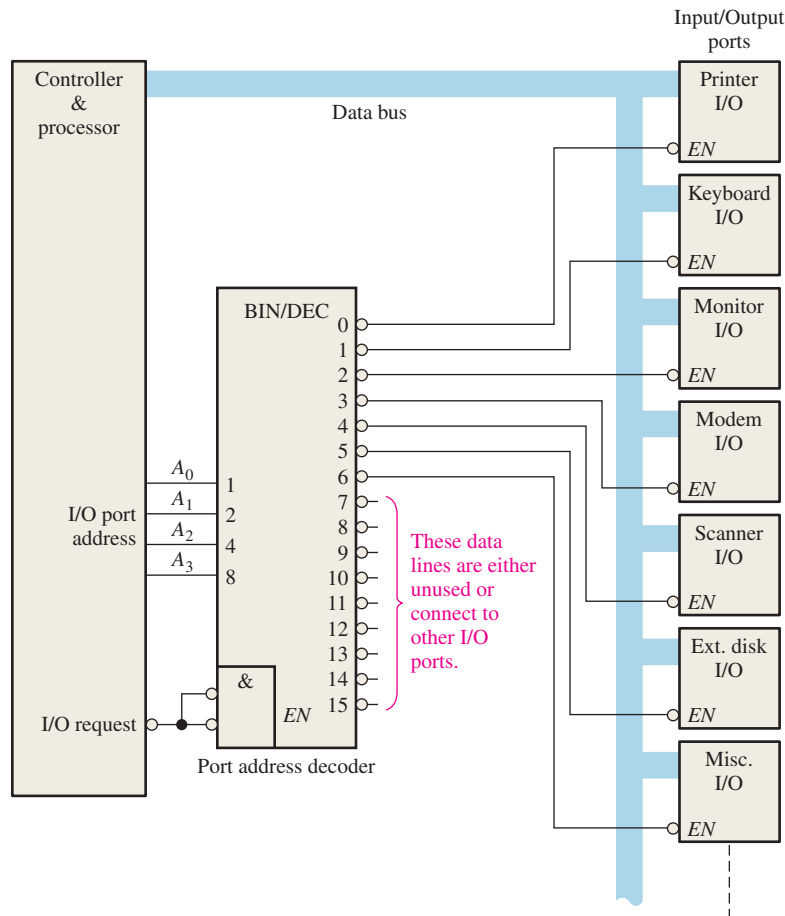


FIGURE 32 A simplified I/O port system with a port address decoder with only four address lines shown.

Computers must communicate with a variety of external devices called *peripherals* by sending and/or receiving data through what is known as input/output (I/O) ports. These external devices include printers, modems, scanners, external disk drives, keyboard, video monitors, and other computers. As illustrated in Figure 32, a decoder can be used to select the I/O port as determined by the computer so that data can be sent or received from a specific external device.

Each I/O port has a number, called an address, which uniquely identifies it. When the computer wants to communicate with a particular device, it issues the appropriate address code for the I/O port to which that particular device is connected. This binary port address is decoded and the appropriate decoder output is activated to enable the I/O port.

As shown in Figure 32, binary data are transferred within the computer on a data bus, which is a set of parallel lines. For example, an 8-bit bus consists of eight parallel lines that can carry one byte of data at a time. The data bus goes to all of the I/O ports, but any data coming in or going out will only pass through the port that is enabled by the port address decoder.

The BCD-to-Decimal Decoder

The BCD-to-decimal decoder converts each BCD code (8421 code) into one of ten possible decimal digit indications. It is frequently referred to as a *4-line-to-10-line decoder* or a *1-of-10 decoder*.

The method of implementation is the same as for the 1-of-16 decoder previously discussed, except that only ten decoding gates are required because the BCD code represents only the ten decimal digits 0 through 9. A list of the ten BCD codes and their corresponding decoding functions is given in Table 5. Each of these decoding functions is implemented with NAND gates to provide active-LOW outputs. If an active-HIGH output is required, AND gates are used for decoding. The logic is identical to that of the first ten decoding gates in the 1-of-16 decoder (see Table 4).

TABLE 5 • BCD decoding functions.

DECIMAL DIGIT	BCD CODE				DECODING FUNCTION
	A_3	A_2	A_1	A_0	
0	0	0	0	0	$\bar{A}_3\bar{A}_2\bar{A}_1\bar{A}_0$
1	0	0	0	1	$\bar{A}_3\bar{A}_2\bar{A}_1A_0$
2	0	0	1	0	$\bar{A}_3\bar{A}_2A_1\bar{A}_0$
3	0	0	1	1	$\bar{A}_3\bar{A}_2A_1A_0$
4	0	1	0	0	$\bar{A}_3A_2\bar{A}_1\bar{A}_0$
5	0	1	0	1	$\bar{A}_3A_2\bar{A}_1A_0$
6	0	1	1	0	$\bar{A}_3A_2A_1\bar{A}_0$
7	0	1	1	1	$\bar{A}_3A_2A_1A_0$
8	1	0	0	0	$A_3\bar{A}_2\bar{A}_1\bar{A}_0$
9	1	0	0	1	$A_3\bar{A}_2\bar{A}_1A_0$

EXAMPLE 9

Figure 33(a) shows a BCD/DEC decoder. If the input waveforms in Figure 33(b) are applied to the inputs of the decoder, show the output waveforms.

SOLUTION

The output waveforms are shown in Figure 33(c). As you can see, the inputs are sequenced through the BCD for digits 0 through 9. The output waveforms in the timing diagram indicate that sequence on the decimal-value outputs.

RELATED PROBLEM

Construct a timing diagram showing input and output waveforms for the case where the BCD inputs sequence through the decimal numbers as follows: 0, 2, 4, 6, 8, 1, 3, 5, and 9.

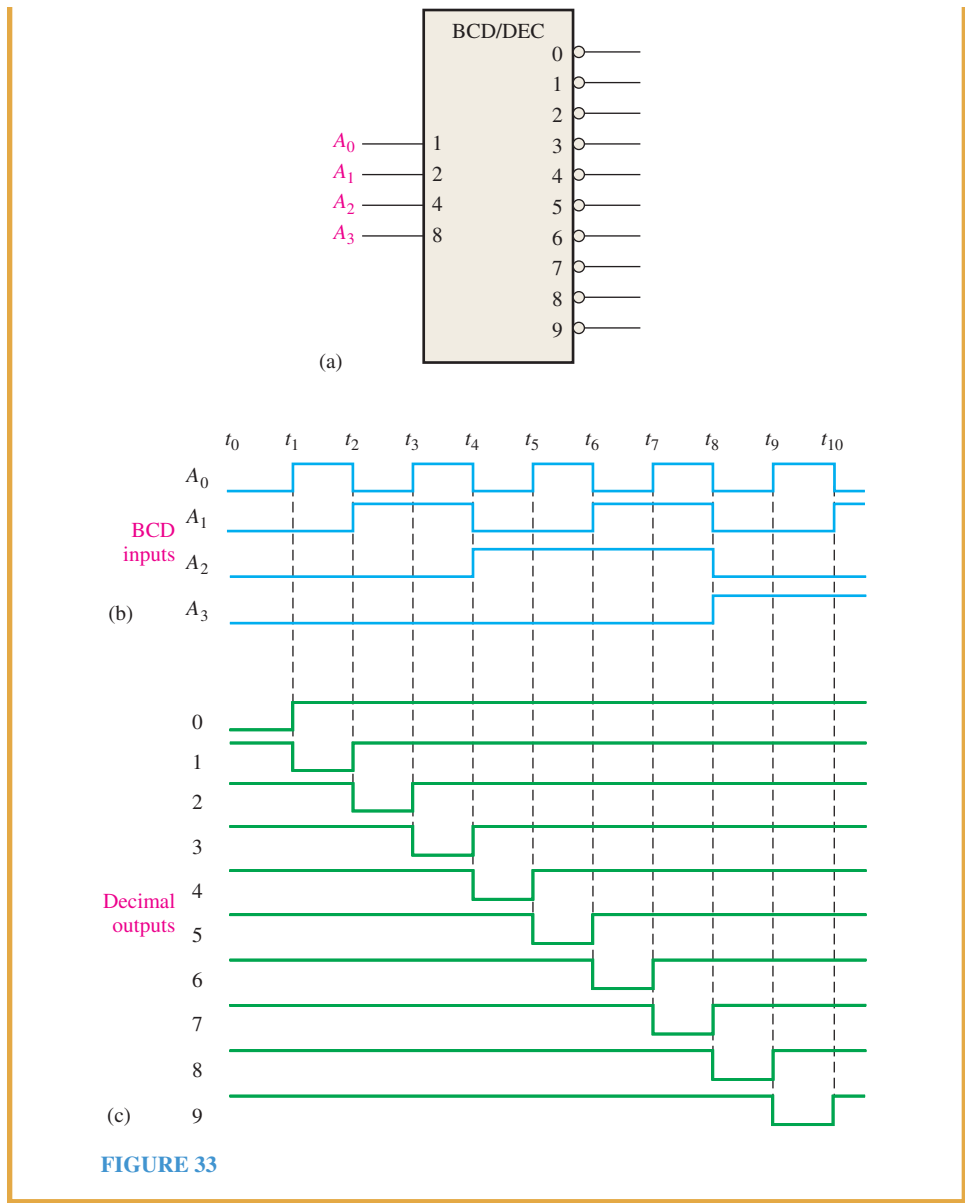


FIGURE 33

The BCD-to-7-Segment Decoder

The BCD-to-7-segment decoder accepts the BCD code on its inputs and provides outputs to drive 7-segment display devices to produce a decimal readout. The logic diagram for a basic 7-segment decoder is shown in Figure 34. The active-LOW outputs drive a common-cathode type of 7-segment display.

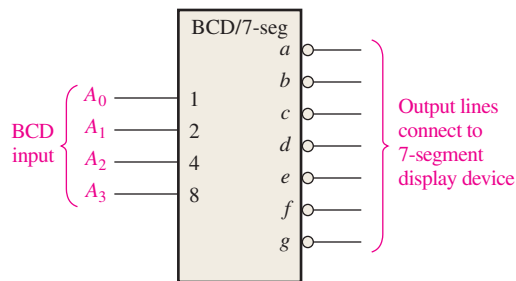


FIGURE 34 Logic symbol for a BCD-to-7-segment decoder/driver with active-LOW outputs. Open file F05-34 to verify operation.

MULTISIM



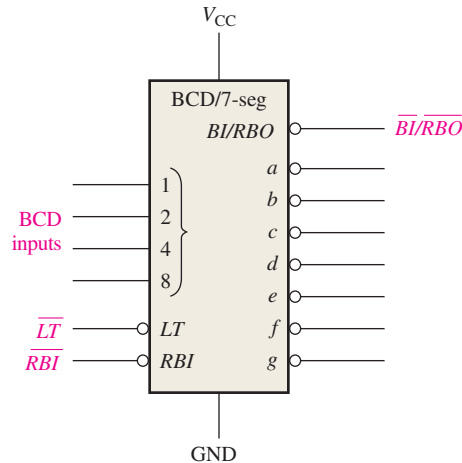
SYSTEM EXAMPLE 3



SEVEN-SEGMENT DISPLAY

In addition to its decoding and segment drive capability, a BCD-to-7-segment decoder/driver often has several additional features as indicated by the \overline{LT} , \overline{RBI} , $\overline{BI}/\overline{RBO}$ functions in the logic symbol of Figure 35. As indicated by the bubbles on the logic symbol, all of the outputs (a through g) are active-LOW as are the \overline{LT} (lamp test), \overline{RBI} (ripple blanking input), and $\overline{BI}/\overline{RBO}$ (blanking input/ripple blanking output) functions. The outputs can drive a common-cathode 7-segment display directly.

FIGURE 35



When a LOW is applied to the \overline{LT} input and the $\overline{BI}/\overline{RBO}$ is HIGH, all of the seven segments in the display are turned on. Lamp test is used to verify that no segments are burned out.

Zero suppression is a feature used for multidigit displays to blank out unnecessary zeros and results in leading or trailing zeros in a number not showing on a display. For example, in a 6-digit display the number 6.4 may be displayed as 006.400 if the zeros are not blanked out. Blanking the zeros at the front of a number is called *leading zero suppression* and blanking the zeros at the back of the number is called *trailing zero suppression*. Keep in mind that only nonessential zeros are blanked. With zero suppression, the number 030.080 will be displayed as 30.08 (the essential zeros remain).

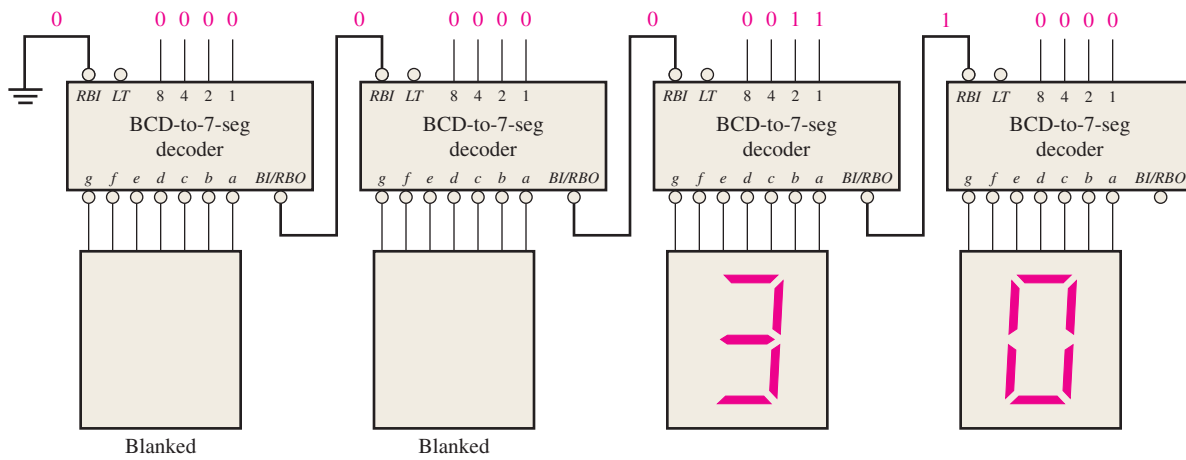
Zero suppression is accomplished using the \overline{RBI} and $\overline{BI}/\overline{RBO}$ functions. \overline{RBI} is the ripple blanking input and \overline{RBO} is the ripple blanking output; these are used for zero suppression. \overline{BI} is the blanking input that shares the same pin with \overline{RBO} ; in other words, the $\overline{BI}/\overline{RBO}$ pin can be used as an input or an output. When used as a \overline{BI} (blanking input), all segment outputs are HIGH (nonactive) when \overline{BI} is LOW, which overrides all other inputs. The \overline{BI} function is not part of the zero suppression capability of the device.

All of the segment outputs of the decoder are nonactive (HIGH) if a zero code (0000) is on its BCD inputs and if its \overline{RBI} is LOW. This causes the display to be blank and produces a LOW \overline{RBO} .

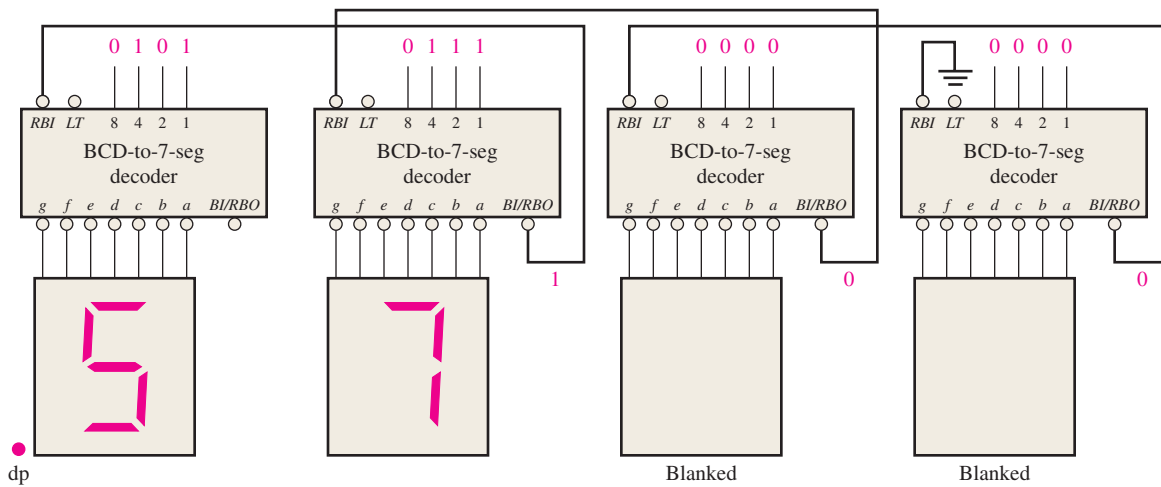
The logic diagram in Figure 36(a) illustrates leading zero suppression for a whole number. The highest-order digit position (left-most) is always blanked if a zero code is on its BCD inputs because the \overline{RBI} of the most-significant decoder is made LOW by connecting it to ground. The \overline{RBO} of each decoder is connected to the \overline{RBI} of the next lowest-order decoder so that all zeros to the left of the first nonzero digit are blanked. For example, in part (a) of the figure the two highest-order digits are zeros and therefore are blanked. The remaining two digits, 3 and 0 are displayed.

The logic diagram in Figure 36(b) illustrates trailing zero suppression for a fractional number. The lowest-order digit (right-most) is always blanked if a zero code is on its BCD inputs because the \overline{RBI} is connected to ground. The \overline{RBO} of each decoder is connected

FUNCTIONS OF COMBINATIONAL LOGIC



(a) Illustration of leading zero suppression



(b) Illustration of trailing zero suppression

FIGURE 36 Examples of zero suppression.

to the \overline{RBI} of the next highest-order decoder so that all zeros to the right of the first nonzero digit are blanked. In part (b) of the figure, the two lowest-order digits are zeros and therefore are blanked. The remaining two digits, 5 and 7 are displayed. To combine both leading and trailing zero suppression in one display and to have decimal point capability, additional logic is required.

SECTION 6 CHECKUP

1. A 3-line-to-8-line decoder can be used for octal-to-decimal decoding. When a binary 101 is on the inputs, which output line is activated?
2. How many 1-of-16 decoders are necessary to decode a 6-bit binary number?
3. Would you select a decoder/driver with active-HIGH or active-LOW outputs to drive a common-cathode 7-segment LED display?

7 ENCODERS

An **encoder** is a combinational logic circuit that essentially performs a “reverse” decoder function. An encoder accepts an active level on one of its inputs representing a digit, such as a decimal or octal digit, and converts it to a coded output, such as BCD or binary. Encoders can also be devised to encode various symbols and alphabetic characters. The process of converting from familiar symbols or numbers to a coded format is called *encoding*.

After completing this section, you should be able to

- Determine the logic for a decimal-to-BCD encoder
- Explain the purpose of the priority feature in encoders
- Expand an encoder
- Apply the encoder to a specific system example

The Decimal-to-BCD Encoder

This type of encoder has ten inputs—one for each decimal digit—and four outputs corresponding to the BCD code, as shown in Figure 37. This is a basic 10-line-to-4-line encoder.

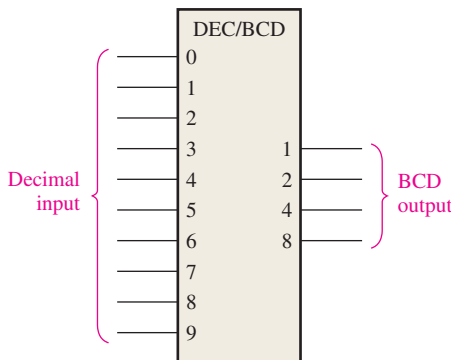


FIGURE 37 Logic symbol for a decimal-to-BCD encoder.

The BCD (8421) code is listed in Table 6. From this table you can determine the relationship between each BCD bit and the decimal digits in order to analyze the logic. For instance, the most significant bit of the BCD code, A_3 , is always a 1 for decimal digit 8 or 9. An OR expression for bit A_3 in terms of the decimal digits can therefore be written as

$$A_3 = 8 + 9$$

Bit A_2 is always a 1 for decimal digit 4, 5, 6 or 7 and can be expressed as an OR function as follows:

$$A_2 = 4 + 5 + 6 + 7$$

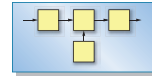
Bit A_1 is always a 1 for decimal digit 2, 3, 6, or 7 and can be expressed as

$$A_1 = 2 + 3 + 6 + 7$$

TABLE 6				
DECIMAL DIGIT	BCD CODE			
	A_3	A_2	A_1	A_0
0	0	0	0	0
1	0	0	0	1
2	0	0	1	0
3	0	0	1	1
4	0	1	0	0
5	0	1	0	1
6	0	1	1	0
7	0	1	1	1
8	1	0	0	0
9	1	0	0	1

An *assembler* can be thought of as a software encoder because it interprets the mnemonic instructions with which a program is written and carries out the applicable encoding to convert each mnemonic to a machine code instruction (series of 1s and 0s) that the computer can understand. Examples of mnemonic instructions for a microprocessor are ADD, MOV (move data), MUL (multiply), XOR, JMP (jump), and OUT (output to a port).

SYSTEM NOTE



Finally, A_0 is always a 1 for decimal digit 1, 3, 5, 7, or 9. The expression for A_0 is

$$A_0 = 1 + 3 + 5 + 7 + 9$$

Now let's look at the logic circuitry required for encoding each decimal digit to a BCD code by using the logic expressions just developed. It is simply a matter of ORing the appropriate decimal digit input lines to form each BCD output. The basic encoder logic resulting from these expressions is shown in Figure 38.

The basic operation of the circuit in Figure 38 is as follows: When a HIGH appears on *one* of the decimal digit input lines, the appropriate levels occur on the four BCD output lines. For instance, if input line 9 is HIGH (assuming all other input lines are LOW), this condition will produce a HIGH on outputs A_0 and A_3 and LOWs on outputs A_1 and A_2 , which is the BCD code (1001) for decimal 9.

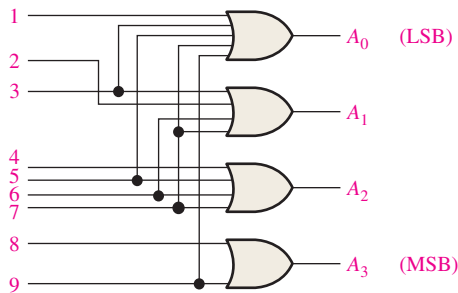


FIGURE 38 Logic diagram of a decimal-to-BCD encoder. A 0-digit input is not needed because the BCD outputs are all LOW when there are no HIGH inputs.

THE DECIMAL-TO-BCD PRIORITY ENCODER This type of encoder performs the same basic encoding function as previously discussed. A **priority encoder** also offers additional flexibility in that it can be used in applications that require priority detection. The priority function means that the encoder will produce a BCD output corresponding to the *highest-order decimal digit* input that is active and will ignore any other lower-order active inputs. For instance, if the 6 and the 3 inputs are both active, the BCD output is 0110 (which represents decimal 6).

A priority encoder with active-LOW inputs (0) for decimal digits 1 through 9 and active-LOW BCD outputs is indicated in the logic symbol in Figure 39. A BCD zero output is represented when none of the inputs is active.

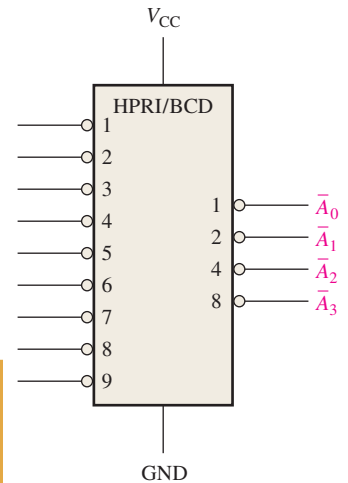


FIGURE 39 A decimal-to-BCD priority encoder (HPRI means highest value input has priority).

EXAMPLE 10

If LOW levels appear on inputs 3, 4, and 7 of the encoder shown in Figure 39, indicate the state of the four outputs. All other inputs are HIGH.

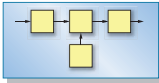
SOLUTION

Input 7 is the highest-order decimal digit input having a LOW level and represents decimal 7. Therefore, the output levels indicate the BCD code for decimal 7 where \bar{A}_0 is the LSB and \bar{A}_3 is the MSB. Output \bar{A}_0 is LOW, \bar{A}_1 is LOW, \bar{A}_2 is LOW, and \bar{A}_3 is HIGH.

RELATED PROBLEM

What are the outputs of the same encoder if all its inputs are LOW? If all its inputs are HIGH?

SYSTEM EXAMPLE 4



KEYPAD ENCODER

The ten decimal digits on a numeric keypad must be encoded for processing by the logic circuitry. In this example, when one of the keys is pressed, the decimal digit is encoded to the corresponding BCD code. Figure 40 shows a simple keyboard encoder arrangement using a priority encoder. The keys are represented by ten push-button switches, each with a **pull-up resistor** to +V. The pull-up resistor ensures that the line is HIGH when a key is not depressed. When a key is depressed, the line is connected to ground, and a LOW is applied to the corresponding encoder input. The zero key is not connected because the BCD output represents zero when none of the other keys is depressed. In systems such as the computer, the keystrokes are encoded into ASCII because both numeric and alphanumeric characters are used.

The BCD complement output of the encoder goes into a storage device, and each successive BCD code is stored until the entire number has been entered.

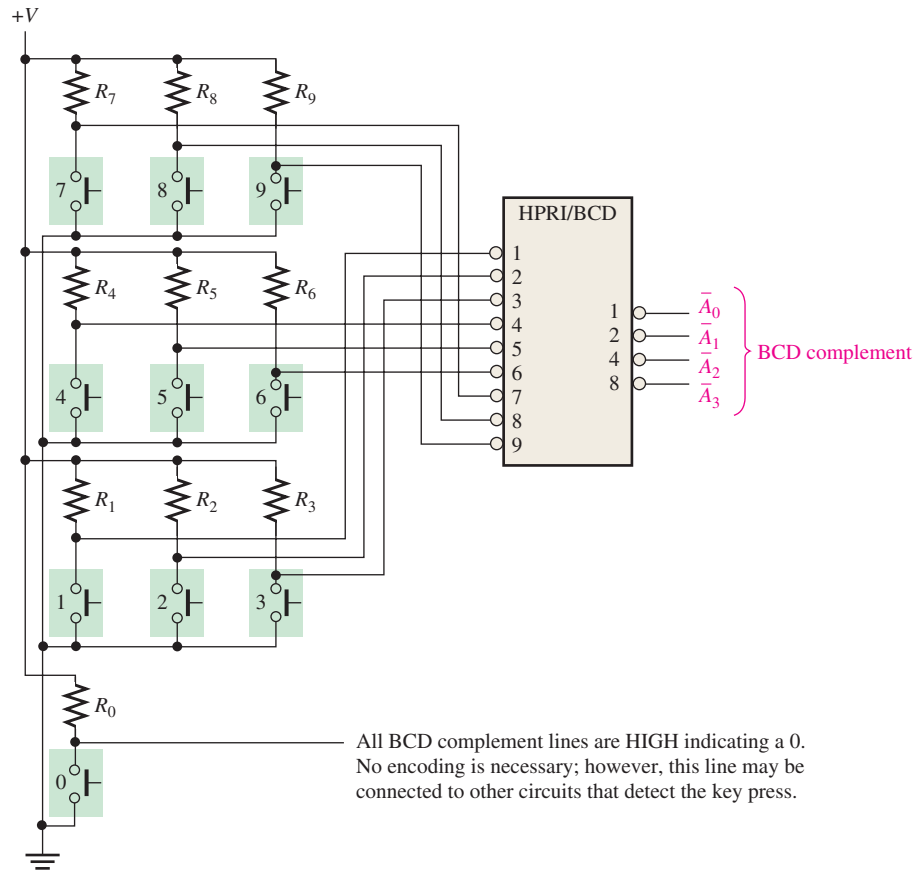


FIGURE 40 A simplified keyboard encoder.

SECTION 7 CHECKUP

- Suppose the HIGH levels are applied to the 2 input and the 9 input of the circuit in Figure 38.
 - What are the states of the output lines?
 - Does this represent a valid BCD code?
 - What is the restriction on the encoder logic in Figure 38?
- What is the $\bar{A}_3 \bar{A}_2 \bar{A}_1 \bar{A}_0$ output when LOWs are applied to inputs 4 and 8 of the priority encoder in Figure 39?
 - What does this output represent?

8 CODE CONVERTERS

In this section, we will examine some methods of using combinational logic circuits to convert from one code to another.

After completing this section, you should be able to

- Explain the process for converting BCD to binary
- Use exclusive-OR gates for conversions between binary and Gray codes

BCD-to-Binary Conversion

One method of BCD-to-binary code conversion uses adder circuits. The basic conversion process is as follows:

- The value, or weight, of each bit in the BCD number is represented by a binary number.
- All of the binary representations of the weights of bits that are 1s in the BCD number are added.
- The result of this addition is the binary equivalent of the BCD number.

A more concise statement of this operation is

The binary numbers representing the weights of the BCD bits are summed to produce the total binary number.

Let's examine an 8-bit BCD code (one that represents a 2-digit decimal number) to understand the relationship between BCD and binary. For instance, you already know that the decimal number 87 can be expressed in BCD as

$$\underbrace{1000}_8 \quad \underbrace{0111}_7$$

The left-most 4-bit group represents 80, and the right-most 4-bit group represents 7. That is, the left-most group has a weight of 10, and the right-most group has a weight of 1. Within each group, the binary weight of each bit is as follows:

	TENS DIGIT				UNITS DIGIT			
Weight:	80	40	20	10	8	4	2	1
Bit designation:	B_3	B_2	B_1	B_0	A_3	A_2	A_1	A_0

FUNCTIONS OF COMBINATIONAL LOGIC

The binary equivalent of each BCD bit is a binary number representing the weight of that bit within the total BCD number. This representation is given in Table 7.

TABLE 7 • Binary representations of BCD bit weights.								
BCD BIT	BCD WEIGHT	(MSB)	BINARY REPRESENTATION					(LSB)
		64	32	16	8	4	2	1
A_0	1	0	0	0	0	0	0	1
A_1	2	0	0	0	0	0	1	0
A_2	4	0	0	0	0	1	0	0
A_3	8	0	0	0	1	0	0	0
B_0	10	0	0	0	1	0	1	0
B_1	20	0	0	1	0	1	0	0
B_2	40	0	1	0	1	0	0	0
B_3	80	1	0	1	0	0	0	0

If the binary representations for the weights of all the 1s in the BCD number are added, the result is the binary number that corresponds to the BCD number. Example 11 illustrates this.

MULTISIM



Open file E05-11 and run the simulation to observe the operation of a BCD-to-binary logic circuit.

EXAMPLE 11

Convert the BCD numbers 00100111 (decimal 27) and 10011000 (decimal 98) to binary.

SOLUTION

Write the binary representations of the weights of all 1s appearing in the numbers, and then add them together.

80	40	20	10	8	4	2	1	
0	0	1	0	0	1	1	1	
								0000001 1
								0000010 2
								0000100 4
								+ 0010100 20
								0011011 Binary for decimal 27

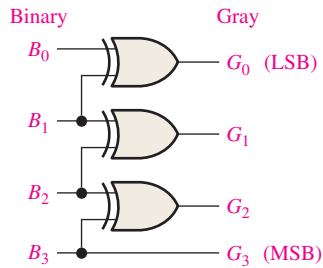
80	40	20	10	8	4	2	1	
1	0	0	1	1	0	0	0	
								0001000 8
								0001010 10
								+ 1010000 80
								1100010 Binary for decimal 98

RELATED PROBLEM

Show the process of converting 01000001 in BCD to binary.

Binary-to-Gray and Gray-to-Binary Conversion

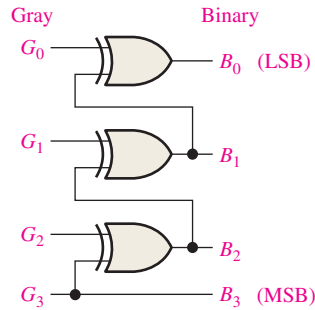
Exclusive-OR gates can be used for Gray-binary conversions. Programmable logic devices (PLDs) can also be programmed for these code conversions. Figure 41 shows a 4-bit binary-to-Gray code converter, and Figure 42 illustrates a 4-bit Gray-to-binary converter.



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FIGURE 41 Four-bit binary-to-Gray conversion logic. Open file F05-41 to verify operation.



MULTISIM



FIGURE 42 Four-bit Gray-to-binary conversion logic. Open file F05-42 to verify operation.

EXAMPLE 12

- Convert the binary number 0101 to Gray code with exclusive-OR gates.
- Convert the Gray code 1011 to binary with exclusive-OR gates.

SOLUTION

- 0101₂ is 0111 Gray. See Figure 43(a).
- 1011 Gray is 1101₂. See Figure 43(b).

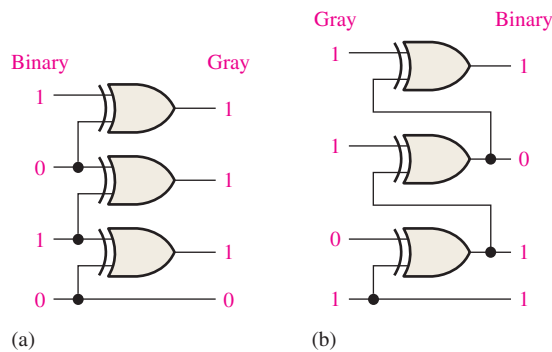


FIGURE 43

RELATED PROBLEM

How many exclusive-OR gates are required to convert 8-bit binary to Gray?

SECTION 8 CHECKUP

- Convert the BCD number 1000101 to binary.
- Draw the logic diagram for converting an 8-bit binary number to Gray code.

9 MULTIPLEXERS (DATA SELECTORS)

A **multiplexer (MUX)** is a device that allows digital information from several sources to be routed onto a single line for transmission over that line to a common destination. The basic multiplexer has several data-input lines and a single output line. It also has data-select inputs, which permit digital data on any one of the inputs to be switched to the output line. Multiplexers are also known as data selectors.

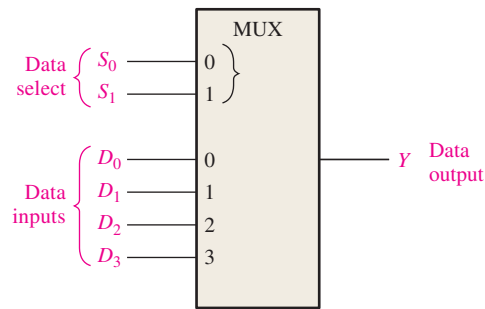
After completing this section, you should be able to

- Explain the basic operation of a multiplexer
- Expand a multiplexer to handle more data inputs
- Use the multiplexer as a logic function generator

In a multiplexer, data goes from several lines to one line.

A logic symbol for a 4-input multiplexer (MUX) is shown in Figure 44. Notice that there are two data-select lines because with two select bits, any one of the four data-input lines can be selected.

FIGURE 44 Logic symbol for a 1-of-4 data selector/multiplexer.



In Figure 44, a 2-bit code on the data-select (S) inputs will allow the data on the selected data input to pass through to the data output. If a binary 0 ($S_1 = 0$ and $S_0 = 0$) is applied to the data-select lines, the data on input D_0 appear on the data-output line. If a binary 1 ($S_1 = 0$ and $S_0 = 1$) is applied to the data-select lines, the data on input D_1 appear on the data output. If a binary 2 ($S_1 = 1$ and $S_0 = 0$) is applied, the data on D_2 appear on the output. If a binary 3 ($S_1 = 1$ and $S_0 = 1$) is applied, the data on D_3 are switched to the output line. A summary of this operation is given in Table 8.

TABLE 8 • Data selection for a 1-of-4-multiplexer.

DATA-SELECT INPUTS		INPUT SELECTED
S_1	S_0	
0	0	D_0
0	1	D_1
1	0	D_2
1	1	D_3

Now let's look at the logic circuitry required to perform this multiplexing operation. The data output is equal to the state of the *selected* data input. You can therefore, derive a logic expression for the output in terms of the data input and the select inputs.

The data output is equal to D_0 only if $S_1 = 0$ and $S_0 = 0$: $Y = D_0\bar{S}_1\bar{S}_0$.

The data output is equal to D_1 only if $S_1 = 0$ and $S_0 = 1$: $Y = D_1\bar{S}_1S_0$.

The data output is equal to D_2 only if $S_1 = 1$ and $S_0 = 0$: $Y = D_2S_1\bar{S}_0$.

The data output is equal to D_3 only if $S_1 = 1$ and $S_0 = 1$: $Y = D_3S_1S_0$.

A *bus* is a single or multiple conductor pathway along which electrical signals are sent from one part of a system to another. In computer networks, a *shared bus* is one that is connected to all the microprocessors in the system in order to exchange data. A shared bus may contain memory and input/output devices that can be accessed by all the microprocessors in the system. Access to the shared bus is controlled by a *bus arbiter* (a multiplexer of sorts) that allows only one microprocessor at a time to use the system's shared bus.

SYSTEM NOTE



When these terms are ORed, the total expression for the data output is

$$Y = D_0\bar{S}_1\bar{S}_0 + D_1\bar{S}_1S_0 + D_2S_1\bar{S}_0 + D_3S_1S_0$$

The implementation of this equation requires four 3-input AND gates, a 4-input OR gate, and two inverters to generate the complements of S_1 and S_0 , as shown in Figure 45. Because data can be selected from any one of the input lines, this circuit is also referred to as a **data selector**.

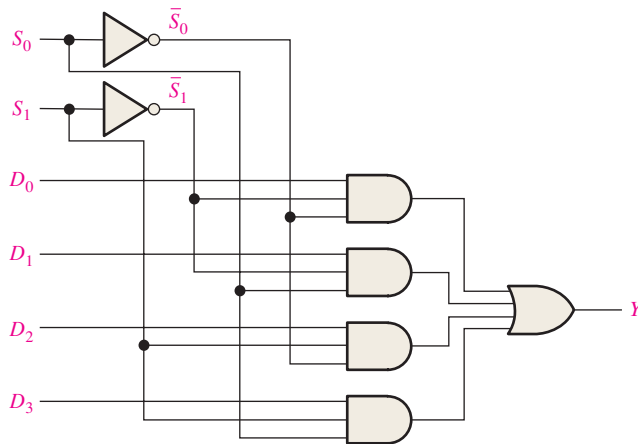


FIGURE 45 Logic diagram for a 4-input multiplexer. Open file F05-45 to verify operation.

MULTISIM



EXAMPLE 13

The data-input and data-select waveforms in Figure 46(a) are applied to the multiplexer in Figure 45. Determine the output waveform in relation to the inputs.

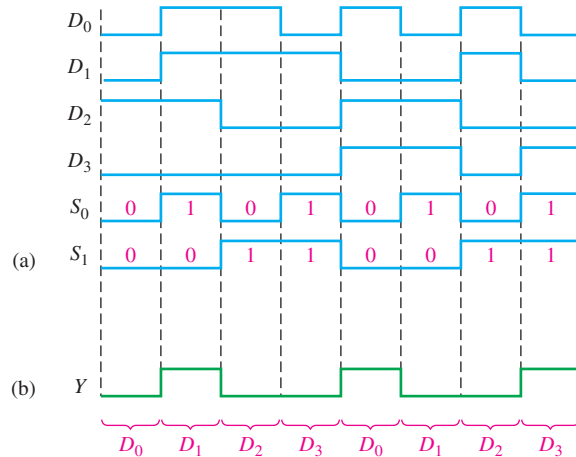


FIGURE 46

SOLUTION

The binary state of the data-select inputs during each interval determines which data input is selected. Notice that the data-select inputs go through a repetitive binary sequence 00, 01, 10, 11, 00, 01, 10, 11, and so on. The resulting output waveform is shown in Figure 46(b).

RELATED PROBLEM

Construct a timing diagram showing all inputs and the output if the S_0 and S_1 waveforms in Figure 46 are interchanged.

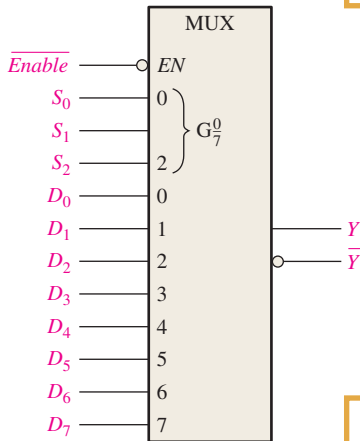


FIGURE 47 Logic symbol for an 8-input data selector/multiplexer.

An 8-input Data Selector/Multiplexer

The multiplexer shown in Figure 47 has eight data inputs (D_0 – D_7) and, therefore, three data-select or address input lines (S_0 – S_2). Three bits are required to select any one of the eight data inputs ($2^3 = 8$). A LOW on the \overline{Enable} input allows the selected input data to pass through to the output. Notice that the data output and its complement are both available. The G_7^0 label within the logic symbol indicates the AND relationship between the data-select inputs and each of the data inputs 0 through 7.

EXAMPLE 14

Use the 8-input multiplexer in Figure 47 and any other logic necessary to multiplex 16 data lines onto a single data-output line.

SOLUTION

An implementation of this function is shown in Figure 48. Four bits are required to select one of 16 data inputs ($2^4 = 16$). In this application the \overline{Enable} input is used as the most significant data-select bit. When the MSB in the data-select code is LOW, the left multiplexer is enabled, and one of the data inputs (D_0 through D_7) is selected by the other three data-select bits. When the data-select MSB is HIGH, the right multiplexer is enabled, and one of the data inputs (D_8 through D_{15}) is selected. The selected input data are then passed through to the negative-OR gate and onto the single output line.

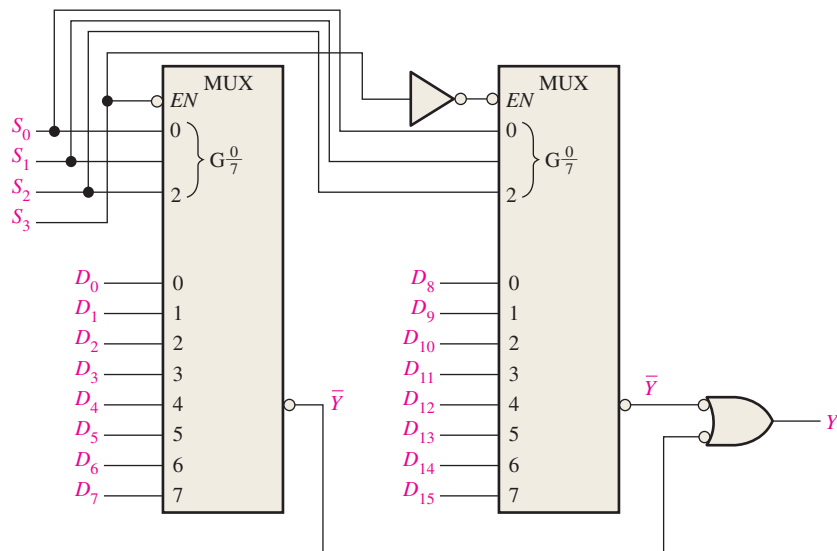


FIGURE 48 A 16-input multiplexer.

RELATED PROBLEM

Determine the codes on the select inputs required to select each of the following data inputs: D_0 , D_4 , D_8 , and D_{13} .

SYSTEM EXAMPLE 5

MULTIPLEXED DISPLAY

Many types of systems require data to be displayed in readable form. Figure 49 shows a simplified method of multiplexing BCD numbers to a 7-segment display. Two digit numbers are displayed on the 7-segment readout by the use of a single BCD-to-7-segment decoder. This basic method of display multiplexing can be extended to displays with any number of digits.

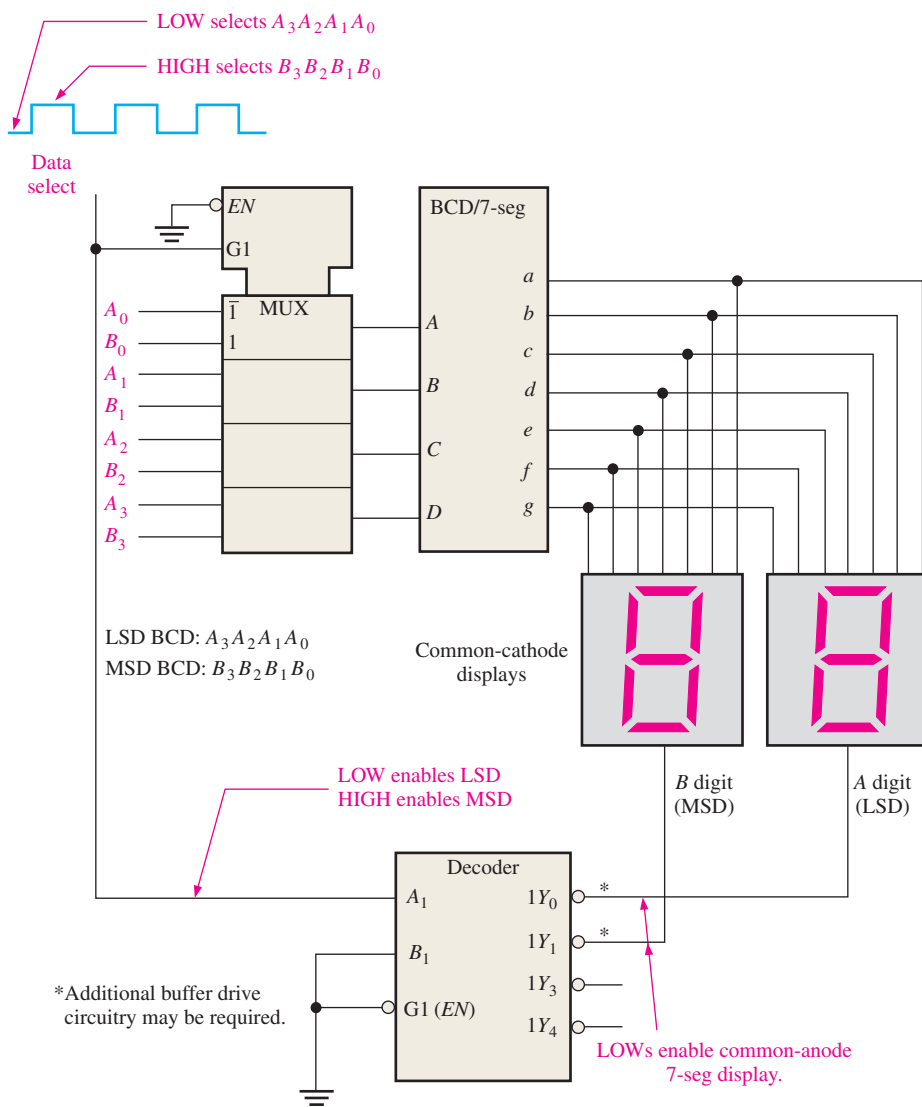
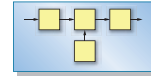


FIGURE 49 Simplified 7-segment display multiplexing logic.

The basic operation is as follows. Two BCD digits ($A_3A_2A_1A_0$ and $B_3B_2B_1B_0$) are applied to the multiplexer, which consists of four separate 2-input multiplexers. Each of the four multiplexers shares a common data-select line and a common *Enable*. Because there are only two inputs to be selected in each multiplexer, a single data-select input is

sufficient. Notice that the four multiplexers are indicated by the partitioned outline and that the inputs common to all four multiplexers are indicated as inputs to the notched block at the top, which is called the *common control block*. All labels within the upper MUX block apply to the other blocks below it.

Notice the 1 and $\bar{1}$ labels in the MUX blocks and the G1 label in the common control block. These labels are an example of the **dependency notation** system specified in the ANSI/IEEE Standard 91-1984. In this case G1 indicates an AND relationship between the data-select input and the data inputs with 1 or $\bar{1}$ labels. (The $\bar{1}$ means that the AND relationship applies to the complement of the G1 input.) In other words, when the data-select input is HIGH, the *B* inputs of the multiplexers are selected; and when the data-select input is LOW, the *A* inputs are selected. A “G” is always used to denote AND dependency.

A square wave is applied to the data-select line, and when it is LOW, the *A* bits ($A_3A_2A_1A_0$) are passed through to the inputs of the BCD-to-7-segment decoder. The LOW on the data-select also puts a LOW on the A_1 input of the 2-line-to-4-line decoder, thus activating its 0 output and enabling the *A*-digit display by effectively connecting its common terminal to ground. The *A* digit is now *on* and the *B* digit is *off*.

When the data-select line goes HIGH, the *B* bits ($B_3B_2B_1B_0$) are passed through to the inputs of the BCD-to-7-segment decoder. Also, the decoder’s 1 output is activated, thus enabling the *B*-digit display. The *B* digit is now *on* and the *A* digit is *off*. The cycle repeats at the frequency of the data-select square wave. This frequency must be high enough to prevent visual flicker as the digit displays are multiplexed.

A LOGIC FUNCTION GENERATOR A useful application of the data selector/multiplexer is in the generation of combinational logic functions in sum-of-products form. When used in this way, the device can replace discrete gates.

To illustrate, an 8-input data selector/multiplexer can be used to implement any specified 3-variable logic function if the variables are connected to the data-select inputs and each data input is set to the logic level required in the truth table for that function. For example, if the function is a 1 when the variable combination is $\bar{A}_2A_1\bar{A}_0$, the 2 input (selected by 010) is connected to a HIGH. This HIGH is passed through to the output when this particular combination of variables occurs on the data-select lines. Example 15 will help clarify this application.

EXAMPLE 15

Implement the logic function specified in Table 9 by using an 8-input data selector/multiplexer.

TABLE 9			
INPUTS			OUTPUT
A_2	A_1	A_0	Y
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0

SOLUTION

Notice from the truth table that Y is a 1 for the following input variable combinations: 001, 011, 101, and 110. For all other combinations, Y is 0. For this function to be implemented with the data selector, the data input selected by each of the above-mentioned combinations must be connected to a HIGH (5 V). All the other data inputs must be connected to a LOW (ground), as shown in Figure 50.

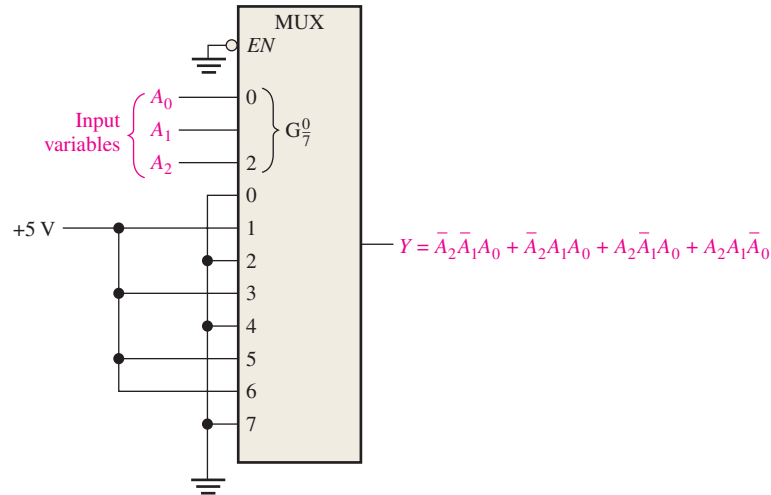


FIGURE 50 Data selector/multiplexer connected as a 3-variable logic function generator.

RELATED PROBLEM

Use the data selector/multiplexer to implement the following expression:

$$Y = \bar{A}_2\bar{A}_1\bar{A}_0 + A_2\bar{A}_1\bar{A}_0 + \bar{A}_2A_1\bar{A}_0$$

Example 15 illustrated how the 8-input data selector can be used as a logic function generator for three variables. Actually, this device can be also used as a 4-variable logic function generator by the utilization of one of the bits (A_0) in conjunction with the data inputs.

A 4-variable truth table has sixteen combinations of input variables. When an 8-bit data selector is used, each input is selected twice: the first time when A_0 is 0 and the second time when A_0 is 1. With this in mind, the following rules can be applied (Y is the output, and A_0 is the least significant bit):

1. If $Y = 0$ both times a given data input is selected by a certain combination of the input variables, $A_3A_2A_1$, connect that data input to ground (0).
2. If $Y = 1$ both times a given data input is selected by a certain combination of the input variables, $A_3A_2A_1$, connect the data input to +V (1).
3. If Y is different the two times a given data input is selected by a certain combination of the input variables, $A_3A_2A_1$, and if $Y = A_0$, connect that data input to A_0 .
4. If Y is different the two times a given data input is selected by a certain combination of the input variables, $A_3A_2A_1$, and if $Y = \bar{A}_0$, connect that data input to \bar{A}_0 .

EXAMPLE 16

Implement the logic function in Table 10 by using an 8-input data selector/multiplexer.

SOLUTION

The data-select inputs are $A_3A_2A_1$. In the first row of the table, $A_3A_2A_1 = 000$ and $Y = A_0$. In the second row, where $A_3A_2A_1$ again is 000, $Y = A_0$. Thus, A_0 is connected to the 0 input. In the third row of the table, $A_3A_2A_1 = 001$ and $Y = \bar{A}_0$. Also, in the fourth row, when $A_3A_2A_1$ again is 001, $Y = \bar{A}_0$. Thus, A_0 is inverted and

TABLE 10					
DECIMAL DIGIT	INPUTS				OUTPUT Y
	A ₃	A ₂	A ₁	A ₀	
0	0	0	0	0	0
1	0	0	0	1	1
2	0	0	1	0	1
3	0	0	1	1	0
4	0	1	0	0	0
5	0	1	0	1	1
6	0	1	1	0	1
7	0	1	1	1	1
8	1	0	0	0	1
9	1	0	0	1	0
10	1	0	1	0	1
11	1	0	1	1	0
12	1	1	0	0	1
13	1	1	0	1	1
14	1	1	1	0	0
15	1	1	1	1	1

connected to the 1 input. This analysis is continued until each input is properly connected according to the specified rules. The implementation is shown in Figure 51.

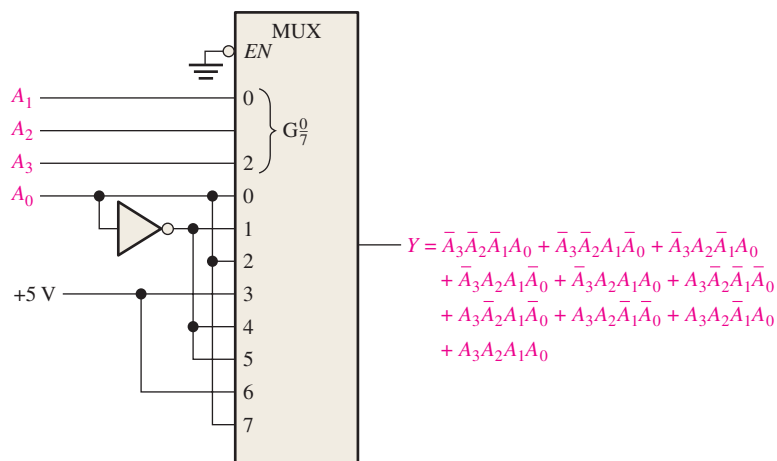


FIGURE 51 Data selector/multiplexer connected as a 4-variable logic function generator.

RELATED PROBLEM

In Table 10, if Y = 0 when the inputs are all zeros and is alternately a 1 and a 0 for the remaining rows in the table, use a data selector/multiplexer to implement the resulting logic function.

SECTION 9 CHECKUP

- In Figure 45, $D_0 = 1$, $D_1 = 0$, $D_2 = 1$, $D_3 = 0$, $S_0 = 1$, and $S_1 = 0$. What is the output?
- How many select or address inputs are required for a 32-bit data selector/multiplexer?
- An 8-bit multiplexer like in Figure 47 has alternating LOW and HIGH levels on its data inputs beginning with $D_0 = 0$. The data-select lines are sequenced through a binary count (000, 001, 010, and so on) at a frequency of 1 kHz. The enable input is LOW. Describe the data output waveform.
- Briefly describe the purpose of each of the following devices in Figure 49:
 - Multiplexer
 - BCD-to-7-segment decoder/driver
 - 2-line-to-4-line decoder

10 DEMULTIPLEXERS

A **demultiplexer (DEMUX)** basically reverses the multiplexing function. It takes digital information from one line and distributes it to a given number of output lines. For this reason, the demultiplexer is also known as a data distributor. As you will learn, decoders can also be used as demultiplexers.

After completing this section, you should be able to

- Explain the basic operation of a demultiplexer
- Describe how the 4-line-to-16-line decoder can be used as a demultiplexer
- Develop the timing diagram for a demultiplexer with specified data and data selection inputs

Figure 52 shows a 1-line-to-4-line demultiplexer (DEMUX) circuit. The data-input line goes to all of the AND gates. The two data-select lines enable only one gate at a time, and the data appearing on the data-input line will pass through the selected gate to the associated data-output line.

In a demultiplexer, data goes from one line to several lines.

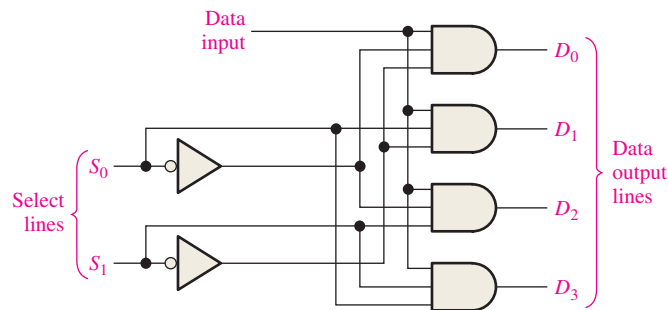


FIGURE 52 A 1-line-to-4-line demultiplexer.

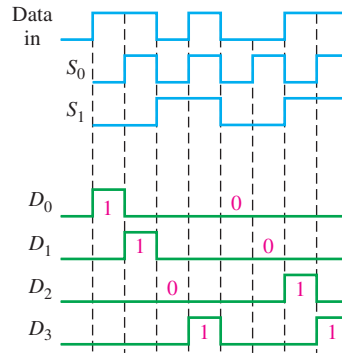
EXAMPLE 17

The serial data-input waveform (Data in) and data-select inputs (S_0 and S_1) are shown in Figure 53. Determine the data-output waveforms on D_0 through D_3 for the demultiplexer in Figure 52.

SOLUTION

Notice that the select lines go through a binary sequence so that each successive input bit is routed to D_0 , D_1 , D_2 , and D_3 in sequence, as shown by the output waveforms in Figure 53.

FIGURE 53



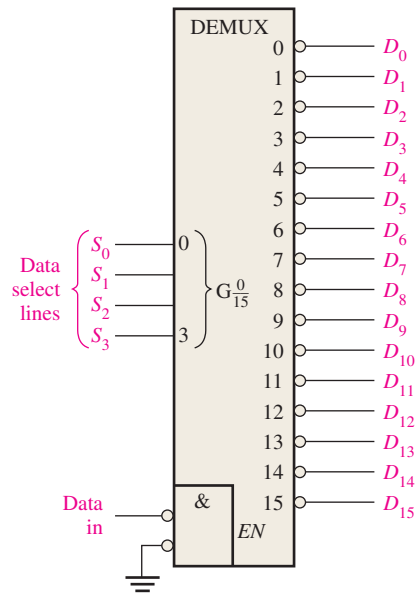
RELATED PROBLEM

Develop the timing diagram for the demultiplexer if the S_0 and S_1 waveforms are both inverted.

A Decoder as a Demultiplexer

The 4-line-to-16-line decoder can also be used in demultiplexing applications. The logic symbol for the decoder used as a demultiplexer is shown in Figure 54. In demultiplexer applications, the input lines are used as the data-select lines. One of the chip select (EN) inputs is used as the data-input line, with the other chip select input held LOW to enable the internal negative-AND gate at the bottom of the diagram.

FIGURE 54 The 4-line-to-16-line decoder used as a demultiplexer.



SECTION 10 CHECKUP

1. Generally, how can a decoder be used as a demultiplexer?
2. The demultiplexer in Figure 54 has a binary code of 1010 on the data-select lines, and the data-input line is LOW. What are the states of the output lines?

11 PARITY GENERATORS/CHECKERS

Errors can occur as digital codes are being transferred from one point to another within a digital system or while codes are being transmitted from one system to another. The errors take the form of undesired changes in the bits that make up the coded information; that is, a 1 can change to a 0, or a 0 to a 1, because of component malfunctions or electrical noise. In most digital systems, the probability that even a single bit error will occur is very small, and the likelihood that more than one will occur is even smaller. Nevertheless, when an error occurs undetected, it can cause serious problems in a digital system.

After completing this section, you should be able to

- Explain the concept of parity
- Implement a basic parity circuit with exclusive-OR gates
- Describe the operation of basic parity generating and checking logic
- Discuss a 9-bit parity generator/checker
- Discuss how error detection can be implemented in a data transmission

The parity method of error detection is a method in which a **parity bit** is attached to a group of information bits in order to make the total number of 1s either even or odd (depending on the system). In addition to parity bits, several specific codes also provide inherent error detection.

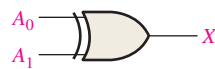
A parity bit indicates if the number of 1s in a code is even or odd for the purpose of error detection.

Basic Parity Logic

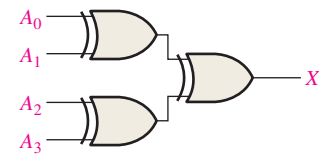
In order to check for or to generate the proper parity in a given code, a basic principle is:

The sum (disregarding carries) of an even number of 1s is always 0, and the sum of an odd number of 1s is always 1.

Therefore, to determine if a given code has **even parity** or **odd parity**, all the bits in that code are summed. As you know, the modulo-2 sum of two bits can be generated by an exclusive-OR gate, as shown in Figure 55(a); the modulo-2 sum of four bits can be formed by three exclusive-OR gates connected as shown in Figure 55(b); and so on. When the number of 1s on the inputs is even, the output X is 0 (LOW). When the number of 1s is odd, the output X is 1 (HIGH).



(a) Summing of two bits

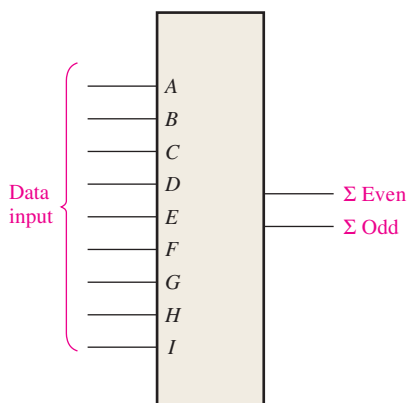


(b) Summing of four bits

FIGURE 55

A 9-bit Parity Generator/Checker

The logic symbol and function table for a 9-bit parity checker/generator are shown in Figure 56. This particular device can be used to check for odd or even parity on a 9-bit code



(a) Traditional logic symbol

NUMBER OF INPUTS A–I THAT ARE HIGH	OUTPUTS	
	Σ EVEN	Σ ODD
0, 2, 4, 6, 8	H	L
1, 3, 5, 7, 9	L	H

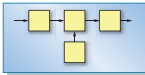
(b) Function table

FIGURE 56 A 9-bit parity generator/checker.

(eight data bits and one parity bit), or it can be used to generate a parity bit for a binary code with up to nine bits. The inputs are A through I ; when there is an even number of 1s on the inputs, the Σ Even output is HIGH and the Σ Odd output is LOW.

PARITY CHECKER When this device is used as an even parity checker, the number of input bits should always be even; and when a parity error occurs, the Σ Even output goes LOW and the Σ Odd output goes HIGH. When it is used as an odd parity checker, the number of input bits should always be odd; and when a parity error occurs, the Σ Odd output goes LOW and the Σ Even output goes HIGH.

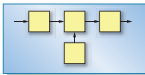
PARITY GENERATOR If this device is used as an even parity generator, the parity bit is taken at the Σ Odd output because this output is a 0 if there is an even number of input bits and it is a 1 if there is an odd number. When used as an odd parity generator, the parity bit is taken at the Σ Even output because it is a 0 when the number of inputs bits is odd.



The microprocessor in a computer performs internal parity checks as well as parity checks of the external data and address buses. In a read operation, the external system can transfer the parity information together with the data bytes. The microprocessor checks whether the resulting parity is even and sends out the corresponding signal. When it sends out an address code, the microprocessor does not perform an address parity check, but it does generate an even parity bit for the address.

SYSTEM NOTE

SYSTEM EXAMPLE 6



A DATA TRANSMISSION SYSTEM WITH ERROR DETECTION

A simplified data transmission system is shown in Figure 57 to illustrate an application of parity generators/checkers, as well as multiplexers and demultiplexers, and to illustrate the need for data storage in some systems.

In this application, digital data from seven sources are multiplexed onto a single line for transmission to a distant point. The seven data bits (D_0 through D_6) are applied to the multiplexer data inputs and, at the same time, to the even parity generator inputs. The Σ Odd output of the parity generator is used as the even parity bit. This bit is 0 if the number of 1s on the inputs A through I is even and is a 1 if the number of 1s on A through I is odd. This bit is D_7 of the transmitted code.

The data-select inputs are repeatedly cycled through a binary sequence, and each data bit, beginning with D_0 , is serially passed through and onto the transmission line (\bar{Y}). In this example, the transmission line consists of four conductors: one carries the serial data and three carry the timing signals (data selects). There are more sophisticated ways of sending the timing information, but we are using this direct method to illustrate a basic principle.

At the demultiplexer end of the system, the data-select signals and the serial data stream are applied to the demultiplexer. The data bits are distributed by the demultiplexer onto the output lines in the order in which they occurred on the multiplexer inputs. That is, D_0 comes out on the D_0 output, D_1 comes out on the D_1 output, and so on. The parity bit comes out on the D_7 output. These eight bits are temporarily stored and applied to the even parity checker. Not all of the bits are present on the parity checker inputs until the parity bit D_7 comes out and is stored. At this time, the error gate is enabled by the data-select code 111. If the parity is correct, a 0 appears on the Σ Even output, keeping the Error output at 0. If the parity is incorrect, all 1s appear on the error gate inputs, and a 1 on the Error output results.

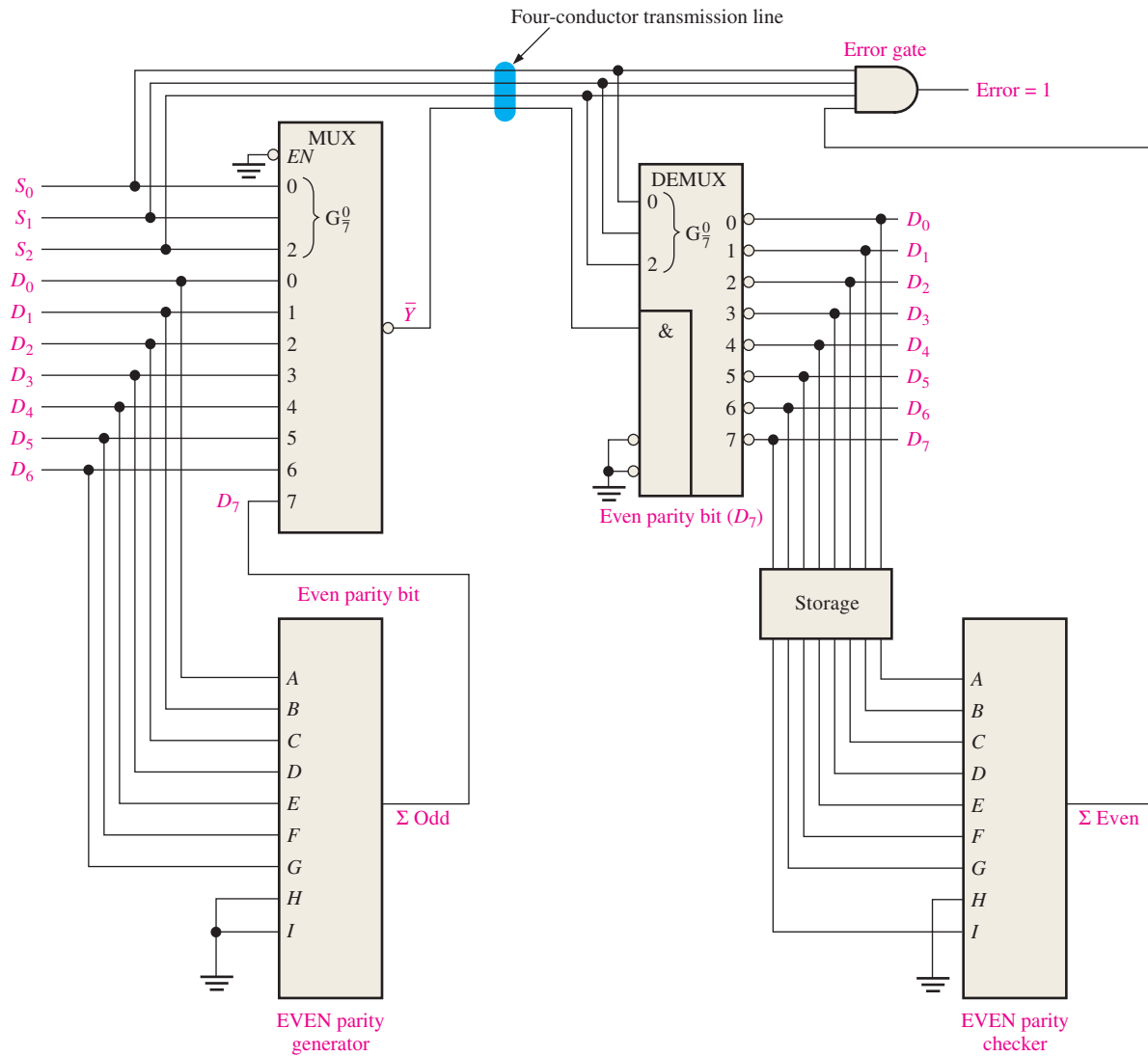


FIGURE 57 Simplified data transmission system with error detection.

This particular system has demonstrated the need for data storage.

The timing diagram in Figure 58 illustrates a specific case in which two 8-bit words are transmitted, one with correct parity and one with an error.

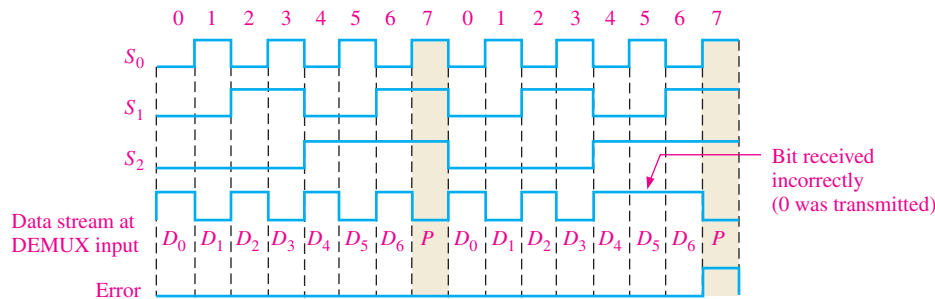


FIGURE 58 Example of data transmission with and without error for the system in Figure 57.

SECTION 11 CHECKUP

1. Add an even parity bit to each of the following codes:
 - (a) 110100
 - (b) 01100011
2. Add an odd parity bit to each of the following codes:
 - (a) 1010101
 - (b) 1000001
3. Check each of the even parity codes for an error.
 - (a) 100010101
 - (b) 1110111001

12 LOGIC FUNCTIONS WITH VHDL AND VERILOG

As you know, any logic function must be described with a hardware description language (HDL) in preparation for programming it into a PLD. In this section, several of the functions covered are described in both VHDL and Verilog. Keep in mind that in both languages there is more than one way to describe a given function. *Tutorials for VHDL and Verilog are on the website.*

After completing this section, you should be able to

- Use VHDL and Verilog to describe several types of combinational logic functions
- Specify variable arrays in both VHDL and Verilog
- Use comment lines

Full-Adder

The full-adder (FA) logic symbol with the Boolean expressions for the sum and output carry is shown in Figure 59. Using the data flow approach, you can describe the FA using VHDL. The Verilog description is also shown.

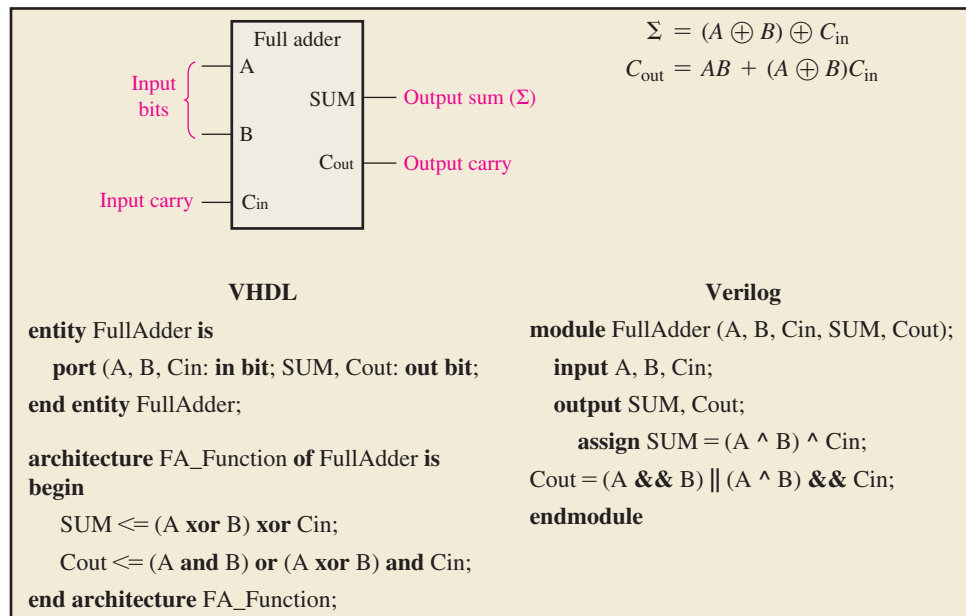


FIGURE 59 Logic symbol and full-adder VHDL and Verilog descriptions.

4-Bit Parallel Adder

Figure 60 shows a 4-bit parallel adder and its VHDL structural description. The VHDL full-adder description is used as a component. For logic functions with multiple input and/or outputs, the VHDL **bit_vector** can be used to group bits together in an array. For example, if you declare an identifier called A for a **bit_vector** data type, the first element in A would be accessed as A(0), the next element would be accessed as A(1), and so on. In the signal declaration, C1, C2, and C3 are the internal carry bits. Inputs A and B and output SUM are bit vector types with 4 bits (0–3) as specified in the entity port statement. Note that **std_logic** and **std_logic_vector** can be used in place of **bit** and **bit_vector**; however, in that case, the lines **library ieee;** and **use ieee.std_logic_1164.all;** must precede the **entity** line.

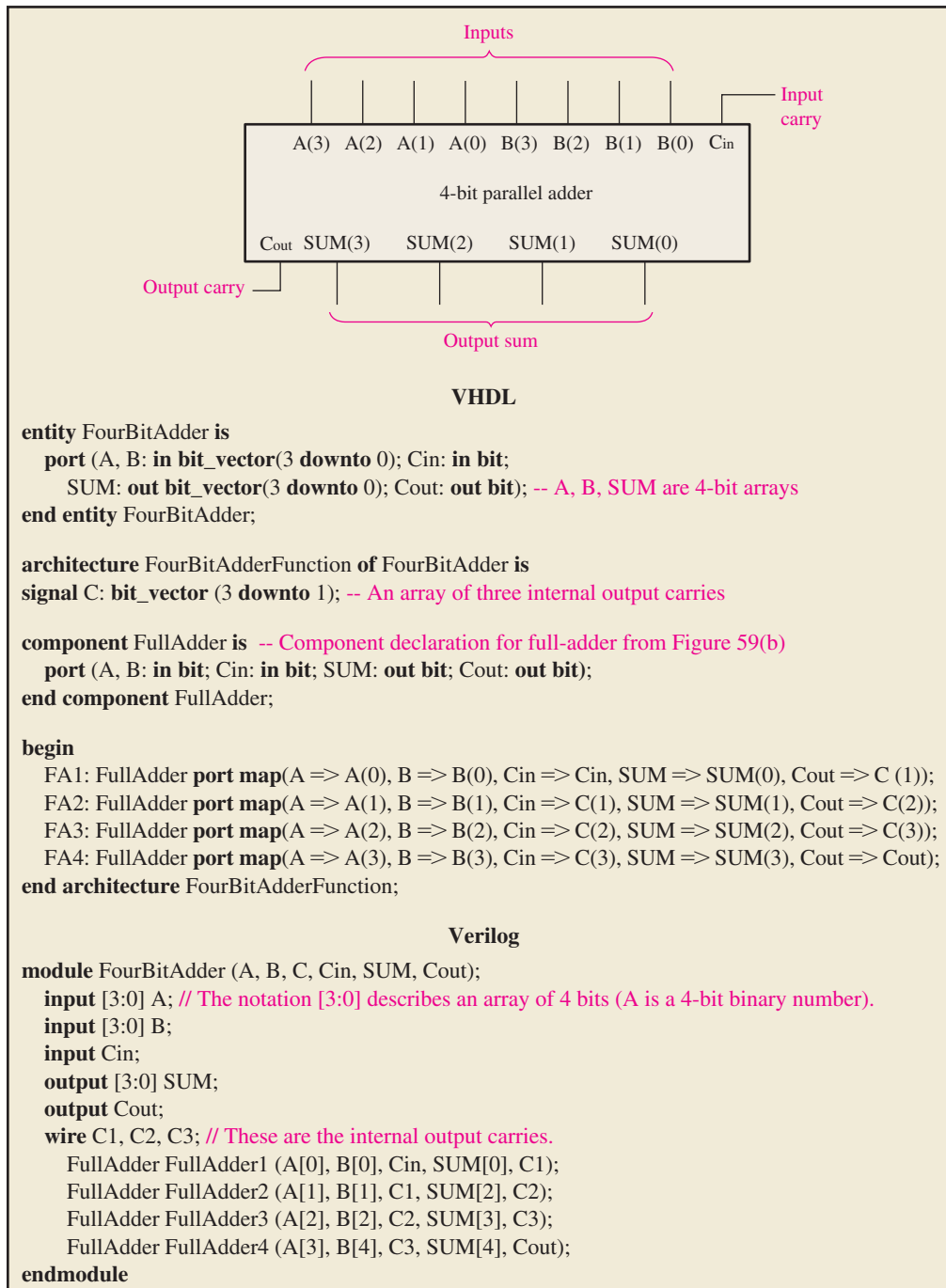


FIGURE 60 Logic symbol and 4-bit parallel adder VHDL and Verilog descriptions.

The Verilog description is shown in Figure 60. Notice that it also uses a special notation to specify an array. The red text in both programs are comments and do not affect the program. In VHDL, a comment line is preceded by two hyphens (--); and in Verilog, a comment line is preceded by two slashes (//).

BCD-to-Decimal Decoder

As you know, the function of the BCD-to-decimal decoder is to accept a group of four BCD bits and decode it into one of the ten outputs that represents the corresponding decimal digit. Again, the use of the **bit_vector** allows the program to reference the input or the output as indexed bits in an array with a single identifier name. Figure 61 shows the symbol for the decoder and the corresponding VHDL and Verilog descriptions.

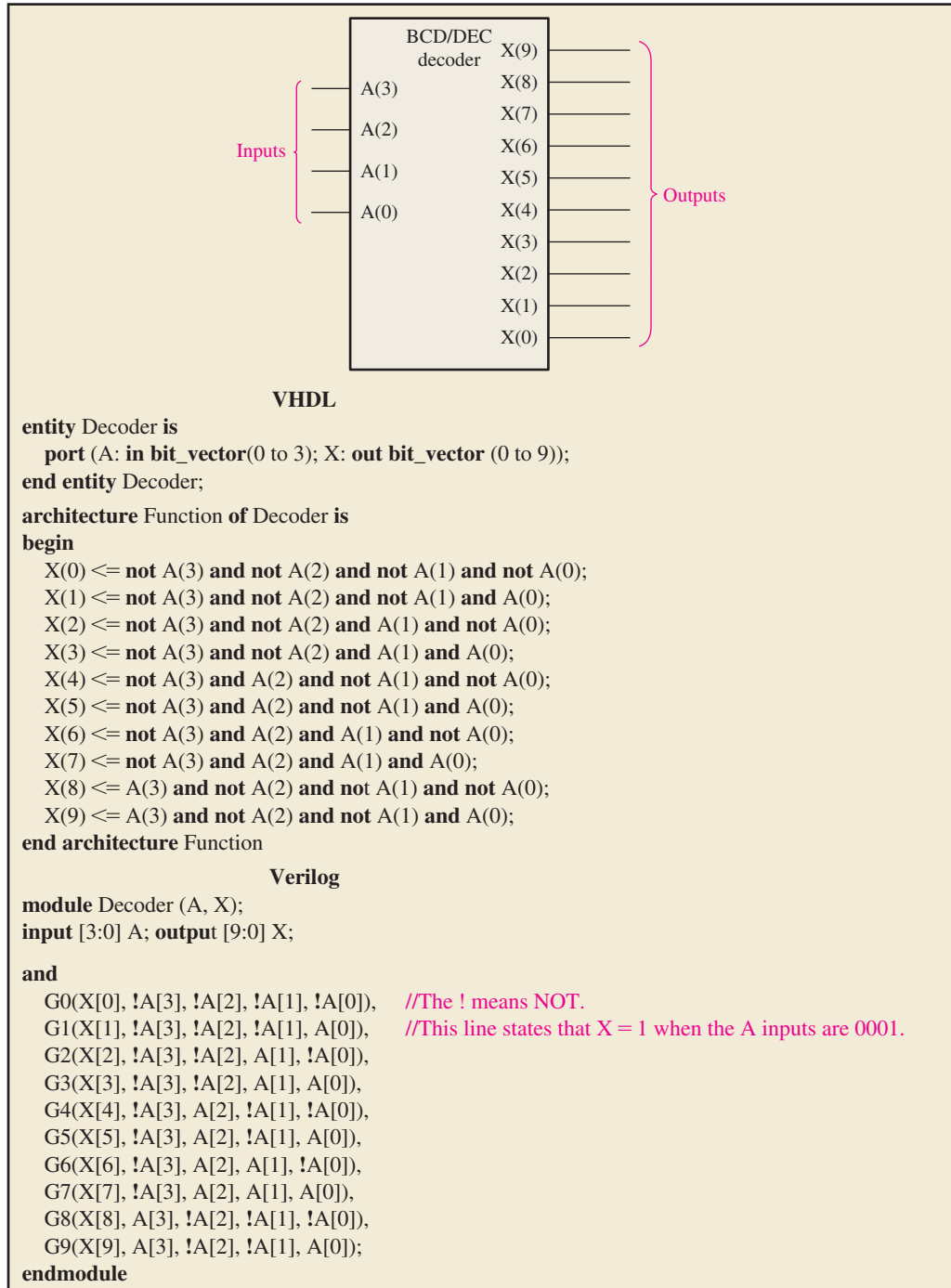


FIGURE 61 Logic symbol and BCD-to-decimal decoder VHDL and Verilog descriptions.

SECTION 12 CHECKUP

1. Specify the input variable A as an 8-bit binary number (array) in VHDL.
2. Specify the input variable A as an 8-bit binary number (array) in Verilog.
3. Which HDL uses the module?
4. What does this line from the Verilog decoder mean: `G6(X[6], !A[3], A[2], A[1], !A[0]);`

13 TROUBLESHOOTING

In this section, the problem of glitches is introduced and examined from a troubleshooting standpoint, using a decoder as an example. A **glitch** is any undesired voltage or current spike (pulse) of very short duration. A glitch can erroneously be interpreted as a valid signal by a logic circuit and may cause improper operation.



After completing this section, you should be able to

- Explain what a glitch is
- Determine the cause of glitches in a decoder application
- Use the method of output strobing to eliminate glitches

A 3-line-to-8-line decoder (binary-to-octal) in Figure 62 illustrates how glitches occur and how to identify their cause. The $A_2A_1A_0$ inputs of the decoder are sequenced through a binary count, and the resulting waveforms of the inputs and outputs can be displayed on the screen of a logic analyzer or oscilloscope, as shown in Figure 62. A_2 transitions are delayed from A_1 transitions and A_1 transitions are delayed from A_0 transitions. This commonly occurs when waveforms are generated by a binary counter.

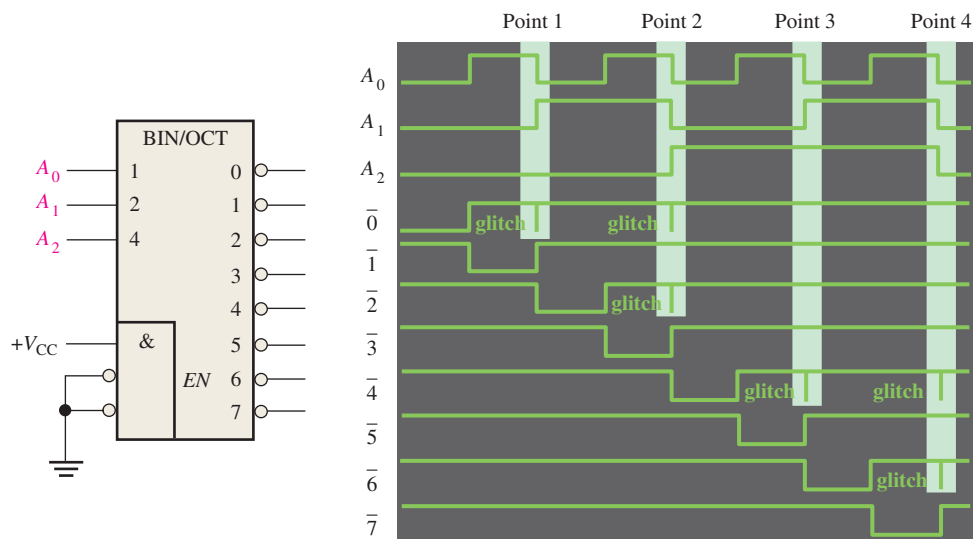


FIGURE 62 Decoder waveforms with output glitches.

The output waveforms are correct except for the glitches that occur on some of the output signals. A logic analyzer or an oscilloscope can be used to display glitches, which are normally very difficult to see. Generally, the logic analyzer is preferred, especially for low



HANDS ON TIP

In addition to glitches that are the result of differences in propagation delays, as you have seen in the case of a decoder, other types of unwanted noise spikes can also be a problem. Current and voltage spikes on the V_{CC} and ground lines are caused by the fast switching waveforms in digital circuits. This problem can be minimized by proper printed circuit board layout and decoupling capacitors. Switching spikes can be absorbed by decoupling the circuit board with a $1\ \mu\text{F}$ capacitor from V_{CC} to ground. Also, smaller decoupling capacitors ($0.022\ \mu\text{F}$ to $0.1\ \mu\text{F}$) should be distributed at various points between V_{CC} and ground over the circuit board. Decoupling should be done especially near devices that are switching at higher rates or driving more loads such as oscillators, counters, buffers, and bus drivers.

FUNCTIONS OF COMBINATIONAL LOGIC

repetition rates (less than 10 kHz) and/or irregular occurrence because most logic analyzers have a *glitch capture* capability. Oscilloscopes can be used to observe glitches with reasonable success, particularly if the glitches occur at a regular high repetition rate (greater than 10 kHz).

The points of interest indicated by the highlighted areas on the input waveforms in Figure 62 are displayed as shown in Figure 63. At point 1 there is a transitional state of 000

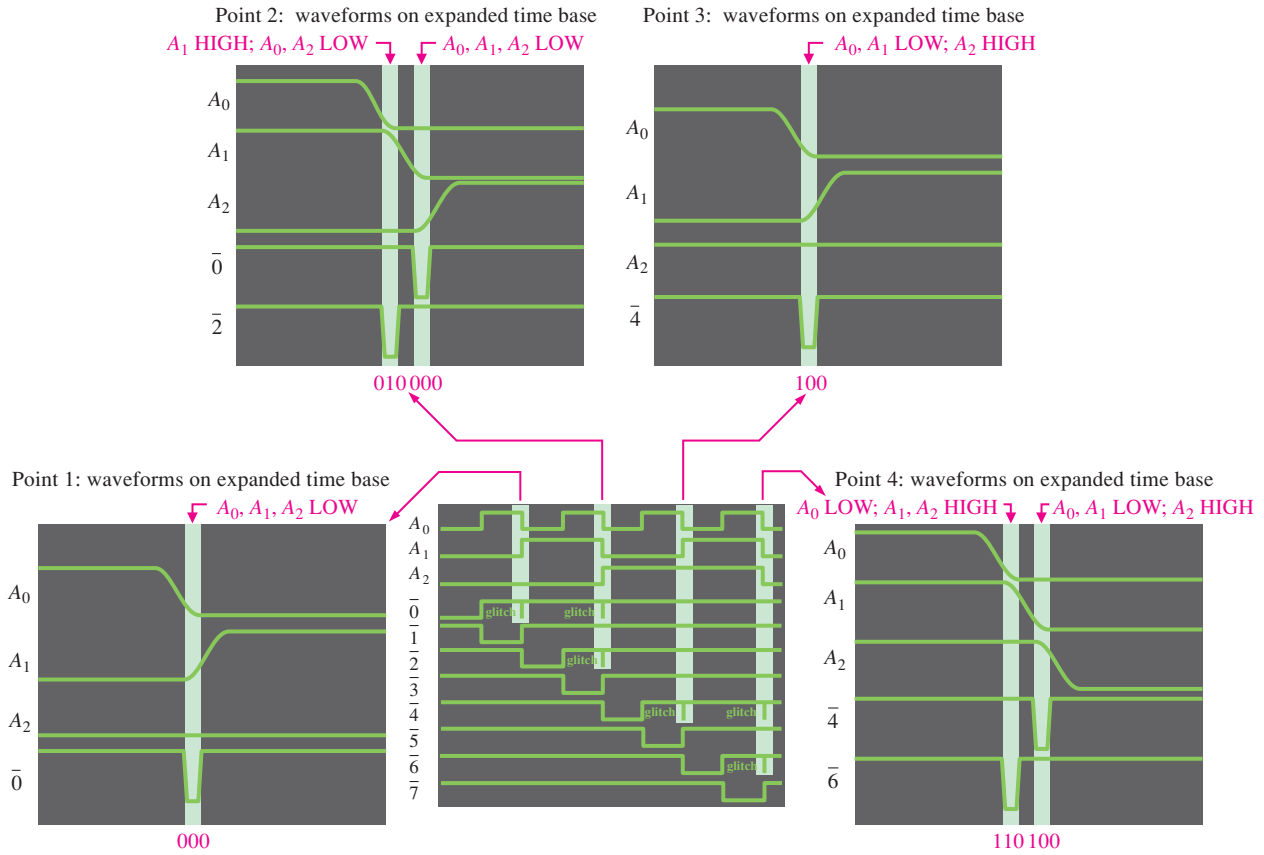


FIGURE 63 Decoder waveform displays showing how transitional input states produce glitches in the output waveforms.

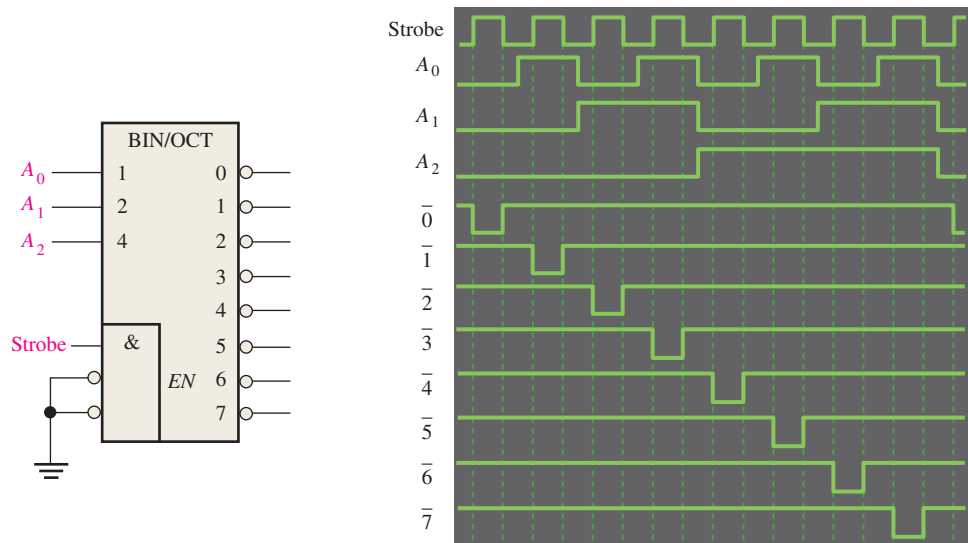


FIGURE 64 Application of a strobe waveform to eliminate glitches on decoder outputs.

due to delay differences in the waveforms. This causes the first glitch on the $\bar{0}$ output of the decoder. At point 2 there are two transitional states, 010 and 000. These cause the glitch on the $\bar{2}$ output of the decoder and the second glitch on the $\bar{0}$ output, respectively. At point 3 the transitional state is 100, which causes the first glitch on the $\bar{4}$ output of the decoder. At point 4 the two transitional states, 110 and 100, result in the glitch on the $\bar{6}$ output and the second glitch on the $\bar{4}$ output, respectively.

One way to eliminate the glitch problem is a method called **strobing**, in which the decoder is enabled by a strobe pulse only during the times when the waveforms are not in transition. This method is illustrated in Figure 64.

SECTION 13 CHECKUP

1. Define the term *glitch*.
2. Explain the basic cause of glitches in decoder logic.
3. Define the term *strobe*.

SUMMARY

- Half-adder and full-adder operations are summarized in Figure 65.
- Standard logic functions from the 74XX series are available for use in a programmable logic design.

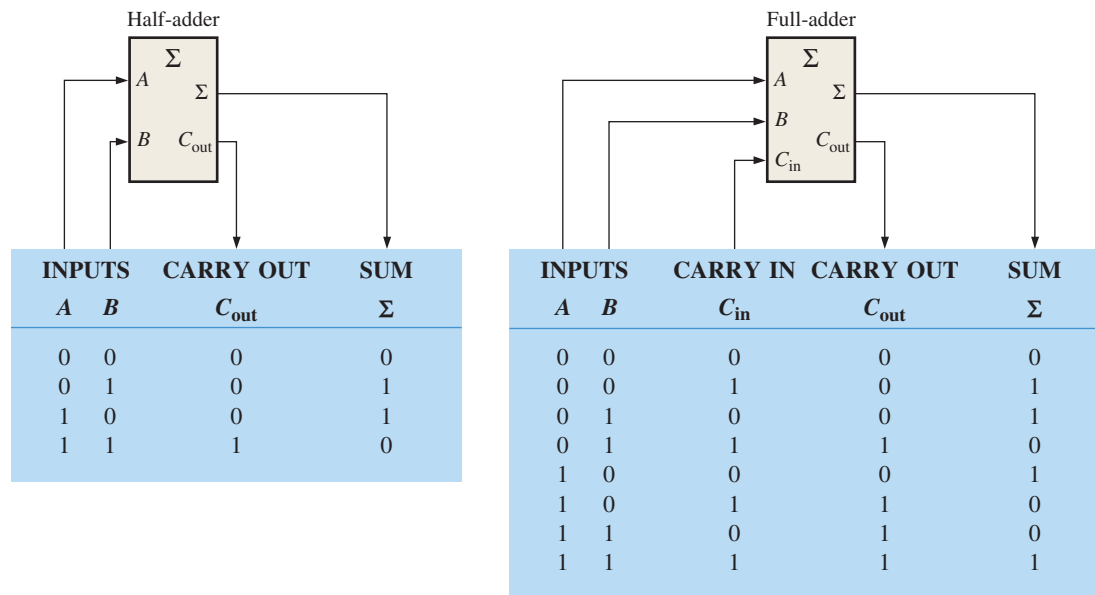


FIGURE 65

KEY TERMS

Cascading Connecting two or more similar devices in a manner that expands the capability of one device.

Decoder A digital circuit that converts coded information into a familiar or noncoded form.

Demultiplexer (DEMUX) A circuit that switches digital data from one input line to several output lines in a specified time sequence.

FUNCTIONS OF COMBINATIONAL LOGIC

Encoder A digital circuit that converts information to a coded form.

Full-adder A digital circuit that adds two bits and an input carry to produce a sum and an output carry.

Glitch A voltage or current spike of short duration, usually unintentionally produced and unwanted.

Half-adder A digital circuit that adds two bits and produces a sum and an output carry. It cannot handle input carries.

Look-ahead carry A method of binary addition whereby carries from preceding adder stages are anticipated, thus eliminating carry propagation delays.

Multiplexer (MUX) A circuit that switches digital data from several input lines onto a single output line in a specified time sequence.

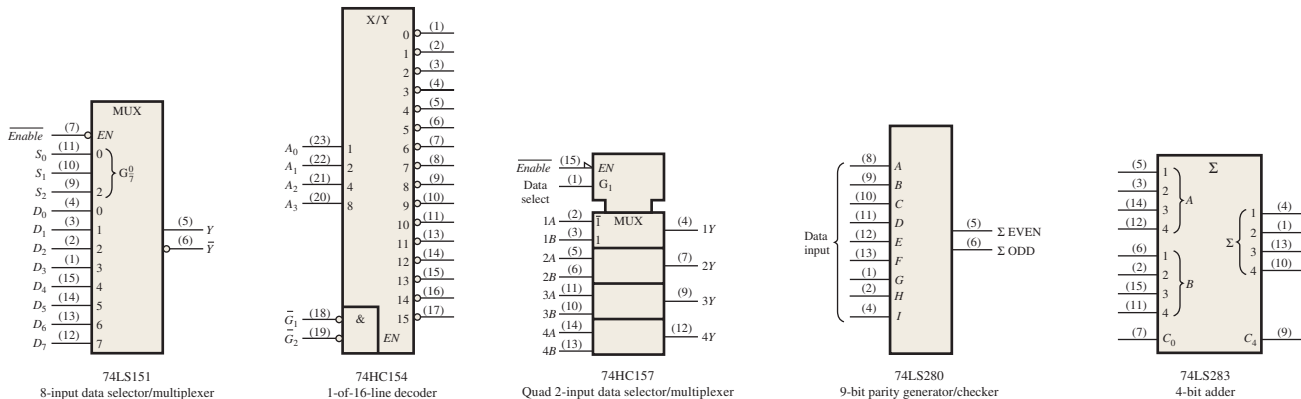
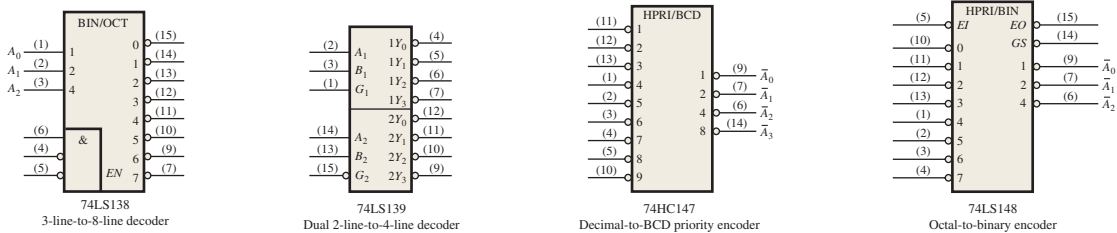
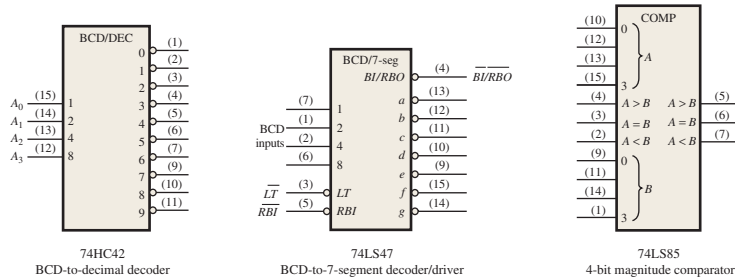
Parity bit A bit attached to each group of information bits to make the total number of 1s odd or even for every group of bits.

Priority encoder An encoder in which only the highest value input digit is encoded and any other active input is ignored.

Ripple carry A method of binary addition in which the output carry from each adder becomes the input carry of the next higher-order adder.

FIXED-FUNCTION LOGIC DEVICES

Pin numbers are in parentheses. Go to ti.com for data sheets.



TRUE/FALSE QUIZ

Answers are at the end of the chapter.

1. A half-adder adds two binary bits.
2. A half-adder has a sum output only.
3. A full-adder adds three bits and produces two outputs.
4. Two 4-bit numbers can be added using two full-adders.
5. When the two input bits are both 1 and the carry input bit is a 1, the sum output of a full adder is 0.
6. A comparator determines when two binary numbers are equal.
7. A decoder detects the presence of a specified combination of input bits.
8. The 4-line-to-10-line decoder and the 1-of-10 decoder are two different types.
9. An encoder essentially performs a reverse decoder function.
10. A multiplexer is a logic circuit that allows digital information from a single source to be routed onto several lines.
11. Any logic function can be described using VHDL or Verilog.

SELF-TEST

Answers are at the end of the chapter.

1. A half-adder is characterized by
 - (a) two inputs and two outputs
 - (b) three inputs and two outputs
 - (c) two inputs and three outputs
 - (d) two inputs and one output
2. A full-adder is characterized by
 - (a) two inputs and two outputs
 - (b) three inputs and two outputs
 - (c) two inputs and three outputs
 - (d) two inputs and one output
3. The inputs to a full-adder are $A = 1$, $B = 1$, $C_{in} = 0$. The outputs are
 - (a) $\Sigma = 1$, $C_{out} = 1$
 - (b) $\Sigma = 1$, $C_{out} = 0$
 - (c) $\Sigma = 0$, $C_{out} = 1$
 - (d) $\Sigma = 0$, $C_{out} = 0$
4. A 4-bit parallel adder can add
 - (a) two 4-bit binary numbers
 - (b) two 2-bit binary numbers
 - (c) four bits at a time
 - (d) four bits in sequence
5. To expand a 4-bit parallel adder to an 8-bit parallel adder, you must
 - (a) use four 4-bit adders with no interconnections
 - (b) use two 4-bit adders and connect the sum outputs of one to the bit inputs of the other
 - (c) use eight 4-bit adders with no interconnections
 - (d) use two 4-bit adders with the carry output of one connected to the carry input of the other
6. If a magnitude comparator has $A = 1011$ and $B = 1001$ on its inputs, the outputs are
 - (a) $A > B = 0$, $A < B = 1$, $A = B = 0$
 - (b) $A > B = 1$, $A < B = 0$, $A = B = 0$
 - (c) $A > B = 1$, $A < B = 1$, $A = B = 0$
 - (d) $A > B = 0$, $A < B = 0$, $A = B = 1$
7. If a 1-of-16 decoder with active-LOW outputs exhibits a LOW on the decimal 12 output, what are the inputs?
 - (a) $A_3A_2A_1A_0 = 1010$
 - (b) $A_3A_2A_1A_0 = 1110$
 - (c) $A_3A_2A_1A_0 = 1100$
 - (d) $A_3A_2A_1A_0 = 0100$
8. A BCD-to-7 segment decoder has 0100 on its inputs. The active outputs are
 - (a) a, c, f, g
 - (b) b, c, f, g
 - (c) b, c, e, f
 - (d) b, d, e, g
9. In general, a multiplexer has
 - (a) one data input, several data outputs, and selection inputs
 - (b) one data input, one data output, and one selection input
 - (c) several data inputs, several data outputs, and selection inputs
 - (d) several data inputs, one data output, and selection inputs

10. Data selectors are basically the same as
 - (a) decoders
 - (b) demultiplexers
 - (c) multiplexers
 - (d) encoders
11. Which of the following codes exhibit even parity?
 - (a) 10011000
 - (b) 01111000
 - (c) 11111111
 - (d) 11010101
 - (e) all
 - (f) both answers (b) and (c)
12. An entity and architecture are associated with
 - (a) Abel
 - (b) Verilog
 - (c) VHDL
 - (d) PLD

PROBLEMS

Answers to odd-numbered problems are at the end of the chapter.

SECTION 1 A System

1. Assume the tablet-bottling control system is set for 36 tablets per bottle. Determine the binary numbers in register A and register B after 5 bottles have been filled.
2. After one more bottle is filled from Problem 1, determine the output of the adder.
3. For Problem 1, what is the output of the BCD-to-binary code converter A?
4. For Problem 1, determine the active outputs from the 3-digit BCD-to-7-segment decoder A.

SECTION 2 Half and Full Adders

5. For the full-adder of Figure 9, determine the logic state (1 or 0) at each gate output for the following inputs:
 - (a) $A = 1, B = 1, C_{in} = 1$
 - (b) $A = 0, B = 1, C_{in} = 1$
 - (c) $A = 0, B = 1, C_{in} = 0$
6. What are the full-adder inputs that will produce each of the following outputs:
 - (a) $\Sigma = 0, C_{out} = 0$
 - (b) $\Sigma = 1, C_{out} = 0$
 - (c) $\Sigma = 1, C_{out} = 1$
 - (d) $\Sigma = 0, C_{out} = 1$
7. Determine the outputs of a full-adder for each of the following inputs:
 - (a) $A = 1, B = 0, C_{in} = 0$
 - (b) $A = 0, B = 0, C_{in} = 1$
 - (c) $A = 0, B = 1, C_{in} = 1$
 - (d) $A = 1, B = 1, C_{in} = 1$

SECTION 3 Parallel Adders

8. For the parallel adder in Figure 66, determine the complete sum by analysis of the logical operation of the circuit. Verify your result by longhand addition of the two input numbers.
9. Repeat Problem 8 for the circuit and input conditions in Figure 67.

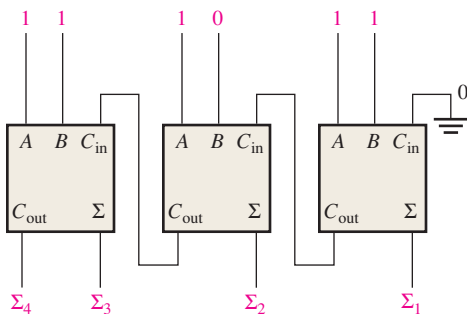


FIGURE 66

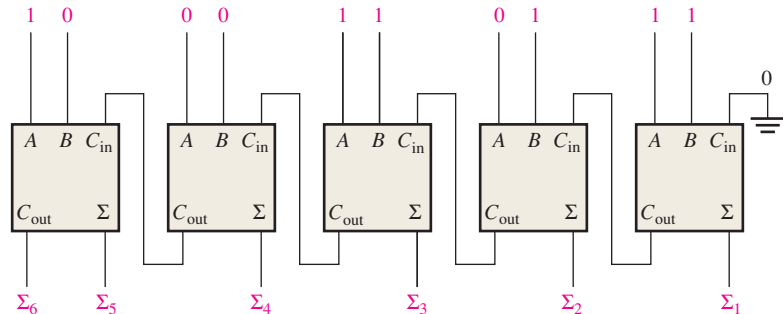


FIGURE 67

10. The circuit shown in Figure 68 is a 4-bit circuit that can add or subtract numbers in a form used in computers (positive numbers in true form; negative numbers in complement form).
 - (a) Explain what happens when the $\overline{Add/Subt.}$ input is HIGH. (b) What happens when $\overline{Add/Subt.}$ is LOW?
11. For the circuit in Figure 68, assume the inputs are $\overline{Add/Subt.} = 1, A = 1001$ and $B = 1100$. What is the output?

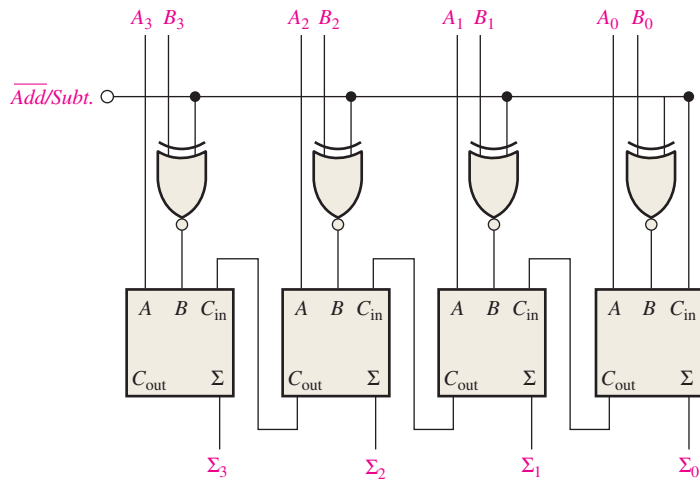


FIGURE 68

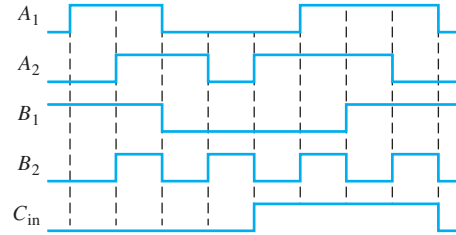


FIGURE 69

12. The input waveforms in Figure 69 are applied to a 2-bit adder. Determine the waveforms for the sum and the output carry in relation to the inputs by constructing a timing diagram.
13. The following sequences of bits (right-most bit first) appear on the inputs to a 4-bit parallel adder. Determine the resulting sequence of bits on each sum output.

A_1	1001
A_2	1110
A_3	0000
A_4	1011
B_1	1111
B_2	1100
B_3	1010
B_4	0010

14. In the process of checking a 4-bit parallel adder, the following logic levels are observed on the inputs: HIGH (MSB), HIGH, HIGH, HIGH, and HIGH (MSB), LOW, LOW, HIGH. The following levels are observed on the outputs: LOW (MSB), HIGH, LOW, HIGH. Determine if the adder is functioning properly.

SECTION 4 Ripple Carry and Look-Ahead Carry Adders

15. Each of the eight full-adders in an 8-bit parallel ripple carry adder exhibits the following propagation delays:
 - A to Σ and C_{out} : 40 ns
 - B to Σ and C_{out} : 40 ns
 - C_{in} to Σ : 35 ns
 - C_{in} to C_{out} : 25 ns

Determine the maximum total time for the addition of two 8-bit numbers.

16. Show the additional logic circuitry necessary to make the 4-bit look-ahead carry adder in Figure 21 into a 5-bit adder.

SECTION 5 Comparators

17. The waveforms in Figure 70 are applied to the comparator as shown. Determine the output ($A = B$) waveform.

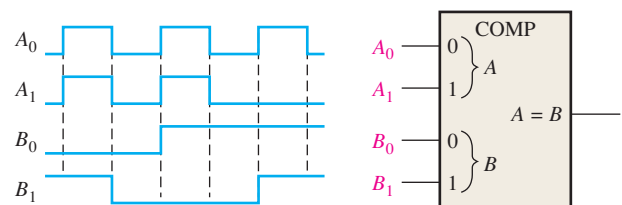


FIGURE 70

18. For the 4-bit comparator in Figure 71, plot each output waveform for the inputs shown. The outputs are active-HIGH.

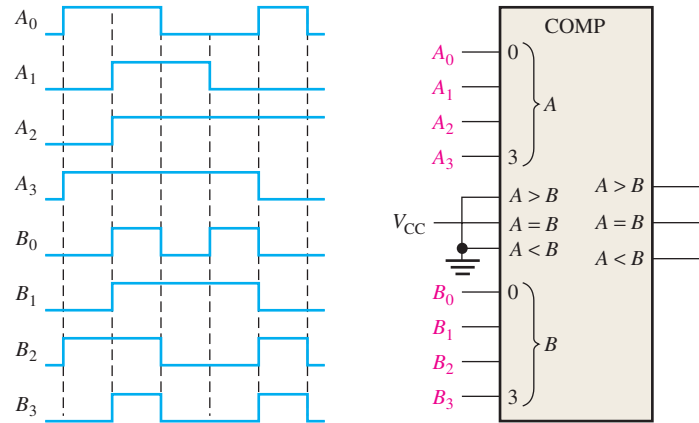


FIGURE 71

19. For each set of binary numbers, determine the output states for the comparator of Figure 25.
- (a) $A_3A_2A_1A_0 = 1100$ (b) $A_3A_2A_1A_0 = 1000$ (c) $A_3A_2A_1A_0 = 0100$
 $B_3B_2B_1B_0 = 1001$ $B_3B_2B_1B_0 = 1011$ $B_3B_2B_1B_0 = 0100$

SECTION 6 Decoders

20. When a HIGH is on the output of each of the decoding gates in Figure 72, what is the binary code appearing on the inputs? The MSB is A_3 .

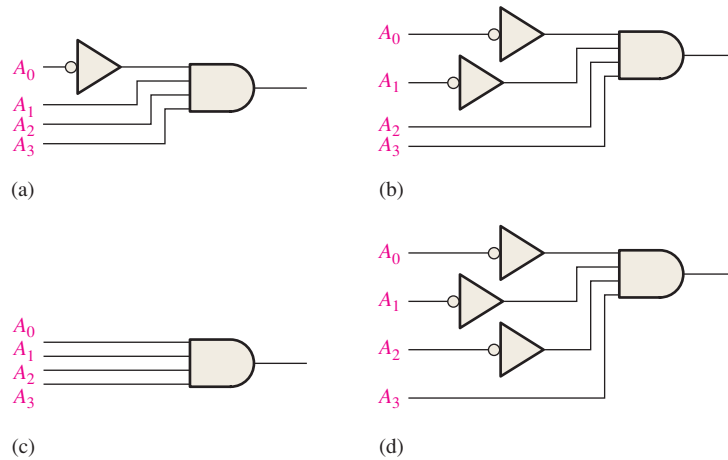


FIGURE 72

21. Show the decoding logic for each of the following codes if an active-HIGH (1) output is required:
- (a) 1101 (b) 1000 (c) 11011 (d) 11100
 (e) 101010 (f) 111110 (g) 000101 (h) 1110110
22. Solve Problem 21, given that an active-LOW (0) output is required.
23. You wish to detect only the presence of the codes 1010, 1100, 0001, and 1011. An active-HIGH output is required to indicate their presence. Develop the decoding logic with a single output that will indicate when any one of these codes is on the inputs. For any other code, the output must be LOW.
24. If the input waveforms are applied to the decoding logic as indicated in Figure 73, sketch the output waveform in proper relation to the inputs.

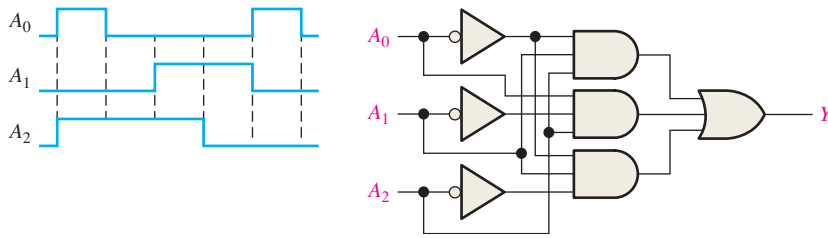


FIGURE 73

25. BCD numbers are applied sequentially to the BCD-to-decimal decoder in Figure 74. Draw a timing diagram, showing each output in the proper relationship with the others and with the inputs.

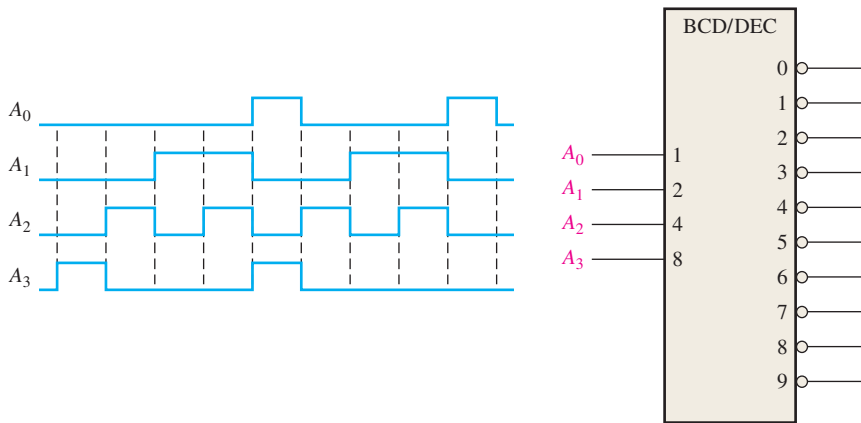


FIGURE 74

26. A 7-segment decoder/driver drives the display in Figure 75. If the waveforms are applied as indicated, determine the sequence of digits that appears on the display.

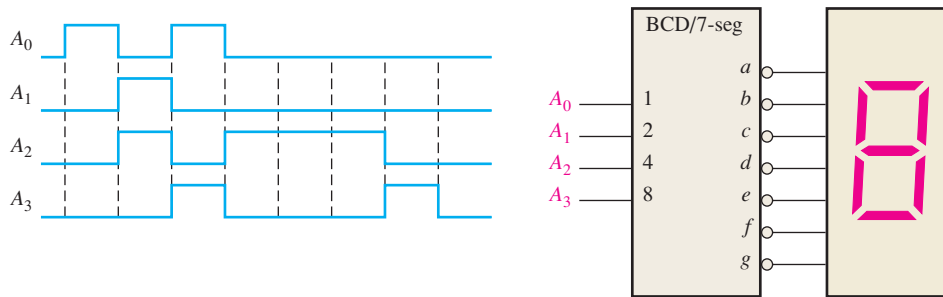


FIGURE 75

SECTION 7 Encoders

27. For the decimal-to-BCD encoder logic of Figure 38, assume that the 9 input and the 3 input are both HIGH. What is the output code? Is it a valid BCD (8421) code?
28. A priority encoder has active-LOW levels on inputs 1, 5, and 9. What BCD code appears on the outputs if all the other inputs are HIGH?

SECTION 8 Code Converters

29. Convert the following decimal numbers to BCD and then to binary.
 (a) 2 (b) 8 (c) 13 (d) 26 (e) 33
30. Show the logic required to convert a 10-bit binary number to Gray code, and use that logic to convert the following binary numbers to Gray code:
 (a) 1010101010 (b) 1111100000 (c) 0000011110 (d) 1111111111

31. Show the logic required to convert a 10-bit Gray code to binary, and use that logic to convert the following Gray code words to binary:
 (a) 1010000000 (b) 0011001100 (c) 1111000111 (d) 0000000001

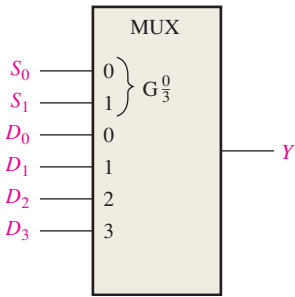


FIGURE 76

SECTION 9 Multiplexers (Data Selectors)

32. For the multiplexer in Figure 76, determine the output for the following input states: $D_0 = 0, D_1 = 1, D_2 = 1, D_3 = 0, S_0 = 1, S_1 = 0$.
 33. If the data-select inputs to the multiplexer in Figure 76 are sequenced as shown by the waveforms in Figure 77, determine the output waveform with the data inputs specified in Problem 32.

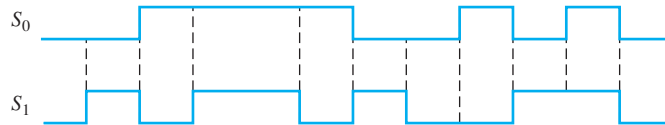


FIGURE 77

34. The waveforms in Figure 78 are observed on the inputs of an 8-input multiplexer. Sketch the Y output waveform.

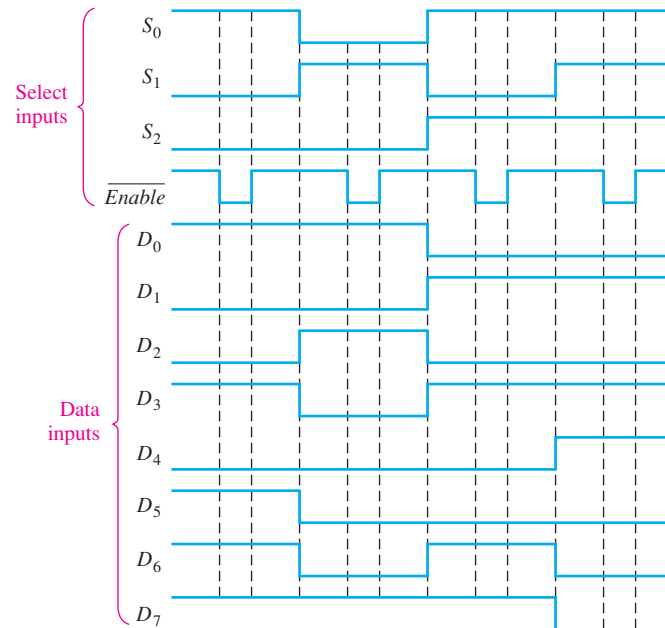


FIGURE 78

SECTION 10 Demultiplexers

35. Develop the total timing diagram (inputs and outputs) for a demultiplexer in which the inputs are as follows: The data-select inputs are repetitively sequenced through a straight binary count beginning with 0000, and the data input is a serial data stream carrying BCD data representing the decimal number 2468. The least significant digit (8) is first in the sequence, with its LSB first, and it should appear in the first 4-bit positions of the output.

SECTION 11 Parity Generators/Checkers

36. The waveforms in Figure 79 are applied to the 4-bit parity logic. Determine the output waveform in proper relation to the inputs. For how many bit times does even parity occur, and how is it indicated? The timing diagram includes eight bit times.

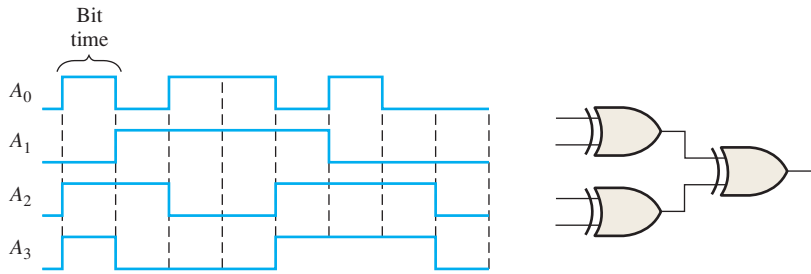


FIGURE 79

37. Determine the Σ Even and the Σ Odd outputs of a 9-bit parity generator/checker for the inputs in Figure 80. Refer to the function table in Figure 56.

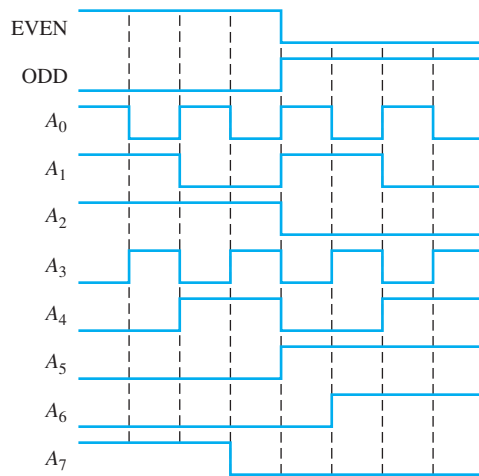


FIGURE 80

SECTION 12 Logic Functions with VHDL and Verilog

- 38. Write a VHDL program for an 8-bit parallel adder.
- 39. Write a Verilog program for an 8-bit parallel adder.
- 40. Write a VHDL program for a decimal-to-BCD encoder.
- 41. Write a Verilog program for a decimal-to-BCD encoder.

SECTION 13 Troubleshooting

42. The full-adder in Figure 81 is tested under all input conditions with the input waveforms shown. From your observation of the Σ and C_{out} waveforms, is it operating properly, and if not, what is the most likely fault?

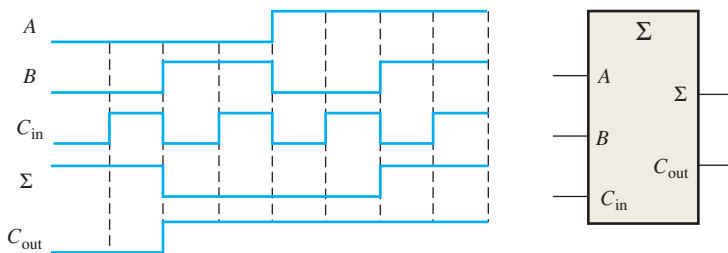


FIGURE 81

43. List the possible faults for each decoder/display in Figure 82.

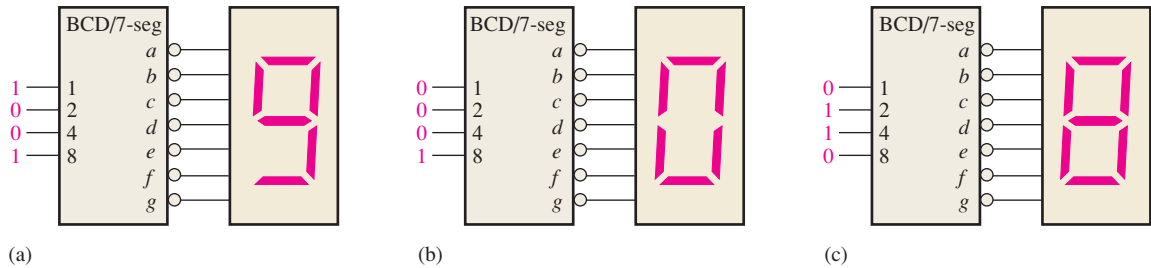


FIGURE 82

44. Develop a systematic test procedure to check out the complete operation of the keyboard encoder in Figure 40.
45. You are testing a BCD-to-binary converter consisting of 4-bit adders as shown in Figure 83. First verify that the circuit converts BCD to binary. The test procedure calls for applying BCD numbers in sequential order beginning with 0_{10} and checking for the correct binary output. What symptom or symptoms will appear on the binary outputs in the event of each of the following faults? For what BCD number is each fault *first* detected?
- (a) The A_1 input is open (top adder).
 - (b) The C_{out} is open (top adder).
 - (c) The Σ_4 output is shorted to ground (top adder).
 - (d) The 32 output is shorted to ground (bottom adder).

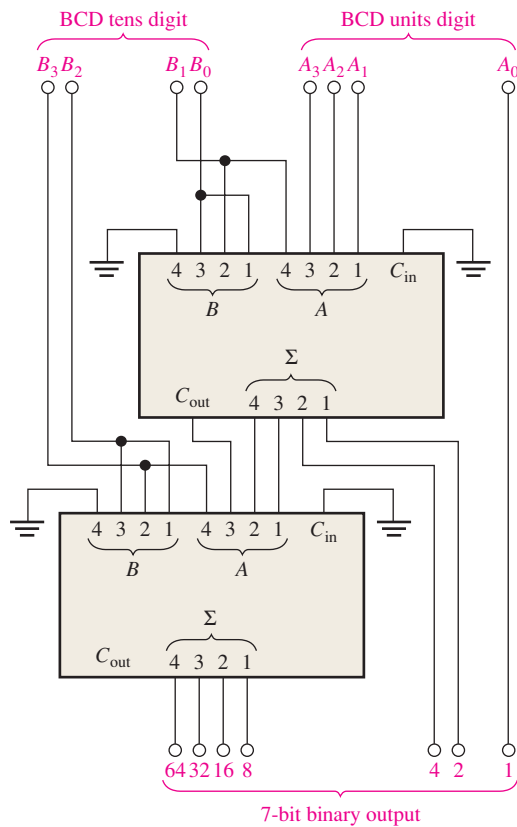


FIGURE 83

46. For the 7-segment display multiplexing system in Figure 49, determine the most likely cause or causes for each of the following symptoms:
- (a) The B -digit (MSD) display does not turn on at all.
 - (b) Neither 7-segment display turns on.
 - (c) The f -segment of both displays appears to be on all the time.
 - (d) There is a visible flicker on the displays.

47. Develop a systematic procedure to fully test the data selector shown in Figure 47.
48. During the testing of the data transmission system in Figure 57, a code is applied to the D_0 through D_6 inputs that contains an odd number of 1s. A single bit error is deliberately introduced on the serial data transmission line between the MUX and the DEMUX, but the system does not indicate an error (error output = 0). After some investigation, you check the inputs to the even parity checker and find that D_0 through D_6 contain an even number of 1s, as you would expect. Also, you find that the D_7 parity bit is a 1. What are the possible reasons for the system not indicating the error?
49. In general, describe how you would fully test the data transmission system in Figure 57, and specify a method for the introduction of parity errors.

Special Problems

50. Modify the design of the 7-segment display multiplexing system in Figure 49 to accommodate two additional digits.
51. Using Table 2, write the SOP expressions for the Σ and C_{out} of a full-adder and show the logic diagrams. Then implement them with inverters and AND-OR logic.
52. Implement the logic function specified in Table 11 and write a VHDL program for the implementation.

TABLE 11				
INPUTS				OUTPUT
A_3	A_2	A_1	A_0	Y
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	1

53. Using two of the 6-position adder modules from Figure 17, develop a 12-position voting system.

MULTISIM



MULTISIM TROUBLESHOOTING PRACTICE

54. Open file P05-54 and follow the instructions given there.
55. Open file P05-55 and follow the instructions given there.
56. Open file P05-56 and follow the instructions given there.
57. Open file P05-57 and follow the instructions given there.

ANSWERS TO SECTION CHECKUPS

SECTION 1 A System

1. Register A: $50 = 110010$; Register B: $200 = 11001000$
2. Register A: $25 = 11001$; Register B: $125 = 1111101$
3. The comparator determines when a bottle is filled with the preset number of tablets.
4. Decoder B detects when register B contains the maximum number.

SECTION 2 Half and Full Adders

1. (a) $\Sigma = 1, C_{out} = 0$
 (b) $\Sigma = 0, C_{out} = 0$
 (c) $\Sigma = 1, C_{out} = 0$
 (d) $\Sigma = 0, C_{out} = 1$
2. $\Sigma = 1, C_{out} = 1$

SECTION 3 Parallel Adders

1. $C_{out}\Sigma_4\Sigma_3\Sigma_2\Sigma_1 = 11001$
2. Three 4-bit adders are required to add two 10-bit numbers.

SECTION 4 Ripple Carry and Look-Ahead Carry Adders

1. $C_g = 0, C_p = 1$
2. $C_{out} = 1$

SECTION 5 Comparators

1. $A > B = 1, A = B = 0, A < B = 0$, when $A = 1011$ and $B = 1010$
2. $A < B = 1; A = B = 0; A > B = 0$

SECTION 6 Decoders

1. Output 5 is active when 101 is on the inputs.
2. Four 1-of-16 decoders are used to decode a 6-bit binary number.
3. Active-HIGH output drives a common-cathode LED display.

SECTION 7 Encoders

1. (a) $A_0 = 1, A_1 = 1, A_2 = 0, A_3 = 1$
 (b) No, this is not a valid BCD code.
 (c) Only one input can be active for a valid output.
2. (a) $\bar{A}_3 = 0, \bar{A}_2 = 1, \bar{A}_1 = 1, \bar{A}_0 = 1$
 (b) The output is 0111, which is the complement of 1000 (8).

SECTION 8 Code Converters

1. 10000101 (BCD) = 1010101_2
2. An 8-bit binary-to-Gray converter consists of seven exclusive-OR gates in an arrangement like that in Figure 41 but with inputs B_0 - B_7 .

SECTION 9 Multiplexers (Data Selectors)

- The output is 0.
- 5 select inputs ($2^5 = 32$).
- The data output alternates between LOW and HIGH as the data-select inputs sequence through the binary states.
- The multiplexer multiplexes the two BCD codes to the 7-segment decoder.
 - The BCD-to-7-segment decoder decodes the BCD to energize the display.
 - The 2-line-to-4-line decoder enables the 7-segment displays alternately.

SECTION 10 Demultiplexers

- A decoder can be used as a multiplexer by using the input lines for data selection and an Enable line for data input.
- The outputs are all HIGH except D_{10} , which is LOW.

SECTION 11 Parity Generators/Checkers

- Even parity: 1110100
 - Even parity: 001100011
- Odd parity: 11010101
 - Odd parity: 11000001
- Code is correct, four 1s.
 - Code is in error, seven 1s

SECTION 12 Logic Functions with VHDL and Verilog

- A: `in bit_vector (7 downto 0);`
- `input [7:0] A;`
- Module is used in Verilog.
- $X = 6$ when the A inputs are 0110.

SECTION 13 Troubleshooting

- A glitch is a very short-duration voltage spike (usually unwanted).
- Glitches are caused by transition states.
- Strobe is the enabling of a device for a specified period of time when the device is not in transition.

ANSWERS TO RELATED PROBLEMS FOR EXAMPLES

- $\Sigma = 1, C_{out} = 1$
- $\Sigma_1 = 0, \Sigma_2 = 0, \Sigma_3 = 1, \Sigma_4 = 1$
- $1011 + 1010 = 10101$
- See Figure 84.

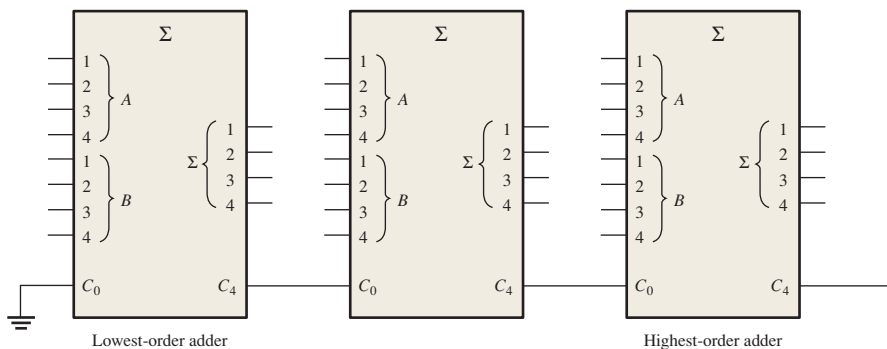


FIGURE 84

FUNCTIONS OF COMBINATIONAL LOGIC

- 5 See Figure 85.
- 6 $A > B = 0, A = B = 0, A < B = 1$
- 7 See Figure 86.

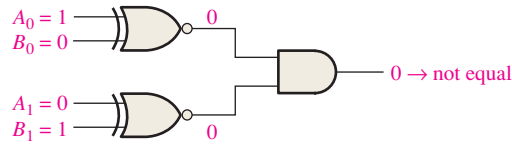


FIGURE 85

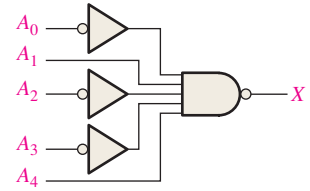


FIGURE 86

- 8 Output 22
- 9 See Figure 87.

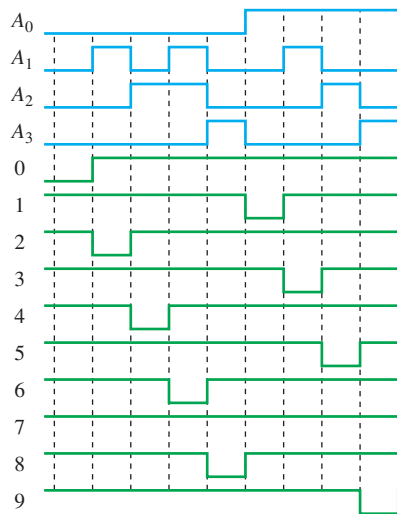


FIGURE 87

- 10 All inputs LOW: $\bar{A}_0 = 0, \bar{A}_1 = 1, \bar{A}_2 = 1, \bar{A}_3 = 0$
All inputs HIGH: All outputs HIGH.
- 11 BCD 0100001

0	0	0	0	0	0	0	0	1
0	0	0	1	0	1	0	0	0
0	0	1	0	1	0	0	1	0
0	0	1	0	1	0	0	1	0
- 12 Seven exclusive-OR gates
- 13 See Figure 88.

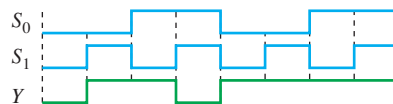


FIGURE 88

- 14 $D_0: S_3 = 0, S_2 = 0, S_1 = 0, S_0 = 0$
 $D_4: S_3 = 0, S_2 = 1, S_1 = 0, S_0 = 0$
 $D_8: S_3 = 1, S_2 = 0, S_1 = 0, S_0 = 0$
 $D_{13}: S_3 = 1, S_2 = 1, S_1 = 0, S_0 = 1$

15 See Figure 89.

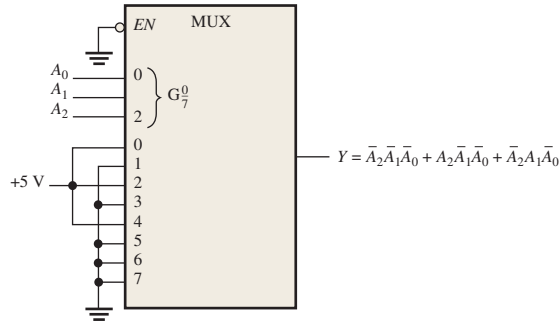


FIGURE 89

16 See Figure 90.

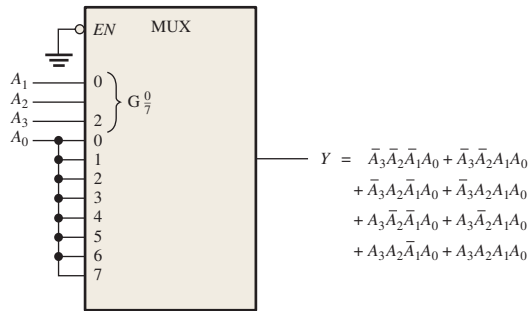


FIGURE 90

17 See Figure 91.

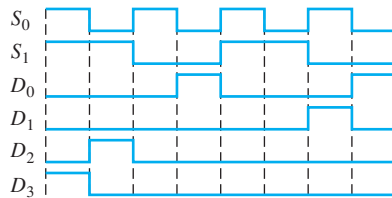


FIGURE 91

ANSWERS TO TRUE/FALSE QUIZ

1. T 2. F 3. T 4. F 5. F 6. T
 7. T 8. F 9. T 10. F 11. T

ANSWERS TO SELF-TEST

1. (a) 2. (b) 3. (c) 4. (a) 5. (d) 6. (b)
 7. (c) 8. (b) 9. (d) 10. (c) 11. (f) 12. (c)

ANSWERS TO ODD-NUMBERED PROBLEMS

1. Register A: 000000110110; Register B: 10110100
3. 00100100
5. (a) $A \oplus B = 0, \Sigma = 1, (A \oplus B)C_{in} = 0, AB = 1, C_{out} = 1$
 (b) $A \oplus B = 1, \Sigma = 0, (A \oplus B)C_{in} = 1, AB = 0, C_{out} = 1$
 (c) $A \oplus B = 1, \Sigma = 1, (A \oplus B)C_{in} = 0, AB = 0, C_{out} = 0$
7. (a) $\Sigma = 1, C_{out} = 0$;
 (b) $\Sigma = 1, C_{out} = 0$;
 (c) $\Sigma = 0, C_{out} = 1$;
 (d) $\Sigma = 1, C_{out} = 1$
9. 11100
11. $\Sigma_3 \Sigma_2 \Sigma_1 \Sigma_0 = 1101$
13. $\Sigma_1 = 0110; \Sigma_2 = 1011; \Sigma_3 = 0110; \Sigma_4 = 0001; \Sigma_5 = 1000$
15. 225 ns
17. $A = B$ is HIGH when $A_0 = B_0$ and $A_1 = B_1$; see Figure P-25.

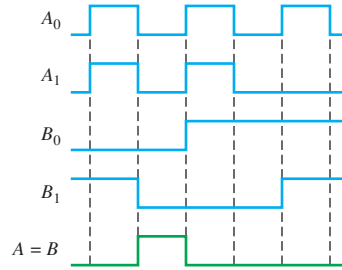


FIGURE P-25

19. (a) $A > B = 1; A = B = 0; A < B = 0$
 (b) $A < B = 1; A = B = 0; A > B = 0$
 (c) $A = B = 1; A < B = 0; A > B = 0$
21. See Figure P-26.

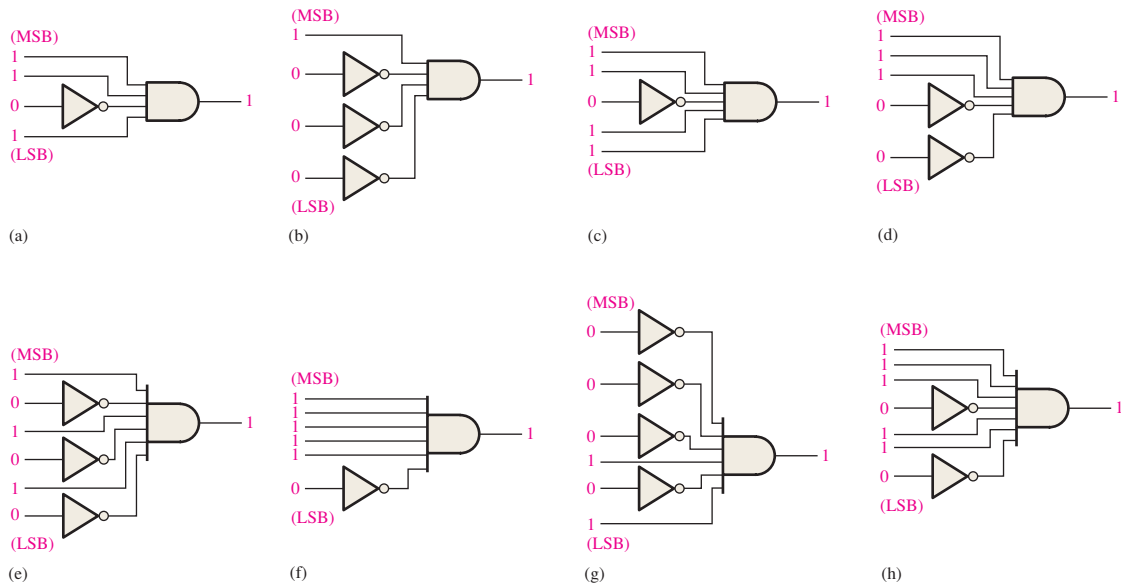


FIGURE P-26

23. $X = \bar{A}_3\bar{A}_2\bar{A}_1A_0 + A_3\bar{A}_2A_1\bar{A}_0 + A_3A_2\bar{A}_1\bar{A}_0 + A_3\bar{A}_2A_1A_0$
 25. See Figure P-27.

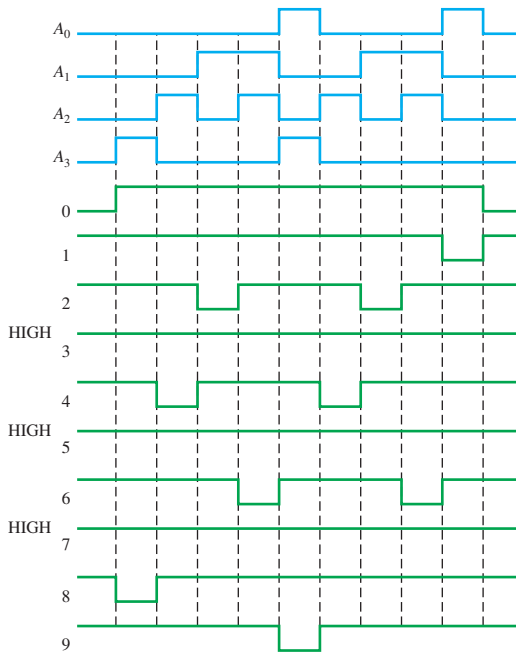


FIGURE P-27

27. $A_3A_2A_1A_0 = 1011$, invalid BCD
 29. (a) $2 = 0010_{\text{BCD}} = 0010_2$
 (b) $8 = 1000_{\text{BCD}} = 1000_2$
 (c) $13 = 00010011_{\text{BCD}} = 1101_2$
 (d) $26 = 00100110_{\text{BCD}} = 11010_2$
 (e) $33 = 00110011_{\text{BCD}} = 100001_2$
 31. (a) 1010000000 Gray \rightarrow 1100000000 binary
 (b) 0011001100 Gray \rightarrow 0010001000 binary
 (c) 1111000111 Gray \rightarrow 1010000101 binary
 (d) 0000000001 Gray \rightarrow 0000000001 binary

See Figure P-28.

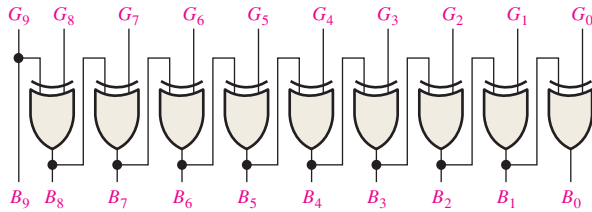


FIGURE P-28

33. See Figure P-29.

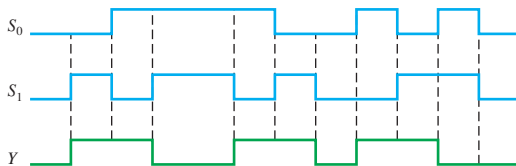


FIGURE P-29

35. See Figure P-30.

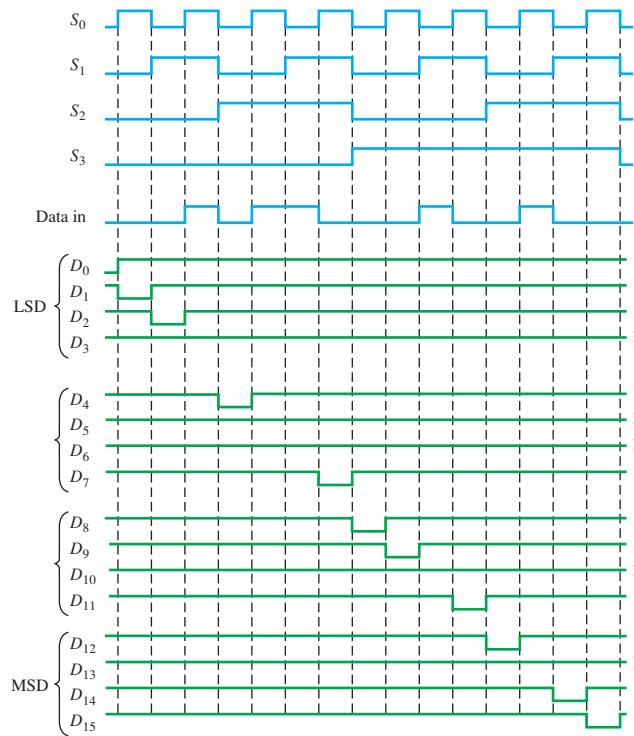


FIGURE P-30

37. See Figure P-31.

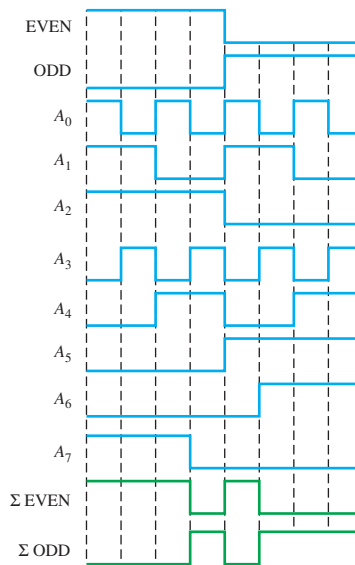


FIGURE P-31

```

39. module 8_Bit_Adder (A, B, C, Cin, SUM, Cout);
    input [7:0] A;
    input [7:0] B;
    input Cin;
    output [7:0] SUM;
    output [7:0] Cout;
    wire C1, C2, C3, C4, C5, C6, C7;
    Full Adder Full Adder 1 (A[0], B[0], Cin, SUM[0], C1);
    Full Adder Full Adder 2 (A[1], B[1], Cin, SUM[1], C2);
    
```

Full Adder Full Adder 3 (A[2], B[2], Cin, SUM[2], C3);
 Full Adder Full Adder 4 (A[3], B[3], Cin, SUM[3], C4);
 Full Adder Full Adder 5 (A[4], B[4], Cin, SUM[4], C5);
 Full Adder Full Adder 6 (A[5], B[5], Cin, SUM[5], C6);
 Full Adder Full Adder 7 (A[6], B[6], Cin, SUM[6], C7);
 Full Adder Full Adder 8 (A[7], B[7], Cin, SUM[7], Cout);

endmodule

41. **module** Encoder (D, X);

input [9:0] D; **output** [3:0] X;

X[0] = (D[1] || D[3] || D[5] || D[7] || D[9]) && !(D[0] || D[2] || D[4] || D[6] || D[8]);

X[1] = (D[2] || D[3] || D[6] || D[7]) && !(D[0] || D[1] || D[4] || D[5] || D[8] || D[9]);

X[2] = (D[4] || D[5] || D[6] || D[7]) && !(D[0] || D[1] || D[2] || D[3] || D[8] || D[9]);

X[3] = (D[8] || D[9]) && !(D[0] || D[1] || D[2] || D[3] || D[4] || D[5] || D[6] || D[7]);

endmodule

43. (a) OK

(b) segment *g* burned out; output G open

(c) Segment *b* output stuck LOW

45. (a) The A_1 input of the top adder is open: All binary values corresponding to a BCD number having a value of 0, 1, 4, 5, 8, or 9 will be off by 2. This will first be seen for a BCD value of 0000 0000.

(b) The carry out of the top adder is open: All values not normally involving an output carry will be off by 32. This will first be seen for a BCD value of 0000 0000.

(c) The Σ_4 output of the top adder is shorted to ground: Same binary values above 15 will be short by 16. The first BCD value to indicate this will be 0001 1000.

(d) The Σ_3 output of the bottom adder is shorted to ground: Every other set of 16 values starting with 16 will be short 16. The first BCD value to indicate this will be 0001 0110.

47. 1. Place a LOW on the Enable input.

2. Apply a HIGH to D_0 and a LOW to D_1 through D_7 .

3. Go through the binary sequence on the select inputs and check Y and \bar{Y} according to Table P-10.

TABLE P-10				
S_2	S_1	S_0	Y	\bar{Y}
0	0	0	1	0
0	0	1	0	1
0	1	0	0	1
0	1	1	0	1
1	0	0	0	1
1	0	1	0	1
1	1	0	0	1
1	1	1	0	1

4. Repeat the binary sequence of select inputs for each set of data inputs listed in Table P-11. A HIGH on the Y output should occur only for the corresponding combinations of select inputs shown.

49. Apply a HIGH in turn to each Data input, D_0 through D_7 with LOWs on all the other inputs. For each HIGH applied to a data input, sequence through all eight binary combinations of select inputs ($S_2S_1S_0$) and check for HIGH on the corresponding data output and LOWs on all the other data outputs.

51. $\Sigma = \bar{A}\bar{B}C_{in} + \bar{A}B\bar{C}_{in} + A\bar{B}\bar{C}_{in} + ABC_{in}$
 $C_{out} = \bar{A}BC_{in} + A\bar{B}C_{in} + \bar{A}B\bar{C}_{in} + ABC_{in}$

TABLE P-11

D_0	D_1	D_2	D_3	D_4	D_5	D_6	D_7	Y	\bar{Y}	S_2	S_1	S_0
L	H	L	L	L	L	L	L	1	0	0	0	1
L	L	H	L	L	L	L	L	1	0	0	1	0
L	L	L	H	L	L	L	L	1	0	0	1	1
L	L	L	L	H	L	L	L	1	0	1	0	0
L	L	L	L	L	H	L	L	1	0	1	0	1
L	L	L	L	L	L	H	L	1	0	1	1	0
L	L	L	L	L	L	L	H	1	0	1	1	1

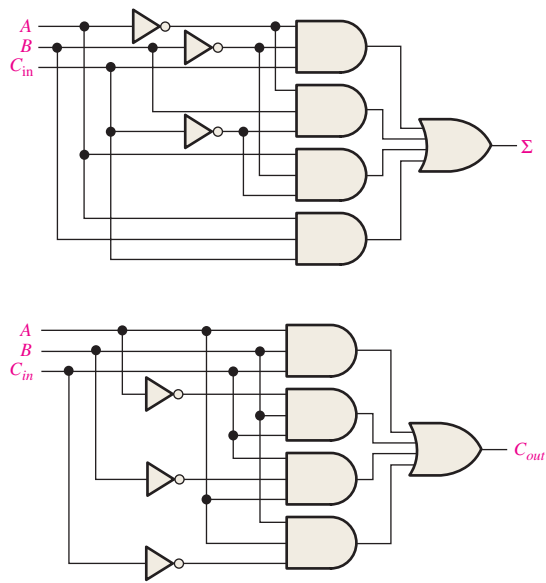


FIGURE P-32

See Figure P-32.

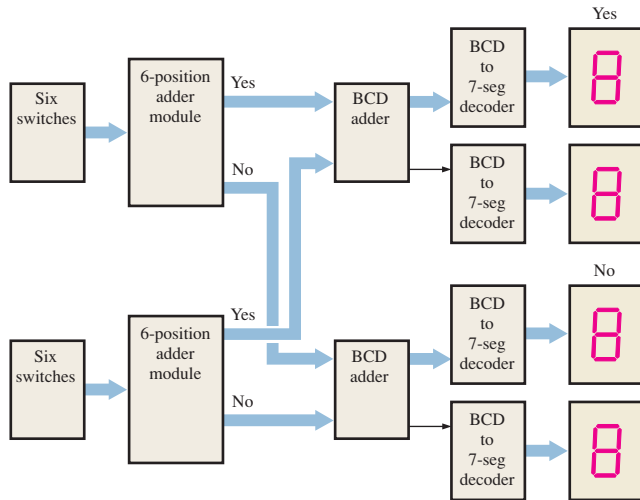


FIGURE P-33

53. See the block diagram in Figure P-33.

55. **Circuit fault:** Input B of 3-to-8 decoder is shorted to V_{CC} .

Predicted effect of fault: Inputs are decoded as follows:

0000 = 2, 0001 = 3, 0010 = 2, 0011 = 3, 0100 = 6, 0101 = 7, 0110 = 6, 0111 = 7,
1000 and higher = no decoded output.

Observed effect of introduced fault: Inputs are decoded as follows:

0000 = 2, 0001 = 3, 0010 = 2, 0011 = 3, 0100 = 6,
0101 = 7, 0110 = 6, 0111 = 7, 1000 and higher = no decoded output.

57. **Observed operation:** Data output X is incorrect for binary inputs of 0011, 0111, 1011, and 1111.

Suspected fault: Line from input S2 to multiplexer input B is shorted to ground.

Effect of introduced fault: Data output X is incorrect for binary inputs of 0011, 0111, 1011, and 1111.

LATCHES, FLIP-FLOPS, AND TIMERS

LATCHES, FLIP-FLOPS, AND TIMERS

OUTLINE

- 1 A System
- 2 Latches
- 3 Flip-Flops
- 4 Flip-Flop Operating Characteristics
- 5 Timers
- 6 Bistable Logic with VHDL and Verilog
- 7 Traffic signal control system with VHDL and Verilog
- 8 Troubleshooting

OBJECTIVES

- Describe a traffic signal control system
- Use logic gates to construct basic latches
- Explain the difference between an S-R latch and a D latch
- Recognize the difference between a latch and a flip-flop
- Explain how D and J-K flip-flops differ
- Understand the significance of propagation delays, set-up time, hold time, maximum operating frequency, minimum clock pulse widths, and power dissipation in the application of flip-flops
- Apply flip-flops in basic applications
- Explain how retriggerable and nonretriggerable one-shots differ
- Connect a 555 timer to operate as either an astable multivibrator or a one-shot
- Use VHDL and Verilog to implement flip-flops

- Use VHDL and Verilog to implement a traffic signal control system
- Discuss system troubleshooting

KEY TERMS

Latch	Preset
Bistable	Clear
SET	Propagation delay time
RESET	Set-up time
Clock	Hold time
Edge-triggered flip-flop	Power dissipation
D flip-flop	Monostable
Synchronous	One-shot
J-K flip-flop	Astable
Toggle	Timer

INTRODUCTION

A traffic signal control system is introduced at the beginning of this chapter. Bistable, monostable, and astable logic devices called *multivibrators* are covered. Two categories of bistable devices are the latch and the flip-flop. Bistable devices have two stable states, called SET and RESET; they can retain either of these states

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indefinitely, making them useful as storage devices. The basic difference between latches and flip-flops is the way in which they are changed from one state to the other. The flip-flop is a basic building block for counters, registers, and other sequential control logic and is used in certain types of memories. The monostable multivibrator, commonly known as the one-shot, has only one stable state. A one-shot produces a single controlled-

width pulse when activated or triggered. The astable multivibrator has no stable state and is used primarily as an oscillator, which is a self-sustained waveform generator. Pulse oscillators are used as the sources for timing waveforms in digital systems. Using VHDL and Verilog to describe bistable logic as well as the traffic signal control system is covered.

1 A SYSTEM

In this section, a traffic signal control system is presented to illustrate how combinational logic, flip-flops, and timers can be used to accomplish a specified function. The system controls the sequencing of traffic lights at a busy main street and an occasionally used side street.

After completing this section, you should be able to

- Describe how the system is implemented
- Explain how timers are used in this system
- Explain how flip-flops are used in this system

Timing Requirements

The following are the timing requirements for the traffic signal control system. These requirements are illustrated in Figure 1.

- The green light for the main street will stay on for a minimum of 25 s or as long as there is no vehicle on the side street.
- The green light for the side street will stay on until there is no vehicle on the side street up to a maximum of 25 s.
- The yellow caution light will stay on for 4 s between changes from green to red on both the main street and the side street.

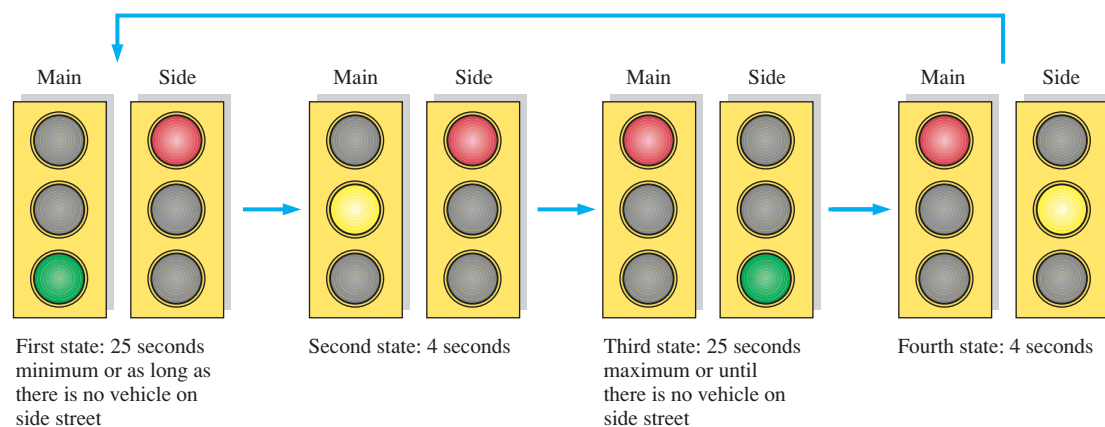


FIGURE 1 Traffic light timing sequence.

The State Diagram

A state diagram graphically shows the sequence of states, the conditions for each state, and the requirements for transitions from one state to the next. Although Figure 1 is a basic

form of state diagram, a standard type of diagram shows the logic states and the Boolean expressions for the transitions.

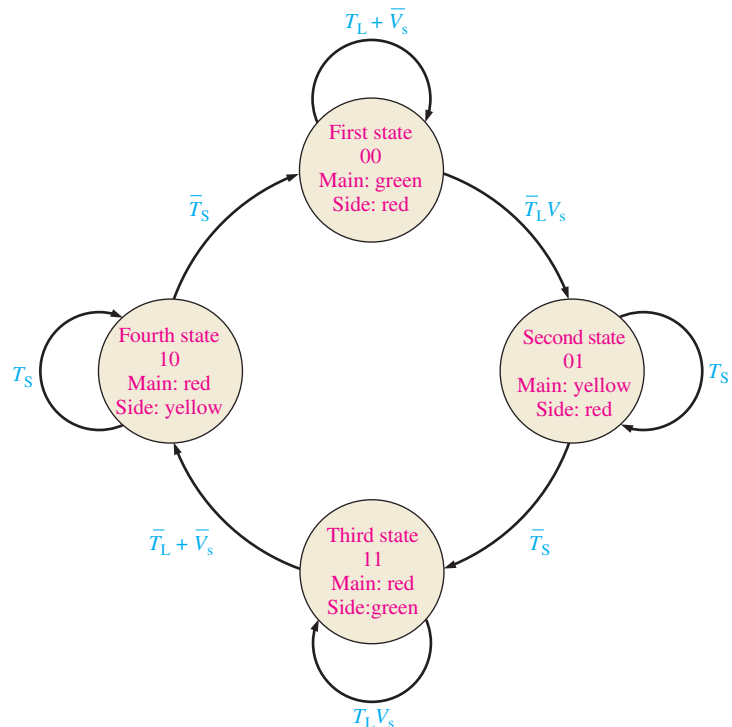
DEFINING THE VARIABLES The variables that determine how the system sequences through the various states are defined as follows:

- V_s A vehicle is present on the side street.
- T_L The 25 s timer (long timer) is *on*.
- T_S The 4 s timer (short timer) is *on*.

A complemented variable indicates the opposite condition.

STATE DESCRIPTIONS A **state diagram*** is shown in Figure 2. Each of the four states is assigned a 2-bit Gray code as indicated. A looping arrow means that the system remains in a state, and an arrow between states means that the system transitions to the next state. The Boolean expression or variable associated with each of the arrows in the state diagram indicates the condition under which the system remains in a state or transitions to the next state.

FIGURE 2 State diagram for the traffic signal control system.



First State The Gray code is 00. In this state (S_1), the light is green on the main street and red on the side street for 25 s when the long timer is *on* or there is no vehicle on the side street. This condition is expressed as $T_L + \bar{V}_s$. The system transitions to the next state when the long timer goes *off* and there is a vehicle on the side street. This condition is expressed as $\bar{T}_L V_s$.

Second State The Gray code is 01. In this state (S_2), the light is yellow on the main street and red on the side street. The system remains in this state for 4 s when the short timer is *on*. This condition is expressed as T_S . The system transitions to the next state when the short timer goes *off*. This condition is expressed as \bar{T}_S .

Third State The Gray code is 11. In this state (S_3), the light is red on the main street and green on the side street for 25 s when the long timer is *on* as long as there is a vehicle on the side street. This condition is expressed as $T_L V_s$. The system transitions to the next state when the long timer goes *off* or when there is no vehicle on the side street. This condition is expressed as $\bar{T}_L + \bar{V}_s$.

*The bold terms in color are key terms and are included in a Key Term glossary at the end of the chapter.

Fourth State The Gray code is 10. In this state (S_4), the light is red on the main street and yellow on the side street. The system remains in this state for 4 s when the short timer is *on*. This condition is expressed as T_S . The system transitions back to the first state when the short timer goes *off*. This condition is expressed as \bar{T}_S .

Block Diagram

The traffic signal control system consists of three parts: combinational logic, sequential logic, and timing circuits, as shown in Figure 3.

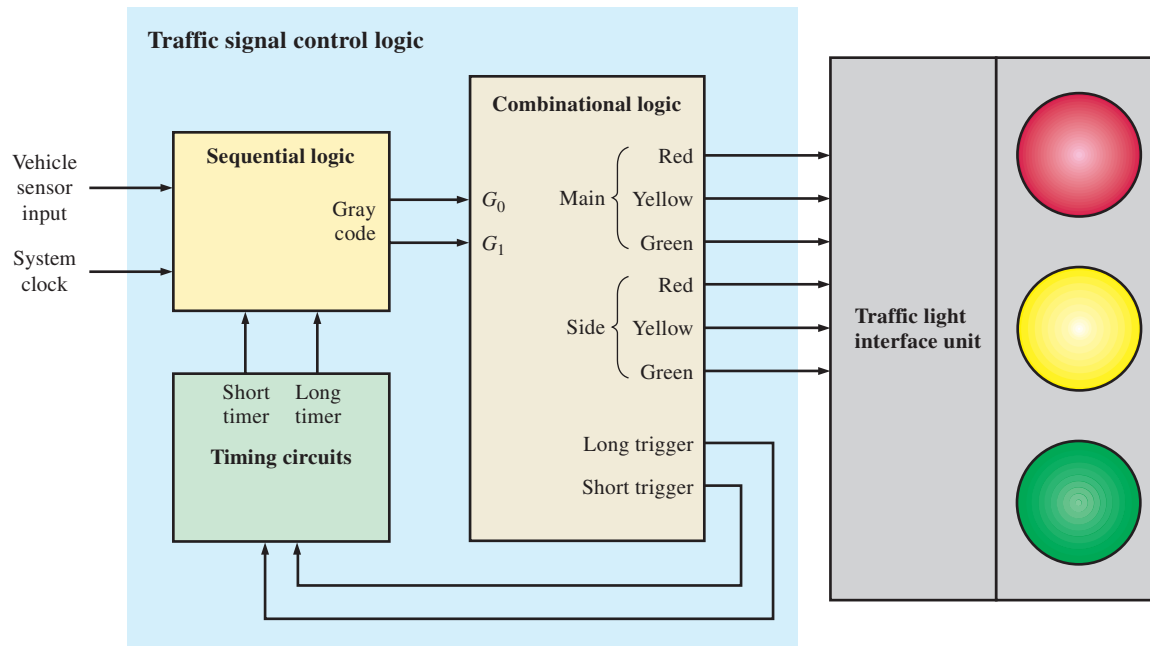


FIGURE 3 Block diagram of the traffic signal control system.

The combinational logic portion of the system provides outputs to turn the signal lights on and off. It also provides trigger outputs to start the long and short timers. The input sequence to this logic represents the four states described by the state diagram. The timing circuits portion of the system provides the 25 s and the 4 s timing outputs. The sequential logic produces the sequence of 2-bit Gray codes representing the four states.

The Combinational Logic

The combinational logic consists of a state decoder, light output logic, and trigger logic.

STATE DECODER This logic decodes the 2-bit Gray code from the sequential logic to determine which of the four states the system is in. The inputs to the state decoder are the two Gray code bits G_1 and G_0 . There are four state outputs S_1 , S_2 , S_3 , and S_4 . For each of the four input codes, one and only one of the outputs is activated. The logic and Boolean expressions are shown in Figure 4.

LIGHT OUTPUT LOGIC This logic has the four state outputs of the state decoder as its inputs and produces six outputs to turn the traffic lights on and off. These outputs are designated MR , MY , MG (main red, main yellow, main green) and SR , SY , SG (side red, side yellow, side green).

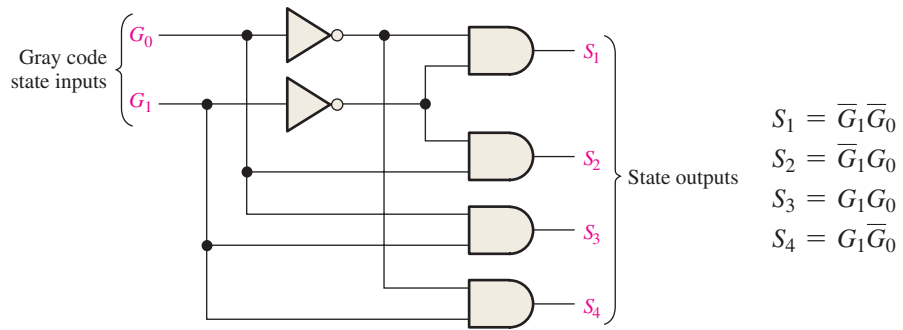


FIGURE 4 State decoder logic and output expressions.

Refer to the state diagram in Figure 2. The main red is *on* in the third state (S_3) or in the fourth state (S_4), so the Boolean expression is

$$MR = S_3 + S_4$$

The main yellow is *on* in the second state (S_2), so the expression is

$$MY = S_2$$

The main green is *on* in the first state (S_1), so the expression is

$$MG = S_1$$

Similarly, the state diagram is used to obtain the following expressions for the side street:

$$SR = S_1 + S_2$$

$$SY = S_4$$

$$SG = S_3$$

TRIGGER LOGIC The trigger logic produces two outputs, the long trigger output and the short trigger output. The long trigger output initiates the 25 s timer on a LOW-to-HIGH transition at the beginning of the first or third states. The short trigger output initiates the 4 s timer on a LOW-to-HIGH transition at the beginning of the second or fourth states. The Boolean expressions for this logic are

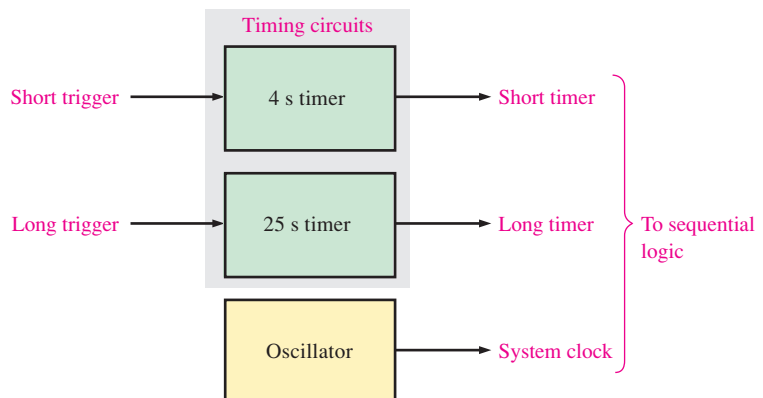
$$LongTrig = S_1 + S_3$$

$$ShortTrig = S_2 + S_4$$

Timing Circuits

The timing circuits portion of the traffic signal control system in Figure 3 consists of a 25 s timer and a 4 s timer, as shown in Figure 5. The 25 s timer and the 4 s timer are triggered by the long trigger and short trigger signals, respectively, from the combinational logic. The system clock is produced by an astable multivibrator (covered later) or other type of oscillator.

FIGURE 5 Block diagram of the timing circuits and the system clock generator.



Sequential Logic

The sequential logic controls the sequencing of the traffic signals, based on inputs from the timing circuits and the side street vehicle sensor. The sequential logic produces a 2-bit Gray code sequence for each of the four states that were described in Figure 2.

THE COUNTER The sequential logic consists of a 2-bit Gray code counter made up of two flip-flops and the associated logic, as shown in Figure 6. The counter produces the four-state sequence on outputs G_0 and G_1 . Transitions from one state to the next are determined by the short timer (T_S), the long timer (T_L), and vehicle sensor for the side street (V_s) inputs. The 10 kHz clock input (CLK) comes from the system clock oscillator in the timing circuits.

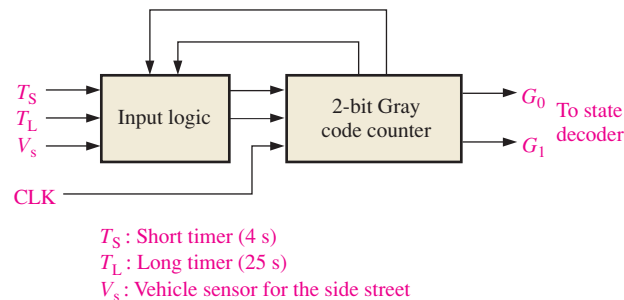


FIGURE 6 Block diagram of the sequential logic.

SECTION 1 CHECKUP*

- Referring to the state diagram, how long can the system remain in the first state?
- How long can the system remain in the fourth state?
- What determines how long the main street light stays red?

*Answers are at the end of the chapter.

2 LATCHES

The **latch** is a type of temporary storage device that has two stable states (bistable) and is normally placed in a category separate from that of flip-flops. Latches are similar to flip-flops because they are bistable devices that can reside in either of two states using a feedback arrangement, in which the outputs are connected back to the opposite inputs. The main difference between latches and flip-flops is in the method used for changing their state.

After completing this section, you should be able to

- Explain the operation of a basic S-R latch
- Explain the operation of a gated S-R latch
- Explain the operation of a gated D latch
- Implement an S-R or D latch with logic gates

The S-R (SET-RESET) Latch

A latch is a type of **bistable** logic device or **multivibrator**. An active-HIGH input S-R (SET-RESET) latch is formed with two cross-coupled NOR gates, as shown in Figure 7(a); an active-LOW input $\bar{S}\bar{R}$ latch is formed with two cross-coupled NAND gates, as shown

A latch can reside in either of its two states, SET or RESET.

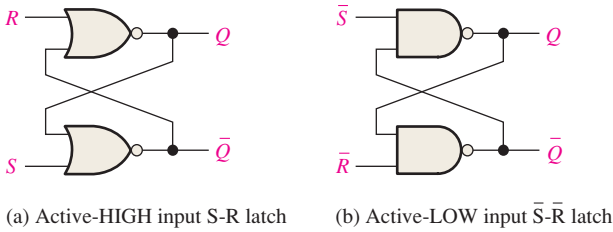


FIGURE 7 Two versions of SET-RESET (S-R) latches. Open files F06-07(a) and (b) and verify the operation of both latches.

MULTISIM

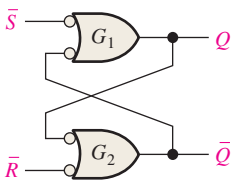


FIGURE 8 Negative-OR equivalent of the NAND gate $\bar{S}\text{-}\bar{R}$ latch in Figure 7(b).

SET means that the Q output is HIGH.

RESET means that the Q output is LOW.

in Figure 7(b). Notice that the output of each gate is connected to an input of the opposite gate. This produces the regenerative **feedback** that is characteristic of all latches and flip-flops.

To explain the operation of the latch, we will use the NAND gate $\bar{S}\text{-}\bar{R}$ latch in Figure 7(b). This latch is redrawn in Figure 8 with the negative-OR equivalent symbols used for the NAND gates. This is done because LOWs on the \bar{S} and \bar{R} lines are the activating inputs.

The latch in Figure 8 has two inputs, \bar{S} and \bar{R} , and two outputs, Q and \bar{Q} . Let's start by assuming that both inputs and the Q output are HIGH, which is the normal latched state.

Since the Q output is connected back to an input of gate G_2 , and the \bar{R} input is HIGH, the output of G_2 must be LOW. This LOW output is coupled back to an input of gate G_1 , ensuring that its output is HIGH.

When the Q output is HIGH, the latch is in the **SET** state. It will remain in this state indefinitely until a LOW is temporarily applied to the \bar{R} input. With a LOW on the \bar{R} input and a HIGH on \bar{S} , the output of gate G_2 is forced HIGH. This HIGH on the \bar{Q} output is coupled back to an input of G_1 , and since the \bar{S} input is HIGH, the output of G_1 goes LOW. This LOW on the Q output is then coupled back to an input of G_2 , ensuring that the \bar{Q} output remains HIGH even when the LOW on the \bar{R} input is removed. When the Q output is LOW, the latch is in the **RESET** state. Now the latch remains indefinitely in the RESET state until a momentary LOW is applied to the \bar{S} input.

In normal operation, the outputs of a latch are always complements of each other.

When Q is HIGH, \bar{Q} is LOW, and when Q is LOW, \bar{Q} is HIGH.

An invalid condition in the operation of an active-LOW input $\bar{S}\text{-}\bar{R}$ latch occurs when LOWs are applied to both \bar{S} and \bar{R} at the same time. As long as the LOW levels are simultaneously held on the inputs, both the Q and \bar{Q} outputs are forced HIGH, thus violating the basic complementary operation of the outputs. Also, if the LOWs are released simultaneously, both outputs will attempt to go LOW. Since there is always some small difference in the propagation delay time of the gates, one of the gates will dominate in its transition to the LOW output state. This, in turn, forces the output of the slower gate to remain HIGH. In this situation, you cannot reliably predict the next state of the latch.

Figure 9 illustrates the active-LOW input $\bar{S}\text{-}\bar{R}$ latch operation for each of the four possible combinations of levels on the inputs. (The first three combinations are valid, but the last is not.) Table 1 summarizes the logic operation in truth table form. Operation of the active-HIGH input NOR gate latch in Figure 7(a) is similar but requires the use of opposite logic levels.

Table 1 • Truth table for an active-LOW input $\bar{S}\text{-}\bar{R}$ latch.

INPUTS		OUTPUTS		COMMENTS
\bar{S}	\bar{R}	Q	\bar{Q}	
1	1	NC	NC	No change. Latch remains in present state.
0	1	1	0	Latch SET.
1	0	0	1	Latch RESET.
0	0	1	1	Invalid condition

Logic symbols for both the active-HIGH input and the active-LOW input latches are shown in Figure 10.

Example 1 illustrates how an active-LOW input $\bar{S}\text{-}\bar{R}$ latch responds to conditions on its inputs. LOW levels are pulsed on each input in a certain sequence and the resulting

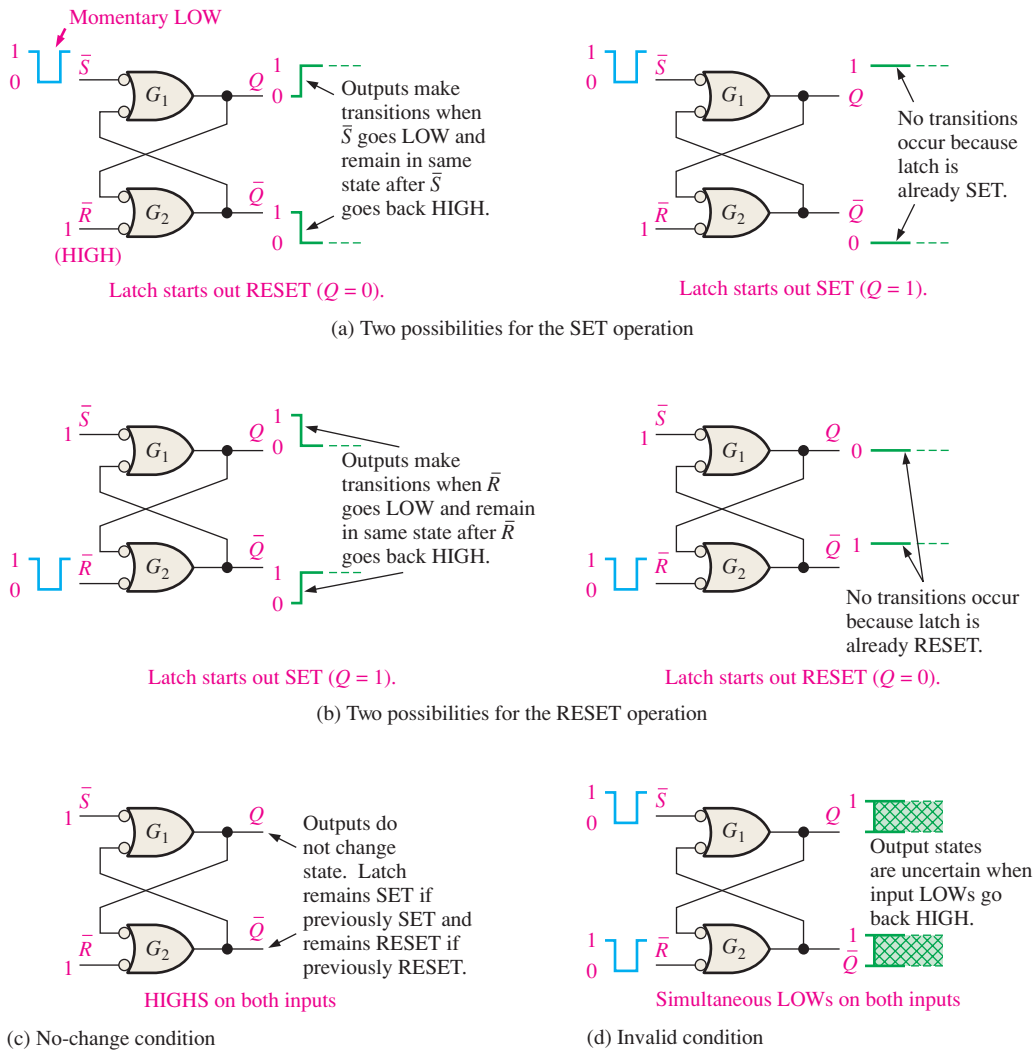


FIGURE 9 The three modes of basic \bar{S} - \bar{R} latch operation (SET, RESET, no-change) and the invalid condition.

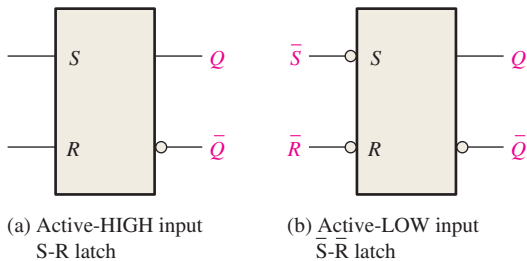


FIGURE 10 Logic symbols for the S-R and \bar{S} - \bar{R} latch.

Q output waveform is observed. The $\bar{S} = 0, \bar{R} = 0$ condition is avoided because it results in an invalid mode of operation and is a major drawback of any SET-RESET type of latch.

EXAMPLE 1

If the \bar{S} and \bar{R} waveforms in Figure 11(a) are applied to the inputs of the latch in Figure 10(b), determine the waveform that will be observed on the Q output. Assume that Q is initially LOW.

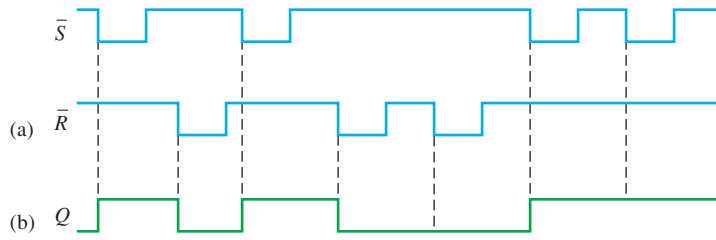


FIGURE 11

SOLUTION

See Figure 11(b).

RELATED PROBLEM*

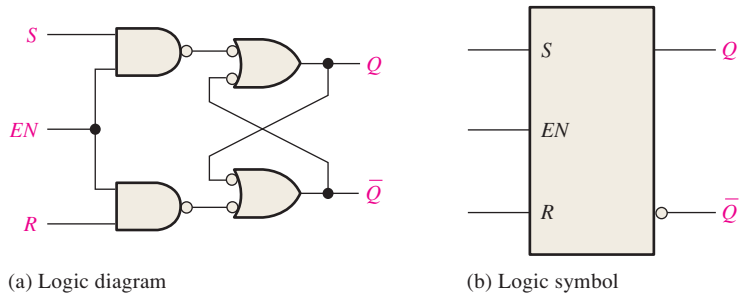
Determine the Q output of an active-HIGH input S-R latch if the waveforms in Figure 11(a) are inverted and applied to the inputs.

*Answers are at the end of the chapter.

The Gated S-R Latch

A gated latch requires an enable input, EN (G is also used to designate an enable input). The logic diagram and logic symbol for a gated S-R latch are shown in Figure 12. The S and R inputs control the state to which the latch will go when a HIGH level is applied to the EN input. The latch will not change until EN is HIGH; but as long as it remains HIGH, the output is controlled by the state of the S and R inputs. The gated latch is a level-sensitive device. In this circuit, the invalid state occurs when both S and R are simultaneously HIGH and EN is also HIGH.

FIGURE 12 A gated S-R latch.



EXAMPLE 2

Determine the Q output waveform if the inputs shown in Figure 13(a) are applied to a gated S-R latch that is initially RESET.

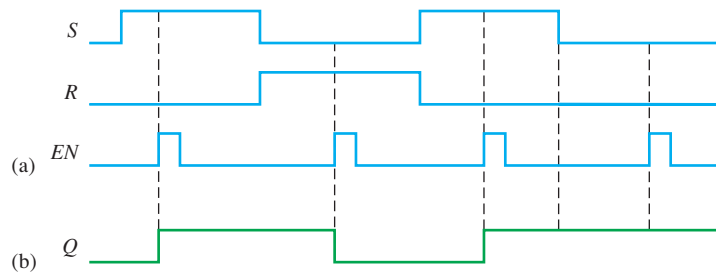


FIGURE 13

SOLUTION

The Q waveform is shown in Figure 13(b). When S is HIGH and R is LOW, a HIGH on the EN input sets the latch. When S is LOW and R is HIGH, a HIGH on the EN input resets the latch. When both S and R are LOW, the Q output does not change from its present state.

RELATED PROBLEM

Determine the Q output of a gated S-R latch if the S and R inputs in Figure 13(a) are inverted.

The Gated D Latch

Another type of gated latch is called the D latch. It differs from the S-R latch because it has only one input in addition to EN . This input is called the D (data) input. Figure 14 contains a logic diagram and logic symbol of a D latch. When the D input is HIGH and the EN input is HIGH, the latch will set. When the D input is LOW and EN is HIGH, the latch will reset. Stated another way, the output Q follows the input D when EN is HIGH.

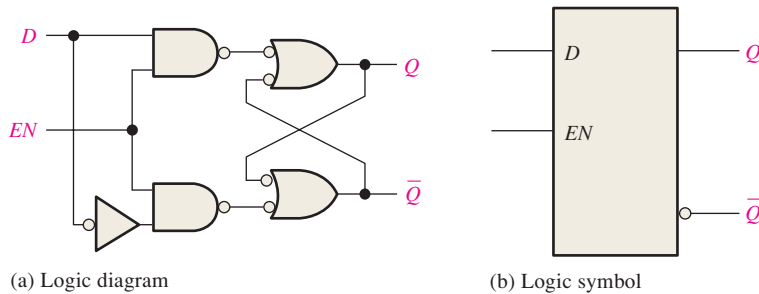


FIGURE 14 A gated D latch.

EXAMPLE 3

Determine the Q output waveform if the inputs shown in Figure 15(a) are applied to a gated D latch, which is initially RESET.

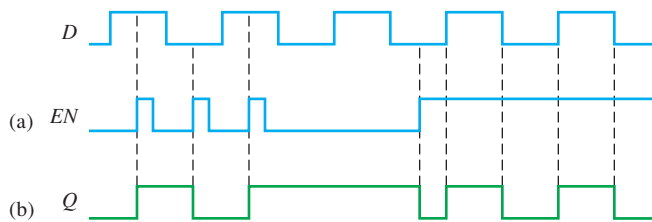


FIGURE 15

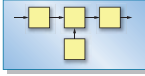
SOLUTION

The Q waveform is shown in Figure 15(b). When D is HIGH and EN is HIGH, Q goes HIGH. When D is LOW and EN is HIGH, Q goes LOW. When EN is LOW, the state of the latch is not affected by the D input.

RELATED PROBLEM

Determine the Q output of the gated D latch if the D input in Figure 15(a) is inverted.

Latches are sometimes used for multiplexing data onto a bus. For example, data being input to a computer from an external source have to share the data bus with data from other sources. When the data bus becomes unavailable to the external source, the existing data must be temporarily stored, and latches placed between the external source and the data bus may be used to do this. When the data bus is unavailable to the external source, the latches must be disconnected from the bus using a method known as tristating. When the data bus becomes available, the external data pass through the latches, thus the term *transparent latch*. The gated D latch performs this function because when it is enabled, the data on its input appear on the output just as though there were a direct connection. Data on the input are stored as soon as the latch is disabled.



SYSTEM NOTE

SECTION 2 CHECKUP

- List three types of latches.
- Develop the truth table for the active-HIGH input S-R latch in Figure 7(a).
- What is the Q output of a D latch when $EN = 1$ and $D = 1$?

3 FLIP-FLOPS

Flip-flops are synchronous bistable devices, also known as *bistable multivibrators*. In this case, the term *synchronous* means that the output changes state only at a specified point (leading or trailing edge) on the triggering input called the **clock** (CLK), which is designated as a control input, C ; that is, changes in the output occur in synchronization with the clock. Flip-flops are edge-sensitive whereas gated latches are level-sensitive.

After completing this section, you should be able to

- Define *clock*
- Define *edge-triggered flip-flop*
- Explain the difference between a flip-flop and a latch
- Identify an edge-triggered flip-flop by its logic symbol
- Discuss the difference between a positive and a negative edge-triggered flip-flop
- Discuss and compare the operation of D and J-K edge-triggered flip-flops and explain the differences in their truth tables.
- Discuss the asynchronous inputs of a flip-flop

Edge-Triggered Flip-Flops

An **edge-triggered flip-flop** changes state either at the positive edge (rising edge) or at the negative edge (falling edge) of the clock pulse and is sensitive to its inputs only at this transition of the clock. Two types of edge-triggered flip-flops are covered in this section: D and J-K. The logic symbols for these flip-flops are shown in Figure 16. Notice that each type can be either positive edge-triggered (no bubble at C input) or negative edge-triggered

The dynamic input indicator \triangleright means the flip-flop changes state only on the edge of a clock pulse.

(bubble at C input). The key to identifying an edge-triggered flip-flop by its logic symbol is the small triangle inside the block at the clock (C) input. This triangle is called the *dynamic input indicator*.

THE EDGE-TRIGGERED D FLIP-FLOP The D input of the **D flip-flop** is called a **synchronous** input because data on the input is transferred to the flip-flop's output only on the triggering edge of the clock pulse. When D is HIGH, the Q output goes HIGH on the triggering edge of the clock pulse, and the flip-flop is SET. When D is LOW, the Q output goes LOW on the triggering edge of the clock pulse, and the flip-flop is RESET.

This basic operation of a positive edge-triggered D flip-flop is illustrated in Figure 17, and Table 2 is the truth table for this type of flip-flop. Remember, *the flip-flop cannot change state except on the triggering edge of a clock pulse*. The D input can change at any time when the clock input is LOW or HIGH (except for a very short interval around the triggering transition of the clock) without affecting the output. Just remember that Q follows D at the triggering edge of the clock.

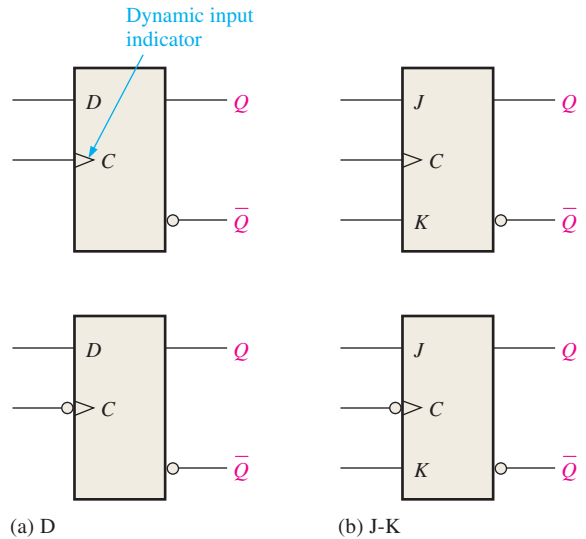
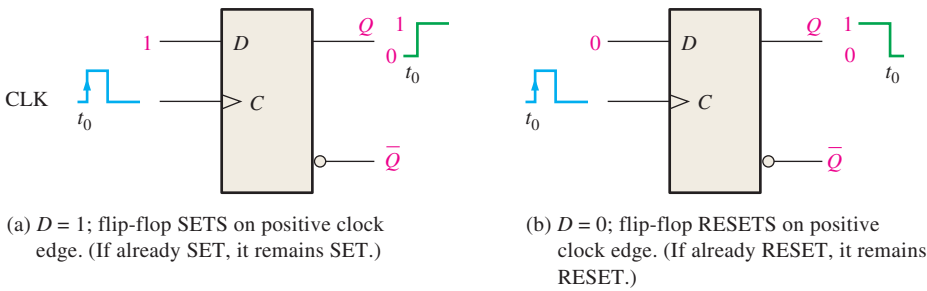


FIGURE 16 Edge-triggered flip-flop logic symbols (top: positive edge-triggered; bottom: negative edge-triggered).



The Q output of a D flip-flop assumes the state of the D input on the triggering edge of the clock.

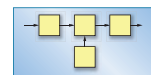
FIGURE 17 Operation of a positive edge-triggered D flip-flop.

Table 2 • Truth table for a positive edge-triggered D flip-flop.				
INPUTS		OUTPUTS		COMMENTS
D	CLK	Q	\bar{Q}	
1	↑	1	0	SET (stores a 1)
0	↑	0	1	RESET (stores a 0)

↑ = clock transition LOW to HIGH

Semiconductor memories in computers consist of large numbers of individual cells. Each storage cell holds a 1 or a 0. One type of memory is the Static Random Access Memory or SRAM, which uses flip-flops for the storage cells because a flip-flop will retain either of its two states indefinitely as long as dc power is applied, thus the term *static*. This type of memory is classified as a *volatile* memory because all the stored data are lost when power is turned off. Another type of memory, the Dynamic Random Access Memory or DRAM, uses capacitance rather than flip-flops as the basic storage element and must be periodically refreshed in order to maintain the stored data.

SYSTEM NOTE



The operation and truth table for a negative edge-triggered D flip-flop are the same as those for a positive edge-triggered device except that the falling edge of the clock pulse is the triggering edge.

EXAMPLE 4

Determine the Q and \bar{Q} output waveforms of the flip-flop in Figure 18 for the D and CLK inputs in Figure 19 (a). Assume that the positive edge-triggered flip-flop is initially RESET.

FIGURE 18

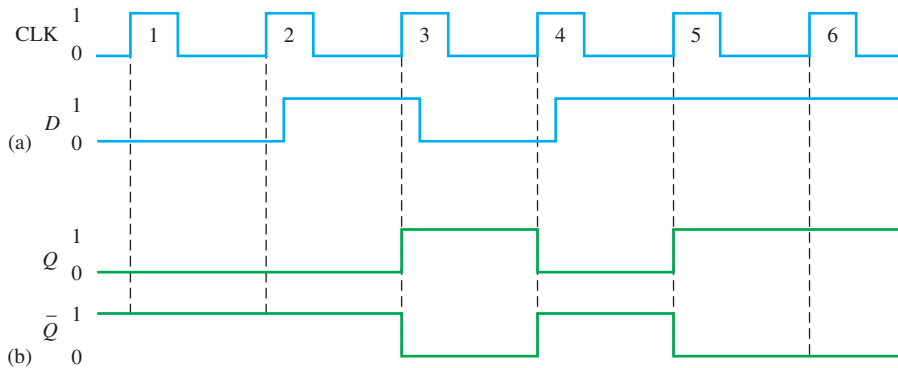
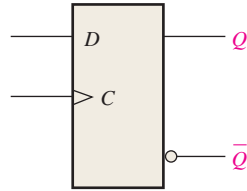


FIGURE 19

SOLUTION

1. At clock pulse 1, D is LOW, so Q remains LOW.
2. At clock pulse 2, D is LOW, so Q remains LOW (RESET).
3. At clock pulse 3, D is HIGH, so Q goes HIGH (SET).
4. At clock pulse 4, D is LOW, so Q goes LOW (RESET).
5. At clock pulse 5, D is HIGH, so Q goes HIGH (SET).
6. At clock pulse 6, D is HIGH, so Q stays HIGH.

Once Q is determined, \bar{Q} is easily found since it is simply the complement of Q . The resulting waveforms for Q and \bar{Q} are shown in Figure 19(b) for the input waveforms.

RELATED PROBLEM

Determine Q and \bar{Q} for the D input in Figure 19(a) if the flip-flop is a negative edge-triggered device.

EXAMPLE 5

Given the waveforms in Figure 20(a) for the D input and the clock, determine the Q output waveform if the flip-flop starts out RESET.

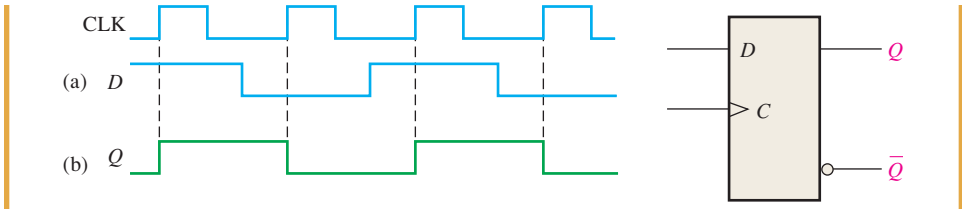


FIGURE 20

SOLUTION

The Q output goes to the state of the D input at the time of the positive-going clock edge. The resulting output is shown in Figure 20(b).

RELATED PROBLEM

Determine the Q output for the D flip-flop if the D input in Figure 20(a) is inverted.

THE EDGE-TRIGGERED J-K FLIP-FLOP The J and K inputs of the **J-K flip-flop** are synchronous inputs because data on these inputs are transferred to the flip-flop's output only on the triggering edge of the clock pulse. When J is HIGH and K is LOW, the Q output goes HIGH on the triggering edge of the clock pulse, and the flip-flop is SET. When J is LOW and K is HIGH, the Q output goes LOW on the triggering edge of the clock pulse, and the flip-flop is RESET. When both J and K are LOW, the output does not change from its prior state. When J and K are both HIGH, the flip-flop changes state on the triggering edge of the clock. This is called the **toggle** mode.

In the toggle mode, a J-K flip-flop changes state on every clock pulse.

This basic operation of a positive edge-triggered flip-flop is illustrated in Figure 21, and Table 3 is the truth table for this type of flip-flop. Remember, *the flip-flop cannot change state except on the triggering edge of a clock pulse*. The J and K inputs can be changed at any time when the clock input is LOW or HIGH (except for a very short interval around the triggering transition of the clock) without affecting the output.

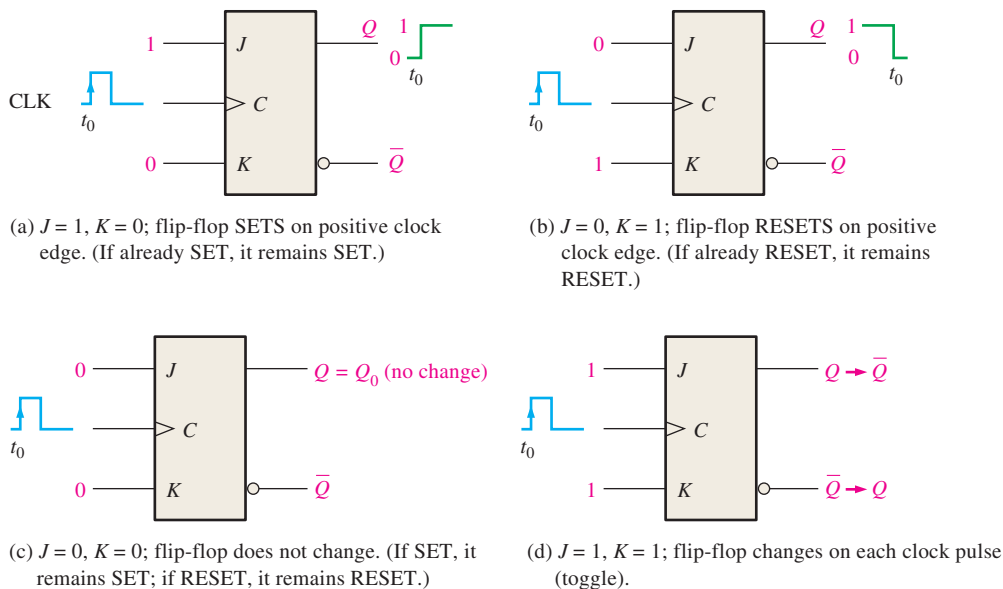


FIGURE 21 Operation of a positive edge-triggered J-K flip-flop.

Table 3 • Truth table for a positive edge-triggered J-K flip-flop.					
INPUTS			OUTPUTS		COMMENTS
J	K	CLK	Q	\bar{Q}	
0	0	↑	Q_0	\bar{Q}_0	No change
0	1	↑	0	1	RESET
1	0	↑	1	0	SET
1	1	↑	\bar{Q}_0	Q_0	Toggle

↑ = clock transition LOW to HIGH
 Q_0 = output level prior to clock transition

The operation and truth table for a negative edge-triggered J-K flip-flop are the same as those for a positive edge-triggered device except that the falling edge of the clock pulse is the triggering edge.

EXAMPLE 6

The waveforms in Figure 22(a) are applied to the J , K , and clock inputs as indicated. Determine the Q output, assuming that the flip-flop is initially RESET.

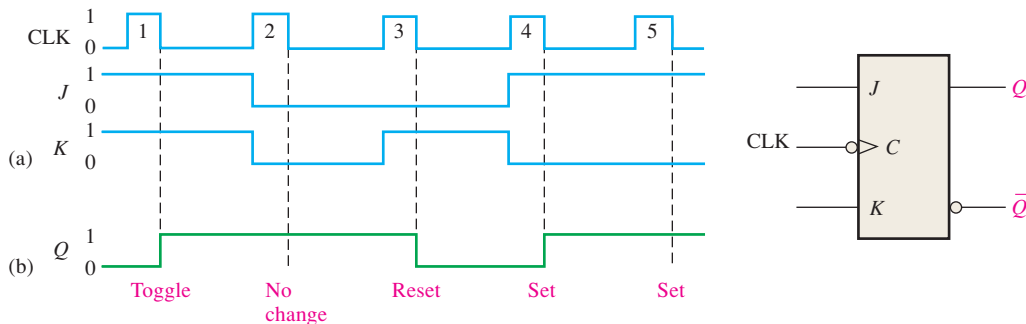


FIGURE 22

SOLUTION

Since this is a negative edge-triggered flip-flop, as indicated by the “bubble” at the clock input, the Q output will change only on the negative-going edge of the clock pulse.

1. At the first clock pulse, both J and K are HIGH; and because this is a toggle condition, Q goes HIGH.
2. At clock pulse 2, a no-change condition exists on the inputs, keeping Q at a HIGH level.
3. When clock pulse 3 occurs, J is LOW and K is HIGH, resulting in a RESET condition; Q goes LOW.
4. At clock pulse 4, J is HIGH and K is LOW, resulting in a SET condition; Q goes HIGH.
5. A SET condition still exists on J and K when clock pulse 5 occurs, so Q will remain HIGH.

The resulting Q waveform is indicated in Figure 22(b).

RELATED PROBLEM

Determine the Q output of the J-K flip-flop if the J and K inputs in Figure 22(a) are inverted.

EXAMPLE 7

Determine the Q and \bar{Q} output waveforms of the flip-flop in Figure 23 for the J , K , and CLK inputs in Figure 24(a). Assume that the positive edge-triggered flip-flop is initially RESET.

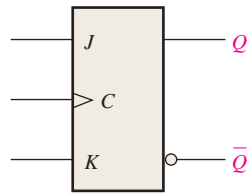


FIGURE 23

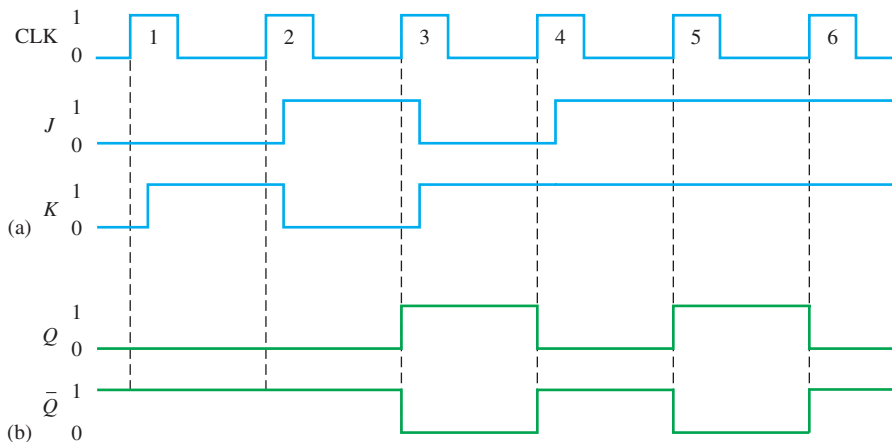


FIGURE 24

SOLUTION

1. At clock pulse 1, J is LOW and K is LOW, so Q does not change.
2. At clock pulse 2, J is LOW and K is HIGH, so Q remains LOW (RESET).
3. At clock pulse 3, J is HIGH and K is LOW, so Q goes HIGH (SET).
4. At clock pulse 4, J is LOW and K is HIGH, so Q goes LOW (RESET).
5. At clock pulse 5, J is HIGH and K is HIGH, so Q toggles HIGH (SET).
6. At clock pulse 6, J is HIGH and K is HIGH, so Q toggles LOW.

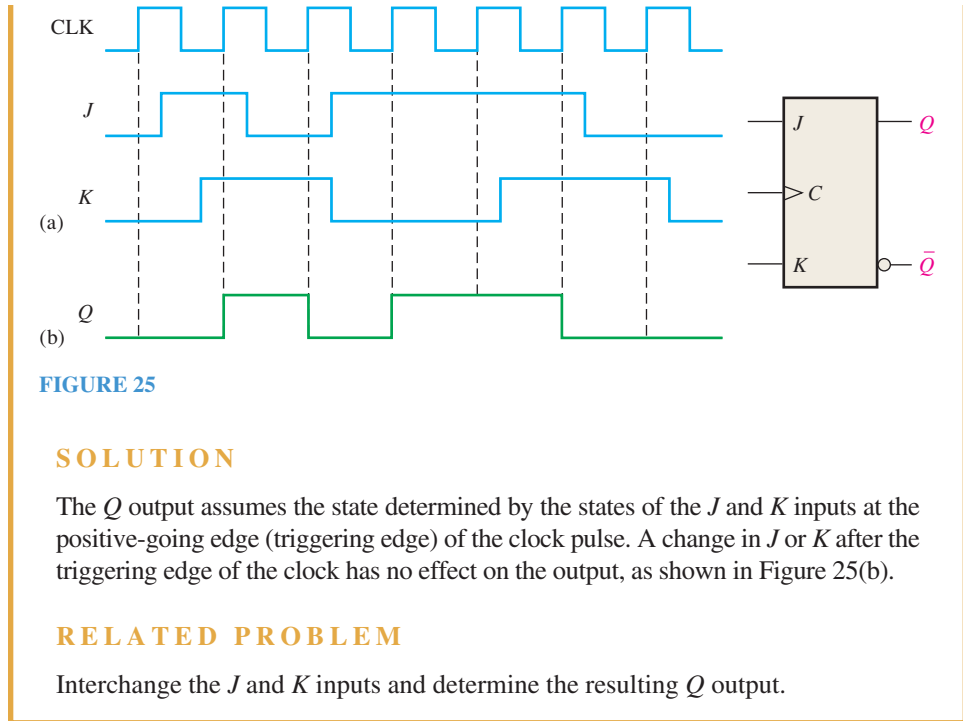
Once Q is determined, \bar{Q} is easily found since it is simply the complement of Q . The resulting waveforms for Q and \bar{Q} are shown in Figure 24(b) for the input waveforms in part (a).

RELATED PROBLEM

Determine Q and \bar{Q} for the J and K inputs in Figure 24(a) if the flip-flop is a negative edge-triggered device.

EXAMPLE 8

The waveforms in Figure 25(a) are applied to the flip-flop as shown. Determine the Q output, starting in the RESET state.



An active preset input makes the Q output HIGH (SET).

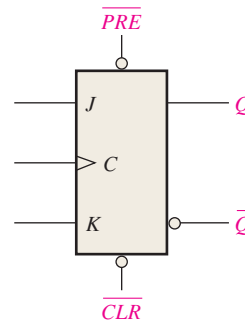
An active clear input makes the Q output LOW (RESET).

Asynchronous Preset and Clear Inputs

For the flip-flops just discussed, the D and J - K inputs are called *synchronous inputs* because data on these inputs are transferred to the flip-flop's output only on the triggering edge of the clock pulse; that is, the data are transferred synchronously with the clock.

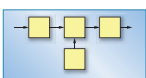
Most flip-flops also have **asynchronous** inputs. These are inputs that affect the state of the flip-flop *independent of the clock*. They are normally called **preset** (PRE) and **clear** (CLR), or *direct set* (S_D) and *direct reset* (R_D). An active level on the preset input will set the flip-flop, and an active level on the clear input will reset it. A logic symbol for a J-K flip-flop with preset and clear inputs is shown in Figure 26. These inputs are active-LOW, as indicated by the bubbles. These preset and clear inputs must both be kept HIGH for synchronous operation. In normal operation, preset and clear would not be LOW at the same time.

FIGURE 26 Logic symbol for a J-K flip-flop with active-LOW preset and clear inputs.



All logic operations that are performed with hardware can also be implemented in software. For example, the operation of a J-K flip-flop can be performed with specific computer instructions. If two bits were used to represent the J and K inputs, the computer would do nothing for 00, a data bit representing the Q output would be set (1) for 10, the Q data bit would be cleared (0) for 01, and the Q data bit would be complemented for 11. Although it may be unusual to use a computer to simulate a flip-flop, the point is that all hardware operations can be simulated using software.

SYSTEM NOTE



EXAMPLE 9

For the positive edge-triggered D flip-flop with preset and clear inputs in Figure 27, determine the Q output for the inputs shown in the timing diagram in part (a) if Q is initially LOW.

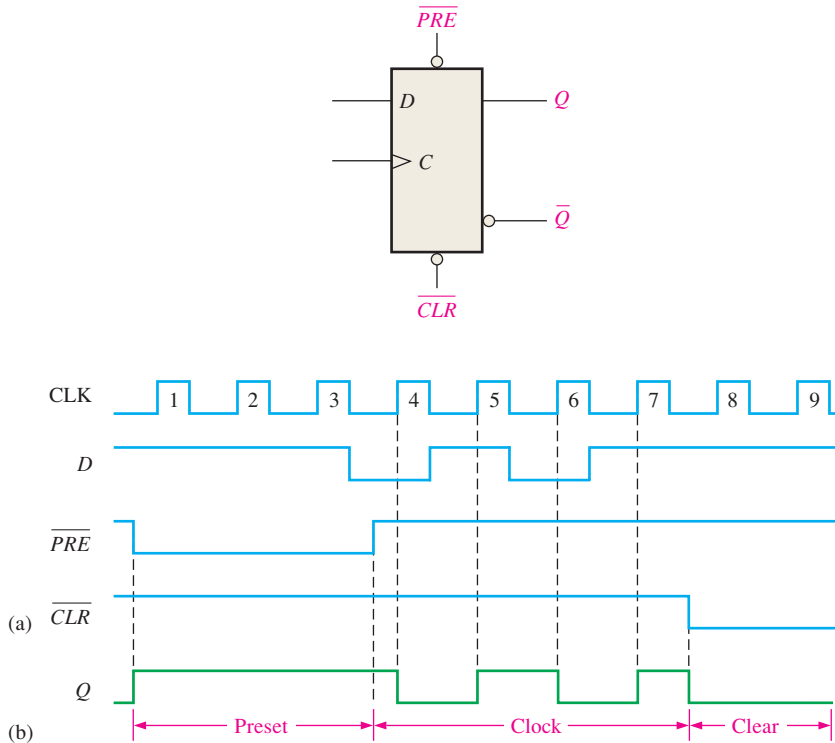


FIGURE 27 Open file F06-27 to verify the operation.

SOLUTION

1. During clock pulses 1, 2, and 3, the preset (\overline{PRE}) is LOW, keeping the flip-flop SET regardless of the synchronous D input.
2. For clock pulses 4, 5, 6, and 7, the output follows the input on the triggering edge of the clock pulse because both \overline{PRE} and \overline{CLR} are HIGH.
3. For clock pulses 8 and 9, the clear (\overline{CLR}) input is LOW, keeping the flip-flop RESET regardless of the synchronous inputs.

The resulting Q output is shown in Figure 27(b).

RELATED PROBLEM

If you interchange the \overline{PRE} and \overline{CLR} waveforms in Figure 27(a), what will the Q output look like?



Frequency Division

One application of a flip-flop is dividing (reducing) the frequency of a periodic waveform. When a pulse waveform is applied to the clock input of a D or J-K flip-flop that is connected to toggle ($D = \overline{Q}$ or $J = K = 1$), the Q output is a square wave with one-half the frequency of the clock input. Thus, a single flip-flop can be applied as a divide-by-2 device, as is illustrated in Figure 28. As you can see, the flip-flop changes state on each triggering clock edge (positive edge-triggered in this case) for both a D and a J-K flip-flop. This results in an output that changes at half the frequency of the clock waveform.

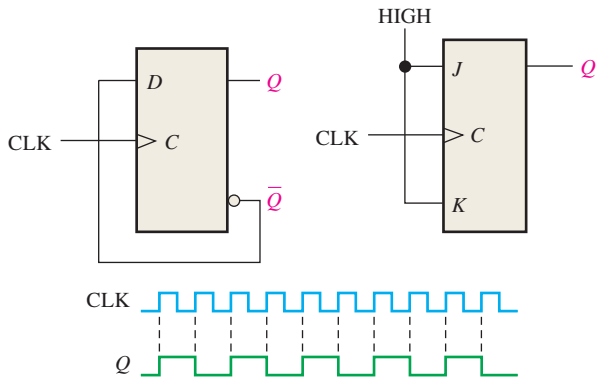


FIGURE 28 The D and J-K flip-flops as divide-by-2 devices. Q is one-half the frequency of CLK.

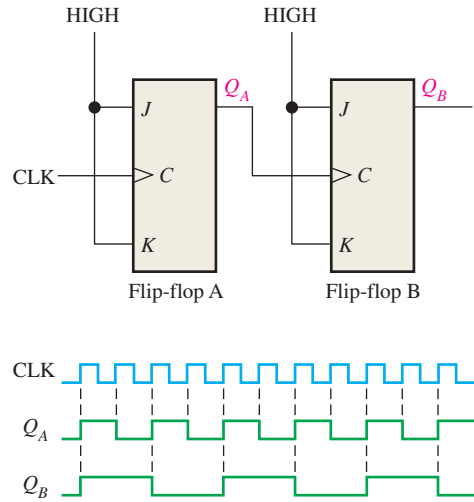


FIGURE 29 Example of two J-K flip-flops used to divide the clock frequency by 4. Q_A is one-half and Q_B is one-fourth the frequency of CLK.

Further division of a clock frequency can be achieved by using the output of one flip-flop as the clock input to a second flip-flop, as shown in Figure 29. The frequency of the Q_A output is divided by 2 by flip-flop B. The Q_B output is, therefore, one-fourth the frequency of the original clock input. Propagation delay times are not shown on the timing diagrams.

By connecting flip-flops in this way, a frequency division of 2^n is achieved, where n is the number of flip-flops. For example, three flip-flops divide the clock frequency by $2^3 = 8$; four flip-flops divide the clock frequency by $2^4 = 16$; and so on.

EXAMPLE 10

Develop the f_{out} waveform for the circuit in Figure 30 when an 8 kHz square wave input is applied to the clock input of flip-flop A.

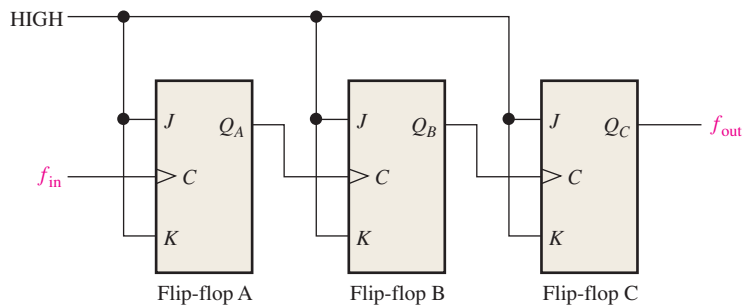


FIGURE 30

SOLUTION

The three flip-flops are connected to divide the input frequency by eight ($2^3 = 8$) and the f_{out} waveform is shown in Figure 31. Since these are positive edge-triggered flip-flops, the outputs change on the positive-going clock edge. There is one output pulse for every eight input pulses, so the output frequency is 1 kHz. Waveforms of Q_A and Q_B are also shown.

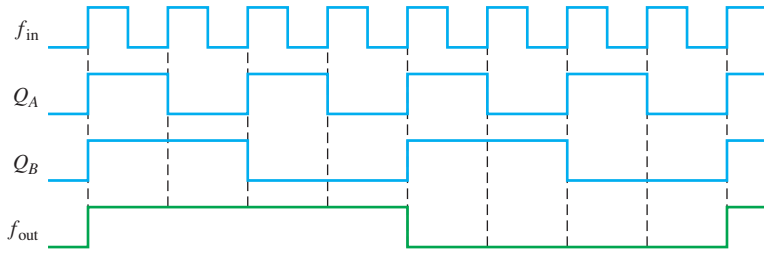


FIGURE 31

RELATED PROBLEM

How many flip-flops are required to divide a frequency by thirty-two?

Counting

Another important application of flip-flops is in digital counters. The concept is illustrated in Figure 32. Negative edge-triggered J-K flip-flops are used for illustration. Both flip-flops are initially RESET. Flip-flop A toggles on the negative-going transition of each clock pulse. The Q output of flip-flop A clocks flip-flop B, so each time Q_A makes a HIGH-to-LOW transition, flip-flop B toggles. The resulting Q_A and Q_B waveforms are shown in the figure.

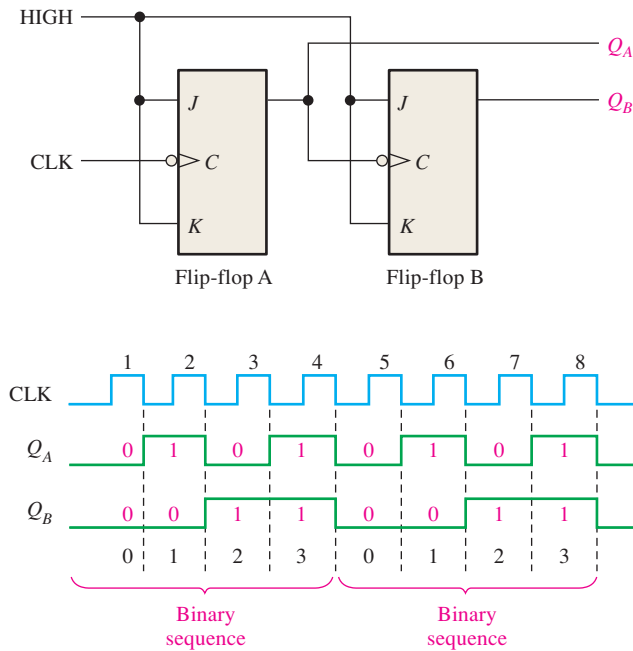


FIGURE 32 Flip-flops used to generate a binary count sequence. Two repetitions (00, 01, 10, 11) are shown.

Observe the sequence of Q_A and Q_B in Figure 32. Prior to clock pulse 1, $Q_A = 0$ and $Q_B = 0$; after clock pulse 1, $Q_A = 1$ and $Q_B = 0$; after clock pulse 2, $Q_A = 0$ and $Q_B = 1$; and after clock pulse 3, $Q_A = 1$ and $Q_B = 1$. If we take Q_A as the least significant bit, a 2-bit sequence is produced as the flip-flops are clocked. This binary sequence repeats every four clock pulses, as shown in the timing diagram of Figure 32. Thus, the flip-flops are counting in sequence from 0 to 3 (00, 01, 10, 11) and then recycling back to 0 to begin the sequence again.

EXAMPLE 11

Determine the output waveforms in relation to the clock for Q_A , Q_B , and Q_C in the circuit of Figure 33 and show the binary sequence represented by these waveforms.

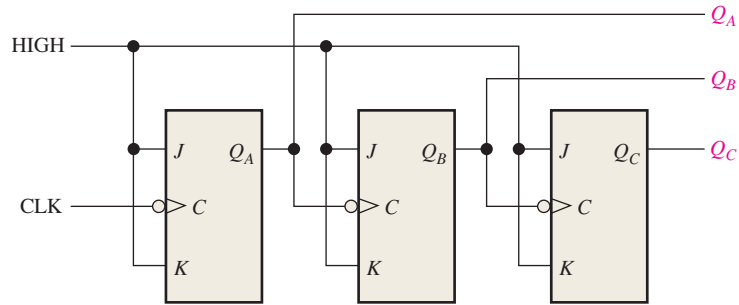


FIGURE 33

SOLUTION

The output timing diagram is shown in Figure 34. Notice that the outputs change on the negative-going edge of the clock pulses. The outputs go through the binary sequence 000, 001, 010, 011, 100, 101, 110, and 111 as indicated.

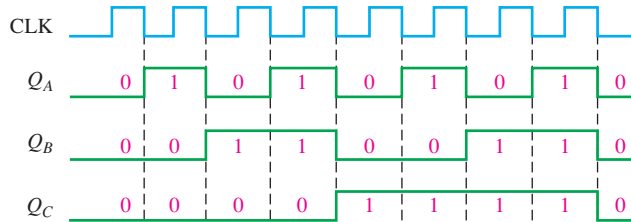
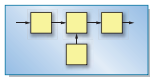


FIGURE 34

RELATED PROBLEM

How many flip-flops are required to produce a binary sequence representing decimal numbers 0 through 15?

SYSTEM EXAMPLE 1



TRAFFIC SIGNAL CONTROL SYSTEM, SEQUENTIAL LOGIC

Recall from Section 1 that the sequential logic is one of the component blocks of the traffic signal control system. The diagram in Figure 35 shows how two D flip-flops can be used to implement the Gray code counter. Outputs for the counter control logic provide the D inputs to the flip-flops, so they sequence through the proper states.

The D flip-flop transition table is shown in Table 4. A next-state table developed from the state diagram in Figure 2 is shown in Table 5.

THE COUNTER CONTROL LOGIC Using Tables 4 and 5, the conditions required for each flip-flop to go to the 1 state can be determined. For example, G_0 goes from 0 to 1 when the present state is 00 and the condition on input D_0 is $\bar{T}_L V_s$, as indicated

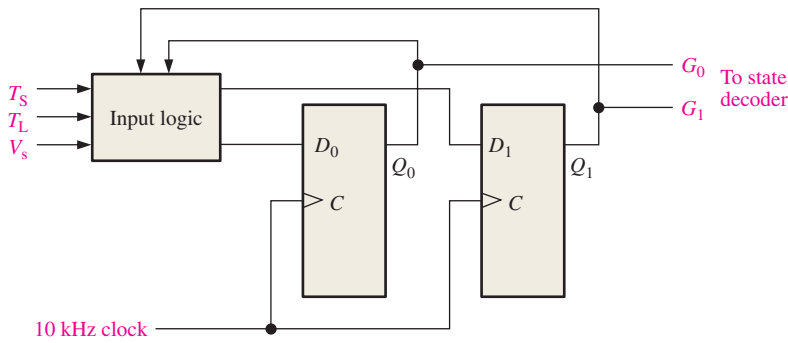


FIGURE 35 Sequential logic diagram with two D flip-flops used to implement a counter.

Table 4 • D flip-flop transition table.

OUTPUT TRANSITIONS		FLIP-FLOP INPUT
Q_N	Q_{N+1}	D
0	→ 0	0
0	→ 1	1
1	→ 0	0
1	→ 1	1

Table 5 • Next-state table for the counter.

PRESENT STATE		NEXT STATE		INPUT CONDITIONS	FF INPUTS	
Q_1	Q_0	Q_1	Q_0		D_1	D_0
0	0	0	0	$T_L + \bar{V}_s$	0	0
0	0	0	1	$\bar{T}_L V_s$	0	1
0	1	0	1	T_S	0	1
0	1	1	1	\bar{T}_S	1	1
1	1	1	1	$T_L V_s$	1	1
1	1	1	0	$\bar{T}_L + \bar{V}_s$	1	0
1	0	1	0	T_S	1	0
1	0	0	0	\bar{T}_S	0	0

on the second row of Table 5. D_0 must be a 1 to make G_0 go to a 1 or to remain a 1 on the next clock pulse. A Boolean expression describing the conditions that make D_0 a 1 is derived from Table 5 as follows, where $Q_1 = G_1$ and $Q_0 = G_0$:

$$D_0 = \bar{G}_1 \bar{G}_0 \bar{T}_L V_s + \bar{G}_1 G_0 T_S + \bar{G}_1 G_0 \bar{T}_S + G_1 G_0 T_L V_s$$

In the two middle terms, the T_S and the \bar{T}_S variables cancel, leaving the expression

$$D_0 = \bar{G}_1 \bar{G}_0 \bar{T}_L V_s + \bar{G}_1 G_0 + G_1 G_0 T_L V_s$$

It can be shown that the D_0 expression can be further simplified using the **Karnaugh map** method (See the website for coverage of the Karnaugh map method).

$$D_0 = \bar{G}_1 \bar{T}_L V_s + \bar{G}_1 G_0 + G_0 T_L V_s$$

Also, from Table 5, an expression for D_1 can be developed as follows where $Q_1 = G_1$ and $Q_0 = G_0$:

$$D_1 = \bar{G}_1 G_0 \bar{T}_S + G_1 G_0 T_L V_s + G_1 G_0 \bar{T}_L + G_1 G_0 \bar{V}_s + G_1 \bar{G}_0 T_S$$

It can be shown that the D_1 expression can be further simplified using Boolean and Karnaugh map methods.

$$D_1 = G_0 \bar{T}_S + G_1 T_S$$

Based on the minimized expressions for D_0 and D_1 , the complete sequential logic diagram is shown in Figure 36.

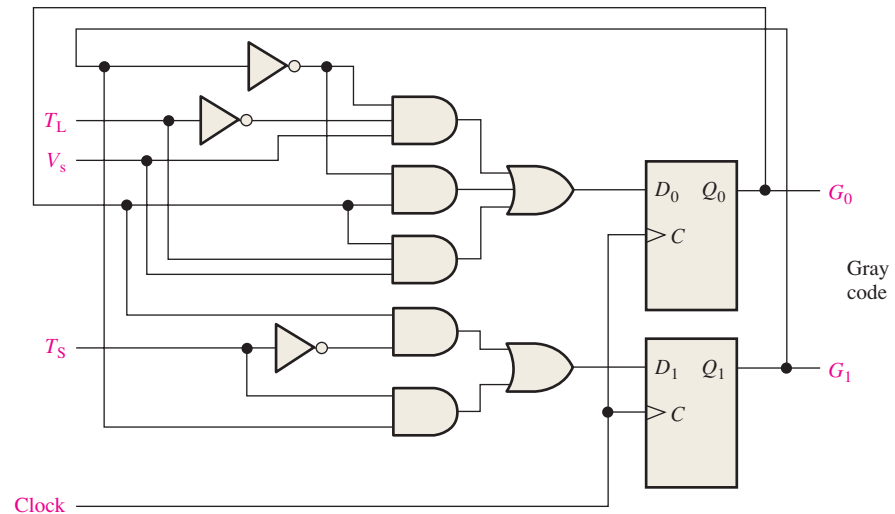


FIGURE 36 Complete diagram of the sequential logic.

SECTION 3 CHECKUP

- Describe the main difference between a gated D latch and an edge-triggered D flip-flop.
- How does a J-K flip-flop differ from a D flip-flop in its basic operation?
- Assume that the flip-flop in Figure 20 is negative edge-triggered. Describe the output waveform for the same CLK and D waveforms.
- How must a J-K flip-flop be connected to function as a divide-by-2 device?
- How many flip-flops are required to produce a divide-by-64 device?

4 FLIP-FLOP OPERATING CHARACTERISTICS

The performance, operating requirements, and limitations of flip-flops are specified by several operating characteristics or parameters found on the data sheet for the device. Generally, the specifications are applicable to all CMOS and bipolar (TTL) flip-flops.

After completing this section, you should be able to

- Define *propagation delay time*
- Explain the various propagation delay time specifications
- Define *set-up time* and discuss how it limits flip-flop operation
- Define *hold time* and discuss how it limits flip-flop operation
- Discuss the significance of maximum clock frequency
- Discuss the various pulse width specifications
- Define *power dissipation* and calculate its value for a specific device

Propagation Delay Times

A **propagation delay time** is the interval of time required after an input signal has been applied for the resulting output change to occur. Four categories of propagation delay times are important in the operation of a flip-flop:

1. Propagation delay t_{PLH} as measured from the triggering edge of the clock pulse to the LOW-to-HIGH transition of the output. This delay is illustrated in Figure 37(a).
2. Propagation delay t_{PHL} as measured from the triggering edge of the clock pulse to the HIGH-to-LOW transition of the output. This delay is illustrated in Figure 37(b).

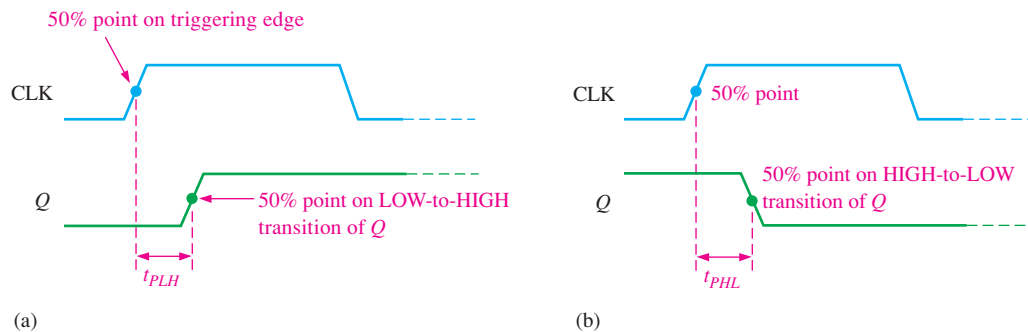


FIGURE 37 Propagation delays, clock to output.

3. Propagation delay t_{PLH} as measured from the leading edge of the preset input to the LOW-to-HIGH transition of the output. This delay is illustrated in Figure 38(a) for an active-LOW preset input.
4. Propagation delay t_{PHL} as measured from the leading edge of the clear input to the HIGH-to-LOW transition of the output. This delay is illustrated in Figure 38(b) for an active-LOW clear input.

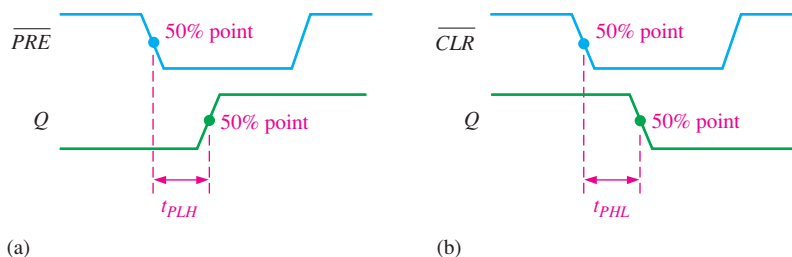


FIGURE 38 Propagation delays, preset input to output and clear input to output.

Set-up Time

The **set-up time** (t_s) is the minimum interval required for the logic levels to be maintained constantly on the inputs (J and K , or D) prior to the triggering edge of the clock pulse in order for the levels to be reliably clocked into the flip-flop. This interval is illustrated in Figure 39 for a D flip-flop.

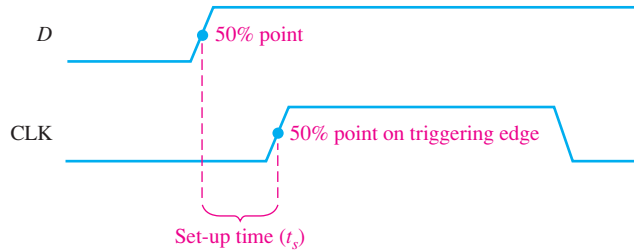


FIGURE 39 Set-up time (t_s). The logic level must be present on the D input for a time equal to or greater than t_s before the triggering edge of the clock pulse for reliable data entry.

Hold Time

The **hold time** (t_h) is the minimum interval required for the logic levels to remain on the inputs after the triggering edge of the clock pulse in order for the levels to be reliably clocked into the flip-flop. This is illustrated in Figure 40 for a D flip-flop.

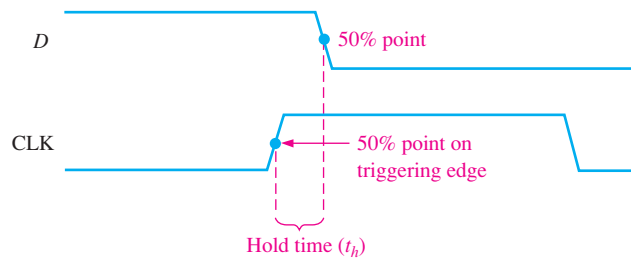


FIGURE 40 Hold time (t_h). The logic level must remain on the D input for a time equal to or greater than t_h after the triggering edge of the clock pulse for reliable data entry.



HANDS ON TIP

An advantage of CMOS is that it can operate over a wider range of dc supply voltages (typically 2 V to 6 V) than bipolar and, therefore, less expensive power supplies that do not have precise regulation can be used. Also, batteries can be used as secondary or primary sources for CMOS circuits. In addition, lower voltages mean that the IC dissipates less power. The drawback is that the performance of CMOS is degraded with lower supply voltages. For example, the guaranteed maximum clock frequency of a CMOS flip-flop is much less at $V_{CC} = 2$ V than at $V_{CC} = 6$ V.

Maximum Clock Frequency

The maximum clock frequency (f_{max}) is the highest rate at which a flip-flop can be reliably triggered. At clock frequencies above the maximum, the flip-flop would be unable to respond quickly enough, and its operation would be impaired.

Pulse Widths

Minimum pulse widths (t_{PW}) for reliable operation are usually specified by the manufacturer for the clock, preset, and clear inputs. Typically, the clock is specified by its minimum HIGH time and its minimum LOW time.

Power Dissipation

The **power dissipation** of any digital circuit is the total power consumption of the device. For example, if the flip-flop operates on a +5 V dc source and draws 5 mA of current, the power dissipation is

$$P = V_{CC} \times I_{CC} = 5 \text{ V} \times 5 \text{ mA} = 25 \text{ mW}$$

The power dissipation is very important in most applications in which the capacity of the dc supply is a concern. As an example, let's assume that you have a digital system that requires a total of ten flip-flops, and each flip-flop dissipates 25 mW of power. The total power requirement is

$$P_T = 10 \times 25 \text{ mW} = 250 \text{ mW} = 0.25 \text{ W}$$

This tells you the output capacity required of the dc supply. If the flip-flops operate on +5 V dc, then the amount of current that the supply must provide is

$$I = \frac{250 \text{ mW}}{5 \text{ V}} = 50 \text{ mA}$$

You must use a +5 V dc supply that is capable of providing at least 50 mA of current.

SECTION 4 CHECKUP

- Define the following:
 - set-up time
 - hold time
- Assume one flip-flop has a $t_{PHL} = 17 \text{ ns}$ and another has a $t_{PHL} = 40 \text{ ns}$. Which flip-flop can be operated at the highest frequency?

5 TIMERS

Two basic types of timing circuits commonly used in electronic systems are the **one-shot** or **monostable** multivibrator and the **free-running** or **astable** multivibrator. The **one-shot** is a device with only one stable state. A one-shot is normally in its stable state and will change to its unstable state only when triggered. Once it is triggered, the one-shot remains in its unstable state for a predetermined length of time and then automatically returns to its stable state. The time that the device stays in its unstable state determines the pulse width of its output. The **astable** multivibrator has no stable state and changes back and forth between its two unstable states at a specified rate.

After completing this section, you should be able to

- Describe the basic operation of a one-shot
- Explain how a nonretriggerable one-shot works
- Explain how a retriggerable one-shot works
- Set up specific one-shots to obtain a given output pulse width
- Describe the basic elements of a 555 timer
- Set up a 555 timer as a one-shot
- Set up a 555 timer as an astable multivibrator

Figure 41 shows the block diagram of a one-shot (monostable multivibrator) that is composed of a logic section and a timing section. When a pulse is applied to the **trigger** input, the output of the one-shot, Q , goes HIGH.

The timing section consists of a resistor and a capacitor. The capacitor immediately begins to charge through R . The rate at which it charges is determined by the RC time constant (the product of the values of the resistor and capacitor). When the capacitor charges to a certain voltage level, the output of the one-shot goes back LOW. The duration of the output pulse, t_{PW} , is proportional to the RC time constant by the equation $t_{PW} = kRC$, where k is a constant of proportionality and depends on the particular device.

A one-shot produces a single pulse each time it is triggered.

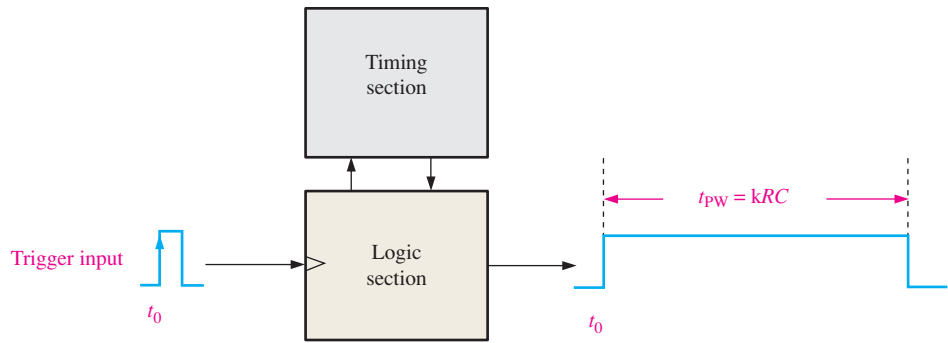


FIGURE 41 Block diagram of a one-shot.

A typical one-shot logic symbol is shown in Figure 42(a), and the same symbol with an external R and C is shown in Figure 42(b). The two basic types of one-shots are nonretriggerable and retriggerable.

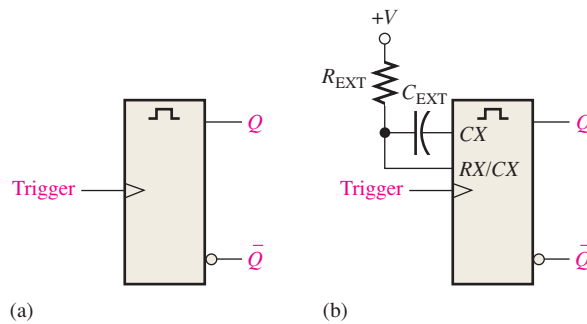


FIGURE 42 Basic one-shot logic symbols. CX and RX stand for external components.

A nonretriggerable one-shot will not respond to any additional trigger pulses from the time it is triggered into its unstable state until it returns to its stable state. In other words, it will ignore any trigger pulses occurring before it times out. The time that the one-shot remains in its unstable state is the pulse width of the output.

Figure 43 shows the nonretriggerable one-shot being triggered at intervals greater than its pulse width and at intervals less than the pulse width. Notice that in the second case, the additional pulses are ignored.

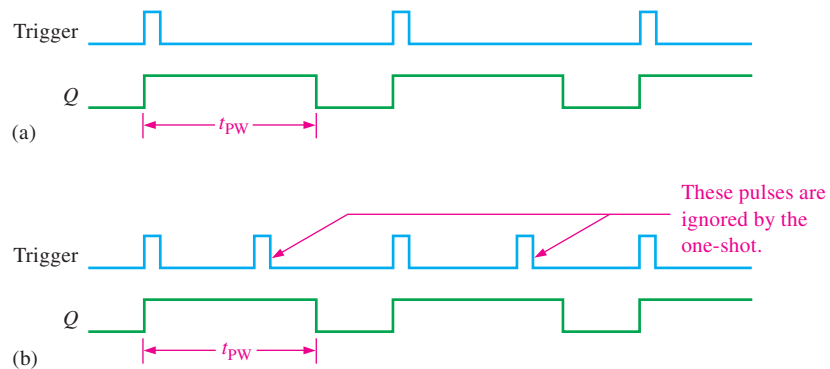


FIGURE 43 Nonretriggerable one-shot action.

A retriggerable one-shot can be triggered before it times out. The result of retriggering is an extension of the pulse width as illustrated in Figure 44.



HANDS ON TIP

In normal operation, a one-shot produces only a single pulse, which can be difficult to measure on an oscilloscope because the pulse does not occur regularly. To obtain a stable display for test purposes, it is useful to trigger the one-shot from a pulse generator that is set to a longer period than the expected pulse width and trigger the oscilloscope from the same pulse. For very long pulses, either store the waveform using a digital storage oscilloscope or shorten the time constant by some known factor. For example, replace a $1000\ \mu\text{F}$ capacitor with a $1\ \mu\text{F}$ capacitor to shorten the time by a factor of 1000. A faster pulse is easier to see and measure in an oscilloscope.

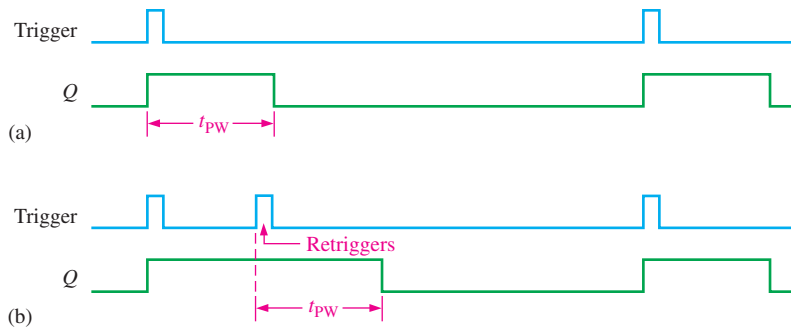


FIGURE 44 Retriggerable one-shot action.

Specific One-Shots

Two specific IC one-shots are the 74121, which is nontriggerable and the 74xx122, which is retriggerable. The output pulse width formula for the 74121 is

$$t_{PW} = 0.7RC_{EXT} \tag{1}$$

R can be either the internal resistor (2 kΩ) or the external resistor (R_{EXT}) with a selected value; 0.7 is the constant of proportionality, k .

The pulse width formula for the 74xx122 is

$$t_{PW} = 0.32RC_{EXT} \left(1 + \frac{0.7}{R} \right) \tag{2}$$

R can be either the internal resistor (10 kΩ) or the external resistor (R_{EXT}) with a selected value; $0.32 (1 + 0.7/R)$ is the constant of proportionality, k . Refer to manufacturer’s data sheet for connection details.

SYSTEM EXAMPLE 2

A SEQUENTIAL TIMER

One practical one-shot application is a sequential timer that can be used to illuminate a series of lights. This type of circuit can be used, for example, in a lane change directional indicator for highway construction projects, as shown in Figure 45, or in sequential turn signals on automobiles.

Figure 46 shows three one-shots connected as a sequential timer. The labels RX/CX and CX are for the external connection of resistance and capacitance. This particular circuit produces a sequence of three 1 s pulses. The first one-shot is triggered by a switch closure or a low-frequency pulse input, producing a 1 s output pulse. When the first one-shot (OS 1) times out and the a 1 s pulse goes LOW, the second one-shot (OS 2) is triggered, also producing a 1 s output pulse. When this second pulse goes LOW, the third one-shot (OS 3) is triggered and the third 1 s pulse is produced. The output timing is illustrated in the figure. Variations of this basic arrangement can be used to produce a variety of timed outputs, such as the one shown in Figure 45, which would require eight one-shots. (A single one-shot controls the arrowhead when all five lights are on at the same time.) The time for each light is set with the timing components.

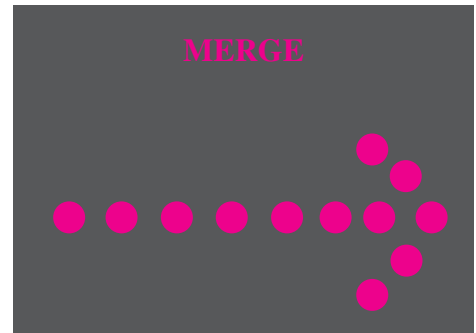
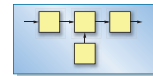


FIGURE 45 Example of a timing application.

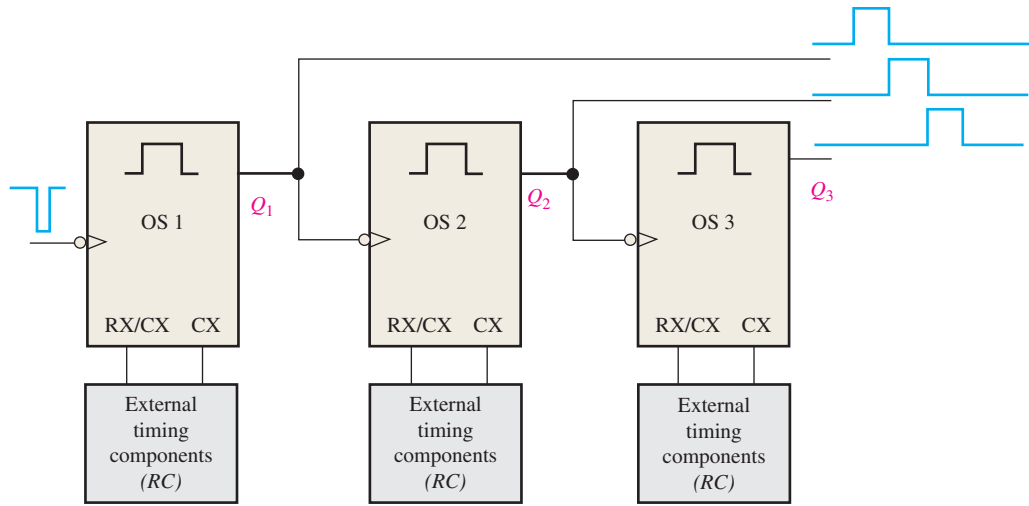


FIGURE 46 Sequential timer.

The 555 Timer as a One-Shot

The 555 timer is a versatile and widely used IC device because it can be configured in two different modes as either a monostable multivibrator (one-shot) or as an astable multivibrator (pulse oscillator).

An external resistor and capacitor connected as shown in Figure 47 are used to set up the 555 timer as a nonretriggerable one-shot. The pulse width of the output is determined by the time constant of R_1 and C_1 according to the following formula:

$$t_{PW} = 1.1R_1C_1 \quad (3)$$

The control voltage input is not used and is connected to a decoupling capacitor C_2 to prevent noise from affecting the trigger and threshold levels.

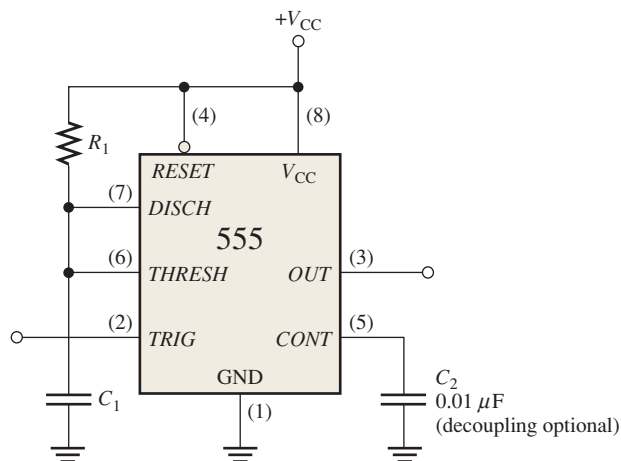


FIGURE 47 The 555 timer connected as a one-shot.

Before a trigger pulse is applied to the one-shot, the output is LOW and an internal transistor is *on*, keeping C_1 discharged. When a negative-going trigger pulse is applied to begin the pulse, the output goes HIGH and the internal transistor turns *off*, allowing capacitor C_1 to begin charging through R_1 . When C_1 charges to one-third of the supply voltage ($1/3 V_{CC}$), the output goes back LOW and the internal transistor turns *on* immediately, discharging C_1 . The charging rate of C_1 determines how long the output is HIGH.

EXAMPLE 12

What is the output pulse width for a 555 monostable circuit with $R_1 = 2.2 \text{ k}\Omega$ and $C_1 = 0.01 \text{ }\mu\text{F}$?

SOLUTION

From Equation 3 the pulse width is

$$t_{PW} = 1.1R_1C_1 = 1.1(2.2 \text{ k}\Omega)(0.01 \text{ }\mu\text{F}) = \mathbf{24.2 \text{ }\mu\text{s}}$$

RELATED PROBLEM

For $C_1 = 0.01 \text{ }\mu\text{F}$, determine the value of R_1 for a pulse width of 1 ms.

The 555 Timer as an Astable Multivibrator

An astable multivibrator is a device that has no stable states; it changes back and forth (oscillates) between two unstable states without any external triggering. The resulting output is typically a square wave that is used as a clock signal in many types of sequential logic circuits. Astable multivibrators are also known as pulse **oscillators**.

A 555 timer connected to operate as an astable multivibrator is shown in Figure 48. Notice that the threshold input (*THRESH*) is now connected to the trigger input (*TRIG*). The external components R_1 , R_2 , and C_1 form the timing network that sets the frequency of oscillation. The $0.01 \text{ }\mu\text{F}$ capacitor, C_2 , connected to the control (*CONT*) input is strictly for decoupling and has no effect on the operation; in some cases it can be left off.

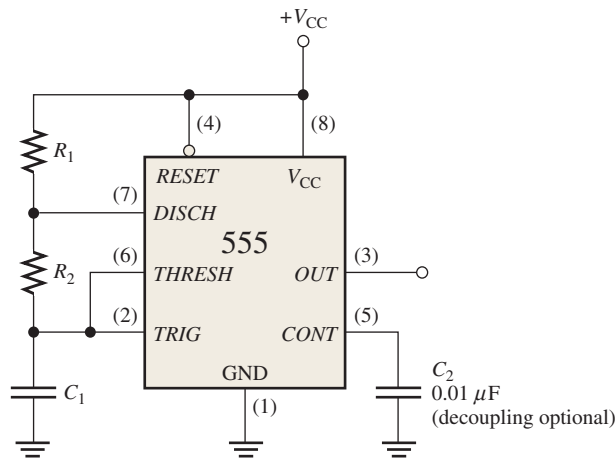
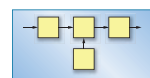


FIGURE 48 The 555 timer connected as an astable multivibrator (oscillator).

Initially, when the power is turned on, the capacitor (C_1) is uncharged and thus the trigger voltage is at 0 V. This causes the internal transistor to be *off*. Now, C_1 begins charging through R_1 and R_2 . When the capacitor voltage reaches $\frac{2}{3} V_{CC}$, the internal transistor

All computers require a timing source to provide accurate clock waveforms. The timing section controls all system timing and is responsible for the proper operation of the system hardware. The timing section usually consists of a crystal-controlled oscillator and counters for frequency division. Using a high-frequency oscillator divided down to a lower frequency provides for greater accuracy and frequency stability.

SYSTEM NOTE



is turned *on*, creating a discharge path for the capacitor through R_2 and the transistor. The capacitor now begins to discharge, and at the point where the capacitor discharges down to $\frac{1}{3} V_{CC}$, the transistor turns *off*. Another charging cycle begins, and the entire process repeats. The result is a rectangular wave output whose duty cycle (ratio of pulse width to period) depends on the values of R_1 and R_2 . The frequency of oscillation is given by the following formula, or it can be found using the graph in Figure 49.

$$f = \frac{1.44}{(R_1 + 2R_2)C_1} \quad (4)$$

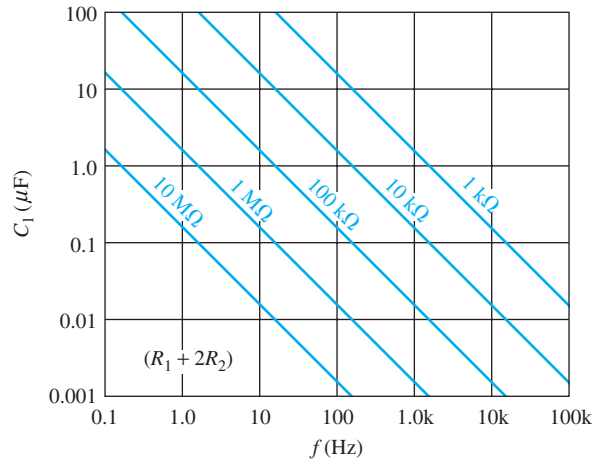


FIGURE 49 Frequency of oscillation as a function of C_1 and $R_1 + 2R_2$. The sloped lines are values of $R_1 + 2R_2$.

By selecting R_1 and R_2 , the duty cycle of the output can be adjusted. Since C_1 charges through $R_1 + R_2$ and discharges only through R_2 , duty cycles approaching a minimum of 50 percent can be achieved if $R_2 \gg R_1$ so that the charging and discharging times are approximately equal.

An expression for the duty cycle is developed as follows. The time that the output is HIGH (t_H) is how long it takes C_1 to charge from $\frac{1}{3} V_{CC}$ to $\frac{2}{3} V_{CC}$. It is expressed as

$$t_H = 0.7(R_1 + R_2)C_1 \quad (5)$$

The time that the output is LOW (t_L) is how long it takes C_1 to discharge from $\frac{1}{3} V_{CC}$ to $\frac{2}{3} V_{CC}$. It is expressed as

$$t_L = 0.7R_2C_1 \quad (6)$$

The period, T , of the output waveform is the sum of t_H and t_L . This is the reciprocal of f in Equation 4.

$$T = t_H + t_L = 0.7(R_1 + 2R_2)C_1$$

Finally, the duty cycle is

$$\text{Duty cycle} = \frac{t_H}{T} = \frac{t_H}{t_H + t_L}$$

$$\text{Duty cycle} = \left(\frac{R_1 + R_2}{R_1 + 2R_2} \right) 100\% \quad (7)$$

EXAMPLE 13

A 555 timer configured to run in the astable mode (pulse oscillator) is shown in Figure 50. Determine the frequency of the output and the duty cycle.

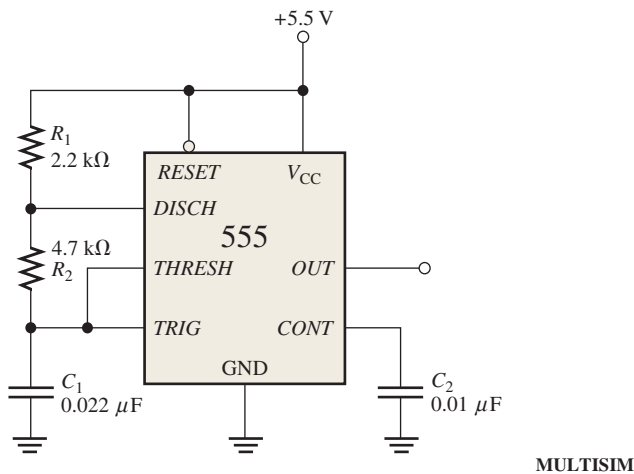


FIGURE 50 Open file F06-50 to verify operation.

MULTISIM

**SOLUTION**

Use Equations 4 and 7.

$$f = \frac{1.44}{(R_1 + 2R_2)C_1} = \frac{1.44}{(2.2 \text{ k}\Omega + 9.4 \text{ k}\Omega)0.022 \text{ }\mu\text{F}} = \mathbf{5.64 \text{ kHz}}$$

$$\text{Duty cycle} = \left(\frac{R_1 + R_2}{R_1 + 2R_2} \right) 100\% = \left(\frac{2.2 \text{ k}\Omega + 4.7 \text{ k}\Omega}{2.2 \text{ k}\Omega + 9.4 \text{ k}\Omega} \right) 100\% = \mathbf{59.5\%}$$

RELATED PROBLEM

What value of R_2 is required to increase the frequency to 10 kHz?

SECTION 5 CHECKUP

- Describe the difference between a nonretriggerable and a retriggerable one-shot.
- How is the output pulse width set in most IC one-shots?
- What is the pulse width of a 555 timer one-shot when $C = 1 \text{ }\mu\text{F}$ and $R = 10 \text{ k}\Omega$?
- Explain the difference in operation between an astable multivibrator and a monostable multivibrator.
- For a certain astable multivibrator, $t_H = 15 \text{ ms}$ and $T = 20 \text{ ms}$. What is the duty cycle of the output?

6 BISTABLE LOGIC WITH VHDL AND VERILOG

As you know, any logic function must be described with a hardware description language (HDL) in preparation for programming it into a PLD. In this section, the S-R latch and the D and J-K flip-flops are described in both VHDL and Verilog. Keep in mind that in both languages there is more than one way to describe a given function. Refer to the VHDL or Verilog tutorials on the website.

After completing this section, you should be able to

- Use VHDL and Verilog to describe several types of latches and flip-flops
- Specify variable arrays in both VHDL and Verilog
- Use comment lines

S-R Latch

The logic diagram for the programming model of an S-R latch is shown in Figure 51. The latch is described using VHDL and Verilog.

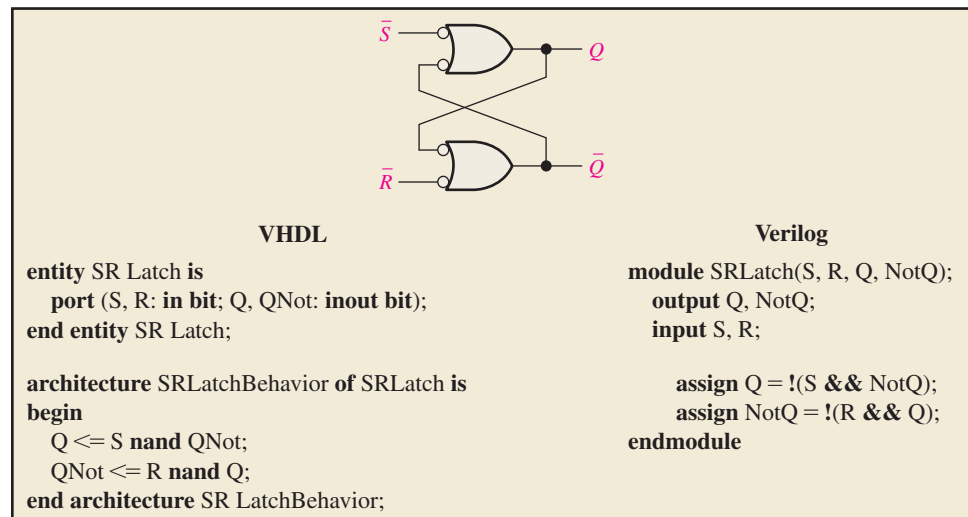


FIGURE 51 Logic diagram and VHDL and Verilog programs for the S-R latch. The symbol && in the Verilog program means AND and the symbol ! means NOT.

D Flip-Flop

The logic diagram for a D flip-flop is shown in Figure 52. The flip-flop is described using VHDL and Verilog. The pulse transition detector converts the clock pulse (CLK) to a short spike (Clock) on its triggering edge. The VHDL program includes this triggering with the **if rising_edge** term and in the Verilog program with the **@(posedge Clock)** term.

J-K Flip-Flop

The logic diagram for a J-K flip-flop is shown in Figure 53. The flip-flop is described using VHDL and Verilog. The pulse transition detector converts the clock pulse (CLK) to a short spike (Clock) on its triggering edge. The VHDL program includes this triggering with the **if rising_edge** term and in the Verilog program with the **@(posedge Clock)** term.

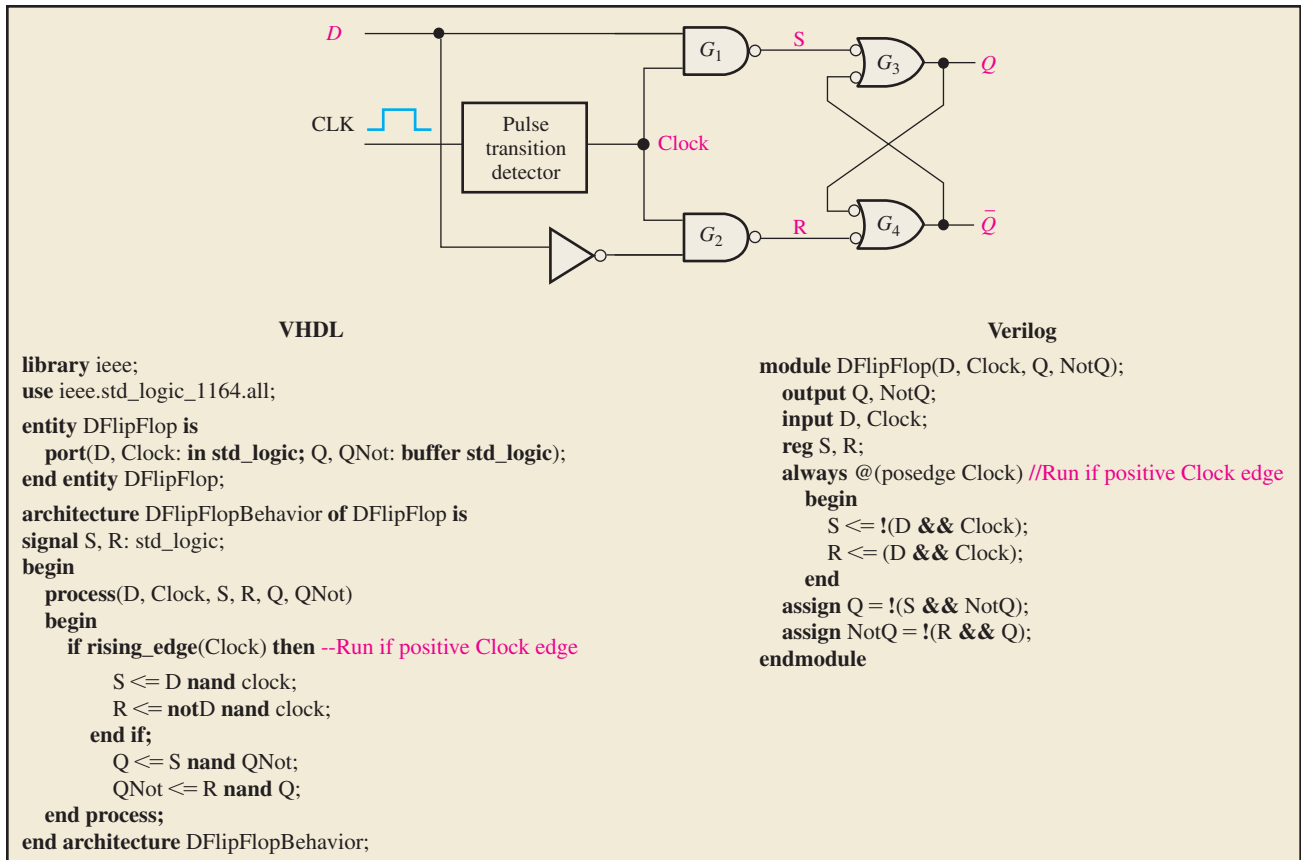


FIGURE 52 Logic diagram and VHDL and Verilog programs for the D flip-flop.

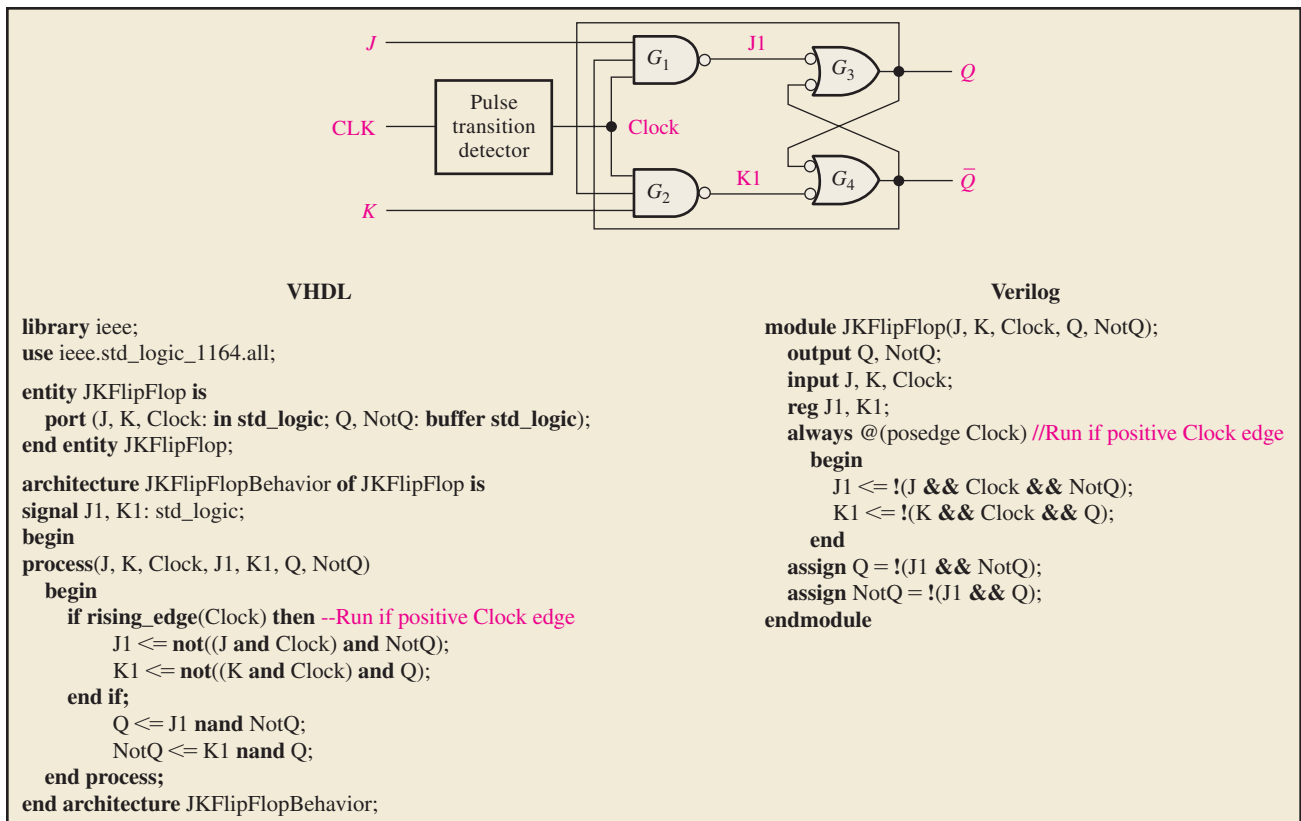


FIGURE 53 Logic diagram and VHDL and Verilog programs for the J-K flip-flop.

SECTION 6 CHECKUP

1. Explain how VHDL specifies an edge-triggered operation.
2. Explain how Verilog specifies an edge-triggered operation.
3. Write the lines of code in both VHDL and Verilog to specify a negative edge-triggered operation.
4. Define each of the following logical Verilog operators: `!`, `||`, and `&&`.

7 TRAFFIC SIGNAL CONTROL SYSTEM WITH VHDL AND VERILOG

The traffic signal control system presented in Section 1 can be implemented in a PLD by first describing it with VHDL or Verilog. In this section, you will see how each block in the system is coded and is used as a component to describe the complete system. As for any VHDL or Verilog coverage, it will be helpful to refer to the tutorials on the website.

After completing this section, you should be able to

- Discuss the general approach to programming a system for implementation in a PLD
- See how the VHDL and Verilog programs are used to implement the system

The traffic signal control system block diagram from Section 1 is repeated in Figure 54. The system consists of three blocks: Timing circuits, Sequential logic, and Combinational logic. There is a small difference in that the system clock now also goes to the timing circuits because of the way in which the timing circuits are implemented.

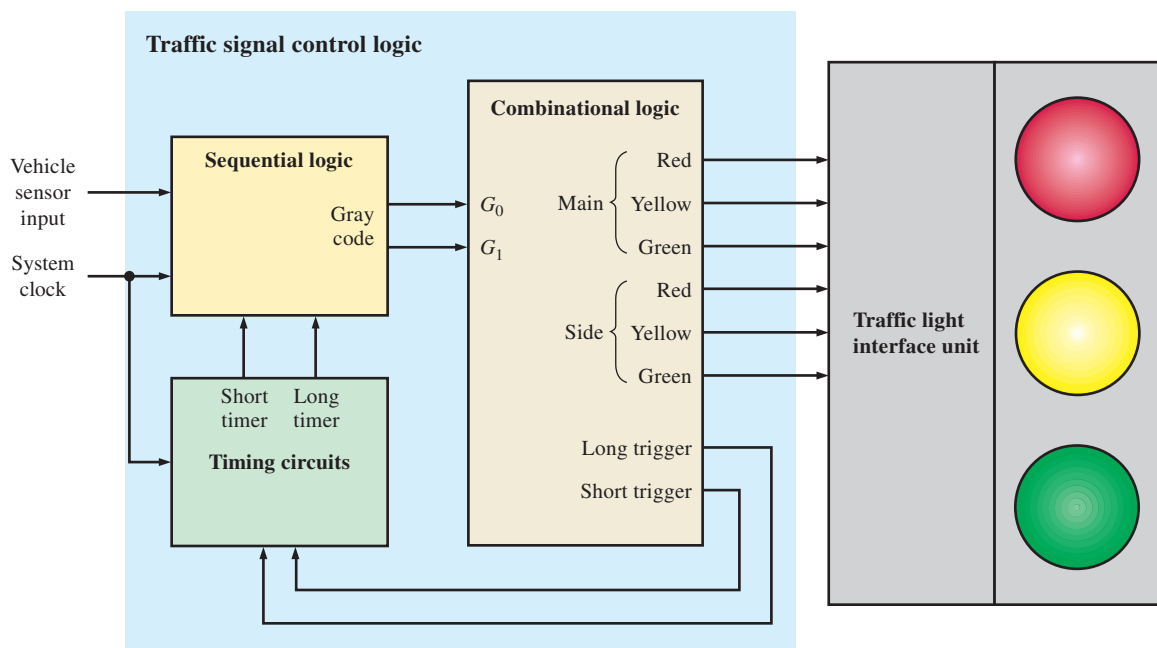


FIGURE 54 Block diagram of the traffic signal control system.

A programming model for the traffic signal control system is shown in Figure 55, where all the input and output labels are given. Notice that the Timing circuits block is split into two parts; the Frequency divider and the Timer circuits; and the Combinational logic block is divided into the State decoder and two logic sections (Light output logic and Trigger logic). This model will be used to develop VHDL and Verilog programs for the system.

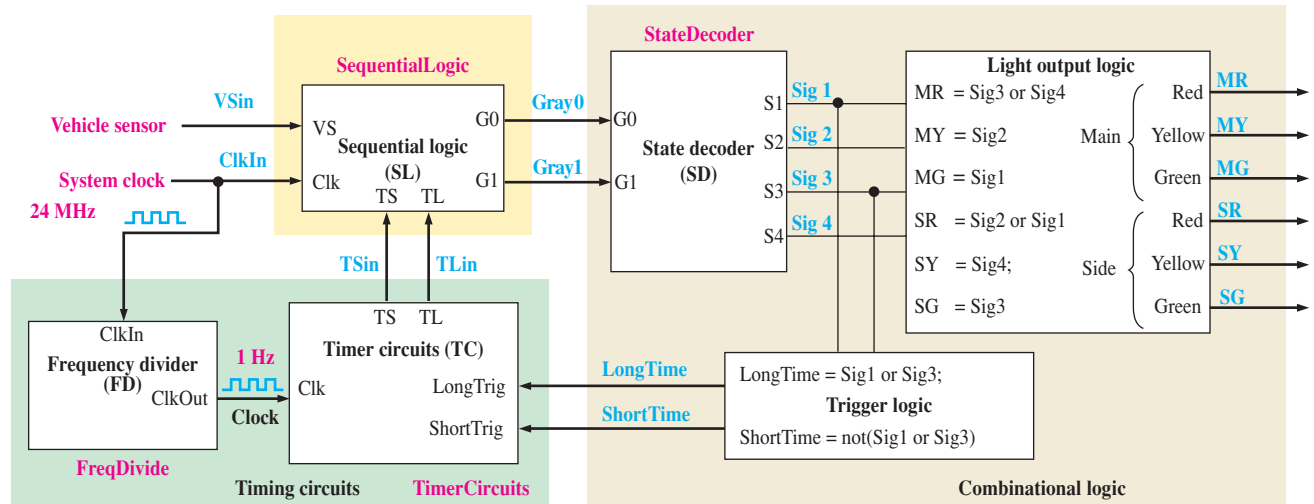


FIGURE 55 Programming model for the traffic signal control system.

The Timing Circuits Block

The two parts of the Timing circuits block are the Frequency divider (FD) and the Timer circuits (TC). A system clock frequency of 24 MHz is assumed. The Frequency divider part divides the 24 MHz system clock down to a 1 Hz clock. The Timer circuits part simulates the one-shot outputs described in Section 1 to produce outputs of $TS = 4$ s and $TL = 25$ s.

FREQUENCY DIVIDER The purpose of the frequency divider is to produce a 1 Hz clock for the timer circuits. The input ClkIn in this application is a 24.00 MHz oscillator that drives the program code. SetCount is used to initialize the count for a 1 Hz interval. The program FreqDivide counts up from zero to the value assigned to SetCount (one-half the oscillator speed) and inverts the output identifier ClkOut.

The integer value Cnt is set to zero prior to operation. The clock pulses are counted and compared to the value assigned to SetCount. When the number of pulses counted reaches the value in SetCount, the output ClkOut is checked to see if it is currently set to a 1 or 0. If ClkOut is currently 0, ClkOut is assigned a 1; otherwise, ClkIn is set to 1. Cnt is assigned a value of 0 and the process repeats. Toggling the output ClkOut each time the value of SetCount is reached creates a 1 Hz clock output with a 50% duty cycle.

VHDL FOR THE FREQUENCY DIVIDER

```

library ieee;
use ieee.std_logic_1164.all;

entity FreqDivide is
port(ClkIn, in std_logic;
     ClkOut: buffer std_logic);
end entity FreqDivide;

architecture FreqDivide Behavior of FreqDivide is
begin
  FreqDivide: process(ClkIn)
    variable Cnt: integer := 0;
    variable SetCount: integer;

```

ClkIn: 24.00 MHz clock driver
ClkOut: Output at 1 Hz

Cnt: Counts up to value in SetCount
SetCount: Holds 1/2 timer interval value


```

begin
  SetCount := 1200000; -- 1/2 duty cycle
  if (ClkIn'EVENT and ClkIn = '1') then
    if (Cnt = SetCount) then
      if ClkOut = '0' then
        ClkOut <= '1'; --Output high 50%
      else
        ClkOut <= '0'; --Output Low 50%
      end if;
      Cnt := 0;
    else
      Cnt := Cnt + 1;
    end if;
  end if;
end process;
end architecture FreqDivideBehavior;

```

SetCount is assigned a value equal to half the system clock to produce a 1 Hz output. In this case, a 24 MHz system clock is used.

The if statement causes program to wait for a clock event and clock = 1 to start operation.

Check that the terminal value in SetCount has been reached at which time ClkOut is toggled and Cnt is reset to 0.

If terminal value has not been reached, Cnt is incremented.

VERILOG FOR THE FREQUENCY DIVIDER

```

module FreqDivide (ClkIn, ClkOut);
  input ClkIn;
  inout ClkOut;
  integer Cnt = 0;
  integer SetCount = 1200000; //1/2 duty cycle
  reg [0:0] Q;

  always @(posedge ClkIn)
  begin
    if (Cnt == SetCount)
    begin
      if (ClkOut == 0)
      begin
        Q = 1; //Output high 50%
      end
      else
      begin
        Q = 0; //Output Low 50%
      end
      Cnt = 0;
    end
    else
    begin
      Cnt = Cnt + 1;
    end
  end
  assign ClkOut = Q;
endmodule

```

ClkIn: 24.00 MHz clock driver
 ClkOut: Output at 1 Hz
 Cnt: Counts up to value in SetCount
 SetCount: Holds 1/2 timer interval value
 Q: Holds output value within the always block

SetCount is assigned a value equal to half the system clock to produce a 1 Hz output. In this case a 24 MHz system clock is used.

The always statement causes program to wait for a positive edge clock event.

Check that the terminal value in SetCount has been reached at which time ClkOut is toggled and Cnt is reset to 0.

If terminal value has not been reached, Cnt is incremented.

Value stored in Q is assigned to ClkOut outside the always block.

TIMER CIRCUITS The program TimerCircuits uses two one-shot instances consisting of a 25 s timer (TLong) and a 4 s timer (TShort). The 25 s and the 4 s timers are triggered by long trigger (LongTrig) and short trigger (ShortTrig). In the VHDL and Verilog programs, countdown timers driven by a 1 Hz clock input (Clk) replicate the one-shot components TLong and TShort. The values stored in SetCountLong and SetCountShort are assigned to the Duration inputs of one-shot components TLong and TShort, setting the

25-second and 4-second timeouts. When Enable is set LOW, the one-shot timer is initiated and output QOut is set HIGH. When the one-shot timers time out, QOut is set LOW. The output of one-shot component TLong is sent to TimerCircuits identifier TL. The output of one-shot component TShort is sent to TimerCircuits identifier TS.

VHDL FOR THE TIMING CIRCUITS

```

library ieee;
use ieee.std_logic_1164.all;

entity TimerCircuits is
  port(LongTrig, ShortTrig, Clk: in std_logic;
        TS, TL: buffer std_logic);
end entity TimerCircuits;

architecture TimerBehavior of TimerCircuits is
  component OneShot is
    port(Enable, Clk: in std_logic;
          Duration :in integer range 0 to 25;
          QOut :buffer std_logic);
  end component OneShot;

  signal SetCountLong, SetCountShort: integer range 0 to 25;
begin
  SetCountLong <= 25; } Long and short count times are hard-coded
  SetCountShort <= 4; } to 25 and 4 based on a 1 Hz clock.
  TLong:OneShot port map(Enable=>LongTrig, Clk=>Clk, Duration=>SetCountLong, QOut=>TL); ← Instantiation TLong
  TShort:OneShotport map(Enable=>ShortTrig, Clk=>Clk, Duration=>SetCountShort, QOut=>TS); ← Instantiation TShort
end architecture TimerBehavior;

```

LongTrig: Long timeout timer enable input
ShortTrig: Short timeout timer enable input
Clk: 1 Hz Clock input
TS: Short timer timeout signal
TL: Long timer timeout signal

Component declaration for OneShot.

SetCountLong: Holds long timer duration
SetCountShort: Holds short timer duration

VERILOG FOR THE TIMING CIRCUITS

```

module TimerCircuits(LongTrig, ShortTrig, Clk, TS, TL);
  input LongTrig, ShortTrig, Clk;
  inout TS, TL;

  wire[8:0] SetCountLong = 25; } Long and short count times are hard-coded
  wire[8:0] SetCountShort = 4; } to 25 and 4 based on a 1 Hz clock.
  OneShot TLong(.Enable(LongTrig), .Clk(Clk), .Duration(SetCountLong), .QOut(TL)); ← Instantiation TLong
  OneShot TShort(.Enable(ShortTrig), .Clk(Clk), .Duration(SetCountShort), .QOut(TS)); ← Instantiation TShort
endmodule

```

LongTrig: Long timeout timer enable input
ShortTrig: Short timeout timer enable input
Clk: 1 Hz Clock input
TS: Short timer timeout signal
TL: Long timer timeout signal

SetCountLong: Holds long timer duration
SetCountShort: Holds short timer duration

The Sequential Logic Block

The Sequential logic (SL) determines the sequence of the traffic lights. The program SequentialLogic provides the Gray code logic needed to drive the traffic signal system based on input from the program TimerCircuits and the side street vehicle sensor. The sequential logic code produces a 2-bit Gray code sequence for each of the four sequence states defined in the program. The component definition dff is used to instantiate two DFlip-Flop instances DFF0 and DFF1. DFF0 and DFF1 drive the two-bit Gray code. The Gray code output sequences the traffic light system through each of four states. Internal variables D0 and D1 store the results of the D0 and D1 Boolean expressions developed in System Example 1. The stored results in D0 and D1 are assigned to DFlipFlops DFF0 and DFF1 along with the system clock to drive outputs G0 and G1 from the DFlipFlop Q outputs.

VHDL FOR THE SEQUENTIAL LOGIC

<pre> library ieee; use ieee.std_logic_1164.all; entity SequentialLogic is port(VS, TL, TS, Clk: in std_logic; G0, G1: inout std_logic); end entity SequentialLogic; architecture SequenceBehavior of SequentialLogic is component dff is port(D, Clk: in std_logic; Q: out std_logic); end component dff; signal D0, D1: std_logic; begin D1 <= (G0 and not TS) or (G1 and TS); D0 <= (not G1 and not TL and VS) or (not G1 and G0) or (G0 and TL and VS); DFF0: dff port map(D=> D0, Clk => Clk, Q => G0); DFF1: dff port map(D=> D1, Clk => Clk, Q => G1); end architecture SequenceBehavior; </pre>	<p>VS: Vehicle sensor input TL: Long timer input TS: Short timer input Clk: System clock G0: Gray code output bit 0 G1: Gray code output bit 1 D0: Logic for DFlipFlop DFF0 D1: Logic for DFlipFlop DFF1</p> <p>Component declaration for D flip-flop (dff)</p> <p>Logic definitions for D flip-flop inputs D0 and D1 derived from Boolean expressions developed in System Example 1.</p> <p>Component instantiations</p>
--	--

VERILOG FOR THE SEQUENTIAL LOGIC

<pre> module SequentialLogic(VS, TL, TS, Clk, G0, G1); input VS, TL, TS, Clk; inout G0, G1; wire D0, D1; assign D1 = (G0 && !TS) (G1 && TS); assign D0 = (!G1 && !TL && VS) (!G1 && G0) (G0 && TL && VS); dff DFF0(.d(D0), .Clk(Clk), .q(G0)); dff DFF1(.d(D1), .Clk(Clk), .q(G1)); endmodule </pre>	<p>VS: Vehicle sensor input TL: Long timer input TS: Short timer input Clk: System clock G0: Gray code output bit 0 G1: Gray code output bit 1 D0: Logic for DFlip-Flop DFF0 D1: Logic for DFlipFlop DFF1</p> <p>Logic definitions for D flip-flop inputs D0 and D1 derived from Boolean expres- sions developed in System Example 1.</p> <p>Component instantiations</p>
---	---

The Combinational Logic Block

The combinational logic block consists of three parts: State decoder, Light output logic, and Trigger logic.

STATE DECODER The state decoder (SD) is part of the Combinational logic block. The source program StateDecoder decodes the 2-bit Gray code from the program SequentialLogic to determine which of four states the system is in. The inputs to the state decoder are the two Gray code bits G1 and G0. The Boolean expressions for the four state outputs S1, S2, S3 and S4, were developed in Section 1. For each of the four input codes, one and only one of the outputs is activated.

VHDL FOR THE STATE DECODER

```

library ieee;
use ieee.std_logic_1164.all;

entity StateDecoder is
port(G0, G1: in std_logic; S1, S2, S3, S4: out std_logic);
end entity StateDecoder;

architecture StateDecoderBehavior of StateDecoder is
begin
S1 <= not G1 and not G0;
S2 <= not G1 and G0;
S3 <= G1 and G0;
S4 <= G1 and not G0;
end architecture StateDecoderBehavior;

```

G0,G1 :Gray code input
S1–S4 :State output

2-Bit Gray Code		
	G1	G0
State 1	0	0
State 2	0	1
State 3	1	1
State 4	1	0

} Logic definitions for state decoder developed in Section 1

VERILOG FOR THE STATE DECODER

```

module StateDecoder(G0, G1, S1, S2, S3, S4);
input G0, G1;
output S1, S2, S3, S4;

assign S1 = !G1 && !G0;
assign S2 = !G1 && G0;
assign S3 = G1 && G0;
assign S4 = G1 && !G0;
endmodule

```

G0,G1 :Gray code input
S1–S4 :State output

2-Bit Gray Code		
	G1	G0
State 1	0	0
State 2	0	1
State 3	1	1
State 4	1	0

} Logic definitions for state decoder developed in Section 1

LIGHT OUTPUT LOGIC This block of logic accepts inputs Sig1–Sig4 from the state decoder and produces the traffic light outputs MR, MY, MG, SR, SY, and SG for the traffic light interface unit. The Boolean expressions were developed in Section 1 and are implemented in the program TrafficLights, which describes the complete system.

TRIGGER LOGIC This block of logic accepts input Sig1 and Sig3 from the state decoder and produces the triggers, LongTime and ShortTime, for the Timer Circuits. The Boolean expressions were developed in Section 1 and are implemented in the program TrafficLights.

The Complete Traffic Signal Control System

The program TrafficLights completes the traffic signal control system. Components Freq-Divide, TimerCircuits, SequentialLogic, and StateDecoder are used to compose the completed system. Signal CLKin from the TrafficLights program source code is the clock input to the FreqDivide component. The frequency divided output ClkOut is stored as local variable Clock and is the divided clock input to the TimerCircuits and Sequential-Logic components. TimerCircuits is controlled by local variables LongTime and ShortTime, which are controlled by the outputs Sig1 and Sig3 from component StateDecoder. StateDecoder also provides outputs Sig1 through Sig4 to control the traffic lights MG, SG, MY, SY, MR, and SR. TimerCircuit timeout signals TS and TL are stored in variables TLin (timer long in) and TSin (timer short in).

Signals TSin and TLin from TimerCircuits are used along with vehicle sensor VSin as inputs to the SequentialLogic component. The outputs from SequentialLogic G0 and G1 are stored in variables Gray0 and Gray1 as inputs to component StateDecoder. Component StateDecoder returns signals S1 through S4 which are in turn passed to variables Sig1 through Sig4. The values stored in variables Sig1 through Sig4 provide the logic for outputs MG, SG, MY, SY, MR, SR; and local timer triggers LongTime and ShortTime are sent to TimerCircuits.

VHDL FOR THE TRAFFIC SIGNAL CONTROL SYSTEM

```

library ieee;
use ieee.std_logic_1164.all;

entity TrafficLights is
port(VSin, ClkIn: in std_logic; MR, SR, MY, SY, MG, SG: out std_logic);
end entity TrafficLights;

architecture TrafficLightsBehavior of TrafficLights is

component StateDecoder is
port(G0, G1: in std_logic; S1, S2, S3, S4: out std_logic);
end component StateDecoder;

component SequentialLogic is
port(VS, TL, TS, Clk: in std_logic; G0, G1: inout std_logic);
end component SequentialLogic;

component TimerCircuits is
port(LongTrig, ShortTrig, Clk: in std_logic; TS, TL: buffer std_logic);
end component TimerCircuits;

component FreqDivide is
port(ClkIn: in std_logic; ClkOut: buffer std_logic);
end component FreqDivide;

signal Sig1, Sig2, Sig3, Sig4, Gray0, Gray1: std_logic;
signal LongTime, ShortTime, TLin, TSin, Clock: std_logic;

begin
MR <= Sig3 or Sig4;
SR <= Sig2 or Sig1;
MY <= Sig2;
SY <= Sig4;
MG <= Sig1;
SG <= Sig3;

LongTime <= Sig1 or Sig3;
ShortTime <= not(Sig1 or Sig3);

SD: StateDecoder port map(G0 => Gray0, G1 => Gray1, S1 => Sig1, S2 => Sig2, S3 => Sig3, S4 => Sig4);
SL: SequentialLogic port map(VS => VSin, TL => TLin, TS => TSin, Clk => Fout, G0 => Gray0, G1 => Gray1);
TC: TimerCircuits port map(LongTrig=>LongTime, ShortTrig=>ShortTime, Clk=>Clock, TS=>TSin, TL=>TLin);
FD: FreqDivide port map(ClkIn => CLKIn, ClkOut => Clock);

end architecture TrafficLightsBehavior

```

VSin : Vehicle sensor input
CLKIn : System Clock
MR : Main red light output
SR : Side red light output
MY : Main yellow light output
SY : Side yellow light output
MG : Main green light output
SG : Side green light output

Component declaration for StateDecoder

Component declaration for SequentialLogic

Component declaration for TimerCircuits

Component declaration for FreqDivider

Sig1-4 : Return values from StateDecoder
Gray0-1 : SequentialLogic Gray code return
LongTime : Trigger input to TimerCircuits
ShortTime : Trigger input to TimerCircuits
TLin : Store TimerCircuits long timeout
TSin : Store TimerCircuits Short timeout
Clock : Divided clock from FreqDivide

Logic definitions for the light output logic

Logic definitions for the trigger logic

Component instantiations

VERILOG FOR THE TRAFFIC SIGNAL CONTROL SYSTEM

```

module TrafficLights(VSin, CLKin, MR, SR, MY, SY, MG, SG);
input VSin, CLKin;
output MR, SR, MY, SY, MG, SG;

```

```

wire Sig1, Sig2, Sig3, Sig4, Gray0, Gray1;
wire LongTime, ShortTime, TLin, TSin, Clk, Clock;

```

```

assign MR = Sig3 || Sig4;
assign SR = Sig2 || Sig1;
assign MY = Sig2;
assign SY = Sig4;
assign MG = Sig1;
assign SG = Sig3;
assign LongTime = Sig1 || Sig3;
assign ShortTime = !(Sig1 || Sig3);

```

Logic definitions for the light output logic

Logic definitions for the trigger logic

```

StateDecoder SD(.G0(Gray0), .G1(Gray1), .S1(Sig1), .S2(Sig2), .S3(Sig3), .S4(Sig4));
SequentialLogic SL(.VS(VSin), .TL(TLin), .TS(TSin), .Clk(Clock), .G0(Gray0), .G1(Gray1));
TimerCircuits TC(.LongTrig(LongTime), .ShortTrig(ShortTime), .Clk(Clock), .TS(TSin), .TL(TLin));
FreqDivide FD(.Clkin(CLKin), .ClkOut(Clock));

```

Component instantiations

```

endmodule

```

VSin : Vehicle sensor input
 CLKin : System Clock
 MR : Main red light output
 SR : Side red light output
 MY : Main yellow light output
 SY : Side yellow light output
 MG : Main green light output
 SG : Side green light output

Sig1-4 : Return values from StateDecoder
 Gray0-1 : SequentialLogic Gray code return
 LongTime : Trigger input to TimerCircuits
 ShortTime : Trigger input to TimerCircuits
 TLin : Store TimerCircuits long timeout
 TSin : Store TimerCircuits short timeout
 Clock : Divided clock from FreqDivide

SECTION 7 CHECKUP

- How are the programs broken down in terms of system blocks?
- How is the complete system program formed?
- Describe the observable difference between VHDL and Verilog programs.

8 TROUBLESHOOTING

It is standard practice to test a new circuit or system design to be sure that it is operating as specified. This process is sometimes referred to as debugging. A circuit or system can be debugged in two ways: software simulation and hardware testing. In software simulation, a program such as Multisim is used to construct and test the new design. In hardware testing, designs are “breadboarded” and tested before the design is finalized. The term *breadboard* refers to a method of temporarily hooking up a circuit so that its operation can be verified and any design flaws worked out before a prototype unit is built. Once a design has been thoroughly tested, the prototype is implemented on one or more circuit boards. A complete system test is then done on the boards. In this section, the traffic signal control system is the focus, and several aspects of testing, debugging, and troubleshooting will be discussed.



After completing this section, you should be able to

- Discuss software simulation applied to system debugging
- Describe prototype breadboarding as a method of testing a design.
- Explain several methods of hardware troubleshooting

Multisim Software Simulation

COMBINATIONAL LOGIC Figure 56 shows the Multisim simulation screen for the complete combinational logic portion of the traffic signal control system including the state decoder, light output logic, and trigger logic. Switches are used to simulate the Gray code inputs, and probes are used to indicate the activity on the outputs of the combinational logic. The switches and probes are for simulation testing only and are not part of the logic circuit.

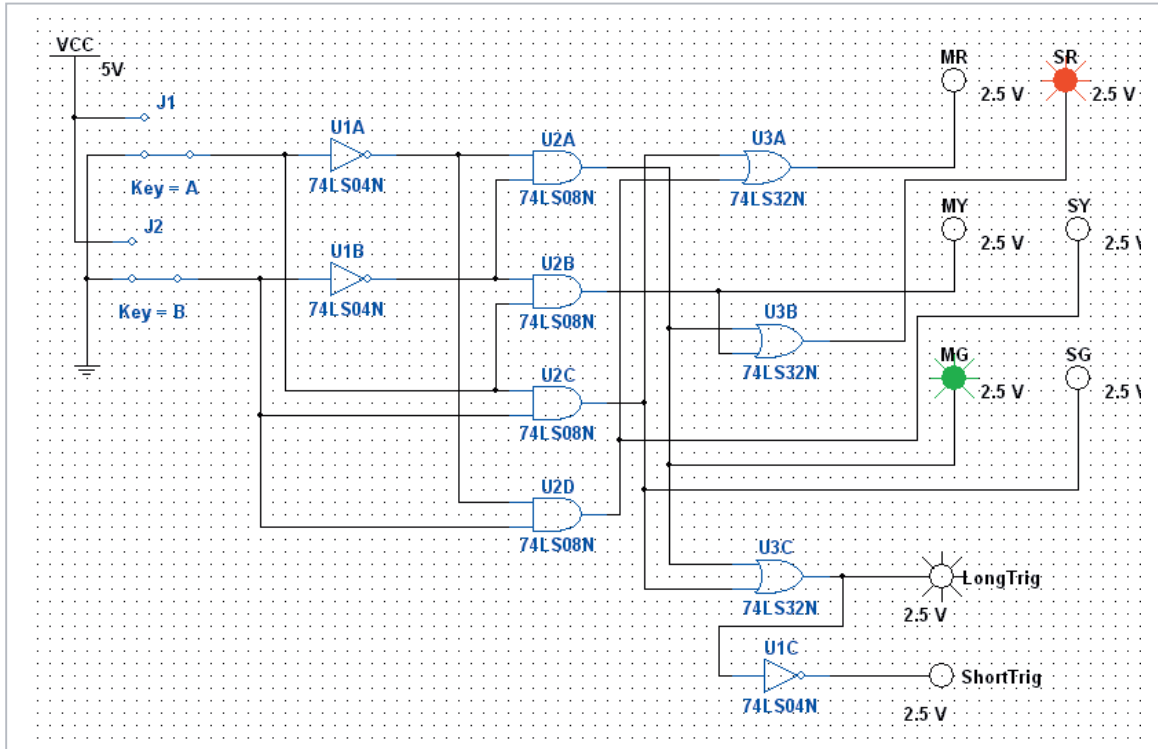


FIGURE 56 Multisim circuit screen for the combinational logic showing the first state. Open Multisim file F06-56 on the website and run the simulation for the combinational logic portion of the traffic signal control system. Observe the operation for each of the four states in the light sequence.

TIMING CIRCUITS Figure 57 shows the simulation screen for the timing circuits portion of the traffic signal control system including the 25 s timer, 4 s timer, and oscillator. This is an alternate version that differs from the HDL description shown earlier in the chapter and represents the implementation using 555 timers.

SIMULATION TIME VERSUS REAL TIME Simulation time is based on the software program and the computer it is running on; it is much greater than real time that will occur in the actual circuit. For the particular computer used to generate the simulation shown in Figure 57, the ratio of simulation time to real time is 1000 but may vary depending on the speed of the computer used to run the software as well as other factors. Because of this ratio of simulation time to real time, the RC time constant values for the one-shots are 1000 times smaller than the values you would use in an actual hardware circuit. By connecting a Multisim probe to a one-shot output and using the switch to trigger that one-shot, you can observe the output in real time. A virtual oscilloscope connected to that output will record a much shorter time than the real time observation. For example, a scope connected to the output of the 25 s long timer (U1) as shown in Figure 58(a) will

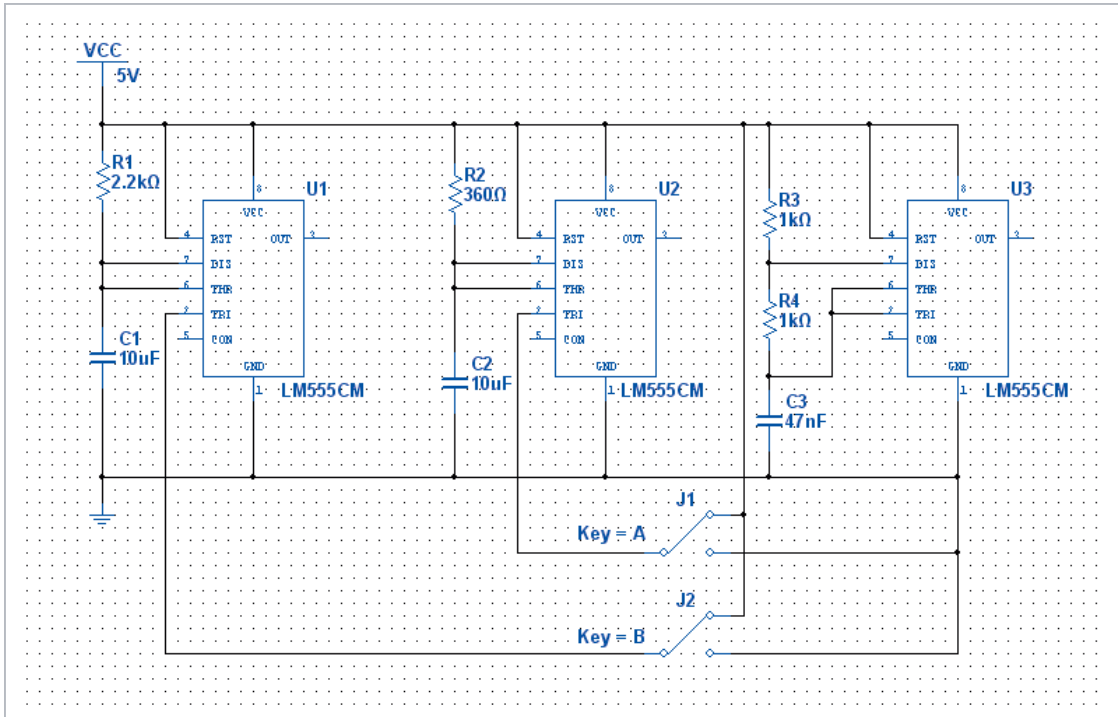
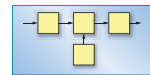


FIGURE 57 Multisim screen for a version of the timing circuits. The switches are for test purposes only.

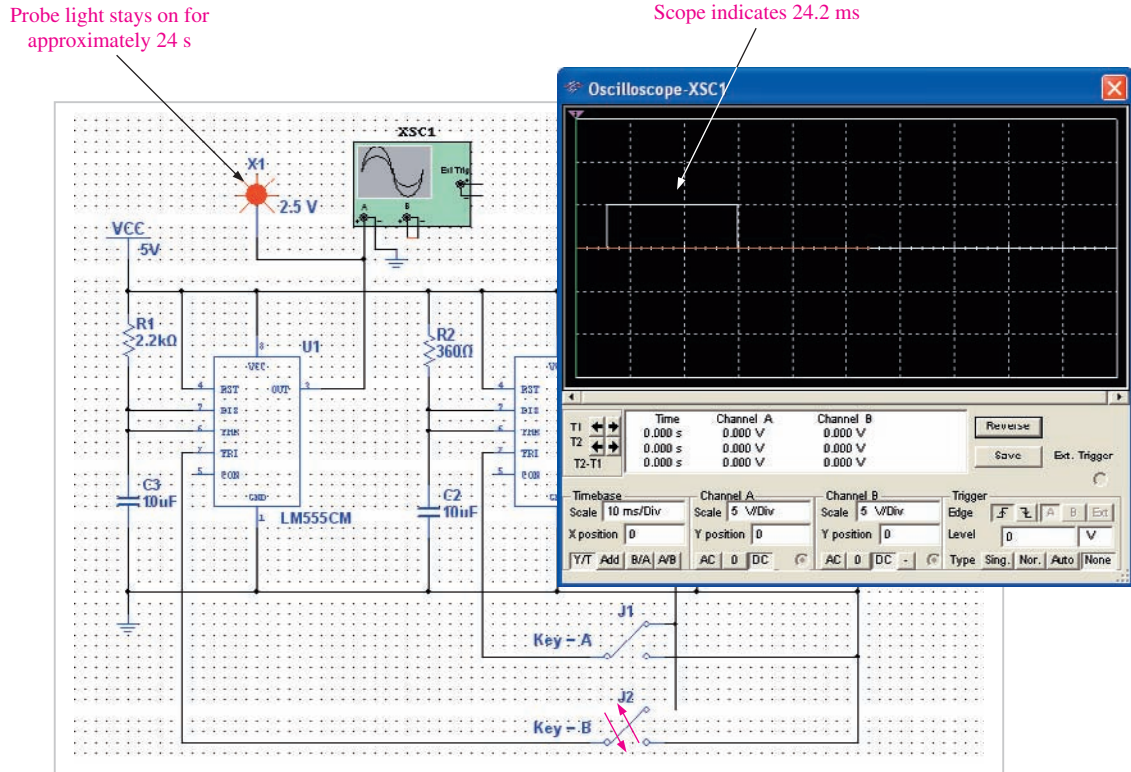
display an output pulse with a duration of 24.2 ms when the timer is triggered. However, a probe connected to that output will stay on for approximately 24 s (depending on the computer and the number of time steps used in the simulation). The output of the 555 timer configured as an oscillator is shown in Figure 58(b) using the virtual scope.

Grace Hopper, a mathematician and pioneer programmer, developed considerable troubleshooting skills as a naval officer working with the Harvard Mark I computer in the 1940s. She found and documented in the Mark I's log the first real computer bug. It was a moth that had been trapped in one of the electromechanical relays inside the machine, causing the computer to malfunction. From then on, when asked if anything was being accomplished, those working on the computer would reply that they were “debugging” the system. The term stuck, and finding problems in a computer (or other electronic device), particularly the software, would always be known as debugging.

SYSTEM NOTE

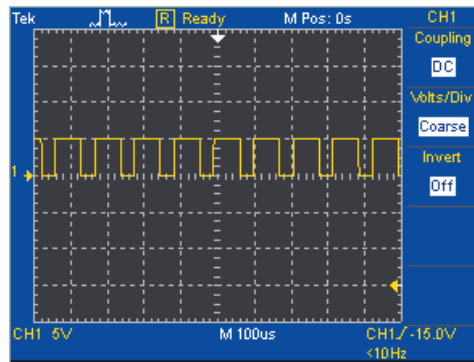


PROTOTYPE CHECK The computer simulation of timers is more likely to have an undetected error because of the simulation versus real time issue previously discussed. It is usually advisable to verify a block like this prior to combining it into the complete system. For this application, the timing circuits are constructed on a prototyping system, and the results are measured carefully. The prototyping system that is selected is one that is closely linked to Multisim and can later be used to develop a circuit board. It is the National Instruments ELVIS system. The prototype circuit and measured data are shown in Figure 59.



(a) Illustration of one-shot simulation.

Switch is moved to ground momentarily to trigger one-shot.



(b) 10 kHz oscillator output

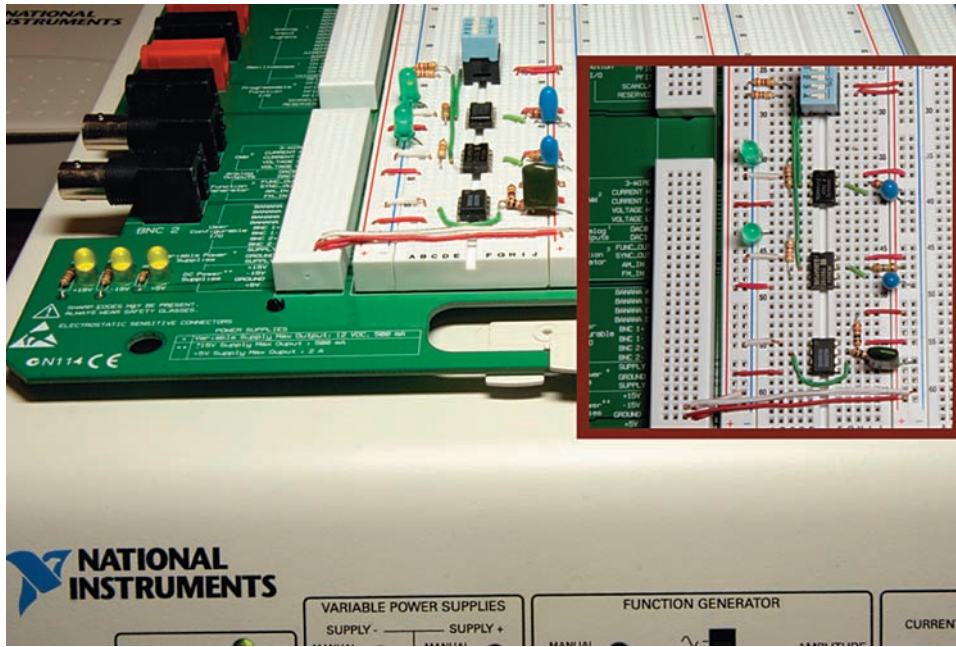
MULTISIM **FIGURE 58** Testing the simulated timer circuit. Open Multisim file F06-58 on the website. Run the timing circuit simulation using your Multisim software and observe the operation.

SEQUENTIAL LOGIC Figure 60 shows the simulation screen for the sequential logic portion of the traffic signal control system.

THE COMPLETE TRAFFIC SIGNAL CONTROL SYSTEM Now that all three parts of the system have been simulated and tested, they are combined to form the complete system. A simulation screen for the complete system is shown in Figure 61. Each part of the system has been converted to a Multisim subcircuit.

The main green light will stay on continuously as long as there is no vehicle on the side street. When a vehicle appears on the side street, the main green light will time out and change to red for 25 s to allow side street traffic to move. If there is continuous traffic on the side street, the main red and green lights will alternate every 25 s.

LATCHES, FLIP-FLOPS, AND TIMERS



CIRCUIT	OUTPUT
U1 Long timer	29 s pulse
U2 Short timer	4.6 s pulse
U3 Oscillator	9.6 kHz

FIGURE 59

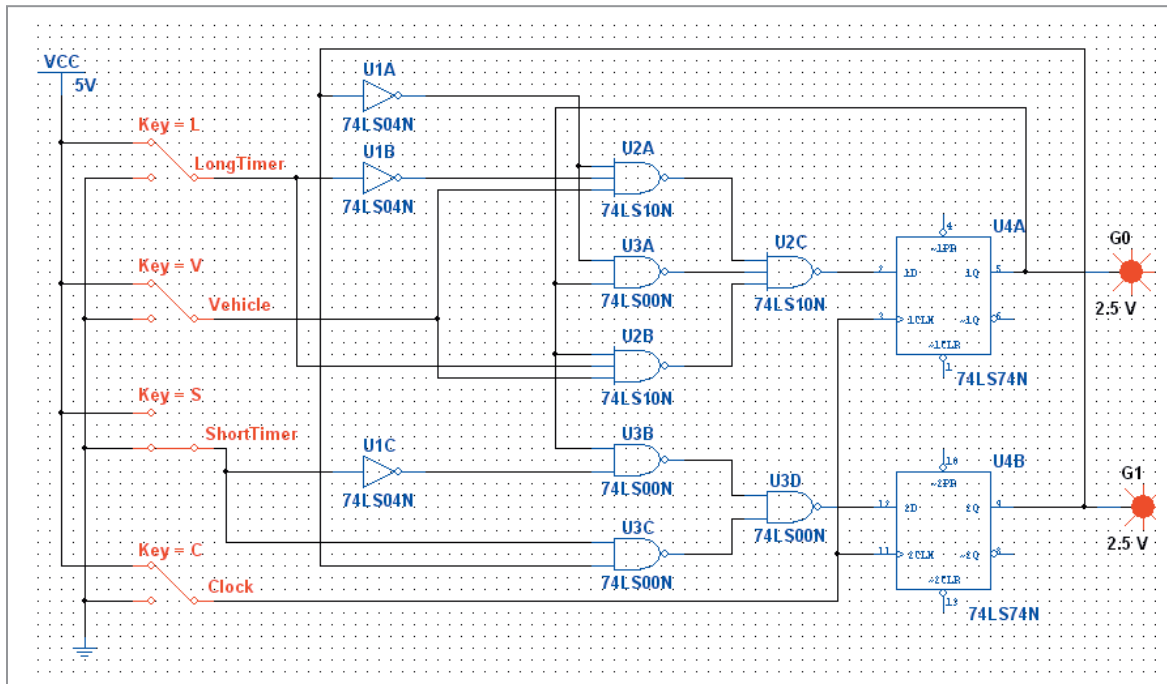


FIGURE 60 Multisim screen for sequential logic simulation. The switches are for test purposes only. When a probe is red, a 1 is indicated. Open file F06-60 on the website using your Multisim software. All of the inputs are shown as switch inputs for simulation purposes. Set up the input conditions for T_L , T_S , and V_s . Then momentarily make the clock input go LOW (ground) and then back HIGH (V_{CC}). Follow the sequence indicated by the state diagram in Figure 2.



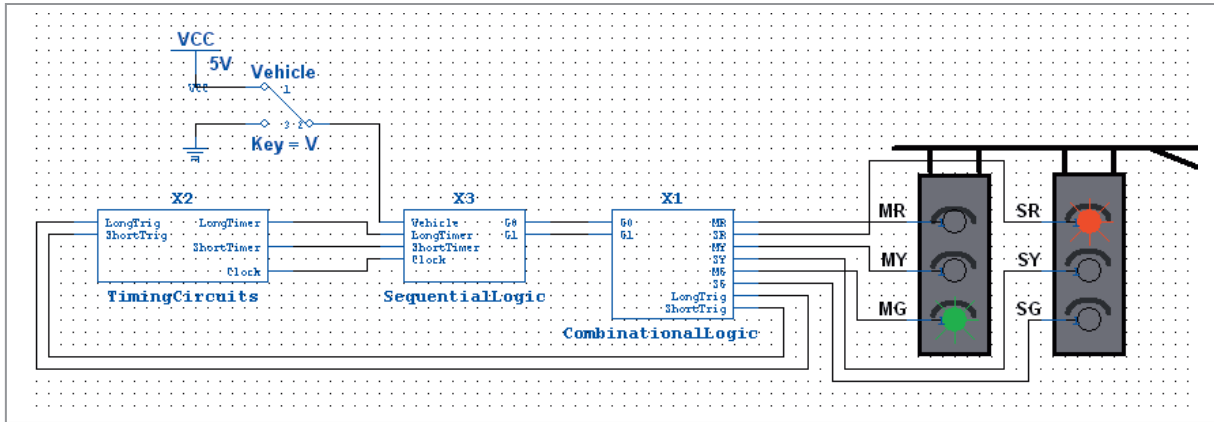
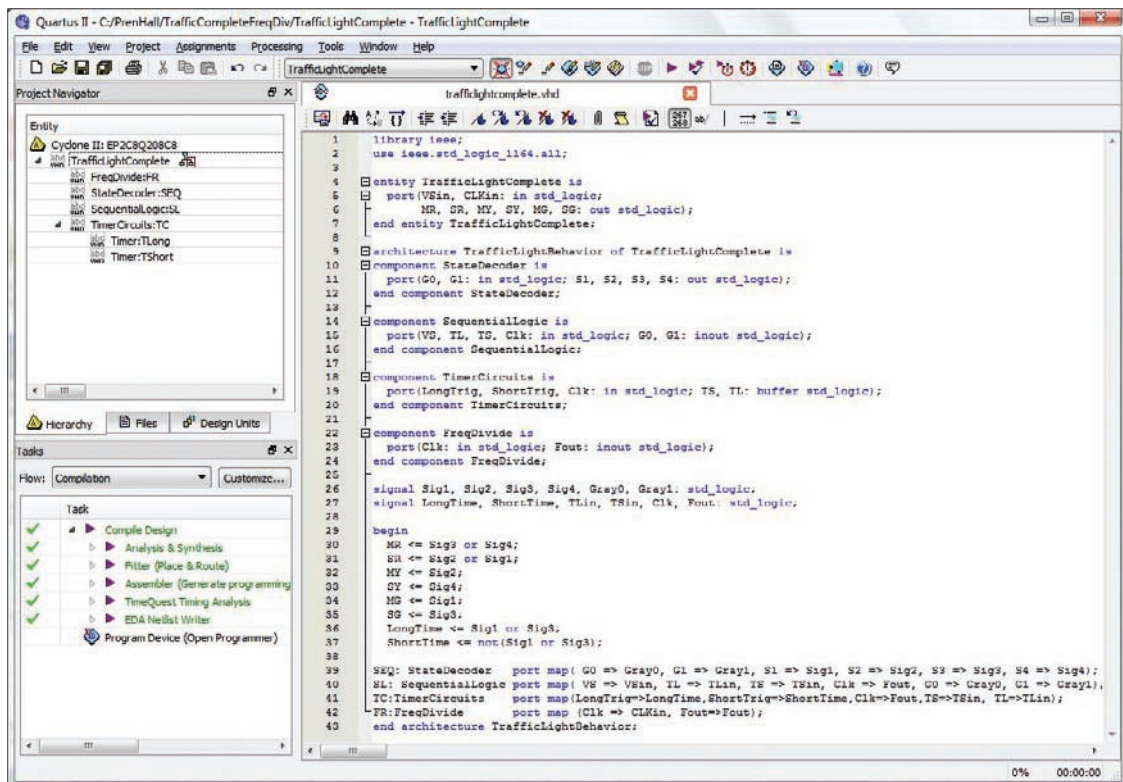


FIGURE 61 Simulation of the traffic signal control system with each part represented by a sub-circuit. Open File F06-61 on the website. Run the traffic signal controller simulation using your Multisim software and observe the operation. Lights will appear randomly when first turned on. Simulation times may vary.



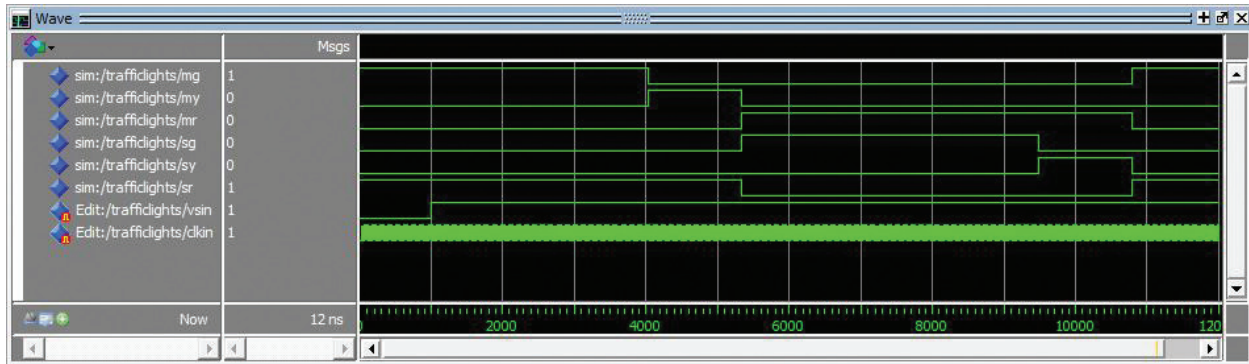
Development Software Simulation

Once a new design has been verified by Multisim simulation and prototyping, it is described with VHDL or Verilog code. The code is then entered into a computer using development software with a *text editor*, as shown in Figure 62(a) for the traffic signal control system with VHDL. The code is then compiled by the computer using the development software that was used to enter the VHDL or Verilog design into the computer. Two major types of software development tools are Altera Quartus and Xilinx ISE, tutorials for which are available on the website. When the code is compiled, a test feature of the



(a) VHDL code is entered on text editor.

FIGURE 62 Traffic signal control design entered in VHDL and simulated using PLD development software (Quartus II in this case).



(b) Simulation waveforms on the waveform editor.

FIGURE 62 (Continued)

development software is used to specify inputs and run a simulation to produce the output waveform(s) on a screen, generally called the *waveform editor*, as shown in Figure 62(b).

Hardware Testing

Let's assume that the traffic signal control system has been described using the VHDL or Verilog code from Section 7 and downloaded into a programmable logic device (PLD) using a development software such as Altera Quartus or Xilinx ISE. The PLD is mounted on a development board such as the one shown in Figure 63. There are several methods for testing system circuit boards with PLDs on them.

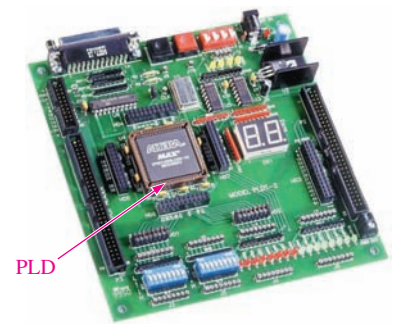


FIGURE 63 A typical development board used for programming and testing a PLD. A design specified in VHDL or Verilog is implemented in the PLD.

TRADITIONAL TESTING Depending on the complexity of the system, standard laboratory or field instruments can be used, as shown in Figure 64. For systems with a large number of waveforms to observe, a logic analyzer instead of an oscilloscope would be used. You can apply input signals to input pins and check the output pins for the proper waveforms. This traditional method is practical for one-of-a-kind development boards and for the preproduction testing of prototype systems.

BED-OF-NAILS TESTING The testing of printed circuit boards at production levels must be done automatically. The **bed-of-nails (BON)** method was one of the first approaches to automated testing. The pc board is placed on a fixture with an array of small nail-like test probes that make contact with test points on the board. The signals at each test point are checked simultaneously by automated test equipment. The concept is illustrated in Figure 65.

Basically, the purpose of automated production testing is to find any manufacturing flaws, such as open or shorted pins and wrong, missing, or misaligned components. This automated process does not primarily test for functionality of the logic. It is assumed that each component has been tested for functionality prior to installation on the circuit board and that the only flaws should be those created during manufacturing.

FLYING PROBE TESTING Another method for testing printed circuit boards is called the **flying probe** method. A typical flying probe and its basic operation are shown in Figure 66. A test probe is positioned above a circuit board that is to be tested. The probe can be automatically moved in three axes—along the *x*-axis, the *y*-axis, and the *z*-axis of the board—to make contact with any specified test points. The movement of the probe is controlled by software that uses the physical layout of the board to determine the coordinates. Many flying probe testers have multiple probes for one board.

The flying probe method of testing overcomes some of the limitations of the bed-of-nails method. First, the BON method requires a different fixture for each type of circuit board, but the flying probe method requires no fixture. Also, the flying probe can access



HANDS ON TIP

Glitches that occur in digital systems are very fast (extremely short in duration) and can be difficult to see on an oscilloscope, particularly at lower sweep rates. A logic analyzer, however, can show a glitch easily. To look for glitches using a logic analyzer, select “latch” mode or (if available) transitional sampling. In the latch mode, the analyzer looks for a voltage level change. When a change occurs, even if it is of extremely short duration (a few nanoseconds), the information is “latched” into the analyzer’s memory as another sampled data point. When the data are displayed, the glitch will show as an obvious change in the sampled data, making it easy to identify.

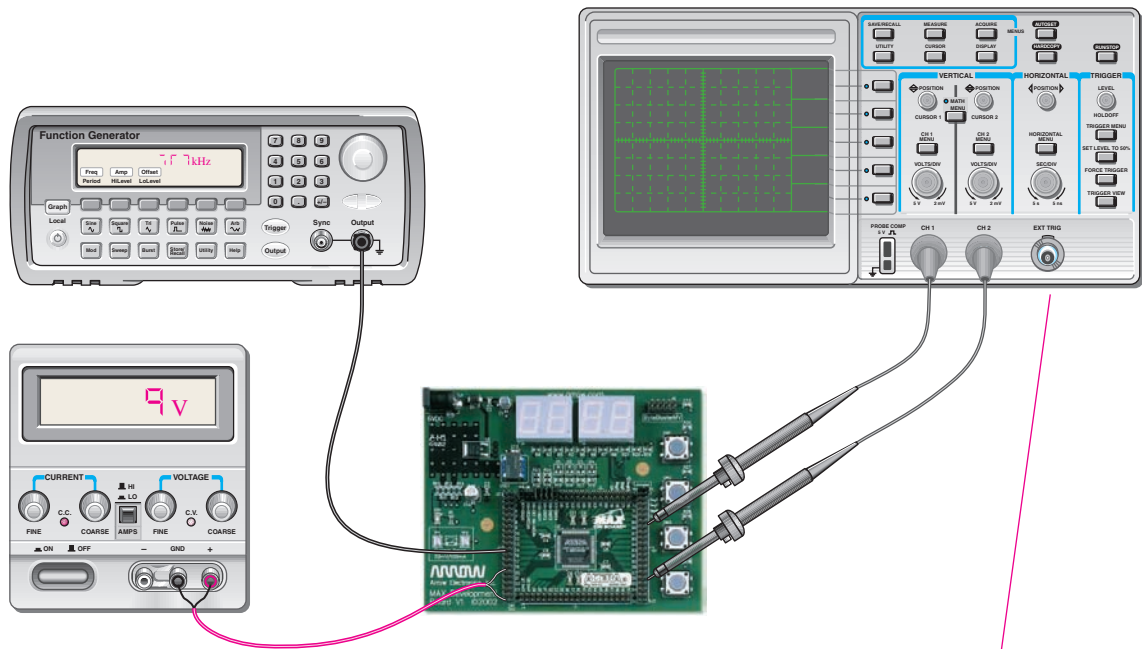
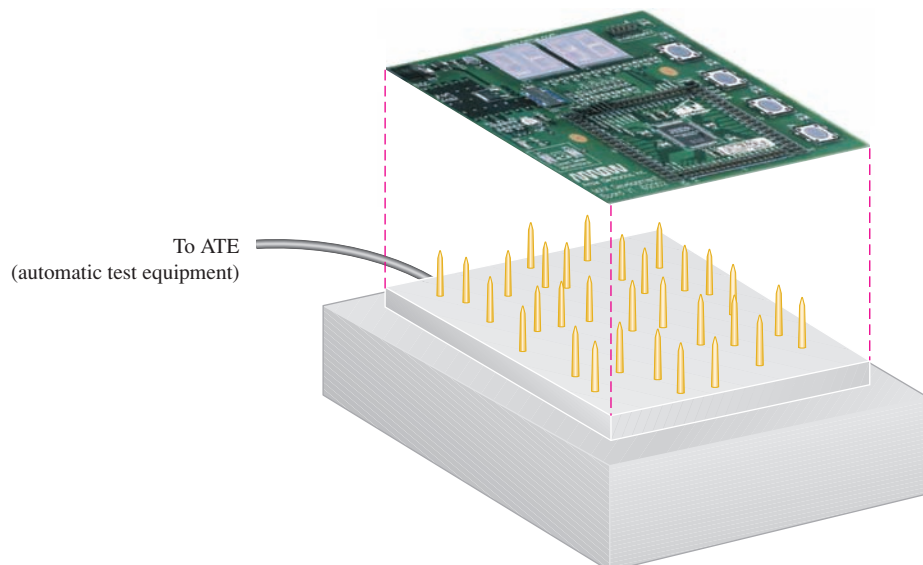


FIGURE 64 Traditional testing using standard instruments. An oscilloscope or a logic analyzer can be used. (Photo used with permission from Tektronix, Inc.)

FIGURE 65 Bed-of-nails automated testing.



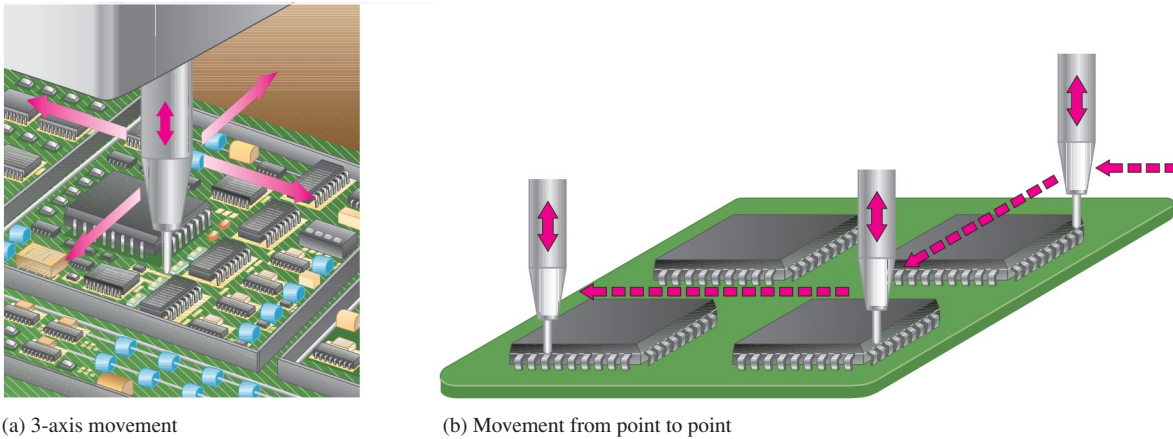


FIGURE 66 Flying probe testing of a circuit board.

more points on a board because the probe can be moved to any position, and it can access the top of the board where the components are.

BOUNDARY SCAN TESTING Limited access to test points led to the concept of placing the test points within the integrated circuit devices themselves. Most PLDs (CPLDs and FPGAs) include boundary scan logic as part of their internal structure independent of the functionality of the logic programmed into the PLD. These devices are JTAG compliant (JTAG is a connection standard).

A circuit, known as a boundary scan cell, is placed between the programmable logic and each input and output pin of the PLD. The cells are basically memory cells that store a 1 or a 0. The cells connected to the programmable logic inputs are called input cells, and those connected to the programmable logic outputs are called output cells. **Boundary scan** testing is based on the JTAG standard (IEEE Std. 1149.1).

TROUBLESHOOTING IN THE FIELD Once a system has been installed on site, faults that may occur generally require on-site troubleshooting. For example, let's assume that the traffic signal control system is in a housing mounted on a pole at the intersection. In this situation, there would not be time for extensive troubleshooting because the traffic light must be back up and working quickly. Unless the fault is obvious and easy to remedy, such as a loose wire or blown fuse, the approach is to replace the circuit board. The faulty board can then be tested and repaired off-site.

SECTION 8 CHECKUP

1. What are the two basic approaches to debugging or testing?
2. How would you test a one-of-a-kind or prototype circuit board?
3. List three methods for production testing a circuit board.

SUMMARY

- Latches are bistable devices whose state normally depends on asynchronous inputs.
- Edge-triggered flip-flops are bistable devices with synchronous inputs whose state depends on the inputs only at the triggering transition of a clock pulse. Changes in the outputs occur at the triggering transition of the clock.
- Monostable multivibrators (one-shots) have one stable state. When the one-shot is triggered, the output goes to its unstable state for a time determined by an RC circuit.

- Astable multivibrators have no stable states and are used as oscillators to generate timing waveforms in digital systems.
- VHDL and Verilog can be used to describe a complete system.
- Two methods of debugging are software simulation and hardware testing.

KEY TERMS

Astable Having no stable state. An astable multivibrator oscillates between two quasi-stable states.

Bistable Having two stable states. Flip-flops and latches are bistable multivibrators.

Clear An input used to reset a flip-flop (make the Q output 0).

Clock The triggering input of a flip-flop.

D flip-flop A type of bistable multivibrator in which the output assumes the state of the D input on the triggering edge of a clock pulse.

Edge-triggered flip-flop A type of flip-flop in which the data are entered and appear on the output on the same clock edge.

Hold time The time interval required for the control levels to remain on the inputs to a flip-flop after the triggering edge of the clock in order to reliably activate the device.

J-K flip-flop A type of flip-flop that can operate in the SET, RESET, no-change, and toggle modes.

Latch A bistable digital circuit used for storing a bit.

Monostable Having only one stable state. A monostable multivibrator, commonly called a *one-shot*, produces a single pulse in response to a triggering input.

One-shot A monostable multivibrator.

Power dissipation The amount of power required by a circuit.

Preset An asynchronous input used to set a flip-flop (make the Q output 1).

Propagation delay time The interval of time required after an input signal has been applied for the resulting output change to occur.

RESET The state of a flip-flop or latch when the output is 0; the action of producing a RESET state.

SET The state of a flip-flop or latch when the output is 1; the action of producing a SET state.

Set-up time The time interval required for the control levels to be on the inputs to a digital circuit, such as a flip-flop, prior to the triggering edge of a clock pulse.

Synchronous Having a fixed time relationship.

Timer A circuit that can be used as a one-shot or as an oscillator.

Toggle The action of a flip-flop when it changes state on each clock pulse.

TRUE/FALSE QUIZ

Answers are at the end of the chapter.

1. A latch has two stable states.
2. A latch is considered to be in the SET state when the Q output is LOW.
3. A gated D latch must be enabled in order to change state.
4. Flip-flops and latches are both bistable devices.
5. An edge-triggered D flip-flop changes state whenever the D input changes.
6. A clock input is necessary for an edge-triggered flip-flop.
7. When both the J and K inputs are HIGH, an edge-triggered J-K flip-flop changes state on each clock pulse.
8. A one-shot is also known as an astable multivibrator.
9. When triggered, a one-shot produces a single pulse.
10. The 555 timer can be used as a one-shot or as a pulse oscillator.

SELF-TEST

Answers are at the end of the chapter.

- If an S-R latch has a 1 on the S input and a 0 on the R input and then the S input goes to 0, the latch will be
(a) set (b) reset (c) invalid (d) clear
- The invalid state of an S-R latch occurs when
(a) $S = 1, R = 0$ (b) $S = 0, R = 1$
(c) $S = 1, R = 1$ (d) $S = 0, R = 0$
- For a gated D latch, the Q output always equals the D input
(a) before the enable pulse (b) during the enable pulse
(c) immediately after the enable pulse (d) answers (b) and (c)
- Like the latch, the flip-flop belongs to a category of logic circuits known as
(a) monostable multivibrators (b) bistable multivibrators
(c) astable multivibrators (d) one-shots
- The purpose of the clock input to a flip-flop is to
(a) clear the device
(b) set the device
(c) always cause the output to change states
(d) cause the output to assume a state dependent on the controlling (J - K or D) inputs.
- For an edge-triggered D flip-flop,
(a) a change in the state of the flip-flop can occur only at a clock pulse edge
(b) the state that the flip-flop goes to depends on the D input
(c) the output follows the input at each clock pulse
(d) all of these answers
- A feature that distinguishes the J-K flip-flop from the D flip-flop is the
(a) toggle condition (b) preset input
(c) type of clock (d) clear input
- A flip-flop is in the toggle condition when
(a) $J = 1, K = 0$ (b) $J = 1, K = 1$
(c) $J = 0, K = 0$ (d) $J = 0, K = 1$
- A J-K flip-flop with $J = 1$ and $K = 1$ has a 10 kHz clock input. The Q output is
(a) constantly HIGH (b) constantly LOW
(c) a 10 kHz square wave (d) a 5 kHz square wave
- A one-shot is a type of
(a) monostable multivibrator (b) astable multivibrator (c) timer
(d) answers (a) and (c) (e) answers (b) and (c)
- The output pulse width of a nonretriggerable one-shot depends on
(a) the trigger intervals (b) the supply voltage
(c) a resistor and capacitor (d) the threshold voltage
- An astable multivibrator
(a) requires a periodic trigger input (b) has no stable state
(c) is an oscillator (d) produces a periodic pulse output
(e) answers (a), (b), (c), and (d) (f) answers (b), (c), and (d) only

PROBLEMS

Answers to odd-numbered problems are at the end of the chapter.

SECTION 1 A System

- How long can the traffic signal control system remain in the first state?
- How long can the system remain in the fourth state?

3. Write the Boolean expressions for the light outputs MR, MY, MG, SR, SY, and SG in terms of G_0 and G_1 .
4. Using the expressions developed in Problem 3, show the logic diagram for the light outputs.

SECTION 2 Latches

5. If the waveforms in Figure 67 are applied to an active-LOW input S-R latch, draw the resulting Q output waveform in relation to the inputs. Assume that Q starts LOW.

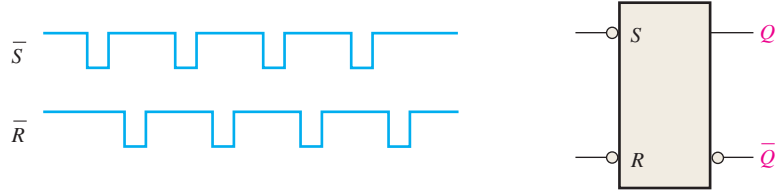


FIGURE 67

6. Solve Problem 5 for the input waveforms in Figure 68 applied to an active-HIGH S-R latch.

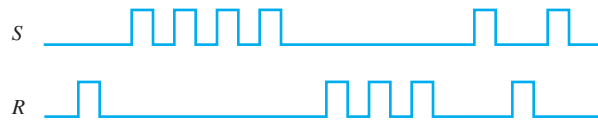


FIGURE 68

7. Solve Problem 5 for the input waveforms in Figure 69.



FIGURE 69

8. For a gated S-R latch, determine the Q and \bar{Q} outputs for the inputs in Figure 70. Show them in proper relation to the enable input. Assume that Q starts LOW.
9. Solve Problem 8 for the inputs in Figure 71.

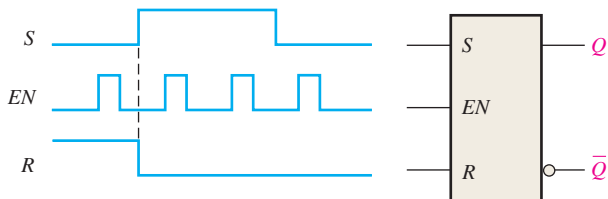


FIGURE 70

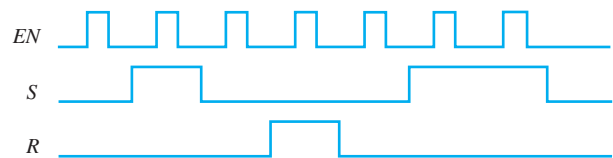


FIGURE 71

10. Solve Problem 8 for the inputs in Figure 72.
11. For a gated D latch, the waveforms shown in Figure 73 are observed on its inputs. Draw the timing diagram showing the output waveform you would expect to see at Q if the latch is initially RESET.

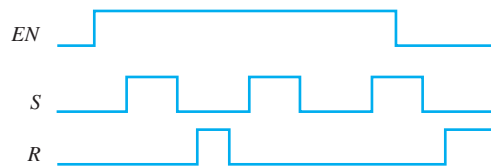


FIGURE 72

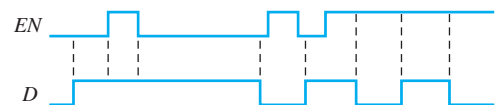


FIGURE 73

SECTION 3 Flip-Flops

12. Two edge-triggered D flip-flops are shown in Figure 74. If the inputs are as shown, draw the Q output of each flip-flop relative to the clock, and explain the difference between the two. The flip-flops are initially RESET.

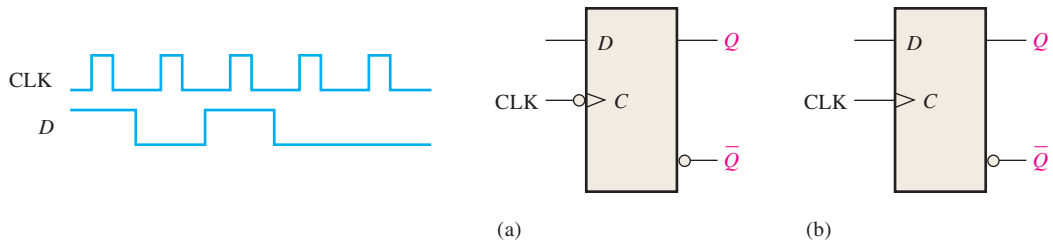


FIGURE 74

13. The Q output of an edge-triggered D flip-flop is shown in relation to the clock signal in Figure 75. Determine the input waveform on the D input that is required to produce this output if the flip-flop is a positive edge-triggered type.

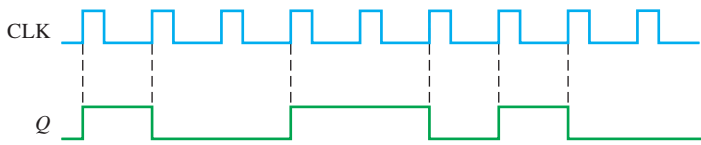


FIGURE 75

14. Draw the Q output relative to the clock for a D flip-flop with the inputs as shown in Figure 76. Assume positive edge-triggering and Q initially LOW.
15. Solve Problem 14 for the inputs in Figure 77.

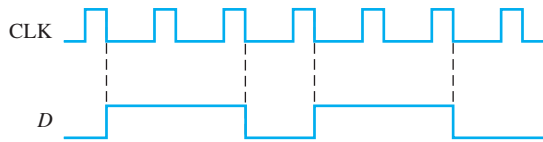


FIGURE 76

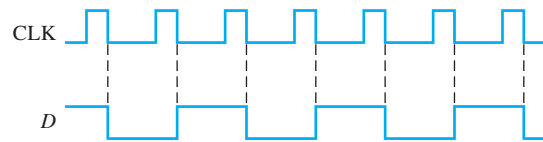


FIGURE 77

16. For a positive edge-triggered J-K flip-flop with inputs as shown in Figure 78, determine the Q output relative to the clock. Assume that Q starts LOW.
17. Solve Problem 16 for the inputs in Figure 79.

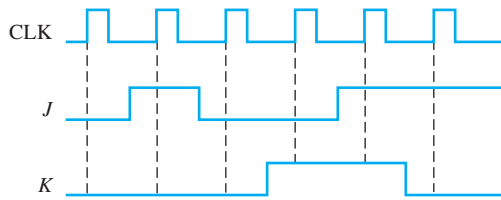


FIGURE 78

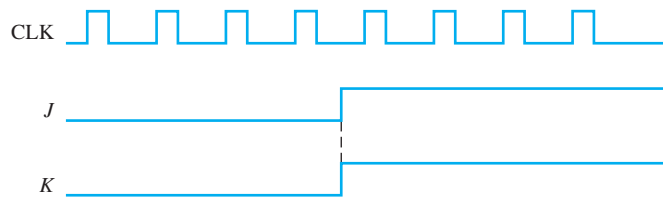


FIGURE 79

18. Determine the Q waveform relative to the clock if the signals shown in Figure 80 are applied to the inputs of the J-K flip-flop. Assume that Q is initially LOW.

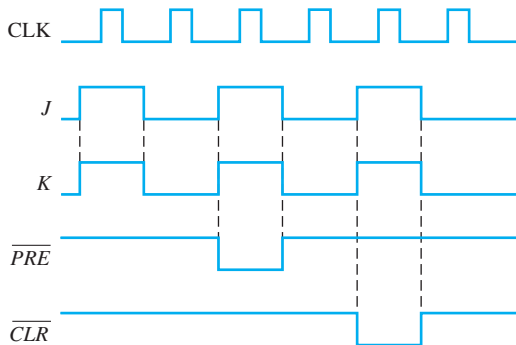
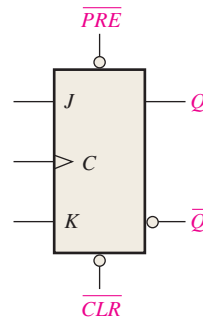


FIGURE 80



19. For a negative edge-triggered J-K flip-flop with the inputs in Figure 81, develop the Q output waveform relative to the clock. Assume that Q is initially LOW.

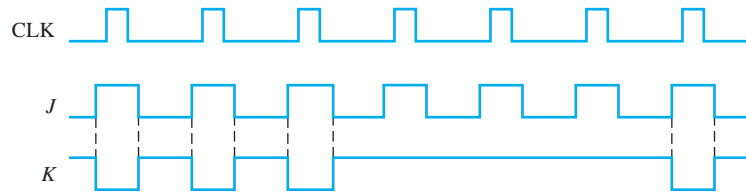


FIGURE 81

20. The following serial data are applied to the flip-flop through the AND gates as indicated in Figure 82. Determine the resulting serial data that appear on the Q output. There is one clock pulse for each bit time. Assume that Q is initially 0 and that \overline{PRE} and \overline{CLR} are HIGH. Rightmost bits are applied first.

J_1 : 1 0 1 0 0 1 1; J_2 : 0 1 1 1 0 1 0; J_3 : 1 1 1 1 0 0 0; K_1 : 0 0 0 1 1 1 0; K_2 : 1 1 0 1 1 0 0; K_3 : 1 0 1 0 1 0 1

21. For the circuit in Figure 82, complete the timing diagram in Figure 83 by showing the Q output (which is initially LOW). Assume \overline{PRE} and \overline{CLR} remain HIGH.

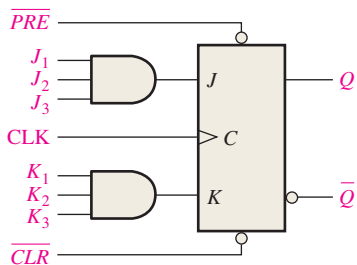


FIGURE 82

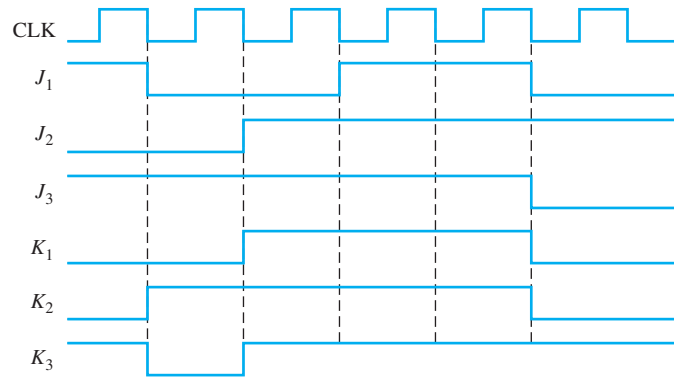


FIGURE 83

22. Solve Problem 21 with the same J and K inputs but with the \overline{PRE} and \overline{CLR} inputs as shown in Figure 84 in relation to the clock.

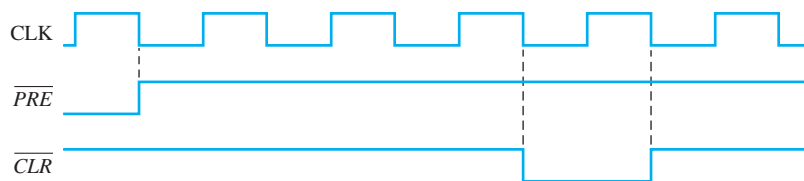


FIGURE 84

23. A D flip-flop is connected as shown in Figure 85. Determine the Q output in relation to the clock. What specific function does this device perform?

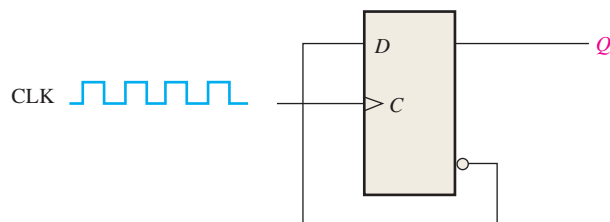


FIGURE 85

24. For the circuit in Figure 86, develop a timing diagram for eight clock pulses, showing the Q_A and Q_B outputs in relation to the clock.

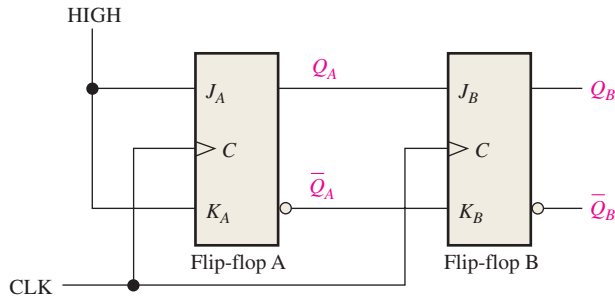


FIGURE 86

SECTION 4 Flip-Flop Operating Characteristics

25. What determines the power dissipation of a flip-flop?
26. Typically, a manufacturer’s data sheet specifies four different propagation delay times associated with a flip-flop. Name and describe each one.
27. The data sheet of a certain flip-flop specifies that the minimum HIGH time for the clock pulse is 30 ns and the minimum LOW time is 37 ns. What is the maximum operating frequency?
28. The flip-flop in Figure 87 is initially RESET. Show the relation between the Q output and the clock pulse if propagation delay t_{PLH} (clock to Q) is 8 ns.
29. The direct current required by a particular flip-flop that operates on a +5 V dc source is found to be 10 mA. A certain digital device uses 15 of these flip-flops. Determine the current capacity required for the +5 V dc supply and the total power dissipation of the system.
30. For the circuit in Figure 86, determine the maximum frequency of the clock signal for reliable operation if the set-up time for each flip-flop is 2 ns and the propagation delays (t_{PLH} and t_{PHL}) from clock to output are 5 ns for each flip-flop.

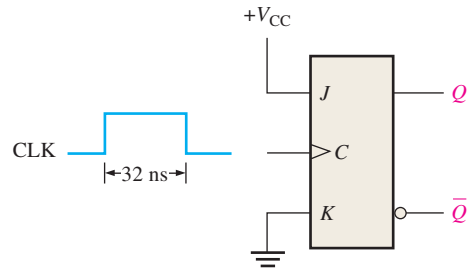


FIGURE 87

SECTION 5 Timers

31. Determine the pulse width of a 555 timer configured as a one-shot if the external resistor is 3.3 kΩ and the external capacitor is 2000 pF.
32. An output pulse of 5 μs duration is to be generated by a 555 operating as a one-shot. Using a capacitor of 10,000 pF, determine the value of external resistance required.
33. Create a one-shot, using a 555 timer that will produce a 0.25 s output pulse.
34. A 555 timer is configured to run as an astable multivibrator as shown in Figure 88. Determine its frequency.
35. Determine the values of the external resistors for a 555 timer used as an astable multivibrator with an output frequency of 20 kHz, if the external capacitor C is 0.002 μF and the duty cycle is to be approximately 75%.

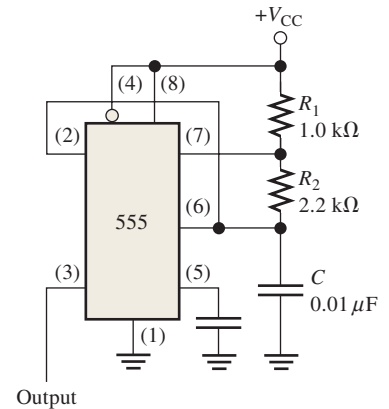


FIGURE 88

SECTION 6 Bistable Logic with VHDL and Verilog

36. Given the following VHDL statement:

```
Q <= J1 nand NotQ;
```

Create the functionally equivalent statement replacing the **nand** operator with the **and** operator.

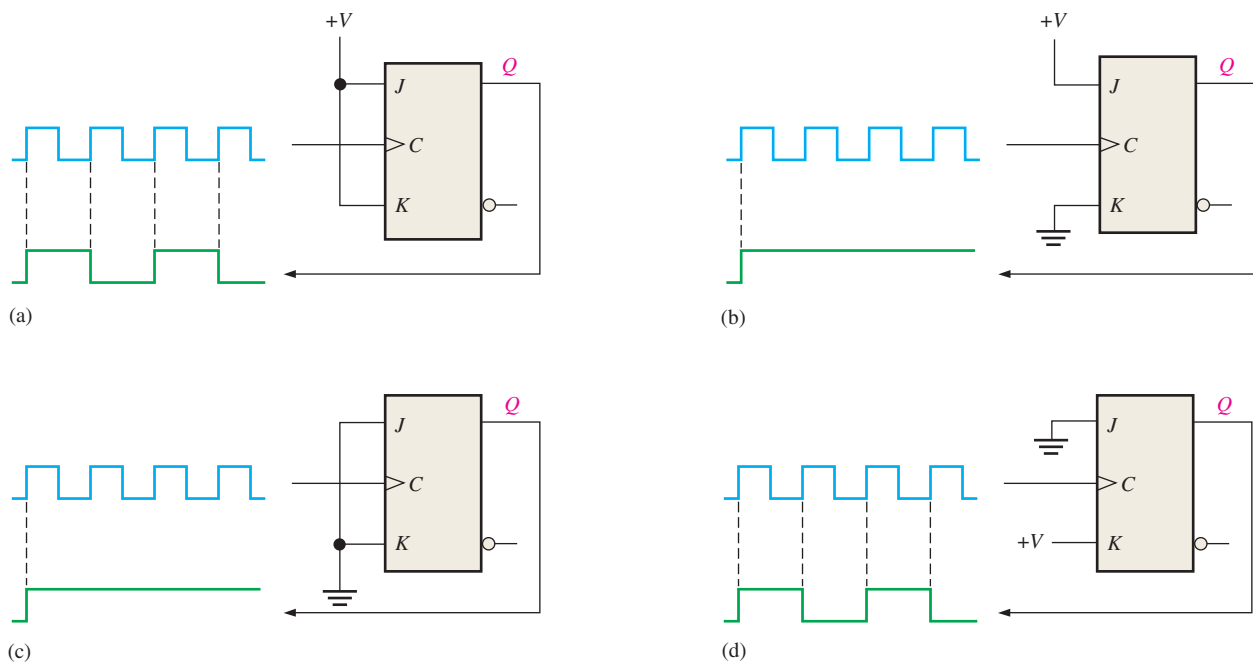
37. In Verilog, the **reg** data type is used to describe the internal identifiers S and R in the DFlipFlop description in Figure 52. Name an equivalent VHDL data type.
38. In the VHDL JKFlipFlop code in Figure 53, a **process** block structure contains the functional code defining the behavior of the flip flop. What Verilog code structure performs this functionality?
39. Name the Verilog keyword required to set the result of a Boolean equation to an output identifier.

SECTION 7 Traffic Signal Control System with VHDL and Verilog

40. In the programming model in Figure 55, what does the FreqDivide block do?
41. List the statements in the VHDL program for the TimerCircuits that result in the 4 s and 25 s time intervals.
42. Repeat Problem 41 for the Verilog program.
43. Write the lines of code in both VHDL and Verilog that describe the sequential logic.
44. What numerical value would be assigned to SetCount in the FreqDivide component of the traffic signal control system if the system clock were reduced to 12 Hz?
45. We would like to add an additional state to the StateDecoder component. Explain the modification required to introduce a fifth output state S5.
46. Can the program TrafficLights be simplified if a 1 Hz clock replaced the 24 MHz system clock? If so, explain the required TrafficLights program source modifications.
47. In the traffic signal control system, a “Walk/Don’t Walk” sign is added to the main and side streets. The “Walk” and “Don’t Walk” displays are to have separate inputs; one for “Walk” and a second for “Don’t”. What changes to the TrafficLights program are needed to operate the new signs?

SECTION 8 Troubleshooting

48. The flip-flop in Figure 89 is tested under all input conditions as shown. Is it operating properly? If not, what is the most likely fault?

**FIGURE 89**

49. A quad NAND gate IC is used to construct a gated S-R latch on a protoboard in the lab as shown in Figure 90. The schematic in part (a) is used to connect the circuit in part (b). When you try to operate the latch, you find that the Q output stays HIGH no matter what the inputs are. Determine the problem.
50. Determine if the flip-flop in Figure 91 is operating properly, and if not, identify the most probable fault.
51. The parallel data storage circuit in Figure 92 does not operate properly. To check it out, you first make sure that V_{CC} and ground are connected, and then you apply LOW levels to all the D inputs and pulse the clock line. You check the Q outputs and find them all to be LOW; so far, so good. Next you apply HIGHS to all the D inputs and again pulse the clock line. When you check the Q outputs, they are still all LOW. What is the problem, and what procedure will you use to isolate the fault to a single device?

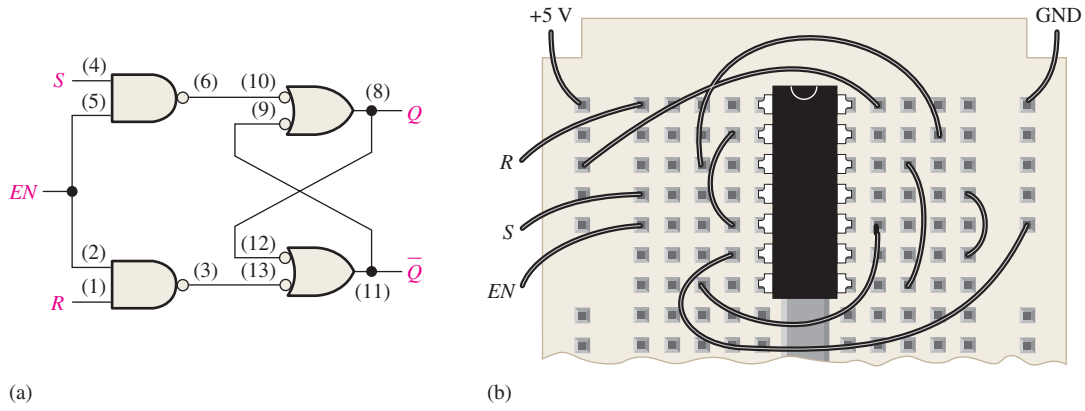


FIGURE 90

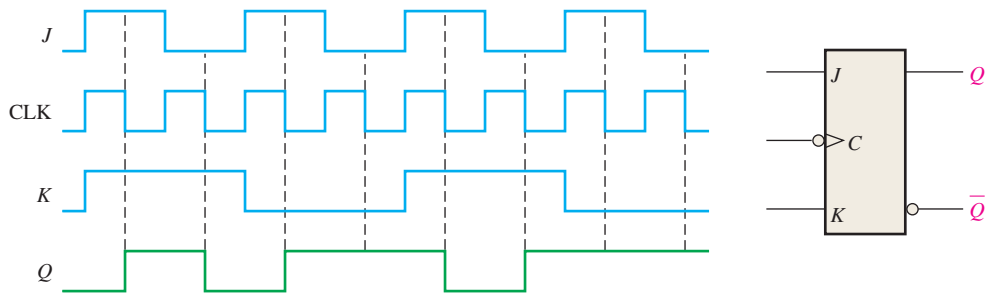


FIGURE 91

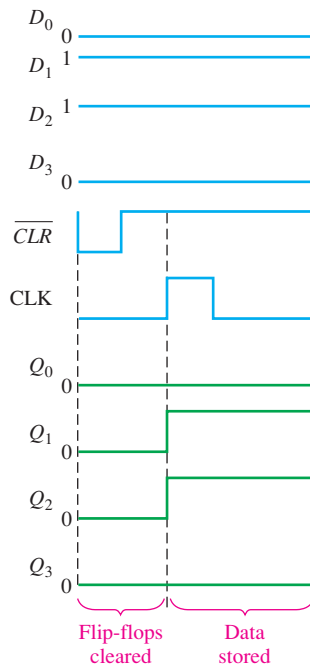
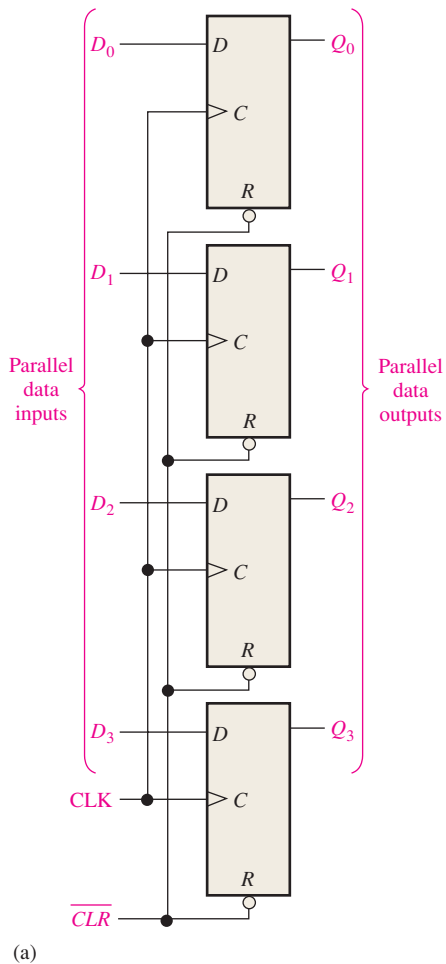


FIGURE 92 Example of flip-flops used in a basic register for parallel data storage.

52. The flip-flop circuit in Figure 93(a) is used to generate a binary count sequence. The gates form a decoder that is supposed to produce a HIGH when a binary zero or a binary three state occurs (00 or 11). When you check the Q_A and Q_B outputs, you get the display shown in part (b), which reveals glitches on the decoder output (X) in addition to the correct pulses. What is causing these glitches, and how can you eliminate them?

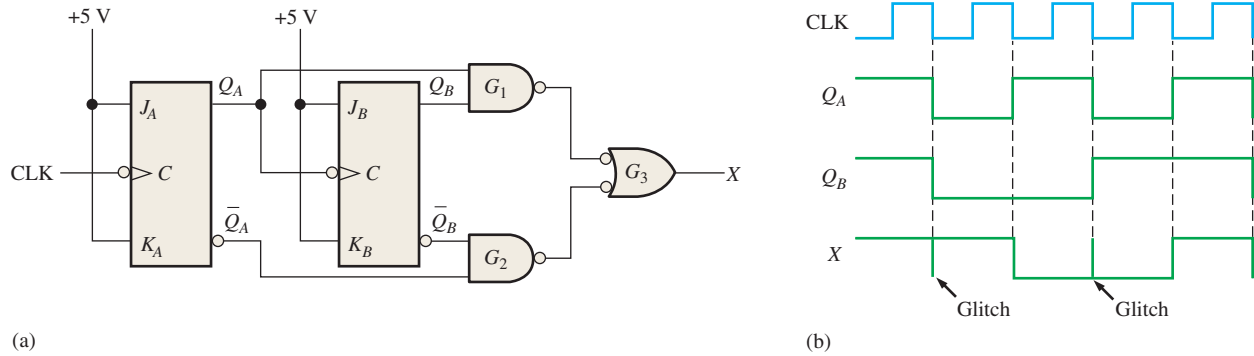


FIGURE 93

53. Determine the Q_A , Q_B and X outputs over six clock pulses in Figure 93(a) for each of the following faults in the bipolar (TTL) circuits. Start with both Q_A and Q_B LOW.
- J_A input open
 - K_B input open
 - Q_B output open
 - clock input to flip-flop B shorted
 - gate G_2 output open
54. Two one-shot ICs are connected on a circuit board as shown in Figure 94. After observing the oscilloscope display, do you conclude that the circuit is operating properly? If not, what is the most likely problem?

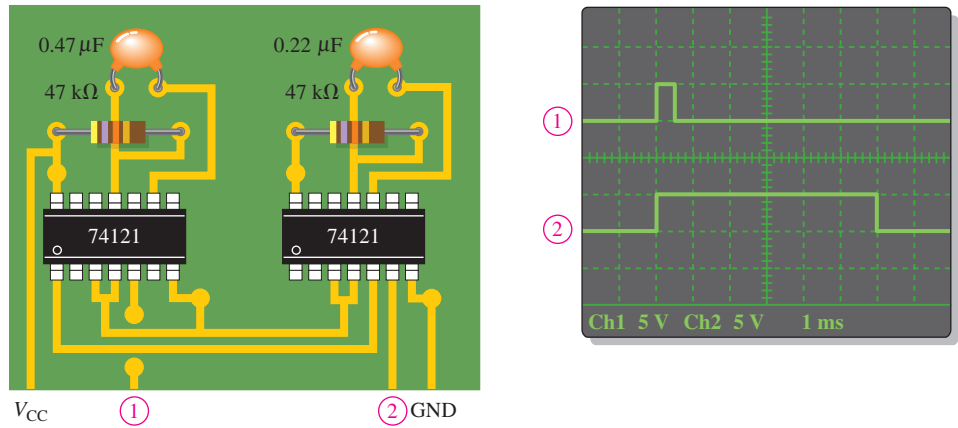


FIGURE 94

Special Problems

55. Implement a basic counting circuit that produces a binary sequence from zero through seven by using negative edge-triggered J-K flip-flops.
56. In the shipping department of a softball factory, the balls roll down a conveyor and through a chute single file into boxes for shipment. Each ball passing through the chute activates a switch circuit that produces an electrical pulse. The capacity of each box is 32 balls. Implement a logic circuit to indicate when a box is full so that an empty box can be moved into position.
57. List the changes that would be necessary in the traffic signal control system to add a 15 s left turn arrow for the main street. The turn arrow will occur after the red light and prior to the green light. Modify the state diagram in Figure 2 to show these changes.

MULTISIM TROUBLESHOOTING PRACTICE

MULTISIM



58. Open file P06-58 and follow the instructions given there.
59. Open file P06-59 and follow the instructions given there.
60. Open file P06-60 and follow the instructions given there.
61. Open file P06-61 and follow the instructions given there.
62. Open file P06-62 and follow the instructions given there.

ANSWERS TO SECTION CHECKUPS

SECTION 1 A System

1. For 25 s (T_L) or as long as there is no vehicle on the side street (\bar{V}_s)
2. For 4 s (T_S)
3. Main will stay red for up to 25 s if there is a vehicle on the side street ($T_L V_s$).

SECTION 2 Latches

1. Three types of latches are S-R, gated S-R, and gated D.
2. $SR = 00$, NC; $SR = 01$, $Q = 0$; $SR = 10$, $Q = 1$; $SR = 11$, invalid
3. $Q = 1$

SECTION 3 Flip-Flops

1. The output of a gated D latch can change any time the gate enable (EN) input is active. The output of an edge-triggered D flip-flop can change only on the triggering edge of a clock pulse.
2. The output of the D flip-flop follows the D input on each clock pulse. The output of the J-K flip-flop depends on both of the states of the J and K inputs.
3. Output Q goes HIGH on the trailing edge of the first clock pulse, LOW on the trailing edge of the second pulse, HIGH on the trailing edge of the third pulse, and LOW on the trailing edge of the fourth pulse.
4. For divide-by-2 operation, the flip-flop must toggle ($J = 1$, $K = 1$).
5. Six flip-flops are used in a divide-by-64 device.

SECTION 4 Flip-Flop Operating Characteristics

1. (a) Set-up time is the time required for input data to be present before the triggering edge of the clock pulse.
(b) Hold time is the time required for data to remain on the inputs after the triggering edge of the clock pulse.
2. The flip-flop with $t_{PHL} = 17$ ns

SECTION 5 Timers

1. A nonretriggerable one-shot times out before it can respond to another trigger input. A retriggerable one-shot responds to each trigger input.
2. Pulse width is set with external R and C components.
3. 11 ms.
4. An astable multivibrator has no stable state. A monostable multivibrator has one stable state.
5. Duty cycle = $(15 \text{ ms}/20 \text{ ms})100\% = 75\%$

SECTION 6 Bistable Logic with VHDL and Verilog

1. VHDL specifies edge-triggered operation with the **if rising_edge** term.
2. Verilog specifies edge-triggered operation with **@(posedge Clock)**.
3. VHDL; **if falling_edge**; Verilog: **@(negedge Clock)**
4. ! is NOT, || is OR, and && is AND.

SECTION 7 Traffic Signal Control System with VHDL and Verilog

1. The program blocks are TimerCircuits, FreqDivide, SequentialLogic, and StateDecoder.
2. The program blocks listed in answer 1 are specified as components in the complete system program. The two timer triggers and the six light control outputs are specified in terms of the state decoder output using Boolean expressions.
3. A noticeable difference is that Verilog generally provides for shorter programs.

SECTION 8 Troubleshooting

1. Multisim software simulation; development software simulation.
2. Test one-of-a-kind circuit board using traditional test methods with lab instruments.
3. Production test using bed-of-nails, flying probe, or boundary scan techniques.

ANSWERS TO RELATED PROBLEMS FOR EXAMPLES

1. The Q output is the same as shown in Figure 11(b).
2. See Figure 95.
3. See Figure 96.

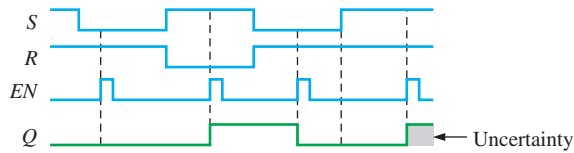


FIGURE 95

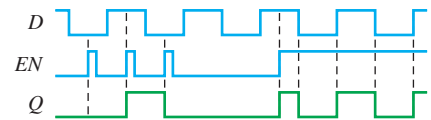


FIGURE 96

4. See Figure 97.
5. See Figure 98.

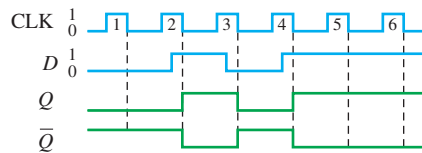


FIGURE 97

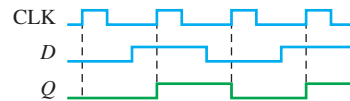


FIGURE 98

6. See Figure 99.
7. See Figure 100.

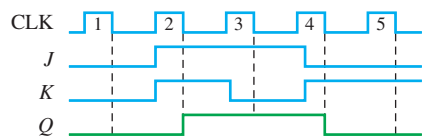


FIGURE 99

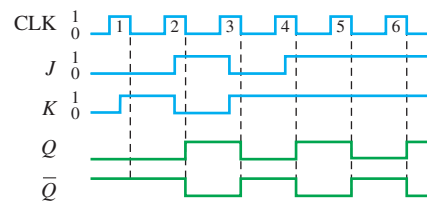


FIGURE 100

- 8 See Figure 101.
- 9 See Figure 102.

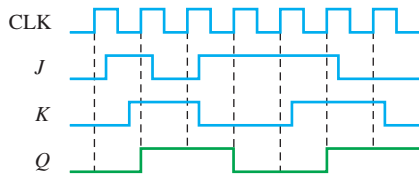


FIGURE 101

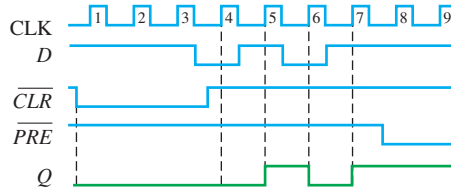


FIGURE 102

- 10 $2^5 = 32$. Five flip-flops are required.
- 11 Sixteen states require four flip-flops ($2^4 = 16$).
- 12 $R_1 = 91 \text{ k}\Omega$
- 13 $R_2 \cong 2.2 \text{ k}\Omega$

ANSWERS TO TRUE/FALSE QUIZ

- 1. T 2. F 3. T 4. T 5. F 6. T
- 7. T 8. F 9. T 10. T

ANSWERS TO SELF-TEST

- 1. (a) 2. (c) 3. (d) 4. (b) 5. (d) 6. (d)
- 7. (a) 8. (b) 9. (d) 10. (d) 11. (c) 12. (f)

ANSWERS TO ODD-NUMBERED PROBLEMS

- 1. The system remains in the first state for 25 s or as long as there is no vehicle on the side street.
- 3. $MR = G_1G_0 + G_1\bar{G}_0$ $MY = \bar{G}_1G_0$ $MG = \bar{G}_1\bar{G}_0$
 $SR = \bar{G}_1\bar{G}_0 + \bar{G}_1G_0$ $SY = G_1\bar{G}_0$ $SG = G_1G_0$

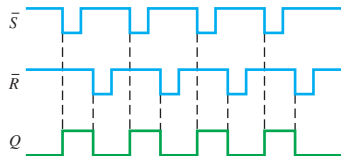


FIGURE P-34

- 5. See Figure P-34.

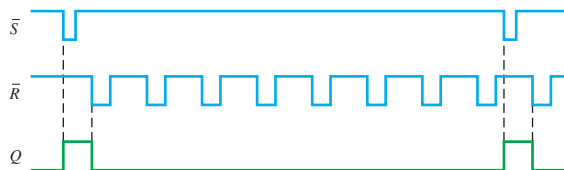


FIGURE P-35

7. See Figure P-35.

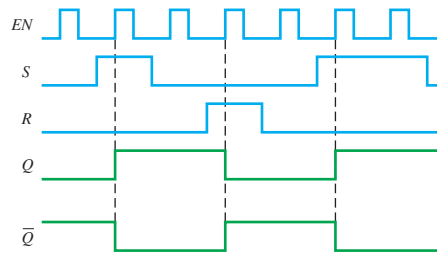


FIGURE P-36

9. See Figure P-36.

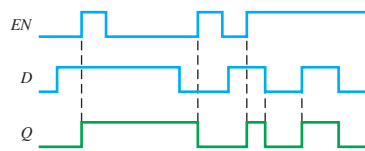


FIGURE P-37

11. See Figure P-37.

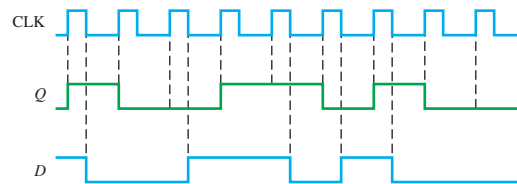


FIGURE P-38

13. See Figure P-38.

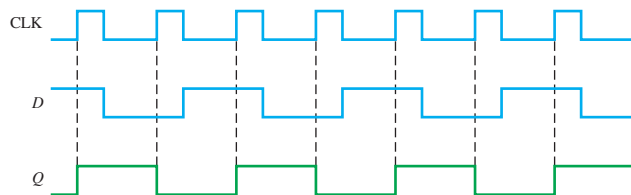


FIGURE P-39

15. See Figure P-39.

17. See Figure P-40.

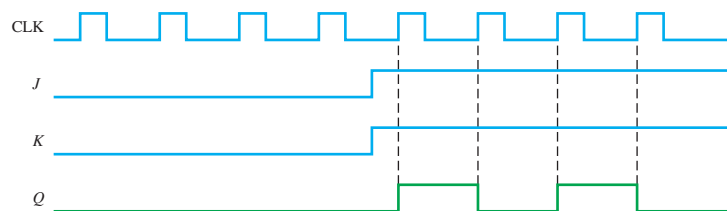


FIGURE P-40

19. See Figure P-41.

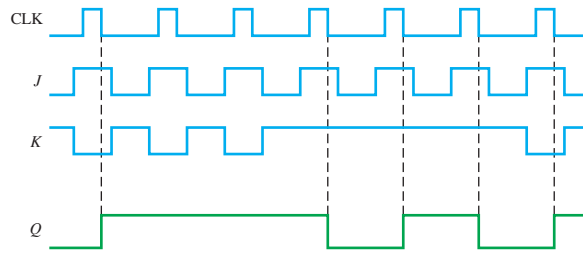


FIGURE P-41

21. See Figure P-42.

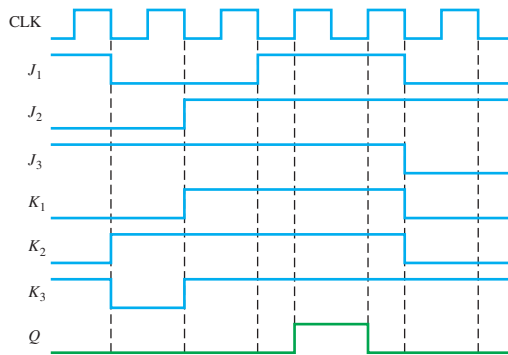


FIGURE P-42

23. divide-by-2; see Figure P-43.

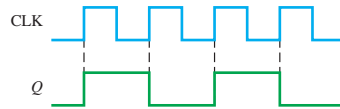


FIGURE P-43

25. Direct current and dc supply voltage

27. 14.9 MHz

29. 150 mA, 750 mW

31. 7.26 μ s

33. $C_1 = 1 \mu$ F, $R_1 = 227 \text{ k}\Omega$ (use 220 k Ω). See Figure P-44.

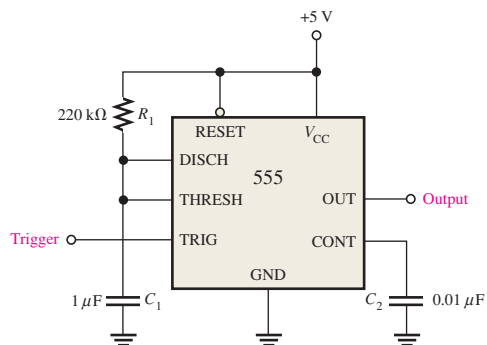


FIGURE P-44

35. $R_1 = 18 \text{ k}\Omega, R_2 = 9.1 \text{ k}\Omega$.
37. **signal**
39. **assign**
41. SetCountLong ≤ 25 ; SetCountShort ≤ 4 ;
43. VHDL: $D1 \leq (G0 \text{ and not } TS) \text{ or } (G1 \text{ and } TS)$;
 $D0 \leq (\text{not } G1 \text{ and not } TL \text{ and } VS) \text{ or } (\text{not } G1 \text{ and } G0) \text{ or } (G0 \text{ and } TL \text{ and } VS)$;
 Verilog: **assign** $D1 = (G0 \ \&\& \ !TS) \ \|\ (G1 \ \&\& \ TS)$;
assign $D0 = (!G1 \ \&\& \ !TS \ \&\& \ VS) \ \|\ (!G1 \ \&\& \ G0) \ \|\ (G0 \ \&\& \ TL \ \&\& \ VS)$;
45. Answers may vary.
1. An additional Gray code bit G3 is added. Additionally, the Gray code input must recycle from count 110 back to 000, requiring a truncated sequence.
 2. Additional output identifier 55 is created.
 3. Combinational logic for S1, S2, S3, S4, and S5 are modified to incorporate the following truncated 3-bit Gray code sequence:
 - State 1 (S1): $G2 = 0, G1 = 0, G0 = 0$
 - State 2 (S2): $G2 = 0, G1 = 0, G0 = 1$
 - State 3 (S3): $G2 = 0, G1 = 1, G0 = 1$
 - State 4 (S4): $G2 = 0, G1 = 1, G0 = 0$
 - State 5 (S5): $G2 = 1, G1 = 1, G0 = 0$
47. Changes are
1. The Walk portion of the sign is simply wired to a HIGH.
 2. Two new output variables are added: DontMain and DontSide are applied to the Don't input of the sign.
 3. Output DontMain is assigned the logic statement for SG. Output DontSide is assigned the logic statement for MG.
49. The wire from pin 6 to pin 10 and the ground wire are reversed on the protoboard.
51. \overline{CLR} shorted to ground.
53. See Figure P-45. Delays not shown.

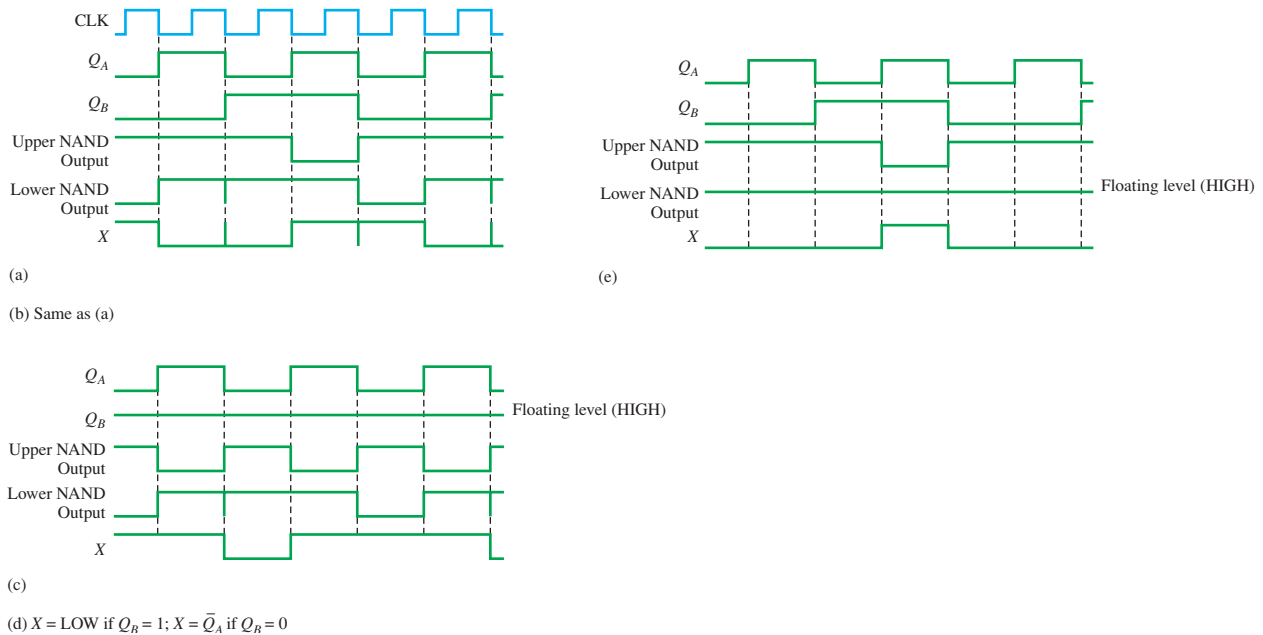


FIGURE P-45

55. See Figure P-46.

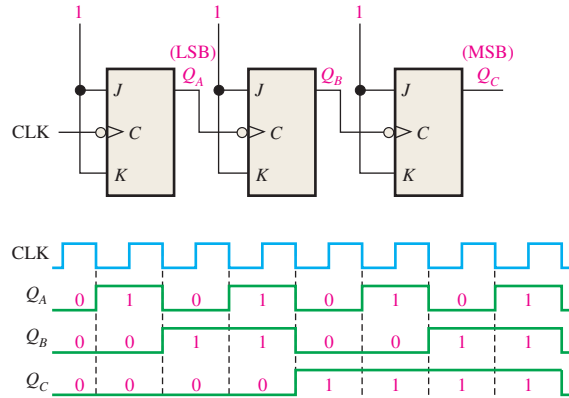


FIGURE P-46

57. Changes required for the system to incorporate a 15 s left turn signal on main:

1. Change the 2-bit Gray code sequence to a 3-bit sequence.
2. Add decoding logic to the State Decoder to decode the turn signal state.
3. Change the Output Logic to incorporate the turn signal output.
4. Change the Trigger Logic to incorporate a trigger output for the turn signal timer.
5. Add a 15 second timer.

See Figure P-47.

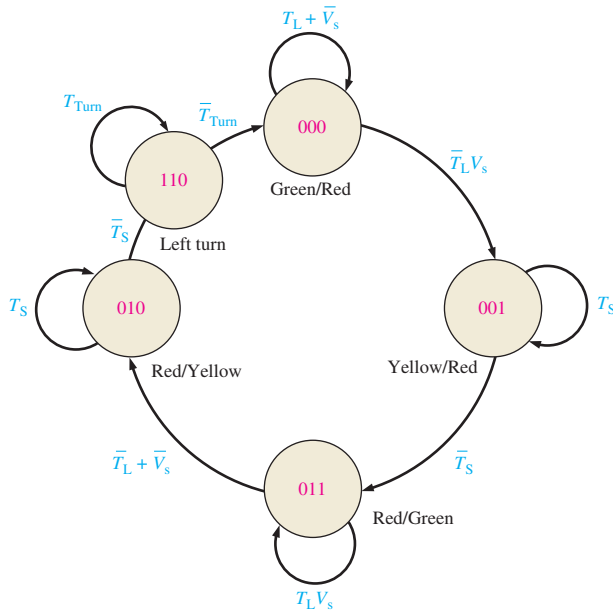


FIGURE P-47

59. **Circuit fault:** Line to K input is shorted to V_{CC} .

Predicted effect of fault: If line to J input is LOW, Q output will go and remain LOW and notQ output will go and remain HIGH. If line to J input is HIGH, Q and notQ will toggle.

Observed effect of introduced fault: If line to J input is LOW, Q output will go and remain LOW and notQ output will go and remain HIGH. If line to J input is HIGH, Q and notQ will toggle.

61. **Observed operation:** Pulse width of one-shot is $690 \mu s$ rather than $6.9 \mu s$.

Suspected fault: $1 \text{ k}\Omega$ resistor accidentally used in place of $10 \text{ k}\Omega$ timing resistor, or a $0.1 \mu F$ capacitor is used in place of the $1 \mu F$ timing capacitor.

Effect of introduced fault: Pulse width of one-shot is $690 \mu s$ rather than $6.9 \mu s$.

SHIFT REGISTERS

SHIFT REGISTERS

OUTLINE

- 1 A System
- 2 Basic Shift Register Operations
- 3 Types of Shift Registers
- 4 Bidirectional Shift Registers
- 5 Shift Register Counters
- 6 Security System with VHDL and Verilog
- 7 Troubleshooting

OBJECTIVES

- Use shift registers in a system
- Identify the basic forms of data movement in shift registers
- Explain how serial in/serial out, serial in/parallel out, parallel in/serial out, and parallel in/parallel out shift registers operate
- Describe how a bidirectional shift register operates
- Determine the sequence of a Johnson counter
- Set up a ring counter to produce a specified sequence
- Construct a ring counter from a shift register
- Use a shift register as a time-delay device

- Use a shift register to implement a serial-to-parallel data converter
- Describe a basic shift-register-controlled keyboard encoder
- Describe a system using VHDL and Verilog

KEY TERMS

Register
Stage

Load
Bidirectional

INTRODUCTION

Shift registers are a type of sequential logic circuit closely related to digital counters. Registers are used primarily for the storage of digital data and typically do not possess a characteristic internal sequence of states as do counters. There are exceptions, however, and these are covered in Section 5.

In this chapter a system using shift registers is introduced. The basic types of shift registers are studied and several applications are presented. Also, troubleshooting methods are discussed, and implementation of a system using VHDL and Verilog is presented.

VISIT THE WEBSITE

Study aids for this chapter are available at
<http://pearsonhighered.com/floyd>

1 A SYSTEM

This section provides an introduction to the use of shift registers for temporarily storing and shifting data in a system. A security system that provides coded access to a secured area is developed. The system consists of a keypad, security code logic, and code-selection logic. When security code is stored in the system, access is achieved by entering the correct code on a keypad.

After completing this section, you should be able to

- Explain the overall operation of the system
- Describe how shift registers are used for both parallel and serial storage and movement of data
- Explain how other devices such as the one-shot, the encoder, and the comparator are used in the system

A block diagram for the security system is shown in Figure 1. The system consists of the security code logic, the code-selection logic, and the keypad. The keypad is a standard numeric keypad.

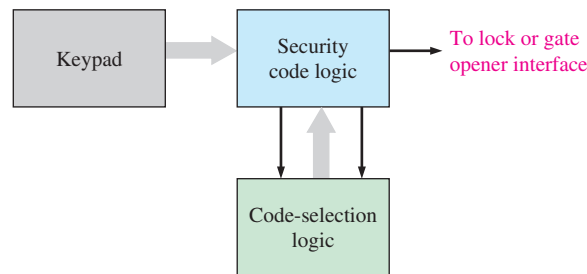


FIGURE 1 Block diagram of the security system.

Basic Operation

A 4-digit entry code is set with user-accessible DIP switches. Initially pressing the # key sets up the system for the first digit in the code. For entry, the code is entered one digit at a time on the keypad and converted to a BCD code for processing by the security code logic. If the entered code agrees with the stored code, the output activates the access mechanism and allows the door or gate, depending on the type of area that is secured, to be opened.

The Security Code Logic

The security code logic compares the code entered on the keypad with the predetermined code. A logic diagram of the security code logic with keypad is shown in Figure 2.

In order to gain entry, first the # key on the keypad is pressed to enable the one-shots to be triggered, thus initializing the 8-bit shift register C with a preset pattern (00010000). Next the four digits of the code are entered in proper sequence on the keypad. As each digit is entered, it is converted to BCD by the decimal-to-BCD encoder, and a clock pulse is produced by one-shot A that shifts the 4-bit code into register A. The one-shot is triggered by a transition on the output of the OR gate when a key is pressed. At the same time, the corresponding BCD digit from the code-selection logic is shifted into register B. Also, one-shot B is triggered after one-shot A to provide a delayed clock pulse for register C to serially shift the preloaded pattern (00010000). The left-most three 0s are simply “fillers” and serve no purpose in the operation of the system. The outputs of registers A and B are applied to the comparator; if the codes are the same, the output of the comparator goes HIGH, placing shift register C in the SHIFT mode.

SHIFT REGISTERS

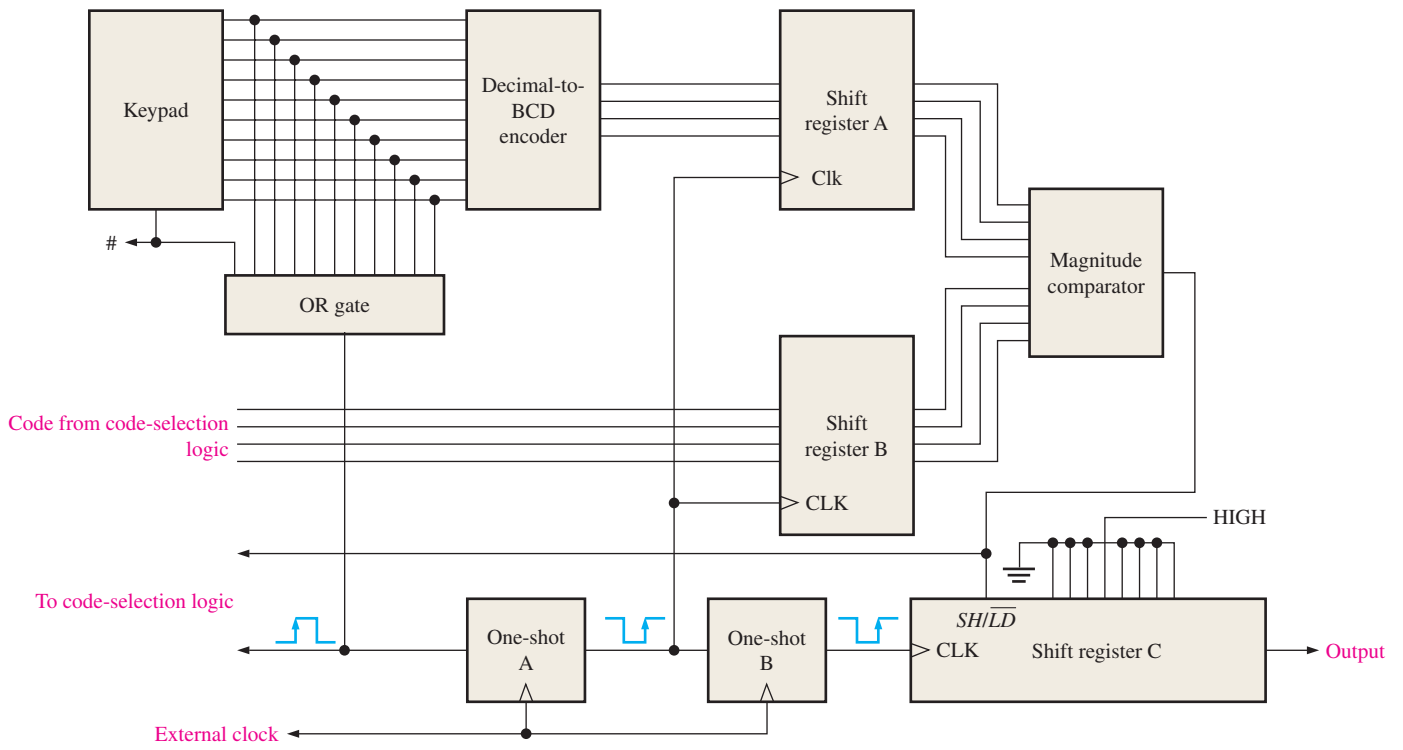


FIGURE 2 Block diagram of the security code logic with keypad.

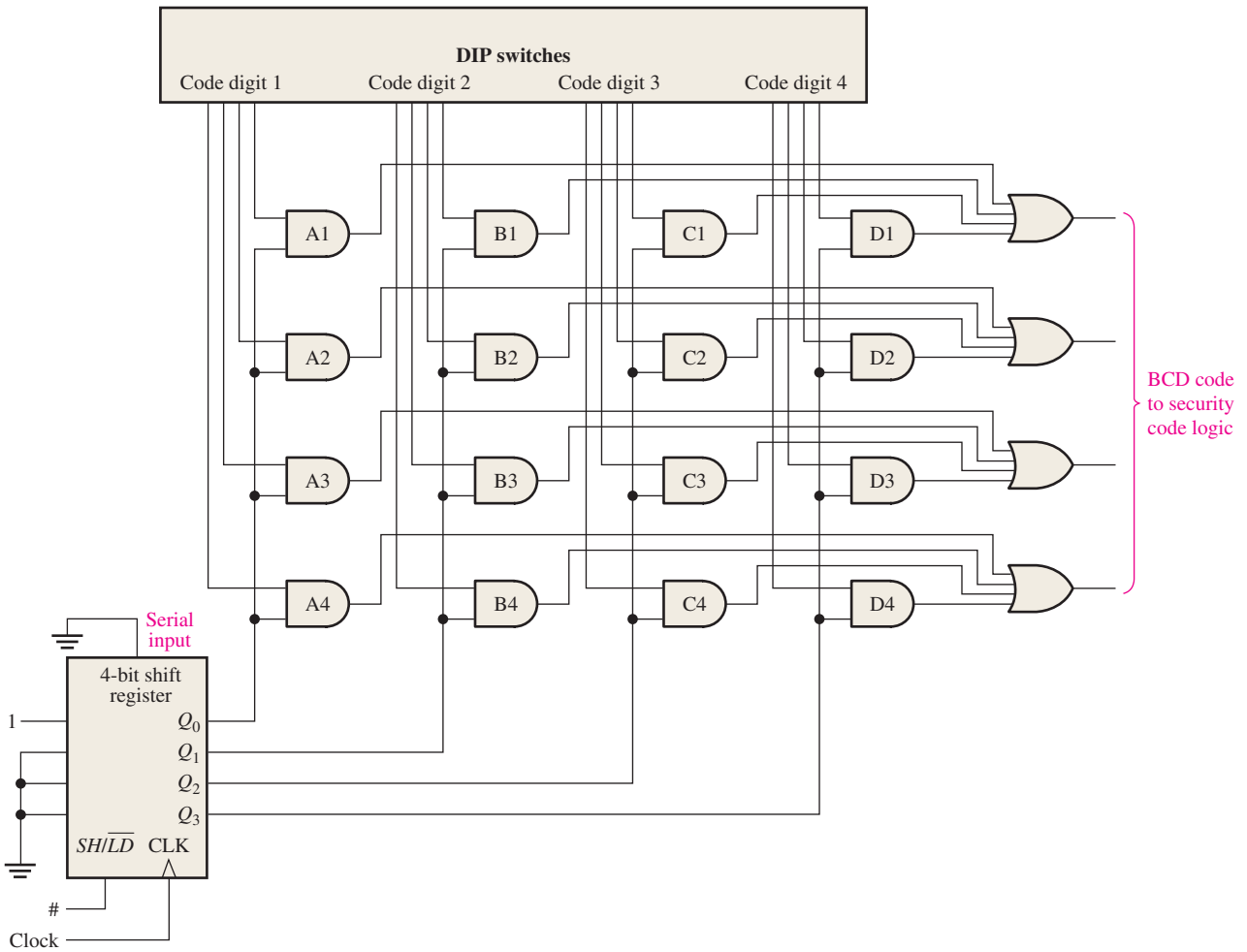


FIGURE 3 Logic diagram of the code-selection logic.

Each time an entered digit agrees with the preset digit, the 1 in shift register C is shifted right one position. On the fourth code agreement, the 1 appears on the output of the shift register and activates the mechanism to unlock the door or open the gate. If the code digits do not agree, the output of the comparator goes LOW, placing shift register C in the LOAD mode so the shift register is reinitialized to the preset pattern (00010000).

The Code-Selection Logic

A logic diagram of the code-selection logic is shown in Figure 3. This part of the system includes a set of DIP switches into which a 4-digit entry code is set. Initially pressing the # key sets up the system for the first digit in the code by causing a preset pattern to be loaded into shift register C (0001). Initially, the four bits in the first code digit are selected by a HIGH on the Q_0 output of the shift register, enabling the four AND gates labeled A1–A4. As each digit of the code is entered on the keypad, the clock from the security code logic shifts the 1 in the shift register to sequentially enable each set of four AND gates. As a result, the BCD digits in the security code appear sequentially on the outputs. In the security code logic, each of the code digits is compared to the digit entered on the keypad.

SECTION 1 CHECKUP*

1. Explain the purpose of the OR gate in Figure 2.
2. If the digit 4 is entered on the keypad, what appears on the output of register A?
3. Explain the purpose of one-shot B in the security code logic.

*Answers are at the end of the chapter.

2 BASIC SHIFT REGISTER OPERATIONS

Shift registers consist of arrangements of flip-flops and are important in applications involving the temporary storage and the transfer of data in a digital system. A register has no specified sequence of states, except in certain very specialized applications. A register, in general, is used solely for storing and shifting data (1s and 0s) entered into it from an external source and typically possesses no characteristic internal sequence of states.

After completing this section, you should be able to

- Explain how a flip-flop stores a data bit
- Define the storage capacity of a shift register
- Describe the shift capability of a register

A **register*** is a digital circuit with two basic functions: data storage and data movement. The storage capability of a register makes it an important type of memory device. Figure 4 illustrates the concept of storing a 1 or a 0 in a D flip-flop. A 1 is applied to the data input as shown, and a clock pulse is applied that stores the 1 by *setting* the flip-flop. When the 1 on the input is removed, the flip-flop remains in the SET state, thereby storing the 1. A similar procedure applies to the storage of a 0 by *resetting* the flip-flop, as also illustrated in Figure 4.

The *storage capacity* of a register is the total number of bits (1s and 0s) of digital data it can retain. Each **stage** (flip-flop) in a shift register represents one bit of storage capacity; therefore, the number of stages in a register determines its storage capacity.

The *shift capability* of a register permits the movement of data from stage to stage within the register or into or out of the register upon application of clock pulses. Figure 5 illustrates the types of data movement in shift registers. The block represents any arbitrary 4-bit register, and the arrows indicate the direction of data movement.

A register can consist of one or more flip-flops used to store and shift data.

*The bold terms in color are key terms and are included in a Key Term glossary at the end of the chapter.

SHIFT REGISTERS

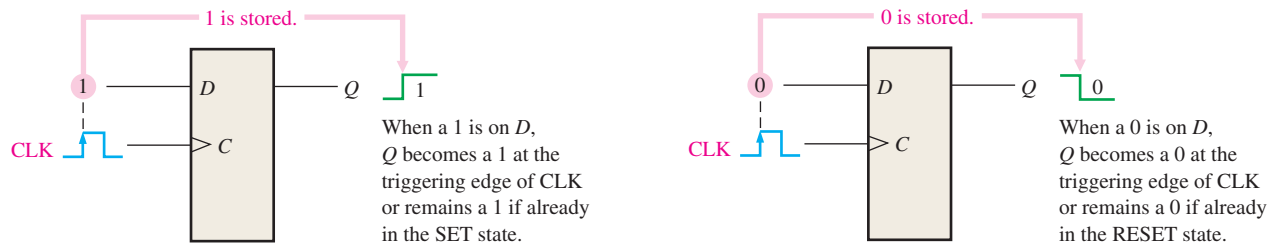


FIGURE 4 The flip-flop as a storage element.

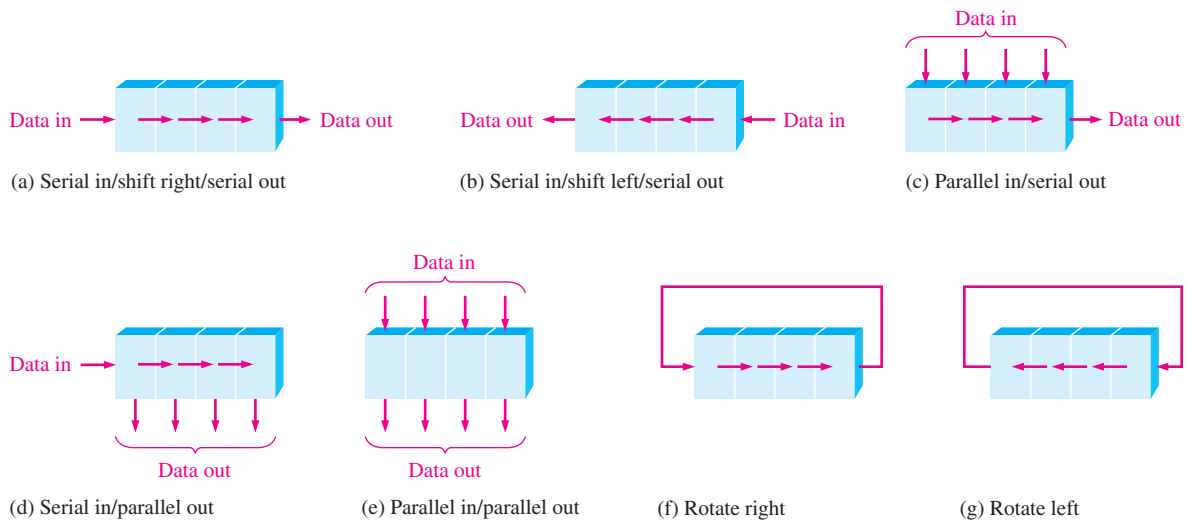


FIGURE 5 Basic data movement in shift registers. (Four bits are used for illustration. The bits move in the direction of the arrows.)

SECTION 2 CHECKUP

1. What two principal functions are performed by a shift register?
2. What indicates when a flip-flop in a register is storing a 1?

3 TYPES OF SHIFT REGISTERS

In this section, four types of shift registers are discussed: serial in/serial out, serial in/parallel out, parallel in/serial out, and parallel in/parallel out.

After completing this section, you should be able to

- Describe the operation of four types of shift register
- Explain how data bits are entered into a shift register
- Describe how data bits are shifted through the register
- Explain how data bits are taken out of a shift register
- Develop and analyze timing diagrams for shift registers

Serial In/Serial Out Shift Registers

The serial in/serial out shift register accepts data serially—that is, one bit at a time on a single line. It produces the stored information on its output also in serial form. Let's first

look at the serial entry of data into a typical shift register. Figure 6 shows a 4-bit device implemented with D flip-flops. With four stages, this register can store up to four bits of data.

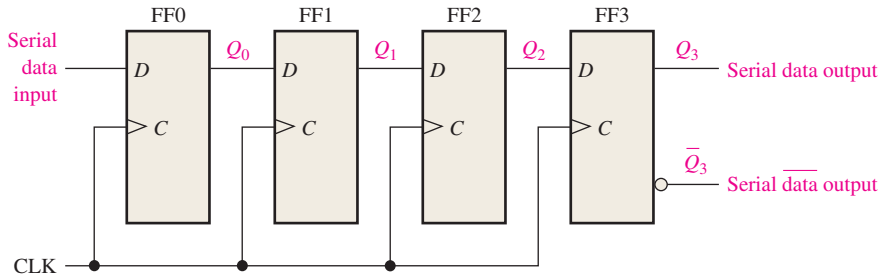


FIGURE 6 Serial in/serial out shift register.

Table 1 shows the entry of the four bits, 1010, into the shift register in Figure 6, beginning with the least significant bit. The register is initially clear. The 0 is put onto the serial data input line, making the data bit $D = 0$ for FF0. When the first clock pulse is applied, FF0 is reset, thus storing the 0.

TABLE 1 • Shifting a 4-bit code into the shift register in Figure 6. Data bits are indicated by a beige screen.				
CLK	FF0 (Q_0)	FF1 (Q_1)	FF2 (Q_2)	FF3 (Q_3)
Initial	0	0	0	0
1	0	0	0	0
2	1	0	0	0
3	0	1	0	0
4	1	0	1	0

Next the second bit, which is a 1, is applied to the serial data input, making $D = 1$ for FF0 and $D = 0$ for FF1 because the D input of FF1 is connected to the Q_0 output. When the second clock pulse occurs, the 1 on the data input is shifted into FF0, causing FF0 to set; and the 0 that was in FF0 is shifted into FF1.

The third bit, a 0, is now put onto the serial data input line, and a third clock pulse is applied. The 0 is entered into FF0, the 1 stored in FF0 is shifted into FF1, and the 0 stored in FF1 is shifted into FF2.

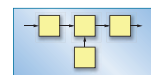
The last bit, a 1, is now applied to the serial data input, and a fourth clock pulse is applied. This time the 1 is entered into FF0, the 0 stored in FF0 is shifted into FF1, the 1 stored in FF1 is shifted into FF2, and the 0 stored in FF2 is shifted into FF3. This completes the serial entry of the four bits into the shift register, where they can be stored for any length of time as long as the flip-flops have dc power.

If you want to get the data out of the register, the bits must be shifted out serially and taken off the Q_3 output, as Table 2 illustrates. After CLK4 in the data-entry operation just

For serial data, one bit at a time is transferred.

Frequently, it is necessary to *clear* an internal register in a computer. For example, a register may be cleared prior to an arithmetic or other operation. One way that registers in a computer are cleared is using software to subtract the contents of the register from itself. The result, of course, will always be zero. For example, a computer instruction that performs this operation is SUB AL,AL. With this instruction, the register named AL is cleared.

SYSTEM NOTE



SHIFT REGISTERS

TABLE 2 • Shifting a 4-bit code out of the shift register in Figure 6. Data bits are indicated by a beige screen.

CLK	FF0 (Q_0)	FF1 (Q_1)	FF2 (Q_2)	FF3 (Q_3)
Initial	1	0	1	0
5	0	1	0	1
6	0	0	1	0
7	0	0	0	1
8	0	0	0	0

described (Table 1), the LSB, 0, appears on the Q_3 output. When clock pulse CLK5 is applied, the second bit appears on the Q_3 output. Clock pulse CLK6 shifts the third bit to the serial data output, and CLK7 shifts the fourth bit to the output. While the original four bits are being shifted out, more bits can be shifted in. All zeros have been shifted in after CLK 8.

EXAMPLE 1

Show the states of the 5-bit register in Figure 7(a) for the specified data input and clock waveforms. Assume that the register is initially cleared (all 0s).

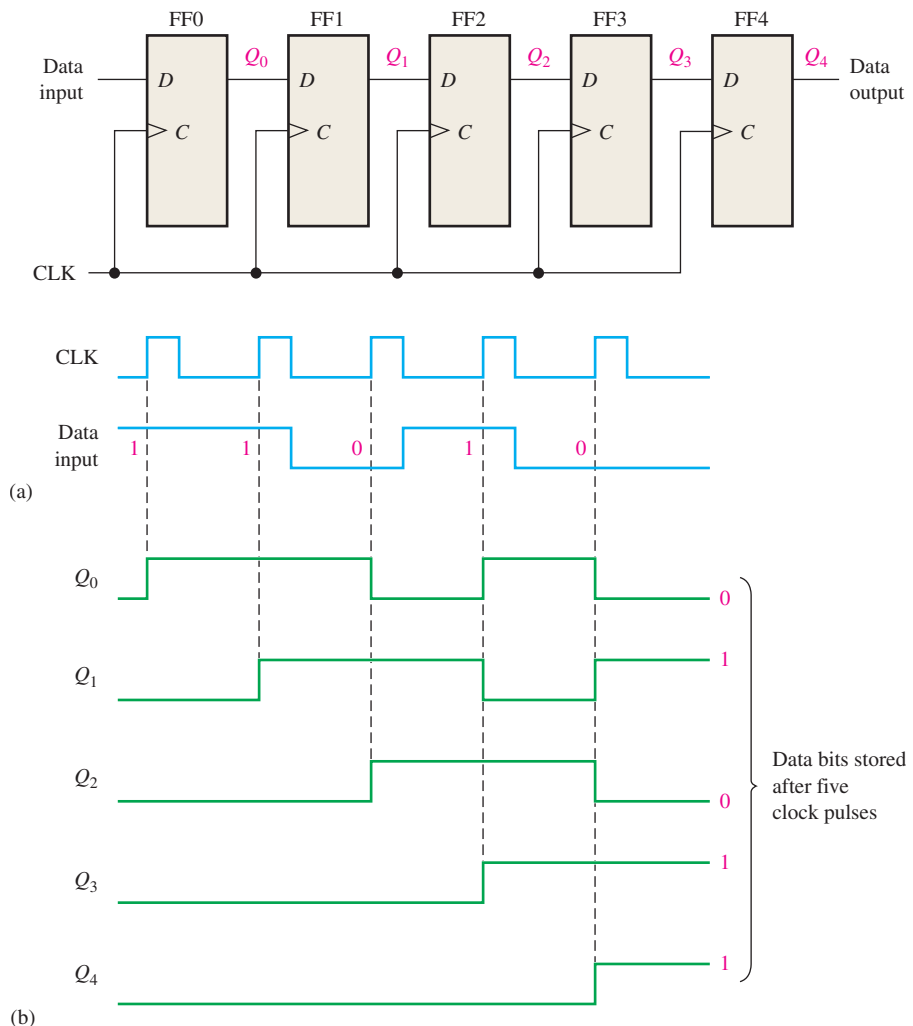


FIGURE 7 Open file F07-07 to verify operation.

SOLUTION

The first data bit (1) is entered into the register on the first clock pulse and then shifted from left to right as the remaining bits are entered and shifted. The register contains $Q_4Q_3Q_2Q_1Q_0 = 11010$ after five clock pulses. See Figure 7(b).

RELATED PROBLEM*

Show the states of the register if the data input is inverted. The register is initially cleared.

*Answers are at the end of the chapter.

A traditional logic block symbol for an 8-bit serial in/serial out shift register is shown in Figure 8. The “SRG 8” designation indicates a shift register (SRG) with an 8-bit capacity.

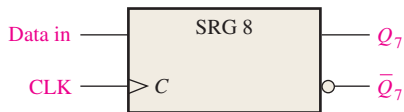
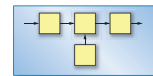


FIGURE 8 Logic symbol for an 8-bit serial in/serial out shift register.

All microprocessors have special instructions that can emulate a serial shift register. The accumulator register can shift data to the left or right. A right shift is equivalent to a divide-by-2 operation and a left shift is equivalent to a multiply-by-2 operation. Data in the accumulator can be shifted left or right with the rotate instructions; ROR is the rotate right instruction, and ROL is the rotate left instruction. Two other instructions treat the carry flag bit as an additional bit for the rotate operation. These are the RCR for rotate carry right and RCL for rotate carry left.

SYSTEM NOTE



Serial In/Parallel Out Shift Registers

Data bits are entered serially (least-significant bit first) into a serial in/parallel out shift register in the same manner as in serial in/serial out shift registers. The difference is the way in which the data bits are taken out of the register; in the parallel out register, the output of each stage is available. Once the data bits are stored, each bit appears on its respective output line, and all bits are available simultaneously, rather than on a bit-by-bit basis as with the serial output. Figure 9 shows a 4-bit serial in/parallel out shift register and its logic block symbol.

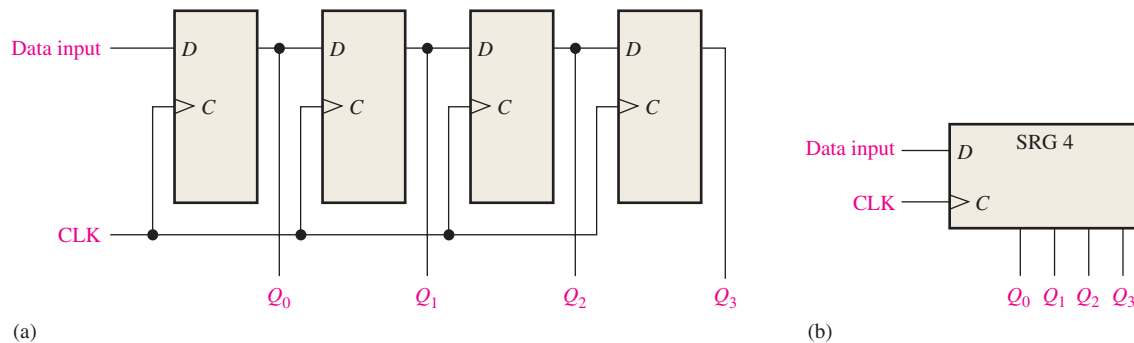


FIGURE 9 A serial in/parallel out shift register.

EXAMPLE 2

Show the states of the 4-bit register (SRG 4) for the data input and clock waveforms in Figure 10(a). The register initially contains all 1s.

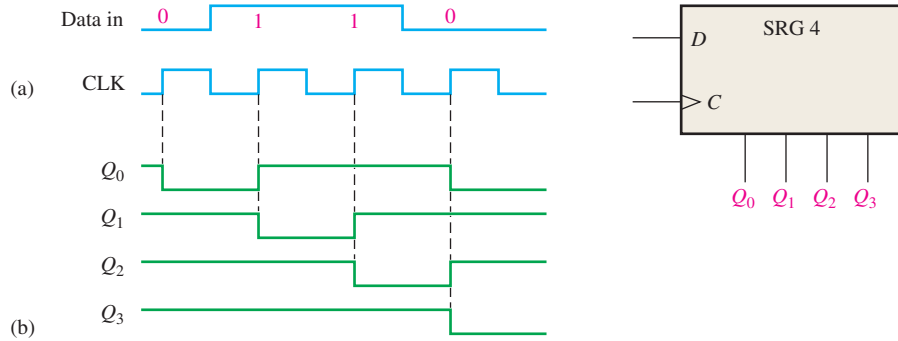


FIGURE 10

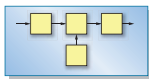
SOLUTION

The register contains 0110 after four clock pulses. See Figure 10(b).

RELATED PROBLEM

If the data input remains 0 after the fourth clock pulse, what is the state of the register after three additional clock pulses?

SYSTEM EXAMPLE 1



TIME DELAY

The serial in/serial out shift register can be used to provide a time delay from input to output that is a function of both the number of stages (n) in the register and the clock frequency.

When a data pulse is applied to the serial input as shown in Figure 11 (A and B connected together), it enters the first stage on the triggering edge of the clock pulse. It is then shifted from stage to stage on each successive clock pulse until it appears on the serial output n clock periods later. This time-delay operation is illustrated in Figure 11, in which an 8-bit serial in/serial out shift register is used with a clock frequency of 1 MHz to achieve a time delay (t_d) of $8 \mu\text{s}$ ($8 \times 1 \mu\text{s}$).

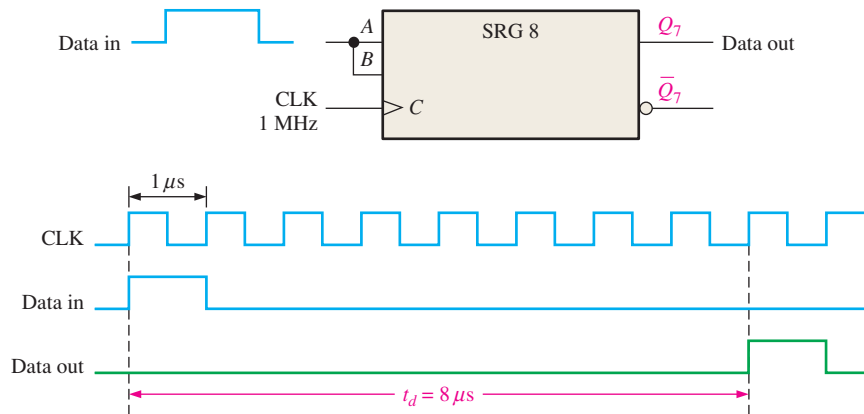


FIGURE 11 The serial in/serial out shift register as a time-delay device.

SHIFT REGISTERS

The time delay can be adjusted up or down by changing the clock frequency. The time delay can also be increased by cascading shift registers and decreased by taking the outputs from successively lower stages in the register if the outputs are available, as illustrated in Figure 12, using an 8-bit serial in/parallel out shift register with a clock period of $2 \mu\text{s}$.

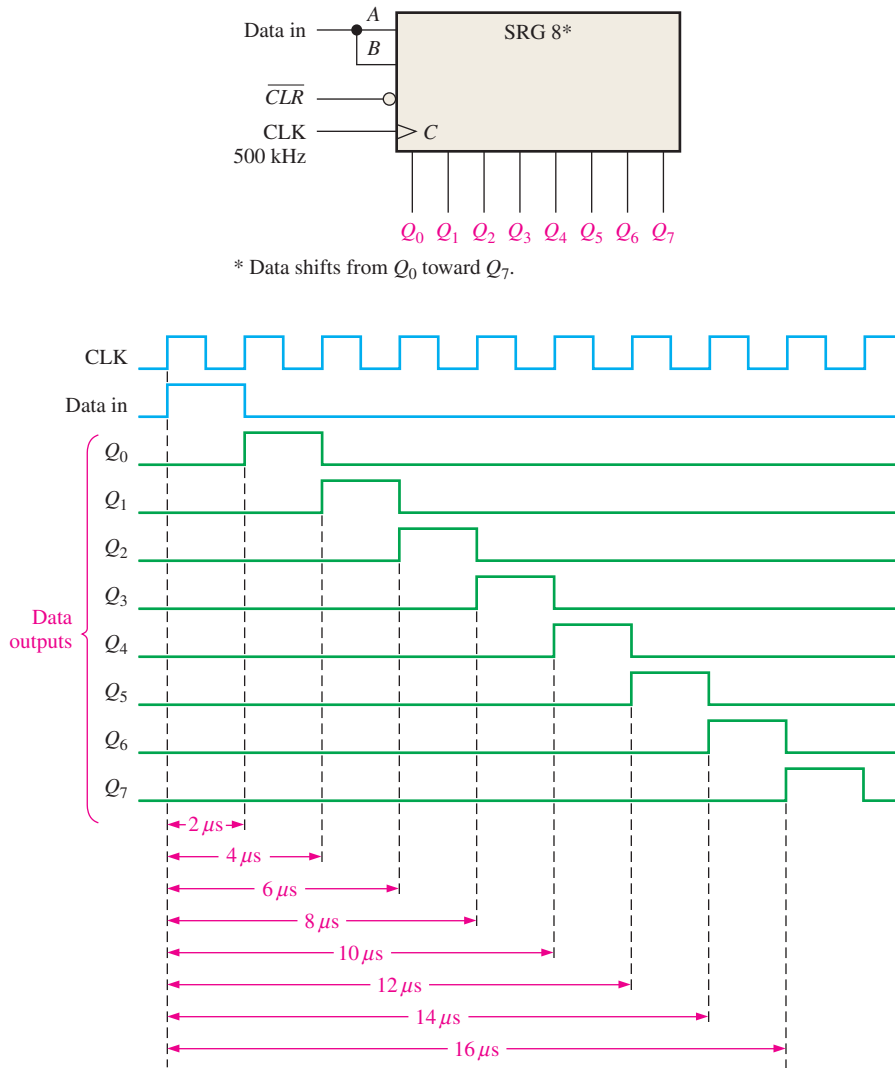


FIGURE 12 Shift register and timing diagram showing time delays.

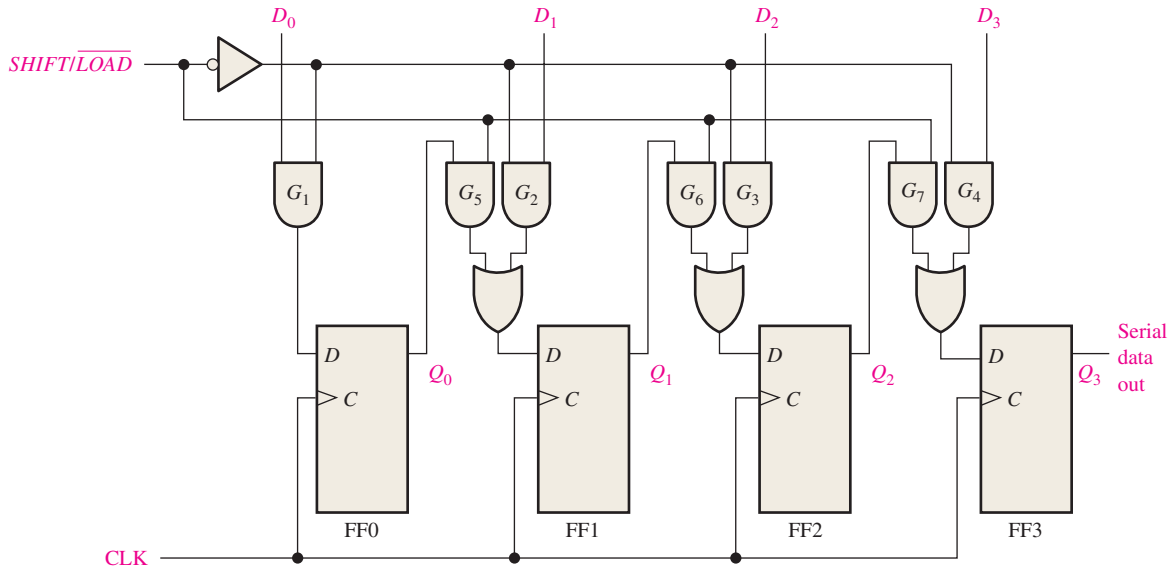
Parallel In/Serial Out Shift Registers

For a register with parallel data inputs, the bits are entered simultaneously into their respective stages on parallel lines rather than on a bit-by-bit basis on one line as with serial data inputs. The serial output is the same as in serial in/serial out shift registers, once the data are completely stored in the register.

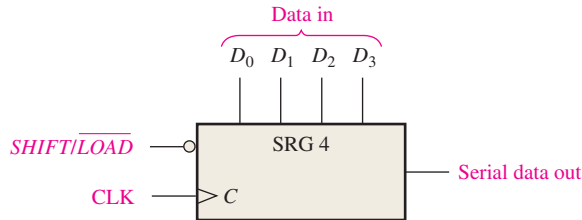
Figure 13 illustrates a 4-bit parallel in/serial out shift register and a typical logic symbol. Notice that there are four data-input lines, D_0 , D_1 , D_2 , and D_3 , and a $\overline{SHIFT/LOAD}$ input, which allows four bits of data to load in parallel into the register. When $\overline{SHIFT/LOAD}$ is LOW, gates G_1 through G_4 are enabled, allowing each data bit to be applied to the D input of its respective flip-flop. When a clock pulse is applied, the flip-flops with $D = 1$ will set and those with $D = 0$ will reset, thereby storing all four bits simultaneously.

For parallel data, multiple bits are transferred at one time.

SHIFT REGISTERS



(a) Logic diagram



(b) Logic symbol

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FIGURE 13 A 4-bit parallel in/serial out shift register. Open file F07-13 to verify operation.

When $SHIFT/\overline{LOAD}$ is HIGH, gates G_1 through G_4 are disabled and gates G_5 through G_7 are enabled, allowing the data bits to shift right from one stage to the next. The OR gates allow either the normal shifting operation or the parallel data-entry operation, depending on which AND gates are enabled by the level on the $SHIFT/\overline{LOAD}$ input. Notice that FF0 has a single AND to disable the parallel input, D_0 . It does not require an AND/OR arrangement because there is no serial data in.

EXAMPLE 3

Show the data-output waveform for a 4-bit register with the parallel input data and the clock and $SHIFT/\overline{LOAD}$ waveforms given in Figure 14(a). Refer to Figure 13(a) for the logic diagram.

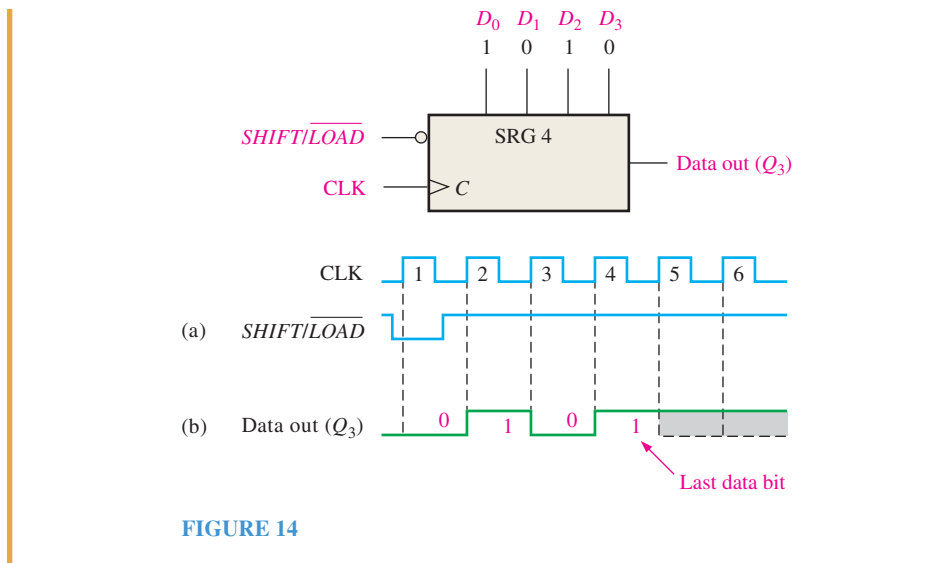
SOLUTION

On clock pulse 1, the parallel data ($D_0D_1D_2D_3 = 1010$) are loaded into the register, making Q_3 a 0. On clock pulse 2, the 1 from Q_2 is shifted onto Q_3 ; on clock pulse 3, the 0 is shifted onto Q_3 ; on clock pulse 4, the last data bit (1) is shifted onto Q_3 ; and on clock pulse 5, all data bits have been shifted out, and only 1s remain in the register (assuming the D_0 input remains a 1). See Figure 14(b).

RELATED PROBLEM

Show the data-output waveform for the clock and $SHIFT/\overline{LOAD}$ inputs shown in Figure 14(a) if the parallel data are $D_0D_1D_2D_3 = 0101$.

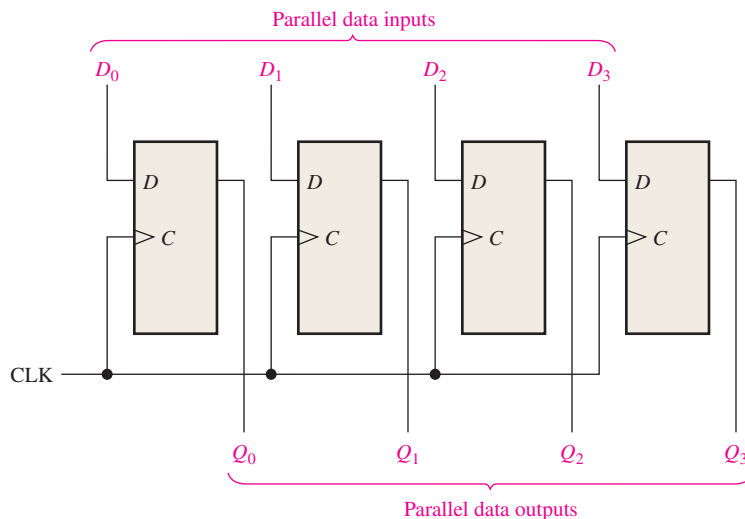
SHIFT REGISTERS



Parallel In/Parallel Out Shift Registers

Both parallel entry and parallel output of data have already been discussed. The parallel in/parallel out register employs both methods. Immediately following the simultaneous entry of all data bits, the bits appear on the parallel outputs. Figure 15 shows the logic diagram of a parallel in/parallel out register.

A universal shift register has both serial and parallel input and output capability.

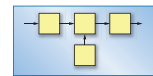


SYSTEM EXAMPLE 2

SERIAL-TO-PARALLEL DATA CONVERTER

Serial data transmission from one digital system to another is commonly used to reduce the number of wires in the transmission line. For example, eight bits can be sent serially over one wire, but it takes eight wires to send the same data in parallel.

Serial data transmission is widely used by peripherals to pass data back and forth to a computer. For example, USB (*universal serial bus*) is used to connect keyboards, printers,



SHIFT REGISTERS

scanners, and more to the computer. All computers process data in parallel form, thus the requirement for serial-to-parallel conversion. A simplified serial-to-parallel data converter, in which two types of shift registers are used, is shown in Figure 16.

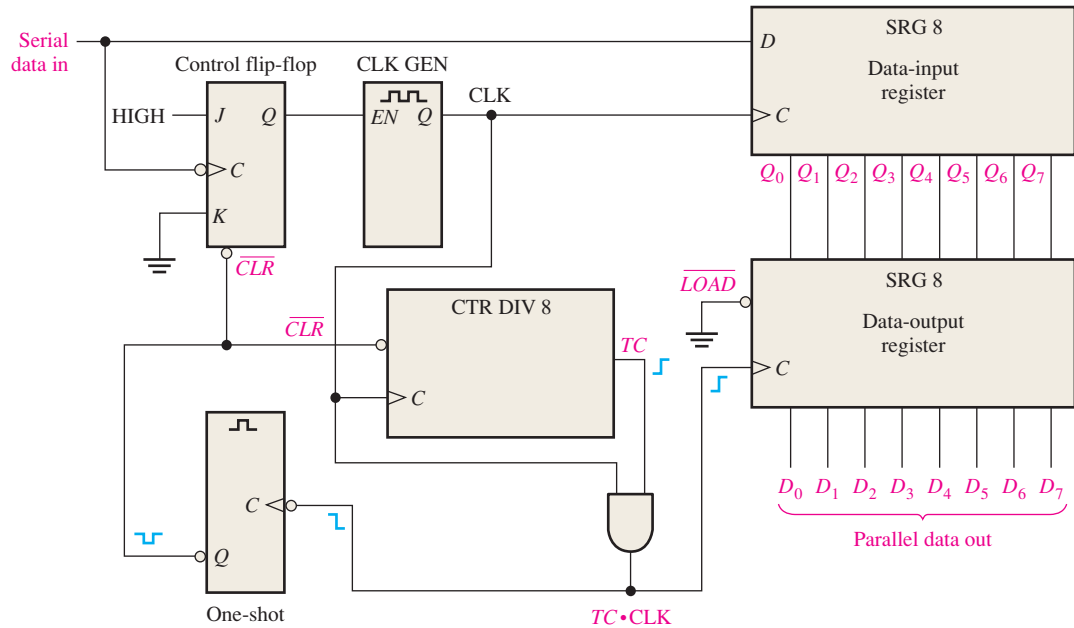


FIGURE 16

To illustrate the operation of this serial-to-parallel converter, the serial data format shown in Figure 17 is used. It consists of eleven bits. The first bit (start bit) is always 0 and always begins with a HIGH-to-LOW transition. The next eight bits (D_7 through D_0) are the data bits (one of the bits can be parity), and the last one or two bits (stop bits) are always 1s. When no data bits are being sent, there is a continuous HIGH on the serial data line.



FIGURE 17 Serial data format.

The HIGH-to-LOW transition of the start bit sets the control flip-flop, which enables the clock generator. After a fixed delay time, the clock generator begins producing a pulse waveform, which is applied to the data-input register and to the divide-by-8 counter. The clock has a frequency precisely equal to that of the incoming serial data, and the first clock pulse after the start bit occurs during the first data bit.

The timing diagram in Figure 18 illustrates the following basic operation: The eight data bits (D_7 through D_0) are serially shifted into the data-input register. Shortly after the eighth clock pulse, the terminal count (TC) goes from LOW to HIGH, indicating the counter is at the last state. This rising edge is ANDed with the clock pulse, which is still HIGH, producing a rising edge at $TC \cdot CLK$. This parallel loads the eight data bits from the data-input shift register to the data-output register. A short time later, the clock pulse goes LOW and this HIGH-to-LOW transition triggers the one-shot, which produces a short-duration pulse to clear the counter and reset the control flip-flop and thus disable the clock generator. The system is now ready for the next group of eleven bits, and it waits for the next HIGH-to-LOW transition at the beginning of the start bit.

By reversing the process just stated, parallel-to-serial data conversion can be accomplished. Since the serial data format must be produced, start and stop bits must be added to the sequence.

SHIFT REGISTERS

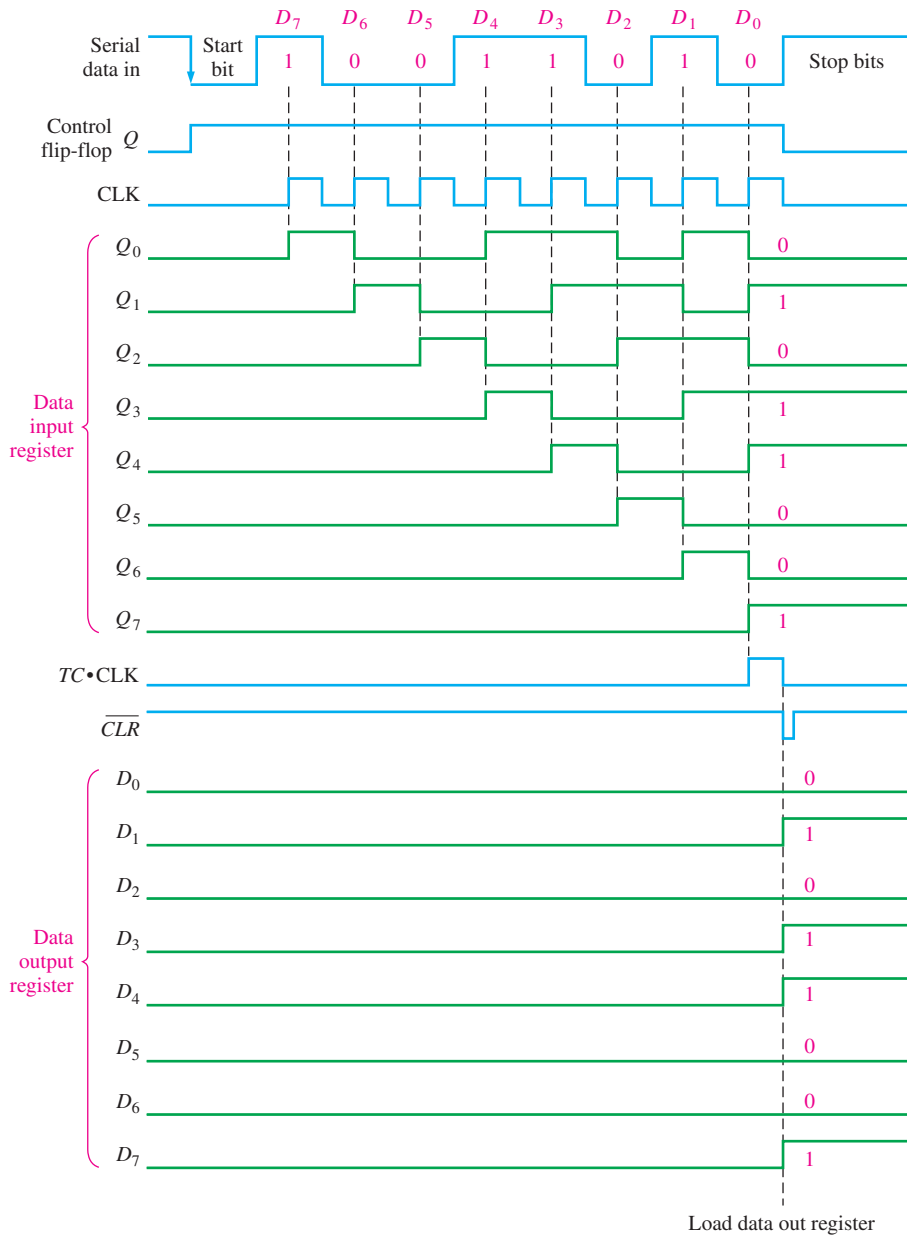
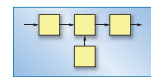


FIGURE 18

SYSTEM EXAMPLE 3

UNIVERSAL ASYNCHRONOUS RECEIVER TRANSMITTER (UART)

Computers and microprocessor-based systems also send and receive data in a parallel format. Frequently, these systems must communicate with external devices that send and/or receive serial data. An interfacing device used to accomplish these conversions is the UART (Universal Asynchronous Receiver Transmitter). Figure 19 illustrates the UART in a general microprocessor-based system application.



SHIFT REGISTERS

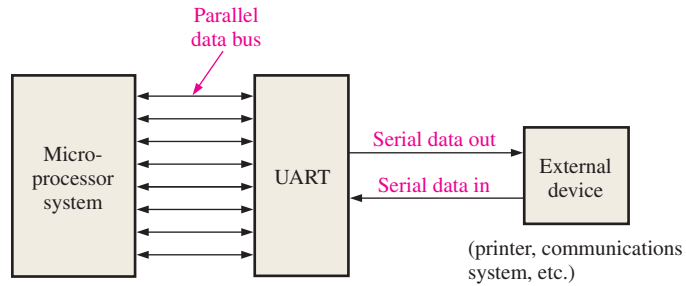


FIGURE 19 UART interface.

A UART includes both serial-to-parallel and parallel-to-serial conversion, as shown in the block diagram in Figure 20. The data bus is basically a set of parallel conductors along which data move between the UART and the microprocessor system. Buffers interface the data registers with the data bus.

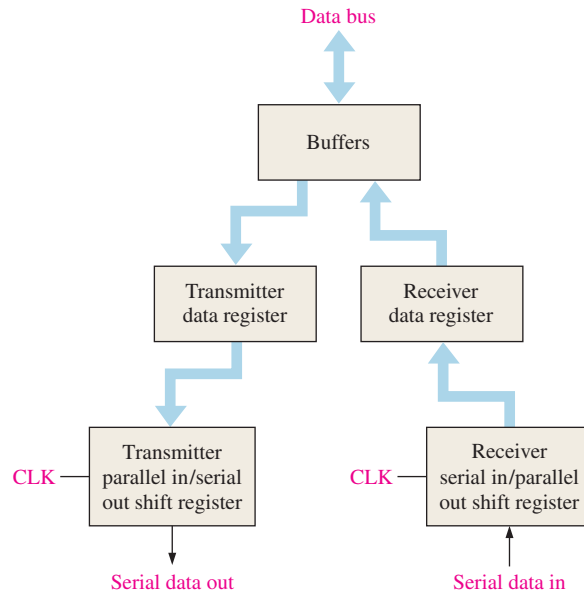


FIGURE 20 Basic UART block diagram.

The UART receives data in serial format, converts the data to parallel format, and places them on the data bus. The UART also accepts parallel data from the data bus, converts the data to serial format, and transmits them to an external device.

SECTION 3 CHECKUP

1. Develop the logic diagram for the shift register in Figure 6, using J-K flip-flops to replace the D flip-flops.
2. How many clock pulses are required to enter a byte of data serially into an 8-bit shift register?
3. The bit sequence 1101 is serially entered (least-significant bit first) into a 4-bit parallel out shift register that is initially clear. What are the Q outputs after two clock pulses?
4. How can a serial in/parallel out register be used as a serial in/serial out register?
5. Explain the function of the $SHIFT/\overline{LOAD}$ input.
6. In Figure 15, $D_0 = 1$, $D_1 = 0$, $D_2 = 0$, and $D_3 = 1$. After three clock pulses, what are the data outputs?

4 BIDIRECTIONAL SHIFT REGISTERS

A **bidirectional** shift register is one in which the data can be shifted either left or right. It can be implemented by using gating logic that enables the transfer of a data bit from one stage to the next stage to the right or to the left, depending on the level of a control line.

After completing this section, you should be able to

- Explain the operation of a bidirectional shift register
- Develop and analyze timing diagrams for bidirectional shift registers

A 4-bit bidirectional shift register is shown in Figure 21. A HIGH on the $RIGHT/\overline{LEFT}$ control input allows data bits inside the register to be shifted to the right, and a LOW enables data bits inside the register to be shifted to the left. An examination of the gating logic will make the operation apparent. When the $RIGHT/\overline{LEFT}$ control input is HIGH, gates G_1 through G_4 are enabled, and the state of the Q output of each flip-flop is passed through to the D input of the *following* flip-flop. When a clock pulse occurs, the data bits are shifted one place to the *right*. When the $RIGHT/\overline{LEFT}$ control input is LOW, gates G_5 through G_8 are enabled, and the Q output of each flip-flop is passed through to the D input of the *preceding* flip-flop. When a clock pulse occurs, the data bits are then shifted one place to the *left*.

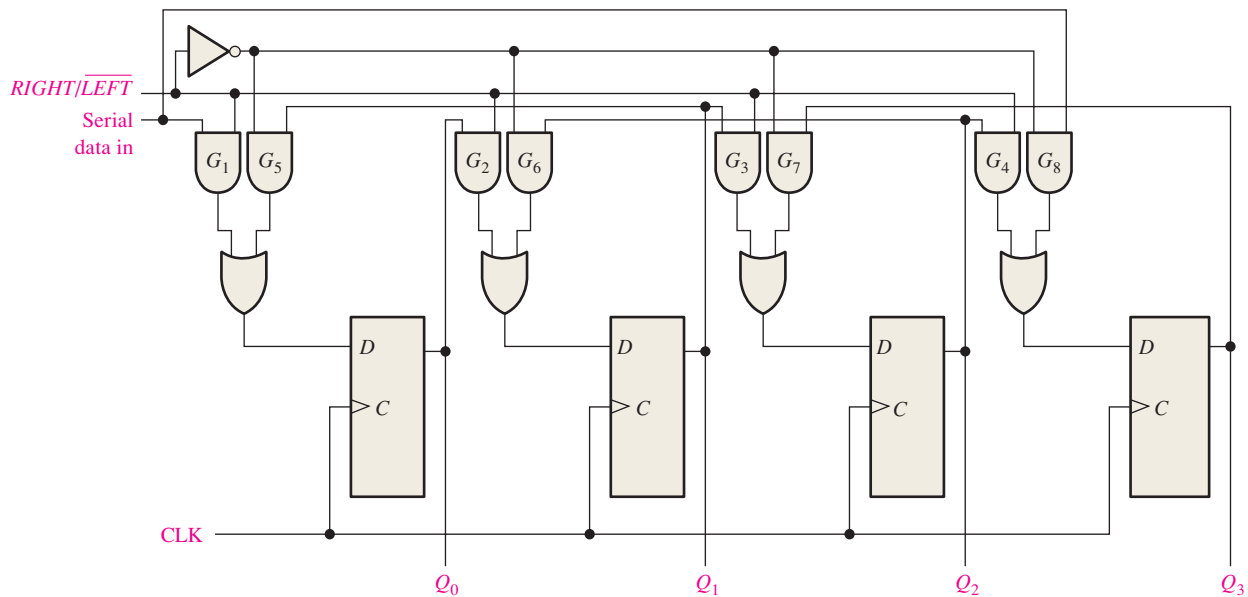


FIGURE 21 Four-bit bidirectional shift register. Open file F07-21 to verify the operation.

MULTISIM



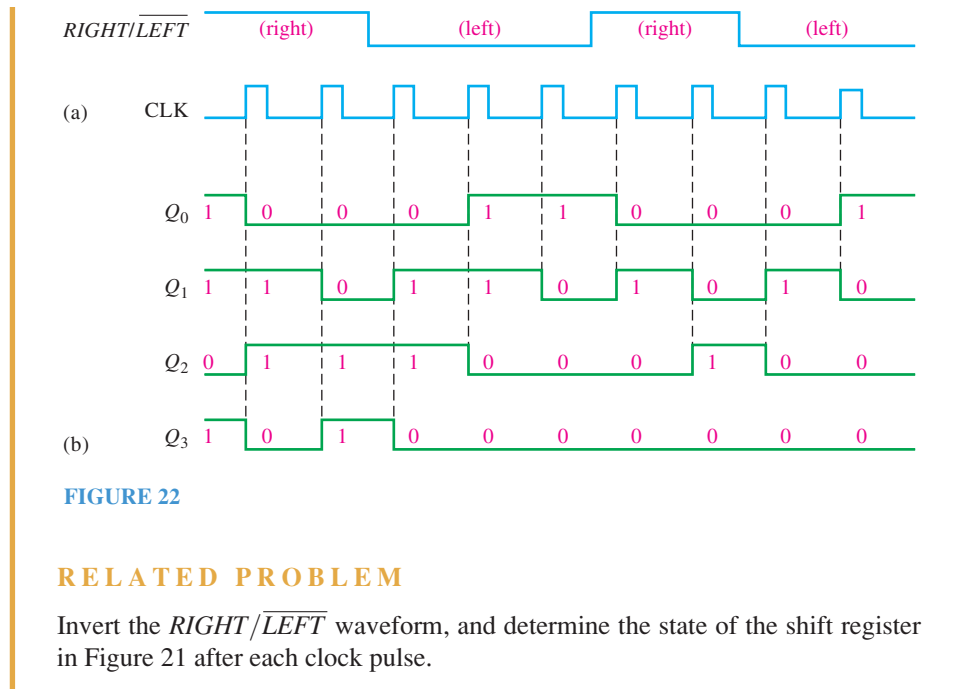
EXAMPLE 4

Determine the state of the shift register of Figure 21 after each clock pulse for the given $RIGHT/\overline{LEFT}$ control input waveform in Figure 22(a). Assume that $Q_0 = 1$, $Q_1 = 1$, $Q_2 = 0$, and $Q_3 = 1$ and that the serial data-input line is LOW.

SOLUTION

See Figure 22(b).

SHIFT REGISTERS



SECTION 4 CHECKUP

1. Assume that the 4-bit bidirectional shift register in Figure 21 has the following contents: $Q_0 = 1$, $Q_1 = 1$, $Q_2 = 0$, and $Q_3 = 0$. There is a 1 on the serial data-input line. If

$RIGHT/\overline{LEFT}$ is HIGH for three clock pulses and LOW for two more clock pulses, what are the contents after the fifth clock pulse?

5 SHIFT REGISTER COUNTERS

A shift register counter is basically a shift register with the serial output connected back to the serial input to produce special sequences. These devices are often classified as counters because they exhibit a specified sequence of states. Two of the most common types of shift register counters, the Johnson counter and the ring counter, are introduced in this section.

After completing this section, you should be able to

- Discuss how a shift register counter differs from a basic shift register
- Explain the operation of a Johnson counter
- Specify a Johnson sequence for any number of bits
- Explain the operation of a ring counter and determine the sequence of any specific ring counter

The Johnson Counter

In a **Johnson counter** the complement of the output of the last flip-flop is connected back to the D input of the first flip-flop (it can be implemented with other types of flip-flops as well). If the counter starts at 0, this feedback arrangement produces a characteristic

SHIFT REGISTERS

sequence of states, as shown in Table 3 for a 4-bit device and in Table 4 for a 5-bit device. Notice that the 4-bit sequence has a total of eight states, or bit patterns, and that the 5-bit sequence has a total of ten states. In general, a Johnson counter will produce a modulus of $2n$, where n is the number of stages in the counter.

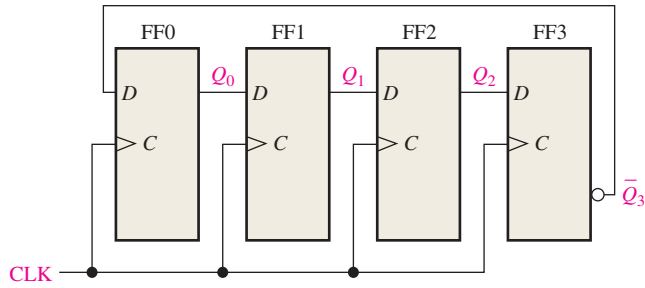
TABLE 3 • Four-bit Johnson sequence.				
CLOCK PULSE	Q_0	Q_1	Q_2	Q_3
0	0	0	0	0
1	1	0	0	0
2	1	1	0	0
3	1	1	1	0
4	1	1	1	1
5	0	1	1	1
6	0	0	1	1
7	0	0	0	1

TABLE 4 • Five-bit Johnson sequence.					
CLOCK PULSE	Q_0	Q_1	Q_2	Q_3	Q_4
0	0	0	0	0	0
1	1	0	0	0	0
2	1	1	0	0	0
3	1	1	1	0	0
4	1	1	1	1	0
5	1	1	1	1	1
6	0	1	1	1	1
7	0	0	1	1	1
8	0	0	0	1	1
9	0	0	0	0	1

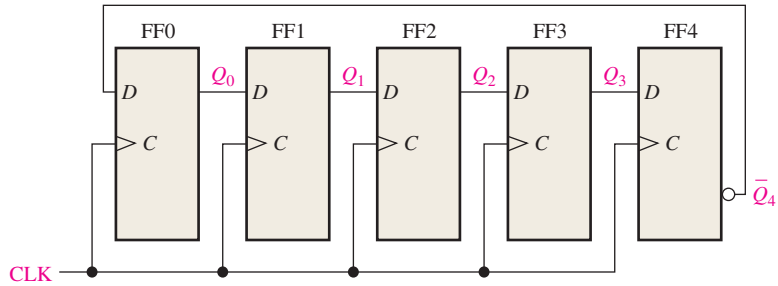
The implementations of the 4-stage and 5-stage Johnson counters are shown in Figure 23. The implementation of a Johnson counter is very straightforward and is the same regardless of the number of stages. The Q output of each stage is connected to the D input of the next stage (assuming that D flip-flops are used). The single exception is that the \bar{Q} output of the last stage is connected back to the D input of the first stage. As the sequences in Table 3 and 4 show, if the counter starts at 0, it will “fill up” with 1s from left to right, and then it will “fill up” with 0s again.

Diagrams of the timing operations of the 4-bit and 5-bit Johnson counters are shown in Figures 24 and 25, respectively.

SHIFT REGISTERS



(a) Four-bit Johnson counter



(b) Five-bit Johnson counter

FIGURE 23 Four-bit and 5-bit Johnson counters.

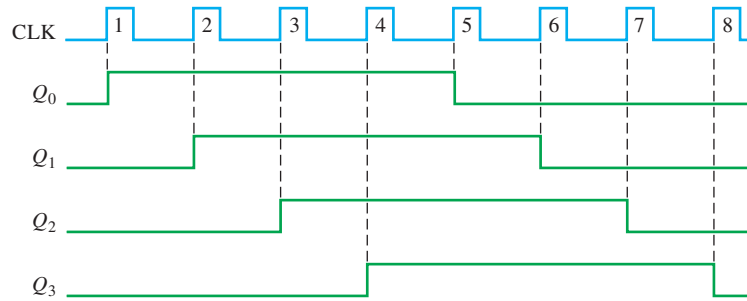


FIGURE 24 Timing sequence for a 4-bit Johnson counter.

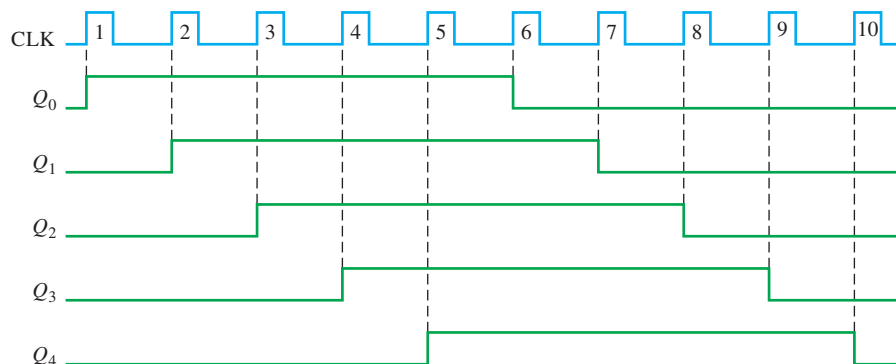


FIGURE 25 Timing sequence for a 5-bit Johnson counter.

The Ring Counter

The **ring counter** utilizes one flip-flop for each state in its sequence. It has the advantage that decoding gates are not required. In the case of a 10-bit ring counter, there is a unique output for each decimal digit.

SHIFT REGISTERS

A logic diagram for a 10-bit ring counter is shown in Figure 26. The sequence for this ring counter is given in Table 5. Initially, a 1 is preset into the first flip-flop, and the rest of the flip-flops are cleared. Notice that the interstage connections are the same as those for a Johnson counter, except that Q rather than \overline{Q} is fed back from the last stage. The ten outputs of the counter indicate directly the decimal count of the clock pulse. For instance, a 1 on Q_0 represents a zero, a 1 on Q_1 represents a one, a 1 on Q_2 represents a two, a 1 on Q_3 represents a three, and so on. You should verify for yourself that the 1 is always retained in the counter and simply shifted “around the ring,” advancing one stage for each clock pulse.

Modified sequences can be achieved by having more than a single 1 in the counter, as illustrated in Example 5.

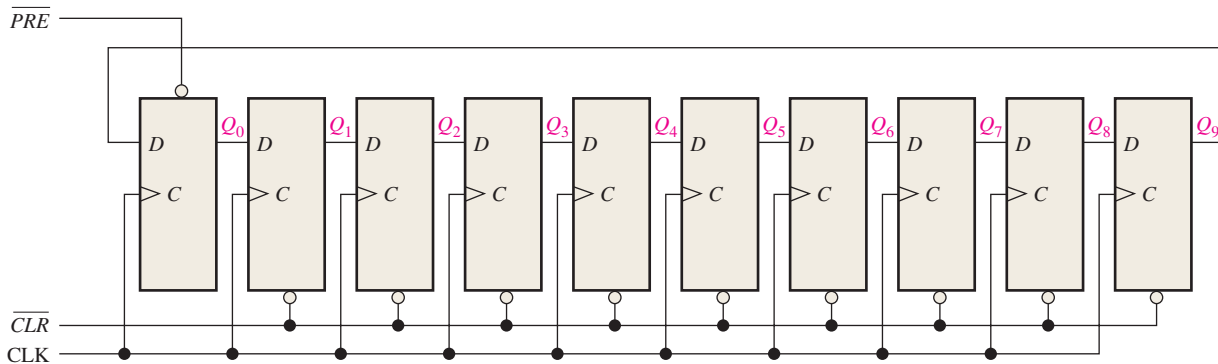


FIGURE 26 A 10-bit ring counter. Open file F07-26 to verify operation.

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TABLE 5 • Ten-bit ring counter sequence.										
CLOCK PULSE	Q_0	Q_1	Q_2	Q_3	Q_4	Q_5	Q_6	Q_7	Q_8	Q_9
0	1	0	0	0	0	0	0	0	0	0
1	0	1	0	0	0	0	0	0	0	0
2	0	0	1	0	0	0	0	0	0	0
3	0	0	0	1	0	0	0	0	0	0
4	0	0	0	0	1	0	0	0	0	0
5	0	0	0	0	0	1	0	0	0	0
6	0	0	0	0	0	0	1	0	0	0
7	0	0	0	0	0	0	0	1	0	0
8	0	0	0	0	0	0	0	0	1	0
9	0	0	0	0	0	0	0	0	0	1

EXAMPLE 5

If a 10-bit ring counter similar to Figure 26 has the initial state 1010000000, determine the waveform for each of the Q outputs.

SOLUTION

See Figure 27.

SHIFT REGISTERS

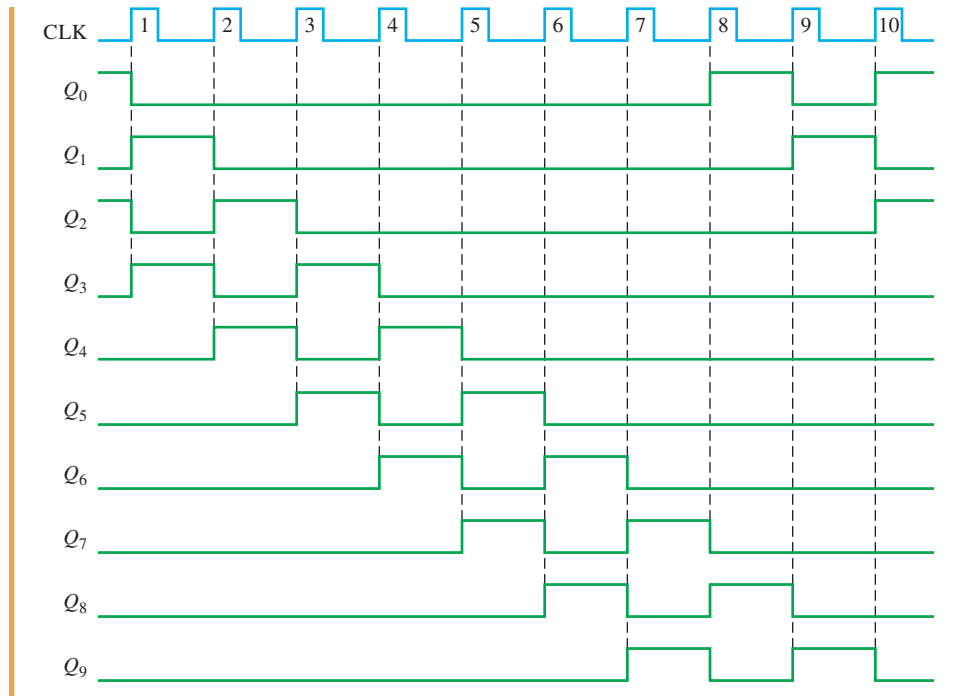
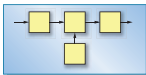


FIGURE 27

RELATED PROBLEM

If a 10-bit ring counter has an initial state 0101001111, determine the waveform for each Q output.

SYSTEM EXAMPLE 4



KEYBOARD ENCODER

The keyboard encoder is a good example of the application of a shift register used as a ring counter in conjunction with other devices.

Figure 28 shows a simplified keyboard encoder for encoding a key closure in a 64-key matrix organized in eight rows and eight columns. Two 4-bit shift registers are connected as an 8-bit ring counter with a fixed bit pattern of seven 1s and one 0 preset into it when the power is turned on. Two priority encoders are used as eight-line-to-three-line encoders (9 input HIGH, 8 output unused) to encode the ROW and COLUMN lines of the keyboard matrix. The parallel in/parallel out register holds the ROW/COLUMN code from the priority encoders.

The basic operation of the keyboard encoder in Figure 28 is as follows: The ring counter “scans” the rows for a key closure as the clock signal shifts the 0 around the counter at a 5 kHz rate. The 0 (LOW) is sequentially applied to each ROW line, while all other ROW lines are HIGH. All the ROW lines are connected to the ROW encoder inputs, so the 3-bit output of the ROW encoder at any time is the binary representation of the ROW line that is LOW. When there is a key closure, one COLUMN line is connected to one ROW line. When the ROW line is taken LOW by the ring counter, that particular COLUMN line is also pulled LOW. The COLUMN encoder produces a binary output corresponding to the COLUMN in which the key is closed. The 3-bit ROW code plus the 3-bit COLUMN code uniquely identifies the key that is closed. This 6-bit code is applied to the inputs of the key code register. When a key is closed, the two one-shots produce a delayed clock pulse to parallel-load the 6-bit code into the key code register. This delay allows the contact bounce to die out. Also, the first one-shot output inhibits the ring counter to prevent it from scanning while the data are being loaded into the key code register.

SHIFT REGISTERS

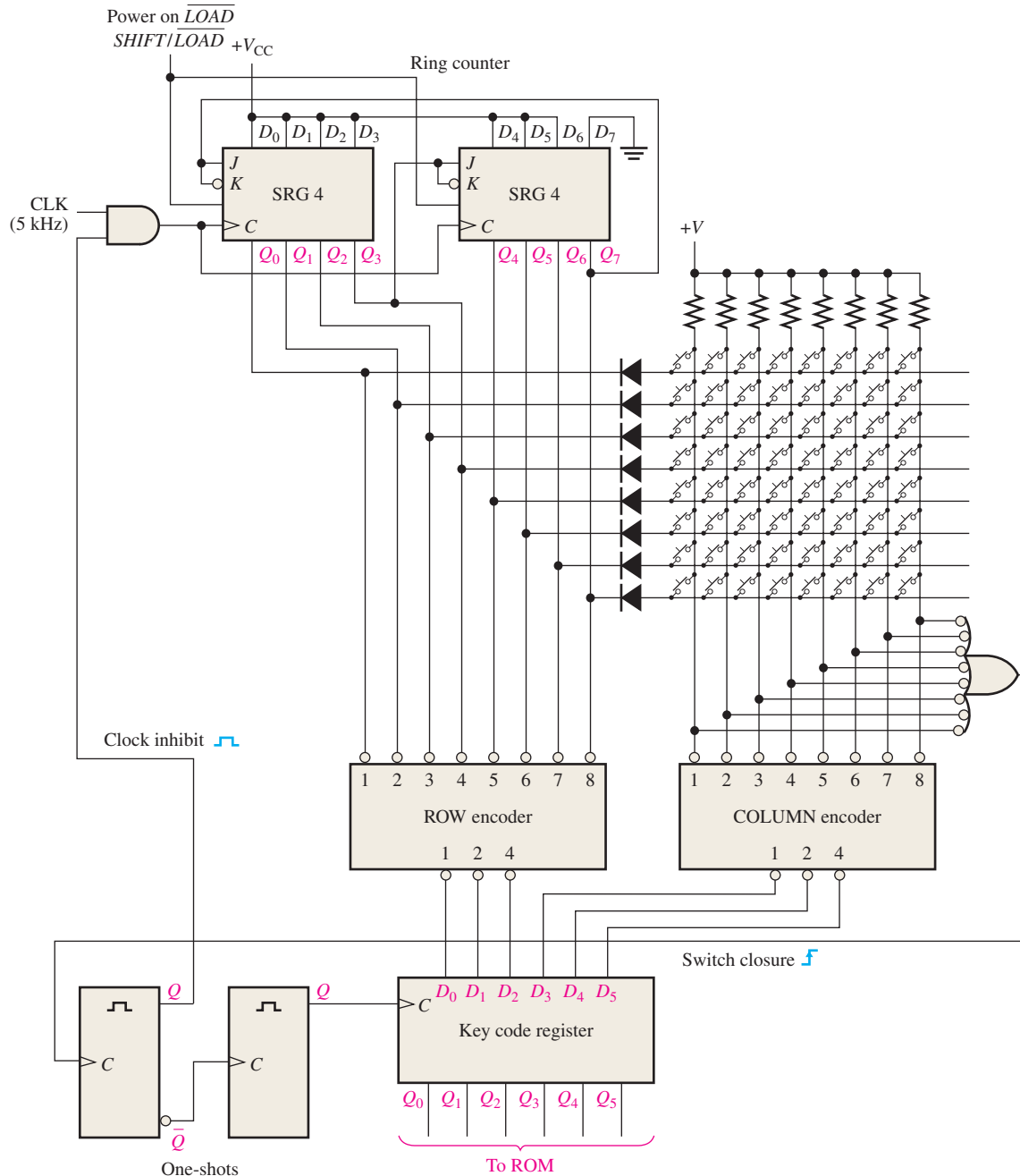


FIGURE 28

The 6-bit code in the key code register is now applied to a ROM (read-only memory) to be converted to an appropriate alphanumeric code that identifies the keyboard character.

SECTION 5 CHECKUP

1. How many states are there in an 8-bit Johnson counter sequence?
2. Write the sequence of states for a 3-bit Johnson counter starting with 000.
3. In the keyboard encoder, how many times per second does the ring counter scan the keyboard?
4. What is the 6-bit ROW/COLUMN code (key code) for the top row and the left-most column in the keyboard encoder?
5. What do you believe is the purpose of the diodes in the keyboard encoder? What do you believe is the purpose of the resistors?

6 SECURITY SYSTEM WITH VHDL AND VERILOG

The security system that was introduced in Section 1 can be described using VHDL or Verilog for implementation in a PLD. The three blocks of the system (keypad, security code logic, and code-selection logic) are combined in the program code to describe the complete system.

After completing this section, you should be able to

- Discuss the general approach to programming a system for implementation in a PLD
- See how the VHDL and Verilog programs are used to implement the system

The security system block diagram is shown in Figure 29 as a programming model. Six program components perform the logical operations of the security system. Each component corresponds to a block or blocks in the figure. The security system program SecuritySystem contains the code that defines how the components interact.

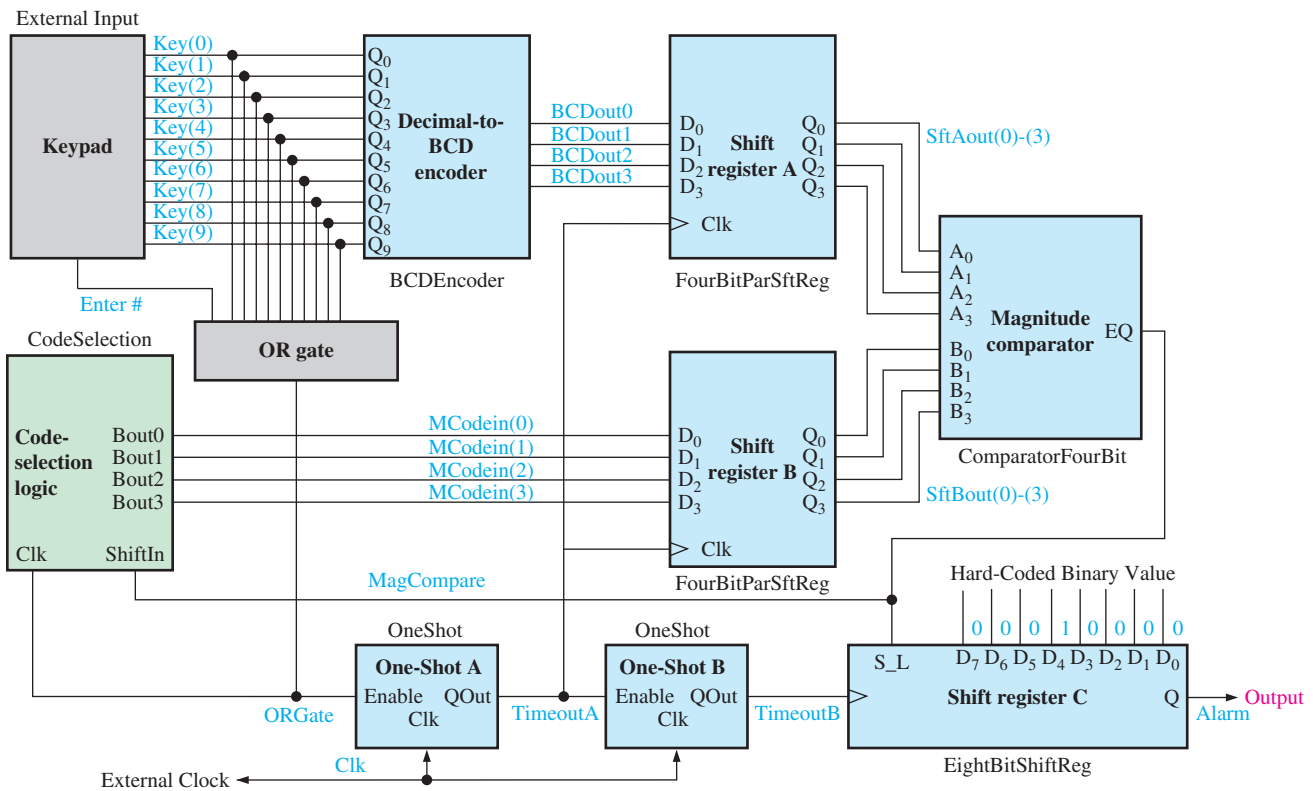


FIGURE 29 Security system block diagram as a programming model.

The security system includes a ten-bit input vector **Key**—one input bit for each decimal digit—and an input **Enter**, representing a typical numeric keypad. Once a key is pressed, the data stored in input array **Key** is sent to the decimal-to-BCD encoder (BCDEncoder). Its 4-bit output is then sent to the inputs of the 4-bit parallel in/parallel out shift register A (FourBitParSftReg). An external system clock applied to input **Clk** drives the overall security system. The **Alarm** output signal is set HIGH upon a successful arming operation.

Pressing the **Enter** key sends an initial HIGH clock signal to the code-selection logic block (CodeSelection), which loads an initial binary value of 1000 to shift register B. At this time, a binary 0000 is stored in shift register A, and the output of the magnitude comparator (ComparatorFourBit) is set LOW. The code-selection logic is now ready to present the first stored code value that is to be compared to the value of the first numeric keypad entry. At this time a LOW on the 8-bit parallel in/serial out shift register C (EightBitShiftReg) **S_L** input loads an initial value of 00010000.

SHIFT REGISTERS

When a numeric key is pressed, the output of the OR gate (ORGate) clocks the first stored value to the inputs of shift register B, and the output of the decimal-to-BCD encoder is sent to the inputs of shift register A. If the values in shift registers A and B match, the output of the magnitude comparator is set HIGH; and the code-selection logic is ready to clock in the next stored code value.

At the conclusion of four successful comparisons of stored code values against four correct keypad entries, the value 00010000 initially in shift register C will shift four places to the right, setting the Alarm output to a HIGH. An incorrect keypad entry will not match the stored code value in shift register B and the magnitude comparator will output a LOW. With the comparator output LOW, the code-selection logic will reset to the first stored code value; and the value 00010000 is reloaded into shift register C, starting the process over again.

To clock the keypad and the stored code values through the system, two one-shots (OneShot) are used. The one-shots allow data to stabilize before acting on it. One-shot A receives an Enable signal from the keypad OR gate, which initiates the first timed process. The OR gate output is also sent to the code-selection logic, and the first code value from the code-selection logic is sent to the inputs of shift register A. When one-shot A times out, the selected keypad entry and the current code from the code-selection logic are stored in shift registers A and B for comparison by the magnitude comparator, and an Enable is sent to one-shot B. If the codes in shift registers A and B match, the value stored in shift register C shifts one place to the right after one-shot B times out.

The six components used in the security system program SecuritySystem are shown in Figure 30. The VHDL and Verilog programs for each component are available in the appendix “Programs for Security System Components.”

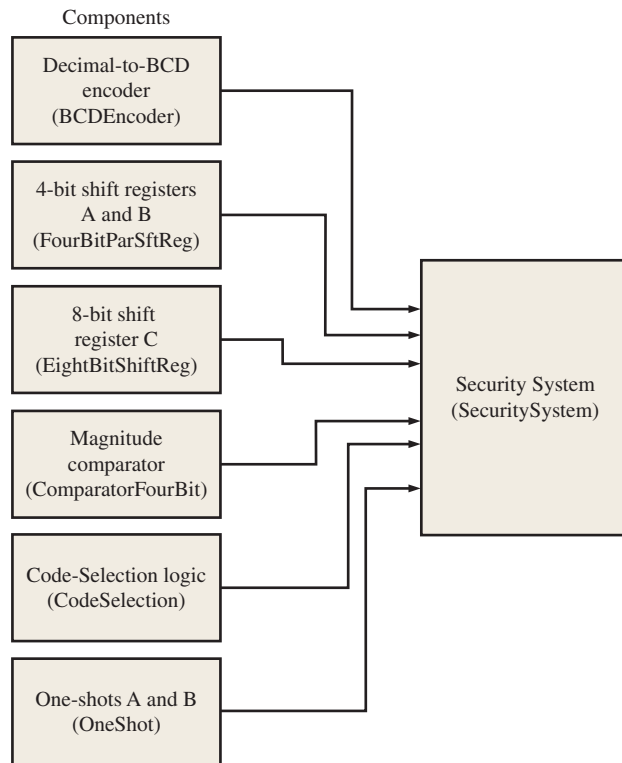


FIGURE 30 Security system components (VHDL/Verilog codes are available in the appendix “Programs for Security System Components.”)

VHDL FOR THE SECURITY SYSTEM

```

library ieee;
use ieee.std_logic_1164.all;
entity SecuritySystem is
port (key: in std_logic_vector(0 to 9); Enter: in std_logic;
      Clk: in std_logic; Alarm: out std_logic);
end entity SecuritySystem;
architecture SecuritySystemBehavior of SecuritySystem is

```

Key : 10 - Key input
Enter : # - Key input
Clk : System clock
Alarm : Alarm output

SHIFT REGISTERS

```

component BCDEncoder is
port(D: in std_logic_vector(0 to 9);
      Q: out std_logic_vector(0 to 3));
end component BCDEncoder;

component FourBitParSftReg is
port(D: in std_logic_vector(0 to 3);
      Clk: in std_logic;
      Q: out std_logic_vector(0 to 3));
end component FourBitParSftReg;

component ComparatorFourBit is
port(A, B: in std_logic_vector(0 to 3);
      EQ: out std_logic);
end component ComparatorFourBit;

component OneShot is
port(Enable, Clk: in std_logic;
      QOut: buffer std_logic);
end component OneShot;

component EightBitShiftReg is
port(S_L, Clk: in std_logic;
      D: in std_logic_vector(0 to 7);
      Q: buffer std_logic);
end component EightBitShiftReg;

component CodeSelection is
port(ShiftIn, Clk: in std_logic;
      Bout: out std_logic_vector(1 to 4));
end component CodeSelection;

signal BCDout: std_logic_vector(0 to 3);
signal SftAout: std_logic_vector(0 to 3);
signal SftBout: std_logic_vector(0 to 3);
signal MCodein: std_logic_vector(0 to 3);
signal ORgate: std_logic;
signal MagCompare: std_logic;
signal TimeoutA, TimeoutB: std_logic;

begin
ORgate <= (Key(0) or Key(1) or Key(2) or Key(3) or Key(4)
          or key(5) or Key(6) or Key(7) or Key(8) or Key(9));

BCD: BCDEncoder
port map(D(0)=>Key(0),D(1)=>Key(1),D(2)=>Key(2),D(3)=>Key(3),
          D(4)=>Key(4),D(5)=>Key(5),D(6)=>Key(6),D(7)=>Key(7),D(8)=>Key(8),D(9)=>Key(9),
          Q(0)=>BCDout(0),Q(1)=>BCDout(1),Q(2)=>BCDout(2),Q(3)=>BCDout(3));

ShiftRegisterA: FourBitParSftReg
port map(D(0)=>BCDout(0),D(1)=>BCDout(1),D(2)=>BCDout(2),D(3)=>BCDout(3),
          Clk=>not TimeoutA,Q(0)=>SftAout(0),Q(1)=>SftAout(1),Q(2)=>SftAout(2),Q(3)=>SftAout(3));

ShiftRegisterB: FourBitParSftReg
port map(D(0)=>MCodein(0),D(1)=>MCodein(1),D(2)=>MCodein(2),D(3)=>MCodein(3),
          Clk=>not TimeoutA,Q(0)=>SftBout(0),Q(1)=>SftBout(1),Q(2)=>SftBout(2),Q(3)=>SftBout(3));
Magnitude Comparator: ComparatorFourBit port map(A=>SftAout,B=>SftBout,EQ=>MagCompare);

OSA:OneShot port map(Enable=>Enter or ORgate,Clk=>Clk,QOut=>TimeoutA);
OSB:OneShot port map(Enable=>not TimeoutA,Clk=>Clk,QOut=>TimeoutB);

ShiftRegisterC:EightBitShiftReg
port map(S_L=>MagCompare,Clk=> TimeoutB,D(0)=>'0',D(1)=>'0',
          D(2)=>'0',D(3)=>'1',D(4)=>'0',D(5)=>'0',D(6)=>'0',D(7)=>'0',Q=>Alarm);
CodeSelectionA: CodeSelection
port map(ShiftIn=>MagCompare,Clk=>Enter or ORGate,Bout=>MCodein);
end architecture SecuritySystemBehavior;

```

BCDout : BCD encoder return
 SftAout : Shift Register A return
 SftBout : Shift Register B return
 MCodein : Security Code value
 ORgate : OR output from 10-keypad
 MagCompare : Key entry to code compare
 TimeoutA/B : One-shot timer variables

Logic definition for ORGate

Component instantiations

VERILOG FOR THE SECURITY SYSTEM

```

module SecuritySystem(Key, Enter, Clk, Alarm);
    input [9:0] Key;
    input Enter;
    input Clk;
    output Alarm;

    wire[3:0] BCDout;
    wire[3:0] SftAout;
    wire[3:0] SftBout;
    wire[3:0] MCodein;
    wire ORGate;
    wire MagCompare;
    wire TimeoutA, TimeoutB;

    BDCout : BCD encoder return
    SftAout : 4-bit shift register A
    SftBout : 4-bit shift register B
    MCodein : Security Code value
    ORgate : OR output from 10-keypad
    MagCompare : Key entry to code compare
    TimeoutA/B : One-shot timer variables

    assign ORGate = ( Key[0] || Key[1] || Key[2] || Key[3] || Key[4] ||
                    Key[5] || Key[6] || Key[7] || Key[8] || Key[9] );

    BCDEncoder BCD(.D(Key),.Q(BCDout));
    FourBitParSftReg ShiftRegisterA(.D(BCDout),.Clk(!TimeoutA),.Q(SftAout));
    FourBitParSftReg ShiftRegisterB(.D(MCodein),.Clk(!TimeoutA),.Q(SftBout));
    ComparatorFourBit MagnitudeComparator(.A(SftAout),.B(SftBout),.EQ(MagCompare));
    OneShot OSA(.Enable(Enter || ORGate),.Clk(Clk),.QOut(TimeoutA));
    OneShot OSB(.Enable(!TimeoutA),.Clk(Clk),.QOut(TimeoutB));
    EightBitShiftReg ShiftRegisterC(.S_L(MagCompare),.Clk(TimeoutB),.D(0010),.Q(Alarm));
    CodeSelection CodeSelectionA(.ShiftIn(MagCompare),.Clk(Enter || ORGate),.Bout(MCodein));
endmodule

```

Key : 10 - Key input
Enter : # - Key input
Clk : System clock
Alarm : Alarm output

Logic definition for OR Gate

Component instantiations

SECTION 6 CHECKUP

- List the types of components used in the VHDL program?
- What is the only block in the security system not defined as a component? How is it described?

7 TROUBLESHOOTING

In this section, in addition to Multisim debugging and software testing, a traditional method of troubleshooting sequential logic and other more complex system hardware is also discussed. This method uses a procedure of “exercising” the circuit under test with a known input waveform (stimulus) and then observing the output for the correct bit pattern.

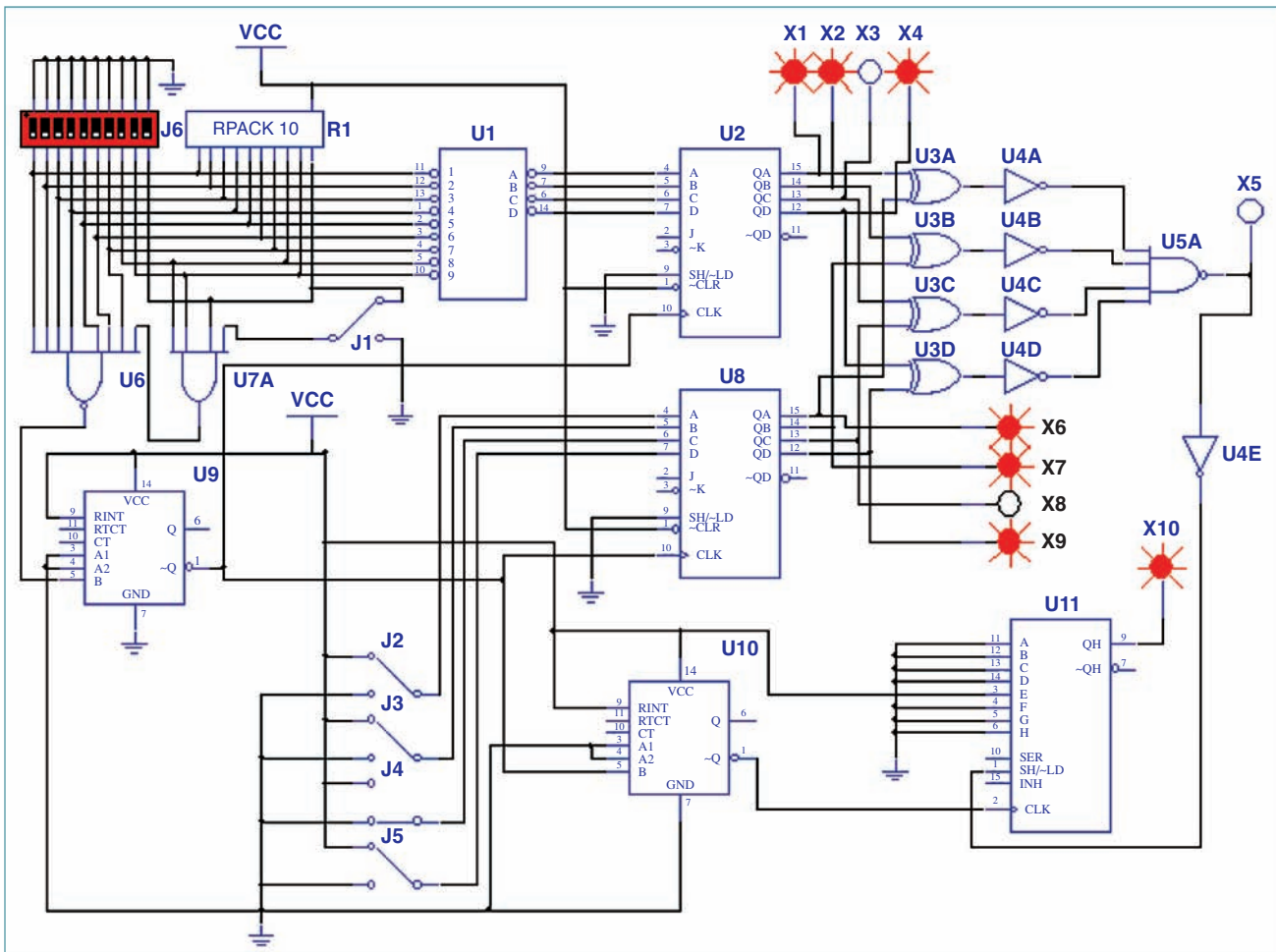


After completing this section, you should be able to

- Use Multisim to debug a system design before implementation
- Describe how development software is used to implement and test a system
- Explain the procedure of “exercising” as a troubleshooting technique
- Discuss troubleshooting of a serial-to-parallel converter

Multisim Simulation

Figure 31 shows the simulation screen for the security code logic that was covered in Section 1. A DIP switch (J6) is used to simulate the 10-digit keypad and switch J1 simulates the # key. Switches J2–J5 are used for test purposes to enter the code that is produced by the code selection logic in the complete system. Probe lights are used only for test purposes to indicate the states of registers A and B, the output of the comparator, and the output of register C.




MULTISIM  **FIGURE 31** Multisim screen for the security code logic. The switches and probe lights are for test purposes only. When a probe light is on, a 1 is indicated. Open F07-31 and run the simulation to verify operation.

Figure 32 shows the simulation screen for the code-selection logic. Switches are selected for this application as the most convenient and cost-effective way to enter and store the code, thus eliminating the need for a semiconductor memory.

Software Development and Testing

A VHDL or Verilog code for a device or system can be tested in software before being committed to hardware (PLD). The 4-bit bidirectional shift register is used for illustration. A development software simulation run with Altera Quartus II for the following 4-bit bidirectional shift register VHDL code is shown in Figure 33.

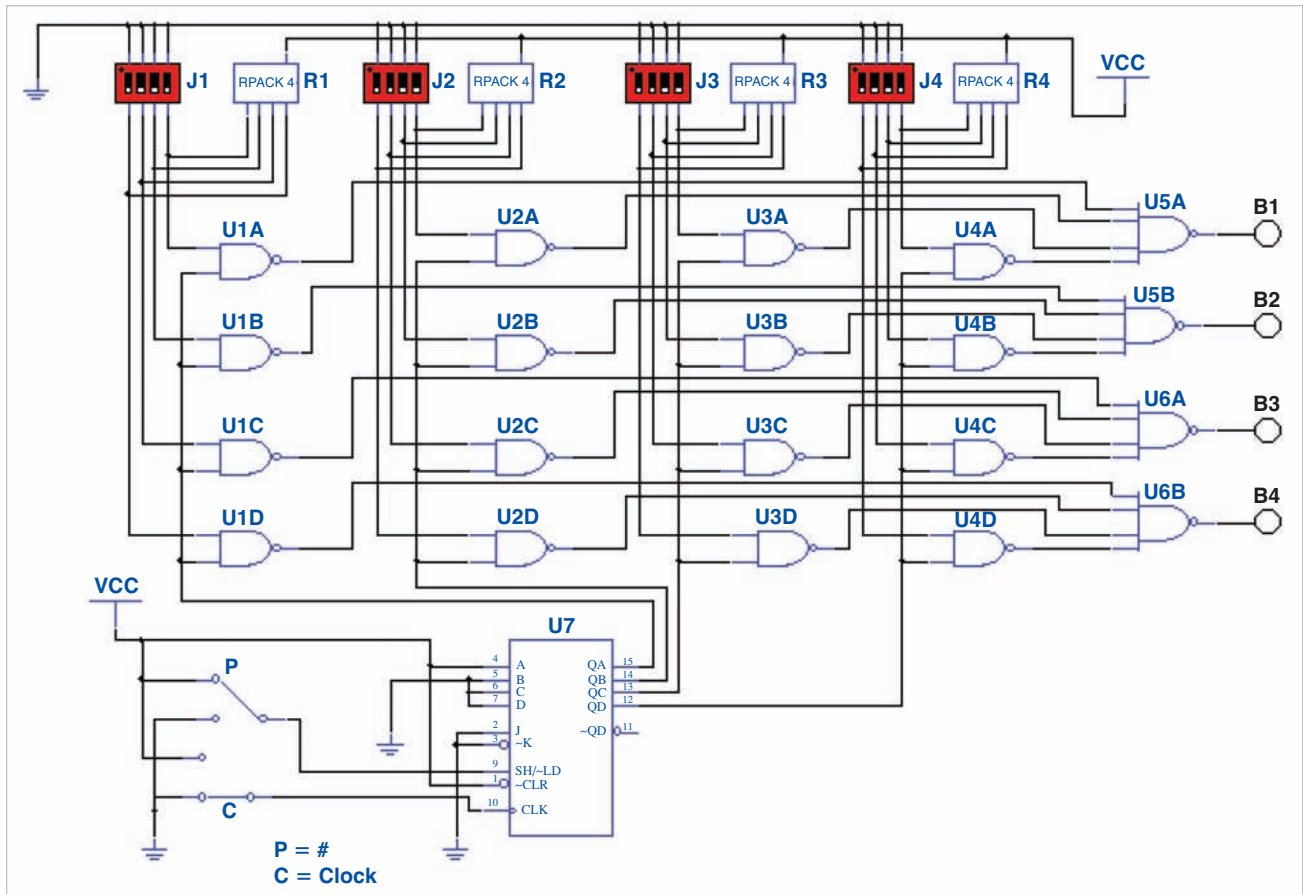


FIGURE 32 Multisim screen for the code-selection logic. The probe lights are for test purposes only. When a probe light is *on*, a 1 is indicated. Open F07-32 and run the code-selection logic simulation to observe the operation.

MULTISIM



```

library ieee;
use ieee.std_logic_1164.all;

entity FourBitBiDirSftReg is
port(R_L, DataIn, Clk: in std_logic;
      Q0, Q1, Q2, Q3: buffer std_logic);
end entity FourBitBiDirSftReg;

architecture FourBitBehavior of FourBitBiDirSftReg is
component dff is
port(D, Clk: in std_logic;
      Q: out std_logic);
end component dff;

signal D0, D1, D2, D3: std_logic;
begin
D0<=(DataIn and R_L) or (not R_L and Q1);
D1<=(Q0 and R_L) or (not R_L and Q2);
D2<=(Q1 and R_L) or (not R_L and Q3);
D3<=(Q2 and R_L) or (not R_L and DataIn);

DFF0:dff port map(D=> D0, Clk => Clk, Q => Q0);
DFF1:dff port map(D=> D1, Clk => Clk, Q => Q1);
DFF2:dff port map(D=> D2, Clk => Clk, Q => Q2);
DFF3:dff port map(D=> D3, Clk => Clk, Q => Q3);
end architecture FourBitBehavior;
    
```

R_L : Right-Left Shift
 DataIn : Serial data in
 Clk : System clock
 Q0-Q3 : Shift register output

D0: Logic for DFlipFlop DFF0
 D1: Logic for DFlipFlop DFF1
 D2: Logic for DFlipFlop DFF2
 D3: Logic for DFlipFlop DFF3

Component declaration
 for D flipflop (dff)

Bidirectional shift register logic
 defined for DFlipFlop stages
 DFF0 through DFF3

Component instantiations

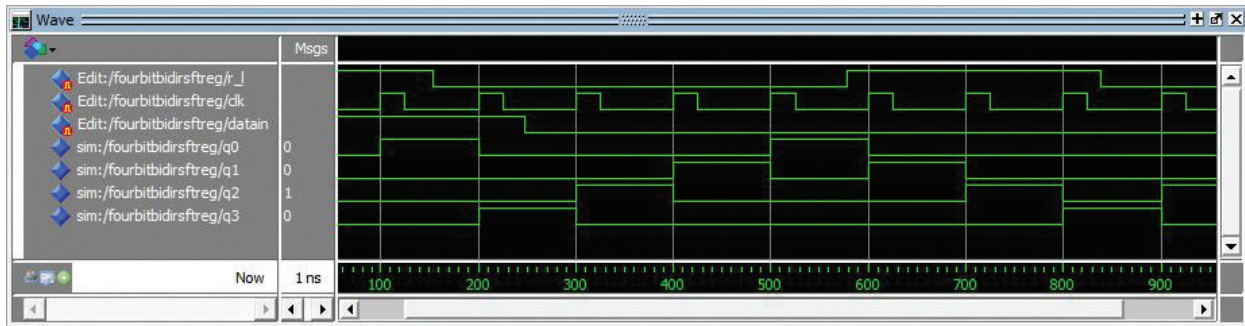


FIGURE 33 Development software simulation of 4-bit bidirectional shift register operation.

The difference in this simulation and a Multisim simulation is as follows. Multisim is used to debug and verify a design before it is described with an HDL such as VHDL or Verilog. The development software simulation is used to test the HDL code before programming it into a PLD. In this simulation Datain is set to a logic HIGH and shifted to Q0, given a logic HIGH on input shift direction R_L. A logic LOW is now assigned to the direction bit R_L and the logic HIGH on Q0 is shifted to Q3. After three clock cycles, the direction bit R_L is set to a logic HIGH and the value shifted to Q0 is shifted back to Q3, demonstrating the action of the 4-bit bidirectional shift register.

Hardware Testing

The serial-to-parallel data converter in Figure 16 in System Example 2 is used to illustrate the “exercising” procedure. The main objective in exercising the circuit is to force all elements (flip-flops and gates) into all of their states to be certain that nothing is stuck in a given state as a result of a fault. The input test pattern, in this case, must be designed to force each flip-flop in the registers into both states; to clock the counter through all of its eight states; and to take the control flip-flop, the clock generator, the one-shot, and the AND gate through their paces.

The input test pattern that accomplishes this objective for the serial-to-parallel data converter is based on the serial data format in Figure 17. It consists of the pattern 10101010 in one serial group of data bits followed by 01010101 in the next group, as shown in Figure 34. These patterns are generated on a repetitive basis by a special test-pattern generator. The basic test setup is shown in Figure 35.

After both patterns have been run through the circuit under test, all the flip-flops in the data-input register and in the data-output register have resided in both SET and RESET states, the counter has gone through its sequence (once for each bit pattern), and all the other devices have been exercised.

To check for proper operation, each of the parallel data outputs is observed for an alternating pattern of 1s and 0s as the input test patterns are repetitively shifted into the data-input register and then loaded into the data-output register. The proper timing diagram is shown in Figure 36. The outputs can be observed in pairs with a dual-trace oscilloscope, or all eight outputs can be observed simultaneously with a logic analyzer configured for timing analysis.

If one or more outputs of the data-output register are incorrect, then you must back up to the outputs of the data-input register. If these outputs are correct, then the problem is associated with the data-output register. Check the inputs to the data-output register directly on the pins of the PLD package for an open input line. Check that power and ground are correct (look for the absence of noise on the ground line). Verify that the load line is a solid LOW and that there are clock pulses on the clock input of the correct amplitude.



HANDS ON TIP

When measuring digital signals with an oscilloscope, you should always use dc coupling, rather than ac coupling. The reason that ac coupling is not best for viewing digital signals is that the 0 V level of the signal will appear at the *average* level of the signal, not at true ground or 0 V level. It is much easier to find a “floating” ground or incorrect logic level with dc coupling. If you suspect an open ground in a digital circuit, increase the sensitivity of the scope to the maximum possible. A good ground will never appear to have noise under this condition, but an open will likely show some noise, which appears as a random fluctuation in the 0 V level.

SHIFT REGISTERS

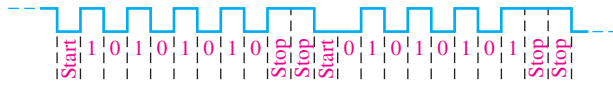


FIGURE 34 Sample test pattern.

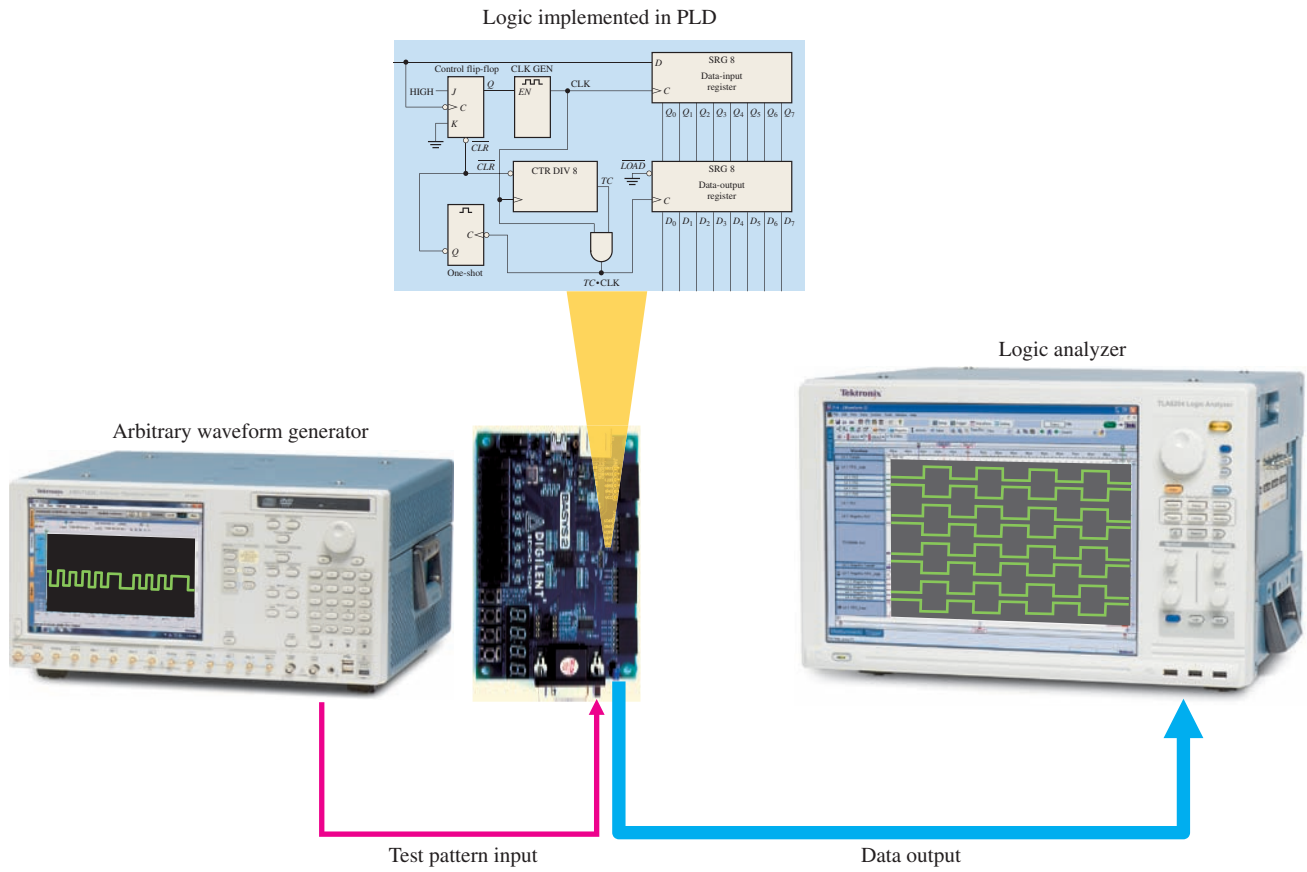


FIGURE 35 Serial-to-parallel data converter implemented in a PLD being exercised. (Instrument photos courtesy of Tektronix, Inc.; board photo courtesy of Digilent, Inc.)

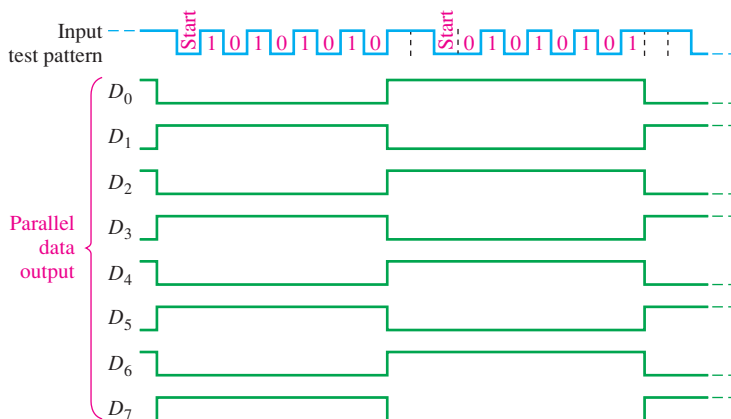


FIGURE 36 Proper outputs for the circuit under test in Figure 35. The input test pattern is shown.

Make sure that the connection to the logic analyzer did not short two output lines together. If all of these checks pass inspection, then it is likely that the output register is defective. If the data-input register outputs are also incorrect, the fault could be associated with the input register itself or with any of the other logic, and additional investigation is necessary to isolate the problem.

SECTION 7 CHECKUP

1. What is the purpose of providing a test input to a sequential logic circuit?
2. Generally, when an output waveform is found to be incorrect, what is the next step to be taken?

SUMMARY

- The basic types of data movement in shift registers are
 1. Serial in/shift right/serial out
 2. Serial in/shift left/serial out
 3. Parallel in/serial out
 4. Serial in/parallel out
 5. Parallel in/parallel out
 6. Rotate right
 7. Rotate left
- Shift register counters are shift registers with feedback that exhibit special sequences. Examples are the Johnson counter and the ring counter.
- The Johnson counter has $2n$ states in its sequence, where n is the number of stages.
- The ring counter has n states in its sequence.

KEY TERMS

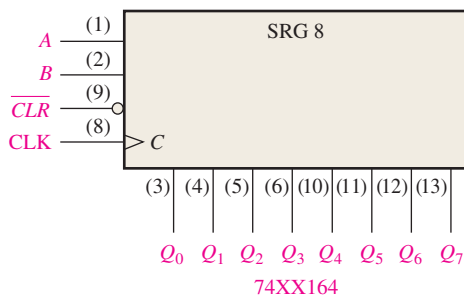
Bidirectional Having two directions. In a bidirectional shift register, the stored data can be shifted right or left.

Load To enter data into a shift register.

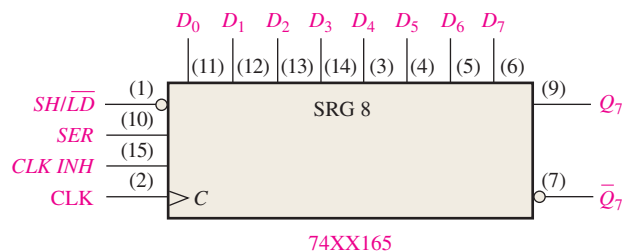
Register One or more flip-flops used to store and shift data.

Stage One storage element in a register.

FIXED-FUNCTION LOGIC

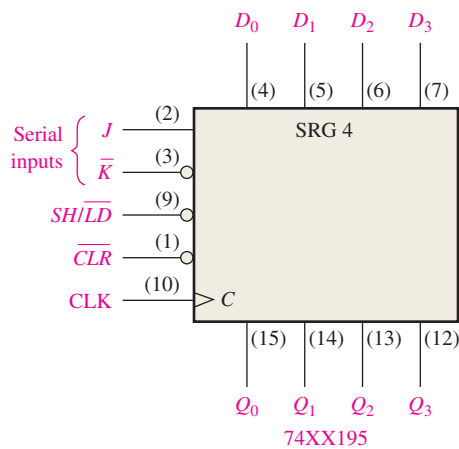


8-bit serial in/parallel out shift register

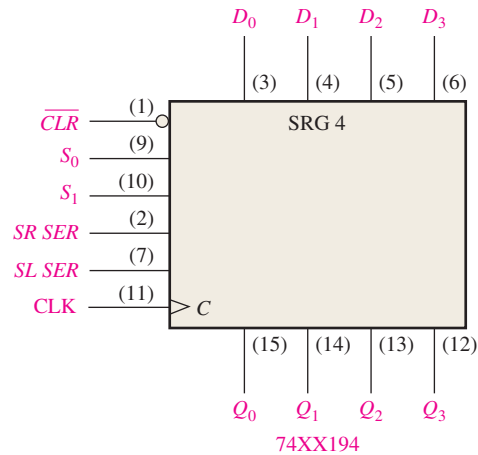


8-bit parallel load shift register

SHIFT REGISTERS



4-bit parallel access shift register



4-bit bidirectional universal shift register

TRUE/FALSE QUIZ

Answers are at the end of the chapter.

- Shift registers consist of an arrangement of flip-flops.
- Two functions of a shift register are data storage and data movement.
- In a serial shift register, several data bits are entered at the same time.
- All shift registers are defined by specified sequences.
- A shift register can have both parallel and serial outputs.
- A shift register with four stages can store a maximum count of fifteen.
- The Johnson counter is a special type of shift register.
- The modulus of an 8-bit Johnson counter is eight.
- A ring counter uses one flip-flop for each state in its sequence.
- A shift register can be used as a time delay device.

SELF-TEST

Answers are at the end of the chapter.

- A stage in a shift register consists of

(a) a latch	(b) a flip-flop
(c) a byte of storage	(d) four bits of storage
- To serially shift a byte of data into a shift register, there must be

(a) one clock pulse	(b) one load pulse
(c) eight clock pulses	(d) one clock pulse for each 1 in the data
- To parallel load a byte of data into a shift register with a synchronous load, there must be

(a) one clock pulse
(b) one clock pulse for each 1 in the data
(c) eight clock pulses
(d) one clock pulse for each 0 in the data
- The group of bits 10110101 is serially shifted (right-most bit first) into an 8-bit parallel output shift register with an initial state of 11100100. After two clock pulses, the register contains

(a) 01011110	(b) 10110101
(c) 01111001	(d) 00101101

SHIFT REGISTERS

5. With a 100 kHz clock frequency, eight bits can be serially entered into a shift register in
 - (a) $80\ \mu\text{s}$
 - (b) $8\ \mu\text{s}$
 - (c) 80 ms
 - (d) $10\ \mu\text{s}$
6. With a 1 MHz clock frequency, eight bits can be parallel entered into a shift register
 - (a) in $8\ \mu\text{s}$
 - (b) in the propagation delay time of eight flip-flops
 - (c) in $1\ \mu\text{s}$
 - (d) in the propagation delay time of one flip-flop
7. A modulus-10 Johnson counter requires
 - (a) ten flip-flops
 - (b) four flip-flops
 - (c) five flip-flops
 - (d) twelve flip-flops
8. A modulus-10 ring counter requires a minimum of
 - (a) ten flip-flops
 - (b) five flip-flops
 - (c) four flip-flops
 - (d) twelve flip-flops
9. When an 8-bit serial in/serial out shift register is used for a $24\ \mu\text{s}$ time delay, the clock frequency must be
 - (a) 41.67 kHz
 - (b) 333 kHz
 - (c) 125 kHz
 - (d) 8 MHz
10. The purpose of the ring counter in the keyboard encoding circuit of Figure 28 is
 - (a) to sequentially apply a HIGH to each row for detection of key closure
 - (b) to provide trigger pulses for the key code register
 - (c) to sequentially apply a LOW to each row for detection of key closure
 - (d) to sequentially reverse bias the diodes in each row

PROBLEMS

Answers to odd-numbered problems are at the end of the chapter.

SECTION 1 A System

1. Write the BCD code sequence produced by the encoder in Figure 2 if a 4-digit access number 4739 is entered on the keypad.
2. What is the state of shift register C in Figure 2 after two correct code digits are entered for the entry code 4739?
3. Assume the entry code is 1939. Determine the states of shift register A and shift register C after the second correct digit has been entered in Figure 2.
4. If the digit 4 is entered on the keypad, what appears on the outputs of shift register A in Figure 2?
5. Initially, what is the state of the Q outputs of the shift register in Figure 3.
6. What is the state of the shift register in Figure 3 after three clock pulses?
7. Assume the entry code is 7646 and the digits 7645 are entered. Determine the states of shift register A and shift register C after each of the digits is entered.
8. To increase the entry code to 5 digits, what would have to be added to the logic in Figure 3?

SECTION 2 Basic Shift Register Operations

9. Why are shift registers considered basic memory devices?
10. What is the storage capacity of a register that can retain two bytes of data?
11. Name two functions of a shift register.

SECTION 3 Types of Shift Registers

12. The sequence 1011 is applied to the input of a 4-bit serial shift register that is initially cleared. What is the state of the shift register after three clock pulses?

SHIFT REGISTERS

13. For the data input and clock in Figure 37, determine the states of each flip-flop in the shift register of Figure 6 and show the Q waveforms. Assume that the register contains all 1s initially.

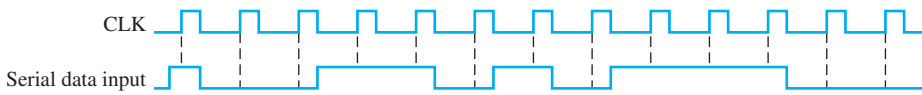


FIGURE 37

14. Solve Problem 13 for the waveforms in Figure 38.

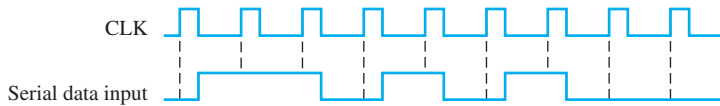


FIGURE 38

15. What is the state of the register in Figure 39 after each clock pulse if it starts in the 101001111000 state?

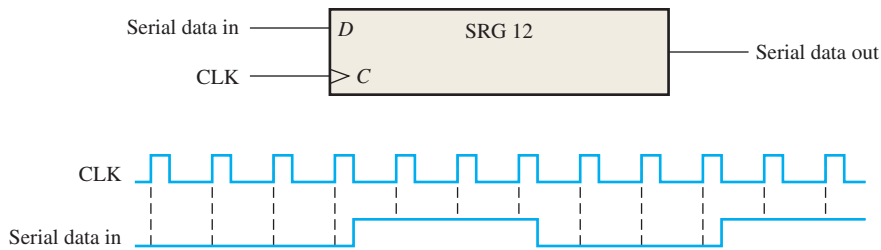


FIGURE 39

16. For the serial in/serial out shift register, determine the data-output waveform for the data-input and clock waveforms in Figure 40. Assume that the register is initially cleared.

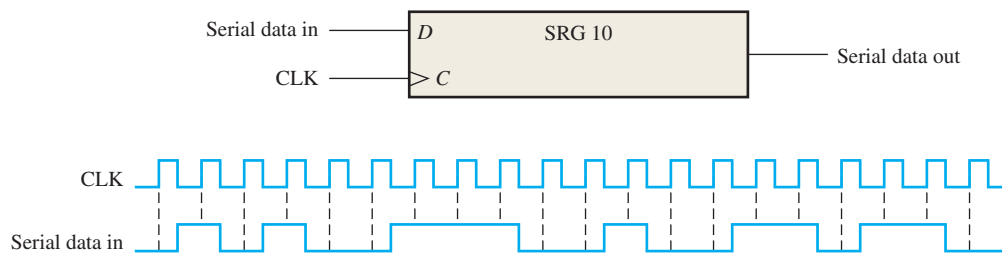


FIGURE 40

17. Solve Problem 16 for the waveforms in Figure 41.



FIGURE 41

SHIFT REGISTERS

18. A leading-edge clocked serial in/serial out shift register has a data-output waveform as shown in Figure 42. What binary number is stored in the 8-bit register if the first data bit out (left-most) is the LSB?

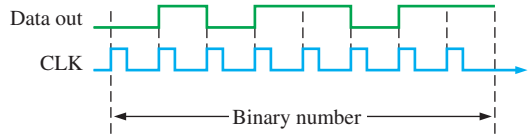


FIGURE 42

19. Show a complete timing diagram including the parallel outputs for the shift register in Figure 9. Use the waveforms in Figure 40 with the register initially clear.
20. Solve Problem 19 for the input waveforms in Figure 41.
21. Develop the Q_0 through Q_7 outputs for an 8-bit serial in/parallel out shift register with the input waveform shown in Figure 43.

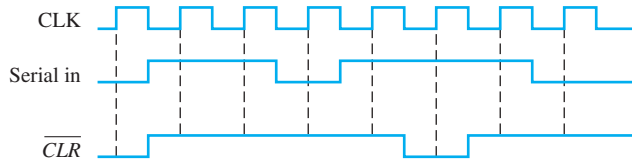


FIGURE 43

22. The shift register in Figure 44(a) has $SHIFT/\overline{LOAD}$ and CLK inputs as shown in part (b). The serial data input (SER) is a 0. The parallel data inputs are $D_0 = 1, D_1 = 0, D_2 = 1,$ and $D_3 = 0$ as shown. Develop the data-output waveform in relation to the inputs.

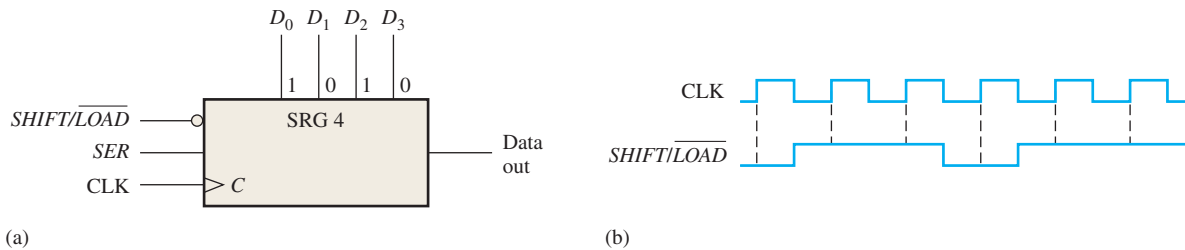


FIGURE 44

23. The waveforms in Figure 45 are applied to an 8-bit parallel in/serial out shift register. The parallel inputs are all 0. Determine the Q_7 waveform.

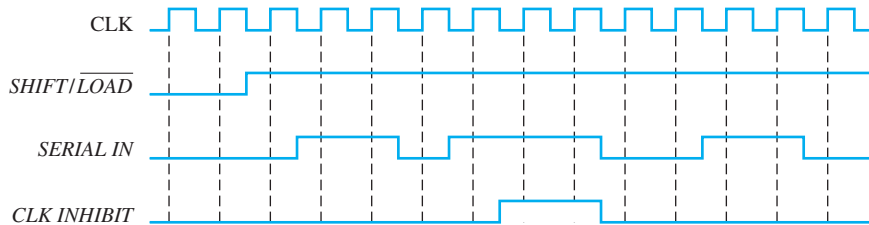


FIGURE 45

24. Solve Problem 23 if the parallel inputs are all 1.
25. Solve Problem 23 if the serial input is inverted.

SHIFT REGISTERS

26. Determine all the Q output waveforms for a 4-bit parallel in/parallel out shift register when the inputs are as shown in Figure 46.

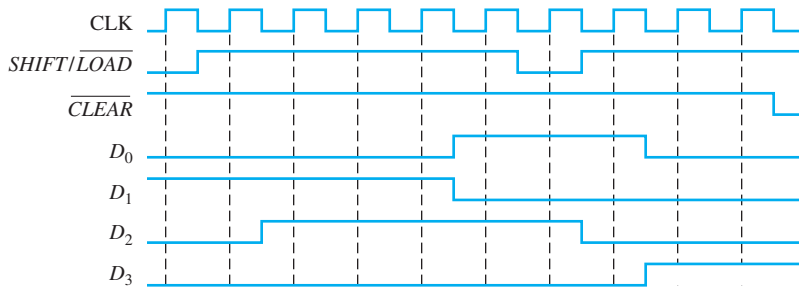


FIGURE 46

27. Solve Problem 26 if the $SHIFT/\overline{LOAD}$ input is inverted and the register is initially clear.
 28. Use two 4-bit shift registers to form an 8-bit shift register. Show the required connections.

SECTION 4 Bidirectional Shift Registers

29. For the 8-bit bidirectional register in Figure 47, determine the state of the register after each clock pulse for the $RIGHT/\overline{LEFT}$ control waveform given. A HIGH on this input enables a shift to the right, and a LOW enables a shift to the left. Assume that the register is initially storing the decimal number seventy-six in binary, with the right-most position being the LSB. There is a LOW on the data-input line.

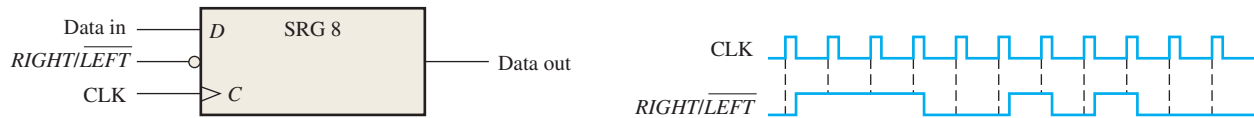


FIGURE 47

30. Solve Problem 29 for the waveforms in Figure 48.



FIGURE 48

31. Use two 4-bit bidirectional shift registers to create an 8-bit bidirectional shift register. Show the connections. Assume each shift register has a shift left (SL) data input and a shift right (SR) data input.
 32. Determine the Q outputs of a 4-bit serial in/parallel out bidirectional shift register with the inputs shown in Figure 49.

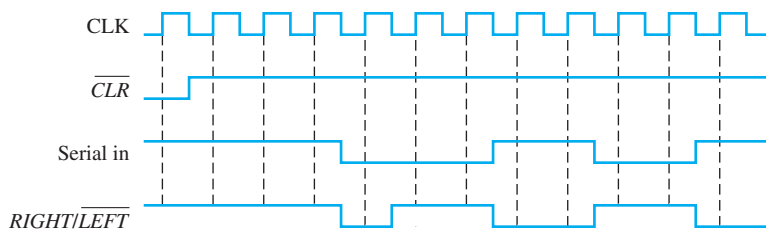


FIGURE 49

SECTION 5 Shift Register Counters

33. How many flip-flops are required to implement each of the following in a Johnson counter configuration:
 - (a) modulus-6
 - (b) modulus-10
 - (c) modulus-14
 - (d) modulus-16
34. Draw the logic diagram for a modulus-18 Johnson counter. Show the timing diagram and write the sequence in tabular form.
35. For the ring counter in Figure 50, show the waveforms for each flip-flop output with respect to the clock. Assume that FF0 is initially SET and that the rest are RESET. Show at least ten clock pulses.

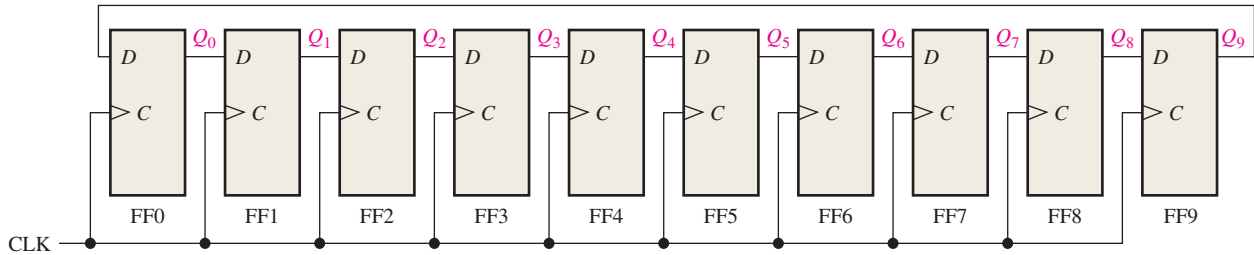


FIGURE 50

36. The waveform pattern in Figure 51 is required. Devise a ring counter, and indicate how it can be preset to produce this waveform on its Q_9 output. At CLK16 the pattern begins to repeat.

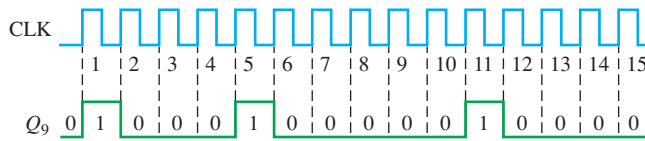


FIGURE 51

SECTION 6 Security System with VHDL and Verilog

37. If the code selection component of the security system is modified to store a five-digit code, what changes are needed to support the additional digit?
38. Explain the need for component one-shot B in the security system.
39. What would happen if two keypad keys were pressed before one-shot A could complete its timeout? How would the system respond?

SECTION 7 Troubleshooting

40. Based on the waveforms in Figure 52(a), determine the most likely problem with the register in part (b) of the figure.

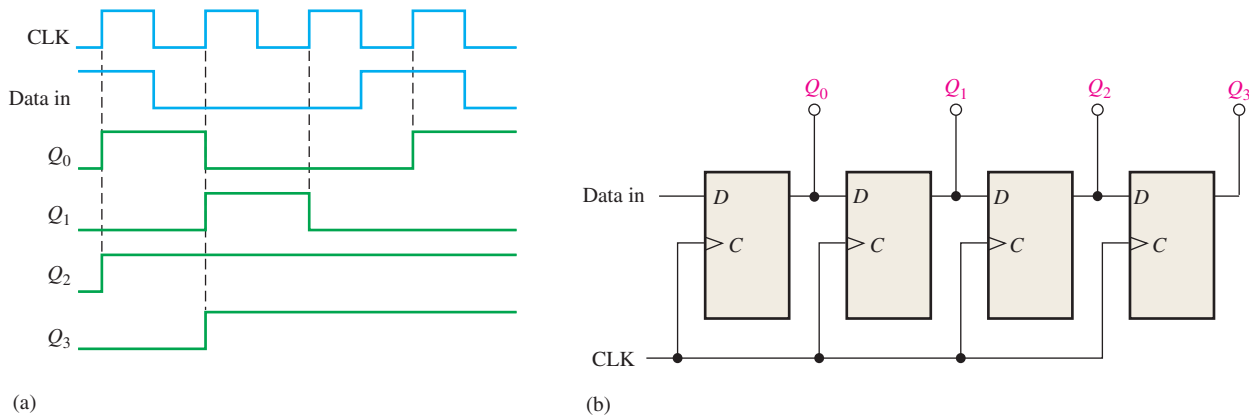
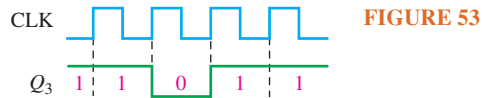


FIGURE 52

41. Refer to the parallel in/serial out shift register in Figure 13. The register is in the state where $Q_0Q_1Q_2Q_3 = 1001$, and $D_0D_1D_2D_3 = 1010$ is loaded in. When the $SHIFT/\overline{LOAD}$ input is taken HIGH, the data shown in Figure 53 are shifted out. Is this operation correct? If not, what is the most likely problem?



42. You have found that the bidirectional register in Figure 21 will shift data right but not left. What is the most likely fault?
43. For the keyboard encoder in Figure 28, list the possible faults for each of the following symptoms:
- The state of the key code register does not change for any key closure.
 - The state of the key code register does not change when any key in the third row is closed. A proper code occurs for all other key closures.
 - The state of the key code register does not change when any key in the first column is closed. A proper code occurs for all other key closures.
 - When any key in the second column is closed, the left three bits of the key code ($Q_0Q_1Q_2$) are correct, but the right three bits are all 1s.
44. Develop a test procedure for exercising the keyboard encoder in Figure 28. Specify the procedure on a step-by-step basis, indicating the output code from the key code register that should be observed at each step in the test.
45. What symptoms are observed for the following failures in the serial-to-parallel converter in Figure 16:
- AND gate output stuck in HIGH state
 - clock generator output stuck in LOW state
 - third stage of data-input register stuck in SET state
 - terminal count output of counter stuck in HIGH state

Special Problems

46. Modify the serial-to-parallel converter in Figure 16 to provide 16-bit conversion.
47. Develop an 8-bit parallel-to-serial data converter that produces the data format in Figure 17. Show a logic diagram and specify the devices.
48. Develop a power-on \overline{LOAD} circuit for the keyboard encoder in Figure 28. This circuit must generate a short-duration LOW pulse when the power switch is turned on.

MULTISIM TROUBLESHOOTING PRACTICE

MULTISIM



49. Open file P07-49 and follow the instructions given there.
50. Open file P07-50 and follow the instructions given there.
51. Open file P07-51 and follow the instructions given there.
52. Open file P07-52 and follow the instructions given there.
53. Open file P07-53 and follow the instructions given there.

ANSWERS TO SECTION CHECKUPS

SECTION 1 A System

- The OR gate detects a key closure and triggers one-shot A.
- 0100
- OS B, provides a delayed clock to register C.

SECTION 2 Basic Shift Register Operations

- Storage and data movement are two functions of a shift register.
- When the Q output of a flip-flop is HIGH, a 1 is stored.

SECTION 3 Types of Shift Registers

1. FF0: data input to J_0 , $\overline{\text{data}}$ input to K_0 ; FF1: Q_0 to J_1 , $\overline{Q_0}$ to K_1 ; FF2: Q_1 to J_2 , $\overline{Q_1}$ to K_2 ; FF3: Q_2 to J_3 , $\overline{Q_2}$ to K_3
2. Eight clock pulses
3. 0100 after 2 clock pulses
4. Take the serial output from the right-most flip-flop for serial out operation.
5. When $\overline{\text{SHIFT/LOAD}}$ is HIGH, the data are shifted right one bit per clock pulse. When $\overline{\text{SHIFT/LOAD}}$ is LOW, the data on the parallel inputs are loaded into the register.
6. The data outputs are 1001.

SECTION 4 Bidirectional Shift Registers

1. 1111 after the fifth clock pulse

SECTION 5 Shift Register Counters

1. Sixteen states are in an 8-bit Johnson counter sequence.
2. For a 3-bit Johnson counter: 000, 100, 110, 111, 011, 001, 000
3. 625 scans/second
4. $Q_5Q_4Q_3Q_2Q_1Q_0 = 011011$
5. The diodes provide unidirectional paths for pulling the ROWs LOW and preventing HIGHS on the ROW lines from being connected to the switch matrix. The resistors pull the COLUMN lines HIGH.

SECTION 6 Security System with VHDL and Verilog

1. Decimal-to-BCD encoder, 4-bit parallel-in/parallel-out shift register, 8-bit parallel-in/serial-out shift register, 4-bit magnitude comparator, code-selection logic, one-shot.
2. The OR gate is not treated as a component. It is described with a Boolean expression.

SECTION 7 Troubleshooting

1. A test input is used to sequence the circuit through all of its states.
2. Check the input to that portion of the circuit. If the signal on that input is correct, the fault is isolated to the circuitry between the good input and the bad output.

ANSWERS TO RELATED PROBLEMS FOR EXAMPLES

- 1 See Figure 54.

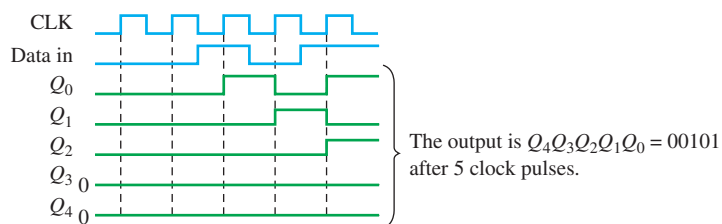


FIGURE 54

SHIFT REGISTERS

- 2 The state of the register after three additional clock pulses is 0000.
- 3 See Figure 55.

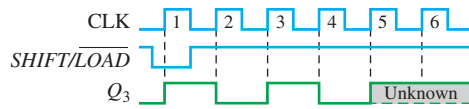


FIGURE 55

- 4 See Figure 56.

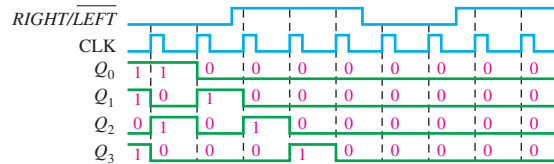


FIGURE 56

- 5 See Figure 57.

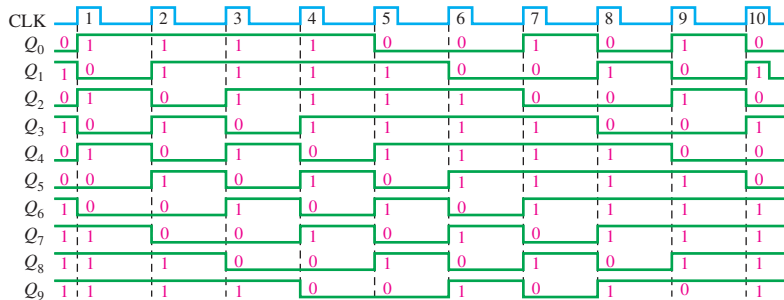


FIGURE 57

ANSWERS TO TRUE/FALSE QUIZ

1. T 2. T 3. F 4. F 5. T 6. T
7. T 8. F 9. T 10. T

ANSWERS TO SELF-TEST

1. (b) 2. (c) 3. (a) 4. (c) 5. (a)
6. (d) 7. (c) 8. (a) 9. (b) 10. (c)

ANSWERS TO ODD-NUMBERED PROBLEMS

1. 1001001101110100
3. shift register A: 1001
shift register C: 00000100
5. Q₀ = 1, Q₁ = 0, Q₂ = 0, Q₃ = 0
7. The states of shift registers A and C after each key closure when entering 7645 are:
After key 7 is pressed:
Shift register A contains 0111
Shift register C contains 11000

SHIFT REGISTERS

After key 6 is pressed:

Shift register A contains 0110

Shift register C contains 11100

After key 4 is pressed:

Shift register A contains 0100

Shift register C contains 11110

After key 5 (an incorrect entry) is pressed:

Shift register A contains 0000

Shift register C contains 10000

- 9. Shift registers store binary data.
- 11. Shift data and store data.
- 13. See Figure P-48.

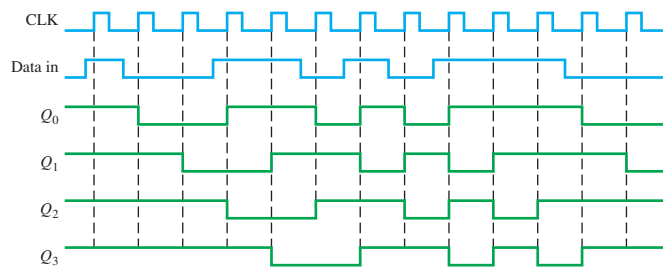


FIGURE P-48

- 15. Initially: 101001111000
- CLK1: 010100111100
- CLK2: 001010011110
- CLK3: 000101001111
- CLK4: 000010100111
- CLK5: 100001010011
- CLK6: 110000101001
- CLK7: 111000010100
- CLK8: 011100001010
- CLK9: 001110000101
- CLK10: 000111000010
- CLK11: 100011100001
- CLK12: 110001110000

- 17. See Figure P-49.

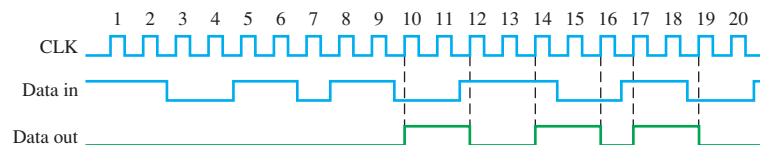


FIGURE P-49

SHIFT REGISTERS

19. See Figure P-50.

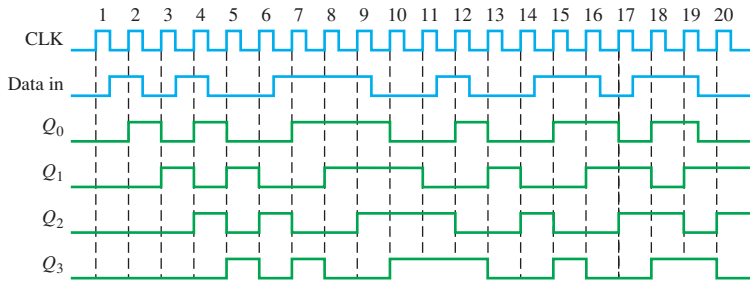


FIGURE P-50

21. See Figure P-51.

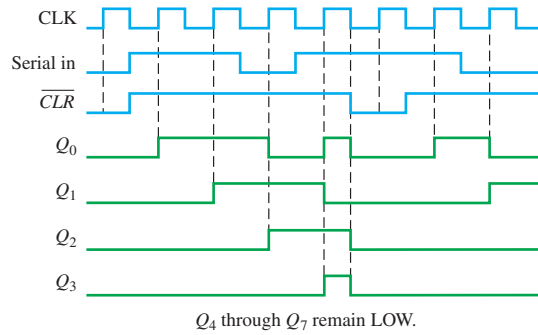


FIGURE P-51

23. See Figure P-52.

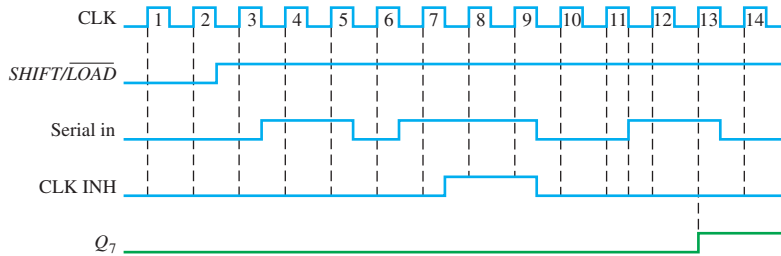


FIGURE P-52

25. See Figure P-53.

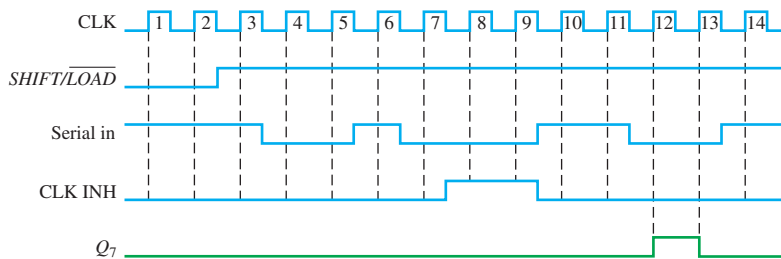


FIGURE P-53

SHIFT REGISTERS

27. See Figure P-54.

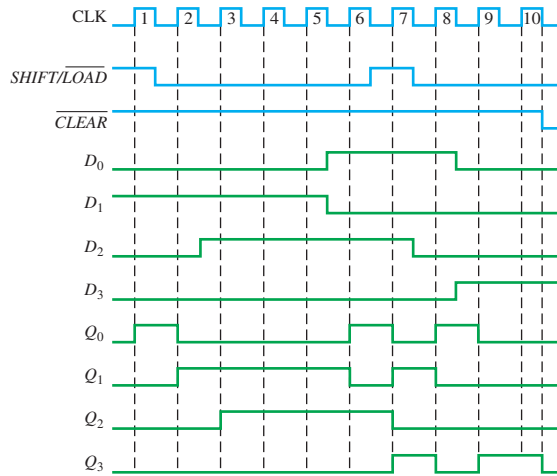


FIGURE P-54

29. Initially (76):	01001100	
CLK1:	10011000	left
CLK2:	01001100	right
CLK3:	00100110	right
CLK4:	00010011	right
CLK5:	00100110	left
CLK6:	01001100	left
CLK7:	00100110	right
CLK8:	01001100	left
CLK9:	00100110	right
CLK10:	01001100	left
CLK11:	10011000	left

31. See Figure P-55.

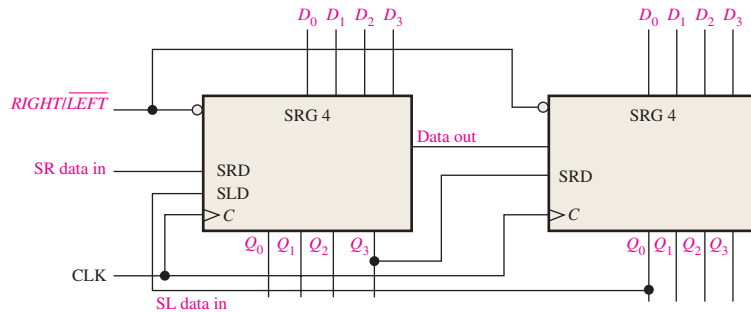


FIGURE P-55

33. (a) 3 (b) 5 (c) 7 (d) 8

35. See Figure P-56.

37. The hard coded binary value stored in the 8-bit shift register C component will need to be changed from 00010000_2 to 00100000_2 .

39. If two key presses were read by the code selection component before one shot A could timeout, we would skip a stored code value. The system would read the second value as an error and the system would not disarm.

SHIFT REGISTERS

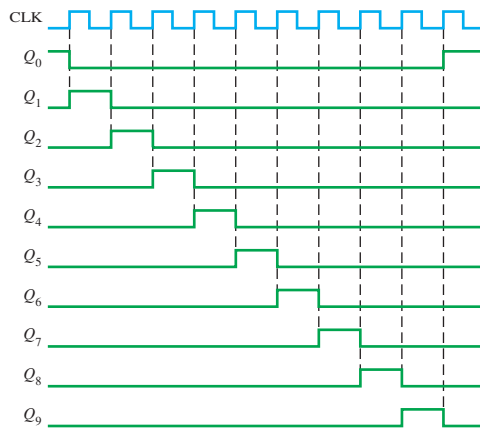


FIGURE P-56

41. D_3 input open
43. (a) No clock at switch closure because of faulty NAND (negative-OR) gate or one-shot; open clock (C) input to key code register; open SH/\overline{LD} input to key code register
 (b) Diode in third row open; Q_2 output of ring counter open
 (c) The NAND (negative-OR) gate input connected to the first column is open or shorted.
 (d) The “2” input to the column encoder is open.
45. (a) Contents of data output register remain constant.
 (b) Contents of both registers do not change.
 (c) Third stage output of data output register remains HIGH.
 (d) Clock generator is disabled after each pulse by the flip-flop being continuously SET and then RESET.
47. See Figure P-57.

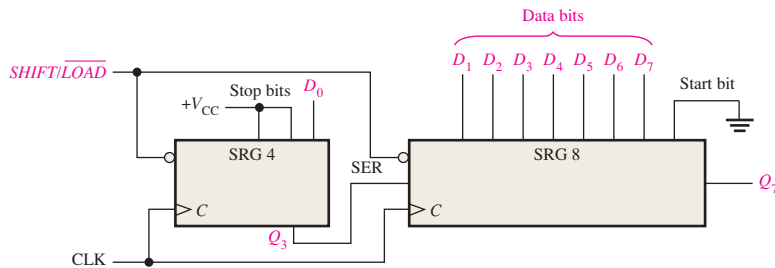


FIGURE P-57

49. **Circuit fault:** Line to CLK input of U3 is open.
Predicted effect of fault: Q0 and Q1 will sequence normally. Q2 and Q3 will remain LOW.
Observed effect of introduced fault: Q0 and Q1 will sequence normally. Q2 and Q3 will remain LOW.
51. **Circuit fault:** The QH output of the 74LS165 shift register is shorted to ground.
Predicted effect of fault: The QH output is always LOW but the notQH output behaves as expected.
Observed effect of introduced fault: The QH output is always LOW but the notQH output behaves as expected.
53. **Observed operation:** The ring counter can initiate circulation of 1s but not 0s.
Suspected fault: The notRESET line of the first stage is shorted to V_{CC} .
Effect of introduced fault: The ring counter can initiate circulation of 1s but not 0s.

COUNTERS

COUNTERS

OUTLINE

- 1 A System
- 2 Finite State Machines
- 3 Asynchronous Counters
- 4 Synchronous Counters
- 5 Up/Down Synchronous Counters
- 6 Cascaded Counters
- 7 Counter Decoding
- 8 Counters with VHDL and Verilog
- 9 Troubleshooting

OBJECTIVES

- Explain how a digital clock operates
- Discuss the types of state machines
- Describe the difference between an asynchronous and a synchronous counter
- Analyze counter timing diagrams
- Analyze counter circuits
- Explain how propagation delays affect the operation of a counter
- Determine the modulus of a counter
- Modify the modulus of a counter
- Recognize the difference between a 4-bit binary counter and a decade counter
- Use an up/down counter to generate forward and reverse binary sequences
- Determine the sequence of a counter
- Use cascaded counters to achieve a higher modulus

- Use logic gates to decode any given state of a counter
- Eliminate glitches in counter decoding
- Troubleshoot counters for various types of faults

KEY TERMS

Counter	Recycle
State machine	Modulus
Moore state machine	Decade
Mealy state machine	Synchronous
Asynchronous	Cascade

INTRODUCTION

Flip-flops can be connected together to perform counting operations. Such a group of flip-flops is a counter. The number of flip-flops used and the way in which they are connected determine the number of states (called the modulus) and also the specific sequence of states that the counter goes through during each complete cycle.

Counters are classified into two broad categories according to the way they are clocked: asynchronous and synchronous. In asynchronous counters, commonly called

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ripple counters, the first flip-flop is clocked by the external clock pulse and then each successive flip-flop is clocked by the output of the preceding flip-flop. In synchronous counters, the clock input is connected to all of the flip-flops

so that they are clocked simultaneously. Within each of these two categories, counters are classified primarily by the type of sequence, the number of states, or the number of flip-flops in the counter.

1 A SYSTEM

A **counter*** is a sequential logic device that is used to divide signal frequency, count events, and generate specified sequences of bits. Counters are made up of flip-flops connected in various ways to produce the desired results. A common example of an application of counters is in timekeeping systems.

After completing this section, you should be able to

- Explain the overall operation of a digital clock
- Describe how counters are used for counting down a frequency to achieve an output that indicates time of day

Figure 1 is a simplified logic diagram of a digital clock that displays seconds, minutes, and hours. First, a 60 Hz sinusoidal ac voltage is converted to a 60 Hz pulse waveform and divided down to a 1 Hz pulse waveform by a divide-by-60 counter formed by a divide-by-10 counter followed by a divide-by-6 counter.

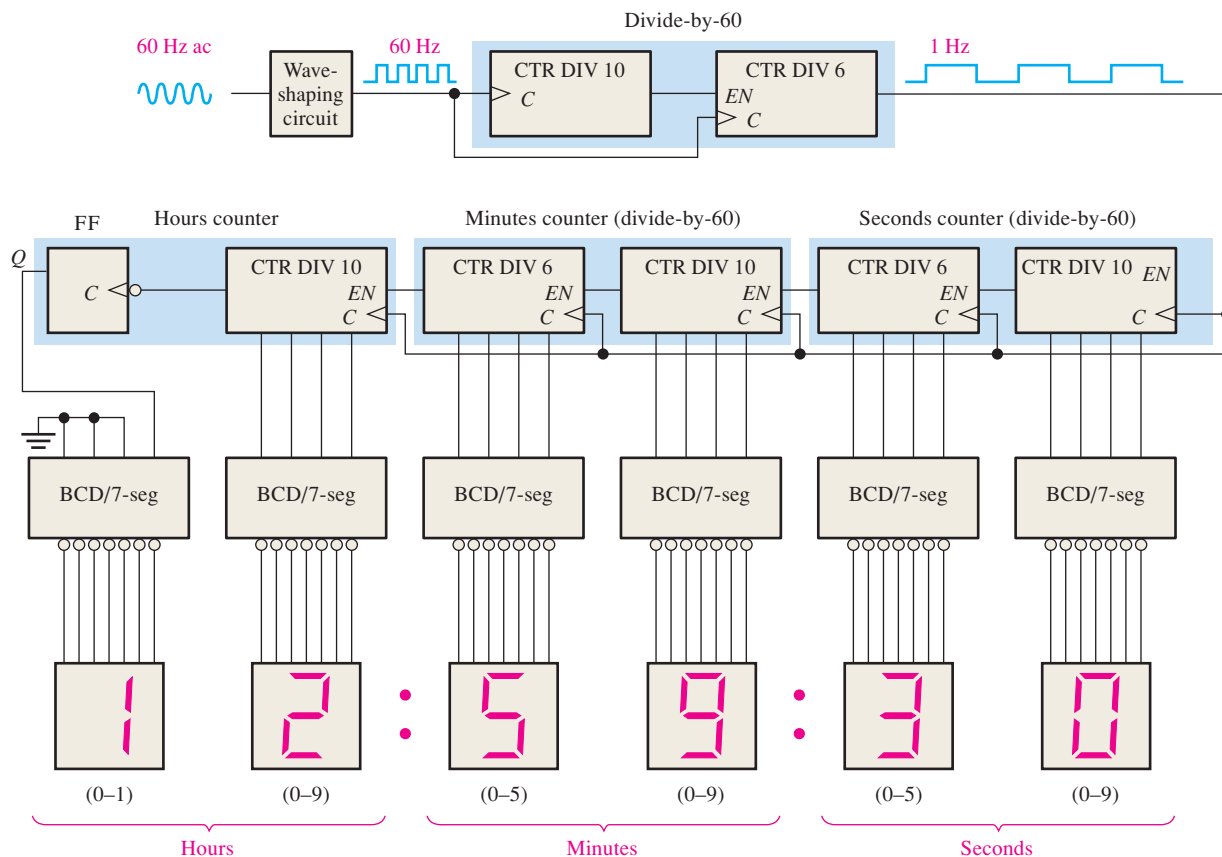


FIGURE 1 Simplified logic diagram for a 12-hour digital clock. Logic details using specific devices are shown in Figures 2 and 3.

*The bold terms in color are key terms and are included in a Key Term glossary at the end of the chapter.

COUNTERS

Both the *seconds* and *minutes* counts are also produced by divide-by-60 counters, the details of which are shown in Figure 2. These counters count from 0 to 59 and then recycle to 0; synchronous decade counters are used in this particular implementation. Notice that the divide-by-6 portion is formed with a decade counter with a truncated sequence achieved by using the decoder count 6 to asynchronously clear the counter. The terminal count (TC), 59, is also decoded to enable the next counter in the chain. The **terminal count** is the final state in a counter's sequence.

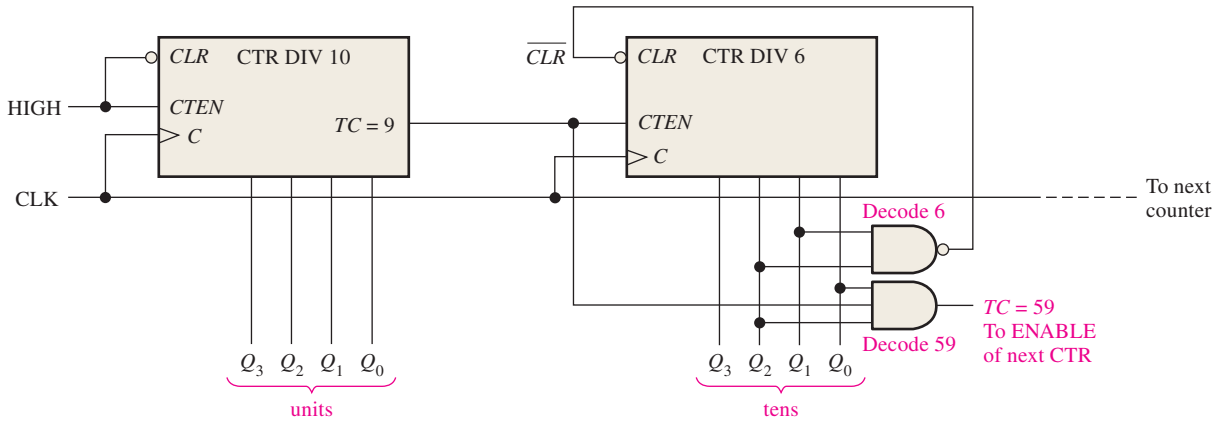


FIGURE 2 Logic diagram of typical divide-by-60 counter using synchronous decade counters. Note that the outputs are in binary order (the right-most bit is the LSB).

The *hours* counter is implemented with a decade counter and a flip-flop as shown in Figure 3. Consider that initially both the decade counter and the flip-flop are RESET, and the decode-12 gate (G_2) and the decode-9 gate (G_1) outputs are HIGH. The decade counter advances through all of its states from zero to nine, and on the clock pulse that recycles it from nine back to zero, the flip-flop goes to the SET state ($J = 1, K = 0$). This

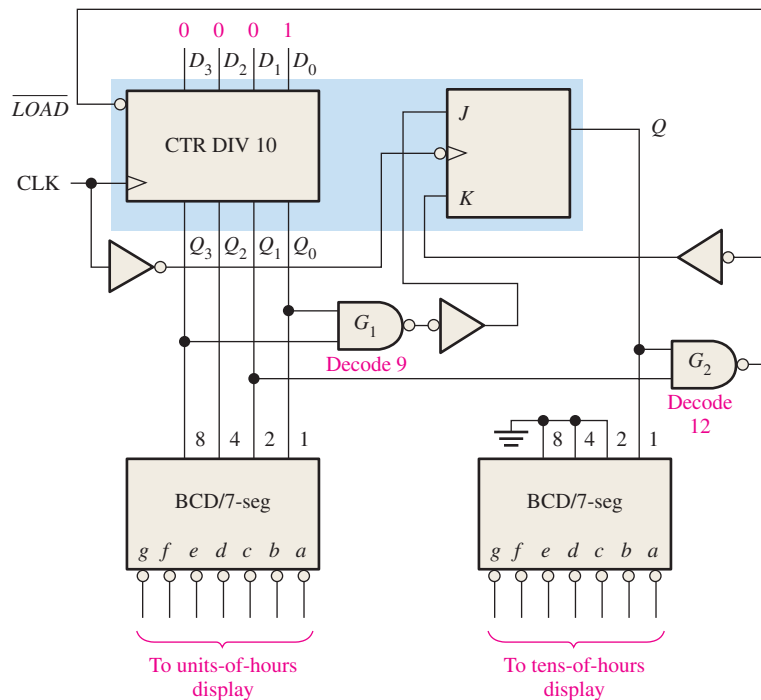


FIGURE 3 Logic diagram for hours counter and decoders. Note that on the counter inputs and outputs, the right-most bit is the LSB.

illuminates a 1 on the tens-of-hours display. The total count is now ten (the decade counter is in the zero state and the flip-flop is SET).

Next, the total count advances to eleven and then to twelve. In state 12 the Q_2 output of the decade counter is HIGH, the flip-flop is still SET, and thus the decode-12 gate output is LOW. This activates the \overline{LOAD} input of the decade counter. On the next clock pulse, the decade counter is preset to 0001 from the data inputs, and the flip-flop is RESET ($J = 0, K = 1$). As you can see, this logic always causes the counter to recycle from twelve back to one rather than back to zero.

SECTION 1 CHECKUP*

1. Explain the purpose of each NAND gate in Figure 3.
2. Identify the two recycle conditions for the hours counter in Figure 1. Explain the reason for each.

*Answers are at the end of the chapter.

2 FINITE STATE MACHINES

A **state machine** is a sequential circuit having a limited (finite) number of states occurring in a prescribed order. A counter is an example of a state machine; the number of states is called the *modulus*. Two types of state machines are the Moore and the Mealy. The **Moore state machine** is one where the outputs depend only on the internal present state. The **Mealy state machine** is one where the outputs depend on both the internal present state and on the inputs. Both types have a timing input (clock) that is not considered a controlling input.

After completing this section, you should be able to

- Describe a Moore state machine
- Describe a Mealy state machine
- Discuss examples of Moore and Mealy state machines

General Models of Finite State Machines

A Moore state machine consists of combinational logic that determines the sequence and memory (flip-flops), as shown in Figure 4(a). A Mealy state machine is shown in part (b). In the Moore machine, the combinational logic is a gate array with outputs that determine the next state of the flip-flops in the memory. There may or may not be inputs to the combinational logic. There may also be output combinational logic, such as a decoder. If there is an input(s), it does not affect the outputs because they always correspond to and are dependent only on the present state of the memory. For the Mealy machine, the present state affects the outputs, just as in the Moore machine; but in addition, the inputs also affect the outputs. The outputs come directly from the combinational logic and not the memory.

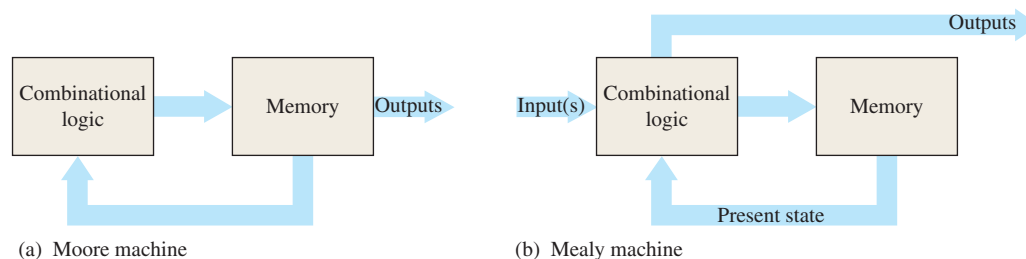


FIGURE 4 Two types of sequential logic.

EXAMPLE OF A MOORE MACHINE Figure 5(a) shows a Moore machine (modulus-26 binary counter with states 0 through 25) that is used to control the number of tablets (25) that go into each bottle in an assembly line. When the binary number in the memory (flip-flops) reaches binary 25 (11001), the counter recycles to 0 and the tablet flow and clock is cut off until the next bottle is in place. The combinational logic for state transitions sets the modulus of the counter so that it sequences from binary state 0 to binary state 25, where 0 is the reset or rest state and the output combinational logic decodes binary state 25. There is no input in this case, other than the clock, so the next state is determined only by the present state, which makes this a Moore machine. One tablet is bottled for each clock pulse. Once a bottle is in place, the first tablet is inserted at binary state 1, the second at binary state 2, and the twenty-fifth tablet when the binary state is 25. Count 25 is decoded and used to stop the flow of tablets and the clock. The counter recycles to binary state 0 and waits until the next bottle is in position. Then the clock resumes, the count goes to binary state 1, and the cycle repeats, as illustrated by the state diagram in Figure 5(b).

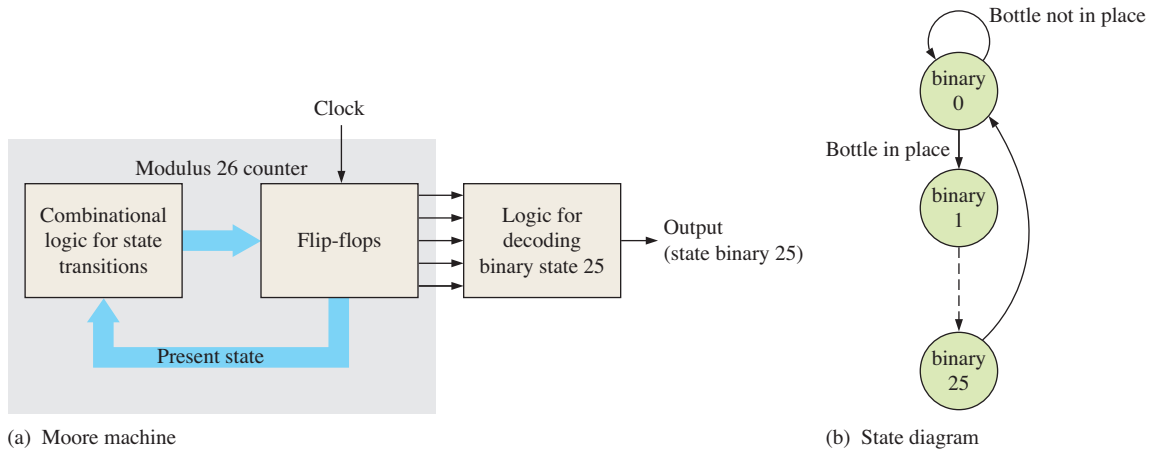


FIGURE 5 A fixed-modulus binary counter as an example of a Moore state machine. The dashed line in the state diagram means the states between binary 1 and 25 are not shown for simplicity.

EXAMPLE OF A MEALY MACHINE Let's assume that the tablet-bottling system uses three different sizes of bottles: a 25-tablet bottle, a 50-tablet bottle, and a 100-tablet bottle. This operation requires a state machine with three different terminal counts: 25, 50, and 100. One approach is illustrated in Figure 6(a). The combinational logic sets the

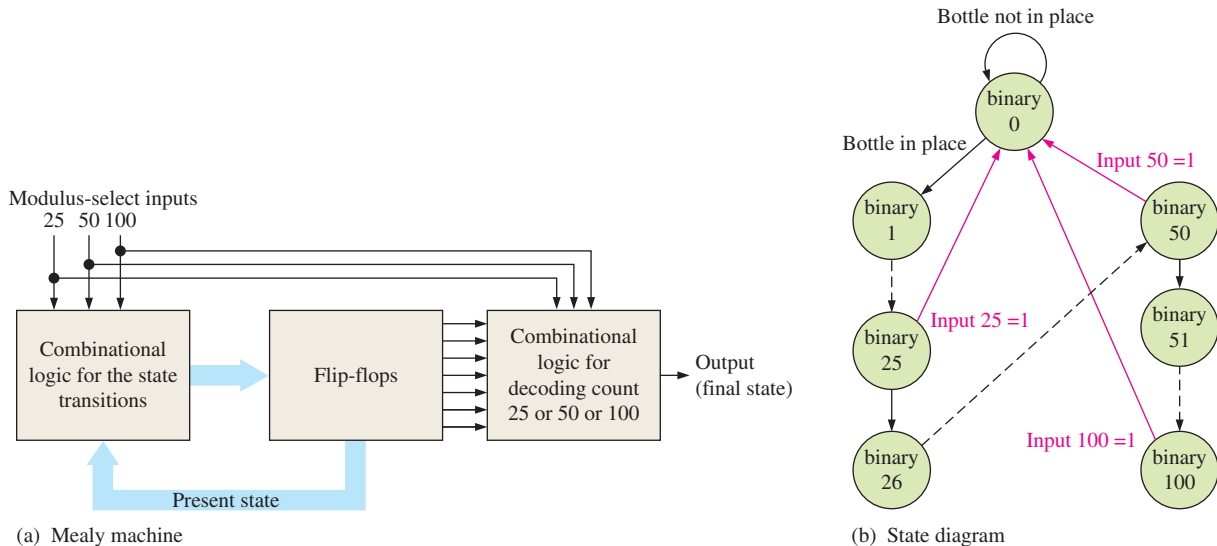


FIGURE 6 A variable-modulus binary counter as an example of a Mealy state machine. The red arrows in the state diagram represent the recycle paths that depend on the input number. The black dashed lines mean the interim states are not shown for simplicity.

modulus of the counter depending on the modulus-select inputs. The output of the counter depends on both the present state and the modulus-select inputs, making this a Mealy machine. The state diagram is shown in part (b).

SECTION 2 CHECKUP

1. What characterizes a finite state machine?
2. Name the types of finite state machines.
3. Explain the difference between the two types of state machines.

3 ASYNCHRONOUS COUNTERS

The term **asynchronous** refers to events that do not have a fixed time relationship with each other and, generally, do not occur at the same time. An *asynchronous counter* is one in which the flip-flops (FF) within the counter do not change states at exactly the same time because they do not have a common clock pulse.

After completing this section, you should be able to

- Describe the operation of a 2-bit asynchronous binary counter
- Describe the operation of a 3-bit asynchronous binary counter
- Define *ripple* in relation to counters
- Describe the operation of an asynchronous decade counter
- Develop counter timing diagrams

A 2-Bit Asynchronous Binary Counter

Figure 7 shows a 2-bit counter connected for asynchronous operation. Notice that the clock (CLK) is applied to the clock input (C) of *only* the first flip-flop, FF0, which is always the least significant bit (LSB). The second flip-flop, FF1, is triggered by the \bar{Q}_0 output of FF0. FF0 changes state at the positive-going edge of each clock pulse, but FF1 changes only when triggered by a positive-going transition of the \bar{Q}_0 output of FF0. Because of the inherent propagation delay time through a flip-flop, a transition of the input clock pulse (CLK) and a transition of the \bar{Q}_0 output of FF0 can never occur at exactly the same time. Therefore, the two flip-flops are never simultaneously triggered, so the counter operation is asynchronous.

The clock input of an asynchronous counter is always connected only to the LSB flip-flop.

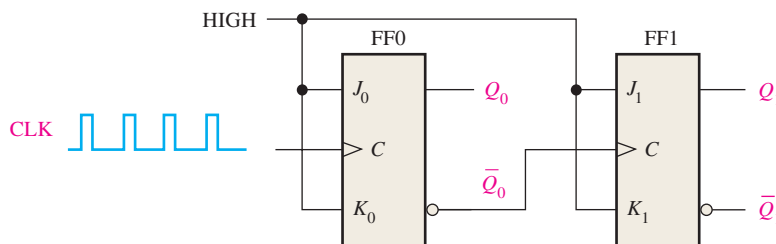


FIGURE 7 A 2-bit asynchronous binary counter. Open file F08-07 to verify operation.



THE TIMING DIAGRAM Let's examine the basic operation of the asynchronous counter of Figure 7 by applying four clock pulses to FF0 and observing the Q output of each flip-flop. Figure 8 illustrates the changes in the state of the flip-flop outputs in response to the clock pulses. Both flip-flops are connected for toggle operation ($J = 1, K = 1$) and are assumed to be initially RESET (Q LOW).

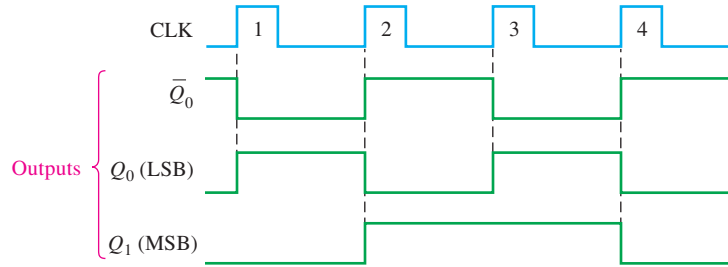


FIGURE 8 Timing diagram for the counter of Figure 7. Output waveforms are shown in green.

Asynchronous counters are also known as ripple counters.

The positive-going edge of CLK1 (clock pulse 1) causes the Q_0 output of FF0 to go HIGH, as shown in Figure 8. At the same time the $\overline{Q_0}$ output goes LOW, but it has no effect on FF1 because a positive-going transition must occur to trigger the flip-flop. After the leading edge of CLK1, $Q_0 = 1$ and $Q_1 = 0$. The positive-going edge of CLK2 causes Q_0 to go LOW. Output $\overline{Q_0}$ goes HIGH and triggers FF1, causing Q_1 to go HIGH. After the leading edge of CLK2, $Q_0 = 0$ and $Q_1 = 1$. The positive-going edge of CLK3 causes Q_0 to go HIGH again. Output $\overline{Q_0}$ goes LOW and has no effect on FF1. Thus, after the leading edge of CLK3, $Q_0 = 1$ and $Q_1 = 1$. The positive-going edge of CLK4 causes Q_0 to go LOW, while $\overline{Q_0}$ goes HIGH and triggers FF1, causing Q_1 to go LOW. After the leading edge of CLK4, $Q_0 = 0$ and $Q_1 = 0$. The counter has now recycled to its original state (both flip-flops are RESET).

In the timing diagram, the waveforms of the Q_0 and Q_1 outputs are shown relative to the clock pulses as illustrated in Figure 8. For simplicity, the transitions of Q_0 , Q_1 , and the clock pulses are shown as simultaneous even though this is an asynchronous counter. There is, of course, some small delay between the CLK and the Q_0 transition and between the $\overline{Q_0}$ transition and the Q_1 transition.

Q_0 is always the LSB unless otherwise specified.

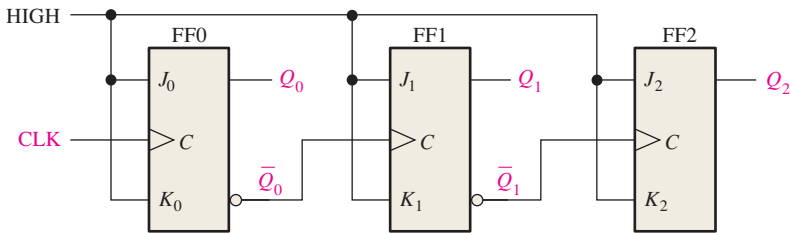
Note in Figure 8 that the 2-bit counter exhibits four different states, as you would expect with two flip-flops ($2^2 = 4$). Also, notice that if Q_0 represents the least significant bit (LSB) and Q_1 represents the most significant bit (MSB), the sequence of counter states represents a sequence of binary numbers as listed in Table 1.

TABLE 1 • Binary state sequence for the counter in Figure 7.		
CLOCK PULSE	Q_1	Q_0
Initially	0	0
1	0	1
2	1	0
3	1	1
4 (recycles)	0	0

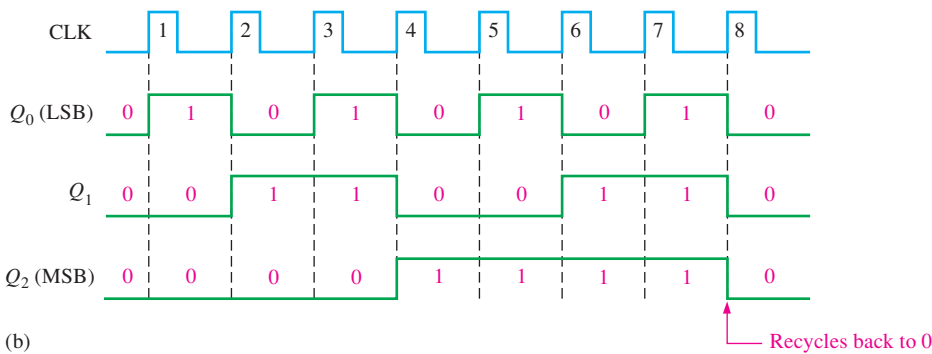
Since it goes through a binary sequence, the counter in Figure 7 is a binary counter. It actually counts the number of clock pulses up to three, and on the fourth pulse it recycles to its original state ($Q_0 = 0, Q_1 = 0$). The term **recycle** is commonly applied to counter operation; it refers to the transition of the counter from its final state back to its original state.

A 3-BIT ASYNCHRONOUS BINARY COUNTER The state sequence for a 3-bit binary counter is listed in Table 2, and a 3-bit asynchronous binary counter is shown in Figure 9(a). The basic operation is the same as that of the 2-bit counter except that the 3-bit counter has eight states, due to its three flip-flops. A timing diagram is shown in Figure 9(b) for eight clock pulses. Notice that the counter progresses through a binary count of zero through seven and then recycles to the zero state. This counter can be easily expanded for higher count, by connecting additional toggle flip-flops.

TABLE 2 • State sequence for a 3-bit binary counter.			
CLOCK PULSE	Q_2	Q_1	Q_0
Initially	0	0	0
1	0	0	1
2	0	1	0
3	0	1	1
4	1	0	0
5	1	0	1
6	1	1	0
7	1	1	1
8 (recycles)	0	0	0



(a)



(b)

FIGURE 9 Three-bit asynchronous binary counter and its timing diagram for one cycle. Open file F08-09 to verify operation.

MULTISIM

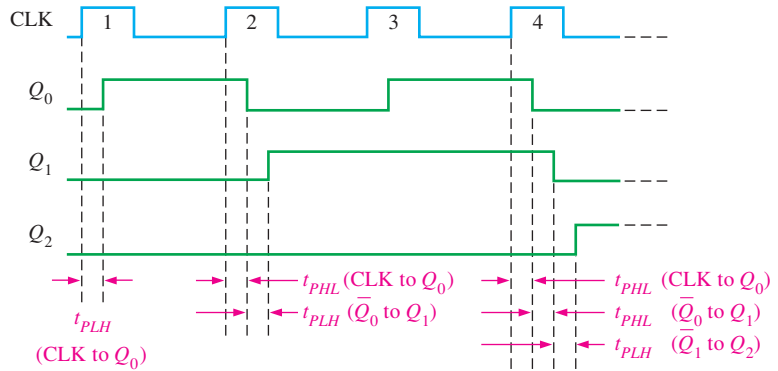


PROPAGATION DELAY Asynchronous counters are commonly referred to as **ripple counters** for the following reason: The effect of the input clock pulse is first “felt” by FF0. This effect cannot get to FF1 immediately because of the propagation delay through FF0. Then there is the propagation delay through FF1 before FF2 can be triggered.

Thus, the effect of an input clock pulse “ripples” through the counter, taking some time, due to propagation delays, to reach the last flip-flop.

To illustrate, notice that all three flip-flops in the counter of Figure 9 change state on the leading edge of CLK4. This ripple clocking effect is shown in Figure 10 for the first four clock pulses, with the propagation delays indicated. The LOW-to-HIGH transition of Q_0 occurs one delay time (t_{PLH}) after the positive-going transition of the clock pulse. The LOW-to-HIGH transition of Q_1 occurs one delay time (t_{PLH}) after the positive-going transition of \bar{Q}_0 . The LOW-to-HIGH transition of Q_2 occurs one delay time (t_{PLH}) after the positive-going transition of \bar{Q}_1 . As you can see, FF2 is not triggered until two delay times after the positive-going edge of the clock pulse, CLK4. Thus, it takes three propagation delay times for the effect of the clock pulse, CLK4, to ripple through the counter and change Q_2 from LOW to HIGH.

FIGURE 10 Propagation delays in a 3-bit asynchronous (ripple-clocked) binary counter.



This cumulative delay of an asynchronous counter is a major disadvantage in many applications because it limits the rate at which the counter can be clocked and creates decoding problems. The maximum cumulative delay in a counter must be less than the period of the clock waveform.

EXAMPLE 1

A 4-bit asynchronous binary counter is shown in Figure 11(a). Each flip-flop is negative edge-triggered and has a propagation delay for 10 nanoseconds (ns). Develop a timing diagram showing the Q output of each flip-flop, and determine the total propagation delay time from the triggering edge of a clock pulse until a corresponding change can occur in the state of Q_3 . Also determine the maximum clock frequency at which the counter can be operated.

SOLUTION

The timing diagram with delays omitted is as shown in Figure 11(b). For the total delay time, the effect of CLK8 or CLK16 must propagate through four flip-flops before Q_3 changes, so

$$t_{p(tot)} = 4 \times 10 \text{ ns} = \mathbf{40 \text{ ns}}$$

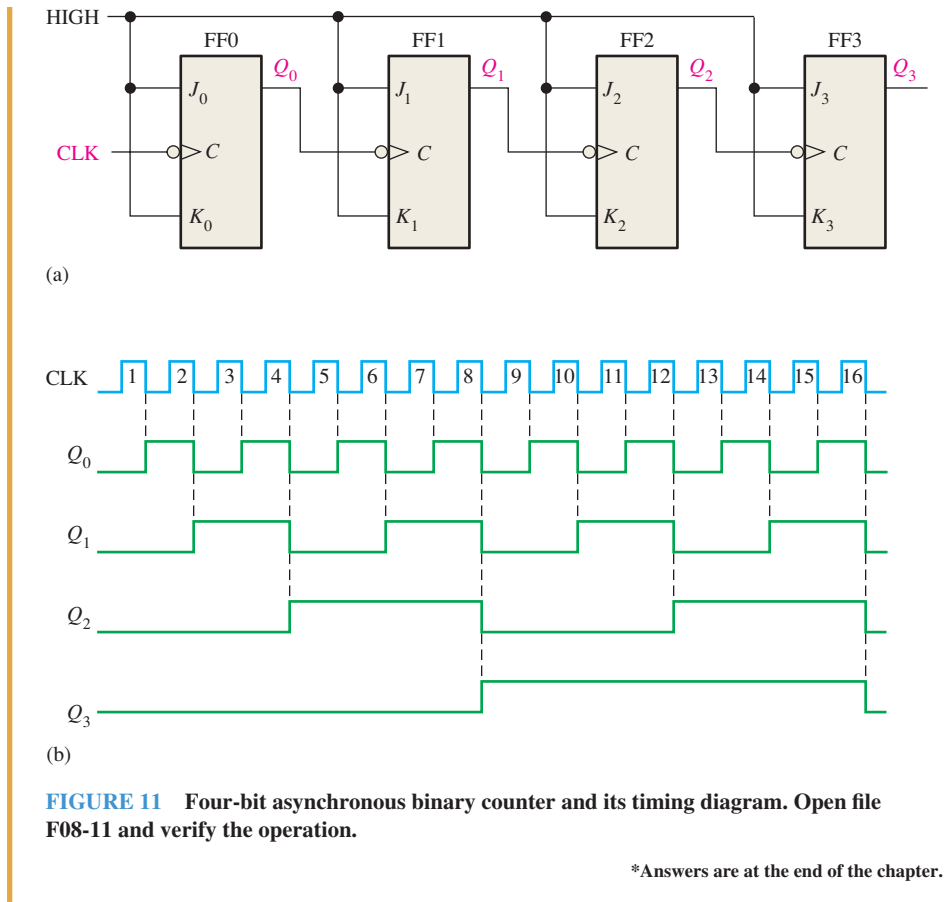
The maximum clock frequency is

$$f_{\max} = \frac{1}{t_{p(tot)}} = \frac{1}{40 \text{ ns}} = \mathbf{25 \text{ MHz}}$$

The counter should be operated below this frequency to avoid problems due to the propagation delay.

RELATED PROBLEM*

Show the timing diagram if all of the flip-flops in Figure 11(a) are positive edge-triggered.



MULTISIM



Asynchronous Decade Counters

The **modulus** of a counter is the number of unique states through which the counter will sequence. The maximum possible number of states (maximum modulus) of a counter is 2^n , where n is the number of flip-flops in the counter. Counters can be designed to have a number of states in their sequence that is less than the maximum of 2^n . This type of sequence is called a *truncated sequence*.

One common modulus for counters with truncated sequences is ten (called MOD10). Counters with ten states in their sequence are called **decade** counters. A **decade counter** with a count sequence of zero (0000) through nine (1001) is a BCD decade counter because its ten-state sequence produces the BCD code. This type of counter is useful in display applications in which BCD is required for conversion to a decimal readout.

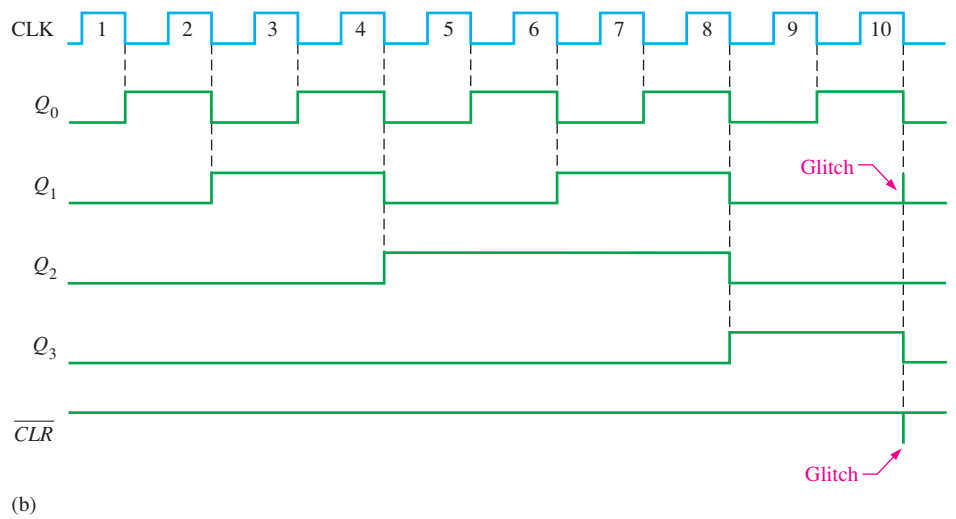
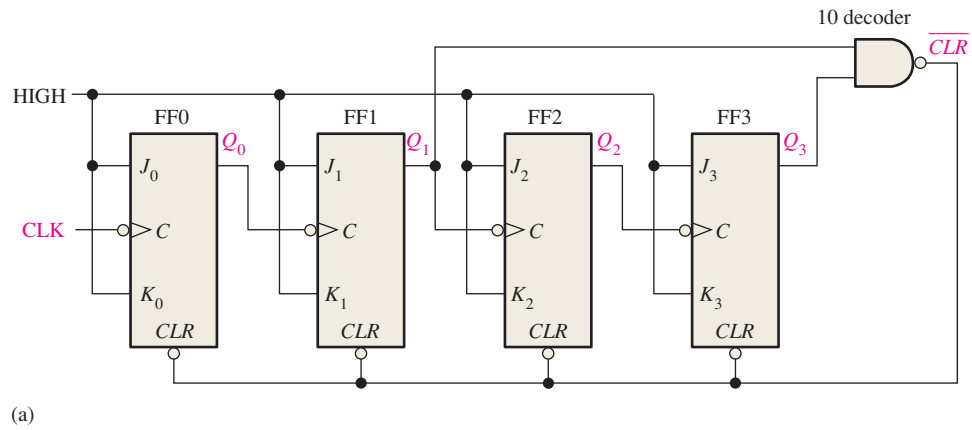
To obtain a truncated sequence, it is necessary to force the counter to recycle before going through all of its possible states. For example, the BCD decade counter must recycle back to the 0000 state after the 1001 state. A decade counter requires four flip-flops (three flip-flops are insufficient because $2^3 = 8$).

Let's use a 4-bit asynchronous counter such as the one in Example 1 and modify its sequence to illustrate the principle of truncated counters. One way to make the counter recycle after the count of nine (1001) is to decode count ten (1010) with a NAND gate and connect the output of the NAND gate to the clear (*CLR*) inputs of the flip-flops, as shown in Figure 12(a).

PARTIAL DECODING Notice in Figure 12(a) that only Q_1 and Q_3 are connected to the NAND gate inputs. This arrangement is an example of *partial decoding*, in which the two unique states ($Q_1 = 1$ and $Q_3 = 1$) are sufficient to decode the count of ten because none of the other states (zero through nine) have both Q_1 and Q_3 HIGH at the same time. When the counter goes into count ten (1010), the decoding gate output goes LOW and asynchronously resets all the flip-flops.

A counter can have 2^n states, where n is the number of flip-flops.

FIGURE 12 An asynchronously clocked decade counter with asynchronous recycling.



The resulting timing diagram is shown in Figure 12(b). Notice that there is a glitch on the Q_1 waveform. The reason for this glitch is that Q_1 must first go HIGH before the count of ten can be decoded. Not until several nanoseconds after the counter goes to the count of ten does the output of the decoding gate go LOW (both inputs are HIGH). Thus, the counter is in the 1010 state for a short time before it is reset to 0000, thus producing the glitch on Q_1 and the resulting glitch on the \overline{CLR} line that resets the counter.

Other truncated sequences can be implemented in a similar way, as Example 2 shows.

EXAMPLE 2

Show how an asynchronous counter can be implemented having a modulus of twelve with a straight binary sequence from 0000 through 1011.

SOLUTION

Since three flip-flops can produce a maximum of eight states, four flip-flops are required to produce any modulus greater than eight but less than or equal to sixteen.

When the counter gets to its last state, 1011, it must recycle back to 0000 rather than going to its normal next state of 1100, as illustrated in the following sequence chart:

Q_3	Q_2	Q_1	Q_0	
0	0	0	0	← Recycles
⋮	⋮	⋮	⋮	
1	0	1	1	
1	1	0	0	← Normal next state

Observe that Q_0 and Q_1 both go to 0 anyway, but Q_2 and Q_3 must be forced to 0 on the twelfth clock pulse. Figure 13(a) shows the modulus-12 counter. The NAND gate partially decodes count twelve (1100) and resets flip-flop 2 and flip-flop 3. Thus, on the twelfth clock pulse, the counter is forced to recycle from count eleven to count zero, as shown in the timing diagram of Figure 13(b). (It is in count twelve for only a few nanoseconds before it is reset by the glitch on \overline{CLR} .)

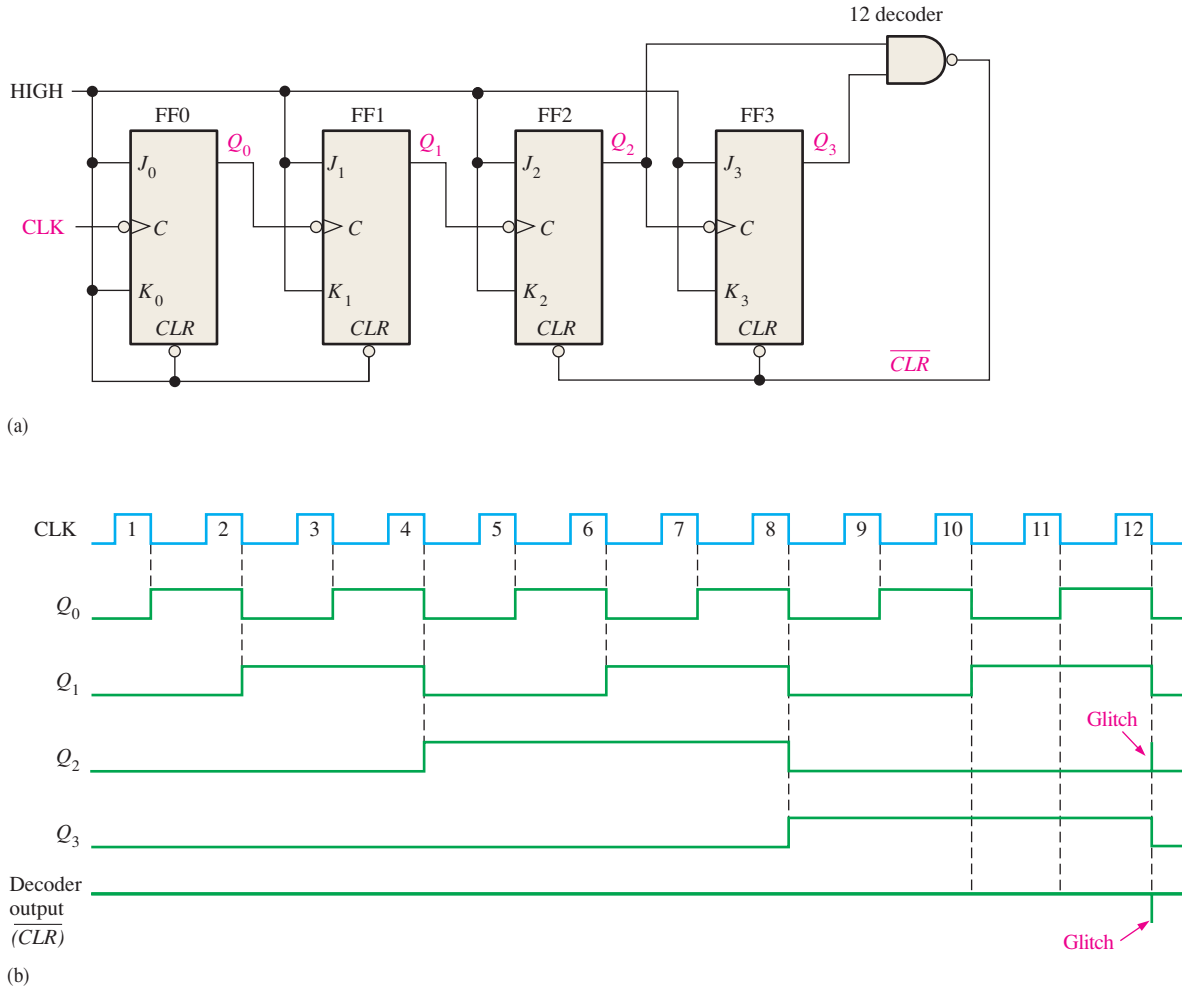


FIGURE 13 Asynchronously clocked modulus-12 counter with asynchronous recycling.

RELATED PROBLEM

How can the counter in Figure 13(a) be modified to make it a modulus-13 counter?

SECTION 3 CHECKUP

1. What does the term *asynchronous* mean in relation to counters?
2. How many states does a modulus-14 counter have? What is the minimum number of flip-flops required?

4 SYNCHRONOUS COUNTERS

The term **synchronous** refers to events that have a fixed time relationship with each other. A **synchronous counter** is one in which all the flip-flops in the counter are clocked at the same time by a common clock pulse.

After completing this section, you should be able to

- Describe the operation of a 2-bit synchronous binary counter
- Describe the operation of a 3-bit synchronous binary counter
- Describe the operation of a 4-bit synchronous binary counter
- Describe the operation of a synchronous decade counter
- Develop counter timing diagrams

A 2-Bit Synchronous Binary Counter

Figure 14 shows a 2-bit synchronous binary counter. Notice that an arrangement different from that for the asynchronous counter must be used for the J_1 and K_1 inputs of FF1 in order to achieve a binary sequence.

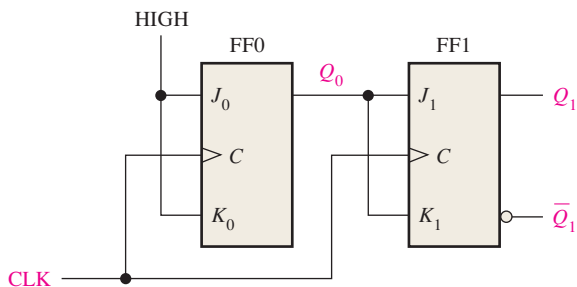


FIGURE 14 A 2-bit synchronous binary counter.

The clock input goes to each flip-flop in a synchronous counter.

The operation of this synchronous counter is as follows: First, assume that the counter is initially in the binary 0 state; that is, both flip-flops are RESET. When the positive edge of the first clock pulse is applied, FF0 will toggle and Q_0 will therefore go HIGH. What happens to FF1 at the positive-going edge of CLK1? To find out, let's look at the input conditions of FF1. Inputs J_1 and K_1 are both LOW because Q_0 , to which they are connected, has not yet gone HIGH. Remember, there is a propagation delay from the triggering edge of the clock pulse until the Q output actually makes a transition. So, $J = 0$ and $K = 0$ when the leading edge of the first clock pulse is applied. This is a no-change condition, and therefore FF1 does not change state. A timing detail of this portion of the counter operation is shown in Figure 15(a).

After CLK1, $Q_0 = 1$ and $Q_1 = 0$ (which is the binary 1 state). When the leading edge of CLK2 occurs, FF0 will toggle and Q_0 will go LOW. Since FF1 has a HIGH ($Q_0 = 1$) on its J_1 and K_1 inputs at the triggering edge of this clock pulse, the flip-flop toggles and Q_1 goes HIGH. Thus, after CLK2, $Q_0 = 0$ and $Q_1 = 1$ (which is a binary 2 state). The timing detail for this condition is shown in Figure 15(b).

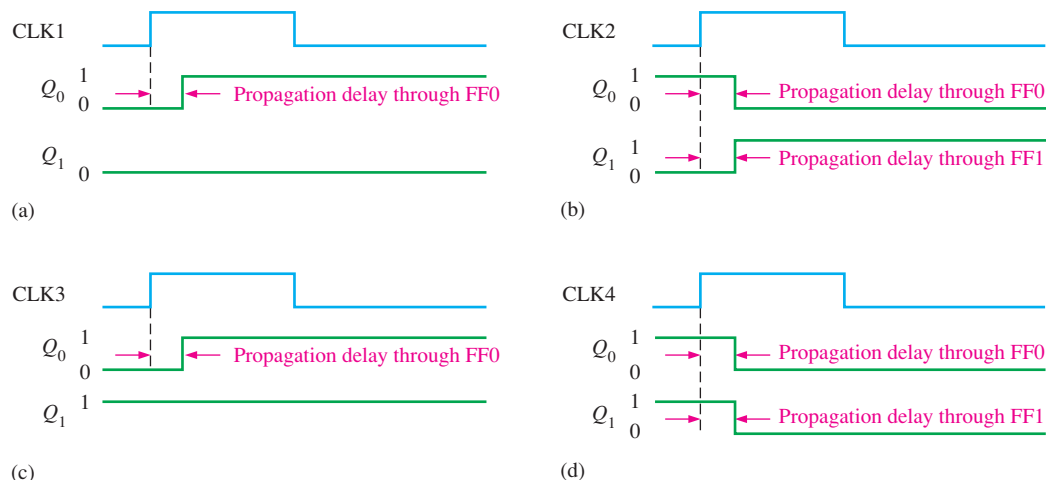


FIGURE 15 Timing details for the 2-bit synchronous counter operation (the propagation delays of both flip-flops are assumed to be equal).

When the leading edge of CLK3 occurs, FF0 again toggles to the SET state ($Q_0 = 1$), and FF1 remains SET ($Q_1 = 1$) because its J_1 and K_1 inputs are both LOW ($Q_0 = 0$). After this triggering edge, $Q_0 = 1$ and $Q_1 = 1$ (which is a binary 3 state). The timing detail is shown in Figure 15(c).

Finally, at the leading edge of CLK4, Q_0 and Q_1 go LOW because they both have a toggle condition on their J and K inputs. The timing detail is shown in Figure 15(d). The counter has now recycled to its original state, binary 0.

The complete timing diagram for the counter in Figure 14 is shown in Figure 16. Notice that all the waveform transitions appear coincident; that is, the propagation delays are not indicated. Although the delays are an important factor in the synchronous counter operation, in an overall timing diagram they are normally omitted for simplicity. Major waveform relationships resulting from the normal operation of a circuit can be conveyed completely without showing small delay and timing differences. However, in high-speed digital circuits, these small delays are an important consideration in design and troubleshooting.

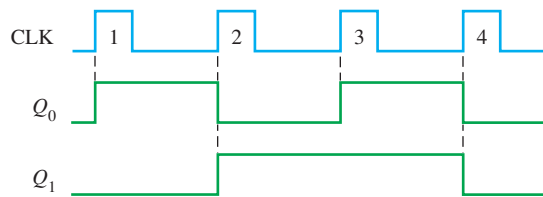


FIGURE 16 Timing diagram for the counter of Figure 14.

A 3-Bit Synchronous Binary Counter

A 3-bit synchronous binary counter is shown in Figure 17, and its timing diagram is shown in Figure 18. You can understand this counter operation by examining its sequence of states as shown in Table 3.

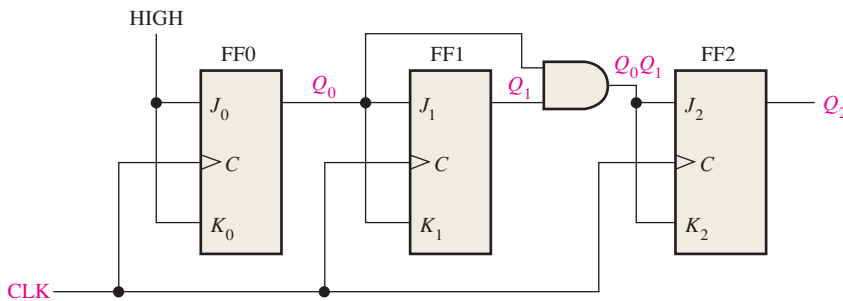


FIGURE 17 A 3-bit synchronous binary counter. Open file F08-17 to verify the operation.

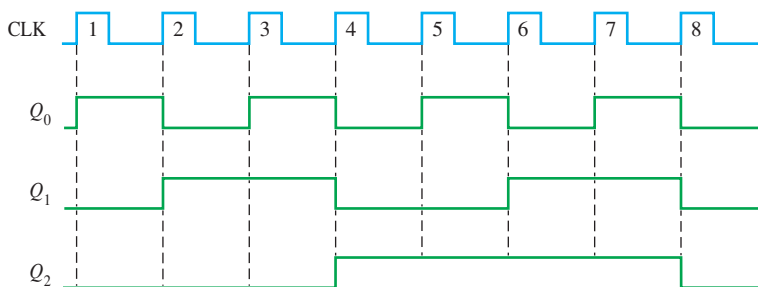


FIGURE 18 Timing diagram for the counter of Figure 17.

TABLE 3 • State sequence for a 3-bit binary counter.

CLOCK PULSE	Q_2	Q_1	Q_0
Initially	0	0	0
1	0	0	1
2	0	1	0
3	0	1	1
4	1	0	0
5	1	0	1
6	1	1	0
7	1	1	1
8 (recycles)	0	0	0

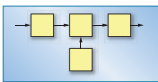
First, let's look at Q_0 . Notice that Q_0 changes on each clock pulse as the counter progresses from its original state to its final state and then back to its original state. To produce this operation, FF0 must be held in the toggle mode by constant HIGHS on its J_0 and K_0 inputs. Notice that Q_1 goes to the opposite state following each time Q_0 is a 1. This change occurs at CLK2, CLK4, CLK6, and CLK8. The CLK8 pulse causes the counter to recycle. To produce this operation, Q_0 is connected to the J_1 and K_1 inputs of FF1. When Q_0 is a 1 and a clock pulse occurs, FF1 is in the toggle mode and therefore changes state. The other times, when Q_0 is a 0, FF1 is in the no-change mode and remains in its present state.

Next, let's see how FF2 is made to change at the proper times according to the binary sequence. Notice that both times Q_2 changes state, it is preceded by the unique condition in which both Q_0 and Q_1 are HIGH. This condition is detected by the AND gate and applied to the J_2 and K_2 inputs of FF2. Whenever both Q_0 and Q_1 are HIGH, the output of the AND gate makes the J_2 and K_2 inputs of FF2 HIGH, and FF2 toggles on the following clock pulse. At all other times, the J_2 and K_2 inputs of FF2 are held LOW by the AND gate output, and FF2 does not change state.

The analysis of the counter in Figure 17 is summarized in Table 4.

The TSC or *time stamp counter* in some microprocessors is used for performance monitoring, which enables a number of parameters important to the overall performance of a system to be determined exactly. By reading the TSC before and after the execution of a procedure, the precise time required for the procedure can be determined based on the processor cycle time. In this way, the TSC forms the basis for all time evaluations in connection with optimizing system operation. For example, it can be accurately determined which of two or more programming sequences is more efficient. This is a very useful tool for compiler developers and system programmers in producing the most effective code.

SYSTEM NOTE



A 4-Bit Synchronous Binary Counter

Figure 19(a) shows a 4-bit synchronous binary counter, and Figure 19(b) shows its timing diagram. This particular counter is implemented with negative edge-triggered flip-flops. The reasoning behind the J and K input control for the first three flip-flops is the

TABLE 4 • Summary of the analysis of the counter in Figure 17.

CLOCK PULSE	OUTPUTS			J-K INPUTS						AT THE NEXT CLOCK PULSE		
	Q_2	Q_1	Q_0	J_2	K_2	J_1	K_1	J_0	K_0	FF2	FF1	FF0
Initially	0	0	0	0	0	0	0	1	1	NC*	NC	Toggle
1	0	0	1	0	0	1	1	1	1	NC	Toggle	Toggle
2	0	1	0	0	0	0	0	1	1	NC	NC	Toggle
3	0	1	1	1	1	1	1	1	1	Toggle	Toggle	Toggle
4	1	0	0	0	0	0	0	1	1	NC	NC	Toggle
5	1	0	1	0	0	1	1	1	1	NC	Toggle	Toggle
6	1	1	0	0	0	0	0	1	1	NC	NC	Toggle
7	1	1	1	1	1	1	1	1	1	Toggle	Toggle	Toggle
										Counter recycles back to 000.		

*NC indicates No Change.

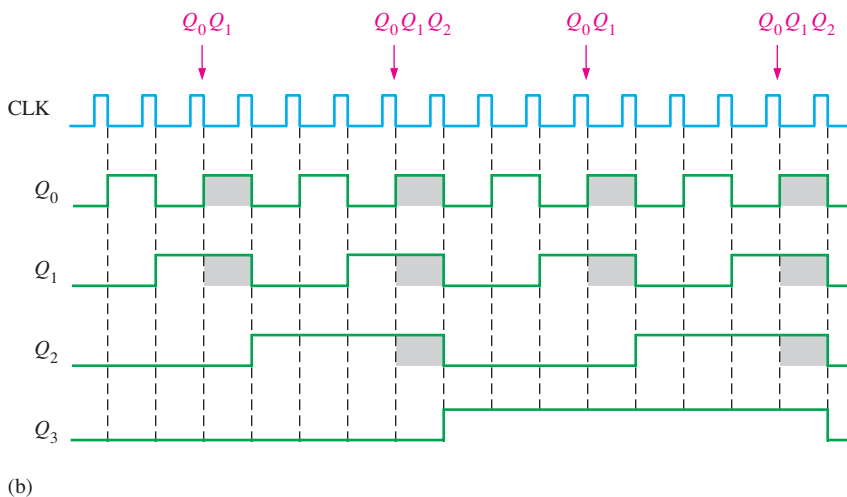
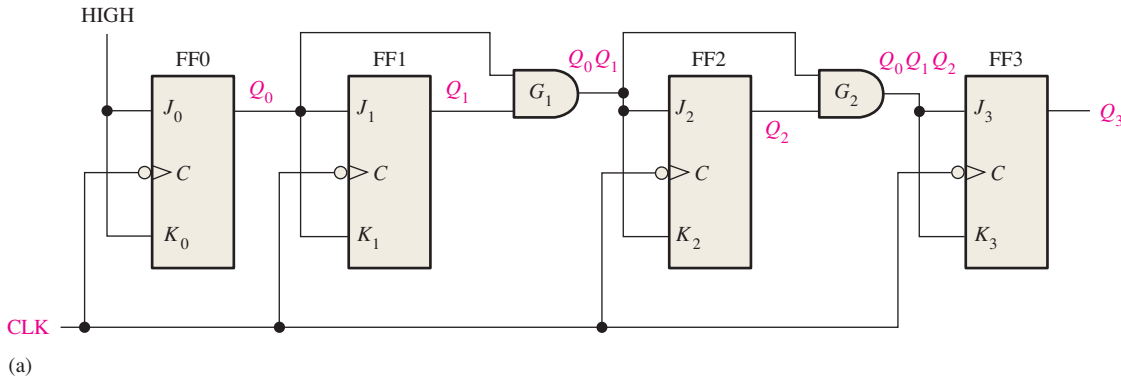


FIGURE 19 A 4-bit synchronous binary counter and timing diagram. Points where the AND gate outputs are HIGH are indicated by the shaded areas.

same as previously discussed for the 3-bit counter. The fourth stage, FF3, changes only twice in the sequence. Notice that both of these transitions occur following the times that Q_0 , Q_1 , and Q_2 are all HIGH. This condition is decoded by AND gate G_2 so that when a clock pulse occurs, FF3 will change state. For all other times the J_3 and K_3 inputs of FF3 are LOW, and it is in a no-change condition.

A 4-Bit Synchronous Decade Counter

A decade counter has ten states.

As you know, a BCD decade counter exhibits a truncated binary sequence and goes from 0000 through the 1001 state. Rather than going from the 1001 state to the 1010 state, it recycles to the 0000 state. A synchronous BCD decade counter is shown in Figure 20. The timing diagram for the decade counter is shown in Figure 21.

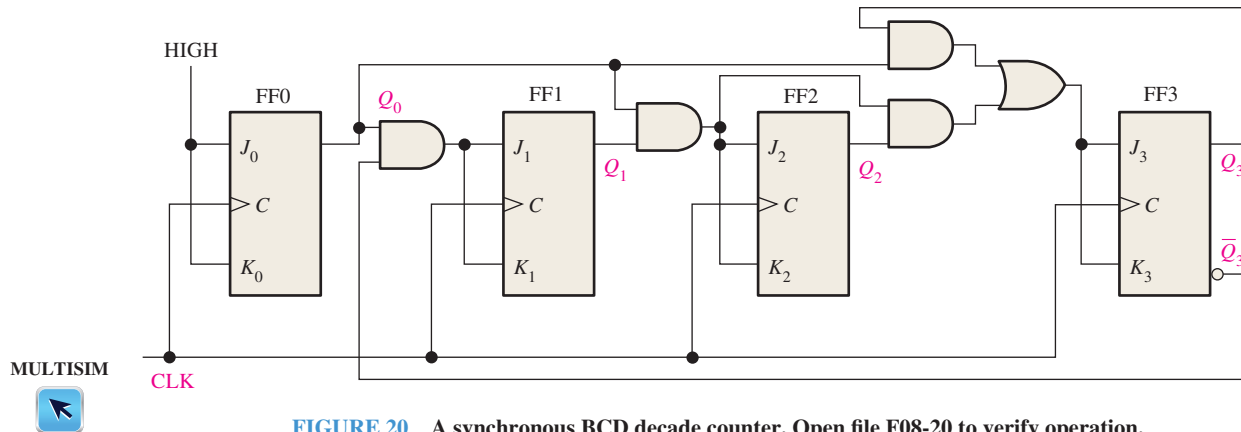
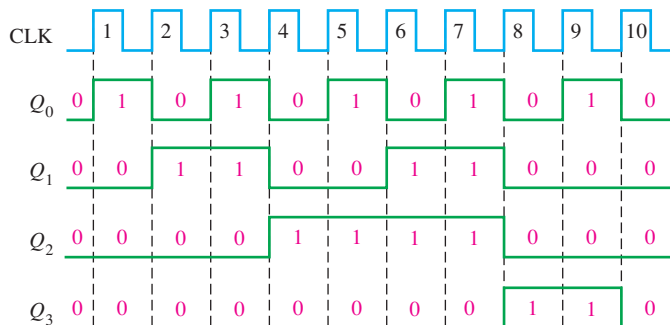


FIGURE 20 A synchronous BCD decade counter. Open file F08-20 to verify operation.

FIGURE 21 Timing diagram for the BCD decade counter (Q_0 is the LSB).



You can understand the counter operation by examining the sequence of states in Table 5 and by following the implementation in Figure 20. First, notice that FF0 (Q_0) toggles on each clock pulse, so the logic equation for its J_0 and K_0 inputs is

$$J_0 = K_0 = 1$$

This equation is implemented by connecting J_0 and K_0 to a constant HIGH level.

Next, notice in Table 5 that FF1 (Q_1) changes on the next clock pulse each time $Q_0 = 1$ and $Q_3 = 0$, so the logic equation for the J_1 and K_1 inputs is

$$J_1 = K_1 = Q_0\bar{Q}_3$$

This equation is implemented by ANDing Q_0 and \bar{Q}_3 and connecting the gate output to the J_1 and K_1 inputs of FF1.

Flip-flop 2 (Q_2) changes on the next clock pulse each time both $Q_0 = 1$ and $Q_1 = 1$. This requires an input logic equation as follows:

$$J_2 = K_2 = Q_0Q_1$$

This equation is implemented by ANDing Q_0 and Q_1 and connecting the gate output to the J_2 and K_2 inputs of FF2.

Finally, FF3 (Q_3) changes to the opposite state on the next clock pulse each time $Q_0 = 1$, $Q_1 = 1$, and $Q_2 = 1$ (state 7), or when $Q_0 = 1$ and $Q_2 = 1$ (state 9). The equation for this is as follows:

$$J_3 = K_3 = Q_0Q_1Q_2 + Q_0Q_2$$

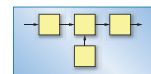
TABLE 5 • States of a BCD decade counter.

CLOCK PULSE	Q_3	Q_2	Q_1	Q_0
Initially	0	0	0	0
1	0	0	0	1
2	0	0	1	0
3	0	0	1	1
4	0	1	0	0
5	0	1	0	1
6	0	1	1	0
7	0	1	1	1
8	1	0	0	0
9	1	0	0	1
10 (recycles)	0	0	0	0

This function is implemented with the AND/OR logic connected to the J_3 and K_3 inputs of FF3 as shown in the logic diagram in Figure 20. Notice that the differences between this decade counter and the modulus-16 binary counter in Figure 19 are the $Q_0\bar{Q}_3$ AND gate, the Q_0Q_3 AND gate, and the OR gate; this arrangement detects the occurrence of the 1001 state and causes the counter to recycle properly on the next clock pulse.

Computers contain an internal counter that can be programmed for various frequencies and tone durations, thus producing “music.” To select a particular tone, the programmed instruction selects a divisor that is sent to the counter. The divisor sets the counter up to divide the basic peripheral clock frequency to produce an audio tone. The duration of a tone can also be set by a programmed instruction; thus, a basic counter is used to produce melodies by controlling the frequency and duration of tones.

SYSTEM NOTE



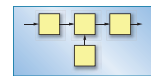
SYSTEM EXAMPLE 1

PARALLEL-TO-SERIAL DATA CONVERSION (MULTIPLEXING)

We have already discussed a data transmission system using multiplexing and demultiplexing techniques. Essentially, the parallel data bits on the multiplexer inputs are converted to serial data bits on the single transmission line. A group of bits appearing simultaneously on parallel lines is called *parallel data*. A group of bits appearing on a single line in a time sequence is called *serial data*.

Parallel-to-serial conversion is normally accomplished by the use of a counter to provide a binary sequence for the data-select inputs of a data selector/multiplexer, as illustrated in Figure 22. The Q outputs of the modulus-8 counter are connected to the data-select inputs of an 8-bit multiplexer.

Figure 23 is a timing diagram illustrating the operation of this circuit. The first byte (eight-bit group) of parallel data is applied to the multiplexer inputs. As the counter goes through a binary sequence from zero to seven, each bit, beginning with D_0 , is sequentially



COUNTERS

FIGURE 22

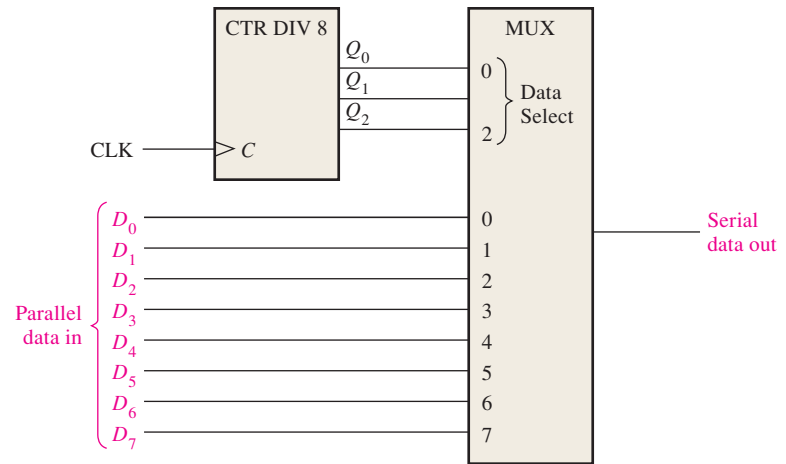
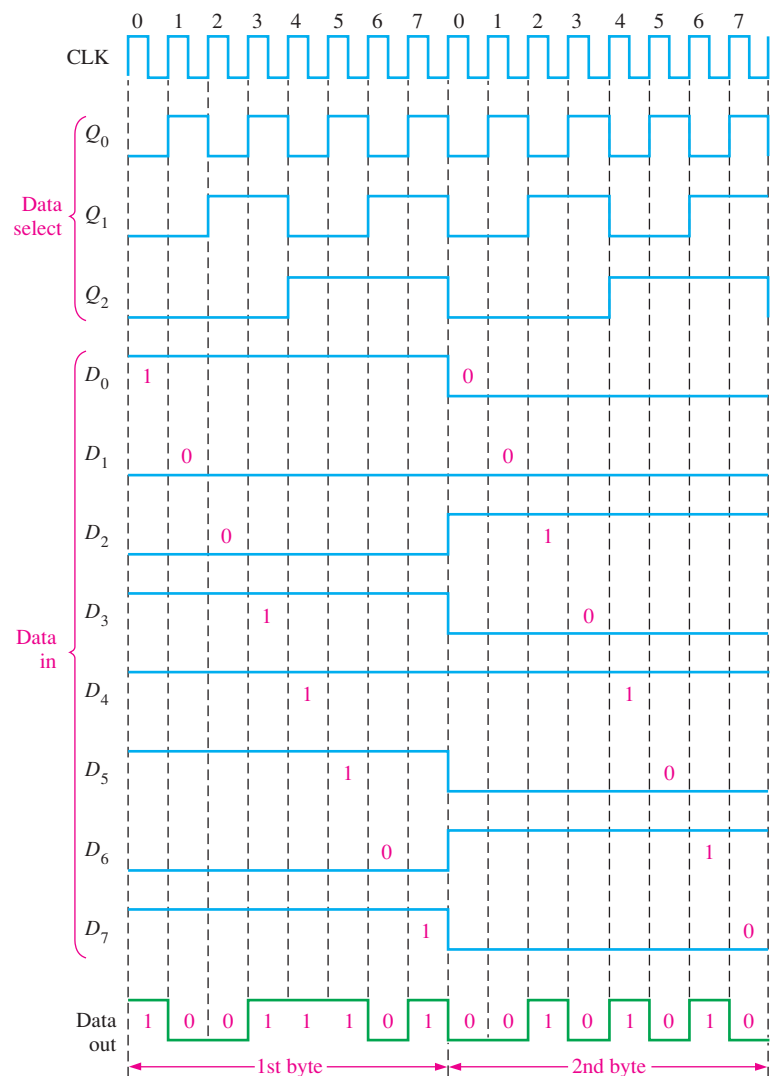


FIGURE 23



selected and passed through the multiplexer to the output line. After eight clock pulses the data byte has been converted to a serial format and sent out on the transmission line. When the counter recycles back to 0, the next byte is applied to the data inputs and is sequentially converted to serial form as the counter cycles through its eight states. This process continues repeatedly as each parallel byte is converted to a serial byte.

SECTION 4 CHECKUP

1. How does a synchronous counter differ from an asynchronous counter?
2. How many states does an 8-bit synchronous binary counter have?

5 UP/DOWN SYNCHRONOUS COUNTERS

An up/down counter is one that is capable of progressing in either direction through a certain sequence. An up/down counter, sometimes called a bidirectional counter, can have any specified sequence of states. A 3-bit binary counter that advances upward through its sequence (0, 1, 2, 3, 4, 5, 6, 7) and then can be reversed so that it goes through the sequence in the opposite direction (7, 6, 5, 4, 3, 2, 1, 0) is an illustration of up/down sequential operation.

After completing this section, you should be able to

- Explain the basic operation of an up/down counter

In general, most up/down counters can be reversed at any point in their sequence. For instance, the 3-bit binary counter can be made to go through the following sequence:

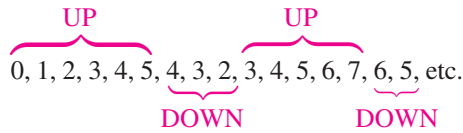


Table 6 shows the complete up/down sequence for a 3-bit binary counter. The arrows indicate the state-to-state movement of the counter for both its UP and its DOWN modes of operation. An examination of Q_0 for both the up and down sequences shows that FF0 toggles on each clock pulse. Thus, the J_0 and K_0 inputs of FF0 are

$$J_0 = K_0 = 1$$

For the up sequence, Q_1 changes state on the next clock pulse when $Q_0 = 1$. For the down sequence, Q_1 changes on the next clock pulse when $Q_0 = 0$. Thus, the J_1 and K_1 inputs of FF1 must equal 1 under the conditions expressed by the following equation:

$$J_1 = K_1 = (Q_0 \cdot \text{UP}) + (\bar{Q}_0 \cdot \text{DOWN})$$

TABLE 6 • Up/Down sequence for a 3-bit binary counter.

CLOCK PULSE	UP	Q_2	Q_1	Q_0	DOWN
0		0	0	0	
1		0	0	1	
2		0	1	0	
3		0	1	1	
4		1	0	0	
5		1	0	1	
6		1	1	0	
7		1	1	1	

Incrementing a counter increases its count by one.

Decrementing a counter decreases its count by one.

For the up sequence, Q_2 changes state on the next clock pulse when $Q_0 = Q_1 = 1$. For the down sequence, Q_2 changes on the next clock pulse when $Q_0 = Q_1 = 0$. Thus, the J_2 and K_2 inputs of FF2 must equal 1 under the conditions expressed by the following equation:

$$J_2 = K_2 = (Q_0 \cdot Q_1 \cdot UP) + (\bar{Q}_0 \cdot \bar{Q}_1 \cdot DOWN)$$

Each of the conditions for the J and K inputs of each flip-flop produces a toggle at the appropriate point in the counter sequence.

Figure 24 shows a basic implementation of a 3-bit up/down binary counter using the logic equations just developed for the J and K inputs of each flip-flop. Notice that the $UP/DOWN$ control input is HIGH for UP and LOW for DOWN.

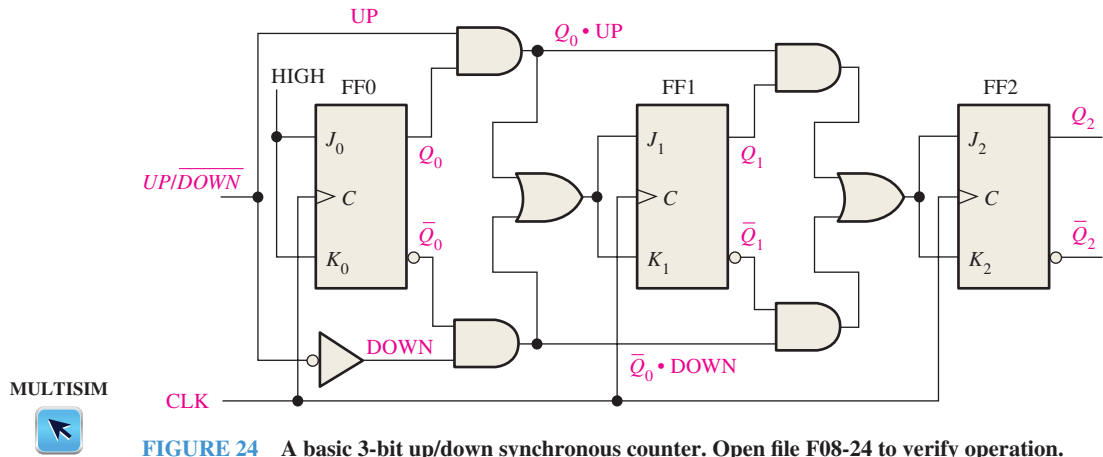


FIGURE 24 A basic 3-bit up/down synchronous counter. Open file F08-24 to verify operation.

EXAMPLE 3

Show the timing diagram and determine the sequence of a 4-bit synchronous binary up/down counter if the clock and $UP/DOWN$ control inputs have waveforms as shown in Figure 25(a). The counter starts in the all-0s state and is positive edge-triggered.

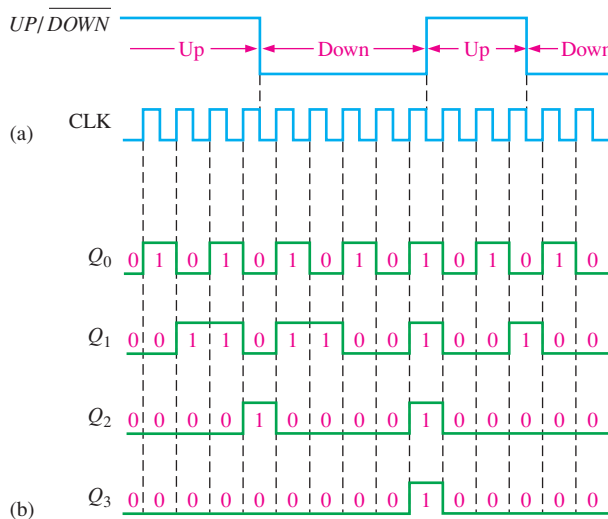


FIGURE 25

SOLUTION

The timing diagram showing the Q outputs is shown in Figure 25(b). From these waveforms, the counter sequence is as shown in Table 7.

TABLE 7

Q_3	Q_2	Q_1	Q_0	
0	0	0	0	UP
0	0	0	1	
0	0	1	0	
0	0	1	1	
0	1	0	0	DOWN
0	0	1	1	
0	0	1	0	
0	0	0	1	
0	0	0	0	UP
1	1	1	1	
0	0	0	0	
0	0	0	1	
0	0	1	0	DOWN
0	0	0	1	
0	0	0	0	

RELATED PROBLEM

Show the timing diagram if the $UP/DOWN$ control waveform in Figure 25(a) is inverted.

SYSTEM EXAMPLE 2

AUTOMOBILE PARKING CONTROL

This system example illustrates the use of an up/down counter to solve an everyday problem. The problem is to devise a means of monitoring available spaces in a one-hundred-space parking garage and provide for an indication of a full condition by illuminating a display sign and lowering a gate bar at the entrance.

A system that solves this problem consists of optoelectronic sensors at the entrance and exit of the garage, an up/down counter and associated circuitry, and an interface circuit that uses the counter output to turn the FULL sign on or off as required and lower or raise the gate bar at the entrance. A general block diagram of this system is shown in Figure 26.

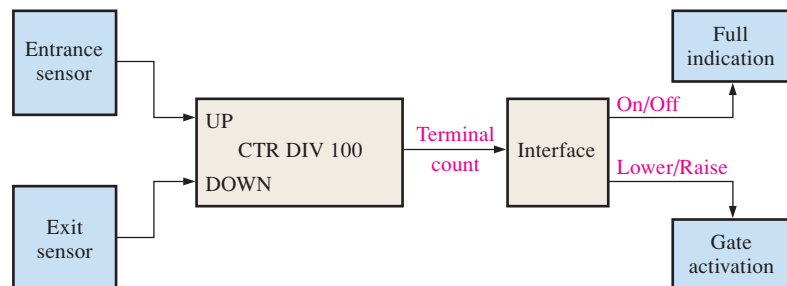
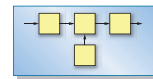


FIGURE 26

COUNTERS

A logic diagram of the up/down counter is shown in Figure 27. It consists of two cascaded up/down decade counters. The operation is described in the following paragraphs.

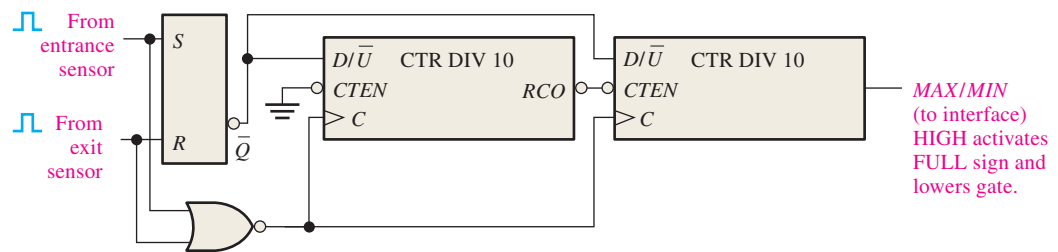


FIGURE 27

The counter is initially preset to 0 using the parallel data inputs, which are not shown. Each automobile entering the garage breaks a light beam, activating a sensor that produces an electrical pulse. This positive pulse sets the S-R latch on its leading edge. The LOW on the \bar{Q} output of the latch puts the counter in the UP mode. Also, the sensor pulse goes through the NOR gate and clocks the counter on the LOW-to-HIGH transition of its trailing edge. Each time an automobile enters the garage, the counter is advanced by one (**incremented**). When the one-hundredth automobile enters, the counter goes to its last state (100_{10}). The *MAX/MIN* output goes HIGH and activates the interface circuit (no detail), which lights the FULL sign and lowers the gate bar to prevent further entry.

When an automobile exits, an optoelectronic sensor produces a positive pulse, which resets the S-R latch and puts the counter in the DOWN mode. The trailing edge of the clock decreases the count by one (**decremented**). If the garage is full and an automobile leaves, the *MAX/MIN* output of the counter goes LOW, turning off the FULL sign and raising the gate.

SECTION 5 CHECKUP

1. A 4-bit up/down binary counter is in the DOWN mode and in the 1010 state. On the next clock pulse, to what state does the counter go?
2. What is the terminal count of a 4-bit binary counter in the UP mode? In the DOWN mode? What is the next state after the terminal count in the DOWN mode?

6 CASCADED COUNTERS

Counters can be connected in cascade to achieve higher-modulus operation. In essence, **cascading** means that the last-stage output of one counter drives the input of the next counter.

After completing this section, you should be able to

- Determine the overall modulus of cascaded counters
- Analyze the timing diagram of a cascaded counter configuration
- Use cascaded counters as a frequency divider
- Use cascaded counters to achieve specified truncated sequences

ASYNCHRONOUS CASCADING An example of two asynchronous counters connected in cascade is shown in Figure 28 for a 2-bit and a 3-bit ripple counter. The timing diagram is shown in Figure 29. Notice that the final output of the modulus-8 counter, Q_4 , occurs once for every 32 input clock pulses. The overall modulus of the two cascaded counters is $4 \times 8 = 32$; that is, they act as a divide-by-32 counter.

The overall modulus of cascaded counters is equal to the product of the individual moduli.

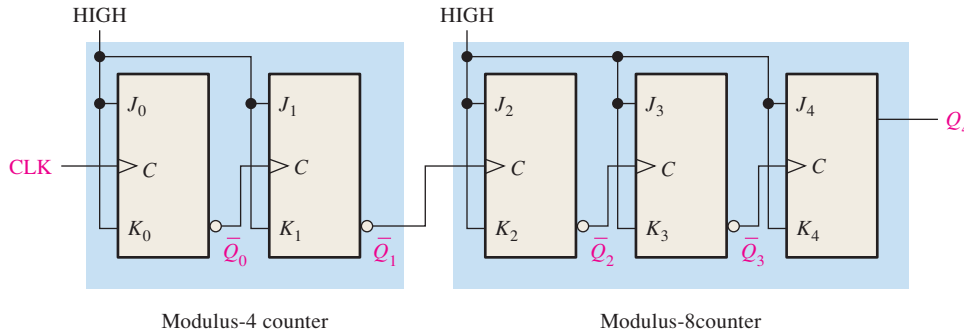


FIGURE 28 Two cascaded asynchronous counters (all J and K inputs are HIGH).

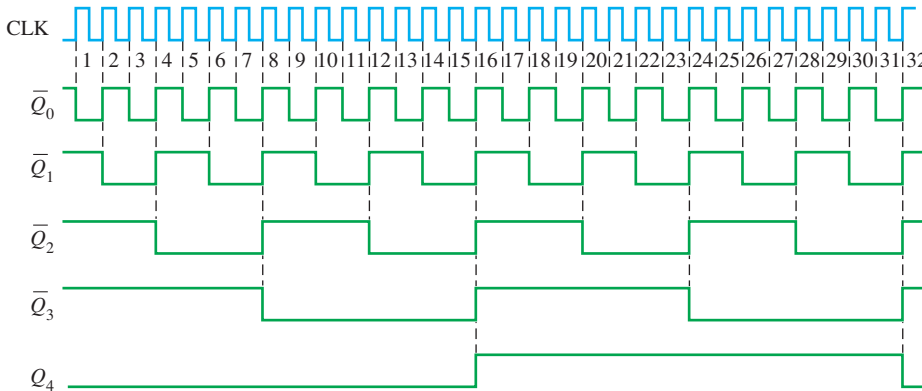


FIGURE 29 Timing diagram for the cascaded counter configuration of Figure 28.

SYNCHRONOUS CASCADING When operating synchronous counters in a cascaded configuration, it is necessary to use the count enable and the terminal count functions to achieve higher-modulus operation. On some devices the count enable is labeled simply $CTEN$ (or some other designation such as G), and terminal count (TC) is analogous to ripple clock output (RCO) on some IC counters.

Figure 30 shows two decade counters connected in cascade. The terminal count (TC) output of counter 1 is connected to the count enable ($CTEN$) input of counter 2. Counter 2 is inhibited by the LOW on its $CTEN$ input until counter 1 reaches its last, or terminal, state and its terminal count output goes HIGH. This HIGH now enables counter 2, so that when the first clock pulse after counter 1 reaches its terminal count (CLK_{10}), counter

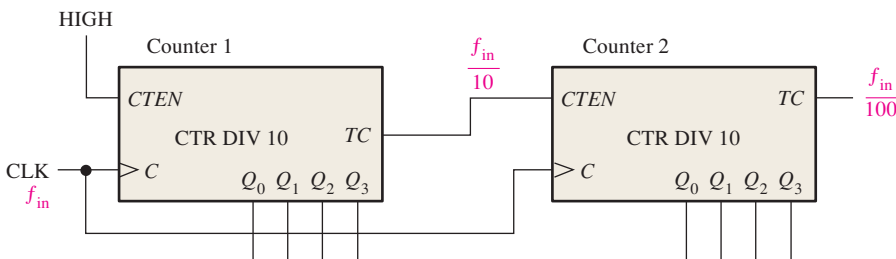
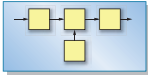


FIGURE 30 A modulus-100 counter using two cascaded decade counters.



The time stamp counter (TSC), mentioned in a previous system note, is a 64-bit counter. It is interesting to observe that if this counter (or any full-modulus 64-bit counter) is clocked at a frequency of 1 GHz, it will take 585 years for it to go through all of its states and reach its terminal count. In contrast, a 32-bit full-modulus counter will exhaust all of its states in approximately 4.3 seconds when clocked at 1 GHz. The difference is astounding.

SYSTEM NOTE

2 goes from its initial state to its second state. Upon completion of the entire second cycle of counter 1 (when counter 1 reaches terminal count the second time), counter 2 is again enabled and advances to its next state. This sequence continues. Since these are decade counters, counter 1 must go through ten complete cycles before counter 2 completes its first cycle. In other words, for every ten cycles of counter 1, counter 2 goes through one cycle. Thus, counter 2 will complete one cycle after one hundred clock pulses. The overall modulus of these two cascaded counters is $10 \times 10 = 100$.

When viewed as a frequency divider, the circuit of Figure 30 divides the input clock frequency by 100. Cascaded counters are often used to divide a high-frequency clock signal to obtain highly accurate pulse frequencies. Cascaded counter configurations used for such purposes are sometimes called *countdown chains*. For example, suppose that you have a basic clock frequency of 1 MHz and you wish to obtain 100 kHz, 10 kHz, and 1 kHz; a series of cascaded decade counters can be used. If the 1 MHz signal is divided by 10, the output is 100 kHz. Then if the 100 kHz signal is divided by 10, the output is 10 kHz. Another division by 10 produces the 1 kHz frequency. The general implementation of this countdown chain is shown in Figure 31.

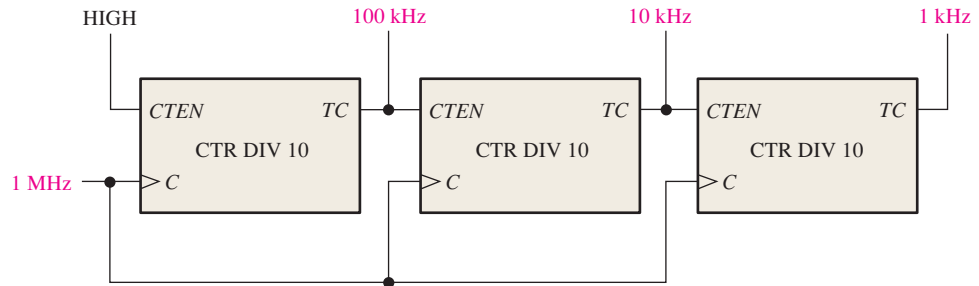


FIGURE 31 Three cascaded decade counters forming a divide-by-1000 frequency divider with intermediate divide-by-10 and divide-by-100 outputs.

EXAMPLE 4

Determine the overall modulus of the two cascaded counter configurations in Figure 32.

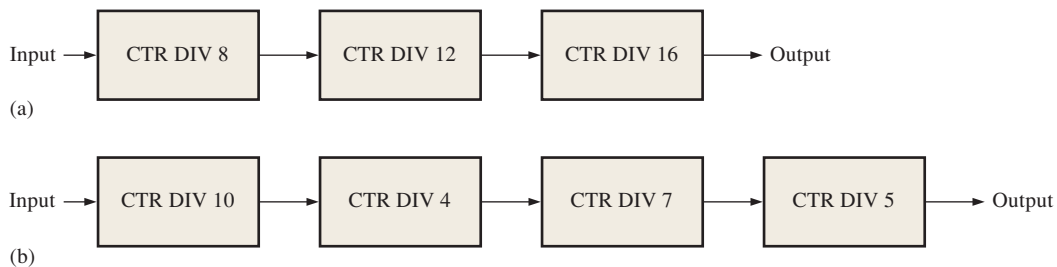


FIGURE 32

SOLUTION

In Figure 32(a), the overall modulus for the 3-counter configuration is

$$8 \times 12 \times 16 = \mathbf{1536}$$

In Figure 32(b), the overall modulus for the 4-counter configuration is

$$10 \times 4 \times 7 \times 5 = \mathbf{1400}$$

RELATED PROBLEM

How many cascaded decade counters are required to divide a clock frequency by 100,000?

EXAMPLE 5

Use up/down decade counters connected in the UP mode to obtain a 10 kHz waveform from a 1 MHz clock. Show the logic diagram.

SOLUTION

To obtain 10 kHz from a 1 MHz clock requires a division factor of 100. Two decade counters must be cascaded as shown in Figure 33. The left counter produces a terminal count (TC) pulse for every 10 clock pulses. The right counter produces a terminal count (TC) pulse for every 100 clock pulses.

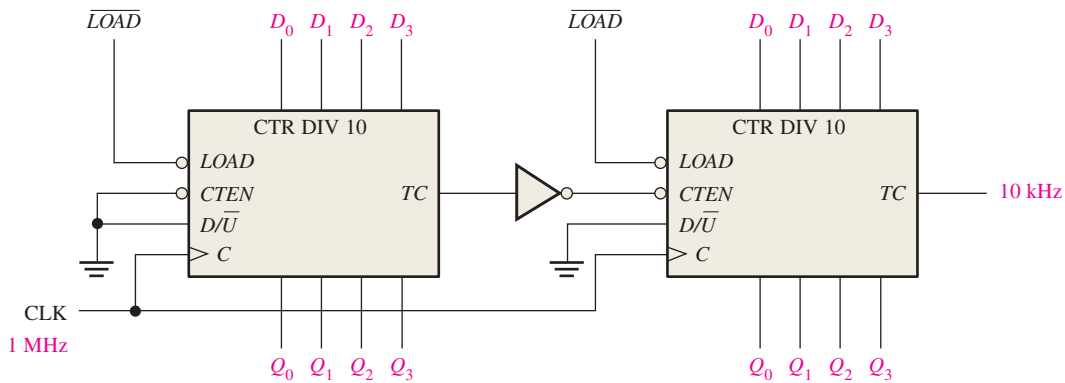


FIGURE 33 A divide-by-100 counter using two decade up/down decade counters connected for the up sequence.

RELATED PROBLEM

Determine the frequency of the waveform at the Q_0 output of the second counter (the one on the right) in Figure 33.

Cascaded Counters with Truncated Sequences

The preceding discussion has shown how to achieve an overall modulus (divide-by-factor) that is the product of the individual moduli of all the cascaded counters. This can be considered *full-modulus cascading*.

Often an application requires an overall modulus that is less than that achieved by full-modulus cascading. That is, a truncated sequence must be implemented with cascaded counters. To illustrate this method, we will use the cascaded counter configuration in Figure 34. This particular circuit uses four 4-bit synchronous binary counters. If these four counters (sixteen bits total) were cascaded in a full-modulus arrangement, the modulus would be

$$2^{16} = 65,536$$

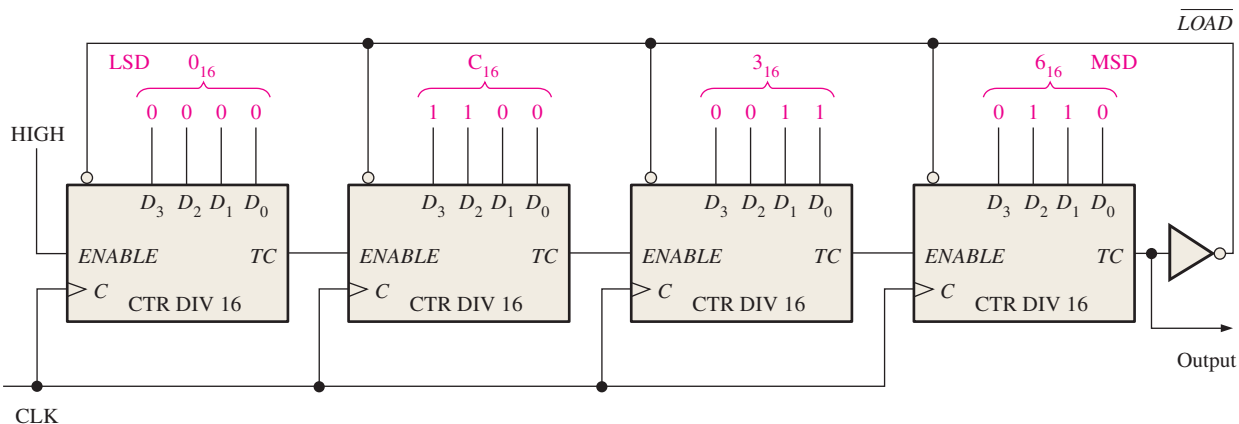


FIGURE 34 A divide-by-40,000 counter using 4-bit binary counters. Note that each of the parallel data inputs is shown in binary order (the right-most bit D_0 is the LSB in each counter).

Let's assume that a certain application requires a divide-by-40,000 counter (modulus 40,000). The difference between 65,536 and 40,000 is 25,536, which is the number of states that must be *deleted* from the full-modulus sequence. The technique used in the circuit of Figure 34 is to preset the cascaded counter to 25,536 ($63C0_{16}$) each time it recycles, so that it will count from 25,536 up to 65,535 on each full cycle. Therefore, each full cycle of the counter consists of 40,000 states.

Notice in Figure 34 that the TC (terminal count) output of the right-most counter is inverted and applied to the \overline{LOAD} input of each 4-bit counter. Each time the count reaches its terminal value of 65,535, which is 11111111111111_2 , TC goes HIGH and causes the number on the parallel data inputs ($63C0_{16}$) to be synchronously loaded into the counter with the clock pulse. Thus, there is one TC pulse from the right-most 4-bit counter for every 40,000 clock pulses.

With this technique any modulus can be achieved by synchronous loading of the counter to the appropriate initial state on each cycle.

SECTION 6 CHECKUP

- How many decade counters are necessary to implement a divide-by-1000 (modulus-1000) counter? A divide-by-10,000?
- Show with general block diagrams how to achieve each of the following, using a flip-flop, a decade counter, and a 4-bit binary counter, or any combination of these:
 - Divide-by-20 counter
 - Divide-by-32 counter
 - Divide-by-160 counter
 - Divide-by-320 counter

7 COUNTER DECODING

In many applications, it is necessary that some or all of the counter states be decoded. The decoding of a counter involves using decoders or logic gates to determine when the counter is in a certain binary state in its sequence. For instance, the terminal count function previously discussed is a single decoded state (the last state) in the counter sequence.

After completing this section, you should be able to

- Implement the decoding logic for any given state in a counter sequence
- Explain why glitches occur in counter decoding logic
- Use the method of strobing to eliminate decoding glitches

Suppose that you wish to decode binary state 6 (110) of a 3-bit binary counter. When $Q_2 = 1$, $Q_1 = 1$, and $Q_0 = 0$, a HIGH appears on the output of the decoding gate, indicating that the counter is at state 6. This can be done as shown in Figure 35. This is called *active-HIGH decoding*. Replacing the AND gate with a NAND gate provides active-LOW decoding.

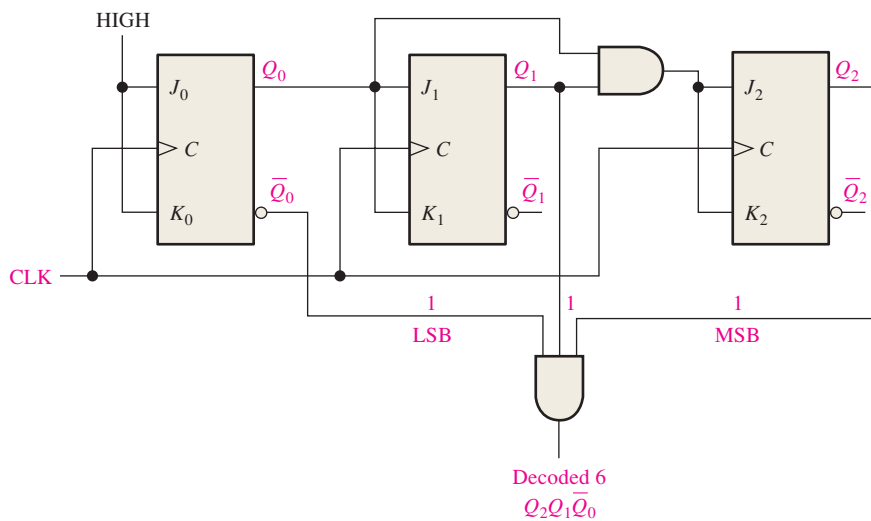


FIGURE 35 Decoding of state 6 (110). Open file F08-35 to verify operation.

MULTISIM



EXAMPLE 6

Implement the decoding of binary state 2 and binary state 7 of a 3-bit synchronous counter. Show the entire counter timing diagram and the output waveforms of the decoding gates. Binary 2 = $\bar{Q}_2Q_1\bar{Q}_0$ and binary 7 = $Q_2Q_1Q_0$.

SOLUTION

See Figure 36. The 3-bit counter was originally discussed in Section 4 (Figure 17).

RELATED PROBLEM

Show the logic for decoding state 5 in the 3-bit counter.

COUNTERS

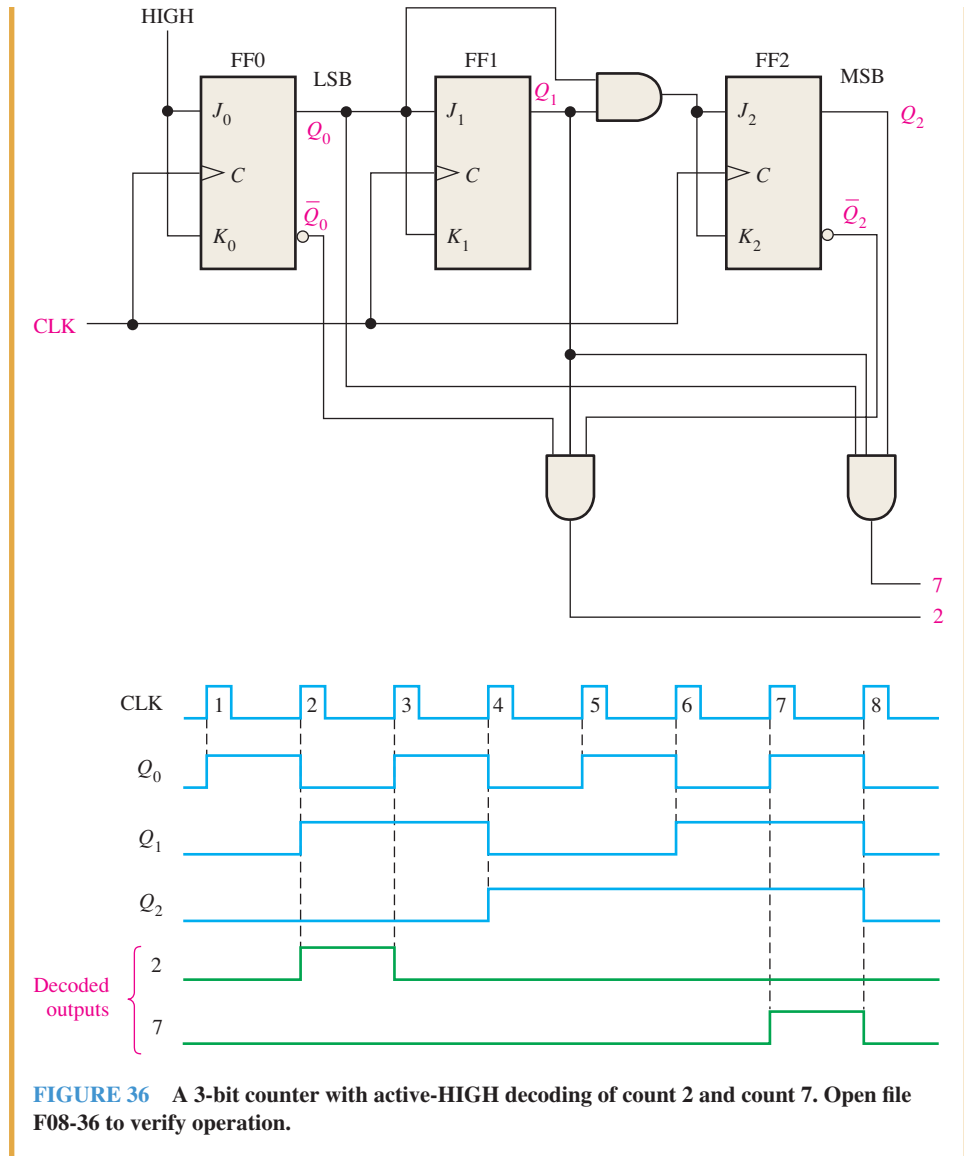


FIGURE 36 A 3-bit counter with active-HIGH decoding of count 2 and count 7. Open file F08-36 to verify operation.

MULTISIM



Decoding Glitches

A glitch is an unwanted spike of voltage.

We have discussed the problem of glitches produced by the decoding process. The propagation delays due to the ripple effect in asynchronous counters create transitional states in which the counter outputs are changing at slightly different times. These transitional states produce undesired voltage spikes of short duration (glitches) on the outputs of a decoder connected to the counter. The glitch problem can also occur to some degree with synchronous counters because the propagation delays from the clock to the Q outputs of each flip-flop in a counter can vary slightly.

Figure 37 shows a basic asynchronous BCD decade counter connected to a BCD-to-decimal decoder. To see what happens in this case, let's look at a timing diagram in which the propagation delays are taken into account, as shown in Figure 38. Notice that these delays cause false states of short duration. The value of the false binary state at each critical transition is indicated on the diagram. The resulting glitches can be seen on the decoder outputs.

COUNTERS

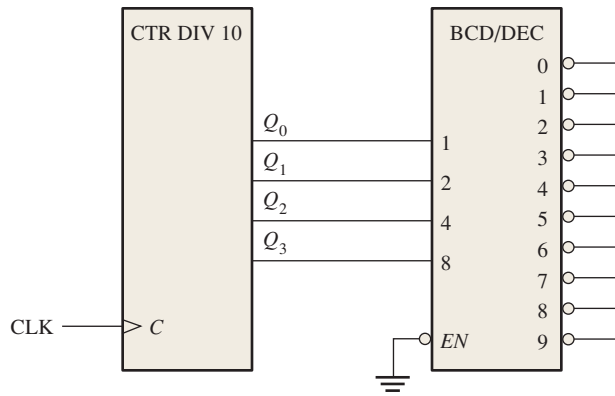


FIGURE 37 A basic BCD decade counter and decoder.

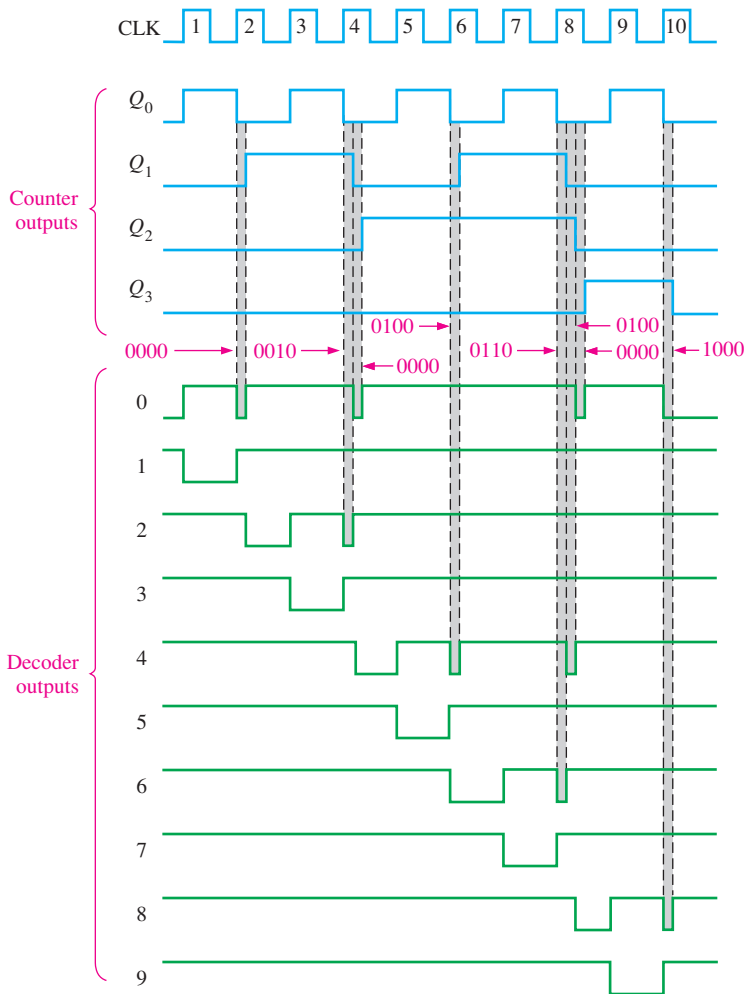


FIGURE 38 Outputs with glitches from the decoder in Figure 37. Glitch widths are exaggerated for illustration and are usually only a few nanoseconds wide.

One way to eliminate the glitches is to enable the decoded outputs at a time after the glitches have had time to disappear. This method is known as *strobing* and can be accomplished in the case of an active-HIGH clock by using the LOW level of the clock to enable the decoder, as shown in Figure 39. The resulting improved timing diagram is shown in Figure 40.

FIGURE 39 The basic BCD decade counter and decoder with strobing to eliminate glitches.

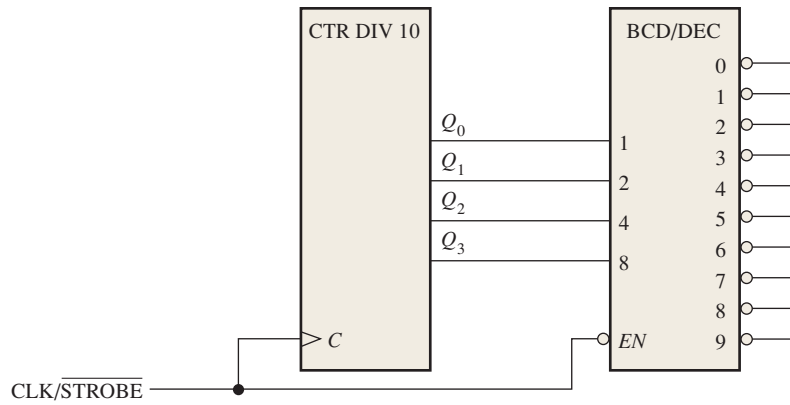
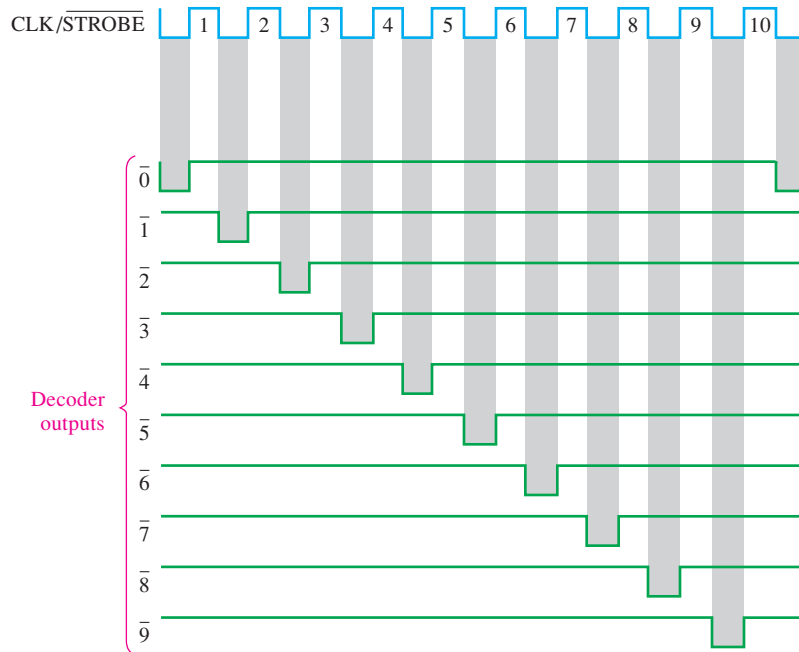


FIGURE 40 Strobed decoder outputs for the circuit of Figure 39.



SECTION 7 CHECKUP

- What transitional states are possible when a 4-bit asynchronous binary counter changes from

 - (a) count 2 to count 3
 - (b) count 3 to count 4
 - (c) count 10₁₀ to count 11₁₀
 - (d) count 15 to count 0

8 COUNTERS WITH VHDL AND VERILOG

In this section, the VHDL and Verilog programs for two types of counters are presented. A 4-bit synchronous binary counter is shown in Figure 41 and a decade counter is shown in Figure 42.

After completing this section, you should be able to

- Discuss the VHDL and Verilog descriptions of a 4-bit synchronous binary counter
- Discuss the VHDL and Verilog descriptions of a decade counter

Four-Bit Binary Counter

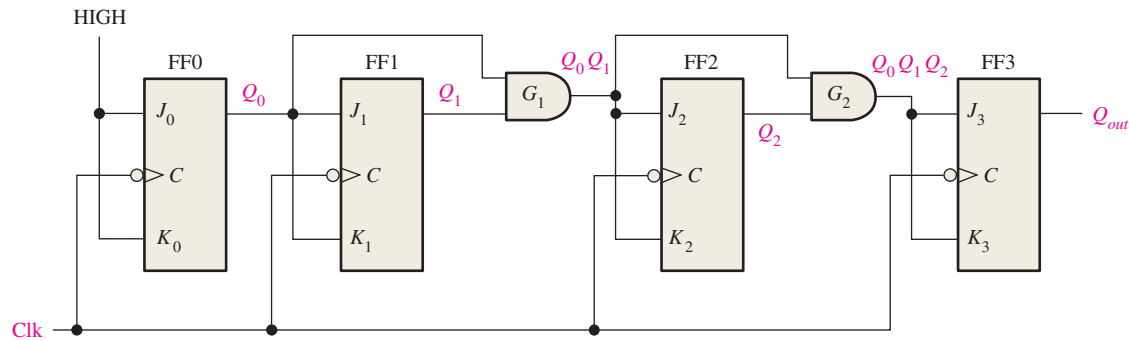


FIGURE 41 4-bit synchronous binary counter.

VHDL FOR FOUR-BIT BINARY COUNTER

```

library ieee;
use ieee.std_logic_1164.all;

entity FourBitBinaryCounter is
port (Clk: in std_logic;
      QOut: out std_logic);
end entity FourBitBinaryCounter;

architecture FourBitCounterBehavior of FourBitBinaryCounter is
  component jkff is
    port (J, K, Clk: in std_logic;
          Q: out std_logic);
  end component jkff;

  signal G1, G2: std_logic;
  signal Q0, Q1, Q2: std_logic;
begin
  G1 <= Q0 and Q1;
  G2 <= G1 and Q2;

  JKFF0: jkff port map (J => '1', K => '1', Clk => Clk, Q => Q0);
  JKFF1: jkff port map (J => Q0, K => Q0, Clk => Clk, Q => Q1);
  JKFF2: jkff port map (J => G1, K => G1, Clk => Clk, Q => Q2);
  JKFF3: jkff port map (J => G2, K => G2, Clk => Clk, Q => QOut);
end architecture FourBitCounterBehavior;

```

VERILOG FOR FOUR-BIT BINARY COUNTER

```

module FourBitBinaryCounter (Clk, QOut);
  input Clk;
  output QOut;

  wire G1, G2;
  wire Q0, Q1, Q2;

  assign G1 = Q0 && Q1;
  assign G2 = G1 && Q2;

  jkff JKFF0(J(1), .K(1), .Clk(Clk), .Prn(1), .clrn(1), .Q(Q0));
  jkff JKFF1(J(Q0), .K(Q0), .Clk(Clk), .Prn(1), .clrn(1), .Q(Q1));
  jkff JKFF2(J(G1), .K(G1), .Clk(Clk), .Prn(1), .clrn(1), .Q(Q2));
  jkff JKFF3(J(G2), .K(G2), .Clk(Clk), .Prn(1), .clrn(1), .Q(QOut));
endmodule

```

Decade Counter

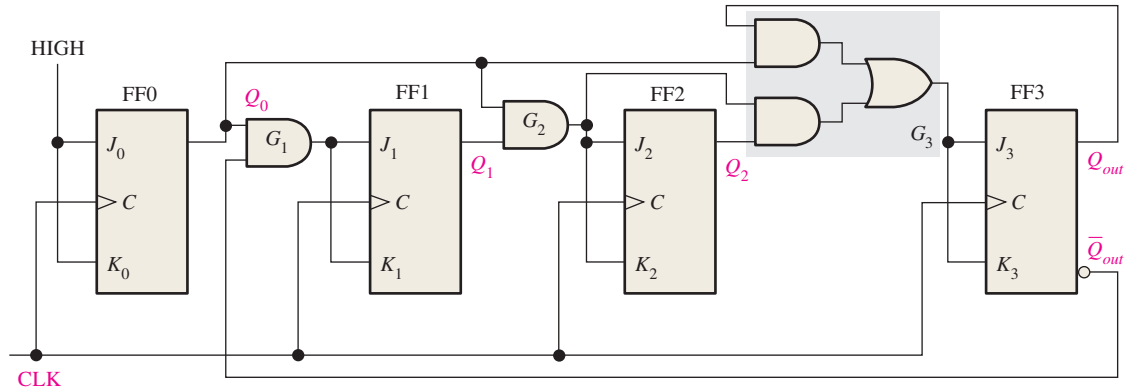


FIGURE 42 Decade counter.

VHDL FOR FOUR-BIT DECADE COUNTER

```

library ieee;
use ieee.std_logic_1164.all;

entity FourBitDecadeCounter is
port(Clk: in std_logic;
     QOut: buffer std_logic);
end entity FourBitDecadeCounter;

architecture FourBitCounterBehavior of FourBitDecadeCounter is
component jkff is
port (J, K, Clk: in std_logic;
     Q: out std_logic);
end component jkff;

signal G1, G2, G3: std_logic;
signal Q0, Q1, Q2: std_logic;
begin
    G1 <= Q0 and not QOut;
    G2 <= Q0 and Q1;
    G3 <= (Q0 and QOut) or (G2 and Q2);

    JKFF0: jkff port map (J => '1', K => '1', Clk => Clk, Q => Q0);
    JKFF1: jkff port map (J => G1, K => G1, Clk => Clk, Q => Q1);
    JKFF2: jkff port map (J => G2, K => G2, Clk => Clk, Q => Q2);
    JKFF3: jkff port map (J => G3, K => G3, Clk => Clk, Q => QOut);
end architecture FourBitCounterBehavior;

```

VERILOG FOR FOUR-BIT DECADE COUNTER

```

module FourBitDecadeCounter (Clk, QOut);
input Clk;
output QOut;

wire G1, G2, G3;
wire Q0, Q1, Q2;

assign G1 = (Q0 && !QOut);
assign G2 = (Q0 && Q1);
assign G3 = (Q0 && QOut) || (G2 && Q2);

jkff JKFF0(J(1), .K(1), .Clk(Clk), .Prn(1), .clrn(1), .Q(Q0));
jkff JKFF1(J(G1), .K(G1), .Clk(Clk), .Prn(1), .clrn(1), .Q(Q1));
jkff JKFF2(J(G2), .K(G2), .Clk(Clk), .Prn(1), .clrn(1), .Q(Q2));
jkff JKFF3(J(G3), .K(G3), .Clk(Clk), .Prn(1), .clrn(1), .Q(QOut));
endmodule

```

SECTION 8 CHECKUP

1. In the VHDL program for the 4-bit synchronous binary counter, what is the purpose of the lines:
 $G1 \leq Q0$ and $Q1$;
 $G2 \leq G1$ and $Q2$;
2. What is the purpose of four jkff lines in the Verilog program for the decade counter?

9 TROUBLESHOOTING

The troubleshooting of counters can be simple or quite involved, depending on the type of counter and the type of fault. This section will give you some insight into how to approach the troubleshooting of sequential circuits.



After completing this section, you should be able to

- Detect a faulty counter
- Isolate faults in maximum-modulus cascaded counters
- Isolate faults in cascaded counters with truncated sequences
- Determine faults in counters implemented with individual flip-flops

Counters

The symptom for a faulty counter is usually that it does not advance its count. If this is the case, then check power and ground on the chip. Look at these lines with a scope to make sure there is no noise present (a noisy ground may actually be open). Check that there are clock pulses and that they have the correct amplitude and rise time and that there is not extraneous noise on the line. (Sometimes clock pulses can be loaded down by other ICs, making it appear that the counter is faulty when it is not). If power, ground, and the clock pulses are okay, check all inputs (including enable, load, and clear inputs), to see that they are connected correctly and that the logic is correct. An open input can cause a counter to work correctly some of the time—inputs should never be left open, even if they are not used. (An unused input should be connected to an inactive level). If the counter is stuck in a state and the clock is present, determine what input should be present to advance the counter. This may point to a faulty input (including clear or load inputs), which can be caused by logic elsewhere in the circuit. If inputs are all checked okay, an output may be pulled LOW or HIGH by an external short or open (or another faulty IC), keeping the output from advancing.

Cascaded Counters with Maximum Modulus

A failure in one of the counters in a chain of cascaded counters can affect all the counters that follow it. For example, if a count enable input opens, it effectively acts as a HIGH (for TTL), and the counter is always enabled. This type of failure in one of the counters will cause that counter to run at the full clock rate and will also cause all the succeeding counters to run at higher than normal rates. This is illustrated in Figure 43 for a divide-by-1000 cascaded counter arrangement where an open enable (*CTEN*) input acts as a TTL HIGH and continuously enables the second counter. Other faults that can affect “downstream” counter stages are open or shorted clock inputs or terminal count outputs. In some of these situations, pulse activity can be observed, but it may be at the wrong frequency. Exact frequency or frequency ratio measurements must be made.

COUNTERS

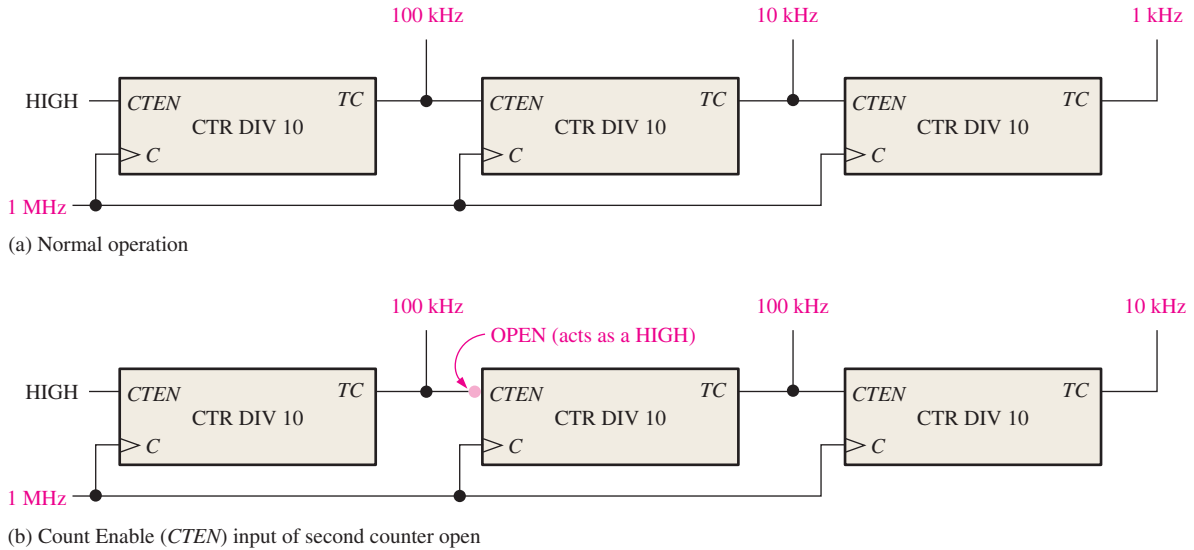


FIGURE 43 Example of a failure that affects following counters in a cascaded arrangement.

Cascaded Counters with Truncated Sequences

The count sequence of a cascaded counter with a truncated sequence, such as that in Figure 44, can be affected by other types of faults in addition to those mentioned for maximum-modulus cascaded counters. For example, a failure in one of the parallel data inputs, the \overline{LOAD} input, or the inverter can alter the preset count and thus change the modulus of the counter.

For example, suppose the D_3 input of the most significant counter in Figure 44 is open and acts as a HIGH. Instead of 6_{16} (0110) being preset into the counter, E_{16} (1110) is preset in. So, instead of beginning with $63C0_{16}$ ($25,536_{10}$) each time the counter recycles, the sequence will begin with $E3C0_{16}$ ($58,304_{10}$). This changes the modulus of the counter from 40,000 to $65,536 - 58,304 = 7232$.

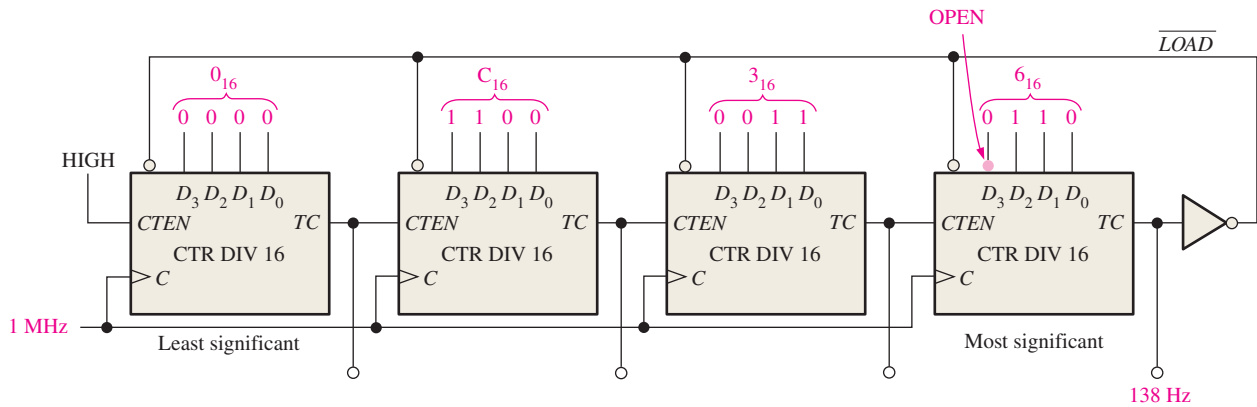


FIGURE 44 Example of a failure in a cascaded counter with a truncated sequence.

To check this counter, apply a known clock frequency, for example 1 MHz, and measure the output frequency at the final terminal count output. If the counter is operating properly, the output frequency is

$$f_{\text{out}} = \frac{f_{\text{in}}}{\text{modulus}} = \frac{1 \text{ MHz}}{40,000} = 25 \text{ Hz}$$

In this case, the specific failure described in the preceding paragraph will cause the output frequency to be

$$f_{\text{out}} = \frac{f_{\text{in}}}{\text{modulus}} = \frac{1 \text{ MHz}}{7232} \cong 138 \text{ Hz}$$

EXAMPLE 7

Frequency measurements are made on the truncated counter in Figure 45 as indicated. Determine if the counter is working properly, and if not, isolate the fault.

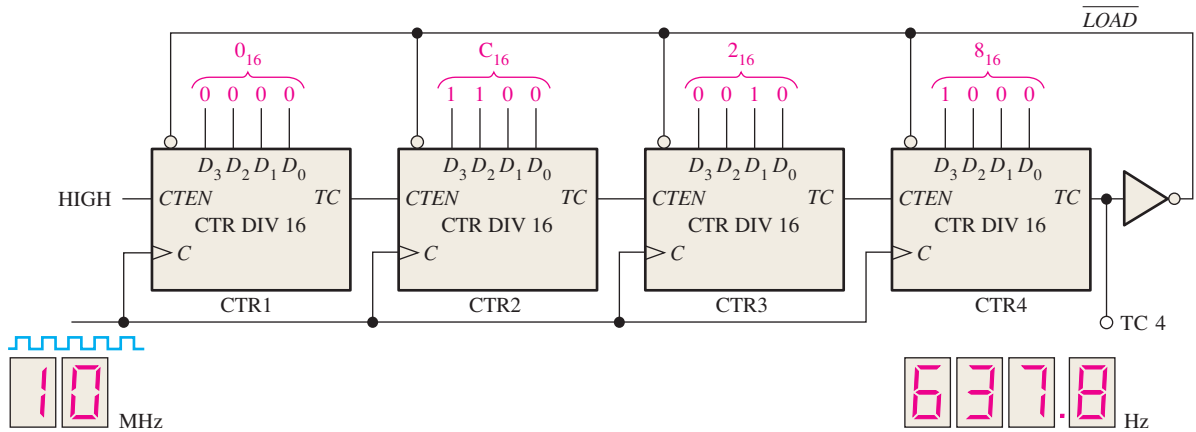


FIGURE 45

SOLUTION

Check to see if the frequency measured at TC 4 is correct. If it is, the counter is working properly.

$$\begin{aligned} \text{truncated modulus} &= \text{full modulus} - \text{preset count} \\ &= 16^4 - 82C_{016} \\ &= 65,536 - 33,472 = 32,064 \end{aligned}$$

The correct frequency at TC 4 is

$$f_4 = \frac{10 \text{ MHz}}{32,064} \cong 312 \text{ Hz}$$

There is a problem. The measured frequency of 637.8 Hz does not agree with the correct calculated frequency of 312 Hz.

To find the faulty counter, determine the actual truncated modulus as follows:

$$\text{modulus} = \frac{f_{\text{in}}}{f_{\text{out}}} = \frac{10 \text{ MHz}}{637.8 \text{ Hz}} = 15,679$$

Because the truncated modulus should be 32,064, most likely the counter is being preset to the wrong count when it recycles. The actual preset count is determined as follows:

$$\begin{aligned} \text{truncated modulus} &= \text{full modulus} - \text{preset count} \\ \text{preset count} &= \text{full modulus} - \text{truncated modulus} \\ &= 65,536 - 15,679 \\ &= 49,857 \\ &= C2C_{016} \end{aligned}$$

This shows that the counter is being preset to C2C₀₁₆ instead of 82C₀₁₆ each time it recycles.

Counters 1, 2, and 3 are being preset properly but counter 4 is not. Since C₁₆ = 1100₂, the D₂ input to counter 4 is HIGH when it should be LOW. This is most likely caused by an **open input**. Check for an external open caused by a bad solder connection, a broken conductor, or a bent pin on the IC. If none can be found, replace the IC and the counter should work properly.

RELATED PROBLEM

Determine what the output frequency at TC 4 would be if the D₃ input of counter 3 were open.

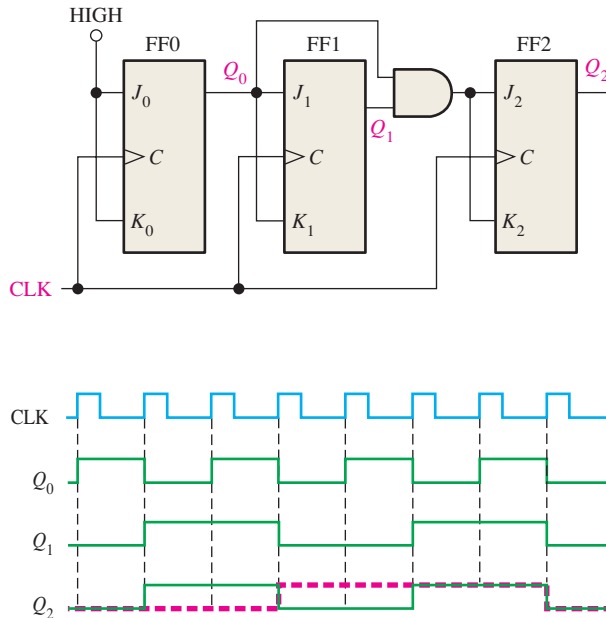
Counters Implemented with Individual Flip-Flops

Counters implemented with individual flip-flop and gate ICs are sometimes more difficult to troubleshoot because there are many more inputs and outputs with external connections than there are in an IC counter. The sequence of a counter can be altered by a single open or short on an input or output, as Example 8 illustrates.

EXAMPLE 8

Suppose that you observe the output waveforms (green) that are indicated for the counter in Figure 46. Determine if there is a problem with the counter.

FIGURE 46



HANDS ON TIP

To observe the time relationship between two digital signals with a dual-trace analog oscilloscope, the proper way to trigger the scope is with the slower of the two signals. The reason for this is that the slower signal has fewer possible trigger points than the faster signal and there will be no ambiguity for starting the sweep. Vertical mode triggering uses a composite of both channels and should never be used for determining absolute time information. Since clock signals are usually the fastest signal in a digital system, they should not be used for triggering.

SOLUTION

The Q_2 waveform is incorrect. The correct waveform is shown as a red dashed line. You can see that the Q_2 waveform looks exactly like the Q_1 waveform, so whatever is causing FF1 to toggle appears to also be controlling FF2.

Checking the J and K inputs to FF2, you find a waveform that looks like Q_0 . This result indicates that Q_0 is somehow getting through the AND gate. The only way this can happen is if the Q_1 input to the AND gate is always HIGH. However, you have seen that Q_1 has a correct waveform. This observation leads to the conclusion that the lower input to the AND gate must be internally open and acting as a HIGH. Replace the AND gate and retest the circuit.

RELATED PROBLEM

Describe the Q_2 output of the counter in Figure 46 if the Q_1 output of FF1 is open.

SECTION 9 CHECKUP

1. What failures can cause the counter in Figure 43 to have no pulse activity on any of the TC outputs?
2. What happens if the inverter in Figure 45 develops an open output?

SUMMARY

- Asynchronous and synchronous counters differ only in the way in which they are clocked. Synchronous counters can run at faster clock rates than asynchronous counters.
- The maximum modulus of a counter is the maximum number of possible states and is a function of the number of stages (flip-flops). Thus,

$$\text{Maximum modulus} = 2^n$$

where n is the number of stages in the counter. The modulus of a counter is the *actual* number of states in its sequence and can be equal to or less than the maximum modulus.

- The overall modulus of cascaded counters is equal to the product of the moduli of the individual counters.

KEY TERMS

Asynchronous Not occurring at the same time.

Cascade To connect “end-to-end” as when several counters are connected from the terminal count output of one counter to the enable input of the next counter.

Counter A sequential logic device that is used to divide signal frequency, count events, and generate specified sequences of bits.

Decade Characterized by ten states or values.

Mealy state machine A state machine in which the outputs depend on both the internal present state and on the inputs.

Modulus The number of unique states through which a counter will sequence.

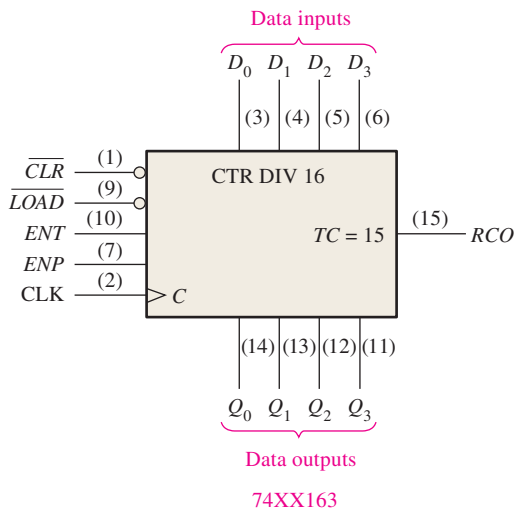
Moore state machine A state machine in which the outputs depend only on the internal present state.

Recycle To undergo transition (as in a counter) from the final or terminal state back to the initial state.

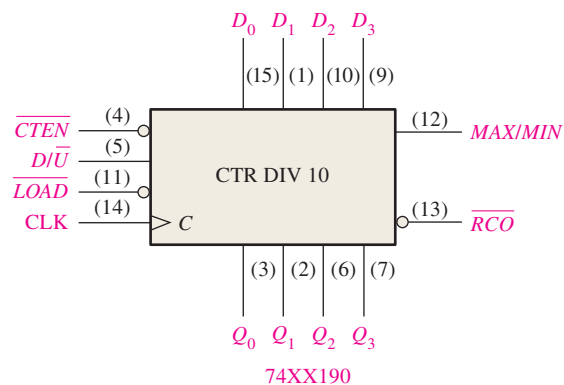
State machine A logic system exhibiting a sequence of states conditioned by internal logic and external inputs; any sequential circuit exhibiting a specified sequence of states.

Synchronous Occurring at the same time.

FIXED-FUNCTION LOGIC



4-bit synchronous binary counter



Up-down synchronous decade counter

TRUE/FALSE QUIZ

Answers are at the end of the chapter.

- In an asynchronous counter, all flip-flops change state at the same time.
- In a synchronous counter, all flip-flops are clocked simultaneously.

COUNTERS

3. An asynchronous counter is also known as a ripple counter.
4. A decade counter has sixteen states.
5. A counter with four stages has a maximum modulus of sixteen.
6. To achieve a maximum modulus of 32, sixteen stages are required.
7. If the present state is 1000, the next state of a 4-bit up/down counter in the DOWN mode is 0111.
8. Two cascaded decade counters divide the clock frequency by 20.
9. A counter with a truncated sequence has less than its maximum number of states.
10. To achieve a modulus of 100, ten decade counters are required.

SELF-TEST

Answers are at the end of the chapter.

1. Asynchronous counters are known as
 - (a) ripple counters
 - (b) multiple clock counters
 - (c) decade counters
 - (d) modulus counters
2. An asynchronous counter differs from a synchronous counter in
 - (a) the number of states in its sequence
 - (b) the method of clocking
 - (c) the type of flip-flops used
 - (d) the value of the modulus
3. The modulus of a counter is
 - (a) the number of flip-flops
 - (b) the actual number of states in its sequence
 - (c) the number of times it recycles in a second
 - (d) the maximum possible number of states
4. A 3-bit binary counter has a maximum modulus of
 - (a) 3
 - (b) 6
 - (c) 8
 - (d) 16
5. A 4-bit binary counter has a maximum modulus of
 - (a) 16
 - (b) 32
 - (c) 8
 - (d) 4
6. A modulus-12 counter must have
 - (a) 12 flip-flops
 - (b) 3 flip-flops
 - (c) 4 flip-flops
 - (d) synchronous clocking
7. Which one of the following is an example of a counter with a truncated modulus?
 - (a) Modulus 8
 - (b) Modulus 14
 - (c) Modulus 16
 - (d) Modulus 32
8. A 4-bit ripple counter consists of flip-flops that each have a propagation delay from clock to Q output of 12 ns. For the counter to recycle from 1111 to 0000, it takes a total of
 - (a) 12 ns
 - (b) 24 ns
 - (c) 48 ns
 - (d) 36 ns
9. A BCD counter is an example of
 - (a) a full-modulus counter
 - (b) a decade counter
 - (c) a truncated-modulus counter
 - (d) answers (b) and (c)
10. Which of the following is an invalid state in an 8421 BCD counter?
 - (a) 1100
 - (b) 0010
 - (c) 0101
 - (d) 1000
11. Three cascaded modulus-10 counters have an overall modulus of
 - (a) 30
 - (b) 100
 - (c) 1000
 - (d) 10,000
12. A 10 MHz clock frequency is applied to a cascaded counter consisting of a modulus-5 counter, a modulus-8 counter, and two modulus-10 counters. The lowest output frequency possible is
 - (a) 10 kHz
 - (b) 2.5 kHz
 - (c) 5 kHz
 - (d) 25 kHz
13. A 4-bit binary up/down counter is in the binary state of zero. The next state in the DOWN mode is
 - (a) 0001
 - (b) 1111
 - (c) 1000
 - (d) 1110
14. The terminal count of a modulus-13 binary counter is
 - (a) 0000
 - (b) 1111
 - (c) 1101
 - (d) 1100

PROBLEMS

Answers to odd-numbered problems are at the end of the chapter.

SECTION 1 A System

1. Assume that the digital clock of Figure 1 is initially reset to 12 o'clock. Determine the binary state of each counter after sixty-two 60 Hz pulses have occurred.
2. What is the output frequency of each counter in the digital clock circuit of Figure 1?

SECTION 2 Finite State Machines

3. Represent a decade counter with the terminal state decoded as a state machine. Identify the type and show the block diagram and the state diagram.
4. Identify the type of state machine for the traffic signal control system in the chapter "Latches, Flip-flops, and Timers." State the reason why it is the type you specified.

SECTION 3 Asynchronous Counters

5. For the ripple counter shown in Figure 47, show the complete timing diagram for eight clock pulses, showing the clock, Q_0 , and Q_1 waveforms.

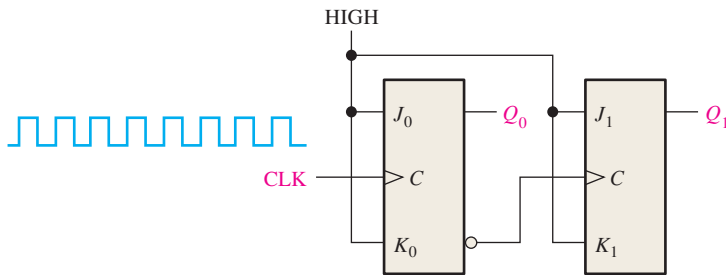


FIGURE 47

6. For the ripple counter in Figure 48, show the complete timing diagram for sixteen clock pulses. Show the clock, Q_0 , Q_1 , and Q_2 waveforms.

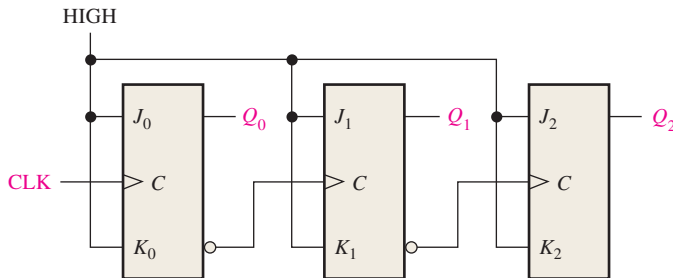


FIGURE 48

7. In the counter of Problem 6, assume that each flip-flop has a propagation delay from the triggering edge of the clock to a change in the Q output of 8 ns. Determine the worst-case (longest) delay time from a clock pulse to the arrival of the counter in a given state. Specify the state or states for which this worst-case delay occurs.
8. Show how to connect a 4-bit asynchronous counter for each of the following moduli using the Clear input:
 - (a) 9
 - (b) 11
 - (c) 13
 - (d) 14
 - (e) 15

SECTION 4 Synchronous Counters

9. If the counter of Problem 7 were synchronous rather than asynchronous, what would be the longest delay time?
10. Show the complete timing diagram for the 5-stage synchronous binary counter in Figure 49. Verify that the waveforms of the Q outputs represent the proper binary number after each clock pulse.

COUNTERS

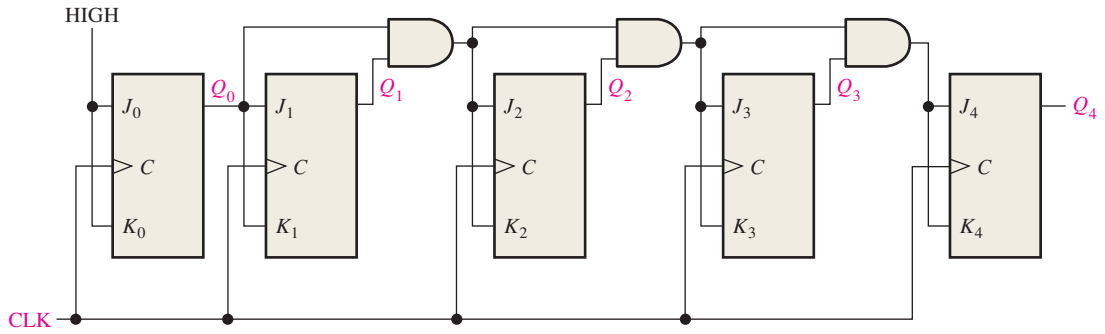


FIGURE 49

11. By analyzing the J and K inputs to each flip-flop prior to each clock pulse, prove that the decade counter in Figure 50 progresses through a BCD sequence. Explain how these conditions in each case cause the counter to go to the next proper state.

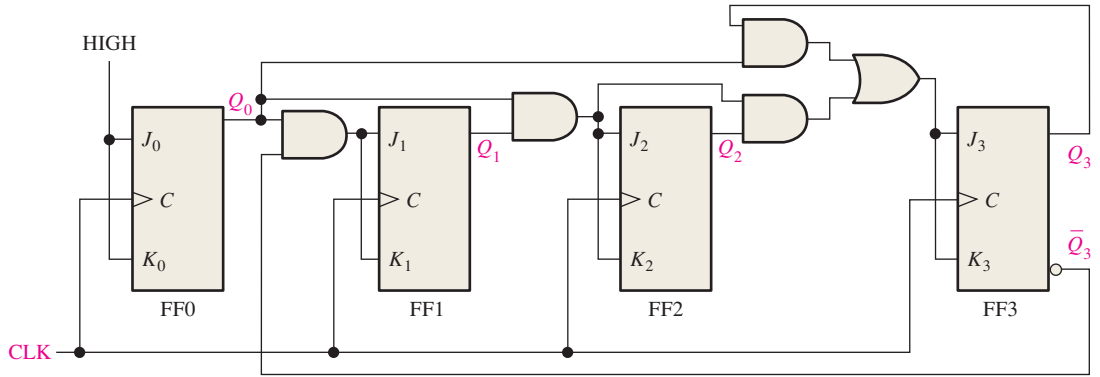


FIGURE 50

12. The waveforms in Figure 51 are applied to the count enable, clear, and clock inputs as indicated. Show the counter output waveforms in proper relation to these inputs. The clear input is asynchronous.

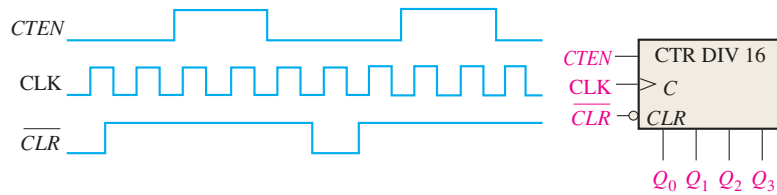


FIGURE 51

13. A BCD decade counter is shown in Figure 52. The waveforms are applied to the clock and clear inputs as indicated. Determine the waveforms for each of the counter outputs (Q_0 , Q_1 , Q_2 , and Q_3). The clear is synchronous, and the counter is initially in the binary 1000 state.

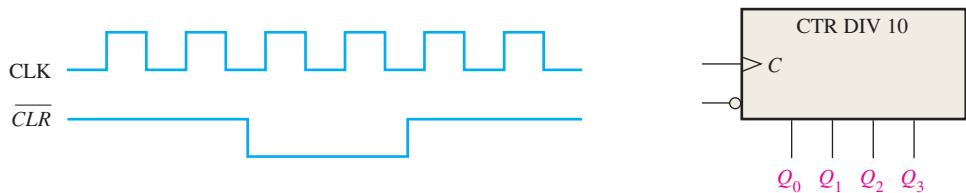


FIGURE 52

SECTION 5 Up/Down Synchronous Counters

14. Show a complete timing diagram for a 3-bit up/down counter that goes through the following sequence. Indicate when the counter is in the UP mode and when it is in the DOWN mode. Assume positive edge-triggering.

0, 1, 2, 3, 2, 1, 2, 3, 4, 5, 6, 5, 4, 3, 2, 1, 0

15. Develop the Q output waveforms for the binary up/down counter with the input waveforms shown in Figure 53. Start with a count of 0000.

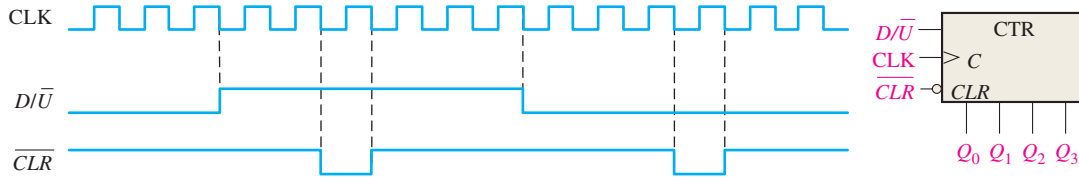


FIGURE 53

16. Repeat Problem 15 if the D/\bar{U} input signal is inverted with the \overline{CLR} the same.
 17. Repeat Problem 15 if the \overline{CLR} is inverted with the D/\bar{U} inputs the same.

SECTION 6 Cascaded Counters

18. For each of the cascaded counter configurations in Figure 54, determine the frequency of the waveform at each point indicated by a circled number, and determine the overall modulus.

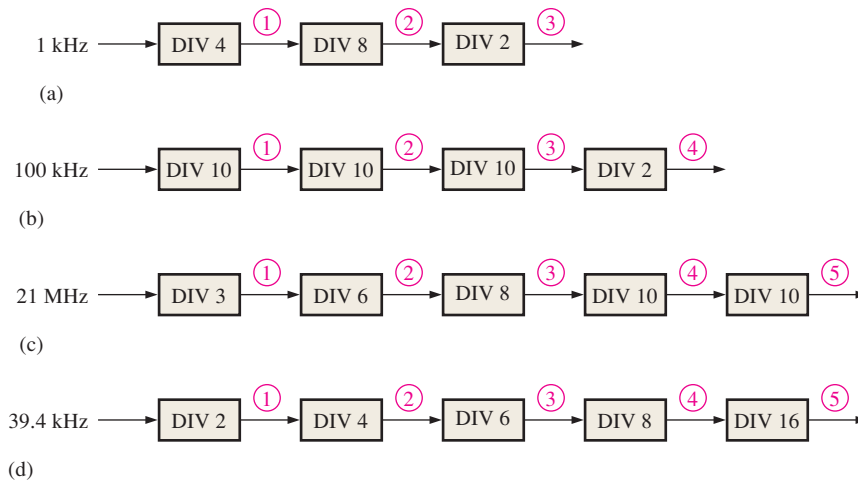


FIGURE 54

19. Expand the counter in Figure 31 to create a divide-by-10,000 counter and a divide-by-100,000 counter.
 20. With general block diagrams, show how to obtain the following frequencies from a 10 MHz clock by using single flip-flops, modulus-5 counters, and decade counters:
 (a) 5 MHz (b) 2.5 MHz (c) 2 MHz (d) 1 MHz (e) 500 kHz
 (f) 250 kHz (g) 62.5 kHz (h) 40 kHz (i) 10 kHz (j) 1 kHz

SECTION 7 Counter Decoding

21. Given a BCD decade counter with only the Q outputs available, show what decoding logic is required to decode each of the following states and how it should be connected to the counter. A HIGH output indication is required for each decoded state. The MSB is to the left.
 (a) 0001 (b) 0011 (c) 0101 (d) 0111 (e) 1000

COUNTERS

22. For the 4-bit binary counter connected to the decoder in Figure 55, determine each of the decoder output waveforms in relation to the clock pulses.

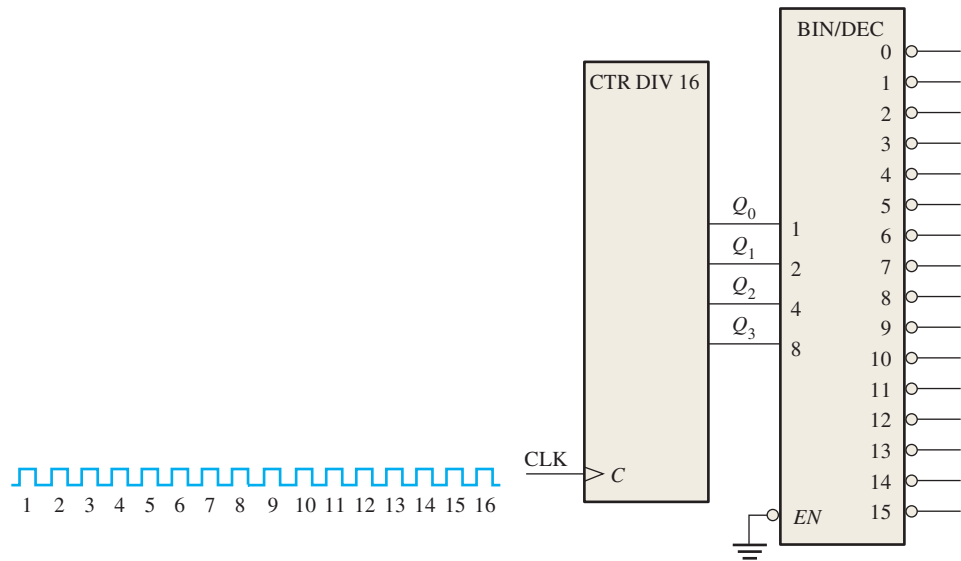


FIGURE 55

23. If the counter in Figure 55 is asynchronous, determine where the decoding glitches occur on the decoder output waveforms.
24. Modify the circuit in Figure 55 to eliminate decoding glitches.
25. Analyze the counter in Figure 35 for the occurrence of glitches on the decode gate output. If glitches occur, suggest a way to eliminate them.
26. Analyze the counter in Figure 36 for the occurrence of glitches on the outputs of the decoding gates. If glitches occur, make a design change that will eliminate them.

SECTION 8 Counters with VHDL and Verilog

27. Expand the 4-bit synchronous binary counter in Figure 41 to five bits. Describe the input requirements for a third AND gate G_3 , required to provide the J_4 and K_4 inputs to the additional JK flip-flop stage. Write the assignment statement for G_3 using VHDL or Verilog.
28. What are three advantages of implementing a counter system using VHDL?
29. Referring to the four-bit synchronous decade counter in Figure 42, draw the resulting timing diagram if the equation for G_3 is modified as follows:
- $$G_3 \leq (Q_0 \text{ and } Q_{Out}) \text{ or } (G_1 \text{ and } Q_1);$$
30. Referring to the 4-bit synchronous binary counter timing diagram in Figure 19, the output of the JKFF2 flip-flop represents the binary value 2 raised to what power?

SECTION 9 Troubleshooting

31. For the counter in Figure 7, show the timing diagram for the Q_0 and Q_1 waveforms for each of the following faults (assume Q_0 and Q_1 are initially LOW):
- clock input to FF0 shorted to ground
 - Q_0 output open
 - clock input to FF1 open
 - J input to FF0 open
 - K input to FF1 shorted to ground
32. Solve Problem 31 for the counter in Figure 14.
33. Isolate the fault in the counter in Figure 9(a) by analyzing the waveforms in Figure 56.
34. From the waveform diagram in Figure 57, determine the most likely fault in the counter of Figure 17.
35. Solve Problem 34 if the Q_2 output has the waveform observed in Figure 58. Outputs Q_0 and Q_1 are the same as in Figure 57.

COUNTERS

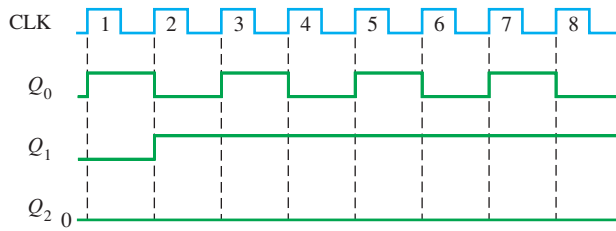


FIGURE 56

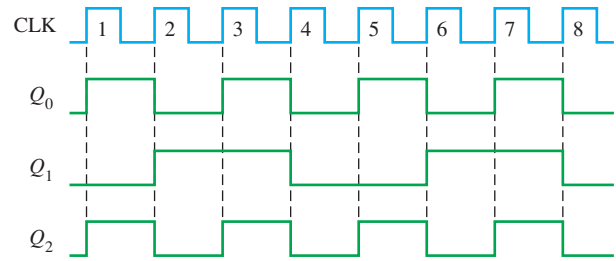


FIGURE 57

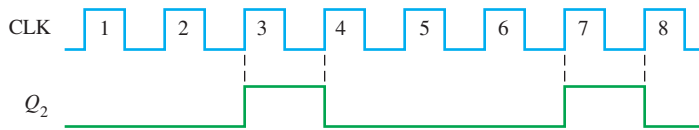


FIGURE 58

36. You apply a 5 MHz clock to the cascaded counter in Figure 34 and measure a frequency of 76.2939 Hz at the last TC output. Is this correct, and if not, what is the most likely problem?
37. Develop a table for use in testing the counter in Figure 34 that will show the frequency at the final TC output for all possible open failures of the parallel data inputs (D_0 , D_1 , D_2 , and D_3) taken one at a time. Use 10 MHz as the test frequency for the clock.
38. The tens-of-hours 7-segment display in the digital clock system of Figure 1 continuously displays a 1. All the other digits work properly. What could be the problem?
39. What would be the visual indication of an open Q_1 output in the tens portion of the minutes counter in Figure 1? Also see Figure 2.
40. One day complaints begin flooding in from patrons of a parking garage that uses the control system depicted in Figures 26 and 27. The patrons say that they enter the garage because the gate is up and the FULL sign is off but that, once in, they can find no empty space. As the technician in charge of this facility, what do you think the problem is, and how will you troubleshoot and repair the system as quickly as possible?

Special Problems

41. For the automobile parking control system in Figure 26, a pattern of entrance and exit sensor pulses during a given 24-hour period are shown in Figure 59. If there were 53 cars already in the garage at the beginning of the period, what is the state of the counter at the end of the 24 hours?

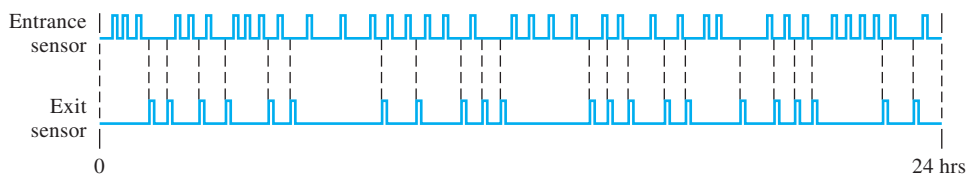


FIGURE 59

42. The binary number for decimal 57 appears on the parallel data inputs of the parallel-to-serial converter in Figure 22 (D_0 is the LSB). The counter initially contains all zeros and a 10 kHz clock is applied. Develop the timing diagram showing the clock, the counter outputs, and the serial data output.
43. Develop a modulus-1000 counter by using decade counters.
44. Modify the counter in Figure 34 to achieve a modulus of 30,000.
45. Repeat Problem 44 for a modulus of 50,000.
46. Modify the digital clock in Figures 1, 2, and 3 so that it can be preset to any desired time.
47. Implement an alarm circuit for the digital clock that can detect a predetermined time (hours and minutes only) and produce a signal to activate an audio alarm.
48. Modify the circuit in Figure 27 for a 1000-space parking garage and a 3000-space parking garage.

MULTISIM



MULTISIM TROUBLESHOOTING PRACTICE

49. Open file P08-49 and follow the instructions given there.
50. Open file P08-50 and follow the instructions given there.
51. Open file P08-51 and follow the instructions given there.
52. Open file P08-52 and follow the instructions given there.
53. Open file P08-53 and follow the instructions given there.

ANSWERS TO SECTION CHECKUPS

SECTION 1 A System

1. Gate G_1 resets flip-flop on first clock pulse after count 9. Gate G_2 decodes count 12 to preset counter to 0001.
2. The hours decade counter advances through each state from zero to nine, and as it recycles from nine back to zero, the flip-flop is toggled to the SET state. This produces a ten (10) on the display. When the hours decade counter is in state 12, the decode NAND gate causes the counter to recycle to state 1 on the next clock pulse. The flip-flop resets. This results in a one (01) on the display.

SECTION 2 Finite State Machines

1. A finite state machine has a limited number of states that occur in a prescribed order.
2. Moore and Mealy are two types of finite state machines.
3. In a Moore machine, only the present state determines the outputs. In a Mealy machine, not only the present state but the input(s) determine the outputs.

SECTION 3 Asynchronous Counters

1. Asynchronous means that each flip-flop after the first one is enabled by the output of the preceding flip-flop.
2. A modulus-14 counter has fourteen states requiring four flip-flops.

SECTION 4 Synchronous Counters

1. All flip-flops in a synchronous counter are clocked simultaneously.
2. An 8-bit synchronous binary counter has 64 states.

SECTION 5 Up/Down Synchronous Counters

1. The counter goes to 1001.
2. UP: 1111; DOWN: 0000; the next state is 1111.

SECTION 6 Cascaded Counters

1. Three decade counters produce $\div 1000$; 4 decade counters produce $\div 10,000$.
2. (a) $\div 20$: flip-flop and DIV 10
 (b) $\div 32$: flip-flop and DIV 16
 (c) $\div 160$: DIV 16 and DIV 10
 (d) $\div 320$: DIV 16 and DIV 10 and flip-flop

SECTION 7 Counter Decoding

1. (a) No transitional states because there is a single bit change
 (b) 0000, 0001, 0010, 0101, 0110, 0111
 (c) No transitional states because there is a single bit change
 (d) 0001, 0010, 0011, 0100, 0101, 0110, 0111, 1000, 1001, 1010, 1011, 1100, 1101, 1110

SECTION 8 Counters with VHDL and Verilog

1. $G1 \leq Q0$ and $Q1$; Defines the logic for gate $G_1 = Q_0Q_1$
 $G2 \leq G1$ and $Q2$; Defines the logic for gate $G_2 = Q_0Q_1Q_2$
2. These four lines define how the flip-flops are connected.

SECTION 9 Troubleshooting

1. No pulses on TC outputs: $CTEN$ of first counter shorted to ground or to a LOW; clock input of first counter open; clock line shorted to ground or to a LOW; TC output of first counter shorted to ground or to a LOW.
2. With the inverter output open, the counter does not recycle at the preset count but acts as a full-modulus counter.

ANSWERS TO RELATED PROBLEMS FOR EXAMPLES

- 1 See Figure 60.

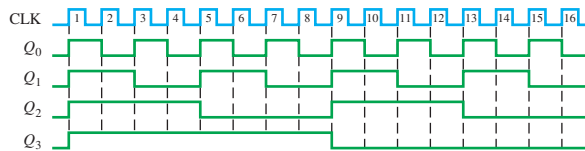


FIGURE 60

- 2 Connect Q_0 to the NAND gate as a third input (Q_2 and Q_3 are two of the inputs). Connect the CLR line to the CLR input of FF0 as well as FF2 and FF3.
- 3 See Figure 61.

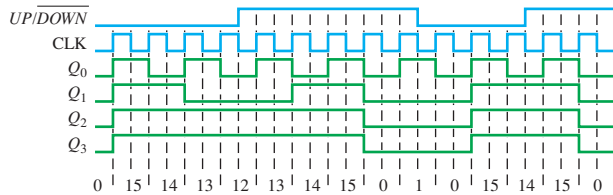


FIGURE 61

- 4 Five decade counters are required. $10^5 = 100,000$
- 5 $f_{Q0} = 1 \text{ MHz} / [(10)(2)] = 50 \text{ kHz}$
- 6 See Figure 62.

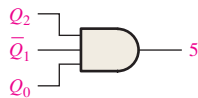


FIGURE 62

- 7 $8AC0_{16}$ would be loaded. $16^4 - 8AC0_{16} = 65,536 - 32,520 = 30,016$
 $f_{TC4} = 10 \text{ MHz} / 30,016 = 333.2 \text{ Hz}$
- 8 See Figure 63.

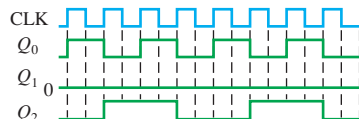


FIGURE 63

ANSWERS TO TRUE/FALSE QUIZ

1. F 2. T 3. T 4. F 5. T
 6. F 7. T 8. F 9. T 10. F

ANSWERS TO SELF-TEST

1. (a) 2. (b) 3. (b) 4. (c) 5. (a) 6. (c) 7. (b)
 8. (c) 9. (d) 10. (a) 11. (c) 12. (b) 13. (b) 14. (d)

ANSWERS TO ODD-NUMBERED PROBLEMS

1. Hours tens: 0001
 Hours units: 0010
 Minutes tens: 0000
 Minutes units: 0001
 Seconds tens: 0000
 Seconds units: 0010
3. This is a Moore machine. See Figure P-58.

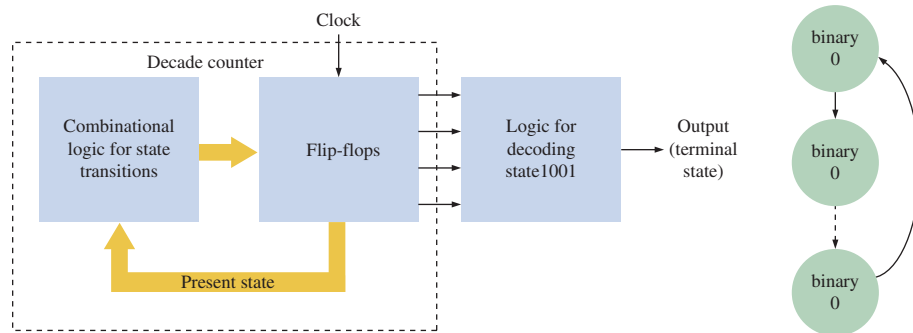


FIGURE P-58

5. See Figure P-59.

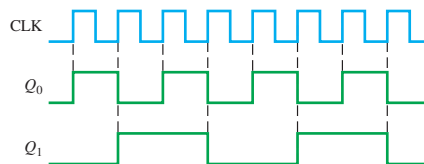


FIGURE P-59

7. Worst-case delay is 24 ns; it occurs when all flip-flops change state from 011 to 100 or from 111 to 000.
9. 8 ns
11. Initially, each flip-flop is reset.
 At CLK1:
 $J_0 = K_0 = 1$ Therefore Q_0 goes to a 1.
 $J_1 = K_1 = 0$ Therefore Q_1 remains a 0.
 $J_2 = K_2 = 0$ Therefore Q_2 remains a 0.
 $J_3 = K_3 = 0$ Therefore Q_3 remains a 0.
 At CLK2:
 $J_0 = K_0 = 1$ Therefore Q_0 goes to a 0.
 $J_1 = K_1 = 1$ Therefore Q_1 goes to a 1.

COUNTERS

$J_2 = K_2 = 0$ Therefore Q_2 remains a 0.

$J_3 = K_3 = 0$ Therefore Q_3 remains a 0.

At CLK3:

$J_0 = K_0 = 1$ Therefore Q_0 goes to a 1.

$J_1 = K_1 = 0$ Therefore Q_1 remains a 1.

$J_2 = K_2 = 0$ Therefore Q_2 remains a 0.

$J_3 = K_3 = 0$ Therefore Q_3 remains a 0.

A continuation of this procedure for the next seven clock pulses will show that the counter progresses through the BCD sequence.

13. See Figure P-60.

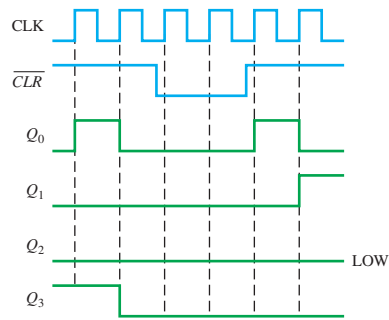


FIGURE P-60

15. See Figure P-61.

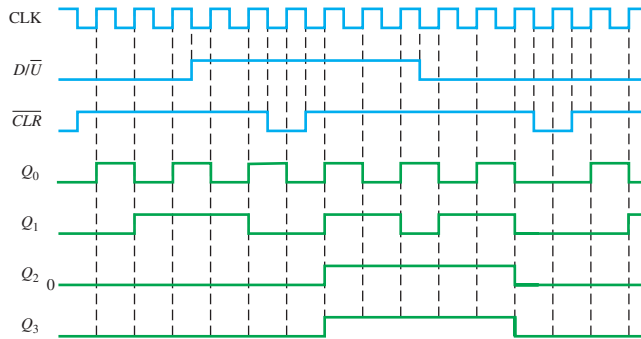


FIGURE P-61

17. See Figure P-62.

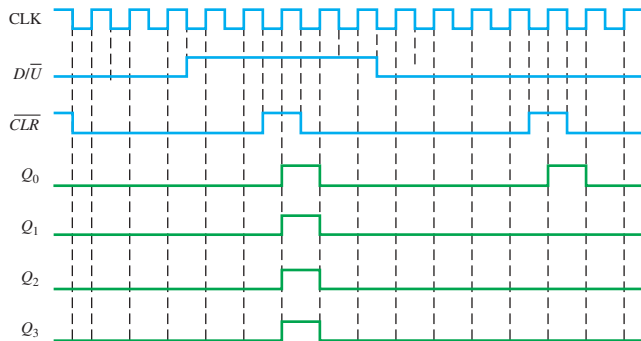


FIGURE P-62

COUNTERS

19. See Figure P-63 for divide-by-10,000. Add one more DIV10 counter to create a divide-by-100,000.

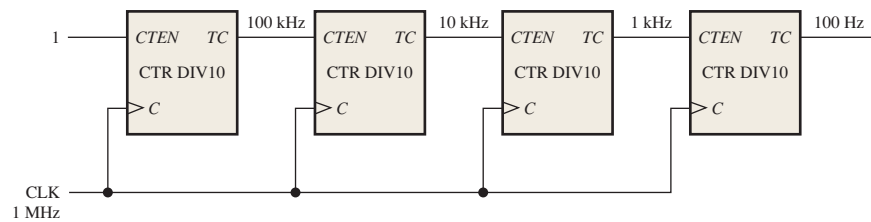


FIGURE P-63

21. See Figure P-64.

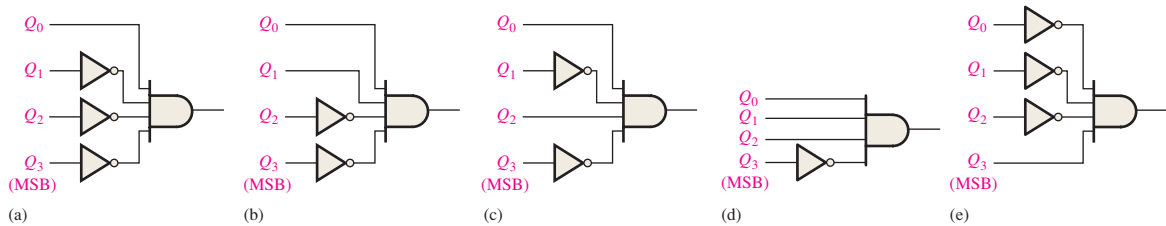


FIGURE P-64

23. CLK2, output 0; CLK4, outputs 2, 0; CLK6, output 4; CLK8, outputs 6, 4, 0; CLK10, output 8; CLK12, outputs 10, 8; CLK14, output 12; CLK16, outputs 14, 12, 8
25. A glitch of the AND gate output occurs on the 111 to 000 transition. Eliminate by ANDing $\overline{\text{CLK}}$ with counter outputs (strobe) or use Gray code.
27. The addition of AND gate (G3) causes the additional fifth J-K flip-flop stage (FF4) to change when Q_0 , Q_1 , Q_2 , and Q_3 are HIGH.
VHDL: $G3 \leq G2 \text{ and } Q3$;
Verilog: **assign** $G3 = G2 \ \&\& \ Q3$;
29. See Figure P-65.



FIGURE P-65

31. (a) Q_0 and Q_1 will not change from their initial state.
 (b) normal operation except Q_0 floating
 (c) Q_0 waveform is normal; Q_1 remains in initial state.
 (d) normal operation
 (e) The counter will not change from its initial state.
33. The K input of FF1 must be connected to ground rather than to the J input. Check for a wiring error.
35. Q_0 input to AND gate open and acting as a HIGH
37. See Table P-12.
39. The decode 6 gate interprets count 4 as a 6 (0110) and clears the counter back to 0 (actually 0010 since Q_1 is open). The apparent sequence of the tens portion of the counter is 0010, 0011, 0010, 0011, 0110.
41. 68
43. See Figure P-66.
45. $65,536 - 50,000 = 15,536$
 Preset the counter to 15,536 so that it counts from 15,536 up to 65,536 on each full cycle, thus producing a sequence of 50,000 states (modulus 50,000).
 $15,536 = 11110010110000_2 = 3CB0_{16}$
 See Figure P-67.

COUNTERS

TABLE P-12			
STAGE	OPEN	LOADED COUNT	f_{OUT}
1	0	63C1	250.006 Hz
1	1	63C2	250.012 Hz
1	2	63C4	250.025 Hz
1	3	63C8	250.050 Hz
2	0	63D0	250.100 Hz
2	1	63E0	250.200 Hz
2	2	63C0	250 Hz
2	3	63C0	250 Hz
3	0	63C0	250 Hz
3	1	63C0	250 Hz
3	2	67C0	256.568 Hz
3	3	6BC0	263.491 Hz
4	0	73C0	278.520 Hz
4	1	63C0	250 Hz
4	2	63C0	250 Hz
4	3	E3C0	1.383 KHZ

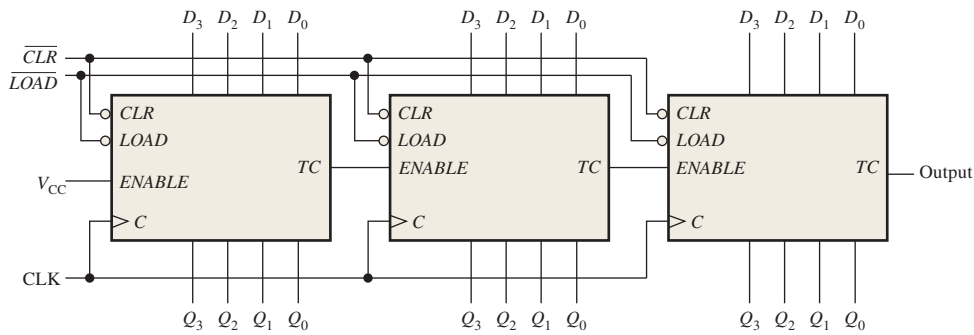


FIGURE P-66

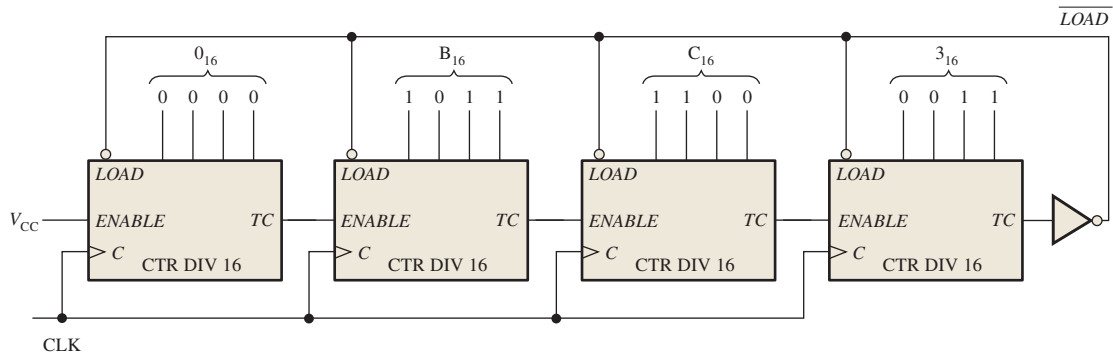


FIGURE P-67

47. See Figure P-68.

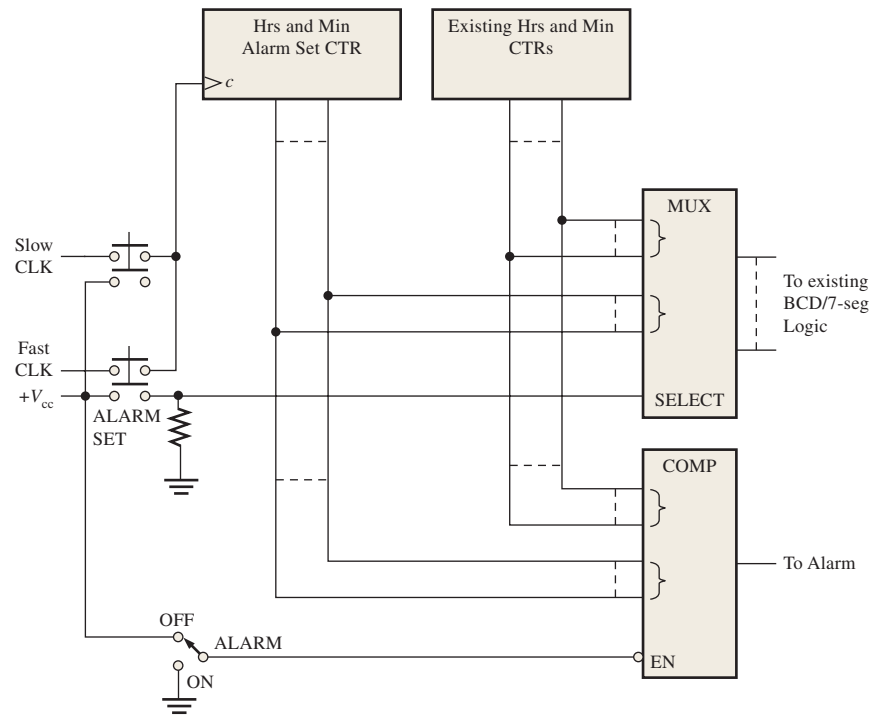


FIGURE P-68

49. **Circuit fault:** Line to CLK input of U3 is open.
Predicted effect of fault: Q0 and Q1 will sequence normally. Q2 and Q3 will remain LOW.
Observed effect of introduced fault: Q0 and Q1 will sequence normally. Q2 and Q3 will remain LOW.
51. **Circuit fault:** The Q output of U3 is shorted to ground.
Predicted effect of fault: The Q3Q2Q1Q0 count sequence is 0000, 0001, 0010, 0011, 0000, . . . rather than a decade up count.
Observed effect of introduced fault: The Q3Q2Q1Q0 count sequence is 0000, 0001, 0010, 0011, 0000, . . . rather than a decade up count.
53. **Observed operation:** The 74LS190 decade counter always functions as a down counter.
Suspected fault: Line to notU/D input of counter always HIGH.
Effect of introduced fault: The 74LS190 decade counter always functions as a down counter.

MEMORY AND STORAGE

MEMORY AND STORAGE

OUTLINE

- 1 Memory System Hierarchy
- 2 Semiconductor Memory Basics
- 3 The Random-Access Memory (RAM)
- 4 The Read-Only Memory (ROM)
- 5 Programmable ROMs
- 6 The Flash Memory
- 7 Memory Expansion
- 8 Special Types of Memories
- 9 Magnetic and Optical Storage
- 10 Troubleshooting

OBJECTIVES

- Explain memory hierarchy
- Define the basic memory characteristics
- Explain what a RAM is and how it works
- Explain the difference between static RAMs (SRAMs) and dynamic RAMs (DRAMs)
- Explain what a ROM is and how it works
- Describe the various types of PROMs
- Discuss the characteristics of a flash memory
- Describe the expansion of ROMs and RAMs to increase word length and word capacity
- Discuss special types of memories such as FIFO and LIFO
- Describe the basic organization of magnetic disks and magnetic tapes
- Describe the basic operation of magneto-optical disks and optical disks

- Describe basic methods for memory testing
- Develop flowcharts for memory testing

KEY TERMS

Memory hierarchy	SRAM
Memory	DRAM
Byte	Bus
Word	DDR
Cell	PROM
Address	EPROM
Capacity	Flash memory
Write	FIFO
Read	LIFO
RAM	Hard disk
ROM	

INTRODUCTION

The memory devices covered in this chapter are generally used for longer-term storage of larger amounts of data as compared to shift registers, which are type of storage device and essentially a small-scale memory.

Computers and other types of systems require the permanent or semipermanent storage of large amounts of binary data. Microprocessor-based systems rely on storage devices and memories for their operation because of

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the necessity for storing programs and for retaining data during processing.

In computer terminology, *memory* usually refers to registers, cache, main (RAM and ROM), and hard disk.

Storage refers to tape, optical disk, and magnetic disk. In this chapter semiconductor memories and magnetic and optical storage media are covered.

1 MEMORY SYSTEM HIERARCHY

A memory system performs the data storage function in a computer. The memory system holds data temporarily during processing and also stores data and programs on a long-term basis. A computer has several types of memory, such as registers, cache, main, and hard disk. Other types of storage can also be used, such as magnetic tape, optical disk, and magnetic disk. Memory hierarchy as well as the system processor determines the processing speed of a computer.

After completing this section, you should be able to

- Discuss several types of memory
- Define memory hierarchy
- Describe key elements in a memory hierarchy

Three key characteristics of memory are cost, capacity, and access time. Memory cost is usually specified in cost per bit. The capacity of a memory is measured in the amount of data (bits or bytes) it can store. The access time is the time it takes to acquire a specified unit of data from the memory. The greater the capacity, the smaller the cost and the greater the access time. The smaller the access time, the greater the cost. The goal of using a memory hierarchy is to obtain the shortest possible average access time while minimizing the cost.

The speed with which data can be processed depends both on the processor speed and on the time it takes to access stored data. **Memory hierarchy*** is the arrangement of various memory system elements within the computer architecture to maximize processing speed and minimize cost. Memory can be classified according to its “distance” from the processor in terms of the number of machine cycles or access time required to get data for processing. Distance is measured in time, not in physical location. Faster memory elements are considered closer to the processor compared to slower types of memory elements. Also, the cost per bit is much greater for the memory close to the processor than for the memory that is further from the processor. Figure 1 illustrates the arrangement of elements in a typical memory hierarchy.

A primary distinction between the memory and storage elements in Figure 1 is the time required for the processor to access data and programs. This access time is known as **memory latency**. The greater the latency, the further from the processor a memory or storage element is considered to be. For example, typical register latency can be up to 1 or 2 ns, cache latency can be up to about 50 ns, main memory latency can be up to about 90 ns, and hard disk latency can be up to about 20 ms. Auxiliary memory latency can range up to several seconds.

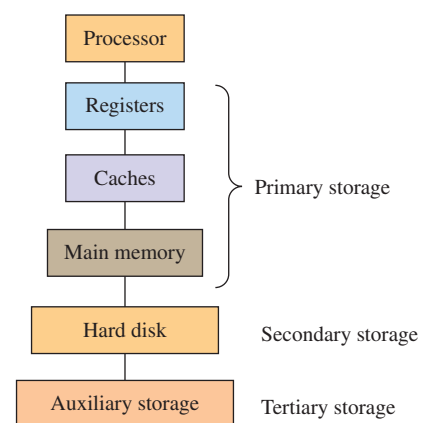


FIGURE 1 Typical memory hierarchy.

Registers

Registers are memory elements that are located within the processor. They have a very small latency as well as a low capacity (number of bits that can be stored). One goal of

*The bold terms in color are key terms and are included in a Key Term glossary at the end of the chapter.

programming is to keep as much frequently used data in the registers as possible. The number of registers in a processor can vary from the tens to hundreds.

Caches

The next level in the hierarchy is the memory cache, which provides temporary storage. The L1 cache is located in the processor, and the L2 cache is outside of the processor. A programming goal is to keep as much of a program as possible in the cache, especially the parts of a program that are most extensively used. There can be more than two caches in a memory system.

Main Memory

Main memory generally consists of two elements: RAM (random-access memory) and ROM (read-only memory). The RAM is a working memory that temporarily stores less frequently used data and program instructions. The RAM is volatile, which means that the stored contents are lost when the power is turned off. The ROM is for permanent storage of frequently used programs and data; ROM is nonvolatile. Registers, caches, and main memory are considered primary storage.

Hard Disk

The hard disk has a very high latency and is used for mass storage of data and programs on a permanent basis. The hard disk is also used for virtual memory, space allocated for data when the primary memory fills up. In effect, virtual memory simulates primary memory with the disadvantage of high latency. Capacities range up to about 1 terabyte (TB).

$$1 \text{ TB} = 1,000,000,000,000 \text{ B} = 10^{12} \text{ B}$$

In addition to the internal hard disk, secondary storage can also include off-line storage. Off-line storage includes DVDs, CD-ROM, CD-RW, and USB flash drive. Off-line storage is removable storage.

Auxiliary Storage

Auxiliary storage, also called *tertiary storage*, includes magnetic tape libraries and optical jukeboxes. A **tape library** can store immense amounts of data (up to hundreds of petabytes). A petabyte (PB) is

$$1 \text{ PB} = 1,000,000,000,000,000 \text{ B} = 10^{15} \text{ B}$$

An **optical jukebox** is a robotic storage device that automatically loads and unloads optical disks. It may have as many as 2,000 slots for disks and can store hundreds of petabytes.

Relationship of Cost, Capacity, and Access Time

Figure 2 shows how capacity (the amount of data a memory can store) and cost per unit of storage varies as the distance from the processor, in terms of access time or latency, increases. The capacity increases and the cost decreases as access time increases.

Memory Hierarchy Performance

In a computer system, the overall processing speed is usually limited by the memory, not the processor. Programming determines how well a particular memory hierarchy is utilized. The goal is to process data at the fastest rate possible. Two key factors in establishing maximum processor performance are locality and hit rate.

If a block of data is referenced, it will tend to be either referenced again soon or a nearby data block will be referenced soon. Frequent referencing of the same data block is

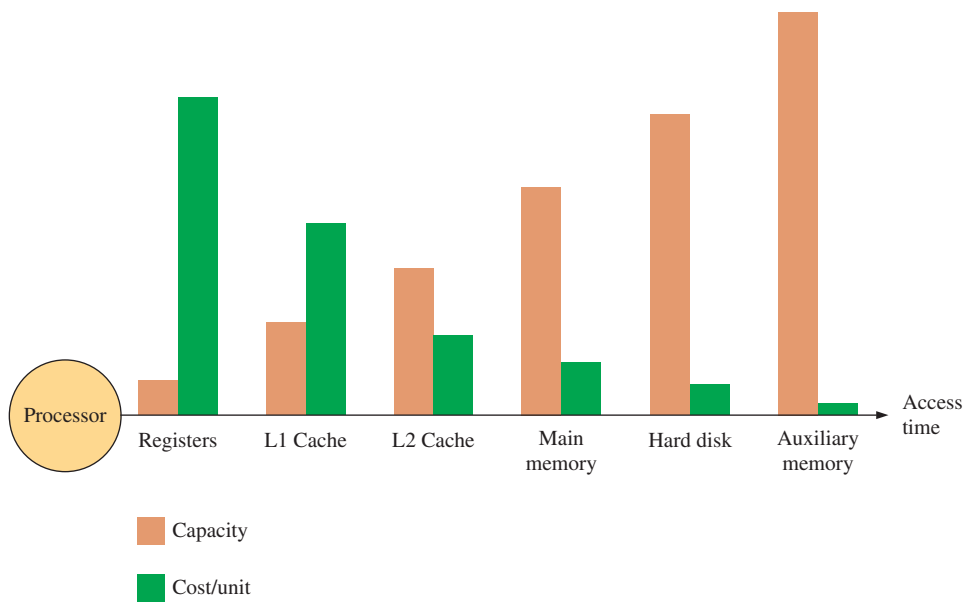


FIGURE 2 Changes in memory capacity and cost per unit of data as latency (access time) increases.

known as *temporal locality*, and the program code should be arranged so that the piece of the data in the cache is reused frequently. Referencing an adjacent data block is known as *spatial locality*, and the program code should be arranged to use consecutive pieces of data on a frequent basis.

A **miss** is a failed attempt by the processor to read or write a block of data in a given level of memory (such as the cache). A miss causes the processor to have to go to a lower level of memory (such as main memory), which has a longer latency. The three types of misses are instruction read miss, data read miss, and data write miss. A successful attempt to read or write a block of data in a given level of memory is called a *hit*. Hits and misses are illustrated in Figure 3, where the processor is requesting data from the cache.

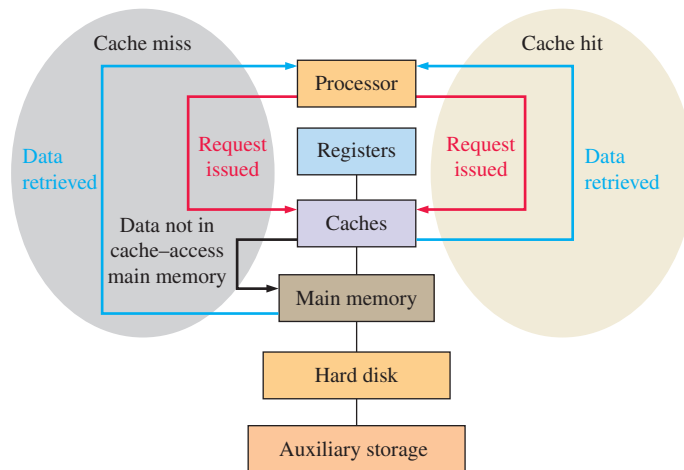


FIGURE 3 Illustration of a cache hit and a miss.

The **hit rate** is the percentage of memory accesses that find the requested data in the given level of memory. The *miss rate* is the percentage of memory accesses that fail to find the requested data in the given level of memory and is equal to $1 - \text{hit rate}$. The time required to access the requested information in a given level of memory is called the *hit time*. The higher the hit rate (hit to miss ratio), the more efficient the memory hierarchy is.

SECTION 1 CHECKUP*

1. State the purpose of memory hierarchy.
2. What is access time?
3. How does memory capacity affect the cost per bit?
4. Does higher level memory generally have lower capacity than lower level memory?
5. What is a hit? A miss?
6. What determines the efficiency of the memory hierarchy?

*Answers are at the end of the chapter.

2 SEMICONDUCTOR MEMORY BASICS

Memory is the portion of a computer or other system that stores binary data. In a computer, memory is accessed millions of times per second, so the requirement for speed and accuracy is paramount. Very fast semiconductor memory is available today in modules with over 1 GB (a gigabyte is one billion bytes) of capacity. These large-memory modules use exactly the same operating principles as smaller units, so we will use smaller ones for illustration in this chapter to simplify the concepts.

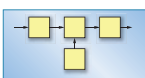
After completing this chapter, you should be able to

- Explain how a memory stores binary data
- Discuss the basic organization of a memory
- Describe the write operation
- Describe the read operation
- Describe the addressing operation
- Explain what RAMs and ROMs are

Units of Binary Data: Bits, Bytes, Nibbles, and Words

As a rule, memories store data in units that have from one to eight bits. The smallest unit of binary data, as you know, is the **bit**. In many applications, data are handled in an 8-bit unit called a **byte** or in multiples of 8-bit units. The byte can be split into two 4-bit units that are called **nibbles**. Bytes can also be grouped into words. The term **word** can have two meanings in computer terminology. In memories, it is defined as a group of bits or bytes that acts as a single entity that can be stored in one memory location. In assembly language, a word is specifically defined as two bytes.

The general definition of *word* is a complete unit of information consisting of a unit of binary data. When applied to computer instructions, a word is more specifically defined as two bytes (16 bits). As a very important part of assembly language used in computers, the DW (Define Word) directive means to define data in 16-bit units. This definition is independent of the particular microprocessor or the size of its data bus. Assembly language also allows definitions of bytes (8 bits) with the DB directive, double words (32 bits) with the DD directive, and quadwords (64 bits) with the QD directive.



SYSTEM NOTE

The Basic Memory Array

Each storage element in a memory can retain either a 1 or a 0 and is called a **cell**. Memories are made up of arrays of cells, as illustrated in Figure 4 using 64 cells as an example. Each block in the **memory array** represents one storage cell, and its location can be identified by specifying a row and a column.

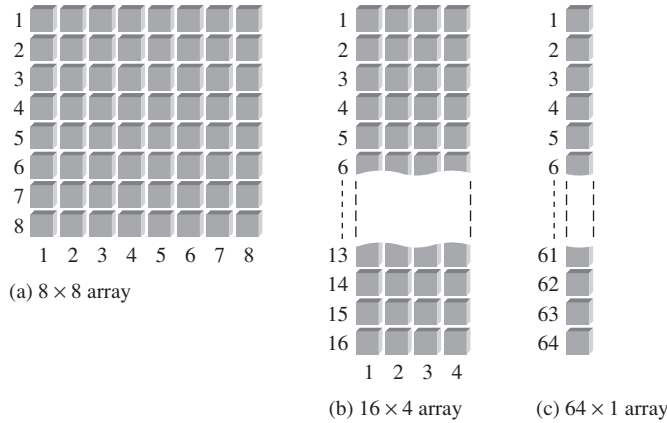


FIGURE 4 A 64-cell memory array organized in three different ways.

The 64-cell array can be organized in several ways based on units of data. Figure 4(a) shows an 8×8 array, which can be viewed as either a 64-bit memory or an 8-byte memory. Part (b) shows a 16×4 array, which is a 16-nibble memory, and part (c) shows a 64×1 array, which is a 64-bit memory. A memory is identified by the number of words it can store times the word size. For example, a $16k \times 8$ memory can store 16,384 words of eight bits each. The inconsistency here is common in memory terminology. The actual number of words is always a power of 2, which, in this case, is $2^{14} = 16,384$. However, it is common practice to state the number to the nearest thousand, in this case, 16k.

Memory Address and Capacity

A representation of a small 8×8 memory chip is shown in Figure 5(a). The location of a unit of data in a memory array is called its **address**. For example, in Figure 5(b), the address of a bit in the 2-dimensional array is specified by the row and column as shown. In Figure 5(c), the address of a byte is specified only by the row. So, as you can see, the address depends on how the memory is organized into units of data. Laptop computers have random-access memories organized in bytes. This means that the smallest group of bits that can be addressed is eight.

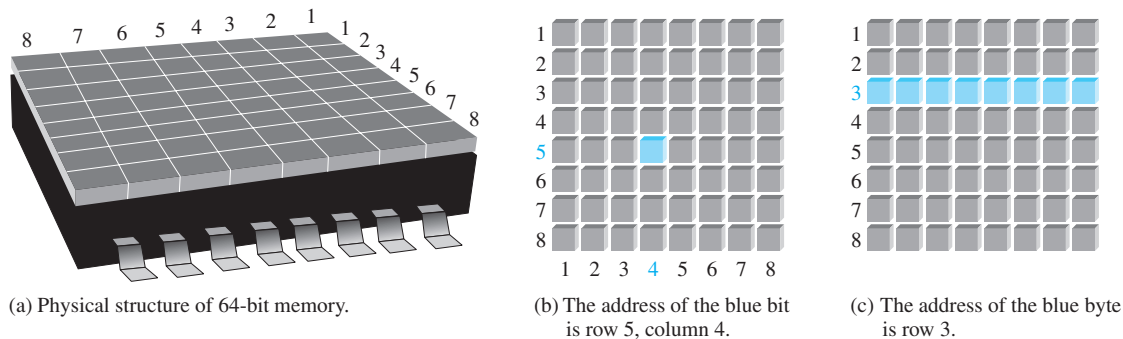


FIGURE 5 Examples of memory address in a 2-dimensional memory array.

Figure 6 illustrates the expansion of the 8×8 (64-bit) array to a 64-byte memory. The address of a byte in the array is specified by the row and column, as shown. In this case, the smallest group of bits that can be accessed is eight (1 byte). This can be viewed as a 3-dimensional array as shown in part (b).

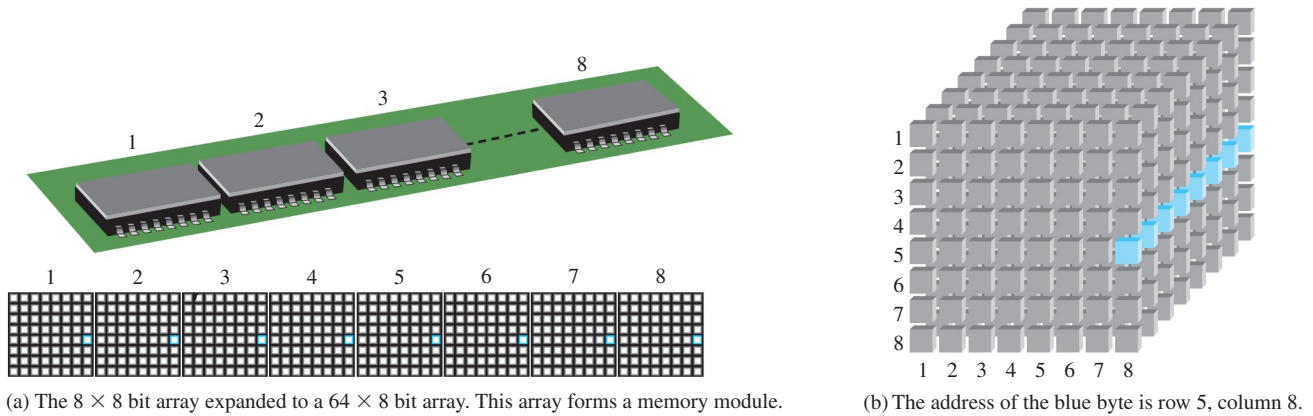


FIGURE 6 Example of memory address in an expanded (multiple) array.

The **capacity** of a memory is the total number of data units that can be stored. For example, in the bit-organized memory array in Figure 5(b), the capacity is 64 bits. In the byte-organized memory array in Figure 5(c), the capacity is 8 bytes, which is also 64 bits. In Figure 6(b), the capacity is 64 bytes. Computer memories typically have 256 MB (megabyte is one million bytes) or more of internal memory. Computers usually transfer and store data as 64-bit words, in which case all eight bits of row five in each chip in Figure 6(a) would be accessed.

MEMORY BANKS AND RANKS A **bank** is a section of memory within a single memory array (chip). A memory chip can have one or more banks. Memory banks can be used for storing frequently used information. When the section of memory is identified, the data can be accessed more quickly. A **rank** is a group of chips that make up a memory module that stores data in units such as words or bytes. These terms are illustrated in Figure 7.

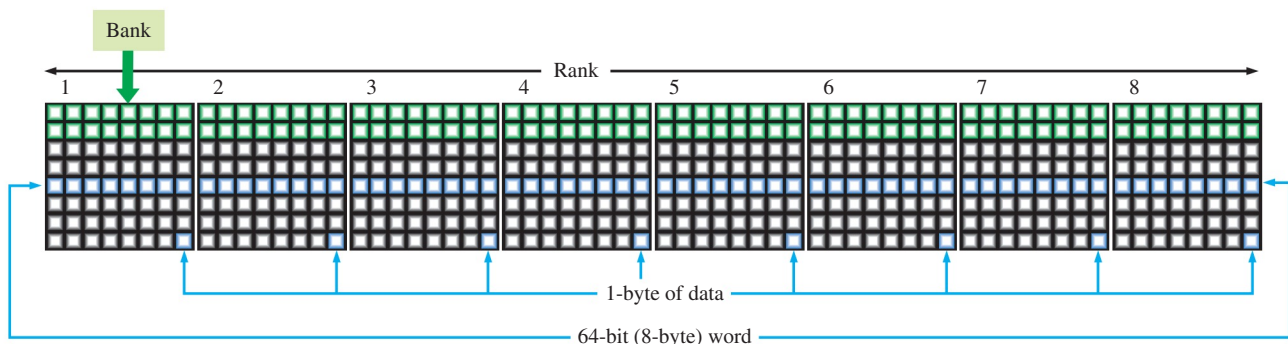


FIGURE 7 Simple illustration of memory bank and memory rank.

Basic Memory Operations

Addressing is the process of accessing a specified location in memory. Since a memory stores binary data, data must be put into the memory and data must be copied from the memory when needed. The **write** operation puts data into a specified address in the memory, and the **read** operation copies data out of a specified address in the memory. The addressing operation, which is part of both the write and the read operations, selects the specified memory address.

Data units go into the memory during a write operation and come out of the memory during a read operation on a set of lines called the *data bus*. As indicated in Figure 8, the data bus is bidirectional, which means that data can go in either direction (into the memory or out of the memory). In this case of byte-organized memories, the data bus has at least eight lines so that all eight bits in a selected address are transferred in parallel. For a write or a read operation, an address is selected by placing a binary code representing the desired address on a set of lines called the *address bus*. The address code is decoded internally, and the appropriate address is selected. In the case of the expanded (multiple) array memory in Figure 8(b) there are two decoders, one for the rows and one for the columns. The number of lines in the address bus depends on the capacity of the memory. For example, a 15-bit address code can select 32,768 locations (2^{15}) in the memory, a 16-bit address code can select 65,536 locations (2^{16}) in the memory, and so on. In personal computers a 32-bit address bus can select 4,294,967,296 locations (2^{32}), expressed as 4G.

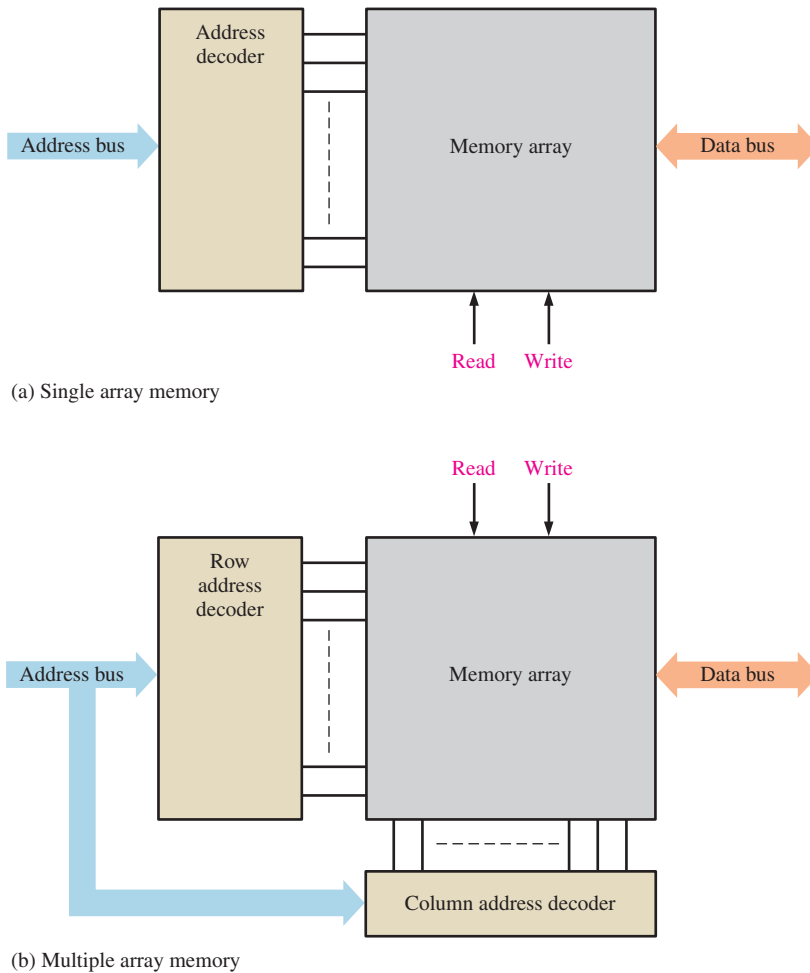
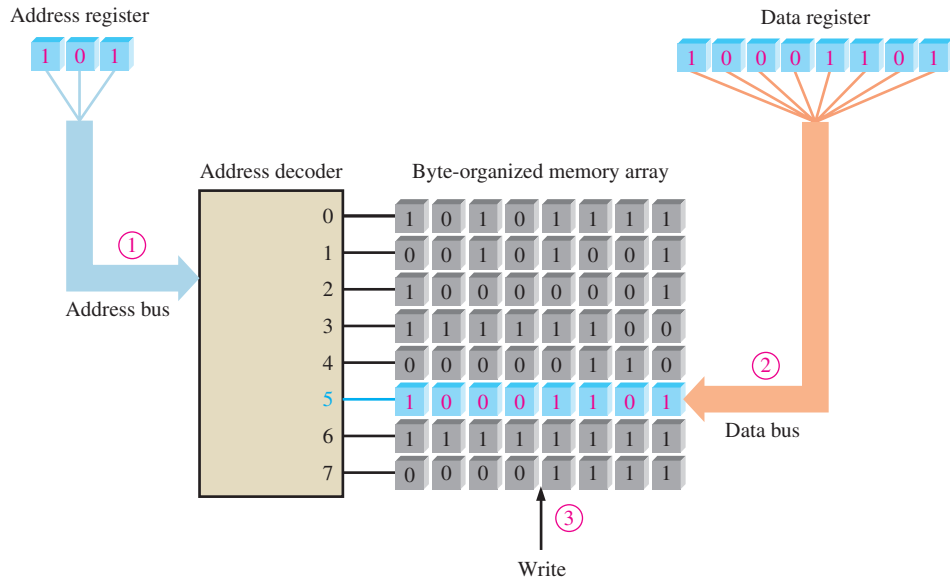


FIGURE 8 Block diagram of a single-array memory and a multiple-array memory showing address bus, address decoder(s), bidirectional data bus, and read/write inputs.

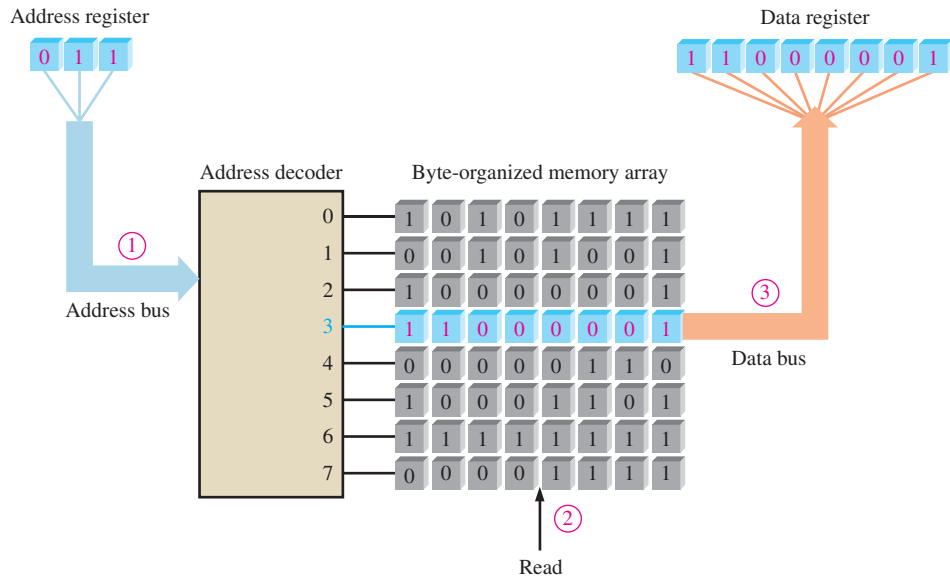
THE WRITE OPERATION A simplified write operation is illustrated in Figure 9. To store a byte of data in the memory, a code held in the address register is placed on the address bus. Once the address code is on the bus, the address decoder decodes the address and selects the specified location in the memory. The memory then gets a write command, and the data byte held in the data register is placed on the data bus and stored in the selected memory address, thus completing the write operation. When a new data byte is written into a memory address, the current data byte stored at that address is overwritten (replaced with a new data byte).



- ① Address code 101 is placed on the address bus and address 5 is selected.
- ② Data byte is placed on the data bus.
- ③ Write command causes the data byte to be stored in address 5, replacing previous data.

FIGURE 9 Illustration of the write operation.

THE READ OPERATION A simplified read operation is illustrated in Figure 10. Again, a code held in the address register is placed on the address bus. Once the address code is on the bus, the address decoder decodes the address and selects the specified location in the memory. The memory then gets a read command, and a “copy” of the data byte that is stored in the selected memory address is placed on the data bus and loaded into the data register, thus completing the read operation. When a data byte is read from a memory address, it also remains stored at that address. This is called *nondestructive read*.



- ① Address code 011 is placed on the address bus and address 3 is selected.
- ② Read command is applied.
- ③ The contents of address 3 is placed on the data bus and shifted into data register. The contents of address 3 is not erased by the read operation.

FIGURE 10 Illustration of the read operation.

RAMs and ROMs

The two major categories of semiconductor memories are the RAM and the ROM. **RAM** (random-access memory) is a type of memory in which all addresses are accessible in an equal amount of time and can be selected in any order for a read or write operation. All RAMs have both *read* and *write* capability. Because RAMs lose stored data when the power is turned off, they are **volatile** memories.

ROM (read-only memory) is a type of memory in which data are stored permanently or semipermanently. Data can be read from a ROM, but there is no write operation as in the RAM. The ROM, like the RAM, is a random-access memory but the term *RAM* traditionally means a random-access *read/write* memory. Several types of RAMs and ROMs will be covered in this chapter. Because ROMs retain stored data even if power is turned off, they are **nonvolatile** memories.

SECTION 2 CHECKUP

1. What is the smallest unit of data that can be stored in a memory?
2. What is the bit capacity of a memory that can store 256 bytes of data?
3. What is a write operation?
4. What is a read operation?
5. How is a given unit of data located in a memory?
6. Describe the difference between a RAM and a ROM.

3 THE RANDOM-ACCESS MEMORY (RAM)

A RAM is a read/write memory in which data can be written into or read from any selected address in any sequence. When a data unit is written into a given address in the RAM, the data unit previously stored at that address is replaced by the new data unit. When a data unit is read from a given address in the RAM, the data unit remains stored and is not erased by the read operation. This nondestructive read operation can be viewed as copying the content of an address while leaving the content intact. A RAM is typically used for short-term data storage because it cannot retain stored data when power is turned off.

After completing this section, you should be able to

- Name the two categories of RAM
- Explain what a SRAM is
- Describe the SRAM storage cell
- Explain the difference between an asynchronous SRAM and a synchronous burst SRAM
- Explain the purpose of a cache memory
- Explain what a DRAM is
- Describe the DRAM storage cells
- Discuss the types of DRAM
- Compare the SRAM with the DRAM

The RAM Family

The two major categories of RAM are the *static RAM* (SRAM) and the *dynamic RAM* (DRAM). **SRAMs** generally use latches as storage elements and can therefore store data indefinitely *as long as dc power is applied*. **DRAMs** use capacitors as storage elements and cannot retain data very long without the capacitors being recharged by a process called

refreshing. Both SRAMs and DRAMs will lose stored data when dc power is removed and, therefore, are classified as volatile memories.

Data can be read much faster from SRAMs than from DRAMs. However, DRAMs can store much more data than SRAMs for a given physical size and cost because the DRAM cell is much simpler, and more cells can be crammed into a given chip area than in the SRAM.

The basic types of SRAM are the *asynchronous SRAM* and the *synchronous SRAM* with a burst feature. The basic types of DRAM are the *Fast Page Mode DRAM* (FPM DRAM), the *Extended Data Out DRAM* (EDO DRAM), the *Burst EDO DRAM* (BEDO DRAM), and the *synchronous DRAM* (SDRAM). These are shown in Figure 11.

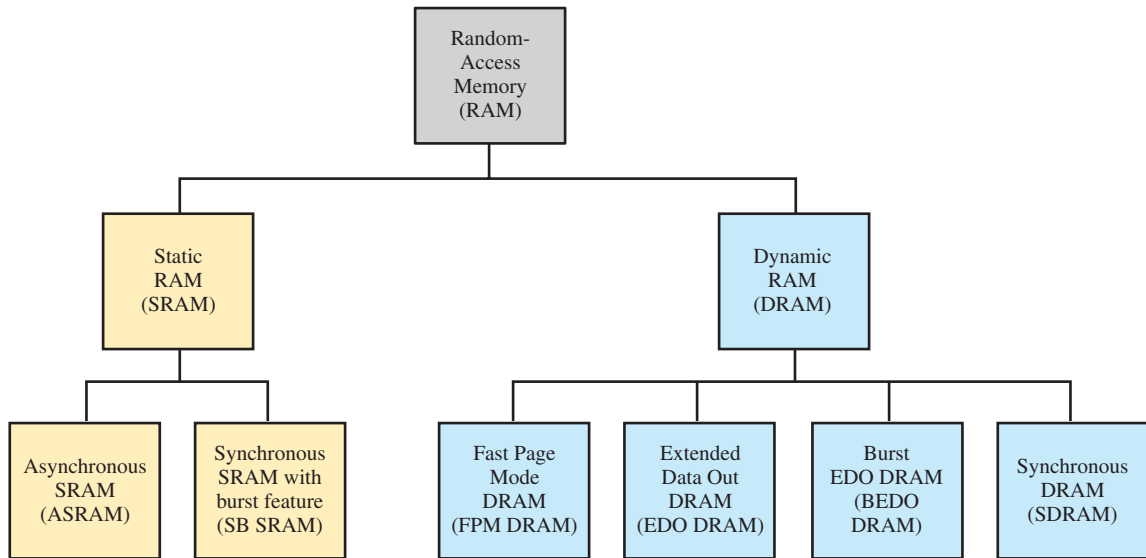


FIGURE 11 The RAM family.

Static RAMs (SRAMs)

MEMORY CELL All SRAMs are characterized by latch memory cells. As long as dc power is applied to a **static memory** cell, it can retain a 1 or 0 state indefinitely. If power is removed, the stored data bit is lost.

Figure 12 shows a basic SRAM gated D latch memory cell. The cell is selected by an active level on the Select line and a data bit (1 or 0) is written into the cell by placing it on the Data in line. A data bit is read by taking it off the Data out line.

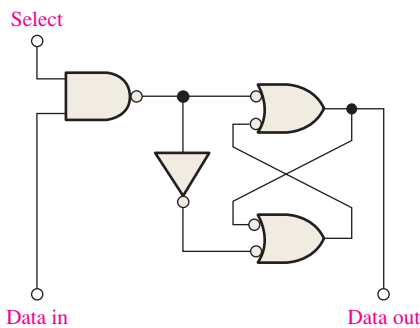


FIGURE 12 A typical SRAM gated D latch memory cell.

BASIC STATIC MEMORY CELL ARRAY The memory cells in a SRAM are organized in rows and columns, as illustrated in Figure 13 for the case of an $n \times 4$ array. All the cells in a row share the same Row Select line. Each set of Data in and Data out lines go to each cell in a given column and are connected to a single data line that serves as both an input and output (Data I/O) through the data input and data output buffers.

To write a data unit, for example a nibble, into a given row of cells in the memory array, the Row Select line is taken to its active state and four data bits are placed on the Data I/O lines. The Write line is then taken to its active state, which causes each data bit to be stored in a selected cell in the associated column. To read a data unit, the Read line is taken to its active state, which causes the four data bits stored in the selected row to appear on the Data I/O lines.

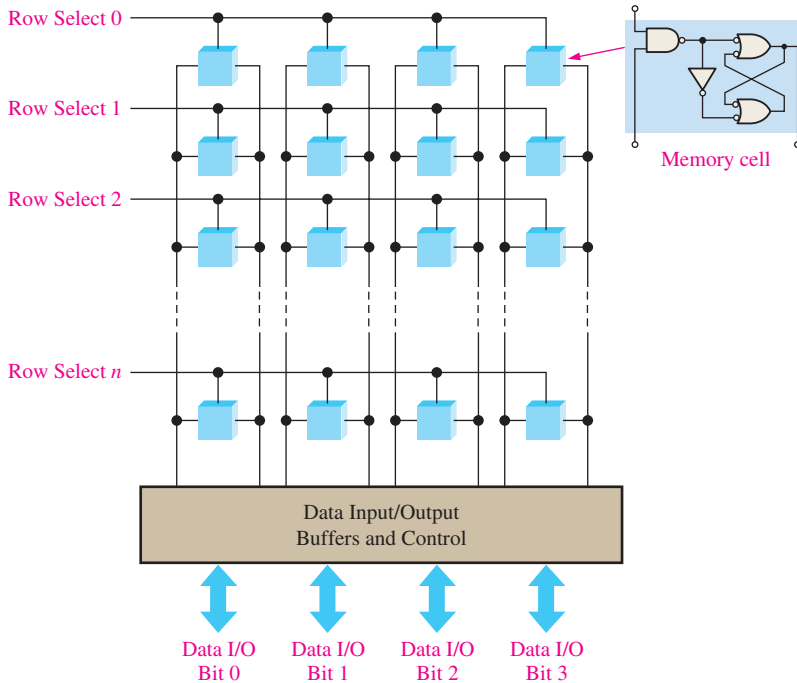


FIGURE 13 Basic SRAM array.

Basic Asynchronous SRAM Organization

An asynchronous SRAM is one in which the operation is not synchronized with a system clock. To illustrate the general organization of a SRAM, a $32k \times 8$ bit memory is used. A logic symbol for this memory is shown in Figure 14.

In the READ mode, the eight data bits that are stored in a selected address appear on the data output lines. In the WRITE mode, the eight data bits that are applied to the data input lines are stored at a selected address. The data input and data output lines (I/O_0 through I/O_7) share the same lines. During READ, they act as output lines (O_0 through O_7) and during WRITE they act as input lines (I_0 through I_7).

TRISTATE OUTPUTS AND BUSES Tristate buffers in a memory allow the data lines to act as either input or output lines and connect the memory to the data bus in a computer. These buffers have three output states: HIGH (1), LOW (0), and HIGH-Z (open). Tristate outputs are indicated on logic symbols by a small inverted triangle (∇), as shown in Figure 14, and are used for compatibility with bus structures such as those found in microprocessor-based systems.

Physically, a **bus** is one or more conductive paths that serve to interconnect two or more functional components of a system or several diverse systems. Electrically, a bus is a collection of specified voltage levels and/or current levels and signals that allow various devices to communicate and work properly together.

A microprocessor is connected to memories and input/output devices by certain bus structures. An address bus allows the microprocessor to address the memories, and a data bus provides for transfer of data between the microprocessor, the memories, and the input/output devices such as monitors, printers, keyboards, and modems. A control bus allows the microprocessor to control data transfers and timing for the various components.

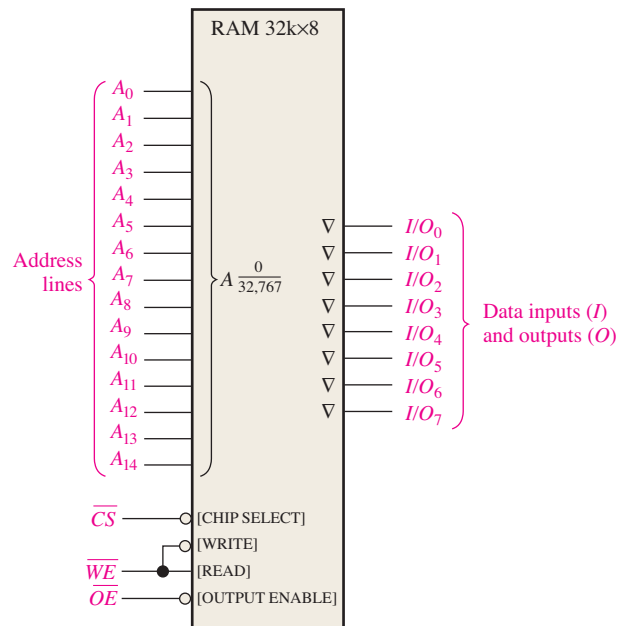


FIGURE 14 Logic diagram for an asynchronous $32k \times 8$ SRAM.

MEMORY ARRAY SRAM chips can be organized in single bits, nibbles (4 bits), bytes (8 bits), or multiple bytes (words with 16, 24, 32 bits, etc.).

Figure 15 shows the organization of a small $32k \times 8$ SRAM. The memory cell array is arranged in 256 rows and 128 columns, each with 8 bits, as shown in part (a). There are actually $2^{15} = 32,768$ addresses and each address contains 8 bits. The capacity of this example memory is 32,768 bytes (typically expressed as 32 kB). Although small by today's standards, this memory serves to introduce the basic concepts.

The SRAM in Figure 15(b) works as follows. First, the chip select, \overline{CS} , must be LOW for the memory to operate. (Other terms for chip select are *enable* or *chip enable*.) Eight of the fifteen address lines are decoded by the row decoder to select one of the 256 rows. Seven of the fifteen address lines are decoded by the column decoder to select one of the 128 8-bit columns.

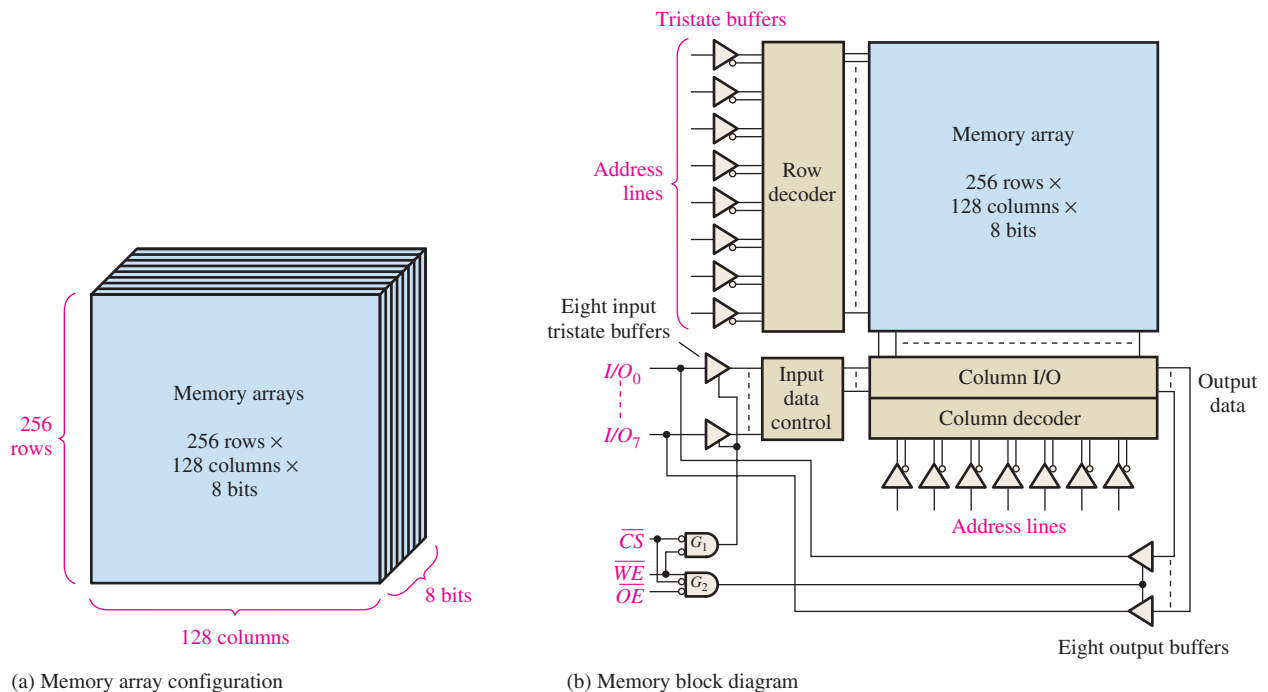
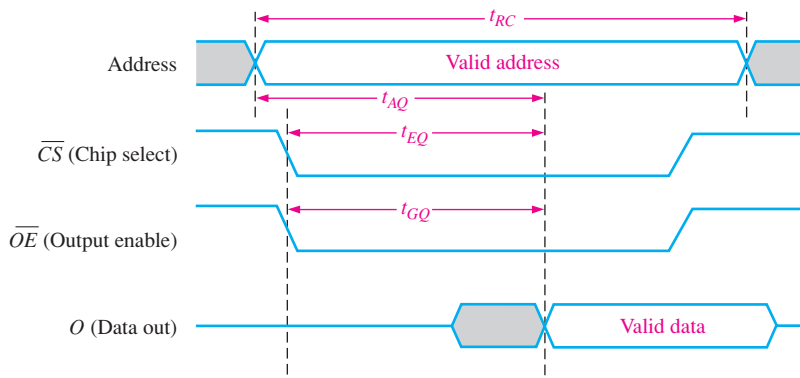


FIGURE 15 Basic organization of an asynchronous $32k \times 8$ SRAM.

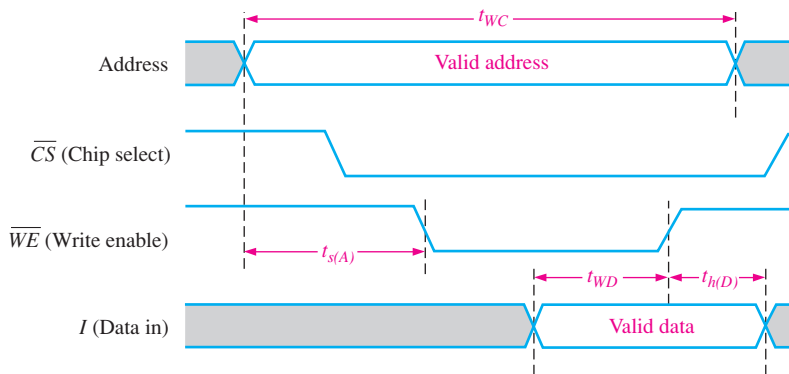
READ In the READ mode, the write enable input, \overline{WE} , is HIGH and the output enable, \overline{OE} , is LOW. The input tristate buffers are disabled by gate G_1 , and the column output tristate buffers are enabled by gate G_2 . Therefore, the eight data bits from the selected address are routed through the column I/O to the data lines (I/O_0 through I/O_7), which are acting as data output lines.

WRITE In the WRITE mode, \overline{WE} is LOW and \overline{OE} is HIGH. The input buffers are enabled by gate G_1 , and the output buffers are disabled by gate G_2 . Therefore, the eight input data bits on the data lines are routed through the input data control and the column I/O to the selected address and stored.

READ AND WRITE CYCLES Figure 16 shows typical timing diagrams for a memory read cycle and a write cycle. For the read cycle shown in part (a), a valid address code is applied to the address lines for a specified time interval called the *read cycle time*, t_{RC} . Next, the chip select (\overline{CS}) and the output enable (\overline{OE}) inputs go LOW. One time interval after the \overline{OE} input goes LOW, a valid data byte from the selected address appears on the data lines. This time interval is called the *output enable access time*, t_{GQ} . Two other access times for the read cycle are the *address access time*, t_{AQ} , measured from the beginning of a valid address to the appearance of valid data on the data lines and the *chip enable*



(a) Read cycle (\overline{WE} HIGH)



(b) Write cycle (\overline{WE} LOW)

FIGURE 16 Basic read and write cycle timing for the SRAM in Figure 15.

access time, t_{EQ} , measured from the HIGH-to-LOW transition of \overline{CS} to the appearance of valid data on the data lines.

During each read cycle, one unit of data, a byte in this case, is read from the memory.

For the write cycle shown in Figure 16(b), a valid address code is applied to the address lines for a specified time interval called the *write cycle time*, t_{WC} . Next, the chip select (\overline{CS}) and the write enable (\overline{WE}) inputs go LOW. The required time interval from the beginning of a valid address until the \overline{WE} input goes LOW is called the *address setup time*, $t_{s(A)}$. The time that the \overline{WE} input must be LOW is the write pulse width. The time that the input \overline{WE} must remain LOW after valid data are applied to the data inputs is designated t_{WD} ; the time that the valid input data must remain on the data lines after the \overline{WE} input goes HIGH is the *data hold time*, $t_{h(D)}$.

During each write cycle, one unit of data is written into the memory.

Basic Synchronous SRAM with Burst Feature

Unlike the asynchronous SRAM, a synchronous SRAM is synchronized with the system clock. For example, in a computer system, the synchronous SRAM operates with the same clock signal that operates the microprocessor so that the microprocessor and memory are synchronized for faster operation.

The fundamental concept of the synchronous feature of a SRAM can be shown with Figure 17, which is a simplified block diagram of a $32k \times 8$ memory for purposes of illustration. The synchronous SRAM is similar to the asynchronous SRAM in terms of the memory array, address decoder, and read/write and enable inputs. The basic difference is that the synchronous SRAM uses clocked registers to synchronize all inputs with the system clock. The address, the read/write input, the chip enable, and the input data are all

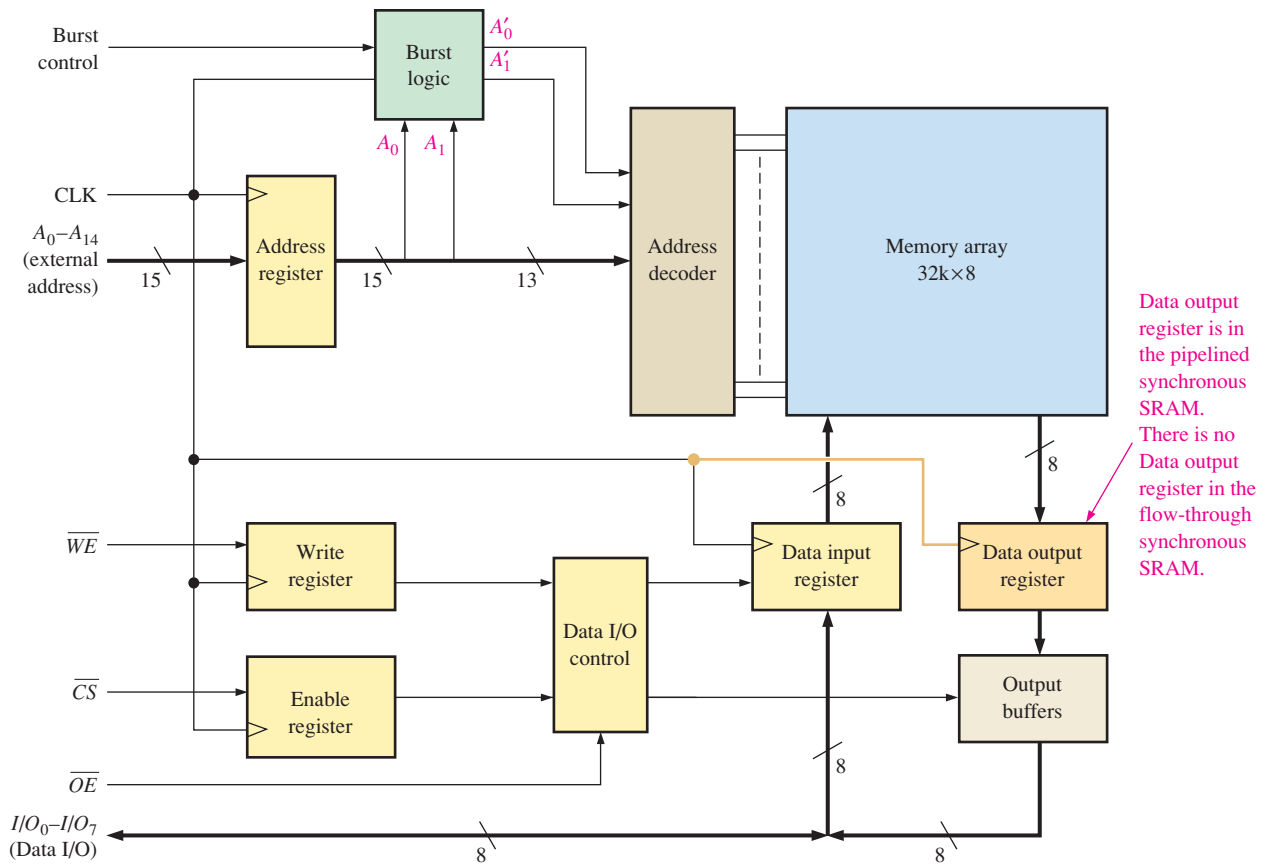
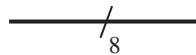


FIGURE 17 A basic block diagram of a synchronous SRAM with burst feature.

latched into their respective registers on an active clock pulse edge. Once this information is latched, the memory operation is in sync with the clock.

For the purpose of simplification, a notation for multiple parallel lines or bus lines is introduced in Figure 17, as an alternative to drawing each line separately. A set of parallel lines can be indicated by a single heavy line with a slash and the number of separate lines in the set. For example, the following notation represents a set of 8 parallel lines:



The address bits A_0 through A_{14} are latched into the Address register on the positive edge of a clock pulse. On the same clock pulse, the state of the write enable (\overline{WE}) line and chip select (\overline{CS}) are latched into the Write register and the Enable register respectively. These are one-bit registers or simply flip-flops. Also, on the same clock pulse the input data are latched into the Data input register for a Write operation, and data in a selected memory address are latched into the Data output register for a Read operation, as determined by the Data I/O control based on inputs from the Write register, Enable register, and the Output enable (\overline{OE}).

Two basic types of synchronous SRAM are the *flow-through* and the *pipelined*. The flow-through synchronous SRAM does not have a Data output register, so the output data flow asynchronously to the data I/O lines through the output buffers. The **pipelined** synchronous SRAM has a Data output register, as shown in Figure 17, so the output data are synchronously placed on the data I/O lines.

THE BURST FEATURE As shown in Figure 17, synchronous SRAMs normally have an address burst feature, which allows the memory to read or write up to four sequential locations using a single address. When an external address is latched in the address register, the two lowest-order address bits, A_0 and A_1 , are applied to the burst

logic. This produces a sequence of four internal addresses by adding 00, 01, 10, and 11 to the two lowest-order address bits on successive clock pulses. The sequence always begins with the base address, which is the external address held in the address register.

The address burst logic in a typical synchronous SRAM consists of a binary counter and exclusive-OR gates, as shown in Figure 18. For 2-bit burst logic, the internal burst address sequence is formed by the base address bits A_2 – A_{14} plus the two burst address bits A'_1 and A'_0 .

To begin the burst sequence, the counter is in its 00 state and the two lowest-order address bits are applied to the inputs of the XOR gates. Assuming that A_0 and A_1 are both 0, the internal address sequence in terms of its two lowest-order bits is 00, 01, 10, and 11.

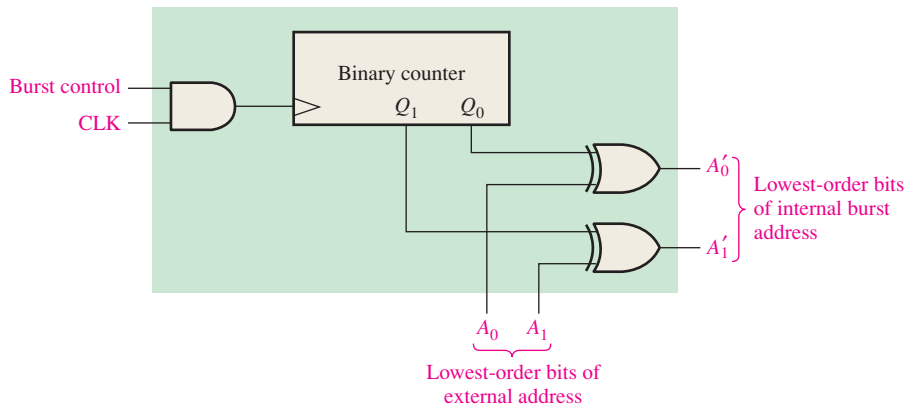


FIGURE 18 Address burst logic.

Cache Memory

One of the major applications of SRAMs is in cache memories in computers. **Cache memory** is a relatively small, high-speed memory that stores the most recently used instructions or data from the larger but slower main memory. Cache memory can also use dynamic RAM (DRAM), which is covered next. Typically, SRAM is several times faster than DRAM. Overall, a cache memory gets stored information to the microprocessor much faster than if only high-capacity DRAM is used. Cache memory is basically a cost-effective method of improving system performance without having to resort to the expense of making all of the memory faster.

The concept of cache memory is based on the idea that computer programs tend to get instructions or data from one area of main memory before moving to another area. Basically, the cache controller “guesses” which area of the slow dynamic memory the CPU (central-processing unit) will need next and moves it to the cache memory so that it is ready when needed. If the cache controller guesses right, the data are immediately available to the microprocessor. If the cache controller guesses wrong, the CPU must go to the main memory and wait much longer for the correct instructions or data. Fortunately, the cache controller is right most of the time.

CACHE ANALOGY There are many analogies that can be used to describe a cache memory, but comparing it to a home refrigerator is perhaps the most effective. A home refrigerator can be thought of as a “cache” for certain food items while the supermarket is the main memory where all foods are kept. Each time you want something to eat or drink, you can go to the refrigerator (cache) first to see if the item you want is there. If it is, you save a lot of time. If it is not there, then you have to spend extra time to get it from the supermarket (main memory).

L1 AND L2 CACHES A first-level cache (L1 cache) is usually integrated into the processor chip and has a very limited storage capacity. L1 cache is also known as *primary cache*. A second-level cache (L2 cache) is a separate memory chip or set of chips external

to the processor and usually has a larger storage capacity than an L1 cache. L2 cache is also known as *secondary cache*. Some systems may have higher-level caches (L3, L4, etc.), but L1 and L2 are the most common. Also, some systems use a disk cache to enhance the performance of the hard disk because DRAM, although much slower than SRAM, is much faster than the hard disk drive. Figure 19 illustrates L1 and L2 cache memories in a computer system.

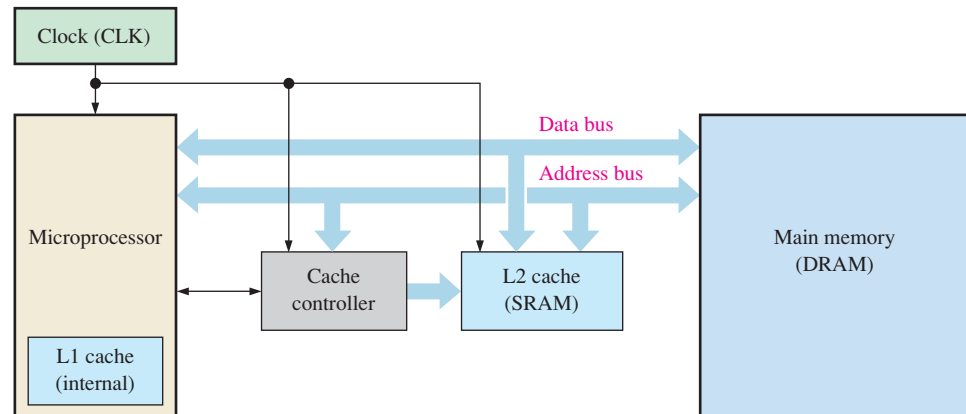


FIGURE 19 Block diagram showing L1 and L2 cache memories in a computer system.

Dynamic RAM (DRAM) Memory Cells

Dynamic memory cells store a data bit in a small capacitor rather than in a latch. The advantage of this type of cell is that it is very simple, thus allowing very large memory arrays to be constructed on a chip at a lower cost per bit. The disadvantage is that the storage capacitor cannot hold its charge over an extended period of time and will lose the stored data bit unless its charge is refreshed periodically. To refresh requires additional memory circuitry and complicates the operation of the DRAM. Figure 20 shows a typical DRAM cell consisting of a single MOS transistor (MOSFET) and a capacitor.

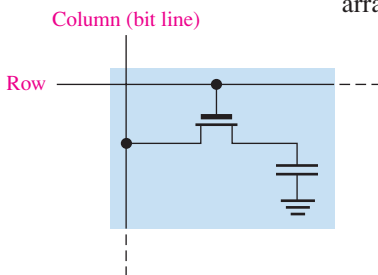


FIGURE 20 A MOS DRAM cell.

In this type of cell, the transistor acts as a switch. The basic simplified operation is illustrated in Figure 21 and is as follows. A LOW on the R/\bar{W} line (WRITE mode) enables the tristate input buffer and disables the output buffer. For a 1 to be written into the cell, the D_{IN} line must be HIGH, and the transistor must be turned on by a HIGH on the row line. The transistor acts as a closed switch connecting the capacitor to the bit line. This connection allows the capacitor to charge to a positive voltage, as shown in Figure 21(a). When a 0 is to be stored, a LOW is applied to the D_{IN} line. If the capacitor is storing a 0, it remains uncharged, or if it is storing a 1, it discharges as indicated in Figure 21(b). When the row line is taken back LOW, the transistor turns off and disconnects the capacitor from the bit line, thus “trapping” the charge (1 or 0) on the capacitor.

To read from the cell, the R/\bar{W} (Read/ \bar{W} rite) line is HIGH, enabling the output buffer and disabling the input buffer. When the row line is taken HIGH, the transistor turns on and connects the capacitor to the bit line and thus to the output buffer (sense amplifier), so the data bit appears on the data-output line (D_{OUT}). This process is illustrated in Figure 21(c).

For refreshing the memory cell, the R/\bar{W} line is HIGH, the row line is HIGH, and the refresh line is HIGH. The transistor turns on, connecting the capacitor to the bit line. The output buffer is enabled, and the stored data bit is applied to the input of the refresh buffer, which is enabled by the HIGH on the refresh input. This produces a voltage on the bit line corresponding to the stored bit, thus replenishing the capacitor. This is illustrated in Figure 21(d).

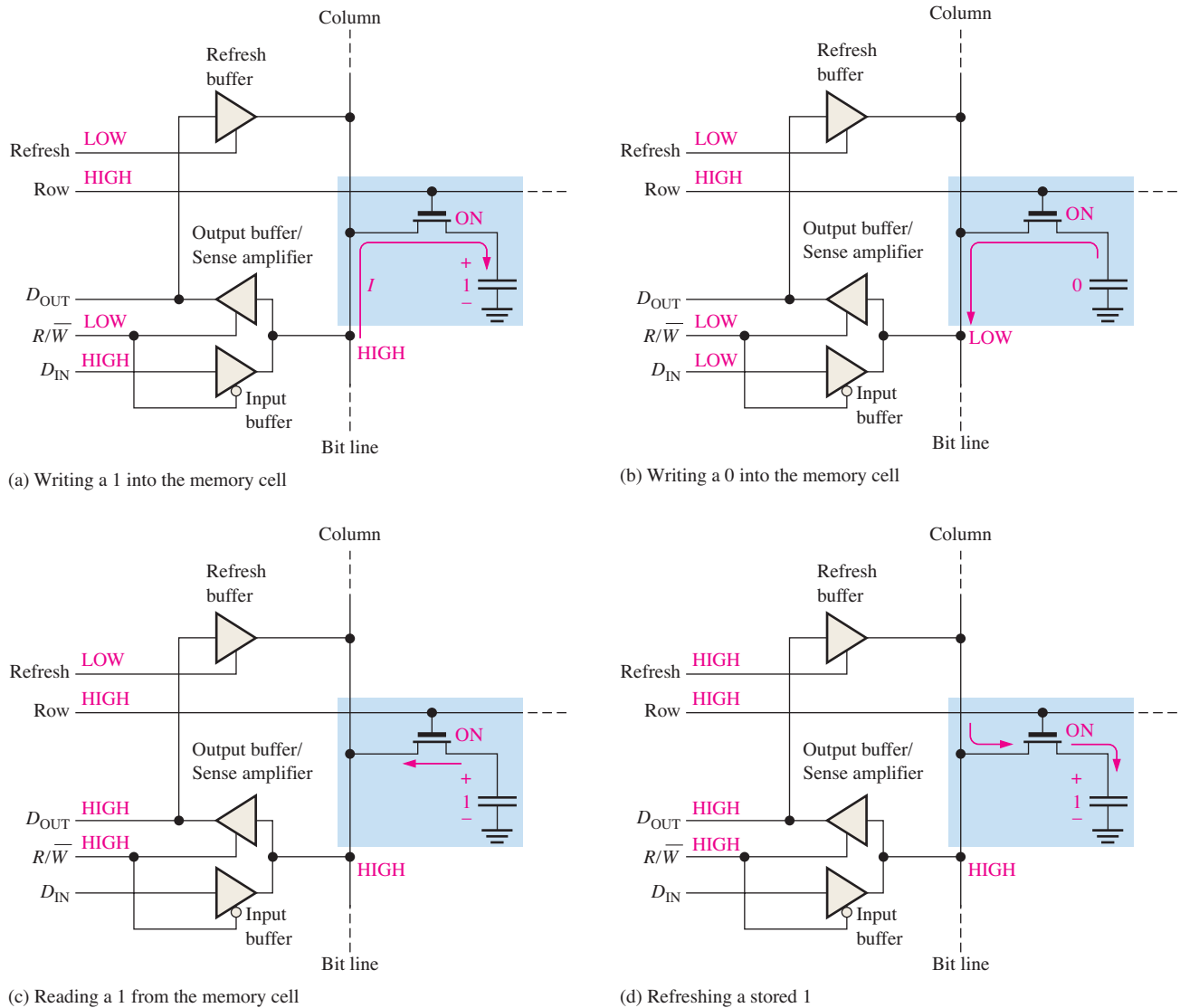


FIGURE 21 Basic operation of a DRAM cell.

Basic DRAM Organization

The major application of DRAMs is in the main memory of computers. The difference between DRAMs and SRAMs is the type of memory cell. As you have seen, the DRAM memory cell consists of one transistor and a capacitor and is much simpler than the SRAM cell. This allows much greater densities in DRAMs and results in greater bit capacities for a given chip area, although much slower access time.

Again, because charge stored in a capacitor will leak off, the DRAM cell requires a frequent refresh operation to preserve the stored data bit. This requirement results in more complex circuitry than in a SRAM. Several features common to most DRAMs are now discussed, using a generic $1\text{M} \times 1$ bit DRAM as an example.

ADDRESS MULTIPLEXING DRAMs use a technique called *address multiplexing* to reduce the number of address lines. Figure 22 shows the block diagram of a 1,048,576-bit (1 Mb) DRAM with a $1\text{M} \times 1$ organization. We will focus on the blue blocks to illustrate address multiplexing. The green blocks represent the refresh logic.

The ten address lines are time multiplexed at the beginning of a memory cycle by the row address select (\overline{RAS}) and the column address select (\overline{CAS}) into two separate 10-bit address fields. First, the 10-bit row address is latched into the row address register. Next, the 10-bit column address is latched into the column address register. The row address and

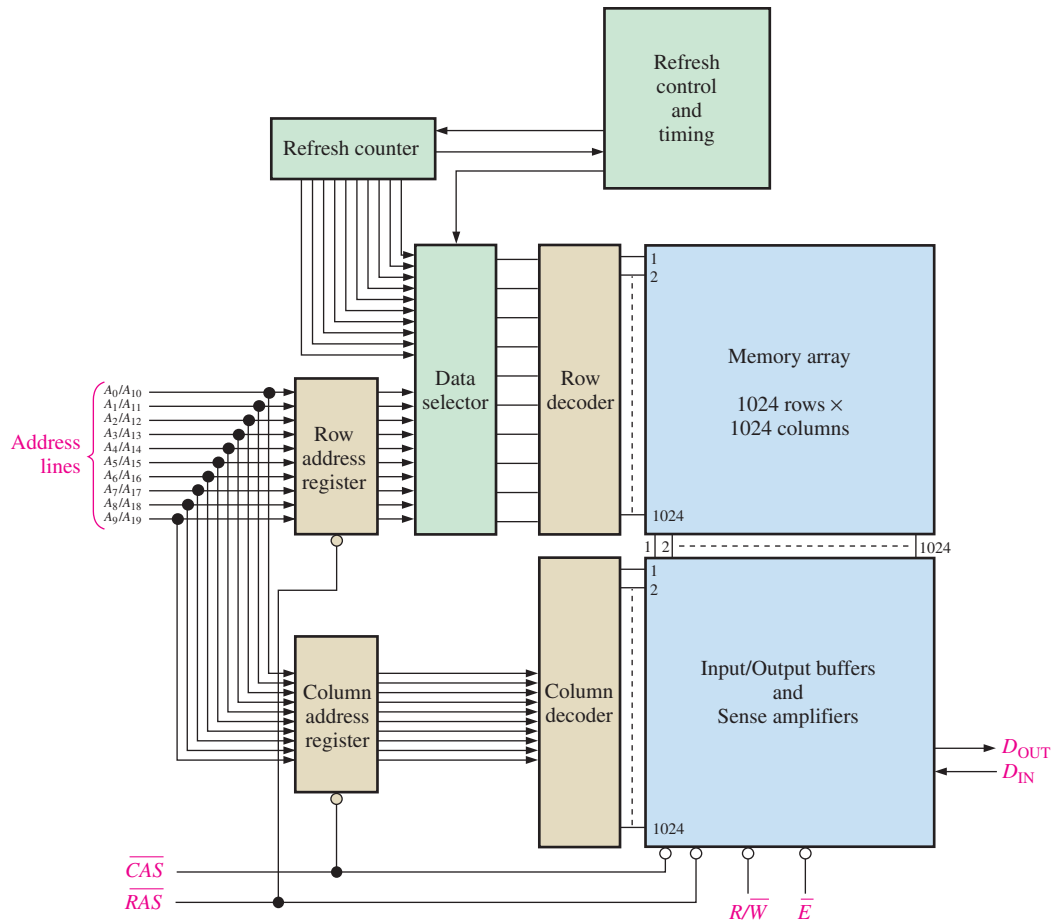


FIGURE 22 Simplified block diagram of a 1M × 1 DRAM.

the column address are decoded to select one of the 1,048,576 addresses ($2^{20} = 1,048,576$) in the memory array. The basic timing for the address multiplexing operation is shown in Figure 23.

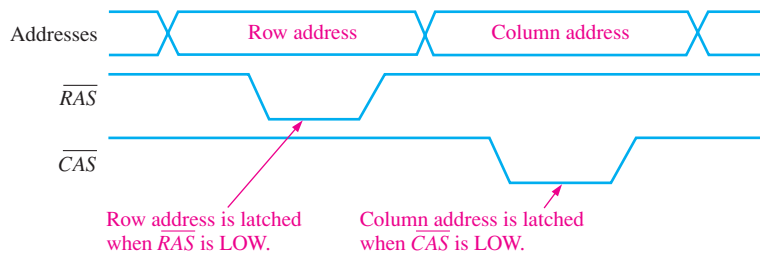


FIGURE 23 Basic timing for address multiplexing.

READ AND WRITE CYCLES At the beginning of each read or write memory cycle, \overline{RAS} and \overline{CAS} go active (LOW) to multiplex the row and column addresses into the registers and decoders. For a read cycle, the R/\overline{W} input is HIGH. For a write cycle, the R/\overline{W} input is LOW. This is illustrated in Figure 24.

FAST PAGE MODE In the normal read or write cycle described previously, the row address for a particular memory location is first loaded by an active-LOW \overline{RAS} and then the column address for that location is loaded by an active-LOW \overline{CAS} . The next location is selected by another \overline{RAS} followed by a \overline{CAS} , and so on.

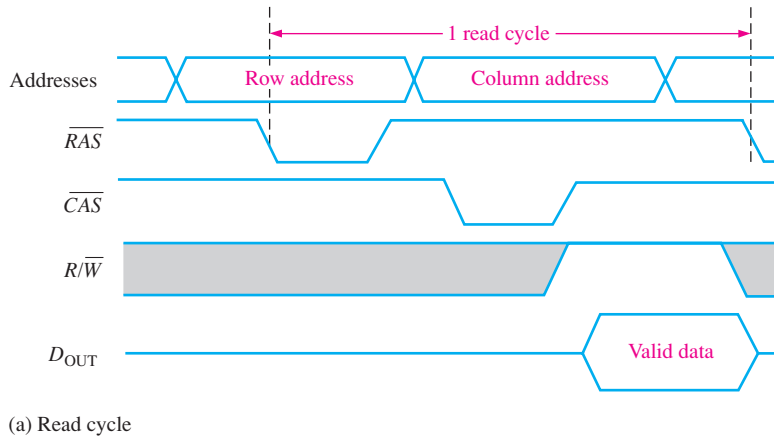
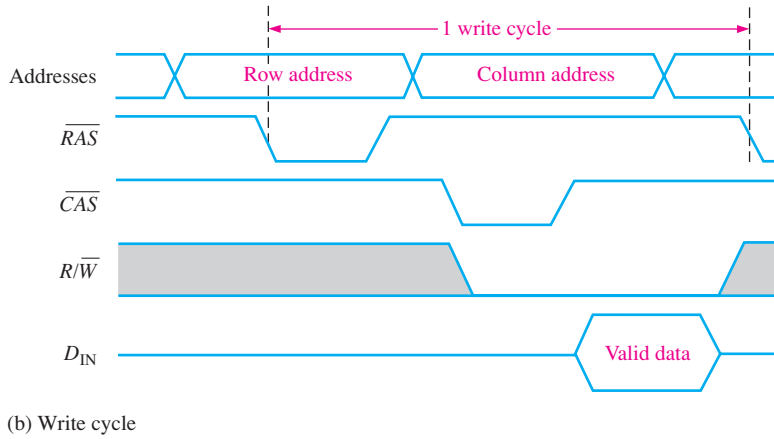


FIGURE 24 Normal read and write cycle timing.



A “page” is a section of memory available at a single row address and consists of all the columns in a row. Fast page mode allows fast successive read or write operations at each column address in a selected row. A row address is first loaded by RAS going LOW and remaining LOW while CAS is toggled between HIGH and LOW. A single row address is selected and remains selected while RAS is active. Each successive CAS selects another column in the selected row. So, after a fast page mode cycle, all of the addresses in the selected row have been read from or written into, depending on R/\bar{W} . For example, a fast page mode cycle for the DRAM in Figure 22 requires CAS to go active 1024 times for each row selected by RAS .

Fast page mode operation for read is illustrated by the timing diagram in Figure 25. When CAS goes to its nonasserted state (HIGH), it disables the data outputs. Therefore, the transition of CAS to HIGH must occur only after valid data are latched by the external system.

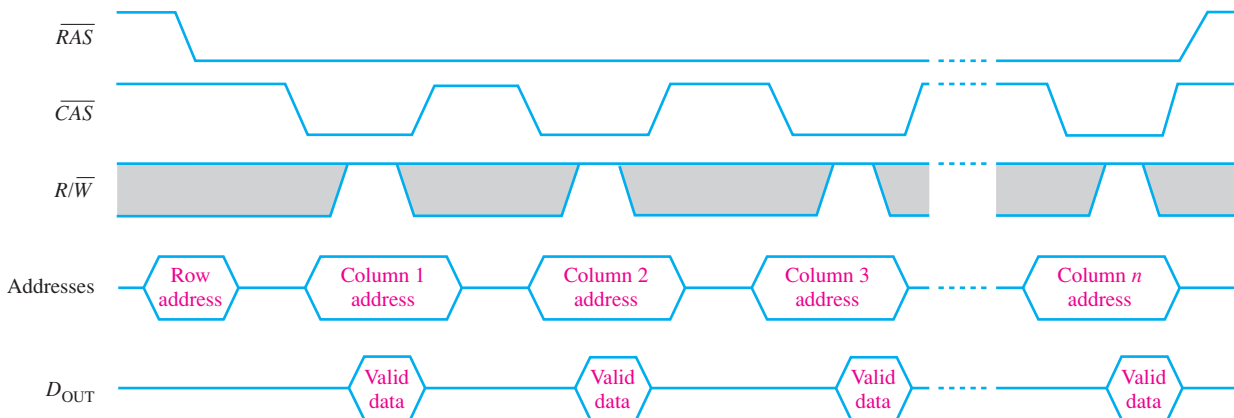


FIGURE 25 Fast page mode timing for a read operation.

REFRESH CYCLES As you know, DRAMs are based on capacitor charge storage for each bit in the memory array. This charge degrades (leaks off) with time and temperature, so each bit must be periodically refreshed (recharged) to maintain the correct bit state. Typically, a DRAM must be refreshed every 8 ms to 16 ms, although for some devices the refresh period can exceed 100 ms.

A read operation automatically refreshes all the addresses in the selected row. However, in typical applications, you cannot always predict how often there will be a read cycle, and so you cannot depend on a read cycle to occur frequently enough to prevent data loss. Therefore, special refresh cycles must be implemented in DRAM systems.

Burst refresh and *distributed refresh* are the two basic refresh modes for refresh operations. In burst refresh, all rows in the memory array are refreshed consecutively each refresh period. For a memory with a refresh period of 8 ms, a burst refresh of all rows occurs once every 8 ms. The normal read and write operations are suspended during a burst refresh cycle. In distributed refresh, each row is refreshed at intervals interspersed between normal read or write cycles. For example, the memory in Figure 22 has 1024 rows. As an example, for an 8 ms refresh period, each row must be refreshed every $8 \text{ ms}/1024 = 7.8 \mu\text{s}$ when distributed refresh is used.

The two types of refresh operations are *RAS only refresh* and *CAS before RAS refresh*. *RAS-only refresh* consists of a $\overline{\text{RAS}}$ transition to the LOW (active) state, which latches the address of the row to be refreshed while $\overline{\text{CAS}}$ remains HIGH (inactive) throughout the cycle. An external counter is used to provide the row addresses for this type of operation.

The *CAS before RAS refresh* is initiated by $\overline{\text{CAS}}$ going LOW before $\overline{\text{RAS}}$ goes LOW. This sequence activates an internal refresh counter that generates the row address to be refreshed. This address is switched by the data selector into the row decoder.

Types of DRAMs

Now that you have learned the basic concept of a DRAM, let's briefly look at some major types. These are the *Fast Page Mode (FPM) DRAM*, the *Extended Data Out (EDO) DRAM*, the *Burst Extended Data Out (BEDO) DRAM*, the *Synchronous (S) DRAM*, and the *Double Data Note (DDR) SDRAM*.

FPM DRAM Fast page mode operation was described earlier. This type of DRAM traditionally has been the most common and has been the type used in computers until the development of the EDO DRAM. Recall that a page in memory is all of the column addresses contained within one row address.

The idea of the **FPM DRAM** is based on the probability that the next several memory addresses to be accessed are in the same row (on the same page). Fortunately, this happens a large percentage of the time. FPM saves time over pure random accessing because in FPM the row address is specified only once for access to several successive column addresses whereas for pure random accessing, a row address is specified for each column address.

Recall that in a fast page mode read operation, the $\overline{\text{CAS}}$ signal has to wait until the valid data from a given address are accepted (latched) by the external system (CPU) before it can go to its nonasserted state. When $\overline{\text{CAS}}$ goes to its nonasserted state, the data outputs are disabled. This means that the next column address cannot occur until after the data from the current column address are transferred to the CPU. This limits the rate at which the columns within a page can be addressed.

EDO DRAM The Extended Data Out DRAM, sometimes called *hyper page mode DRAM*, is similar to the FPM DRAM. The key difference is that the $\overline{\text{CAS}}$ signal in the **EDO DRAM** does not disable the output data when it goes to its nonasserted state because the valid data from the current address can be held until $\overline{\text{CAS}}$ is asserted again. This means that the next column address can be accessed before the external system accepts the current valid data. The idea is to speed up the access time.

BEDO DRAM The Burst Extended Data Out DRAM is an EDO DRAM with address burst capability. Recall from the discussion of the synchronous burst SRAM that the address

burst feature allows up to four addresses to be internally generated from a single external address, which saves some access time. This same concept applies to the **BEDO DRAM**.

SDRAM Faster DRAMs are needed to keep up with the ever-increasing speed of microprocessors. The Synchronous DRAM is one way to accomplish this. Like the synchronous SRAM discussed earlier, the operation of the **SDRAM** is synchronized with the system clock, which also runs the microprocessor in a computer system. The same basic ideas described in relation to the synchronous burst SRAM, also apply to the SDRAM.

This synchronized operation makes the SDRAM totally different from the other asynchronous DRAM types. With asynchronous memories, the microprocessor must wait for the DRAM to complete its internal operations. However, with synchronous operation, the DRAM latches addresses, data, and control information from the processor under control of the system clock. This allows the processor to handle other tasks while the memory read or write operations are in progress, rather than having to wait for the memory to do its thing as is the case in asynchronous systems.

DDR SDRAM **DDR** stands for double data rate. A DDR SDRAM is clocked on both edges of a clock pulse, whereas a SDRAM is clocked on only one edge. Because of the double clocking, a DDR SDRAM is theoretically twice as fast as an SDRAM. Sometimes the SDRAM is referred to as an SDR SDRAM (single data rate SDRAM) for contrast with the DDR SDRAM.

SECTION 3 CHECKUP

1. List two types of SRAM.
2. What is a cache?
3. Explain how SRAMs and DRAMs differ.
4. Describe the refresh operation in a DRAM.
5. List four types of DRAM.

4 THE READ-ONLY MEMORY (ROM)

A ROM contains permanently or semipermanently stored data, which can be read from the memory but either cannot be changed at all or cannot be changed without specialized equipment. A ROM stores data that are used repeatedly in system applications, such as tables, conversions, or programmed instructions for system initialization and operation. ROMs retain stored data when the power is off and are therefore nonvolatile memories.

After completing this section, you should be able to

- List the types of ROMs
- Describe a basic mask ROM storage cell
- Explain how data are read from a ROM
- Discuss internal organization of a typical ROM

The ROM Family

Figure 26 shows how semiconductor ROMs are categorized. The mask ROM is the type in which the data are permanently stored in the memory during the manufacturing process. The **PROM**, or programmable ROM, is the type in which the data are electrically stored by

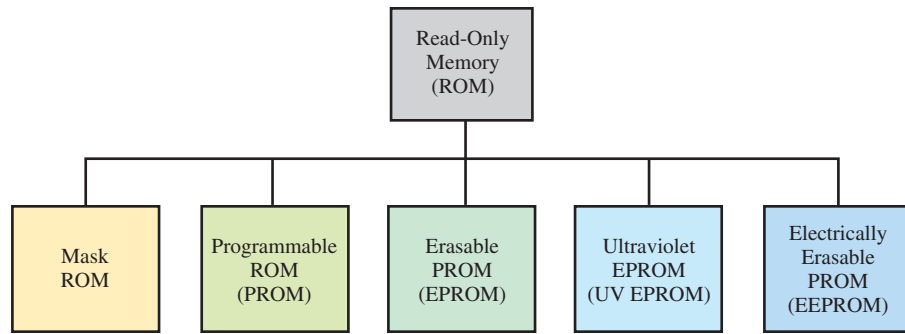


FIGURE 26 The ROM family.

the user with the aid of specialized equipment. Both the mask ROM and the PROM can be of either MOS or bipolar technology. The **EPROM**, or erasable PROM, is strictly a MOS device. The **UV EPROM** is electrically programmable by the user, but the stored data must be erased by exposure to ultraviolet light over a period of several minutes. The electrically erasable PROM (**EEPROM** or **E²PROM**) can be erased in a few milliseconds.

The Mask ROM

The mask ROM is usually referred to simply as a ROM. It is permanently programmed during the manufacturing process to provide widely used standard functions, such as popular conversions, or to provide user-specified functions. Once the memory is programmed, it cannot be changed. Most IC ROMs utilize the presence or absence of a transistor connection at a row/column junction to represent a 1 or a 0.

Figure 27 shows MOS ROM cells. The presence of a connection from a row line to the gate of a transistor represents a 1 at that location because when the row line is taken HIGH, all transistors with a gate connection to that row line turn on and connect the HIGH (1) to the associated column lines. At row/column junctions where there are no gate connections, the column lines remain LOW (0) when the row is addressed.

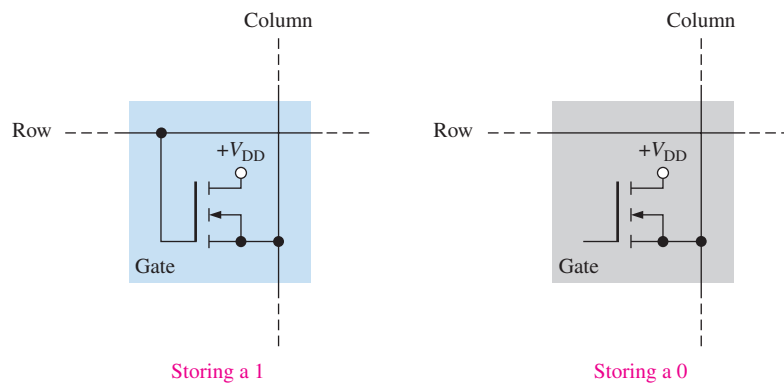


FIGURE 27 ROM cells.

To illustrate the ROM concept, Figure 28 shows a small, simplified ROM array. The blue squares represent stored 1s, and the gray squares represent stored 0s. The basic read operation is as follows. When a binary address code is applied to the address input lines, the corresponding row line goes HIGH. This HIGH is connected to the column lines through the transistors at each junction (cell) where a 1 is stored. At each cell where a 0 is stored, the column line stays LOW because of a terminating resistor. The column lines form the data output. The eight data bits stored in the selected row appear on the output lines.

As you can see, the example ROM in Figure 28 is organized into 16 addresses, each of which stores 8 data bits. Thus, it is a 16 × 8 (16-by-8) ROM, and its total capacity is 128 bits or 16 bytes. ROMs can be used as look-up tables (LUTs) for code conversions and logic function generation.

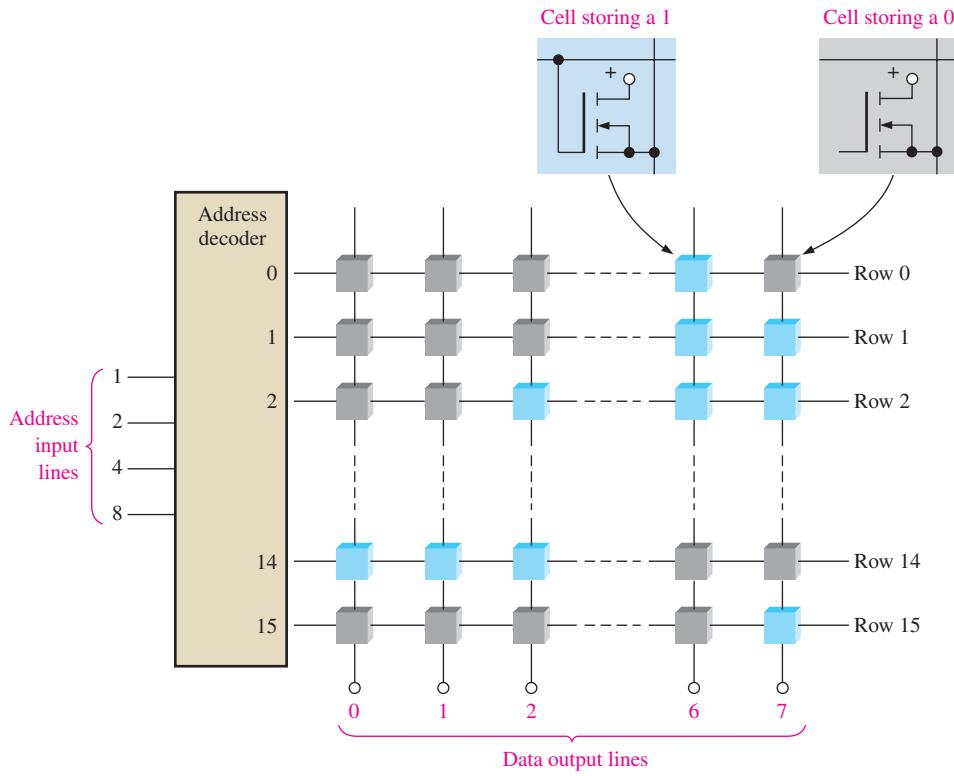


FIGURE 28 A representation of a 16×8 -bit ROM array.

EXAMPLE 1

Show a basic ROM, similar to the one in Figure 28, programmed for a 4-bit binary-to-Gray conversion.

SOLUTION

Table 1 is developed for use in programming the ROM.

TABLE 1							
BINARY				GRAY			
B_3	B_2	B_1	B_0	G_3	G_2	G_1	G_0
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	1
0	0	1	0	0	0	1	1
0	0	1	1	0	0	1	0
0	1	0	0	0	1	1	0
0	1	0	1	0	1	1	1
0	1	1	0	0	1	0	1
0	1	1	1	0	1	0	0
1	0	0	0	1	1	0	0
1	0	0	1	1	1	0	1
1	0	1	0	1	1	1	1
1	0	1	1	1	1	1	0
1	1	0	0	1	0	1	0
1	1	0	1	1	0	1	1
1	1	1	0	1	0	0	1
1	1	1	1	1	0	0	0

The resulting 16×4 ROM array is shown in Figure 29. You can see that a binary code on the address input lines produces the corresponding Gray code on the output lines (columns). For example, when the binary number 0110 is applied to the address input lines, address 6, which stores the Gray code 0101, is selected.

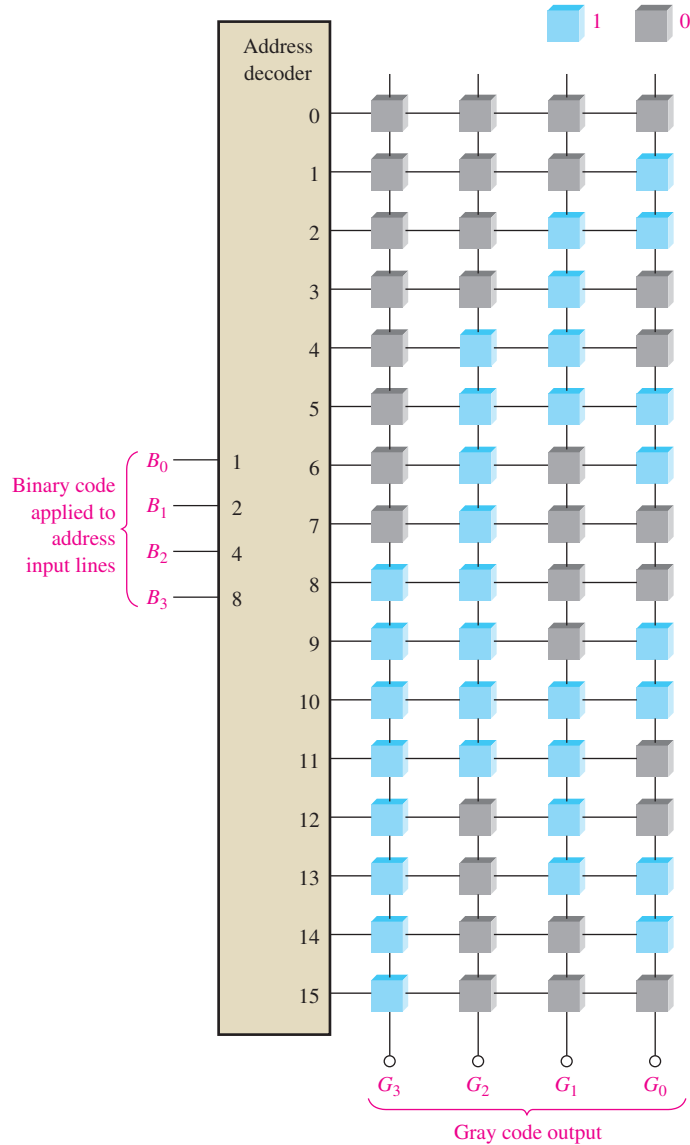


FIGURE 29 Representation of a ROM programmed as a binary-to-Gray code converter.

RELATED PROBLEM*

Using Figure 29, determine the Gray code output when a binary code of 1011 is applied to the address input lines.

*Answers are at the end of the chapter.

INTERNAL ROM ORGANIZATION Most IC ROMs have a more complex internal organization than that in the basic simplified example just presented. To illustrate how an IC ROM is structured, let's use a 1024-bit device with a 256×4 organization. The logic symbol is shown in Figure 30. When any one of 256 binary codes (eight bits)

is applied to the address lines, four data bits appear on the outputs if the chip select inputs are LOW. (256 addresses require eight address lines.)

Although the 256×4 organization of this device implies that there are 256 rows and 4 columns in the memory array, this is not actually the case. The memory cell array is actually a 32×32 matrix (32 rows and 32 columns), as shown in the block diagram in Figure 31.

The ROM in Figure 31 works as follows. Five of the eight address lines (A_0 through A_4) are decoded by the row decoder (often called the Y decoder) to select one of the 32 rows. Three of the eight address lines (A_5 through A_7) are decoded by the column decoder (often called the X decoder) to select four of the 32 columns. Actually, the column decoder consists of four 1-of-8 decoders (data selectors), as shown in Figure 31.

The result of this structure is that when an 8-bit address code (A_0 through A_7) is applied, a 4-bit data word appears on the data outputs when the chip select lines (\overline{CS}_0 and \overline{CS}_1) are LOW to enable the output buffers.

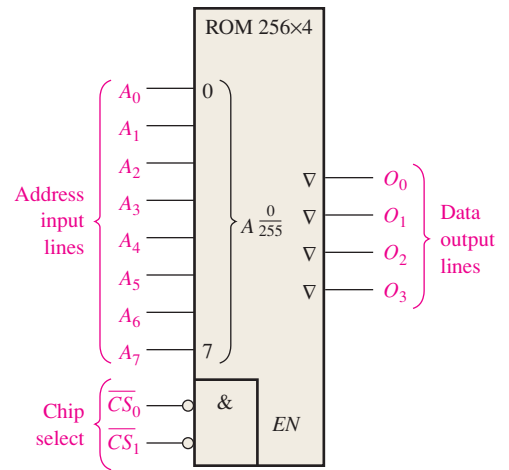


FIGURE 30 A 256×4 ROM logic symbol. The $A \frac{0}{255}$ designator means that the 8-bit address code selects addresses 0 through 255.

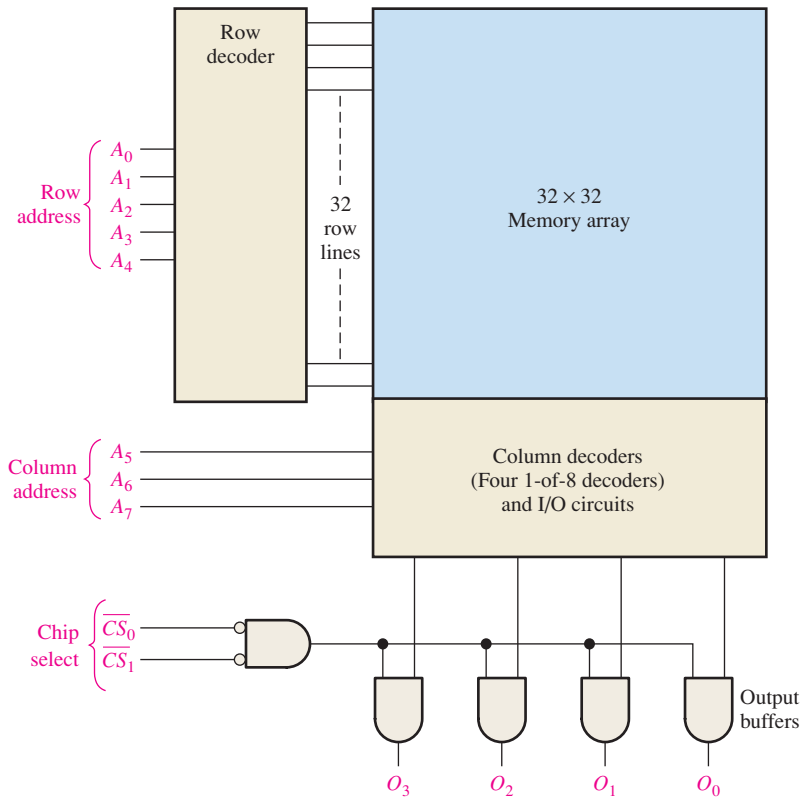
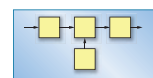


FIGURE 31 A 1024-bit ROM with a 256×4 organization based on a 32×32 array.

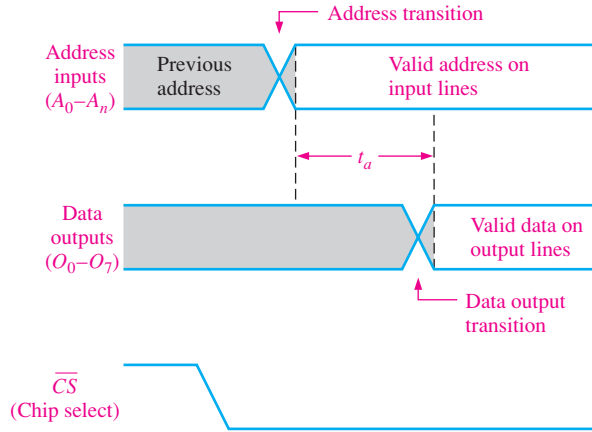
ROM is used in a computer to store the BIOS (Basic Input/Output System). These are programs that are used to perform fundamental supervisory and support functions for the computer. For example, BIOS programs stored in the ROM control certain video monitor functions, provide for disk formatting, scan the keyboard for inputs, and control certain printer functions.

SYSTEM NOTE



ROM ACCESS TIME A typical timing diagram that illustrates ROM access time is shown in Figure 32. The **access time**, t_a , of a ROM is the time from the application of a valid address code on the input lines until the appearance of valid output data. Access time can also be measured from the activation of the chip select (\overline{CS}) input to the occurrence of valid output data when a valid address is already on the input lines.

FIGURE 32 ROM access time (t_a) from address change to data output with chip select already active.



SECTION 4 CHECKUP

1. What is the bit storage capacity of a ROM with a 512×8 organization?
2. List the types of read-only memories.
3. How many address bits are required for a 2048-bit memory organized as a 256×8 memory?

5 PROGRAMMABLE ROMS

Programmable ROMs (PROMs) are basically the same as mask ROMs once they have been programmed. As you have learned, ROMs are a type of programmable logic device. The difference is that PROMs come from the manufacturer unprogrammed and are custom programmed in the field to meet the user's needs.

After completing this section, you should be able to

- Distinguish between a mask ROM and a PROM
- Describe a basic PROM memory cell
- Discuss EPROMs including UV EPROMs and EEPROMs
- Analyze an EPROM programming cycle

PROMs

A **PROM** uses some type of fusing process to store bits, in which a memory *link* is burned open or left intact to represent a 0 or a 1. The fusing process is irreversible; once a PROM is programmed, it cannot be changed.

Figure 33 illustrates a MOS PROM array with fusible links. The fusible links are manufactured into the PROM between the source of each cell's transistor and its column line. In the programming process, a sufficient current is injected through the fusible link to burn it open to create a stored 0. The link is left intact for a stored 1.

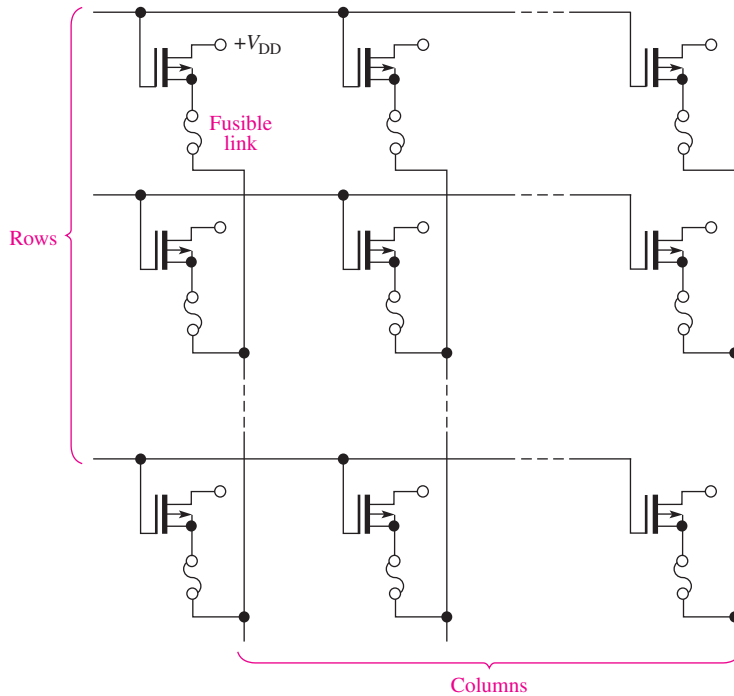


FIGURE 33 MOS PROM array with fusible links. (All drains are commonly connected to V_{DD} .)

Three basic fuse technologies used in PROMs are metal links, silicon links, and pn junctions. A brief description of each of these follows.

1. Metal links are made of a material such as nichrome. Each bit in the memory array is represented by a separate link. During programming, the link is either “blown” open or left intact. This is done basically by first addressing a given cell and then forcing a sufficient amount of current through the link to cause it to open.
2. Silicon links are formed by narrow, notched strips of polycrystalline silicon. Programming of these fuses requires melting of the links by passing a sufficient amount of current through them. This amount of current causes a high temperature at the fuse location that oxidizes the silicon and forms an insulation around the now-open link.
3. Shorted junction, or avalanche-induced migration, technology consists basically of two semiconductor pn junctions arranged back-to-back. During programming, one of the diode junctions is avalanche, and the resulting voltage and heat cause aluminum ions to migrate and short the junction. The remaining junction is then used as a forward-biased diode to represent a data bit.

EPROMs

An **E**PROM is an erasable PROM. Unlike an ordinary PROM, an EPROM can be reprogrammed if an existing program in the memory array is erased first.

An EPROM uses an NMOSFET array with an isolated-gate structure. The isolated transistor gate has no electrical connections and can store an electrical charge for indefinite periods of time. The data bits in this type of array are represented by the presence or absence of a stored gate charge. Erasure of a data bit is a process that removes the gate charge.

A typical EPROM is represented in Figure 34 by a logic diagram. Its operation is representative of that of other typical EPROMs of various sizes. As the logic symbol

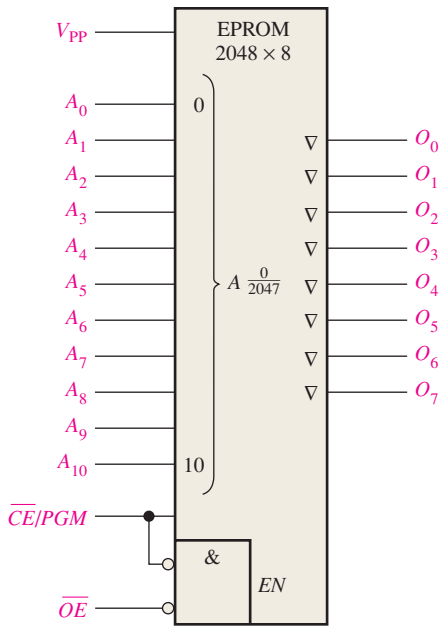


FIGURE 34 The logic symbol for a 2048×8 EPROM.

shows, this device has 2048 addresses ($2^{11} = 2048$), each with eight bits. Notice that the eight outputs are tristate (∇).

Two basic types of erasable PROMs are the ultraviolet erasable PROM (UV EPROM) and the electrically erasable PROM (EEPROM).

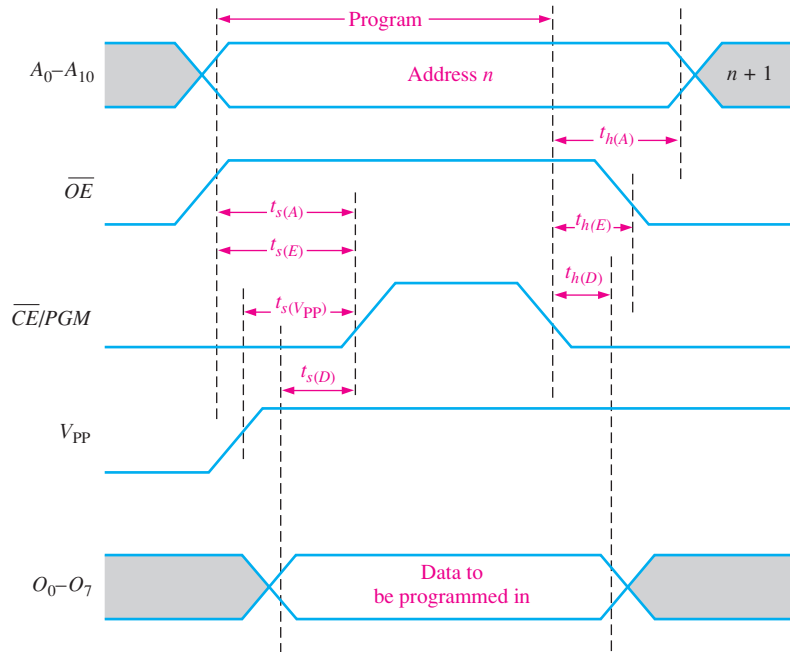
UV EPROMS You can recognize the UV EPROM device by the UV transparent window on the package. The isolated gate in the FET of an ultraviolet EPROM is “floating” within an oxide insulating material. The programming process causes electrons to be removed from the floating gate. Erasure is done by exposure of the memory array chip to high-intensity ultraviolet radiation through the UV window on top of the package. The positive charge stored on the gate is neutralized after several minutes to an hour of exposure time.

To read from the memory, the output enable input (\overline{OE}) must be LOW and the power-down/program (\overline{CE}/PGM) input LOW.

To program or write to the device, a high dc voltage is applied to V_{PP} and \overline{OE} is HIGH. The eight data bits to be programmed into a given address are applied to the outputs (O_0 through O_7), and the address is selected on inputs A_0 through A_{10} . Next, a HIGH level pulse is applied to the \overline{CE}/PGM input. The addresses can be programmed in any order.

A timing diagram for the programming is shown in Figure 35. These signals are normally produced by an EPROM programmer.

FIGURE 35 Timing diagram for a 2048×8 UV EPROM programming cycle, with critical setup times (t_s) and hold times (t_h) indicated.



EEPROMS An electrically erasable PROM can be both erased and programmed with electrical pulses. Since it can be both electrically written into and electrically erased, the EEPROM can be rapidly programmed and erased in-circuit for reprogramming.

Two types of EEPROMs are the floating-gate MOS and the metal nitride-oxide silicon (MNOS). The application of a voltage on the control gate in the floating-gate structure permits the storage and removal of charge from the floating gate.

SECTION 5 CHECKUP

1. How do PROMs differ from ROMs?
2. After erasure, all bits are (1s, 0s) in a typical EPROM.
3. What is the normal mode of operation for a PROM?

6 THE FLASH MEMORY

The ideal memory has high storage capacity, nonvolatility, in-system read and write capability, comparatively fast operation, and cost effectiveness. The traditional memory technologies such as ROM, PROM, EPROM, EEPROM, SRAM, and DRAM individually exhibit one or more of these characteristics. Flash memory has all of the desired characteristics.

After completing this section, you should be able to

- Discuss the basic characteristics of a flash memory
- Describe the basic operation of a flash memory cell
- Compare flash memories with other types of memories
- Discuss the USB flash drive

Flash memories are high-density read/write memories (high-density translates into large bit storage capacity) that are nonvolatile, which means that data can be stored indefinitely without power. They are sometimes used in place of small-capacity hard disk drives in laptop computers.

High-density means that a large number of cells can be packed into a given surface area on a chip; that is, the higher the density, the more bits that can be stored on a given size chip. This high density is achieved in flash memories with a storage cell that consists of a single floating-gate MOS transistor. A data bit is stored as charge or the absence of charge on the floating gate depending if a 0 or a 1 is stored.

Flash Memory Cell

A single-transistor cell in a flash memory is represented in Figure 36. The stacked gate MOS transistor consists of a control gate and a floating gate in addition to the drain and source. The floating gate stores electrons (charge) as a result of a sufficient voltage applied to the control gate. A 0 is stored when there is more charge and a 1 is stored when there is less or no charge. The amount of charge present on the floating gate determines if the transistor will turn on and conduct current from the drain to the source when a control voltage is applied during a read operation.

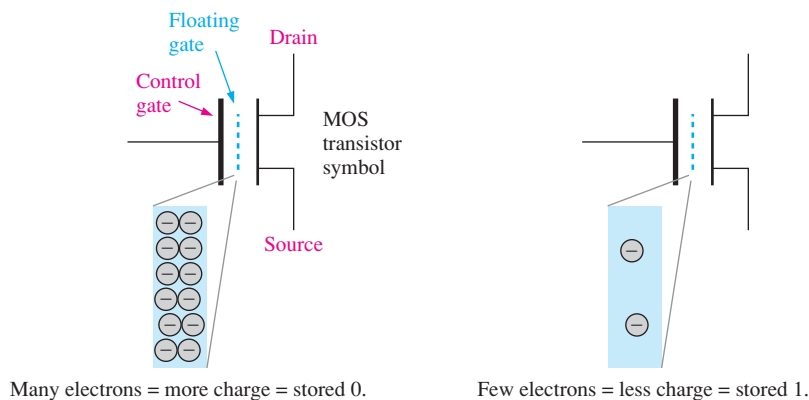


FIGURE 36 The storage cell in a flash memory.

Basic Flash Memory Operation

There are three major operations in a flash memory: the *programming* operation, the *read* operation, and the *erase* operation.

PROGRAMMING Initially, all cells are at the 1 state because charge was removed from each cell in a previous erase operation. The programming operation adds electrons (charge) to the floating gate of those cells that are to store a 0. No charge is added to those cells that are to store a 1. Application of a sufficient positive voltage to the control gate with respect to the source during programming attracts electrons to the floating gate, as indicated in Figure 37. Once programmed, a cell can retain the charge for up to 100 years without any external power.

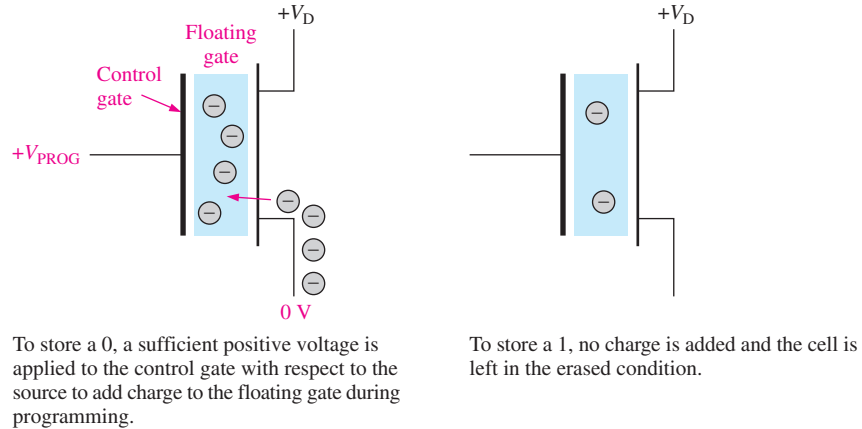


FIGURE 37 Simplified illustration of storing a 0 or a 1 in a flash cell during the programming operation.

READ During a read operation, a positive voltage is applied to the control gate. The amount of charge present on the floating gate of a cell determines whether or not the voltage applied to the control gate will turn on the transistor. If a 1 is stored, the control gate voltage is sufficient to turn the transistor on. If a 0 is stored, the transistor will not turn on because the control gate voltage is not sufficient to overcome the negative charge stored in the floating gate. Think of the charge on the floating gate as a voltage source that opposes the voltage applied to the control gate during a read operation. So the floating gate charge associated with a stored 0 prevents the control gate voltage from reaching the turn-on threshold, whereas the small or zero charge associated with a stored 1 allows the control gate voltage to exceed the turn-on threshold.

When the transistor turns on, there is current from the drain to the source of the cell transistor. The presence of this current is sensed to indicate a 1, and the absence of this current is sensed to indicate a 0. This basic idea is illustrated in Figure 38.

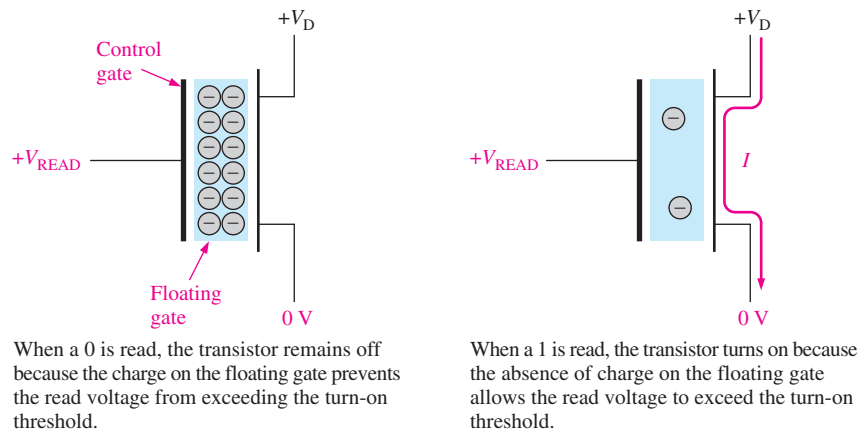
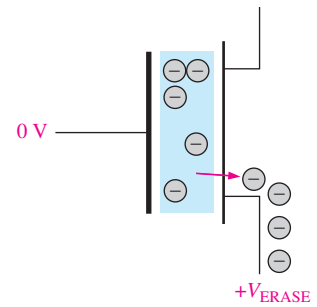


FIGURE 38 The read operation of a flash cell in an array.

ERASE During an erase operation, charge is removed from all the memory cells. A sufficient positive voltage is applied to the transistor source with respect to the control gate. This is opposite in polarity to that used in programming. This voltage attracts electrons from the floating gate and depletes it of charge, as illustrated in Figure 39. A flash memory is always erased prior to being reprogrammed.

Basic Flash Memory Array

A simplified array of flash memory cells is shown in Figure 40. Only one row line is accessed at a time. When a cell in a given bit line turns on (stored 1) during a read operation, there is current through the bit line, which produces a voltage drop across the active load. This voltage drop is compared to a reference voltage with a comparator circuit and an output level indicating a 1 is produced. If a 0 is stored, then there is no current or little current in the bit line and an opposite level is produced on the comparator output.



To erase a cell, a sufficient positive voltage is applied to the source with respect to the control gate to remove charge from the floating gate during the erase operation.

FIGURE 39 Simplified illustration of removing charge from a cell during erase.

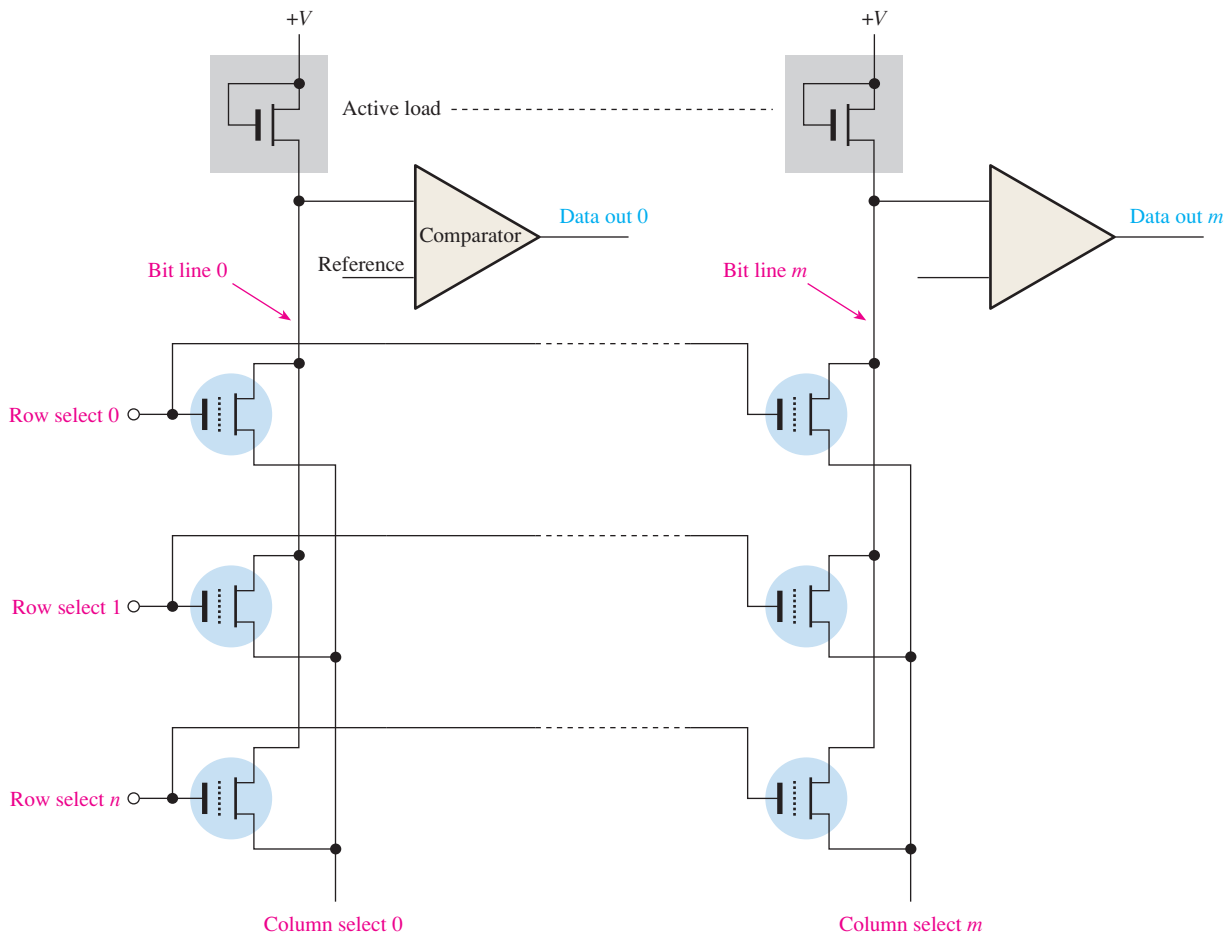


FIGURE 40 Basic flash memory array.

The memory stick is a storage medium that uses flash memory technology in a physical configuration smaller than a stick of chewing gum. Memory sticks are typically available in 128 MB to 32 GB capacities and as a kit with a PC card adaptor. Because of its compact design, it is ideal for use in small digital electronics products, such as laptop computers and digital cameras.

Comparison of Flash Memories with Other Memories

Let’s compare flash memories with other types of memories with which you are already familiar.

FLASH VS. ROM, EPROM, AND EEPROM Read-only memories are high-density, nonvolatile devices. However, once programmed the contents of a ROM can never be altered. Also, the initial programming is a time-consuming and costly process.

Although the EPROM is a high-density, nonvolatile memory, it can be erased only by removing it from the system and using ultraviolet light. It can be reprogrammed only with specialized equipment.

The EEPROM has a more complex cell structure than either the ROM or EPROM and so the density is not as high, although it can be reprogrammed without being removed from the system. Because of its lower density, the cost/bit is higher than ROMs or EPROMs.

A flash memory can be reprogrammed easily in the system because it is essentially a READ/WRITE device. The density of a flash memory compares with the ROM and EPROM because both have single-transistor cells. A flash memory (like a ROM, EPROM, or EEPROM) is nonvolatile, which allows data to be stored indefinitely with power off.

FLASH VS. SRAM As you have learned, static random-access memories are volatile READ/WRITE devices. A SRAM requires constant power to retain the stored data. In many applications, a battery backup is used to prevent data loss if the main power source is turned off. However, since battery failure is always a possibility, indefinite retention of the stored data in a SRAM cannot be guaranteed. Because the memory cell in a SRAM is basically a flip-flop consisting of several transistors, the density is relatively low.

A flash memory is also a READ/WRITE memory, but unlike the SRAM it is non-volatile. Also, a flash memory has a much higher density than a SRAM.

FLASH VS. DRAM Dynamic random-access memories are volatile high-density READ/ WRITE devices. DRAMs require not only constant power to retain data but also that the stored data must be refreshed frequently. In many applications, backup storage such as hard disk must be used with a DRAM.

Flash memories exhibit higher densities than DRAMs because a flash memory cell consists of one transistor and does not need refreshing, whereas a DRAM cell is one transistor plus a capacitor that has to be refreshed. Typically, a flash memory consumes much less power than an equivalent DRAM and can be used as a hard disk replacement in many applications.

Table 2 provides a comparison of the memory technologies.

MEMORY TYPE	NONVOLATILE	HIGH-DENSITY	ONE-TRANSISTOR CELL	IN-SYSTEM WRITABILITY
Flash	Yes	Yes	Yes	Yes
SRAM	No	No	No	Yes
DRAM	No	Yes	Yes	Yes
ROM	Yes	Yes	Yes	No
EPROM	Yes	Yes	Yes	No
EEPROM	Yes	No	No	Yes

USB Flash Drive

A USB flash drive consists of a flash memory connected to a standard USB connector housed in a small case about the size of a cigarette lighter. The USB connector can be plugged into a port on a personal computer and obtains power from the computer. These memories are usually rewritable and can have a storage capacity up to 256 GB (a number which is constantly increasing), with most ranging from 2 GB to 64 GB. A typical USB flash drive is shown in Figure 41(a), and a basic block diagram is shown in part (b).

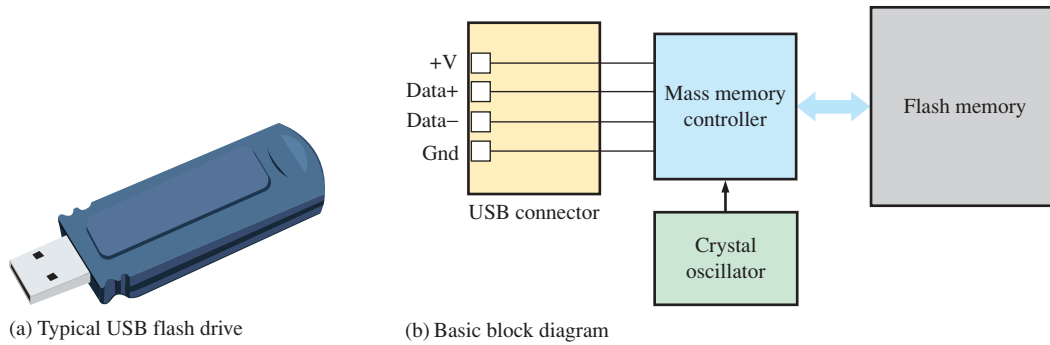


FIGURE 41 The USB flash drive.

The USB flash drive uses a standard USB A-type connector for connection to the computer, as shown in Figure 42(a). Peripherals, such as printers, use the USB B-type connector, which has a different shape and physical pin configuration. The USB icon is shown in part (b).

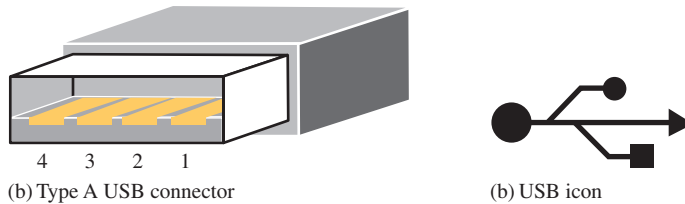


FIGURE 42

SECTION 6 CHECKUP

1. What types of memories are nonvolatile?
2. What is a major advantage of a flash memory over a SRAM or DRAM?
3. List the three modes of operation of a flash memory.

7 MEMORY EXPANSION

Available memory can be expanded to increase the word length (number of bits in each address) or the word capacity (number of different addresses) or both. Memory expansion is accomplished by adding an appropriate number of memory chips to the address, data, and control buses. SIMMs and DIMMs, which are types of memory expansion modules, are introduced.

After completing this section, you should be able to

- Define *word-length expansion*
- Show how to expand the word length of a memory
- Define *word-capacity expansion*
- Show how to expand the word capacity of a memory

Word-Length Expansion

To increase the **word length** of a memory, the number of bits in the data bus must be increased. For example, an 8-bit word length can be achieved by using two memories, each with 4-bit words as illustrated in Figure 43(a). As you can see in part (b), the 16-bit address bus is commonly connected to both memories so that the combination memory still has the same number of addresses ($2^{16} = 65,536$) as each individual memory. The 4-bit data buses from the two memories are combined to form an 8-bit data bus. Now when an address is selected, eight bits are produced on the data bus—four from each memory. Example 2 shows the details of $65,536 \times 4$ to $65,536 \times 8$ expansion.

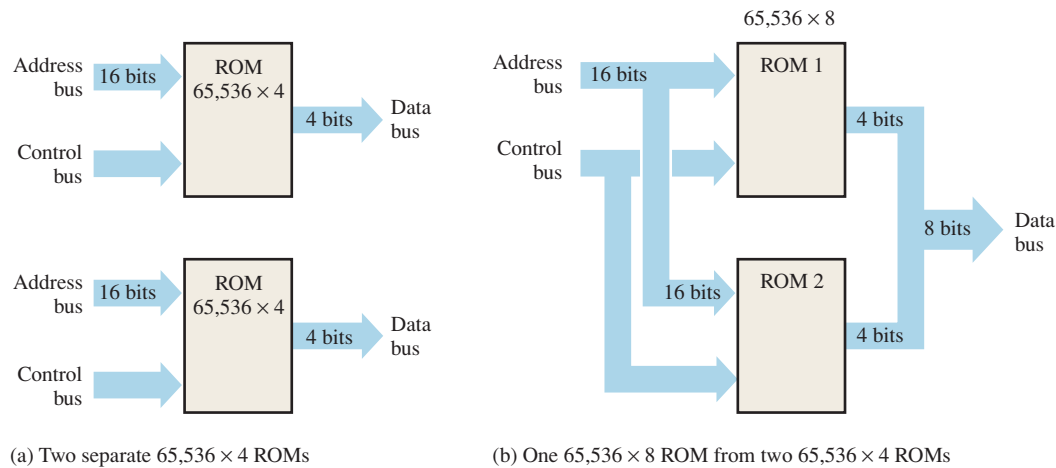


FIGURE 43 Expansion of two $65,536 \times 4$ ROMs into a $65,536 \times 8$ ROM to illustrate word-length expansion.

EXAMPLE 2

Expand the $65,536 \times 4$ ROM ($64k \times 4$) in Figure 44 to form a $64k \times 8$ ROM. Note that “64k” is the accepted shorthand for 65,536. Why not “65k”? Maybe it’s because 64 is also a power-of-two.

SOLUTION

Two $64k \times 4$ ROMs are connected as shown in Figure 45.

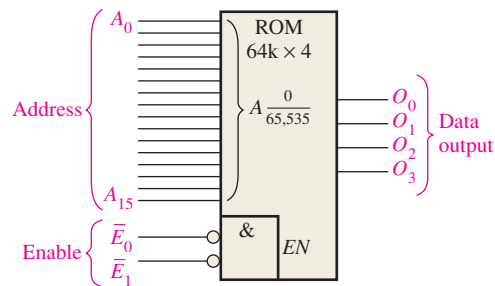


FIGURE 44 A $64k \times 4$ ROM.

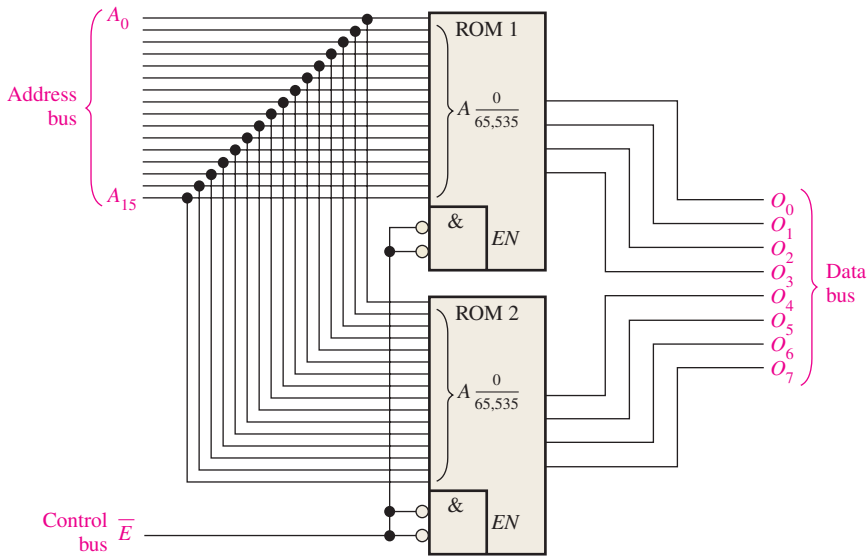


FIGURE 45

Notice that a specific address is accessed in ROM 1 and ROM 2 at the same time. The four bits from a selected address in ROM 1 and the four bits from the corresponding address in ROM 2 go out in parallel to form an 8-bit word on the data bus. Also notice that a LOW on the enable line, \overline{E} , which forms a simple control bus, enables *both* memories.

RELATED PROBLEM

Describe how you would expand a $64k \times 1$ ROM to a $64k \times 8$ ROM.

EXAMPLE 3

Use the memories in Example 2 to form a $64k \times 16$ ROM.

SOLUTION

In this case you need a memory that stores 65,536 16-bit words. Four $64k \times 4$ ROMs are required to do the job, as shown in Figure 46.

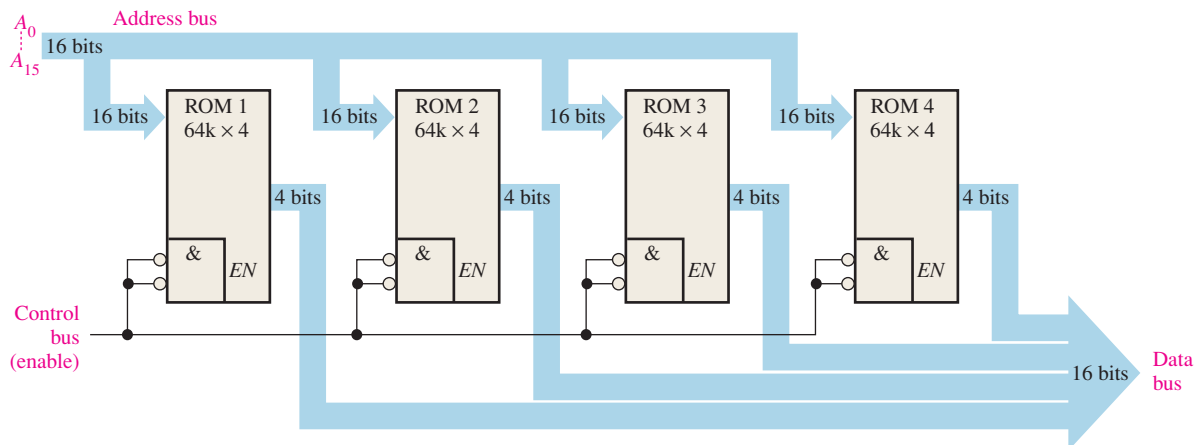


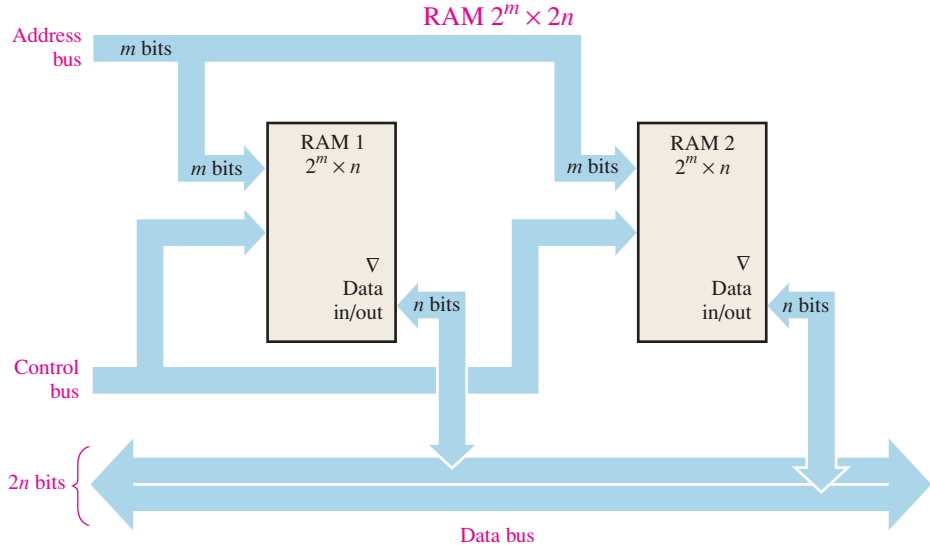
FIGURE 46

RELATED PROBLEM

How many $64k \times 1$ ROMs would be required to implement the memory shown in Figure 46?

A ROM has only data outputs, but a RAM has both data inputs and data outputs. For word-length expansion in a RAM (SRAM or DRAM), the data inputs *and* data outputs form the data bus. Because the same lines are used for data input and data output, tristate buffers are required. Most RAMs provide internal tristate circuitry. Figure 47 illustrates RAM expansion to increase the data word length.

FIGURE 47 Illustration of word-length expansion with two $2^m \times n$ RAMs forming a $2^m \times 2n$ RAM.



EXAMPLE 4

Use $1\text{M} \times 4$ SRAMs to create a $1\text{M} \times 8$ SRAM.

SOLUTION

Two $1\text{M} \times 4$ SRAMs are connected as shown in the simplified block diagram of Figure 48.

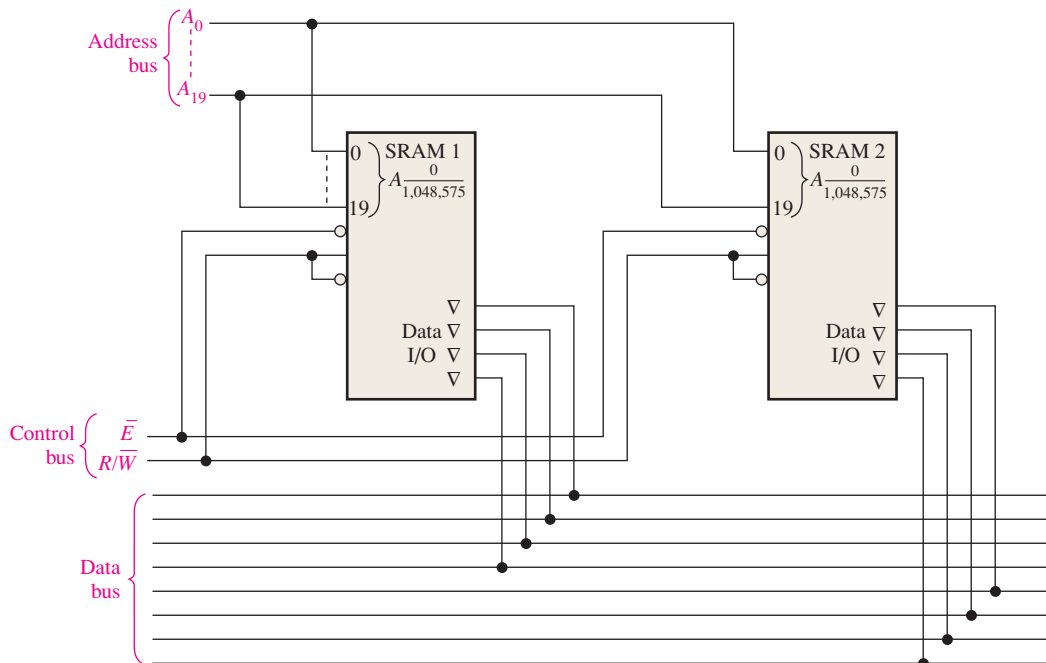


FIGURE 48

RELATED PROBLEM

Use $1\text{M} \times 8$ SRAMs to create a $1\text{M} \times 16$ SRAM.

Word-Capacity Expansion

When memories are expanded to increase the **word capacity**, the *number of addresses is increased*. To achieve this increase, the number of address bits must be increased, as illustrated in Figure 49, (where two $1\text{M} \times 8$ RAMs are expanded to form a $2\text{M} \times 8$ memory).

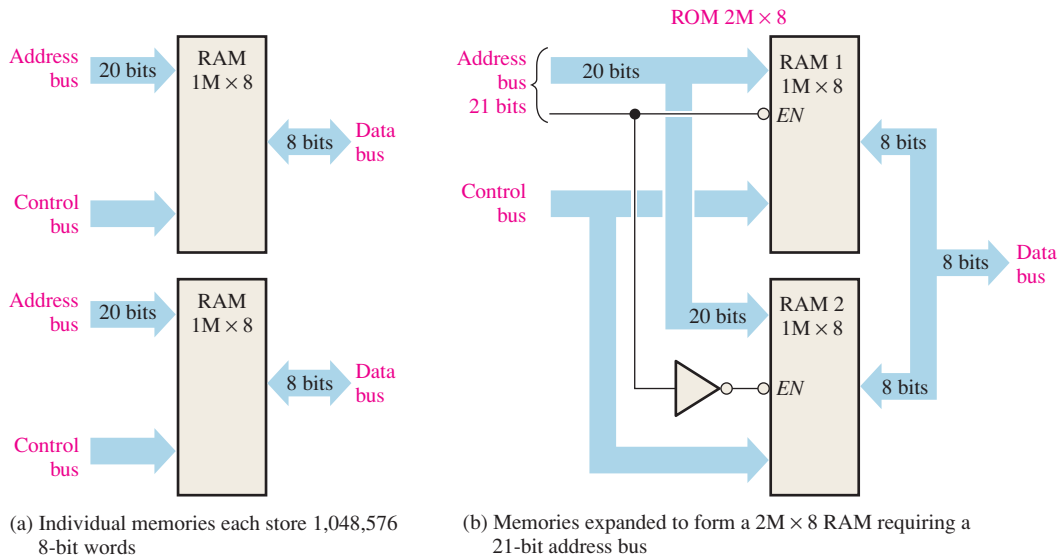


FIGURE 49 Illustration of word-capacity expansion.

Each individual memory has 20 address bits to select its 1,048,576 addresses, as shown in part (a). The expanded memory has 2,097,152 addresses and therefore requires 21 address bits, as shown in part (b). The twenty-first address bit is used to enable the appropriate memory chip. The data bus for the expanded memory remains eight bits wide. Details of this expansion are illustrated in Example 5.

EXAMPLE 5

Use $512\text{k} \times 4$ RAMs to implement a $1\text{M} \times 4$ memory.

SOLUTION

The expanded addressing is achieved by connecting the enable (\bar{E}_0) input to the twentieth address bit (A_{19}), as shown in Figure 50. Input \bar{E}_1 is used as an enable input common to both memories. When the twentieth address bit (A_{19}) is LOW, RAM 1 is selected (RAM 2 is disabled), and the nineteen lower-order address bits ($A_0 - A_{18}$) access each of the addresses in RAM 1. When the twentieth address bit (A_{19}) is HIGH, RAM 2 is enabled by a LOW on the inverter output (RAM 1 is disabled), and the nineteen lower-order address bits ($A_0 - A_{18}$) access each of the RAM 2 addresses.

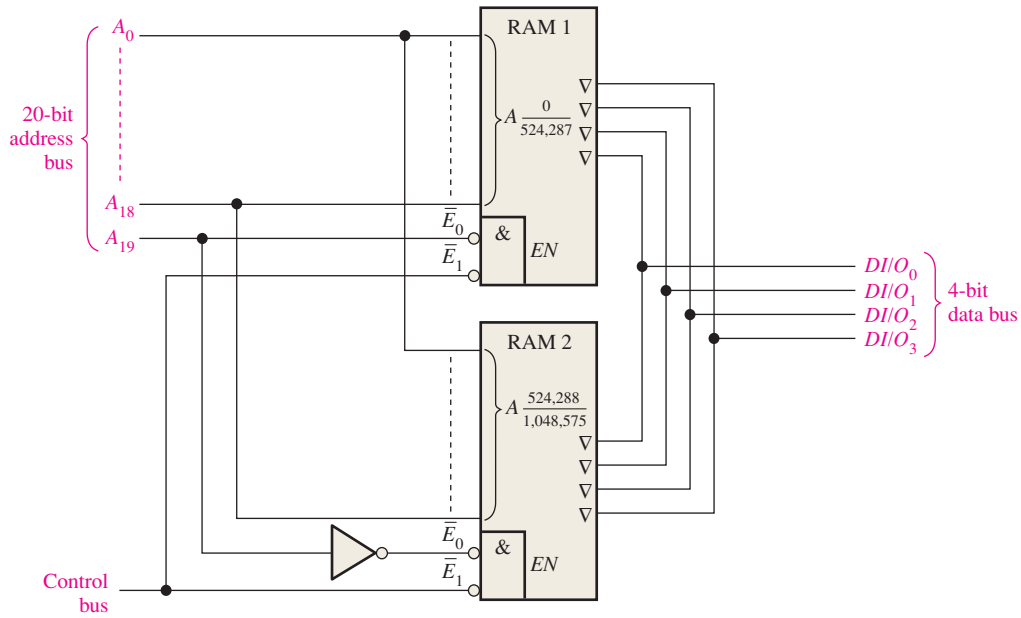


FIGURE 50

RELATED PROBLEM

What are the ranges of addresses in RAM 1 and in RAM 2 in Figure 50?



HANDS ON TIP

Memory components are extremely sensitive to static electricity. Use the following precautions when handling memory chips or modules such as DIMMs:

- Before handling, discharge your body’s static charge by touching a grounded surface or wear a grounding wrist strap containing a high-value resistor if available. A convenient, reliable ground is the ac outlet ground.
- Do not remove components from their antistatic bags until you are ready to install them.
- Do not lay parts on the antistatic bags because only the inside is antistatic.
- When handling DIMMs, hold by the edges or the metal mounting bracket. Do not touch components on the boards or the edge connector pins.
- Never slide any part over any type of surface.
- Avoid plastic, vinyl, styrofoam, and nylon in the work area.

continued

Memory Modules

SDRAMs are available in modules consisting of multiple memory ICs arranged on a printed circuit board. The most common type of SDRAM memory module is called a **DIMM** (dual in-line memory module). Another version of the DIMM is the SODIMM (small-outline DIMM). Another type of memory module, generally found in older equipment and essentially obsolete, is the SIMM (single in-line memory module). Whereas a SIMM has connection pins on one side of the pc board, a DIMM has connection pins on both sides of the board. DIMMs plug into a socket on the system motherboard for memory expansion. A generic representation of a memory module is shown in Figure 51 with the system board connectors into which the modules are inserted.

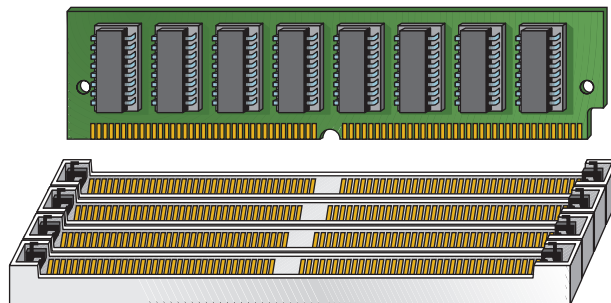


FIGURE 51 A memory module with connectors.

DIMMs generally contain DDR SDRAM memory chips. A DDR SDRAM transfers two blocks of data for each clock cycle rather than one like a standard SDRAM. There are currently three basic types of modules: DDR, DDR2 and DDR3 as follows:

- DDR modules have 184 pins and require a 2.5 voltage source.
- DDR2 modules have 240 pins and require a 1.8 voltage source.
- DDR3 modules have 240 pins and require a 1.5 voltage source.

The DDR, DDR2, and DDR3 have transfer data rates of 1600 MBps, 3200 MBps, and 6400 MBps, respectively.

When installing DIMMs, follow these steps:

1. Line up the notches on the DIMM board with the notches in the memory socket.
2. Push firmly on the module until it is securely seated in the socket.
3. Generally, the latches on both sides of the socket will snap into place when the module is completely inserted. These latches also release the module, so it can be removed from the socket.

SECTION 7 CHECKUP

1. How many $16k \times 1$ RAMs are required to achieve a memory with a word capacity of $16k$ and a word length of eight bits?
2. To expand the $16k \times 8$ memory in question 1 to a $32k \times 8$ organization, how many more $16k \times 1$ RAMs are required?
3. What does DIMM stand for?
4. What does DDR mean?

8 SPECIAL TYPES OF MEMORIES

In this section, the first in–first out (FIFO) memory, the last in–first out (LIFO) memory, the memory stack, and the charge-coupled device memory are covered.

After completing this section, you should be able to

- Describe a FIFO memory
- Describe a LIFO memory
- Discuss memory stacks
- Explain how to use a portion of RAM as a memory stack
- Describe a basic CCD memory

First In–First Out (FIFO) Memories

This type of memory is formed by an arrangement of shift registers. The term **FIFO** refers to the basic operation of this type of memory, in which the first data bit written into the memory is the first to be read out.

One important difference between a conventional shift register and a FIFO register is illustrated in Figure 52. In a conventional register, a data bit moves through the register only as new data bits are entered; in a FIFO register, a data bit immediately goes through the register to the right-most bit location that is empty.

Figure 53 is a block diagram of a FIFO serial memory. This particular memory has four serial 64-bit data registers and a 64-bit control register (marker register). When data are entered by a shift-in pulse, they move automatically under control of the marker register to the empty location closest to the output. Data cannot advance into occupied positions. However, when a data bit is shifted out by a shift-out pulse, the data bits remaining in the registers automatically move to the next position toward the output. In an asynchronous FIFO, data are shifted out independent of data entry, with the use of two separate clocks.

CONVENTIONAL SHIFT REGISTER					
INPUT	X	X	X	X	OUTPUT
0	0	X	X	X	→
1	1	0	X	X	→
1	1	1	0	X	→
0	0	1	1	1	→

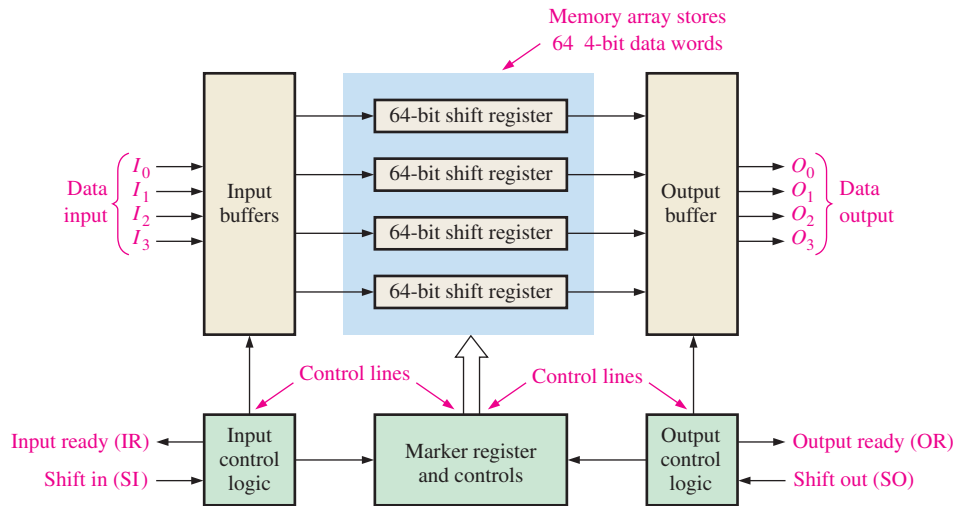
FIFO SHIFT REGISTER					
INPUT	—	—	—	—	OUTPUT
0	—	—	—	0	→
1	—	—	1	0	→
1	—	1	1	0	→
0	0	1	1	0	→

X = unknown data bits.
 In a conventional shift register, data stay to the left until “forced” through by additional data.

— = empty positions.
 In a FIFO shift register, data “fall” through (go right).

FIGURE 52 Comparison of conventional and FIFO register operation.

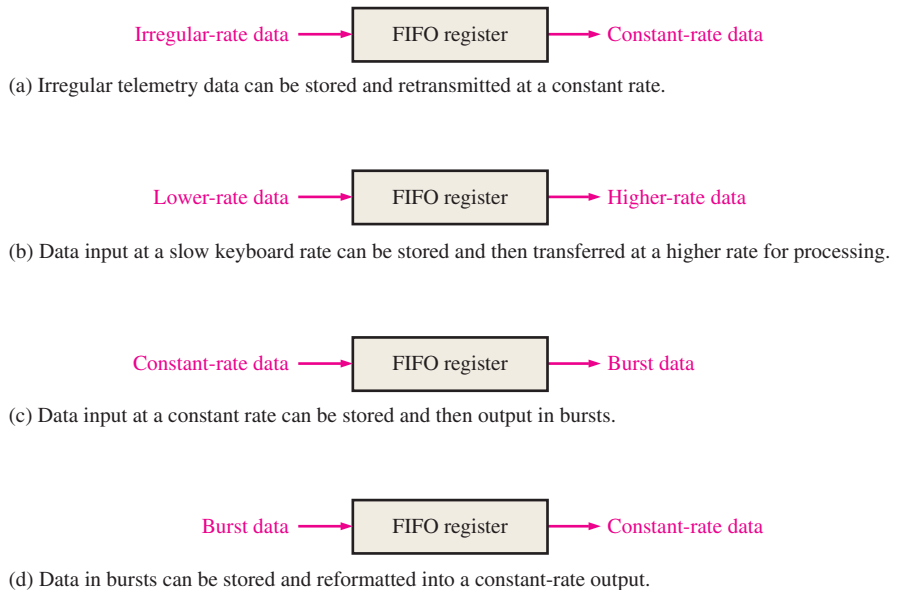
FIGURE 53 Block diagram of a typical FIFO serial memory.



FIFO Applications

One important application area for the FIFO register is the case in which two systems of differing data rates must communicate. Data can be entered into a FIFO register at one rate and taken out at another rate. Figure 54 illustrates how a FIFO register might be used in these situations.

FIGURE 54 Examples of the FIFO register in data-rate buffering applications.



Last In–First Out (LIFO) Memories

The **LIFO** (last in–first out) memory is found in applications involving microprocessors and other computing systems. It allows data to be stored and then recalled in reverse order; that is, the last data byte to be stored is the first data byte to be retrieved.

REGISTER STACKS A LIFO memory is commonly referred to as a push-down stack. In some systems, it is implemented with a group of registers as shown in Figure 55. A stack can consist of any number of registers, but the register at the top is called the *top-of-stack*.

To illustrate the principle, a byte of data is loaded in parallel onto the top of the stack. Each successive byte pushes the previous one down into the next register. This process is illustrated in Figure 56. Notice that the new data byte is always loaded into the top register and the previously stored bytes are pushed deeper into the stack. The name *push-down stack* comes from this characteristic.

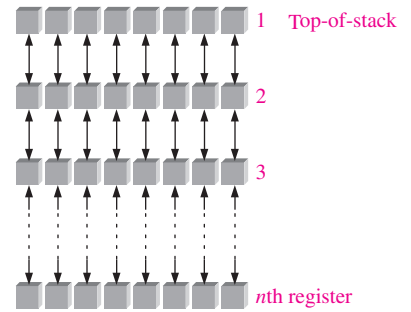


FIGURE 55 Register stack.

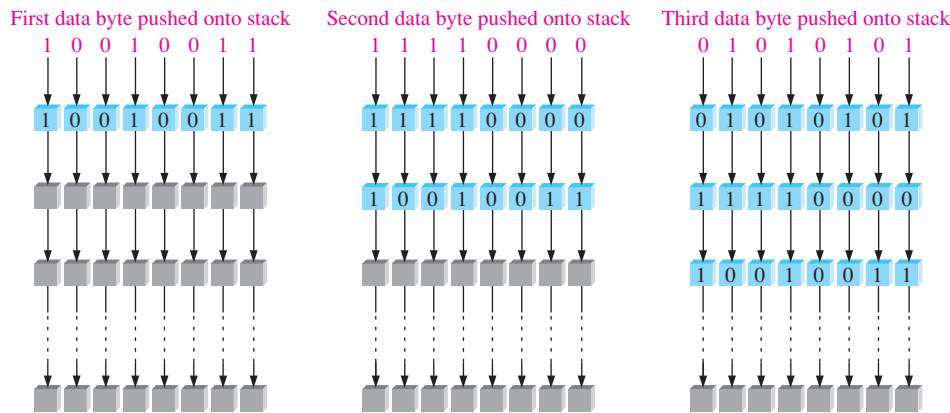


FIGURE 56 Simplified illustration of pushing data onto the stack.

Data bytes are retrieved in the reverse order. The last byte entered is always at the top of the stack, so when it is pulled from the stack, the other bytes pop up into the next higher locations. This process is illustrated in Figure 57.

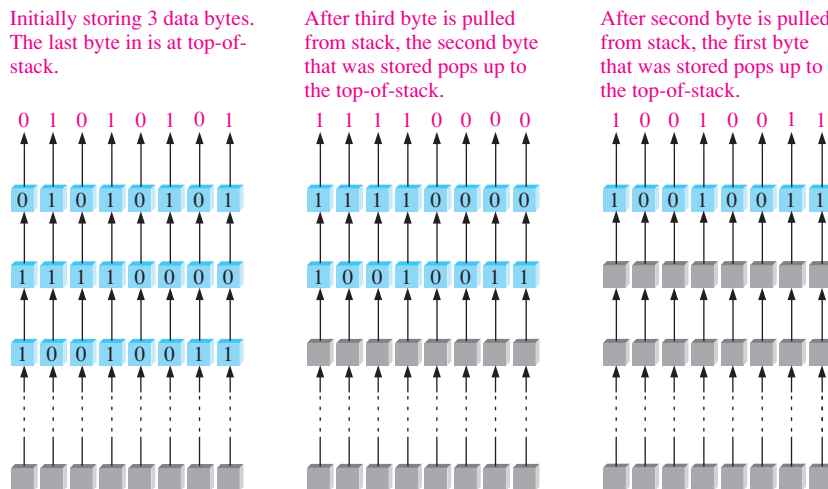


FIGURE 57 Simplified illustration of pulling data from the stack.

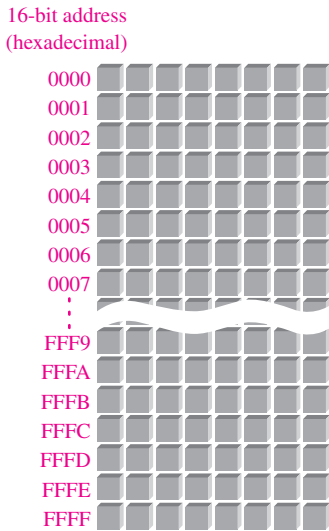


FIGURE 58 Representation of a 64 kB memory with the 16-bit addresses expressed in hexadecimal.

RAM STACK Another approach to LIFO memory used in microprocessor-based systems is the allocation of a section of RAM as the stack rather than the use of a dedicated set of registers. As you have seen, for a register stack the data moves up or down from one location to the next. In a RAM stack, the data itself does not move but the top-of-stack moves under control of a register called the stack pointer.

Consider a random-access memory that is byte organized—that is, one in which each address contains eight bits—as illustrated in Figure 58. The binary address 0000000000001111, for example, can be written as 000F in hexadecimal. A 16-bit address can have a *minimum* hexadecimal value of 0000₁₆ and a *maximum* value of FFFF₁₆. With this notation, a 64 kB memory array can be represented as shown in Figure 58. The lowest memory address is 0000₁₆ and the highest memory address is FFFF₁₆.

Now, consider a section of RAM set aside for use as a stack. A special separate register, the stack pointer, contains the address of the top of the stack, as illustrated in Figure 59. A 4-digit hexadecimal representation is used for the binary addresses. In the figure, the addresses are chosen for purposes of illustration.

Now let’s see how data are pushed onto the stack. The stack pointer is initially at address FFEE₁₆, which is the top of the stack as shown in Figure 59(a). The stack pointer is then decremented (decreased) by two to FFEC₁₆. This moves the top of the stack to a lower memory address, as shown in Figure 59(b). Notice that the top of the stack is not stationary as in the fixed register stack but moves downward (to lower addresses) in the RAM as data words are stored. Figure 59(b) shows that two bytes (one data word) are then pushed onto the stack. After the data word is stored, the top of the stack is at FFEC₁₆.

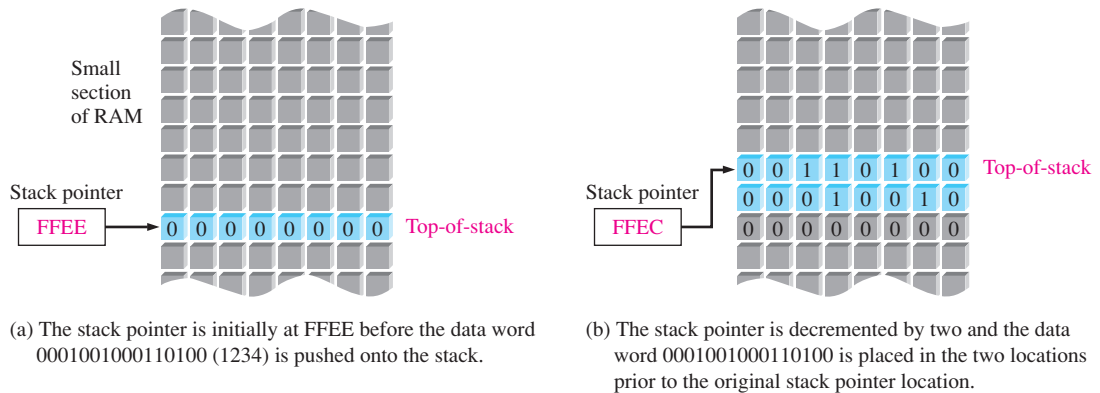


FIGURE 59 Illustration of the PUSH operation for a RAM stack.

Figure 60 illustrates the POP operation for the RAM stack. The last data word stored in the stack is read first. The stack pointer that is at FFEC is incremented (increased) by two to address FFEE₁₆ and a POP operation is performed as shown in part (b). Keep in

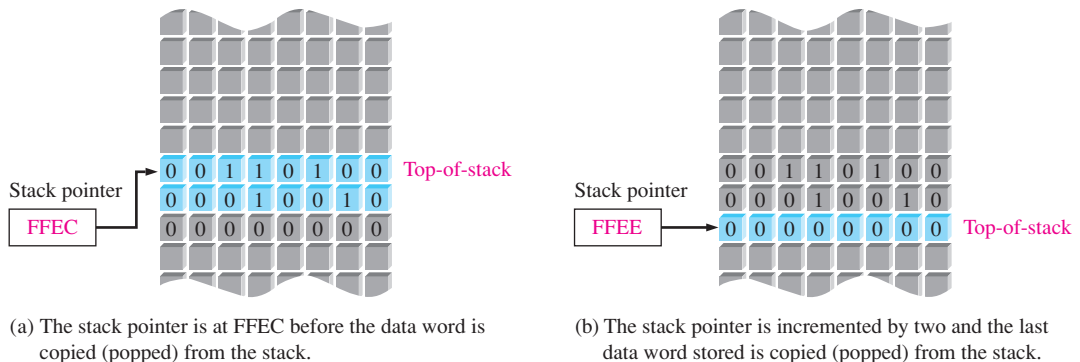


FIGURE 60 Illustration of the POP operation for the RAM stack.

mind that RAMs are nondestructive when read, so the data word still remains in the memory after a POP operation. A data word is destroyed only when a new word is written over it.

A RAM stack can be of any depth, depending on the number of continuous memory addresses assigned for that purpose.

CCD Memories

The **CCD** (charge-coupled device) memory stores data as charges on capacitors. Unlike the DRAM, however, the storage cell does not include a transistor. High density is the main advantage of CCDs, and these devices are widely used in digital imaging.

The CCD memory consists of long rows of semiconductor capacitors, called *channels*. Data are entered into a channel serially by depositing a small charge for a 0 and a large charge for a 1 on the capacitors. These charge packets are then shifted along the channel by clock signals as more data are entered.

As with the DRAM, the charges must be refreshed periodically. This process is done by shifting the charge packets serially through a refresh circuit. Figure 61 shows the basic concept of a CCD channel. Because data are shifted serially through the channels, the CCD memory has a relatively long access time. CCD arrays are used in some modern cameras to capture video images in the form of light-induced charge.

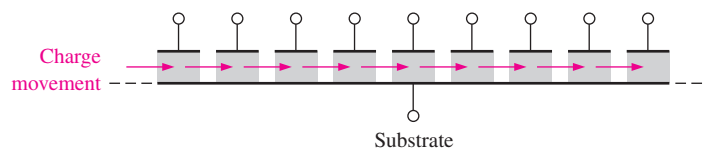


FIGURE 61 A CCD (charge-coupled device) channel.

SECTION 8 CHECKUP

1. What is a FIFO memory?
2. What is a LIFO memory?
3. Explain the PUSH operation in a memory stack.
4. Explain the POP operation in a memory stack.
5. What does the term *CCD* stand for?

9 MAGNETIC AND OPTICAL STORAGE

In this section, the basics of magnetic disks, magnetic tape, magneto-optical disks, and optical disks are introduced. These storage media are important, particularly in computer applications, where they are used for mass nonvolatile storage of data and programs.

After completing this section, you should be able to

- Describe a magnetic hard disk
- Discuss removable hard disks
- Explain the principle of magneto-optical disks
- Discuss the CD-ROM, CD-R, and CD-RW disks
- Describe the WORM
- Discuss the DVD-ROM

Magnetic Storage

MAGNETIC HARD DISKS Computers use hard disks as the internal mass storage media. **Hard disks** are rigid “platters” made of aluminum alloy or a mixture of glass and ceramic covered with a magnetic coating. Hard disk drives mainly come in three diameter sizes, 3.5 in., 2.5 in., and 1.8 in. Older formats of 8 in. and 5.25 in. are considered obsolete. A hard disk drive is hermetically sealed to keep the disks dust-free.

Typically, two or more platters are stacked on top of each other on a common shaft or spindle that turns the assembly at several thousand rpm. A separation between each disk allows for a magnetic read/write head that is mounted on the end of an actuator arm, as shown in Figure 62. There is a read/write head for both sides of each disk since data are recorded on both sides of the disk surface. The drive actuator arm synchronizes all the read/write heads to keep them in perfect alignment as they “fly” across the disk surface with a separation of only a fraction of a millimeter from the disk. A small dust particle could cause a head to “crash,” causing damage to the disk surface.

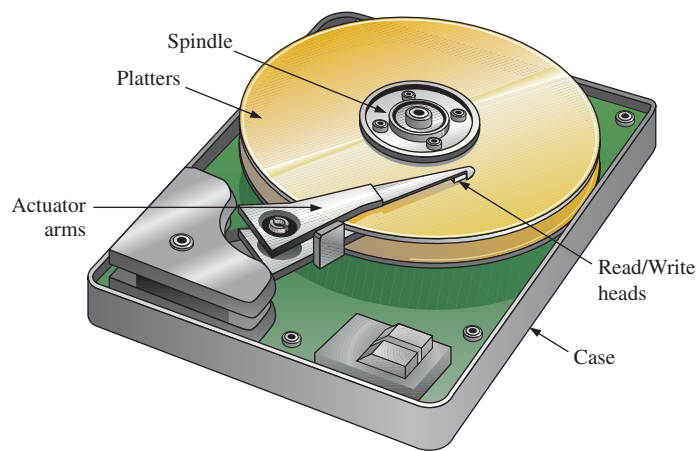


FIGURE 62 A hard disk drive.

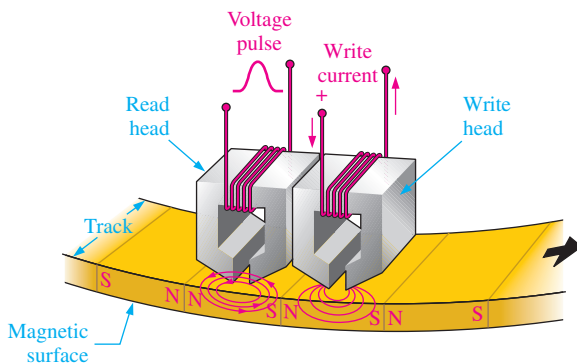
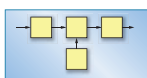


FIGURE 63 Simplified read/write head operation.

BASIC READ/WRITE HEAD PRINCIPLES The hard drive is a random-access device because it can retrieve stored data anywhere on the disk in any order. A simplified diagram of the magnetic surface read/write operation is shown in Figure 63. The direction or polarization of the magnetic domains on the disk surface is controlled by the direction of the magnetic flux lines (magnetic field) produced by the write head according to the direction of a current pulse in the winding. This magnetic flux magnetizes a small spot on the disk surface in the direction of the magnetic field. A magnetized spot of one polarity represents a binary 1, and one of the opposite polarity represents a binary 0. Once a spot on the disk surface is magnetized, it remains until written over with an opposite magnetic field.

Data are stored on a hard drive in the form of files. Keeping track of the location of files is the job of the device driver that manages the hard drive (sometimes referred to as hard drive BIOS). The device driver and the computer’s operating system can access two tables to keep track of files and file names. The first table is called the FAT (File Allocation Table). The FAT shows what is assigned to specific files and keeps a record of open sectors and bad sectors. The second table is the Root Directory which has file names, type of file, time and date of creation, starting cluster number, and other information about the file. Other types of tables include NTFS (New Technology File System) and HFS (Hierarchical File System).

SYSTEM NOTE



When the magnetic surface passes a read head, the magnetized spots produce magnetic fields in the read head, which induce voltage pulses in the winding. The polarity of these pulses depends on the direction of the magnetized spot and indicates whether the stored bit is a 1 or a 0. The read and write heads are usually combined in a single unit.

HARD DISK FORMAT A hard disk is organized or formatted into tracks and sectors, as shown in Figure 64(a). Each track is divided into a number of sectors, and each track and sector has a physical address that is used by the operating system to locate a particular data record. Hard disks typically have from a few hundred to thousands of tracks and are available with storage capacities of up to 1 TB or more. As you can see in the figure, there is a constant number of tracks/sector, with outer sectors using more surface area than the inner sectors. The arrangement of tracks and sectors on a disk is known as the *format*.

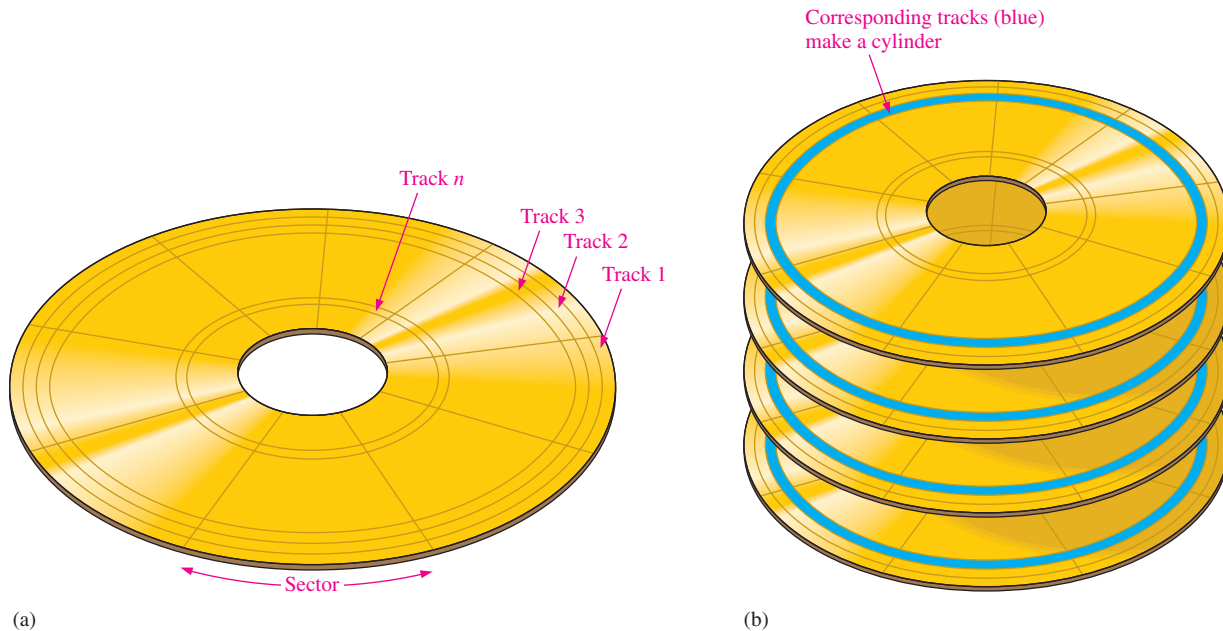


FIGURE 64 Hard disk organization and formatting.

A hard disk stack is illustrated in Figure 64(b). Hard disk drives differ in the number of platters in a stack, but there is always a minimum of two. All of the same corresponding tracks on each platter are collectively known as a cylinder, as indicated.

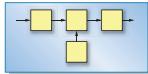
HARD DISK PERFORMANCE Several basic parameters determine the performance of a given hard disk drive. A *seek* operation is the movement of the read/write head to the desired track. The **seek time** is the average time for this operation to be performed. Typically, hard disk drives have an average seek time of several milliseconds, depending on the particular drive.

The **latency period** is the time it takes for the desired sector to spin under the head once the head is positioned over the desired track. A worst case is when the desired sector is just past the head position and spinning away from it. The sector must rotate almost a full revolution back to the head position. *Average latency period* assumes that the disk must make half of a revolution. Obviously, the latency period depends on the constant rotational speed of the disk. Disk rotation speeds are different for different disk drives but typically are from 4200 rpm to 15,000 rpm. Some disk drives rotate at 10,033 rpm and have an average latency period of less than 3 ms.

The sum of the average seek time and the average latency period is the *access time* for the disk drive.

REMOVABLE HARD DISK Removable hard disk drives with capacities of 1 TB are available. Keep in mind that the technology is changing so rapidly that there most likely will be further advancements at the time you are reading this.

MAGNETIC TAPE Tape is used for backup data from mass storage devices and typically is slower than disks because data on tape is accessed serially rather than randomly. There are several types that are available, including QIC, DAT, 8 mm, and DLT.



Tape is a viable alternative to disk due to its lower cost per bit. Though the density is lower than for a disk drive, the available surface on a tape is far greater. The highest-capacity tape media are generally on the same order as the largest available disk drive (about 1 TB—a terabyte is one trillion bytes.) Tape has historically offered enough advantage in cost over disk storage to make it a viable product, particularly for backup, where media removability is also important.

SYSTEM NOTE

QIC is an abbreviation for quarter-inch cartridge and looks much like audio tape cassettes with two reels inside. Various QIC standards have from 28 to 72 tracks that can store from 80 MB to 1.2 GB. More recent innovations under the Travan standard have lengthened the tape and increased its width allowing storage capacities up to 4 GB. QIC tape drives use read/write heads that have a single write head with a read head on each side. This allows the tape drive to verify data just written when the tape is running in either direction. In the record mode, the tape moves past the read/write heads at approximately 100 inches/second, as indicated in Figure 65.

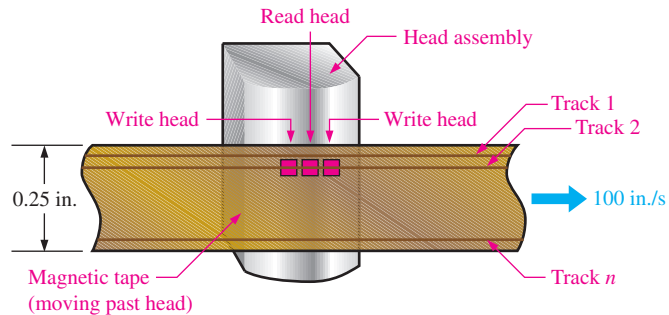


FIGURE 65 QIC tape.

DAT, which is an abbreviation for digital audio tape, uses a technique called helical scan recording. DATs offer storage capacities ranging up to 160 GB but is more expensive than QIC.

8 mm, a third type of tape format, was originally designed for the video industry but has been adopted by the computer industry as a reliable way to store large amounts of computer data. 8 mm is similar to DAT but offers storage capacities up to about 80 GB.

DLT is an abbreviation for digital linear tape. DLT is a half-inch wide tape, which is 60% wider than 8 mm and, of course, twice as wide as standard QIC. Basically, DLT differs in the way the tape-drive mechanism works to minimize tape wear compared to other systems. DLT offers storage capacities up to 110 GB.

Magneto-Optical Storage

As the name implies, magneto-optical (MO) storage devices use a combination of magnetic and optical (laser) technologies. A **magneto-optical disk** is formatted into tracks and sectors similar to magnetic disks.

The basic difference between a purely magnetic disk and an MO disk is that the magnetic coating used on the MO disk requires heat to alter the magnetic polarization. Therefore, the MO is extremely stable at ambient temperature, making data unchangeable. To write a data bit, a high-power laser beam is focused on a tiny spot on the disk, and the temperature of that tiny spot is raised above a temperature level called the Curie point (about 200 °C). Once heated, the magnetic particles at that spot can easily have their direction (polarization) changed by a magnetic field generated by the write head. Information is read from the disk with a less-powerful laser than used for writing, making use of the Kerr effect where the polarity of the reflected laser light is altered depending on the orientation of the magnetic particles. Magnetic spots of one polarity represent 0s and magnetic spots of the opposite polarity represent 1s. Basic MO operation is shown in Figure 66, which represents a small cross-sectional area of a disk.

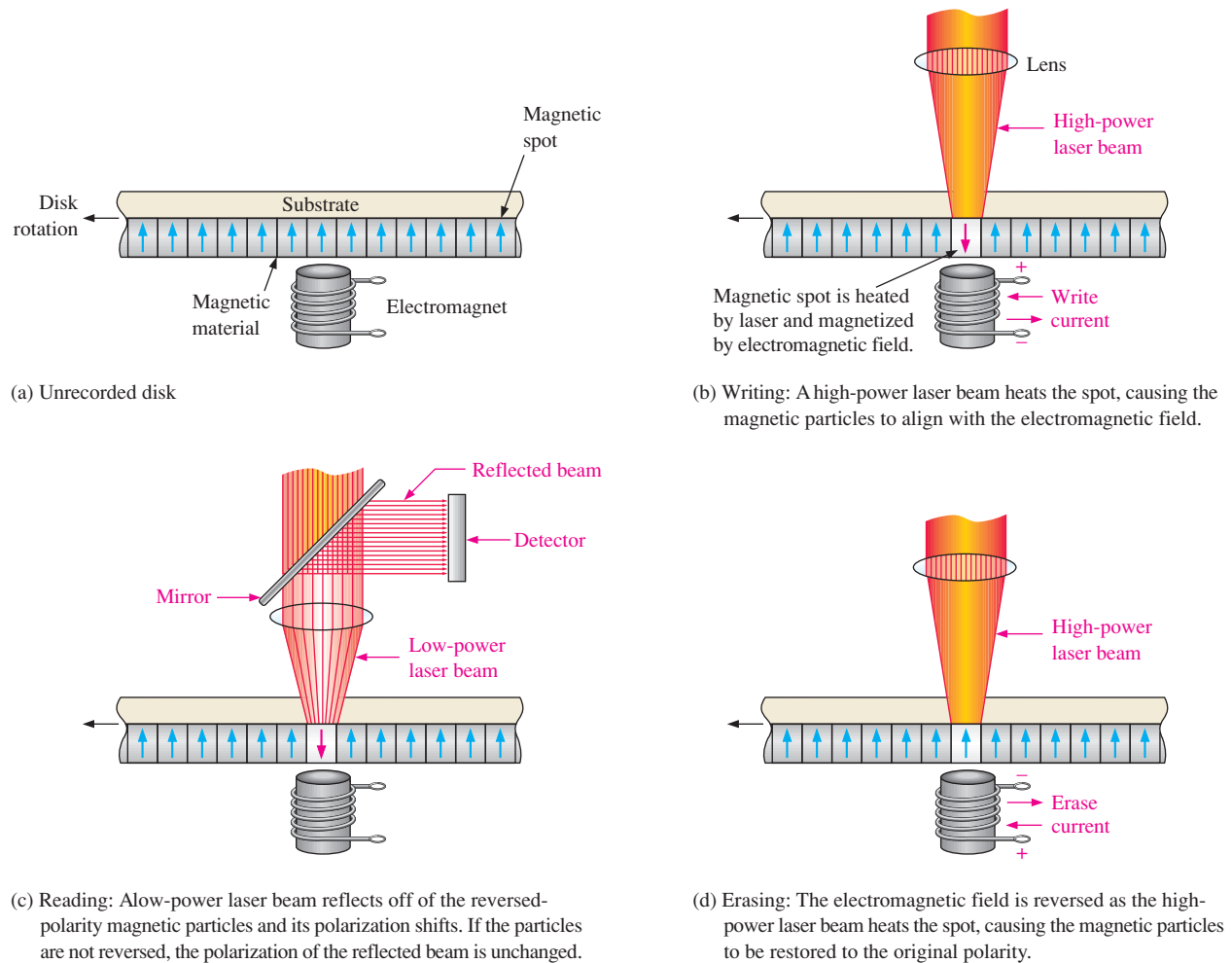


FIGURE 66 Basic principle of a magneto-optical disk.

Optical Storage

CD-ROM The basic Compact Disk–Read-Only Memory is a 120 mm diameter disk with a sandwich of three coatings: a polycarbonate plastic on the bottom, a thin aluminum sheet for reflectivity, and a top coating of lacquer for protection. The **CD-ROM** disk is formatted in a single spiral track with sequential 2 kB sectors and has a capacity of 680 MB. Data are prerecorded at the factory in the form of minute indentations called *pits* and the flat area surrounding the pits called *lands*. The pits are stamped into the plastic layer and cannot be erased.

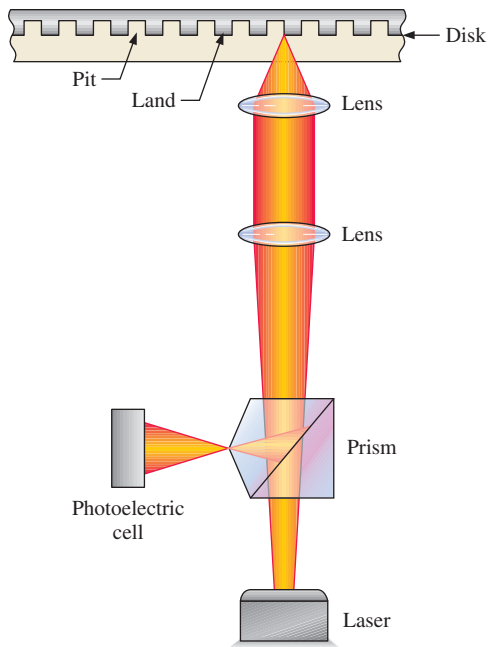


FIGURE 67 Basic operation of reading data from a CD-ROM.

A CD player reads data from the spiral track with a low-power infrared laser, as illustrated in Figure 67. The data are in the form of pits and lands as shown. Laser light reflected from a pit is 180° out-of-phase with the light reflected from the lands. As the disk rotates, the narrow laser beam strikes the series of pits and lands of varying lengths, and a photodiode detects the difference in the reflected light. The result is a series of 1s and 0s corresponding to the configuration of pits and lands along the track.

WORM Write Once/Read Many (**WORM**) is a type of optical storage that can be written onto one time after which the data cannot be erased but can be read many times. To write data, a low-power laser is used to burn microscopic pits on the disk surface. 1s and 0s are represented by the burned and nonburned areas.

CD-R This is essentially a type of WORM. The difference is that the CD-Recordable allows multiple write sessions to different areas of the disk. The **CD-R** disk has a spiral track like the CD-ROM, but instead of mechanically pressing indentations on the disk to represent data, the CD-R uses a laser to burn microscopic spots into an organic dye surface. When heated beyond a critical temperature with a laser during read, the burned spots change color and reflect less light than the nonburned areas. Therefore, 1s and 0s are represented on a CD-R by burned and nonburned areas, whereas on a CD-ROM they are represented by pits and lands. Like the CD-ROM, the data cannot be erased once it is written.

CD-RW The CD-Rewritable disk can be used to read and write data. Instead of the dye-based recording layer in the CD-R, the **CD-RW** commonly uses a crystalline compound with a special property. When it is heated to a certain temperature, it becomes crystalline when it cools; but if it is heated to a certain higher temperature, it melts and becomes amorphous when it cools. To write data, the focused laser beam heats the material to the melting temperature resulting in an amorphous state. The resulting amorphous areas reflect less light than the crystalline areas, allowing the read operation to detect 1s and 0s. The data can be erased or overwritten by heating the amorphous areas to a temperature above the crystallization temperature but lower than the melting temperature that causes the amorphous material to revert to a crystalline state.

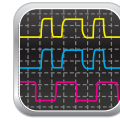
DVD-ROM Originally DVD was an abbreviation for Digital Video Disk but eventually came to represent *Digital Versatile Disk*. Like the CD-ROM, **DVD-ROM** data are prestored on the disk. However, the pit size is smaller than for the CD-ROM, allowing more data to be stored on a track. The major difference between CD-ROM and DVD-ROM is that the CD is single-sided, while the DVD has data on both sides. Also, in addition to double-sided DVD disks, there are also multiple-layer disks that use semitransparent data layers placed over the main data layers, providing storage capacities of tens of gigabytes. To access all the layers, the laser beam requires refocusing going from one layer to the other.

SECTION 9 CHECKUP

1. List the major types of magnetic storage.
2. Generally, how is a magnetic disk organized?
3. How are data written on and read from a magneto-optical disk?
4. List the types of optical storage.

10 TROUBLESHOOTING

Because memories can contain large numbers of storage cells, testing each cell can be a lengthy and frustrating process. Fortunately, memory testing is usually an automated process performed with a programmable test instrument or with the aid of software for in-system testing. Most microprocessor-based systems provide automatic memory testing as part of their system software.



After completing this section, you should be able to

- Discuss the checksum method of testing ROMs
- Discuss the checkerboard pattern method of testing RAMs

ROM Testing

Since ROMs contain known data, they can be checked for the correctness of the stored data by reading each data word from the memory and comparing it with a data word that is known to be correct. One way of doing this is illustrated in Figure 68. This process requires a reference ROM that contains the same data as the ROM to be tested. A special test instrument is programmed to read each address in both ROMs simultaneously and to compare the contents. A flowchart in Figure 69 illustrates the basic sequence.

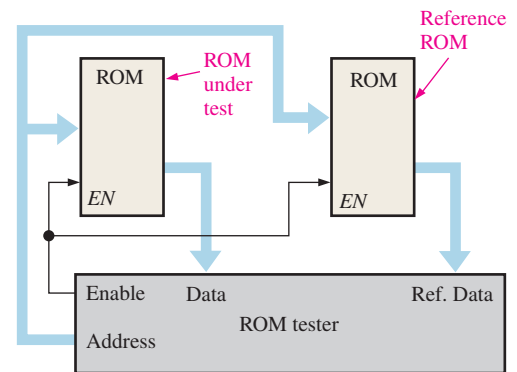
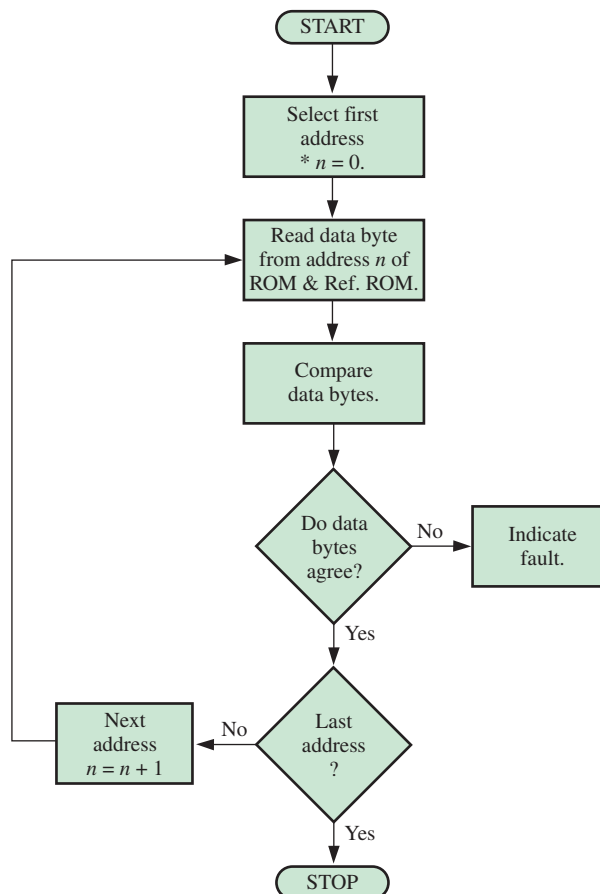


FIGURE 68 Block diagram for a complete contents check of a ROM.



* n is the address number.

FIGURE 69 Flowchart for a complete contents check of a ROM.

CHECKSUM METHOD Although the previous method checks each ROM address for correct data, it has the disadvantage of requiring a reference ROM for each different ROM to be tested. Also, a failure in the reference ROM can produce a fault indication.

In the checksum method a number, the sum of the contents of all the ROM addresses, is stored in a designated ROM address when the ROM is programmed. To test the ROM, the contents of all the addresses except the checksum are added, and the result is compared with the checksum stored in the ROM. If there is a difference, there is definitely a fault. If the checksums agree, the ROM is most likely good. However, there is a remote possibility that a combination of bad memory cells could cause the checksums to agree.

This process is illustrated in Figure 70 with a simple example. The checksum in this case is produced by taking the sum of each column of data bits and discarding the carries. This is actually an XOR sum of each column. The flowchart in Figure 71 illustrates the basic checksum test.

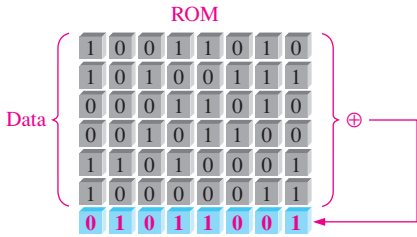


FIGURE 70 Simplified illustration of a programmed ROM with the checksum stored at a designated address.

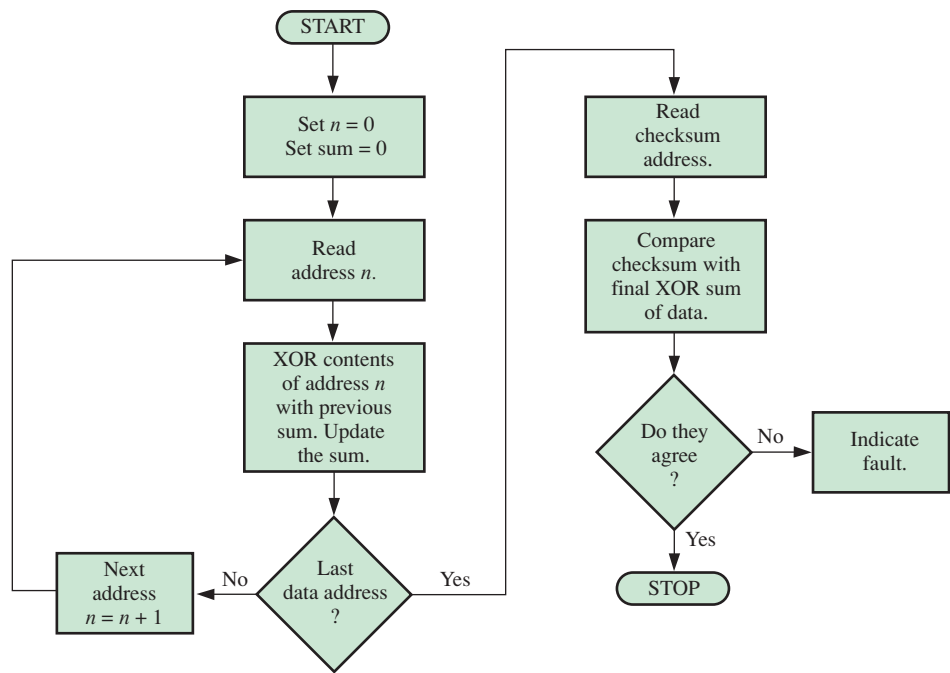


FIGURE 71 Flowchart for a basic checksum test.

The checksum test can be implemented with a special test instrument, or it can be incorporated as a test routine in the built-in (system) software or microprocessor-based systems. In that case, the ROM test routine is automatically run on system start-up.

RAM Testing

To test a RAM for its ability to store both 0s and 1s in each cell, first 0s are written into all the cells in each address and then read out and checked. Next, 1s are written into all the cells in each address and then read out and checked. This basic test will detect a cell that is stuck in either a 1 state or a 0 state.

Some memory faults cannot be detected with the all-0s–all-1s test. For example, if two adjacent memory cells are shorted, they will always be in the same state, both 0s or both 1s. Also, the all-0s–all-1s test is ineffective if there are internal noise problems such that the contents of one or more addresses are altered by a change in the contents of another address.

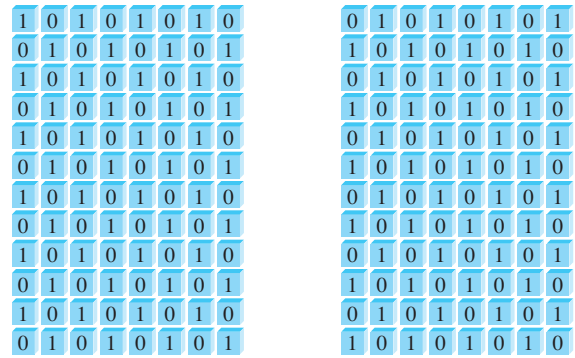
THE CHECKERBOARD PATTERN TEST One way to more fully test a RAM is by using a checkerboard pattern of 1s and 0s, as illustrated in Figure 72. Notice that

all adjacent cells have opposite bits. This pattern checks for a short between two adjacent cells; if there is a short, both cells will be in the same state.

After the RAM is checked with the pattern in Figure 72(a), the pattern is reversed, as shown in part (b). This reversal checks the ability of all cells to store both 1s and 0s.

A further test is to alternate the pattern one address at a time and check all the other addresses for the proper pattern. This test will catch a problem in which the contents of an address are dynamically altered when the contents of another address change.

A basic procedure for the checkerboard test is illustrated by the flowchart in Figure 73. The procedure can be implemented with the system software in microprocessor-based systems so that either the tests are automatic when the system is powered up or they can be initiated from the keyboard.



(a) (b) **FIGURE 72** The RAM checkerboard test pattern.

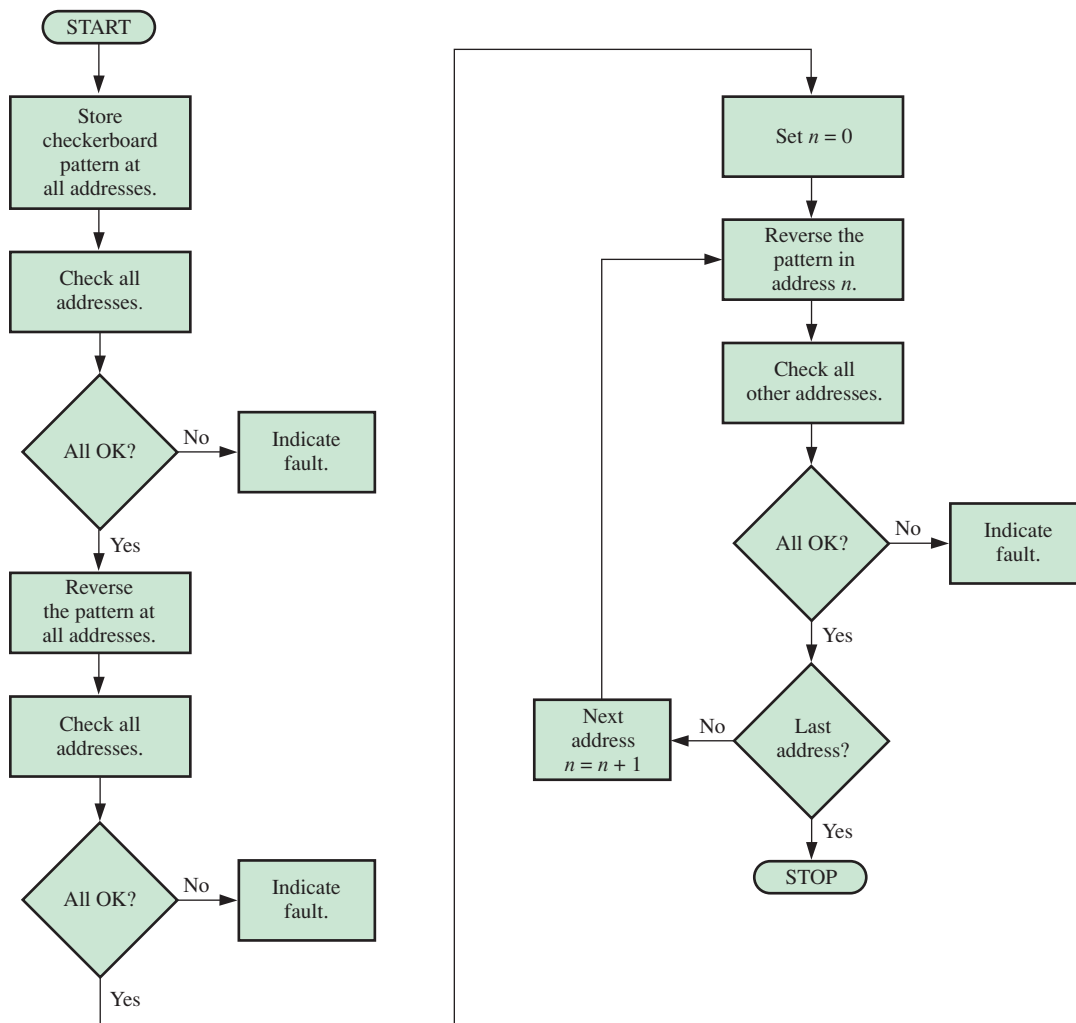


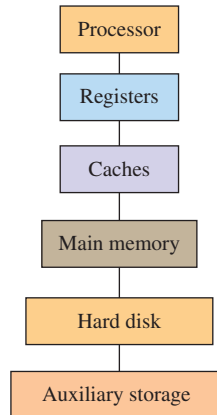
FIGURE 73 Flowchart for basic RAM checkerboard test.

SECTION 10 CHECKUP

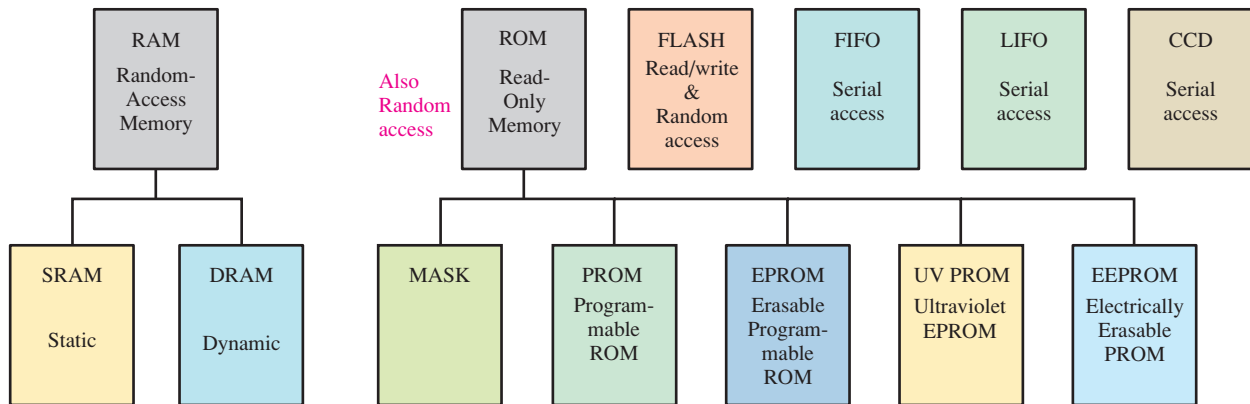
1. Describe the checksum method of ROM testing.
2. Why can the checksum method not be applied to RAM testing?
3. List the three basic faults that the checkerboard pattern test can detect in a RAM.

SUMMARY

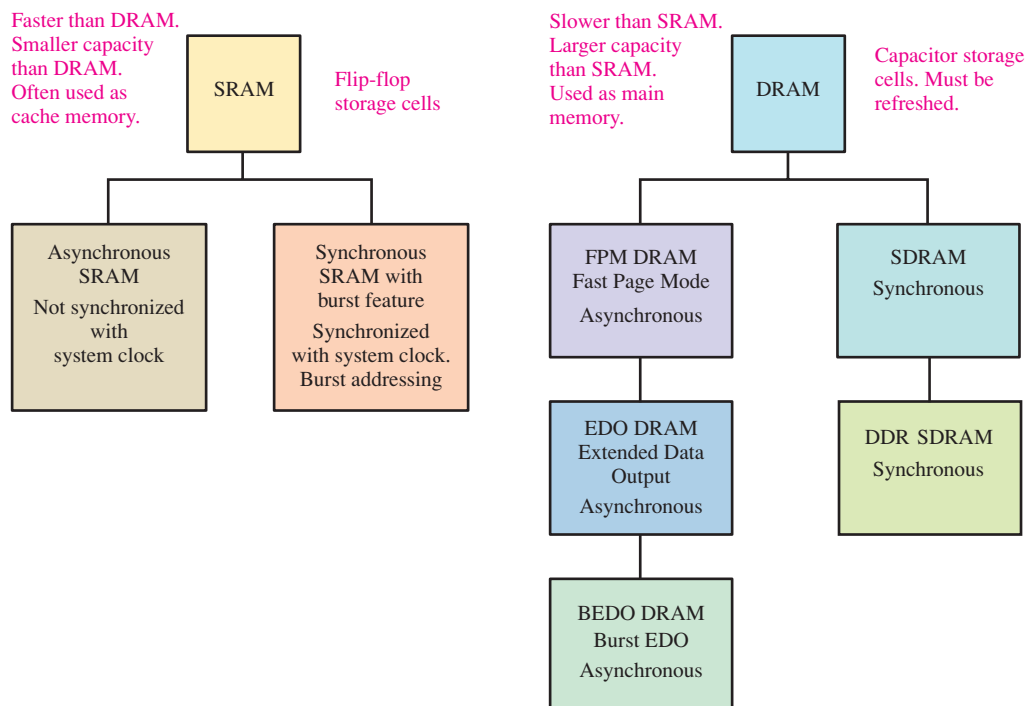
- Memory hierarchy:



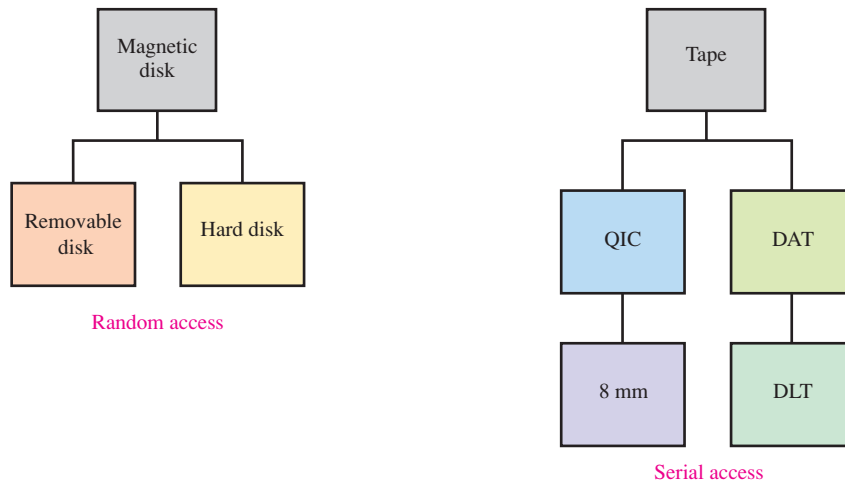
- Types of semiconductor memories:



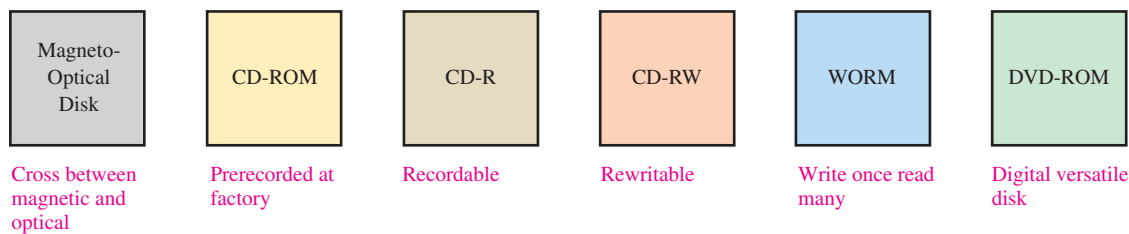
- Types of SRAMs (Static RAMs) and DRAMs (Dynamic RAMs):



- Types of magnetic storage:



- Types of optical (laser) storage:



KEY TERMS

Address The location of a given storage cell or group of cells in a memory.

Bus One or more interconnections that interface one or more devices based on a standardized specification.

Byte A group of eight bits.

Capacity The total number of data units (bits, nibbles, bytes, words) that a memory can store.

Cell A single storage element in a memory.

DDR Double data rate.

DRAM Dynamic random-access memory; a type of semiconductor memory that uses capacitors as the storage elements and is a volatile, read/write memory.

EPROM Erasable programmable read-only memory; a type of semiconductor memory device that typically uses ultraviolet light to erase data.

FIFO First in–first out memory.

Flash memory A nonvolatile read/write random-access semiconductor memory in which data are stored as charge on the floating gate of a certain type of FET.

Hard disk A magnetic storage device; typically, a stack of two or more rigid disks enclosed in a sealed housing.

LIFO Last in–first out memory; a memory stack.

Memory The portion of a computer or other system that stores binary data.

Memory hierarchy The arrangement of various memory elements to maximize speed and minimize cost.

PROM Programmable read-only memory; a type of semiconductor memory.

RAM Random-access memory; a volatile read/write semiconductor memory.

Read The process of retrieving data from a memory.

ROM Read-only memory; a nonvolatile random-access semiconductor memory.

SRAM Static random-access memory; a type of volatile read/write semiconductor memory.

Word A group of bits or bytes that acts as a single entity that can be stored in one memory location; two bytes.

Write The process of storing data in a memory.

TRUE/FALSE QUIZ

Answers are at the end of the chapter.

1. A data byte consists of eight bits.
2. A memory cell can store a byte of data.
3. The write operation stores data in memory.
4. The read operation always erases the data byte.
5. RAM is a *random address memory*.
6. Stored data is lost if power is removed from a static RAM.
7. Cache is a type of memory used for intermediate or temporary storage of data.
8. Dynamic RAMs must be periodically refreshed to retain data.
9. ROM is a *random output memory*.
10. A flash memory uses a flashing beam of light to store data.

SELF-TEST

Answers are at the end of the chapter.

1. Memory hierarchy determines
 - (a) storage capacity
 - (b) processing speed
 - (c) access time
 - (d) both (b) and (c)
2. The bit capacity of a memory that has 1024 addresses and can store 8 bits at each address is
 - (a) 1024
 - (b) 8192
 - (c) 8
 - (d) 4096
3. A 32-bit data word consists of
 - (a) 2 bytes
 - (b) 4 nibbles
 - (c) 4 bytes
 - (d) 3 bytes and 1 nibble
4. Data are stored in a random-access memory (RAM) during the
 - (a) read operation
 - (b) enable operation
 - (c) write operation
 - (d) addressing operation
5. Data that are stored at a given address in a random-access memory (RAM) is lost when
 - (a) power goes off
 - (b) the data are read from the address
 - (c) new data are written at the address
 - (d) answers (a) and (c)
6. A ROM is a
 - (a) nonvolatile memory
 - (b) volatile memory
 - (c) read/write memory
 - (d) byte-organized memory

7. A memory with 256 addresses has
 - (a) 256 address lines (b) 6 address lines
 - (c) 1 address line (d) 8 address lines
8. A byte-organized memory has
 - (a) 1 data output line (b) 4 data output lines
 - (c) 8 data output lines (d) 16 data output lines
9. The storage cell in a SRAM is
 - (a) a flip-flop (b) a capacitor
 - (c) a fuse (d) a magnetic domain
10. A DRAM must be
 - (a) replaced periodically (b) refreshed periodically
 - (c) always enabled (d) programmed before each use
11. A flash memory is
 - (a) volatile (b) a read-only memory
 - (c) a read/write memory (d) nonvolatile
 - (e) answers (a) and (c) (f) answers (c) and (d)
12. Optical storage devices employ
 - (a) ultraviolet light (b) electromagnetic fields
 - (c) optical couplers (d) lasers

PROBLEMS

Answers to odd-numbered problems are at the end of the chapter.

SECTION 1 Memory System Hierarchy

1. What is a cache in memory terminology and where is it generally located in a system?
2. What does main memory consist of?
3. What part of a memory system has the highest latency?
4. A certain optical jukebox can store 150 PB. Express this in terms of bytes.
5. Assume the cache in Figure 3 has a latency of 30 ns and the main memory a latency of 75 ns. Determine the time required for the processor to acquire a block of data for a cache hit and for a cache miss as illustrated in the figure.
6. Define the terms *temporal locality* and *spatial locality*.

SECTION 2 Semiconductor Memory Basics

7. Identify the ROM and the RAM in Figure 74.

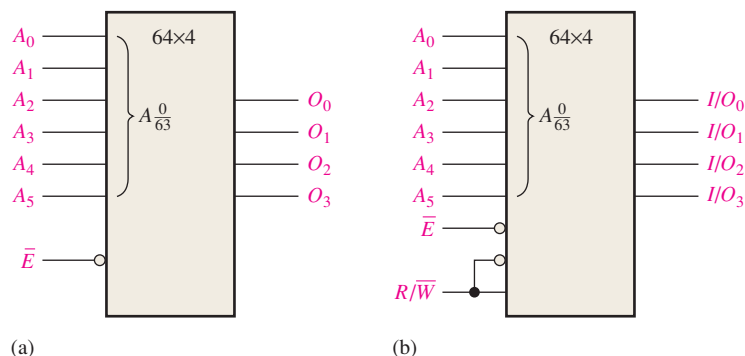


FIGURE 74

8. Explain why RAMs and ROMs are both random-access memories.
9. Explain the purposes of the address bus and the data bus.
10. What memory address (0 through 256) is represented by each of the following hexadecimal numbers:
 (a) $0A_{16}$ (b) $3F_{16}$ (c) CD_{16}

SECTION 3 The Random-Access Memory (RAM)

11. A static memory array with four rows similar to the one in Figure 13 is initially storing all 0s. What is its content after the following conditions? Assume a 1 selects a row.

Row 0 = 1, Data in (Bit 0) = 1

Row 1 = 0, Data in (Bit 1) = 1

Row 2 = 1, Data in (Bit 2) = 1

Row 3 = 0, Data in (Bit 3) = 0

12. Draw a basic logic diagram for a 512×8 -bit static RAM, showing all the inputs and outputs.
13. Assuming that a $64k \times 8$ SRAM has a structure similar to that of the SRAM in Figure 15, determine the number of rows and 8-bit columns in its memory cell array.
14. Redraw the block diagram in Figure 15 for a $64k \times 8$ memory.
15. Explain the difference between a SRAM and a DRAM.
16. What is the capacity of a DRAM that has twelve address lines?

SECTION 4 The Read-Only Memory (ROM)

17. For the ROM array in Figure 75, determine the outputs for all possible input combinations, and summarize them in tabular form (Blue cell is a 1, gray cell is a 0).

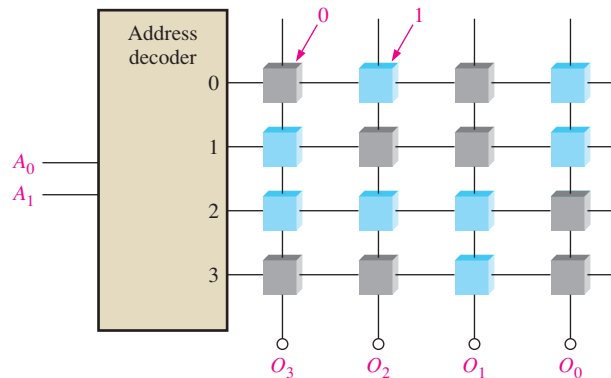


FIGURE 75

18. Determine the truth table for the ROM in Figure 76.
19. Using a procedure similar to that in Example 1, show a ROM for conversion of single-digit BCD to excess-3 code.
20. What is the total *bit* capacity of a ROM that has 14 address lines and 8 data outputs?

SECTION 5 Programmable ROMs

21. Assuming that the PROM matrix in Figure 77 is programmed by blowing a fuse link to create a 0, indicate the links to be blown to program an X^3 look-up table, where X is a number from 0 through 7.

MEMORY AND STORAGE

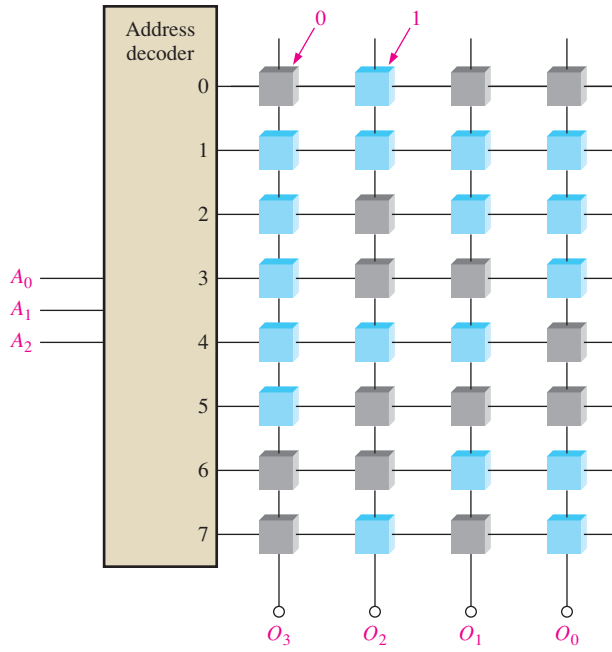


FIGURE 76

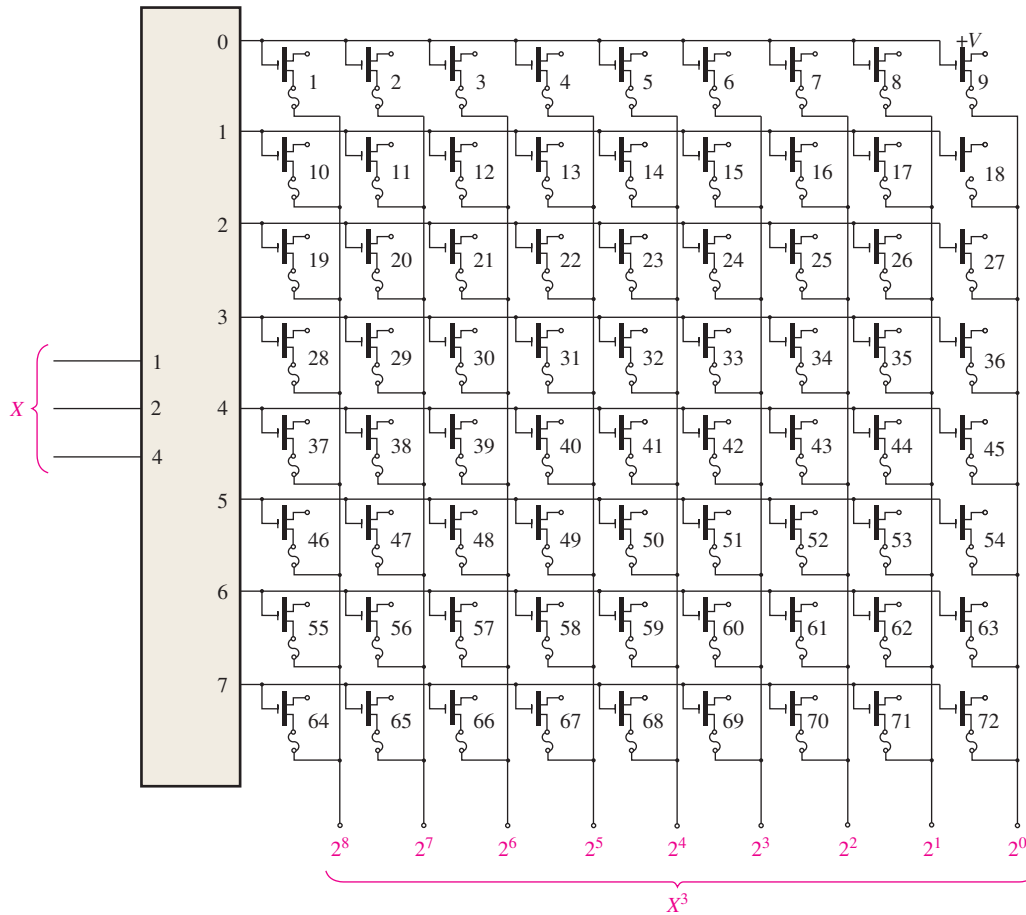


FIGURE 77

22. Determine the addresses that are programmed and the contents of each address after the programming sequence in Figure 78 has been applied to an EPROM like the one shown in Figure 34.

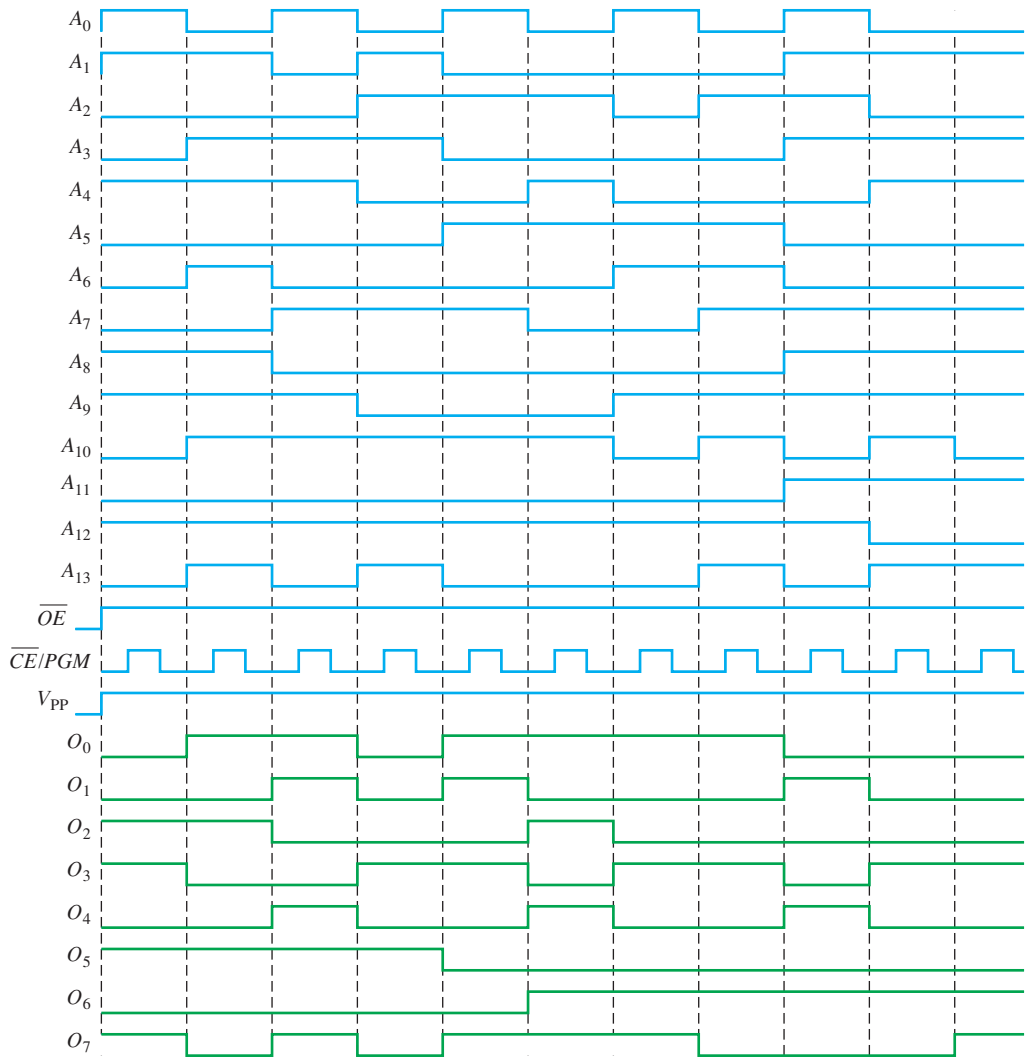


FIGURE 78

SECTION 7 Memory Expansion

23. Use $16k \times 4$ DRAMs to build a $64k \times 8$ DRAM. Show the logic diagram.
24. Using a block diagram, show how $64k \times 1$ dynamic RAMs can be expanded to build a $256k \times 4$ RAM.
25. What is the word length and the word capacity of the memory of Problem 23? Problem 24?

SECTION 8 Special Types of Memories

26. Complete the timing diagram in Figure 79 by showing the output waveforms that are initially all LOW for a FIFO serial memory like that shown in Figure 53.

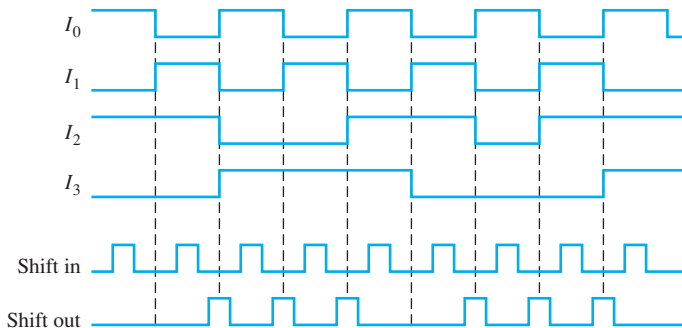


FIGURE 79

- 27. Consider a 4096×8 RAM in which the last 64 addresses are used as a LIFO stack. If the first address in the RAM is 000_{16} , designate the 64 addresses used for the stack.
- 28. In the memory of Problem 27, sixteen bytes are pushed into the stack. At what address is the first byte in located? At what address is the last byte in located?

SECTION 9 Magnetic and Optical Storage

- 29. Describe the general format of a hard disk.
- 30. Explain seek time and latency period in a hard disk drive.
- 31. Why does magnetic tape require a much longer access time than does a disk?
- 32. Explain the differences in a magneto-optical disk, a CD-ROM, and a WORM.

SECTION 10 Troubleshooting

- 33. Determine if the contents of the ROM in Figure 80 are correct.

ROM	
1	0 1 1 1
1	1 1 1 0
1	1 0 1 1
1	0 1 1 0
1	1 1 1 0
1	1 1 1 0
0	0 0 0 1
Checksum	0 1 1 0

FIGURE 80

- 34. A 128×8 ROM is implemented as shown in Figure 81. The decoder decodes the two most significant address bits to enable the ROMs one at a time, depending on the address selected.
 - (a) Express the lowest address and the highest address of each ROM as hexadecimal numbers.
 - (b) Assume that a single checksum is used for the entire memory and it is stored at the highest address. Develop a flowchart for testing the complete memory system.
 - (c) Assume that each ROM has a checksum stored at its highest address. Modify the flowchart developed in part (b) to accommodate this change.
 - (d) What is the disadvantage of using a single checksum for the entire memory rather than a checksum for each individual ROM?

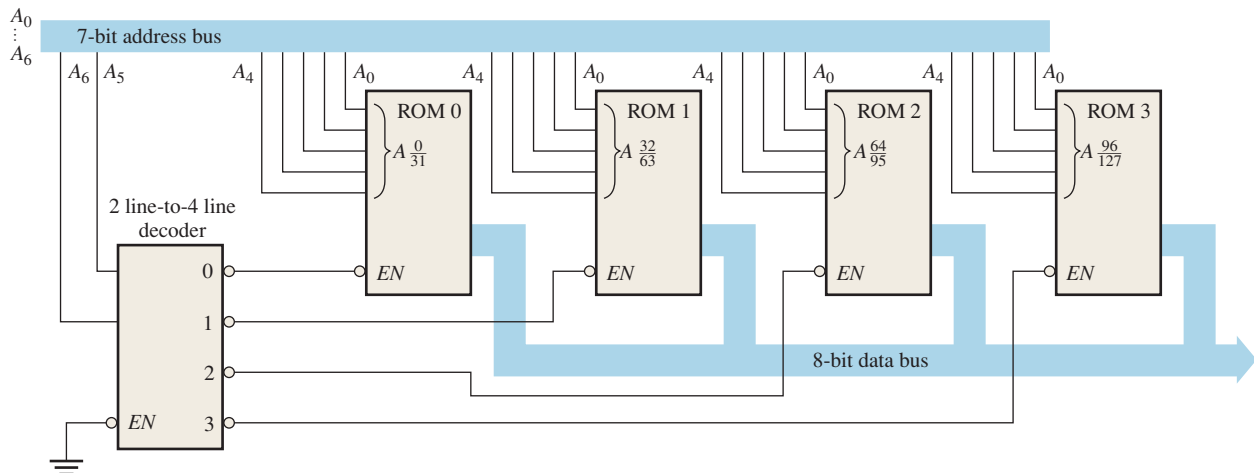


FIGURE 81

- 35. Suppose that a checksum test is run on the memory in Figure 81 and each individual ROM has a checksum at its highest address. What IC or ICs will you replace for each of the following error messages that appear on the system's video monitor?
 - (a) ADDRESSES 40-5F FAULTY
 - (b) ADDRESSES 20-3F FAULTY
 - (c) ADDRESSES 00-7F FAULTY

ANSWERS TO SECTION CHECKUPS

SECTION 1 Memory System Hierarchy

1. The purpose of memory hierarchy is to obtain the fastest access time at the lowest cost.
2. Access time is the time it takes a processor to retrieve (read) or write a block of data stored in the memory?
3. Generally, the higher the capacity the lower the cost per bit.
4. Yes
5. A hit is when the processor finds the requested data at the first place it looks. A miss is when the processor fails to find the requested data and has to go to another level of memory to find it.
6. The hit rate

SECTION 2 Semiconductor Memory Basics

1. Bit is the smallest unit of data.
2. 256 bytes is 2048 bits.
3. A write operation stores data in memory.
4. A read operation takes a copy of data from memory.
5. A unit of data is located by its address.
6. A RAM is volatile and has read/write capability. A ROM is nonvolatile and has only read capability.

SECTION 3 The Random-Access Memory (RAM)

1. Asynchronous and synchronous with burst feature
2. A small fast temporary memory between the CPU and main memory
3. SRAMs have latch storage cells that can retain data indefinitely while power is applied. DRAMs have capacitive storage cells that must be periodically refreshed.
4. The refresh operation prevents data from being lost because of capacitive discharge. A stored bit is restored periodically by recharging the capacitor to its nominal level.
5. FPM, EDO, BEDO, Synchronous

SECTION 4 The Read-Only Memory (ROM)

1. 512×8 equals 4096 bits.
2. Mask ROM, PROM, EPROM, UV EPROM, EEPROM
3. Eight bits of address are required for 256 byte locations ($2^8 = 256$).

SECTION 5 Programmable ROMs

1. PROMs are field-programmable; ROMs are not.
2. 1s are left after EPROM erasure.
3. Read is the normal mode of operation for a PROM.

SECTION 6 The Flash Memory

1. Flash, ROM, EPROM, and EEPROM are nonvolatile.
2. Flash is nonvolatile; SRAM and DRAM are volatile.
3. Programming, read, erase

SECTION 7 Memory Expansion

1. Eight RAMs
2. Eight RAMs
3. DIMM: Dual in-line memory module
4. DDR: double data rate

SECTION 8 Special Types of Memories

1. In a FIFO memory the *first* bit (or word) *in* is the *first* bit (or word) *out*.
2. In a LIFO memory the *last* bit (or word) *in* is the *first* bit (or word) *out*. A stack is a LIFO.

3. The PUSH operation or instruction adds data to the memory stack.
4. The POP operation or instruction removes data from the memory stack.
5. CCD is a charge-coupled device.

SECTION 9 Magnetic and Optical Storage

1. Magnetic storage: hard disk, tape, and magneto-optical disk.
2. A magnetic disk is organized in tracks and sectors.
3. A magneto-optical disk uses a laser beam and an electromagnet.
4. Optical storage: CD-ROM, CD-R, CD-RW, DVD-ROM, WORM

SECTION 10 Troubleshooting

1. The contents of the ROM are added and compared with a prestored checksum.
2. Checksum cannot be used because the contents of a RAM are not fixed.
3. (1) a short between adjacent cells; (2) an inability of some cells to store both 1s and 0s; (3) dynamic altering of the contents of one address when the contents of another address change.

ANSWERS TO RELATED PROBLEMS FOR EXAMPLES

- 1 $G_3G_2G_1G_0 = 1110$
- 2 Connect eight $64k \times 1$ ROMs in parallel to form a $64k \times 8$ ROM.
- 3 Sixteen $64k \times 1$ ROMs
- 4 See Figure 82.

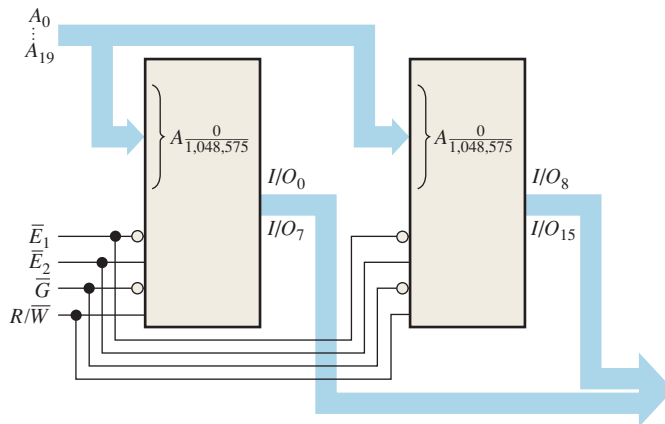


FIGURE 82

- 5 ROM 1: 0 to 524,287; ROM 2: 524,288 to 1,048,575

ANSWERS TO TRUE/FALSE QUIZ

- | | | | | |
|------|------|------|------|-------|
| 1. T | 2. F | 3. T | 4. F | 5. F |
| 6. T | 7. T | 8. T | 9. F | 10. F |

ANSWERS TO SELF-TEST

- | | | | | | |
|--------|--------|--------|---------|---------|---------|
| 1. (d) | 2. (b) | 3. (c) | 4. (c) | 5. (d) | 6. (a) |
| 7. (d) | 8. (c) | 9. (a) | 10. (b) | 11. (f) | 12. (d) |

ANSWERS TO ODD-NUMBERED PROBLEMS

1. Cache is a small area of fast memory used by the central processing unit. The L1 cache is located in the processor, and the L2 cache is outside of the processor.
3. Hard disk has the highest latency.
5. Cache hit: 30 ns; cache miss: 105 ns.
7. (a) ROM
(b) RAM
9. *Address bus* provides for transfer of address code to memory for accessing any memory location in any order for a read or write operation. *Data bus* provides for transfer of data between the microprocessor and the memory or I/O.

11.

	BIT 0	BIT 1	BIT 2	BIT 3
Row 0	1	0	0	0
Row 1	0	0	0	0
Row 2	0	0	1	0
Row 3	0	0	0	0

13. 512 rows \times 128 8-bit columns
15. A SRAM stores bits in flip-flops indefinitely as long as power is applied. A DRAM stores bits in capacitors that must be refreshed periodically to retain the data.
17. See Table P-13.

TABLE P-13

INPUTS		OUTPUTS			
A ₁	A ₀	O ₃	O ₂	O ₁	O ₀
0	0	0	1	0	1
0	1	1	0	0	1
1	0	1	1	1	0
1	1	0	0	1	0

19. See Figure P-73.

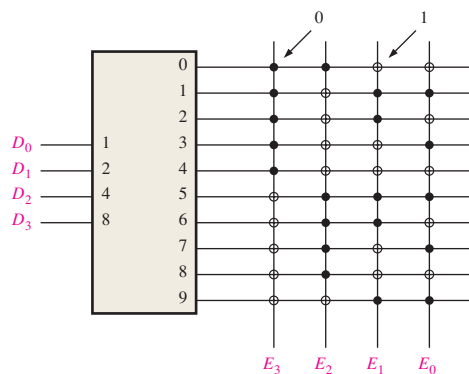


FIGURE P-73

MEMORY AND STORAGE

21. Blown links: 1–17, 19–23, 25–31, 34, 37, 38, 40–47, 53, 55, 58, 61, 62, 63, 65, 67, 69
23. Use eight $16\text{k} \times 4$ DRAMs with sixteen address lines. Two of the address lines are decoded to enable the selected memory chips. Four data lines go to each chip.
25. 8 bits, 64k words; 4 bits, 256k words
27. lowest address: FC0_{16}
highest address: FFF_{16}
29. A hard disk is formatted into tracks and sectors. Each track is divided into a number of sectors with each sector of a track having a physical address. Hard disks typically have from a few hundred to a few thousand tracks.
31. Magnetic tape has a longer access time than disk because data must be accessed sequentially rather than randomly.
33. Checksum content is in error.
35. (a) ROM 2 (b) ROM 1 (c) All ROMs

Conversions

DECIMAL	BCD(8421)	OCTAL	BINARY	DECIMAL	BCD(8421)	OCTAL	BINARY	DECIMAL	BCD(8421)	OCTAL	BINARY
0	0000	0	0	34	00110100	42	100010	68	01101000	104	1000100
1	0001	1	1	35	00110101	43	100011	69	01101001	105	1000101
2	0010	2	10	36	00110110	44	100100	70	01110000	106	1000110
3	0011	3	11	37	00110111	45	100101	71	01110001	107	1000111
4	0100	4	100	38	00111000	46	100110	72	01110010	110	1001000
5	0101	5	101	39	00111001	47	100111	73	01110011	111	1001001
6	0110	6	110	40	01000000	50	101000	74	01110100	112	1001010
7	0111	7	111	41	01000001	51	101001	75	01110101	113	1001011
8	1000	10	1000	42	01000010	52	101010	76	01110110	114	1001100
9	1001	11	1001	43	01000011	53	101011	77	01110111	115	1001101
10	00010000	12	1010	44	01000100	54	101100	78	01111000	116	1001110
11	00010001	13	1011	45	01000101	55	101101	79	01111001	117	1001111
12	00010010	14	1100	46	01000110	56	101110	80	10000000	120	1010000
13	00010011	15	1101	47	01000111	57	101111	81	10000001	121	1010001
14	00010100	16	1110	48	01001000	60	110000	82	10000010	122	1010010
15	00010101	17	1111	49	01001001	61	110001	83	10000011	123	1010011
16	00010110	20	10000	50	01010000	62	110010	84	10000100	124	1010100
17	00010111	21	10001	51	01010001	63	110011	85	10000101	125	1010101
18	00011000	22	10010	52	01010010	64	110100	86	10000110	126	1010110
19	00011001	23	10011	53	01010011	65	110101	87	10000111	127	1010111
20	00100000	24	10100	54	01010100	66	110110	88	10001000	130	1011000
21	00100001	25	10101	55	01010101	67	110111	89	10001001	131	1011001
22	00100010	26	10110	56	01010110	70	111000	90	10010000	132	1011010
23	00100011	27	10111	57	01010111	71	111001	91	10010001	133	1011011
24	00100100	30	11000	58	01011000	72	111010	92	10010010	134	1011100
25	00100101	31	11001	59	01011001	73	111011	93	10010011	135	1011101
26	00100110	32	11010	60	01100000	74	111100	94	10010100	136	1011110
27	00100111	33	11011	61	01100001	75	111101	95	10010101	137	1011111
28	00101000	34	11100	62	01100010	76	111110	96	10010110	140	1100000
29	00101001	35	11101	63	01100011	77	111111	97	10010111	141	1100001
30	00110000	36	11110	64	01100100	100	1000000	98	10011000	142	1100010
31	00110001	37	11111	65	01100101	101	1000001	99	10011001	143	1100011
32	00110010	40	100000	66	01100110	102	1000010				
33	00110011	41	100001	67	01100111	103	1000011				

CONVERSIONS

Powers of Two

2^n	n	2^{-n}
1	0	1.0
2	1	0.5
4	2	0.25
8	3	0.125
16	4	0.0625
32	5	0.03125
64	6	0.015625
128	7	0.0078125
256	8	0.00390625
512	9	0.001953125
1024	10	0.0009765625
2048	11	0.00048828125
4096	12	0.000244140625
8192	13	0.0001220703125
16384	14	0.00006103515625
32768	15	0.000030517578125
65536	16	0.0000152587890625
131072	17	0.00000762939453125
262144	18	0.000003814697265625
524288	19	0.0000019073486328125
1048576	20	0.00000095367431640625
2097152	21	0.000000476837158203125
4194304	22	0.0000002384185791015625
8388608	23	0.00000011920928955078125
16777216	24	0.000000059604644775390625
33554432	25	0.0000000298023223876953125
67108864	26	0.00000001490116119384765625
134217728	27	0.000000007450580596923828125
268435456	28	0.0000000037252902984619140625
536870912	29	0.00000000186264514923095703125
1073741824	30	0.000000000931322574615478515625
2147483648	31	0.0000000004656612873077392578125
4294967296	32	0.00000000023283064365386962890625
8589934592	33	0.00000000011641532182693481453125
17179869184	34	0.0000000000582076609134674072265625
34359738368	35	0.00000000002910383045673370361328125
68719476736	36	0.000000000014551915228366851806640625
137438953472	37	0.0000000000072759576141834259033203125
274877906944	38	0.00000000000363797880709171295166015625
549755813888	39	0.000000000001818989403545856475830078125
1099511627776	40	0.0000000000009094947017729282379150390625
2199023255552	41	0.00000000000045474735088646411895751953125
4398046511104	42	0.000000000000227373675443232059478759765625
8796093022208	43	0.0000000000001136868377216160297393798828125
17592186044416	44	0.00000000000005684341886080801486968994140625
35184372088832	45	0.0000000000000284217094304040074348449703125
70368744177664	46	0.0000000000000142108547152020037174224853515625
140737488355328	47	0.00000000000000710542735760100185871124267578125
281474976710656	48	0.000000000000003552713678800500929355621337890625
562949953421312	49	0.0000000000000017763568394002504646778106689453125
1125899906842624	50	0.00000000000000088817841970012523233890533447265625
2251799813685248	51	0.000000000000000444089209850062616169452667236328125
4503599627370496	52	0.0000000000000002220446049250313080847263336181640625
9007199254740992	53	0.00000000000000011102230246251565404236316680908203125
18014398509481984	54	0.000000000000000055511151231257827021181583404541015625
36028797018963968	55	0.0000000000000000277555756156289135105907917022705078125
72057594037927936	56	0.00000000000000001387778780781445675529539585113525390625
144115188075855872	57	0.000000000000000006938893903907228377647697925567626953125
288230376151711744	58	0.0000000000000000034694469519536141888238489627838134765625
576460752303423488	59	0.00000000000000000173472347597680709441192448139190673828125
1152921504606846976	60	0.000000000000000000867361737988403547205962240695953369140625
2305843009213693952	61	0.0000000000000000004336808689942017736029811203479766845703125
4611686018427387904	62	0.00000000000000000021684043449710088680149056017398834228515625
9223372036854775808	63	0.000000000000000000108420217248550443400745280086994171142578125
18446744073709551616	64	0.0000000000000000000542101086242752217003726400434970855712890625
36893488147419103232	65	0.00000000000000000002710505431213761085018632002174854278564453125
73786976294838206464	66	0.00000000000000000001355252715608880542509316001087427139282265625
147573952589676412928	67	0.0000000000000000000067762635780344027125465800054371356964111328125
295147905179352825856	68	0.0000000000000000000033881317890172013562732900027185678482056640625
590295810358705651712	69	0.000000000000000000001694065894508600678136645001359283924102783203125
1180591620717411303424	70	0.0000000000000000000008470329472543003390683225006796419620513916015625
2361183241434822606848	71	0.00000000000000000000042351647362715016953416125033982098102569580078125
4722366482869645213696	72	0.000000000000000000000211758236813575084767080625169910490512847900390625

Programs for Security System Components

BCDEncoder–VHDL

```
library ieee;
use ieee.std_logic_1164.all;

entity BCDEncoder is
port(D: in std_logic_vector(0 to 9);
     Q: out std_logic_vector(0 to 3));
end entity BCDEncoder;

architecture BCDBehavior of BCDEncoder is
begin
    Q(0) <= D(9) or D(7) or D(5) or D(3) or D(1);
    Q(1) <= D(7) or D(6) or D(3) or D(2);
    Q(2) <= D(7) or D(6) or D(5) or D(4);
    Q(3) <= D(9) or D(8);
end architecture BCDBehavior;
```

CodeSelection–VHDL

```
library ieee;
use ieee.std_logic_1164.all;

entity CodeSelection is
port(ShiftIn, Clk: in std_logic;
     Bout: out std_logic_vector(1 to 4));
end entity CodeSelection;

architecture CodeSelectionBehavior of CodeSelection is
component FourBitShiftReg is
port(R_L, Clk: in std_logic;
     D0, D1, D2, D3: in std_logic;
     Q0, Q1, Q2, Q3: buffer std_logic);
end component FourBitShiftReg;

signal A: std_logic_vector(0 to 3);
signal B: std_logic_vector(0 to 3);
signal C: std_logic_vector(0 to 3);
signal D: std_logic_vector(0 to 3);
signal Q: std_logic_vector(0 to 3);
signal Code1: std_logic_vector(0 to 3);
signal Code2: std_logic_vector(0 to 3);
signal Code3: std_logic_vector(0 to 3);
signal Code4: std_logic_vector(0 to 3);

begin
    Code1 <= "0001";
    Code2 <= "1001";
    Code3 <= "1001";
    Code4 <= "0001";
    A(0) <= Q(0) and Code1(0); B(0) <= Q(1) and Code2(0);
    C(0) <= Q(2) and Code3(0); D(0) <= Q(3) and Code4(0);
    A(1) <= Q(0) and Code1(1); B(1) <= Q(1) and Code2(1);
    C(1) <= Q(2) and Code3(1); D(1) <= Q(3) and Code4(1);
    A(2) <= Q(0) and Code1(2); B(2) <= Q(1) and Code2(2);
    C(2) <= Q(2) and Code3(2); D(2) <= Q(3) and Code4(2);
    A(3) <= Q(0) and Code1(3); B(3) <= Q(1) and Code2(3);
    C(3) <= Q(2) and Code3(3); D(3) <= Q(3) and Code4(3);
    Bout(1) <= D(0) or C(0) or B(0) or A(0);
    Bout(2) <= D(1) or C(1) or B(1) or A(1);
    Bout(3) <= D(2) or C(2) or B(2) or A(2);
    Bout(4) <= D(3) or C(3) or B(3) or A(3);

    ShiftReg: FourBitShiftReg
port map(R_L=>ShiftIn, Clk=>Clk, D0=>'1', D1=>'0', D2=>'0',
        D3=>'0', Q0=>Q(0), Q1=>Q(1), Q2=>Q(2),
        Q3=>Q(3));
end architecture CodeSelectionBehavior;
```

EightBitShiftReg–VHDL

```
library ieee;
use ieee.std_logic_1164.all;

entity EightBitShiftReg is
port(R_L, Clk: in std_logic;
     D: in std_logic_vector(0 to 7);
     Q: buffer std_logic);
end entity EightBitShiftReg;

architecture EightBitBehavior of EightBitShiftReg is
component dff is
port(D, Clk: in std_logic;
     Q: out std_logic);
end component dff;

signal D0, D1, D2, D3, D4, D5, D6, D7: std_logic;
signal Q0, Q1, Q2, Q3, Q4, Q5, Q6: std_logic;

begin
    D0 <= (not R_L and D(0));
    D1 <= (Q0 and R_L) or (not R_L and D(1));
    D2 <= (Q1 and R_L) or (not R_L and D(2));
    D3 <= (Q2 and R_L) or (not R_L and D(3));
    D4 <= (Q3 and R_L) or (not R_L and D(4));
    D5 <= (Q4 and R_L) or (not R_L and D(5));
    D6 <= (Q5 and R_L) or (not R_L and D(6));
    D7 <= (Q6 and R_L) or (not R_L and D(7));

    DFF0: dff port map(D => D0, Clk => Clk, Q => Q0);
    DFF1: dff port map(D => D1, Clk => Clk, Q => Q1);
    DFF2: dff port map(D => D2, Clk => Clk, Q => Q2);
    DFF3: dff port map(D => D3, Clk => Clk, Q => Q3);
    DFF4: dff port map(D => D4, Clk => Clk, Q => Q4);
    DFF5: dff port map(D => D5, Clk => Clk, Q => Q5);
    DFF6: dff port map(D => D6, Clk => Clk, Q => Q6);
    DFF7: dff port map(D => D7, Clk => Clk, Q => Q7);
end architecture EightBitBehavior;
```

FourBitParSftReg–VHDL

```
library ieee;
use ieee.std_logic_1164.all;

entity FourBitParSftReg is
port(D: in std_logic_vector(0 to 3);
     Clk: in std_logic;
     Q: out std_logic_vector(0 to 3));
end entity FourBitParSftReg;

architecture FourBitBehavior of FourBitParSftReg is
component dff is
port(D, Clk: in std_logic;
     Q: out std_logic);
end component dff;

begin
    DFF0: dff port map(D => D(0), Clk => Clk, Q => Q(0));
    DFF1: dff port map(D => D(1), Clk => Clk, Q => Q(1));
    DFF2: dff port map(D => D(2), Clk => Clk, Q => Q(2));
    DFF3: dff port map(D => D(3), Clk => Clk, Q => Q(3));
end architecture FourBitBehavior;
```

OneShot–VHDL

```

library ieee;
use ieee.std_logic_1164.all;

entity OneShot is
port(Enable, Clk: in std_logic;
      QOut: buffer std_logic);
end entity OneShot;

architecture OneShotBehavior of OneShot is
begin
process(Enable, Clk)
variable Flag : boolean := true;
variable Cnt : integer range 0 to 255;
variable SetCount : integer range 0 to 255;
begin
SetCount := 2;
if (Clk'EVENT and Clk = '1') then
if Enable = '0' then
Flag := true;
end if;

if Enable = '1' and Flag then
Cnt := 1;
Flag := False;
end if;

if cnt = SetCount then
Qout <= '0';
Cnt := 0;
Flag := false;
else
if Cnt > 0 then
Cnt := Cnt + 1;
if Cnt > 1 then
Qout <= '1';
end if;
end if;
end if;
end process;
end architecture OneShotBehavior;
    
```

ComparatorFourBit–VHDL

```

library ieee;
use ieee.std_logic_1164.all;

entity ComparatorFourBit is
port(A, B: in std_logic_vector(0 to 3);
      EQ: out std_logic);
end entity ComparatorFourBit;

architecture ComparatorBehavior of
ComparatorFourBit is
begin
process (A,B)
begin
if (A = B) and not (A = "0000") then
EQ <= '1';
else
EQ <= '0';
end if;
end process;
end architecture ComparatorBehavior;
    
```

BCDEncoder–Verilog

```

module BCDEncoder(D, Q);
input [9:0] D;
output [3:0] Q;

assign Q[0] = D[9] || D[7] || D[5] || D[3] || D[1];
assign Q[1] = D[7] || D[6] || D[3] || D[2];
assign Q[2] = D[7] || D[6] || D[5] || D[4];
assign Q[3] = D[9] || D[8];
endmodule
    
```

CodeSelection–Verilog

```

module CodeSelection(ShiftIn, Clk, Bout);
input ShiftIn;
input Clk;
output [4:1]Bout;

wire[3:0] A;
wire[3:0] B;
wire[3:0] C;
wire[3:0] D;
wire[3:0] Q;
wire[3:0] Code1;
wire[3:0] Code2;
wire[3:0] Code3;
wire[3:0] Code4;

assign Code1 = 4'b1001;
assign Code2 = 4'b1000;
assign Code3 = 4'b1000;
assign Code4 = 4'b1001;
assign A[0]=Q[0] && Code1[0];assign B[0]=Q[1] && Code2[0]
assign C[0]=Q[2] && Code3[0];assign D[0]=Q[3] && Code4[0];
assign A[1]=Q[0] && Code1[1];assign B[1]=Q[1] && Code2[1];
assign C[1]=Q[2] && Code3[1];assign D[1]=Q[3] && Code4[1];
assign A[2]=Q[0] && Code1[2];assign B[2]=Q[1] && Code2[2];
assign C[2]=Q[2] && Code3[2];assign D[2]=Q[3] && Code4[2];
assign A[3]=Q[0] && Code1[3];assign B[3]=Q[1] && Code2[3];
assign C[3]=Q[2] && Code3[3];assign D[3]=Q[3] && Code4[3];

assign Bout[1] = D[0] || C[0] || B[0] || A[0];
assign Bout[2] = D[1] || C[1] || B[1] || A[1];
assign Bout[3] = D[2] || C[2] || B[2] || A[2];
assign Bout[4] = D[3] || C[3] || B[3] || A[3];

FourBitShiftReg ShiftReg(.S_L(ShiftIn),
.Clk(Clk),.D0(1),.D1(0),.D2(0),.D3(0),
.Q0(Q[0]),.Q1(Q[1]),.Q2(Q[2]),.Q3(Q[3]));
endmodule;
    
```

EightBitShiftReg–Verilog

```

module EightBitShiftReg(S_L, Clk, D, Q);
input S_L;
input Clk;
input [7:0] D;
output Q;

wire D0, D1, D2, D3, D4, D5, D6, D7;
wire Q0, Q1, Q2, Q3, Q4, Q5, Q6;

assign D0 = (!S_L && D[0]);
assign D1 = (Q0 && S_L) || (!S_L && D[1]);
assign D2 = (Q1 && S_L) || (!S_L && D[2]);
assign D3 = (Q2 && S_L) || (!S_L && D[3]);
assign D4 = (Q3 && S_L) || (!S_L && D[4]);
assign D5 = (Q4 && S_L) || (!S_L && D[5]);
assign D6 = (Q5 && S_L) || (!S_L && D[6]);
assign D7 = (Q6 && S_L) || (!S_L && D[7]);

dff DFF0(.d(D0), .Clk(Clk), .q(Q0));
dff DFF1(.d(D1), .Clk(Clk), .q(Q1));
dff DFF2(.d(D2), .Clk(Clk), .q(Q2));
dff DFF3(.d(D3), .Clk(Clk), .q(Q3));
dff DFF4(.d(D4), .Clk(Clk), .q(Q4));
dff DFF5(.d(D5), .Clk(Clk), .q(Q5));
dff DFF6(.d(D6), .Clk(Clk), .q(Q6));
dff DFF7(.d(D7), .Clk(Clk), .q(Q));
endmodule
    
```

FourBitParSftReg–Verilog

```

module FourBitParSftReg(D, Clk, Q);
input [3:0] D;
input Clk;
output [3:0]Q;

dff DFF0(.d(D[0]), .Clk(Clk), .Q(Q[0]));
dff DFF1(.d(D[1]), .Clk(Clk), .Q(Q[1]));
dff DFF2(.d(D[2]), .Clk(Clk), .Q(Q[2]));
dff DFF3(.d(D[3]), .Clk(Clk), .Q(Q[3]));
endmodule
    
```

OneShot–Verilog

```

module OneShot(Enable, Clk, QOut);
input Enable;
input Clk;
output QOut;

integer SetCount = 2;
integer Cnt = 0 ;
reg[0:0] Flag;
reg QOut;

initial Flag = 1'b1;
always @(posedge Clk)
begin
  if (Enable == 0)
    begin
      Flag = 1;
    end
  else
    begin
      if ((Enable == 1) && (Flag == 1))
        begin
          Cnt = 1;
          Flag = 0;
        end end
      if (Cnt == SetCount)
        begin
          QOut = 0;
          Cnt = 0;
          Flag = 0;
        end
      else
        begin
          if (Cnt > 0)
            begin
              Cnt = Cnt + 1;
              if (Cnt > 1)
                begin
                  QOut = 1;
                end
            end
        end
      end
    end
end
endmodule

```

ComparatorFourBit–Verilog

```

module ComparatorFourBit(A, B, EQ);
input [3:0] A;
input [3:0] B;
output EQ;

reg Out;

always @(A, B)
  if ((A == B) && !(A == 0))
    begin
      Out = 1'b1;
    end
  else
    begin
      Out = 1'b0;
    end
  assign EQ = Out;
endmodule

```


GLOSSARY

acceptor A receiving device on a bus.

access time The time from the application of a valid memory address to the appearance of valid output data.

addend In addition, the number that is added to another number called the augend.

adder A logic circuit used to add two binary numbers.

address The location of a given storage cell or group of cells in a memory; a unique memory location containing one byte.

address bus A one-way group of conductors from the microprocessor to a memory, or other external device, on which the address code is sent.

adjacency Characteristic of cells in a Karnaugh map in which there is a single-variable change from one cell to another cell next to it on any of its four sides.

AGP Accelerated graphic port.

aliasing The effect created when a signal is sampled at less than twice the signal frequency. Aliasing creates unwanted frequencies that interfere with the signal frequency.

alphanumeric Consisting of numerals, letters, and other characters.

ALU Arithmetic logic unit; the key processing element of a microprocessor that performs arithmetic and logic operations.

amplitude In a pulse waveform, the height or maximum value of the pulse as measured from its low level.

analog Being continuous or having continuous values, as opposed to having a set of discrete values.

analog system A system that processes data in analog form only.

analog-to-digital (A/D) conversion The process of converting an analog signal to digital form.

analog-to-digital converter (ADC) A device used to convert an analog signal to a sequence of digital codes.

AND A basic logic operation in which a true (HIGH) output occurs only when all the input conditions are true (HIGH).

AND array An array of AND gates consisting of a matrix of programmable interconnections.

AND gate A logic gate that produces a HIGH output only when all of the inputs are HIGH.

ANSI American National Standards Institute.

antifuse A type of PLD nonvolatile programmable link that can be left open or can be shorted once as directed by the program.

architecture The VHDL unit that describes the internal operation of a logic function; the internal functional arrangement of the elements that give a device its particular operating characteristics.

array In a PLD, a matrix formed by rows of product-term lines and columns of input lines with a programmable cell at each junction. In VHDL, an array is an ordered set of individual items called elements with a single identifier name.

ASCII American Standard Code for Information Interchange; the most widely used alphanumeric code.

ASK Amplitude shift keying; a form of modulation in which a digital signal modulates the amplitude of a higher frequency sine wave.

assembler A program that converts English-like mnemonics into machine code.

assembly language A programming language that uses English-like words and has a one-to-one correspondence to machine language.

associative law In addition (ORing) and multiplication (ANDing) of three or more variables, the order in which the variables are grouped makes no difference.

astable Having no stable state. An astable multivibrator oscillates between two quasi-stable states.

asynchronous Having no fixed time relationship; a condition in which signals or systems are not aligned or synchronized in terms of timed events.

asynchronous counter A type of counter in which each stage is clocked from the output of the preceding stage.

attenuation The loss of energy as a signal propagates through a medium.

augend In addition, the number to which the addend is added.

backside bus A bus that connects the CPU to the cache to provide faster access to RAM.

bank A section of memory within a single memory array (chip).

base One of the three regions in a bipolar junction transistor.

base address The beginning address of a segment of memory.

baud The number of symbols per second in a data transmission.

BCD Binary coded decimal; a digital code in which each of the decimal digits, 0 through 9, is represented by a group of four bits.

BEDO DRAM Burst extended data output dynamic random-access memory.

bed-of-nails A method for the automated testing of printed circuit boards in which the board is mounted on a fixture that resembles a bed of nails that makes contact with test points.

BiCMOS A family of logic circuits that combines CMOS and bipolar logic.

bidirectional Having two directions. In a bidirectional shift register, the stored data can be shifted right or left.

binary Having two values or states; describes a number system that has a base of two and utilizes 1 and 0 as its digits.

BIOS Basic input/output system; a set of programs in ROM that interfaces the I/O devices in a computer system.

bipolar A class of integrated logic circuits implemented with bipolar transistors; also known as TTL.

bistable Having two stable states. Flip-flops and latches are bistable multivibrators.

bit A binary digit, which can be either a 1 or 0.

bit rate The number of bits per second in a data transmission.

bitstream A series of bits describing a final design that is sent to the target device during programming.

bit time The interval of time occupied by a single bit in a sequence of bits; the period of the clock.

BIU Bus interface unit; the portion of the CPU that interfaces with the system buses and fetches instructions, reads operands, and writes results.

BJT Bipolar junction transistor; a semiconductor device used for switching or amplification. A BJT has two junctions, the base-emitter junction and the base-collector junction.

Boolean addition In Boolean algebra, the OR operation.

Boolean algebra The mathematics of logic circuits.

Boolean expression An expression of variables and operators used to express the operation of a logic circuit.

Boolean multiplication In Boolean algebra, the AND operation.

boundary scan A method for internally testing a PLD based on the JTAG standard (IEEE Std. 1149.1).

break point A flag placed within a program source code to stop a program for investigation.

buffer A circuit that prevents loading of an input or output.

bus One or more interconnections that interface one or more devices based on a standardized specification.

bus arbitration The process that prevents two sources from using a bus at the same time.

bus bandwidth The number of bytes per clock cycle times the number of clock cycles per second.

bus bridge A device that interfaces two buses, usually a faster bus with a slower bus.

bus contention An adverse condition that could occur if two or more devices try to communicate at the same time on a bus.

bus frequency The clock frequency at which the bus can operate.

bus master Any device that can control and manage the system buses in a computer system.

bus network topology A type of physical network layout in which all devices are connected to a single common bus.

bus protocol A set of rules that allow two or more devices to communicate through a bus.

bus transfer speed The number of bytes per clock cycle.

bus width The number of bits that a bus can transmit at one time.

byte A group of eight bits.

cache memory A relatively small, high-speed memory that stores the most recently used instructions or data from the larger but slower main memory.

caching The process of copying frequently accessed program instructions from main memory into faster memory to increase processing speed.

CAN Controller area network; a bus standard used in automotive and other applications.

capacity The total number of data units (bits, nibbles, bytes, words) that a memory can store.

carry The digit generated when the sum of two binary digits exceeds 1.

carry generation The process of producing an output carry in a full-adder when both input bits are 1s.

carry propagation The process of rippling an input carry to become the output carry in a full-adder when either or both of the input bits are 1s and the input carry is a 1.

cascade To connect “end-to-end” as when several counters are connected from the terminal count output of one counter to the enable input of the next counter.

cascading Connecting two or more similar devices in a manner that expands the capability of one device.

CCD Charge-coupled device; a type of semiconductor memory that stores data in the form of charge packets and is serially accessed.

CD-R CD-Recordable; an optical disk storage device on which data can be stored once.

CD-ROM An optical disk storage device on which data are prestored and can only be read.

CD-RW CD-Rewritable; an optical disk storage on which data can be written and overwritten many times.

cell A single storage element in a memory; a fused cross point of a row and column in a PLD.

character A symbol, letter, or numeral.

circuit An arrangement of electrical and/or electronic components interconnected in such a way as to perform a specified function.

CLB Configurable logic block; a unit of logic in an FPGA that is made up of multiple smaller logic modules and a local programmable interconnect that is used to connect logic modules within the CLB.

clear An input used to reset a flip-flop (make the Q output 0); to place a register or counter in the state in which it contains all 0s.

client/server A networking application architecture that handles tasks between service providers called *servers* and service requesters called *clients*.

clock The basic timing signal in a digital system; a periodic waveform used to synchronize operation.

CMOS Complementary metal oxide semiconductor; a class of integrated logic circuits that is implemented with a type of field-effect transistor.

coaxial cable A type of data transmission media in which a shielded conductor is used to minimize EMI.

code A set of bits arranged in a unique pattern and used to represent such information as numbers, letters, and other symbols; in VHDL, program statements.

codec A combined coder and decoder.

collector One of the three regions in a bipolar transistor.

combinational logic A combination of logic gates interconnected to produce a specified Boolean function with no storage or memory capability; sometimes called *combinatorial logic*.

commutative law In addition (ORing) and multiplication (ANDing) of two variables, the order in which the variables are ORed or ANDed makes no difference.

comparator A digital circuit that compares the magnitudes of two quantities and produces an output indicating the relationship of the quantities.

compiler An application program in development software packages that controls the design flow process and translates

source code into object code in a format that can be logically tested or downloaded to a target device.

complement The inverse or opposite of a number; in Boolean algebra, the inverse function, expressed with a bar over the variable. The complement of a 1 is a 0, and vice versa.

component A VHDL feature that can be used to predefine the logic function for multiple use throughout a program or programs.

contiguous Joined together.

control bus A set of conductive paths that connects the CPU to other parts of the computer to coordinate its operations and to communicate with external devices.

controller An instrument that can specify each of the other instruments on the bus as either a talker or a listener for the purpose of data transfer.

control unit The portion within the microprocessor that provides the timing and control signals for getting data into and out of the microprocessor and for synchronizing the execution of instructions.

counter A digital circuit capable of counting electronic events, such as pulses, by progressing through a sequence of binary states.

CPLD A complex programmable logic device that consists basically of multiple SPLD arrays with programmable interconnections.

CPU Central processing unit; the main part of a computer responsible for control and processing of data; the core of a DSP that processes the program instructions.

cross-assembler A program that translates an assembly language program for one type of microprocessor to an assembly language for another type of microprocessor.

current sinking The action of a circuit in which it accepts current into its output from a load.

current sourcing The action of a circuit in which it sends current out of its output and into a load.

cyclic redundancy check (CRC) A type of error detection code.

DAT Digital audio tape; a type of magnetic tape format.

data Information in numeric, alphabetic, or other form.

data bus A bidirectional set of conductive paths on which data or instruction codes are transferred into a microprocessor or on which the result of an operation is sent out from the microprocessor.

data selector A circuit that selects data from several inputs one at a time in a sequence and places them on the output; also called a multiplexer.

data sheet A document that specifies parameter values and operating conditions for an integrated circuit or other device.

DCE Data communications equipment.

DDR Double data rate.

decade Characterized by ten states or values.

decade counter A digital counter having ten states.

decimal Describes a number system with a base of ten.

decode A stage of the DSP pipeline operation in which instructions are assigned to functional units and are decoded.

decoder A digital circuit (device) that converts coded information into another (familiar) or noncoded form.

decrement To decrease the binary state of a counter by one.

delta modulation A method of analog-to-digital conversion using a 1-bit quantization process.

design flow The process or sequence of operations carried out to program a target device.

D flip-flop A type of bistable multivibrator in which the output assumes the state of the *D* input on the triggering edge of a clock pulse.

demultiplexer (demux) A circuit (digital device) that switches digital data from one input line to several output lines in a specified time sequence.

dependency notation A notational system for logic symbols that specifies input and output relationships, thus fully defining a given function; an integral part of ANSI/IEEE Std. 91-1984.

difference The result of a subtraction.

differential operation A bus operation that uses two wires for data (one for data and one for the complement of the data) and one wire for ground.

digit A symbol used to express a quantity.

digital Related to digits or discrete quantities; having a set of discrete values as opposed to continuous values.

digital system An arrangement of the individual logic functions connected to perform a specified operation or produce a defined output.

digital-to-analog (D/A) conversion The process of converting a sequence of digital codes to an analog form.

digital-to-analog converter (DAC) A device in which information in digital form is converted to analog form.

DIMM Dual in-line memory module.

diode A semiconductor device that conducts current in only one direction.

DIP Dual in-line package; a type of IC package whose leads must pass through holes to the other side of a PC board.

distortion The change in shape or other parameters of a signal waveform due to characteristics and imperfections in the transmission media.

distributive law The law that states that ORing several variables and then ANDing the result with a single variable is equivalent to ANDing the single variable with each of the several variables and then ORing the product.

dividend In a division operation, the quantity that is being divided.

divisor In a division operation, the quantity that is divided into the dividend.

DLT Digital linear tape; a type of magnetic tape format.

DMA Direct memory access; a method to directly interface a peripheral device to memory without using the CPU for control.

domain All of the variables in a Boolean expression.

“Don’t care” A combination of input literals that cannot occur and can be used as a 1 or a 0 for simplification.

downloading A design flow process in which the logic design is transferred from software to hardware.

drain One of the terminals of a field-effect transistor.

DRAM Dynamic random-access memory; a type of semiconductor memory that uses capacitors as the storage elements and is a volatile, read/write memory.

DSP Digital signal processor; a special type of microprocessor that processes data in real time.

DSP core The central processing unit of a digital system processor.

DTE Data terminal equipment.

duty cycle The ratio of pulse width to period expressed as a percentage.

DVD-ROM Digital versatile disk-ROM; also known as digital video disk-ROM; a type of optical storage device on which data is prestored with a much higher capacity than a CD-ROM.

dynamic memory A type of semiconductor memory having capacitive storage cells that lose stored data over a period of time and, therefore, must be refreshed.

ECL Emitter-coupled logic; a class of integrated logic circuits that are implemented with nonsaturating bipolar junction transistors.

E²CMOS Electrically erasable CMOS (EECMOS); the circuit technology used for the reprogrammable cells in a PLD.

edge-triggered flip-flop A type of flip-flop in which the data are entered and appear on the output on the same clock edge.

EDIF Electronic design interchange format; a standard form of netlist.

EDO DRAM Extended data output dynamic random-access memory.

EEPROM Electrically erasable programmable read-only memory; a type of nonvolatile PLD reprogrammable link based on electrically-erasable programmable read-only memory cells and can be turned on or off repeatedly by programming.

EIA-232 Also known as RS-232.

8 mm A type of magnetic tape format.

electromagnetic waves Related to the electromagnetic spectrum, which includes radio waves, microwaves, infrared, visible, ultraviolet, X-rays, and gamma rays.

embedded system Generally, a single-purpose system, such as a processor, built into a larger system for the purpose of controlling the system.

EMI Electromagnetic interference.

emitter One of the three regions in a bipolar junction transistor.

encoder A digital circuit (device) that converts information to a coded form.

entity The VHDL unit that describes the inputs and outputs of a logic function.

EPROM Erasable programmable read-only memory; A type of PLD nonvolatile programmable link based on electrically programmable read-only memory cells and can be turned either on or off once with programming.

error detection The process of detecting bit errors in a digital code.

Ethernet A widely used standard local area network (LAN) technology or protocol; also known as IEEE-802.3.

EU Execution unit; the portion of a CPU that executes instructions; it contains the arithmetic logic unit (ALU), the general registers, and the flags.

even parity The condition of having an even number of 1s in every group of bits.

exception Any software event that requires special handling by the processor.

exclusive-NOR (XNOR)gate A logic gate that produces a LOW only when the two inputs are at opposite levels.

exclusive-OR (XOR) A basic logic operation in which a HIGH occurs when the two inputs are at opposite levels.

exclusive-OR (XOR) gate A logic gate that produces a HIGH only when the two inputs are at opposite levels.

execute A CPU process in which an instruction is carried out; a stage of the DSP pipeline operation in which the decoded instructions are carried out.

exponent The part of a floating-point number that represents the number of places that the decimal point (or binary point) is to be moved.

fall time The time interval between the 90% point and the 10% point on the negative-going edge of a pulse.

fan-out The number of equivalent gate inputs of the same family series that a logic gate can drive.

FDM Frequency division multiplexing; a broadband technique in which the total bandwidth available to a system is divided into frequency sub-bands and information is sent in analog form.

feedback The output voltage or a portion of it that is connected back to the input of a circuit.

FET Field-effect transistor.

fetch A CPU process in which an instruction is obtained from the memory; a stage of the DSP pipeline operation in which an instruction is obtained from the program memory.

FIFO First in–first out memory.

FireWire A high-speed external serial bus standard developed by Apple Inc. and used in high-speed communications and real-time data transfer, also known as IEEE-1394.

firmware Small fixed programs and/or data structures that internally control various electronic devices; usually stored in ROM.

fixed-function logic A category of digital integrated circuits having functions that cannot be altered.

flag A bit that indicates the result of an arithmetic or logic operation or is used to alter an operation.

flash A type of PLD nonvolatile reprogrammable link technology based on a single transistor cell.

flash ADC A simultaneous analog-to-digital converter.

flash memory A nonvolatile read/write random-access semiconductor memory in which data is stored as charge on the floating gate of a certain FET.

flip-flop A basic storage circuit that can store only one bit at a time; a synchronous bistable device.

floating-point number A number representation based on scientific notation in which the number consists of an exponent and a mantissa.

flying probe A method for the automated testing of printed circuit boards, in which a probe or probes move from place to place to contact test points.

forward bias A voltage polarity condition that allows a semiconductor *pn* junction in a transistor or diode to conduct current.

FPGA Field-programmable gate array; a programmable logic device that uses the LUT as the basic logic elements and generally employs either antifuse or SRAM-based process technology.

- FPM DRAM** Fast page mode dynamic random-access memory.
- frequency (*f*)** The number of pulses in one second for a periodic waveform. The unit of frequency is the hertz.
- frontside bus** A system bus that connects the major components of a computer system.
- FSK** Frequency shift keying; a form of modulation in which a digital signal modulates the frequency of a higher frequency sine wave.
- full-adder** A digital circuit that adds two bits and an input carry to produce a sum and an output carry.
- full-duplex** A connection in which the data flows both ways simultaneously in the same channel.
- functional simulation** A software process that tests the logical or functional operation of a design.
- fuse** A type of PLD nonvolatile programmable link that can be left shorted or can be opened once as directed by the program; also called a fusible link.
- GAL** Generic array logic; a reprogrammable type of SPLD that is similar to a PAL except that it uses a reprogrammable process technology, such as EEPROM (E² CMOS), instead of fuses.
- gate** A logic circuit that performs a basic logic operation, such as AND or OR; one of the three terminals of a field-effect transistor.
- gateway** A network point that provides access to another network.
- glitch** A voltage or current spike of short duration, usually unintentionally produced and unwanted.
- graphic (schematic) entry** A method of entering a logic design into software by graphically creating a logic diagram (schematic) on a design screen.
- GPIB** General-purpose interface bus based on the IEEE 488 standard.
- Gray code** An unweighted digital code characterized by a single bit change between adjacent code numbers in a sequence.
- half-adder** A digital circuit that adds two bits and produces a sum and an output carry. It cannot handle input carries.
- half-duplex** A connection in which the data flows both ways but not at the same time in the same channel.
- handshake** A routine by which two devices initiate and complete a bus transfer.
- handshaking** The process of signal interchange by which two digital devices or systems jointly establish communication.
- hard core** A fixed portion of logic in an FPGA that is put in by the manufacturer to provide a specific function.
- hard disk** A magnetic disk storage device; typically, a stack of two or more rigid disks enclosed in a sealed housing.
- hardware** The circuitry and physical components of a computer system (as opposed to the directions called software).
- HDL** Hardware description language; a language used for describing a logic design using software.
- hexadecimal** Describes a number system with a base of 16.
- high-level language** A type of computer language closest to human language that is a level above assembly language.
- high-Z** The high-impedance state of a tristate circuit in which the output is effectively disconnected from the rest of the circuit.
- hit** A successful attempt to read or write a block of data in a given level of memory.
- hit rate** The percentage of memory accesses that find the requested data in the given level of memory.
- hold time** The time interval required for the control levels to remain on the inputs to a flip-flop after the triggering edge of the clock in order to reliably activate the device.
- HPIB** Hewlett-Packard interface bus; same as GPIB (general-purpose interface bus).
- hub** A common connection point containing multiple ports for devices in a computer or network.
- hysteresis** A characteristic of a threshold-triggered circuit, such as the Schmitt trigger, where the device turns on and off at different input levels.
- IEEE** Institute of Electrical and Electronics Engineers.
- IEEE 488 bus** Same as GPIB (general-purpose interface bus); a standard parallel bus used widely for test and measurement interfacing.
- IEEE 1394** A serial bus for high-speed data transfer; also known as FireWire.
- I²L** Integrated injection logic; an IC technology.
- implementation** The software process where the logic structures described by the netlist are mapped into the structure of the target device.
- increment** To increase the binary state of a counter by one.
- input** The signal or line going into a circuit; a signal that controls the operation of a circuit.
- input/output (I/O)** A terminal of a device that can be used as either an input or as an output.
- instruction** One step in a computer program; a unit of information that tells the CPU what to do.
- instruction pairing** The process of combining certain independent instructions so that they can be executed simultaneously by two separate execution units.
- In-system programming (ISP)** A method for programming SPLDs after they are installed on a printed circuit board and operating in a system.
- integer** A whole number.
- integrated circuit (IC)** A type of circuit in which all of the components are integrated on a single chip of semiconductive material of very small size.
- intellectual property (IP)** Designs owned by the manufacturer of programmable logic devices.
- interfacing** The process of making two or more electronic devices or systems operationally compatible with each other so that they function properly together.
- interrupt** Any hardware event that requires special handling by the processor; an event that causes the current process to be temporarily stopped while a service routine is run.
- inversion** The conversion of a HIGH level to a LOW level or vice versa; also called complementation.
- inverter** A NOT circuit; a circuit that changes a HIGH to a LOW or vice versa.
- I/O port** Input/output port; the interface between an internal bus and a peripheral.

IP Instruction pointer; a special register within the CPU that holds the offset address of the next instruction to be executed.

IP address Internet protocol address; an address assigned to each device in a network that uses the Internet protocol and serves to identify the network and the location of the device within the network.

I²C Inter-integrated circuit bus; an internal serial bus primarily for connecting ICs on a PC board.

ISA bus Industry standard architecture bus; an internal parallel bus standard.

J-K flip-flop A type of flip-flop that can operate in the SET, RESET, no-change, and toggle modes.

Johnson counter A type of register in which a specific prestored pattern of 1s and 0s is shifted through the stages, creating a unique sequence of bit patterns.

JTAG Joint test action group; the IEEE Std. 1149.1 standard interface for in-system programming.

junction The boundary between an *n* region and a *p* region in a BJT.

Karnaugh map An arrangement of cells representing the combinations of literals in a Boolean expression and used for a systematic simplification of the expression.

LAB Logic array block; an SPLD array in a CPLD.

LAN Local area network.

latch A bistable digital circuit used for storing a bit.

latency period The time it takes for the desired sector to spin under the head once the head is positioned over the desired track of a magnetic hard disk.

LCC Leadless ceramic chip; an SMT package that has metallic contacts molded into its body.

LCD Liquid crystal display.

leading edge The first transition of a pulse.

least significant bit (LSB) Generally, the right-most bit in a binary whole number or code.

LED Light-emitting diode.

LIFO Last in–first out memory, memory stack.

listener An instrument capable of receiving data on a GPIB (general-purpose interface bus) when it is addressed by the computer.

literal A constant value assigned to a variable or the complement of a variable.

load To enter data into a shift register.

loading The effect of the multiple inputs degrading the voltage or timing specifications of an output.

local bus The internal bus of a computer system which includes the system bus, the PCI bus, and the ISA bus, among others.

local interconnect A set of lines that allows interconnections among the eight logic elements in a logic array block without using the row and column interconnects.

logic In digital electronics, the decision-making capability of gate circuits, in which a HIGH represents a true statement and a LOW represents a false one.

logical network topology The description of how devices in a network interact in order to send and receive data based on protocols.

logic array block (LAB) A group of macrocells that can be interconnected with other LABs or to other I/Os using a programmable interconnect array; also called a function block.

logic element The smallest section of logic in an FPGA that typically contains an LUT, associated logic, and a flip-flop.

look-ahead carry A method of binary addition whereby carries from preceding adder stages are anticipated, thus eliminating carry propagation delays.

LSI Large-scale integration; a level of fixed-function IC complexity in which there are from more than 100 to 10,000 equivalent gates per chip.

LUT Look-up table; a type of memory that can be programmed to produce SOP functions.

machine code The basic binary instructions understood by the processor.

machine language Computer instructions written in binary code that are understood by a computer; the lowest level of programming language.

macrocell An SOP logic array with combinational and registered outputs; part of a PAL or GAL that generally consists of one OR gate and some associated output logic. Multiple interconnected macrocells form a CPLD.

magneto-optical disk A storage device that uses electro-magnetism and a laser beam to read and write data.

magnitude The size or value of a quantity.

main memory Memory used by computer systems to store the bulk of programs and associated data.

MAN Metropolitan area network.

Manchester encoding A method of encoding called biphasic in which a 1 is represented by a positive-going transition and a 0 is represented by a negative-going transition.

mantissa The magnitude of a floating-point number.

Mealy state machine A state machine in which the outputs depend on both the internal present state and on the inputs.

memory The portion of a computer or other system that stores binary data.

memory array An array of memory cells arranged in rows and columns.

memory hierarchy The arrangement of various memory elements to maximize speed and minimize cost.

memory latency The time required to access a memory.

mesh network topology A type of physical network layout in which each device connects to all other devices providing multiple routes for data.

MFLOPS Million floating-point operations per second.

microcontroller A semiconductor device that combines a microprocessor, memory, and various hardware peripherals on a single IC.

microprocessor A large-scale digital integrated circuit that can be programmed to perform arithmetic, logic, or other operations; the CPU of a computer.

minuend The number from which another number is subtracted.

MIPS Million instructions per second.

miss A failed attempt by the processor to read or write a block or data in a given level of memory.

- MMACS** Million multiply/accumulates per second.
- MMU** Memory management unit; a device responsible for handling accesses to memory requested by the CPU.
- mnemonic** An English-like instruction that is converted by an assembler into a machine code for use by a processor.
- modem** A modulator/demodulator for interfacing digital devices to analog transmission systems such as telephone lines.
- module** A Verilog code block that defines inputs, outputs, and logic structure or function.
- modulus** The number of unique states through which a counter will sequence.
- monostable** Having only one stable state. A monostable multivibrator, commonly called a one-shot, produces a single pulse in response to a triggering input.
- monotonic** The characteristic of a DAC defined by the absence of any incorrect step reversals; one type of digital-to-analog linearity.
- Moore state machine** A state machine in which the outputs depend only on the internal present state.
- MOS** Metal-oxide semiconductor; a type of transistor technology.
- MOSFET** Metal-oxide semiconductor field-effect transistor.
- most significant bit (MSB)** The left-most bit in a binary whole number or code.
- MSI** Medium-scale integration; a level of fixed-function IC complexity in which there are from 10 to 100 equivalent gates per chip.
- multicore processor** A microprocessor chip with more than one processor.
- multimode** The characteristic of an optical fiber in which the light is propagated in multiple rays.
- multiplexer (mux)** A circuit (digital device) that switches digital data from several input lines onto a single output line in a specified time sequence.
- multiplicand** The number that is being multiplied by another number.
- multiplier** The number that multiplies the multiplicand.
- multiprocessing** A data-processing technique that uses more than one processor.
- multitasking** A technique by which a processor runs multiple programs concurrently.
- multithreading** The process of executing different parts of a program, called threads, simultaneously.
- multivibrator** A class of digital circuits in which the output is connected back to the input (an arrangement called feedback) to produce either two stable states, one stable state, or no stable states, depending on the configuration.
- NAND gate** A logic circuit in which a LOW output occurs only if all the inputs are HIGH.
- negative-AND** An equivalent NOR gate operation in which the HIGH is the active input when all inputs are LOW.
- negative-OR** An equivalent NAND gate operation in which the HIGH is the active input when one or more of the inputs are LOW.
- netlist** A detailed listing of information necessary to describe a circuit, such as types of elements, inputs, and outputs, and all interconnections.
- network** A set of computers and associated devices that are interconnected in a specified way in order to communicate to share information and resources.
- network topology** The physical and logical arrangement of devices in a network.
- nibble** A group of four bits.
- NMOS** An *n*-channel metal-oxide semiconductor.
- node** A common connection point in a circuit in which a gate output is connected to one or more gate inputs.
- noise** The unwanted electrical disturbance caused by both natural and man-made sources.
- noise immunity** The ability of a circuit to reject unwanted signals.
- noise margin** The amount by which the actual signal level exceeds the minimum acceptable level for an error-free transmission.
- nonvolatile** A term that describes a memory that can retain stored data when the power is removed.
- NOR gate** A logic gate in which the output is LOW when any or all of the inputs are HIGH.
- Northbridge** A bridge that serves as an interface generally to the AGP and RAM.
- NOT** A basic logic operation that performs inversions.
- NRZ** Nonreturn to zero; a type of data format in which the signal level does not return to zero during a bit time after a high-level (1) data bit occurs.
- numeric** Related to numbers.
- Nyquist frequency** The highest signal frequency that can be sampled at a specified sampling frequency; a frequency equal to or less than half the sampling frequency.
- object program** A machine language translation of a high-level source program.
- octal** Describes a number system with a base of eight.
- odd parity** The condition of having an odd number of 1s in every group of bits.
- offset address** The distance in number of bytes of a physical address from the base address.
- OLMC** Output logic macrocell; the part of a GAL that can be programmed for either combinational or registered outputs; a block of logic in a GAL that contains a fixed OR gate and other logic for handling inputs and/or outputs.
- one-shot** A monostable multivibrator.
- op code** Operation code; the code representing a particular microprocessor instruction; a mnemonic.
- open-collector** A type of output in a logic circuit in which the collector of the output transistor is left disconnected from any internal circuitry and is available for external connection; normally used for driving higher-current or higher-voltage loads.
- operand** The object to be manipulated by the instruction.
- operating system** The software that controls the computer system and oversees the execution of application software.
- operational amplifier (op-amp)** A device with two differential inputs that has very high gain, very high input impedance, and very low output impedance.
- optical fiber** A type of data transmission media used for transmitting light signals.

optical jukebox A type of auxiliary storage for very large amounts of data.

OR A basic logic operation in which a true (HIGH) output occurs when one or more of the input conditions are true (HIGH).

OR gate A logic gate that produces a HIGH output when one or more inputs are HIGH.

oscillator An electronic circuit that is based on the principle of regenerative feedback and produces a repetitive output waveform; a signal source.

OSI Open systems interconnection; a model in which all protocol operations and specifications for communicating on a network are broken down into seven parts called layers.

OTP One-time programmable.

output The signal or line coming out of a circuit.

overflow The condition that occurs when the number of bits in a sum exceeds the number of bits in each of the numbers added.

packet A formatted block of digital data.

PAL Programmable array logic; a type of one-programmable SPLD that consists of a programmable array of AND gates that connects to a fixed array of OR gates.

PAM Pulse amplitude modulation; a method of modulation in which the height or amplitude of the pulses are varied according to the modulating analog signal, and each pulse represents a value of amplitude of the analog signal.

parallel In digital systems, data occurring simultaneously on several lines; the transfer or processing of several bits simultaneously.

parallel bus A bus that consists of multiple conductors and carries several data bits simultaneously, one on each conductor.

parallel data Data that is represented by pulses sent simultaneously over multiple channels.

parity In relation to binary codes, the condition of evenness or oddness of the number of 1s in a code group.

parity bit A bit attached to each group of information bits to make the total number of 1s odd or even for every group of bits.

PCI Peripheral component interconnect.

PCI bus An internal synchronous bus for interconnecting chips, expansion boards, and processor/memory subsystems.

PCI-Express Also designated as PCIe or PCI-E. This bus differs from the PCI and PCI-X buses in that it does not use a shared bus.

PCI-X A high-performance enhancement of the PCI bus that is backward compatible with PCI.

PCM Pulse code modulation; A method of modulation that involves sampling of an analog signal amplitude at regular intervals and converting the sampled values to a digital code.

period (T) The time required for a periodic waveform to repeat itself.

periodic Describes a waveform that repeats itself at a fixed interval.

peripheral A device or instrument that provides communication with a computer or provides auxiliary services or functions for the computer.

physical address The actual location of a data unit in memory.

PIC Programmable interrupt controller; handles the interrupts on a priority basis.

pipeline As applied to memories, an implementation that allows a read or write operation to be initiated before the previous operation is completed; part of the DSP architecture that allows multiple instructions to be processed simultaneously.

pipelining A technique where the processor begins executing the next instruction before the previous instruction has been completed.

PLA Programmable logic array; an SPLD with programmable AND and OR arrays.

platform FPGA An FPGA that contains either or both hard core and soft core embedded processors and other functions.

PLCC Plastic leaded chip carrier; an SMT package whose leads are turned up under its body in a J-type shape.

PLD Programmable logic device; an integrated circuit that can be programmed with any specified logic function.

PMOS A *p*-channel metal-oxide semiconductor.

pointer The contents of a register (or registers) that contain an address.

polling The process of checking a series of peripheral devices to determine if any require service from the CPU.

port A physical interface on a computer through which data are passed to or from peripherals.

POS Product-of-sums; a form of Boolean expression that is basically the ANDing of ORed terms.

positive logic The system of representing a binary 1 with a HIGH and a binary 0 with a LOW.

power dissipation The product of the dc supply voltage and the dc supply current in an electronic circuit; the amount of power required by a circuit.

PPM Pulse position modulation; a method of modulation in which the position of each pulse relative to a reference or timing signal is varied proportional to the amplitude of the modulating signal waveform.

prefetching The process of executing instructions at the same time as other instructions are "fetched," eliminating idle time; also called pipelining.

preset An asynchronous input used to set a flip-flop (make the *Q* output 1).

priority encoder An encoder in which only the highest value input digit is encoded and any other active input is ignored.

probe An accessory used to connect a voltage to the input of an oscilloscope or other instrument.

processes Instances of a computer program that are being executed.

product The result of a multiplication.

product term The Boolean product of two or more literals equivalent to an AND operation.

program A sequential set of computer instructions designed to accomplish a given task(s).

programmable interconnect array (PIA) An array consisting of conductors that run throughout the CPLD chip and to which connections from the macrocells in each LAB can be made.

programmable logic A category of digital integrated circuits capable of being programmed to perform specified functions.

programmable logic device (PLD) A type of integrated circuit (IC) that starts as a "blank slate" and into which a logic design is programmed.

- PROM** Programmable read-only semiconductor memory; an SPLD with a fixed AND array and programmable OR array; used as a memory device and normally not as a logic circuit device.
- propagation delay time** The time interval between the occurrence of an input transition and the occurrence of the corresponding output transition in a logic circuit.
- pseudo-operation** An instruction to the assembler (as opposed to a processor).
- PSK** Phase shift keying; a form of modulation in which a digital signal modulates the phase of a higher frequency sine wave.
- pull-up resistor** A resistor with one end connected to the dc supply voltage used to keep a given point in a circuit HIGH when in the inactive state.
- pulse** A sudden change from one level to another, followed after a time, called the pulse width, by a sudden change back to the original level.
- pulse width (t_{PW})** The time interval between the 50% points of the leading and trailing edges of the pulse; the duration of the pulse.
- PWM** Pulse width modulation; a method of modulation in which the width or duration of the pulses and duty cycle are varied according to the modulating analog signal, and each pulse width represents an amplitude value of the analog signal.
- QAM** Quadrature amplitude modulation; a form of modulation that uses a combination of PSK and amplitude modulation to send information.
- QIC** Quarter-inch cassette; a type of magnetic tape.
- quantization** The process whereby a binary code is assigned to each sampled value during analog-to-digital conversion.
- queue** A high-speed memory that stores instructions or data.
- quotient** The result of a division.
- race** A condition in a logic network in which the difference in propagation times through two or more signal paths in the network can produce an erroneous output.
- RAM** Random-access memory; a volatile read/write semiconductor memory.
- rank** A group of chips that make up a memory module that stores data in units such as words or bytes.
- read** The process of retrieving data from a memory.
- real mode** Operation of an Intel processor in a manner to emulate the 8086's 1 MB of memory.
- recycle** To undergo transition (as in a counter) from the final or terminal state back to the initial state.
- refresh** To renew the contents of a dynamic memory by recharging the capacitor storage cells.
- register** A digital circuit capable of storing and shifting binary information; typically used as a temporary storage device.
- register array** A set of temporary storage locations within the microprocessor for keeping data and addresses that need to be accessed quickly by the program.
- registered** A CPLD macrocell output configuration where the output comes from a flip-flop.
- relocatable code** A program that can be moved anywhere within the memory space without changing the basic code.
- remainder** The amount left over after a division.
- RESET** The state of a flip-flop or latch when the output is 0; the action of producing a RESET state.
- resolution** The number of bits used in an ADC.
- reverse bias** A voltage polarity condition that prevents a *pn* junction of a transistor or diode from conducting current.
- ring counter** A register in which a certain pattern of 1s and 0s is continuously recirculated.
- ring network topology** A type of physical network layout in which the devices are daisy-chained and each device communicates only with its two neighboring devices.
- ripple carry** A method of binary addition in which the output carry from each adder becomes the input carry of the next higher-order adder.
- ripple counter** An asynchronous counter.
- rise time** The time required for the positive-going edge of a pulse to go from 10% of its full value to 90% of its full value.
- ROM** Read-only semiconductor memory, accessed randomly; also referred to as mask-ROM.
- router** A device that routes a data packet to the correct destination based on the IP address.
- RS-232** A bus standard, also known as EIA-232, used in industrial and telecommunication applications as well as scientific instrumentation, but largely replaced by USB in computer applications.
- RS-422** A bus standard for differential data transmission.
- RS-423** A bus standard for single-ended data transmission.
- RS-485** A bus standard for differential data transmission.
- RZ** Return to zero; a type of data format in which the signal level goes to or remains at zero after each data bit.
- sampling** The process of taking a sufficient number of discrete values at points on a waveform that will define the shape of the waveform.
- schematic (graphic) entry** A method of placing a logic design into software using schematic symbols.
- Schottky** A specific type of transistor-transistor logic circuit technology.
- SCSI** Small computer system interface; an external parallel bus standard.
- SDRAM** Synchronous dynamic random-access memory.
- seek time** The time for the read/write head in a hard drive to position itself over the desired track for a read operation.
- segment** A 64k block of memory.
- serial** Having one element following another, as in a serial transfer of bits; occurring, as pulses, in sequence rather than simultaneously.
- serial bus** A bus that carries data bits sequentially one at a time on a single conductor.
- serial data** Data that is represented by pulses sent one at a time over a single channel.
- SET** The state of a flip-flop or latch when the output is 1; the action of producing a SET state.
- set-up time** The time interval required for the control levels to be on the inputs to a digital circuit, such as a flip-flop, prior to the triggering edge of clock pulse.

shared bus A bus, such as PCI, that is shared by multiple devices.

shared media topology A type of logical network topology where all devices can access the physical network at any time as long as no other devices are attempting access.

signal A type of VHDL object that holds data.

signal-to-noise ratio (SNR) A measure of the signal strength relative to background noise, usually expressed in decibels (dB).

signal tracing A troubleshooting technique in which waveforms are observed in a step-by-step manner beginning at the input and working toward the output or vice versa. At each point the observed waveform is compared with the correct signal for that point.

sign bit The left-most bit of a binary number that designates whether the number is positive (0) or negative (1).

simplex A connection in which data flows in only one direction from the sender (transmitter) to the receiver.

single-ended operation A bus operation that uses one wire for data and one wire for ground.

single mode The characteristic of an optical fiber in which the light tends to propagate in a single beam or ray.

SMT Surface-mount technology; an IC package technique in which the packages are smaller than DIPs and are mounted on the printed surface of the PC board.

soft core A portion of logic in an FPGA; similar to hard core except it has some programmable features.

software Computer programs; programs that instruct a computer what to do in order to carry out a given set of tasks.

software interrupt An instruction that invokes an interrupt service routine.

SOIC Small-outline integrated circuit; an SMT package that resembles a small DIP but has its leads bent out in a “gull-wing” shape.

SOP Sum-of-products; a form of Boolean expression that is basically the ORing of ANDed terms.

source A sending device.

source program A program written in either assembly or high-level language.

Southbridge A bridge that handles all I/O functions.

speed-power product A performance parameter that is the product of the propagation delay time and the power dissipation in a digital circuit.

SPI Serial-to-peripheral interface bus; a synchronous serial communications bus that uses four wires for communication between a “master” device and a “slave” device.

SPLD Simple programmable logic device; an array of AND gates and OR gates that can be programmed to achieve specified logic functions. Four types are PROM, PLA, PAL, and GAL.

SRAM Static random-access memory; a type of PLD volatile reprogrammable link based on static random-access memory cells and can be turned on or off repeatedly with programming.

SSI Small-scale integration; a level of fixed-function IC complexity in which there are up to 10 equivalent gates per chip.

SSOP Shrink small-outline package.

stage One storage element (flip-flop) in a register.

star network topology A type of physical network layout containing a central connection point or hub, and all devices are connected through the hub with individual cables.

state diagram A graphic depiction of a sequence of states or values.

state machine A logic system exhibiting a sequence of states conditioned by internal logic and external inputs; any sequential circuit exhibiting a specified sequence of states.

static memory A volatile semiconductor memory that uses flip-flops as the storage cells and is capable of retaining data without refreshing.

storage The capability of a digital device to retain bits; the process of retaining digital data for later use.

STP Shielded twisted pair; a type of transmission media.

string A contiguous sequence of bytes or words.

strobing A process of using a pulse to sample the occurrence of an event at a specified time in relation to the event.

subroutine A series of instructions that can be assembled together and used repeatedly by a program but programmed only once.

subtractor A logic circuit used to subtract two binary numbers.

subtrahend The number that is being subtracted from the minuend.

sum The result when two or more numbers are added together.

sum term The Boolean sum of two or more literals equivalent to an OR operation.

synchronous A condition that describes signals or systems that are aligned or synchronized with each other in terms of timed events, two or more systems that have the same timing signal.

synchronous counter A type of counter in which each stage is clocked by the same pulse.

synthesis The software process where the design is translated into a netlist.

system bus The interconnecting paths in a computer system including the address bus, data bus and control bus.

talker A device capable of sending data over the GPIB.

tape library A type of auxiliary storage for very large amounts of data.

target device A PLD mounted on a programming fixture or development board into which a software logic design is to be downloaded; the programmable logic device that is being programmed.

TCP/IP Transmission Control Protocol/Internet Protocol; the communication protocol for the Internet.

TDM Time division multiplexing; a technique in which data from several sources are interleaved on a time basis and sent on a single communication channel or data link.

terminal count The final state in a counter’s sequence.

terminated The condition of a bus connection in which the signal is prevented from reflecting back when it reaches the end of the bus or transmission line. The condition when a resistor is connected from the bus to ground.

text entry A method of entering a logic design into software using a hardware description language (HDL).

throughput The average speed with which a program is executed.

timer A circuit that can be used as a one-shot or as an oscillator; a circuit that produces a fixed time interval output.

timing diagram A graph of digital waveforms showing the proper time relationship of two or more waveforms and how each waveform changes in relation to the others.

GLOSSARY

- timing simulation** A software process that uses information on propagation delays and netlist data to test both the logical operation and the worst-case timing of a design.
- toggle** The action of a flip-flop when it changes state on each clock pulse.
- token-based topology** A type of logical network topology where a code, called a token, travels around the network allowing a device to send data only if it attached the data packet to a token.
- totem-pole** A type of output in TTL circuits.
- trailing edge** The second transition of a pulse.
- transistor** A semiconductor device exhibiting current and/or voltage gain. When used as a switching device, it approximates an open or closed switch.
- tree topology** A type of physical network layout which is a hybrid combining bus topology and star topology.
- trigger** A pulse used to initiate a change in the state of a logic circuit.
- tristate** A type of output in logic circuits that exhibits three states: HIGH, LOW, and high-Z; also known as 3-state.
- tristate buffer** A circuit used to interface one device to another to prevent loading.
- troubleshooting** The technique of systematically identifying, isolating, and correcting a fault in a circuit or system.
- truth table** A table showing the inputs and corresponding output level of a logic circuit.
- TTL** Transistor-transistor logic; a class of integrated logic circuit that uses bipolar junction transistors. Also called *bipolar*.
- ULSI** Ultra large-scale integration; a level of IC complexity in which there are more than 100,000 equivalent gates per chip.
- unit load** A measure of fan-out. One gate input represents a unit load to the output of a gate within the same IC family.
- universal gate** Either a NAND gate or a NOR gate. The term *universal* refers to the property of a gate that permits any logic function to be implemented by that gate or by a combination of gates of that kind.
- up/down counter** A counter that can progress in either direction through a certain sequence.
- USB** Universal serial bus; a widely used standard serial bus for connecting peripherals to a computer.
- UTP** Unshielded twisted pair; a type of transmission media.
- UV EPROM** Ultraviolet erasable programmable ROM.
- variable** symbol used to represent an action, a condition, or data that can have a value of 1 or 0, usually designated by an italic letter or word.
- Verilog** A standard hardware description language that uses a module structure to describe a function.
- VHDL** A standard hardware description language that describes a function with an entity/architecture structure; IEEE Std. 1076–1993.
- VLSI** Very large-scale integration; a level of IC complexity in which there are from more than 10,000 to 100,000 equivalent gates per chip.
- volatile** The characteristic of a programmable logic device that loses programmed data when power is turned off.
- wait state** A system bus delay equal to one processor clock cycle. Wait states are used to ensure that the system bus timing satisfies the address, data, and control timing specifications of a system.
- WAN** Wide area network.
- weight** The value of a digit in a number based on its position in the number.
- word** A group of bits or bytes that acts as a single entity that can be stored in one memory location; two bytes.
- word capacity** The number of words that a memory can store.
- word length** The number of bits in a word.
- WORM** Write once-read many; a type of optical storage device.
- write** The process of storing data in a memory.
- zero suppression** The process of blanking out leading or trailing zeros in a digital display.

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